

## Function Documentation: rhs

Computes the derivatives of the system's state and the control input based on the current state and other system parameters.

Inputs:

currentState (vector): Represents the current state of the system, provided by bike sensors.

- currentState(2):  $x$  - X-coordinate.
- currentState(3):  $y$  - Y-coordinate.
- currentState(4):  $\phi$  - Roll angle.
- currentState(5):  $\psi$  - Yaw angle.
- currentState(6):  $\delta$  - Steering angle.
- currentState(7):  $\dot{\phi}$  - Roll angular velocity.
- currentState(8):  $v$  - Velocity.

p (struct): Contains various system parameters.

- p.g:  $g$  - Gravitational acceleration.
- p.l:  $l$  - Wheelbase length.
- p.b:  $b$  - Distance between the center of mass and the rear axle.
- p.h:  $h$  - Height of the center of mass above the ground.

K (vector): Contains control gains, sourced from simulations by the navigation subteam.

- K(1):  $k_1$  - Gain for the roll angle.
- K(2):  $k_2$  - Gain for the roll angular velocity.
- K(3):  $k_3$  - Gain for the steering angle.

delta\_offset (scalar): Offset for the steering angle ( $\delta$ ), sourced from simulations by the navigation subteam.

phi\_offset (scalar): Offset for the roll angle ( $\phi$ ), sourced from simulations by the navigation subteam.

linear (logical): Indicates whether to use a linear or nonlinear model. Note: This variable isn't actively used in the provided code.

## Equations:

### 1. Control Variable Calculation:

$$u = k_1(\phi - \phi_{\text{offset}}) + k_2\dot{\phi} + k_3(\delta - \delta_{\text{offset}})$$

### 2. State Derivative Calculations:

#### a. Position Derivatives:

$$\dot{x} = v \cdot \cos(\psi)$$

$$\dot{y} = v \cdot \sin(\psi)$$

#### b. Orientation Derivatives:

$$\dot{\phi} = \text{phi\_dot}$$

$$\dot{\psi} = \left(\frac{v}{l}\right) \cdot \frac{\tan(\delta)}{\cos(\phi)}$$

#### c. Steering Angle Derivative:

$$\dot{\delta} = u$$

#### d. Velocity Derivative:

$$\dot{v} = 0$$

#### e. Roll Angle Acceleration (Nonlinear EOM):

$$\ddot{\phi} = \frac{1}{h} \left[ g \sin(\phi) - \tan(\delta) \left( \frac{v^2}{l} + \frac{b\dot{v}}{l} + \tan(\phi) \left( \frac{bv\dot{\phi}}{l} - \frac{hv^2 \tan(\delta)}{l^2} \right) \right) - \frac{bv\dot{\delta}}{l \cos^2(\delta)} \right]$$

Note: I assume the velocity derivative equation(d) is set to 0 as there is no acceleration on the bike. This might need to be adjusted.