

Compute Actuator Transverse Component at P (Vector method) ~ Calculations:

Actuator direction from G_2 to P :

$$\begin{aligned} r = P - G_2 &= (0.90905934 - 1.00, 0.41666667 - 0)) \\ &= (-0.09094066, 0.41666667) \end{aligned}$$

Length of actuator line

$$|r| = \sqrt{(-0.09094066)^2 + (0.41666667)^2} = 0.426475456 \text{ m}$$

Unit vectors:

$$\text{Beam unit vector } \hat{\vec{u}}_{beam} = (\cos\theta, \sin\theta) = (0.90905934, 0.41666667)$$

$$\text{Actuator unit vector } \hat{\vec{u}}_{act} = r/|r| = (-0.2133957, 0.9769693)$$

Perpendicular component magnitude factor (2D cross product magnitude):

$$\left| \hat{\vec{u}}_{act} \times \hat{\vec{u}}_{beam} \right| = \left| \hat{\vec{u}}_{act,x} \cdot \hat{\vec{u}}_{beam,y} - \hat{\vec{u}}_{act,y} \cdot \hat{\vec{u}}_{beam,x} \right| \approx 0.9770003436$$

Actuator transverse (perpendicular) force at P:

$$F_{\perp} = F_a \cdot \left| \hat{\vec{u}}_{act} \times \hat{\vec{u}}_{beam} \right| = 35,810 \times 0.9770003436 \approx 34,986.38 \text{ N}$$

So essentially most of the actuator thrust contributes to bending