

Lecture 7: Classification Models and Cross Validation

INFO 1998: Introduction to Machine Learning



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Agenda

1. **Decision Trees**
2. **Logistic Regression and Its Applications**
3. **Cross Validation**

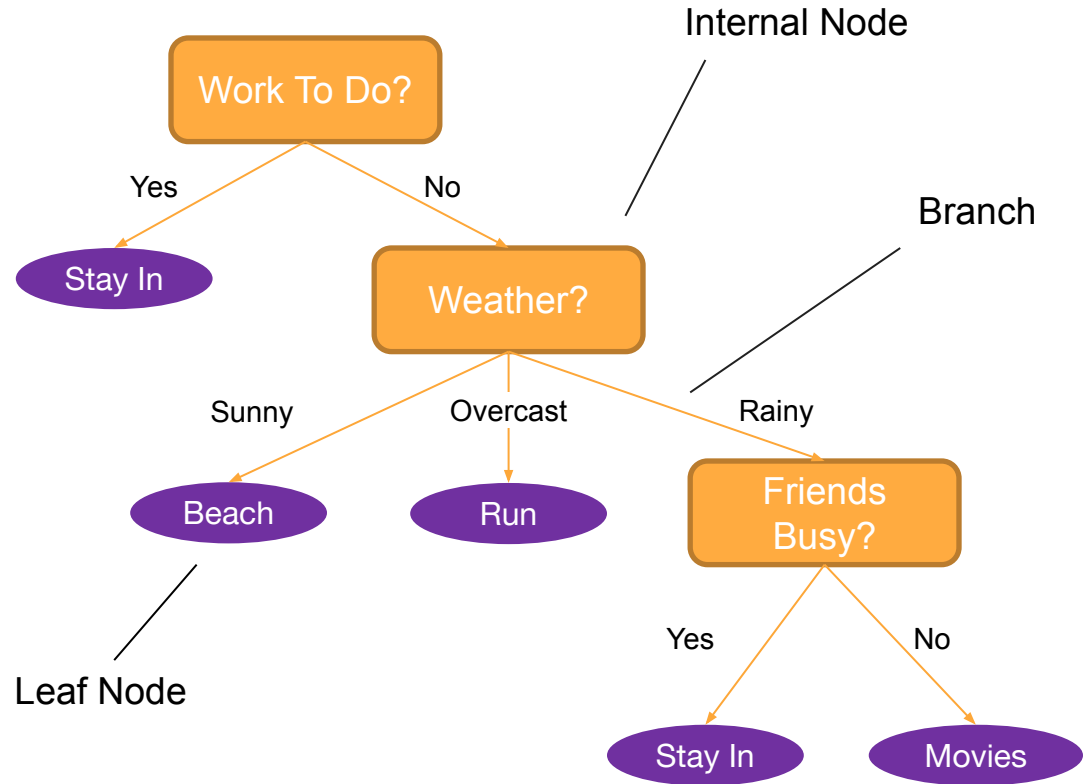


Decision Trees



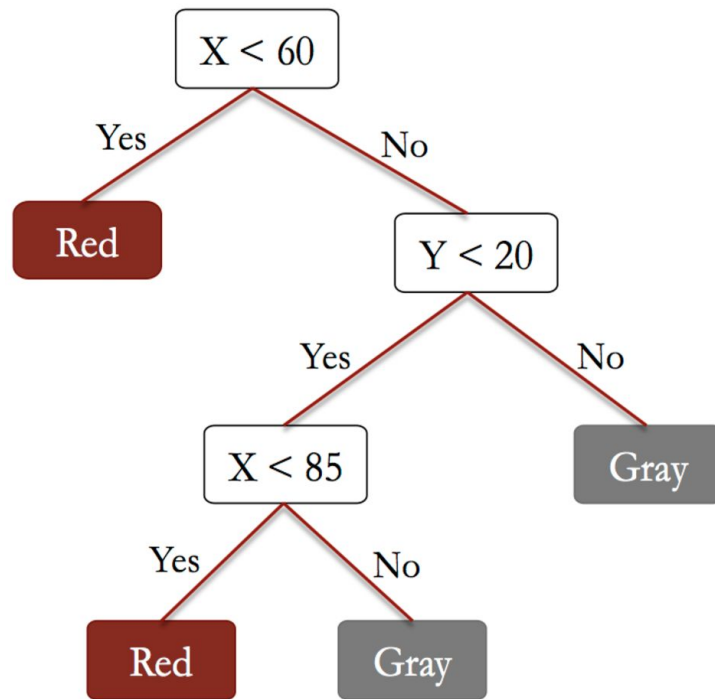
How Should I Spend My Weekends

A **decision tree** is a supervised machine learning model used to predict a target by learning decision rules from features. As the name suggests, we can think of this model as **breaking down** our data by **making a decision** based on **asking a series of questions**.



CART (Classification and Regression Trees)

- Used for Classification and Regression
- At each node, split on variables
- Each split minimizes error function
- Very interpretable
- Models a non-linear relationship!



Pros and Cons of Using Decision Trees

Pros	Cons
Easy to interpret	Overfitting 😞
Requires little data preparation (robust to missing data)	Requires parameter tuning (max depth)
Can use a lot of features	
Can capture non-linear relationships	



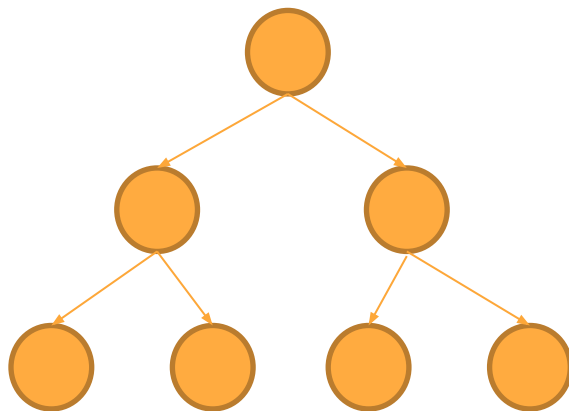
How to Reduce Overfitting

1. Limit the max depth of the tree

Depth = 0

Depth = 1

Depth = 2



Model
Complexity

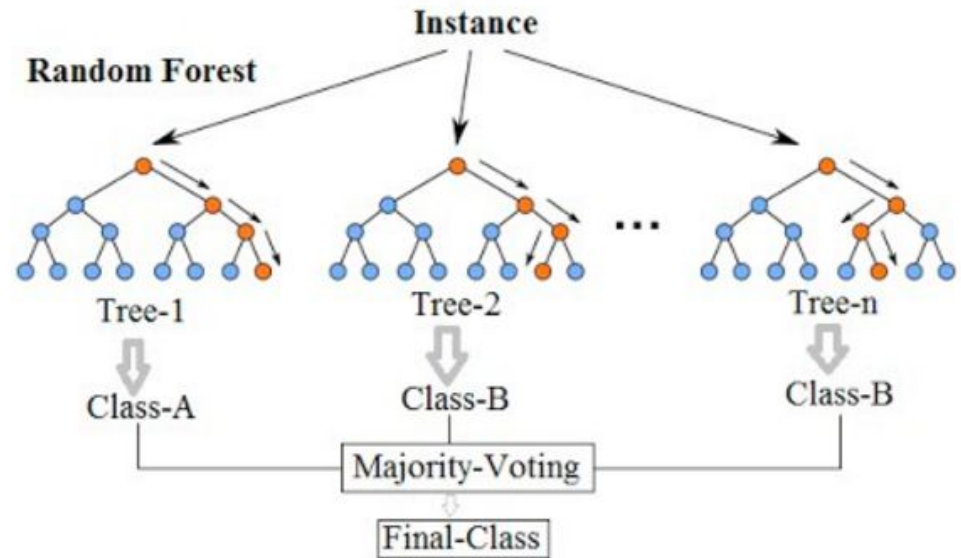
When training a decision tree, we have to specify the maximum depth a constructed tree can have



How to Reduce Overfitting

2) Train multiple decision trees and determine final output based on output of each decision tree

This is called a
Random Forest Classifier



Demo



Logistic Regression



Logistic Regression

- Used for Binary Classification:

$$Y = \begin{cases} 1 \\ 0 \end{cases}$$

- Fits a linear relationship between the variables
- Transforms the linear relationship of probability that the outcome is 1 by using the **sigmoid function**

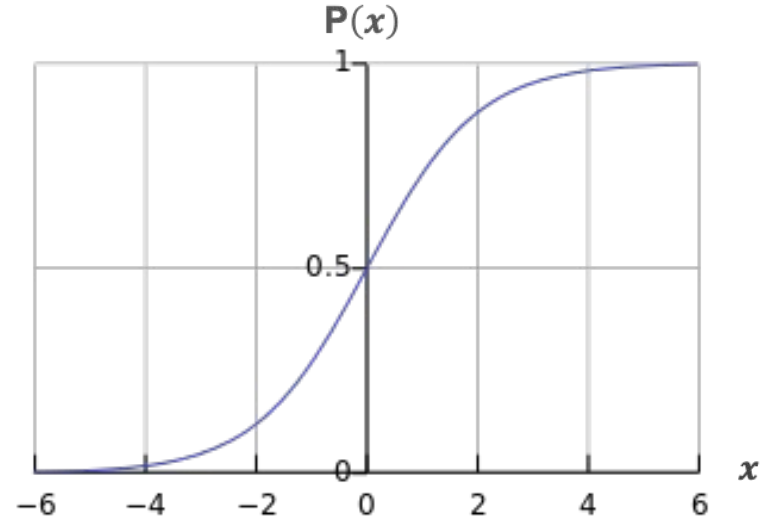
Formula:

$$P(x) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 x_1 + \dots + \beta_k x_k)}} \longrightarrow \ln\left(\frac{P}{1-P}\right) = \beta_0 + \beta_1 x_1 + \dots + \beta_k x_k$$



Logistic Function

$$\hat{P}(x) = \frac{1}{1 + e^{-x}}$$



The Logistic Function “**squeezes**” numbers to be between 0 and 1

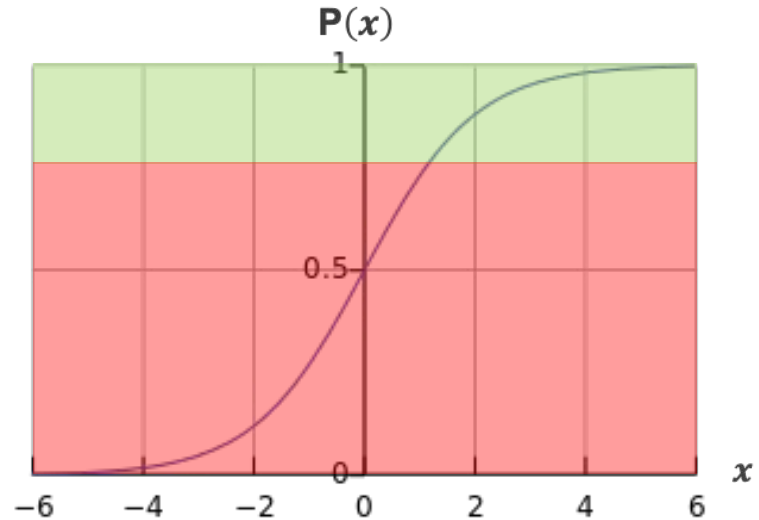


Allows us to interpret our prediction as a
“**probability**” that something is true

Threshold

At what point do we differentiate between our classifications?

- $f(x)$ **below** threshold: predict 0
- $f(x)$ **above** threshold: predict 1



Pros and Cons of Using Logistic Regression

Pros	Cons
Easy to interpret (probability)	Only Capable of Binary Classification
Computationally efficient to compute	
Does not require parameter tuning	

Logistic Regression is a simple model, therefore, oftentimes it is used as a good “baseline” to compare more complex models to



Demo



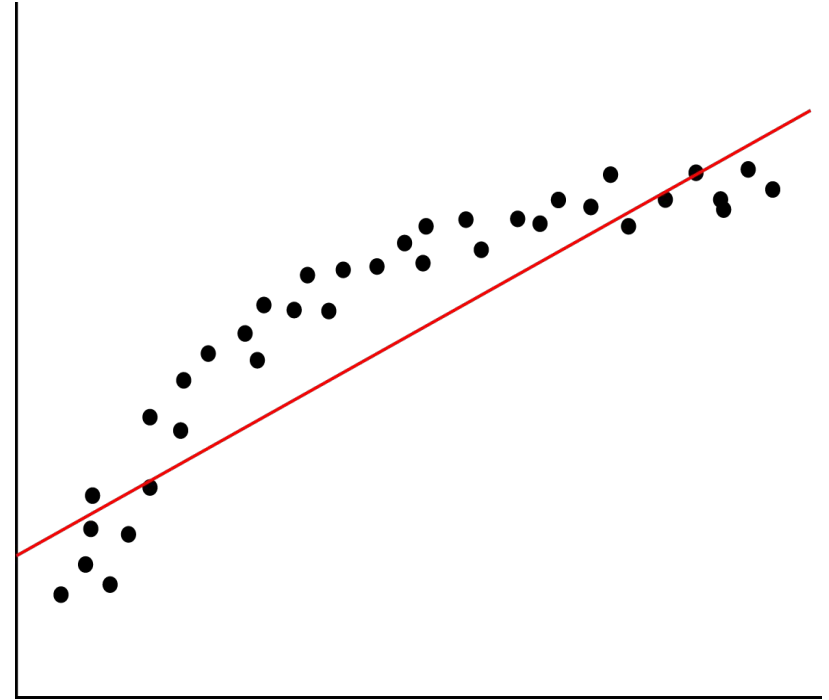
Cross Validation



Underfitting

Underfitting means we have high bias and low variance.

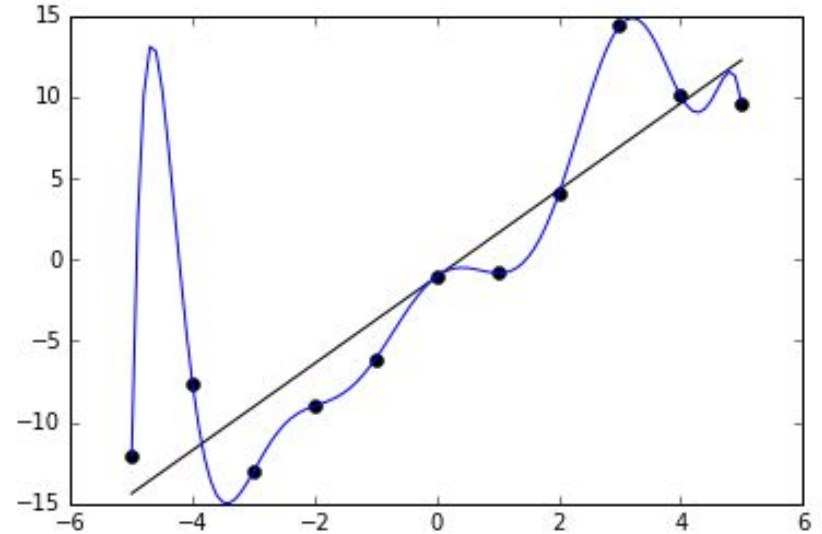
- Lack of relevant variables/factor
- Imposing limiting assumptions
 - Linearity
 - Assumptions on distribution
 - Wrong values for parameters



Overfitting

Overfitting means we have low bias and high variance.

- Model fits too well to specific cases
- Model is over-sensitive to sample-specific noise
- Model introduces too many variables/complexities than needed



K-fold Cross Validation



Often used in practice with $k=5$ or $k=10$.

Create equally sized k partitions, or **folds**, of training data

For each fold:

- Treat the $k-1$ other folds as training data.
- Test on the chosen fold.

The average of these errors is the validation error



***K*-fold Cross Validation**

Dataset

**Suppose $K = 5$,
5-Fold CV**



***K*-fold Cross Validation**

Fold 1

Fold 2

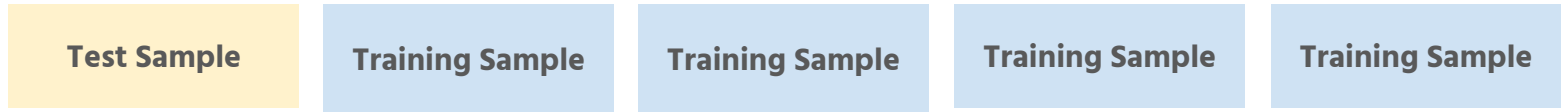
Fold 3

Fold 4

Fold 5



***K*-fold Cross Validation**



Calculate $MSE = mse_1$



***K*-fold Cross Validation**

Training Sample

Test Sample

Training Sample

Training Sample

Training Sample

Calculate $MSE = mse_2$



***K*-fold Cross Validation**

Training Sample

Training Sample

Test Sample

Training Sample

Training Sample

Calculate $MSE = mse_3$



***K*-fold Cross Validation**

And so on



K-fold Cross Validation

Fold 1

Fold 2

Fold 3

Fold 4

Fold 5

$$\text{MSE} = \text{Avg}(\text{mse1...5})$$



***K*-fold Cross Validation**

**Matters less
how we divide
up**

**Selection bias
not present**



Leave-1-Out Cross Validation

For each sample:

- Treat all other data as training data.
- Test on that one sample

The average of these errors is the validation error

Pro: Better on small datasets

Pro: More realistic (trained on most of the data)

Con: Takes longer to run



Demo

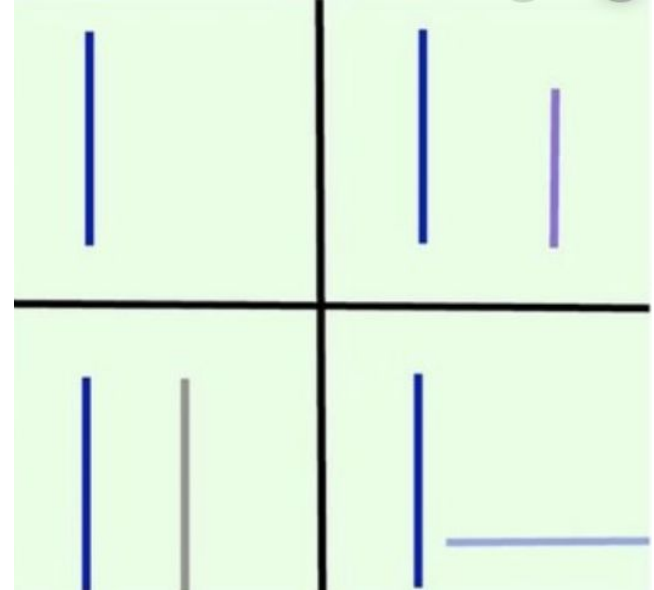


Review



Loss, Cost, and Score Functions

- **Loss Function**
 - Penalty for missing a single data point
- **Cost Function**
 - Indicates how bad the whole model is
 - Applies loss function to each point, then combines that into a single number
 - ex: average of (loss from each point)
- **Score Function**
 - A more interpretable version of the cost function



Cost -> Accuracy Score

- sklearn's score function is:

$$1 - ([\text{Cost of model}] / [\text{Cost of baseline}])$$

- 1 is very, very good
- 0 means you were as bad as the baseline
- <0 means either your baseline predictions were very good, or you really, really messed up



Balancing Bias and Variance

$$\text{Error} = (\text{Bias})^2 + (\text{Variance}) + (\varepsilon)$$

Bias = expected loss of accuracy

Variance = inconsistency of model

ε = irreducible error



Linear Regression

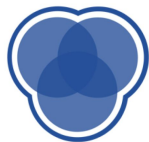
$$y = B_0 + B_1x_1 + \dots + B_px_p + \varepsilon$$

- x is an input; x_1, x_2, \dots, x_p are the features of x
- y is an output (usually a single value)
- B 's are “weights”
 - A linear regression equation is defined by its B 's
 - This linear regression equation is the “program” produced by ML
- Given a set of x 's and y 's, the program finds a set of B 's that (almost) satisfies the equation above for all x 's and y 's
 - **Minimizes bias, but not variance**
 - Then, you can plug in the feature values of a new x and to predict its y



Coming Up

- **Assignment 7:** Due 4:30pm on Nov. 10
- **Next Lecture:** Linear Classifiers and Model Validation
- **Final Project Check in:** Due 4:30pm on Nov. 10



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