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Given a 2D design space of 150cm long and 50cm tall, a rigid bar of a fixed length (your choice), 3 pin supports of which two need to be mounted on the ground and a linear actuator (pick from this [online catalog](#), use max force values only), design a frame/mechanism to lift the maximum possible weight to the highest possible height. Assume all the supports and bar/actuator are rigid.

Using Actuator: Mode IMASS-RNOS

Max Load: 35.8 kN

Min stroke: 76.2 mm

max stroke: 457.4 mm

base length: 403.8 mm

Plan:

Design space 2-D  $\rightarrow$  150 cm (length)  $\times$  50 cm (height)

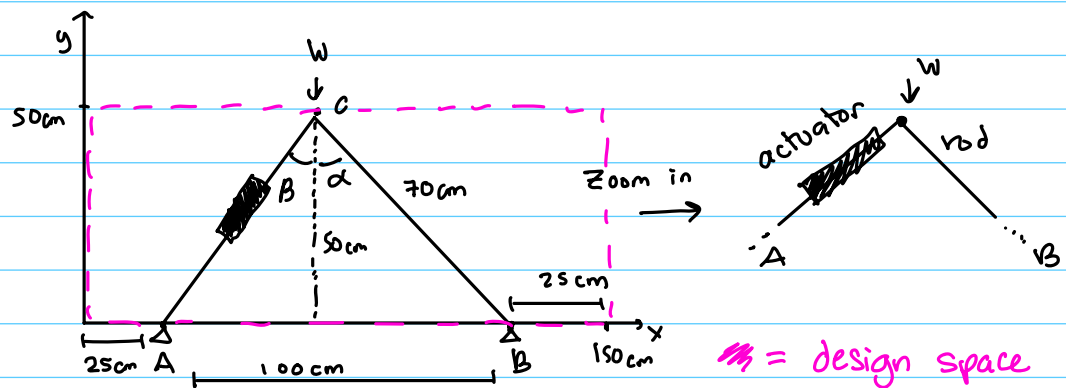
Choose points for pins to be connected to ground

i) Place A (25,0) and B (125,0) for pins connected to ground

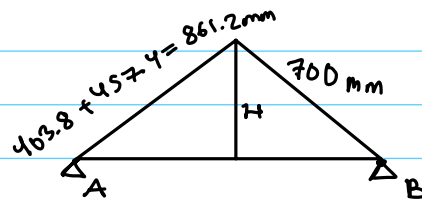
ii) select a 70 cm rod

iii) design a toggle type mechanism

Sketch:



Note: since max height = 50 cm, the actuator cannot use max stroke.  
Sketch if it opens to max stroke:



Here,  $H = 591.6 \text{ mm} > 500 \text{ mm}$  which doesn't match given boundary.  
Therefore, H is limited to 50 cm

$$DB = \sqrt{700^2 - 500^2} = 489.9 \text{ mm}$$

$$AD = \underbrace{(1250 - 250)}_{AB} - 489.9 = 510.1 \text{ mm}$$

$$\text{Actuator Length (AC)}: \sqrt{(500)^2 + (510.1)^2} = 714.3 \text{ mm}$$

$$\alpha = \tan^{-1}(DB/CD) = \tan^{-1}\left(\frac{489.9}{500}\right) = 44.42^\circ$$

$$\beta = \tan^{-1}(AD/CD) = \tan^{-1}\left(\frac{510.1}{500}\right) = 45.57^\circ$$

Calculating  $W$  (pick up load):

$$\sum F_x = 0$$

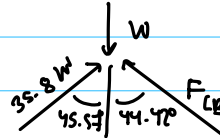
$$35.8 (\sin 45.57) = F_{CB} \sin 44.42$$

$$F_{CB} = 36.53 \text{ kN}$$

$$\sum F_y = 0$$

$$W = 35.8 (\cos 45.57) + 36.53 (\cos 44.42)$$

$$W = 25.06 + 26.09 = \boxed{51.15 \text{ kN}}$$



Find max pick-up height:

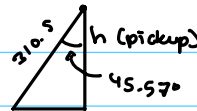
$$\text{open actuator length (AC)} = 714.3 \text{ mm}$$

$$\text{base length} = 403.8 \text{ mm}$$

$$\text{stroke length: } 714.3 - 403.8 = 310.5 \text{ mm}$$

$$h(\text{pickup}) = 310.5 \text{ at } 45.57^\circ$$

$$h(\text{pickup}) = \boxed{217.4 \text{ mm}}$$



Overall results: Any other smaller stroke less than 310.5 mm results in smaller pickup load and smaller pick-up height

Follow the following two steps, and questions to update your portfolio page:

**Step 1:** Consider the bar in your design to be rigid. Follow these steps to update your portfolio page from HW5:

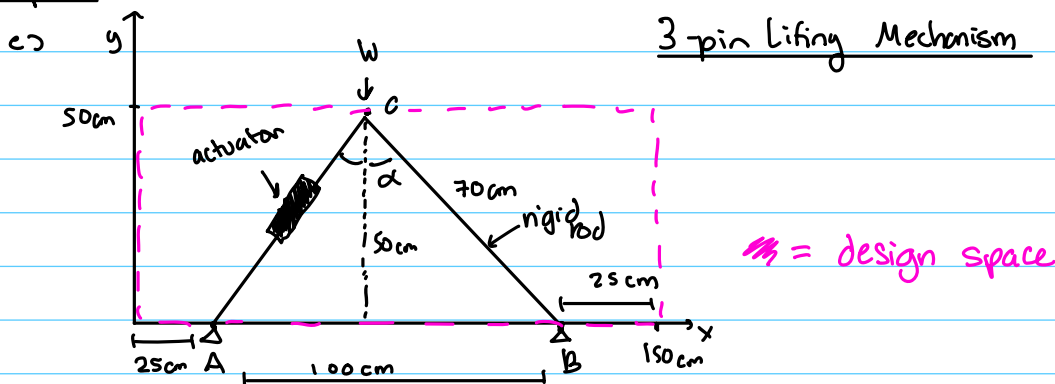
- Create sections to define the problem, your constraints/objectives, and your design degrees of freedom.
- Treating the bar as rigid, revisit your submission for HW5 by describing the static analysis you conducted to determine your final design.
- Ppresent your final mechanism design in an image or drawing.

**Step 2:** The bar in your mechanism is no longer rigid. In fact, it is now best described as a beam which bends due to the combined action of the weight and the actuator force. Consider only the components of these forces transverse to your beam:

- Find the maximum deflection in your beam. State your assumptions clearly and describe your analysis.
- Choose a beam design (cross-section, material) such that its vertical deflection is below 2% of its length and is the most mass-efficient possible.
- Ppresent your final beam design in an image or drawing.

any changes not reflected in this pdf are on the github

Step 1



Part 2

a) Even though the rod is acting like a beam, since we have a 3-pin system, moment and shear will NOT develop in the rod. The rod goes under axial load only. Therefore, the results obtained in the last assignment are still valid.

$$\text{Rod (CB) axial force} = 36.53 \text{ kN}$$

$$\Delta_a = \frac{FL}{AE}$$

$A = \text{area (mm}^2\text{)} \rightarrow \text{assume a circular rod with radius of } R$

$$E = 200,000 \text{ N/mmL} = 200 \text{ kN/mmL} \quad (\text{modulus of elasticity of steel})$$

$F = \text{axial force (kN)}$

$$\Delta_a = \frac{FL}{AE} = \frac{36.53L}{(\pi R^2)(200)}$$

$$\text{b) } \Delta_a \leq 0.02L$$

$$(\Delta_a)_{\max} = 0.02L = \frac{36.53L}{(\pi R^2)(200)} \rightarrow R_{\min} = 1.705 \text{ mm}$$

$\hookrightarrow$  we can make a rod with a 1.75 mm radius

