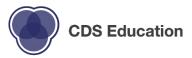
# **Lecture 7: Supervised Learning Pt. 1**

Linear Classifiers and Cross Validation INFO 1998: Introduction to Machine Learning



# **Agenda**

- 1. Linear Classifiers
  - Linear Perceptron
  - Support Vector Machines (SVMs)
- 2. Cross Validation (K-Fold)



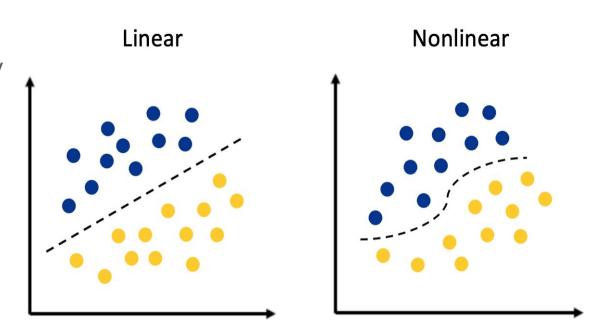
# **Linear Classifiers**



### **Linear Classifiers**

A linear classifier is a hyper plane that is used to classify our data points

A hyperplane is our decision boundary and our goal is to find the best hyper plane for our data.



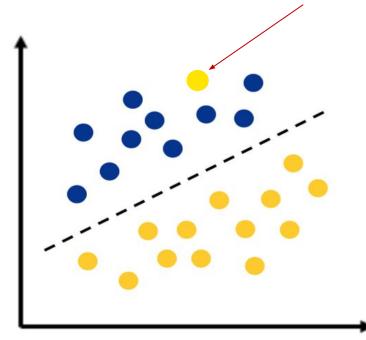


# **Linearly Separable**

In this example, we cannot partition our dataset into yellow and purple with a linear decision boundary. This means that our data is not linearly separable.

Outliers are frequently the reason a data set is not linearly separable.

This data set is not linearly separable because of an <u>outlier</u>





## **Perceptron Learning Algorithm**

Goal: find a normal vector w that perfectly classifies all the points in our data set Algorithm:

Initialize classifier as some random hyperplane
While there exists a misclassified point x:
 Adjust classifier slightly so that it classifies x correctly
 (or, is a little closer to classifying x correctly)
End While

"Use your mistakes as your stepping stones"



### **History of the Linear Perceptron**

Frank Rosenblatt was first to implement perceptron!

→ Cornell professor and alum PHD '56 6

Gave him the title of 'Father of Deep Learning'

**Deep Learning** 

→ Neural Networks a.k.a. Multilayer Perceptrons





### **Limitations of Perceptron**

The training algorithm will never terminate if your training dataset is not linearly separable •

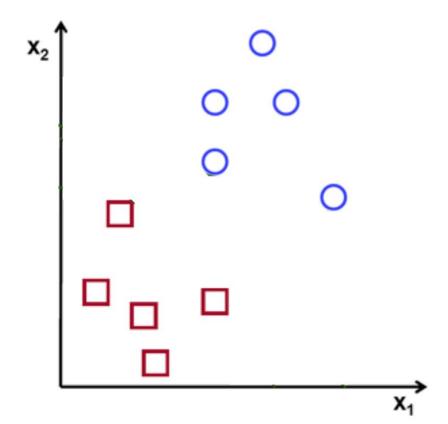
Is a great model to understand the intuition behind the training of a linear classifier: iteratively improve classifier by using misclassified points  $\rightleftharpoons$ 



# **Support Vector Machines**

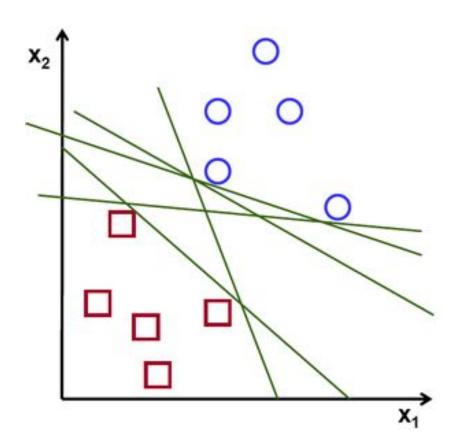


# Classify (+) and (-)



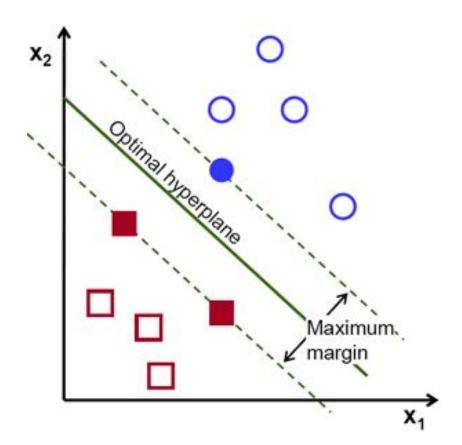


# Which Hyperplane?



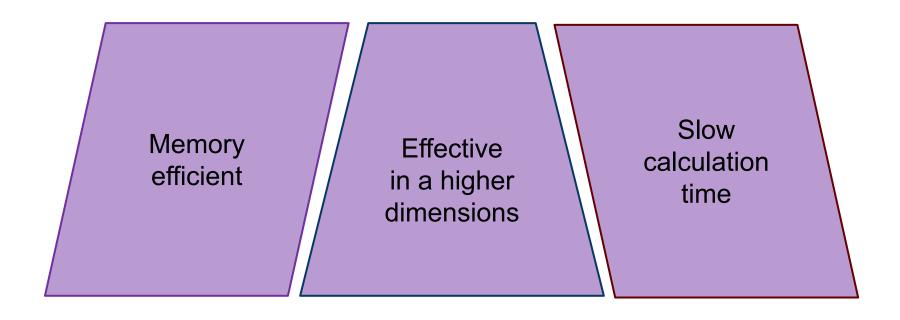


# **Optimal Hyperplane**





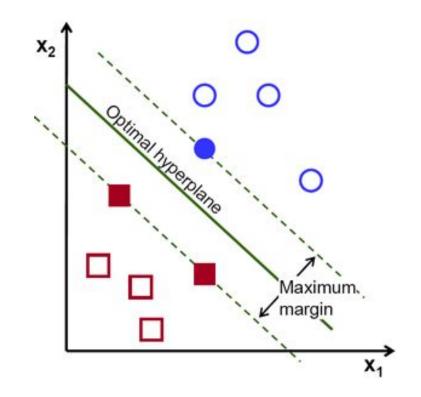
## **Support Vector Machine**





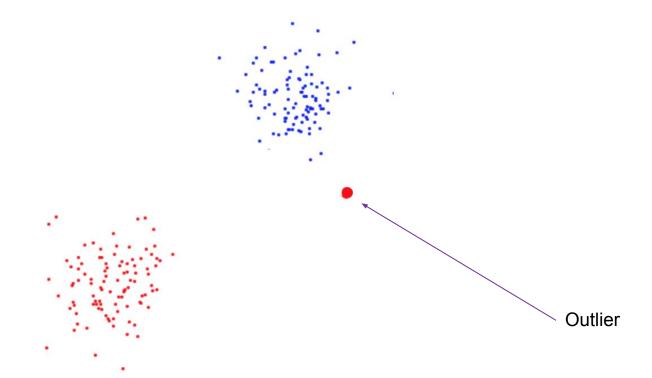
# **Maximal Margin Classifier**

- We want to find a separating hyperplane
- Once we find candidates for the hyperplane, we try to maximize the margin, the normal distance from borderline points
  - Only Support Vectors matter



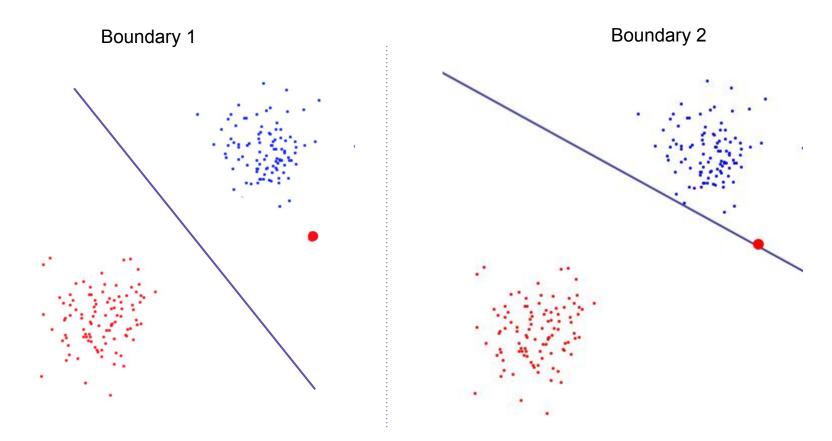


# What if...





# **Which Decision Boundary is better?**





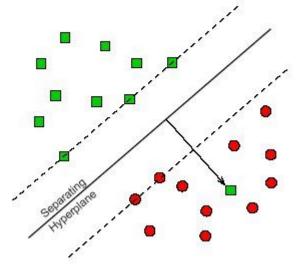
## **Margins**

Use cost function to penalize misclassified points

Choice of cost function makes margin "hard" vs. "soft"

#### Non-separable training sets

Use linear separation, but admit training errors.

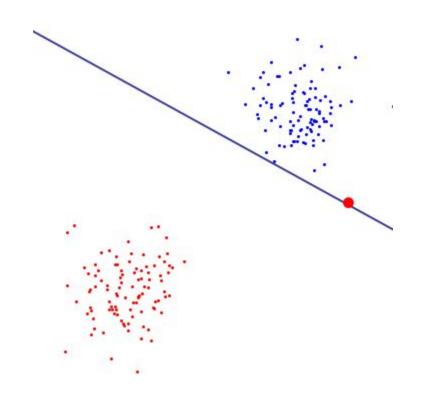


Penalty of error: distance to hyperplane multiplied by error cost C.



# **Hard Margins**

- High penalty value
- The hyperplane can be dictated by a single outlier



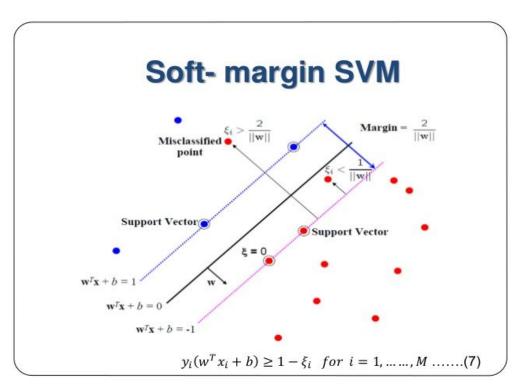


# **Soft Margins**

Used in non-linearly separable datasets

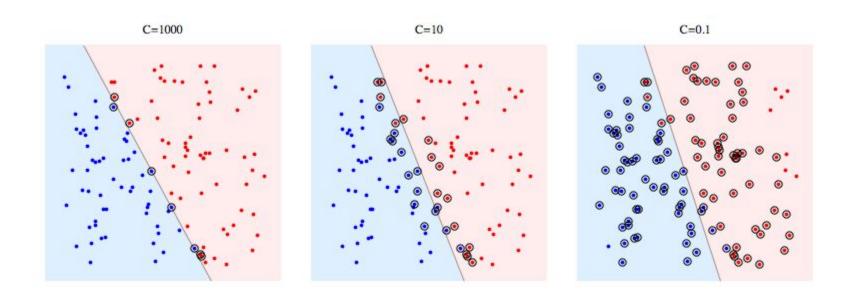
Allow for misclassification

 Can account for "dirty" boundaries





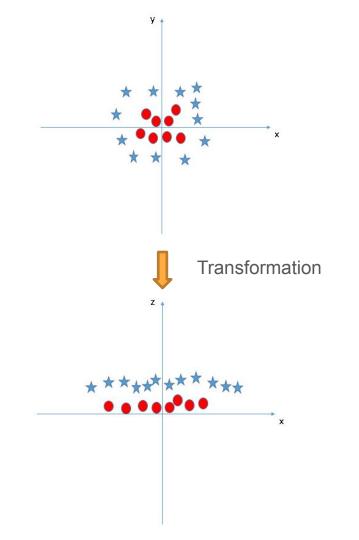
# **Misclassification Penalty C**





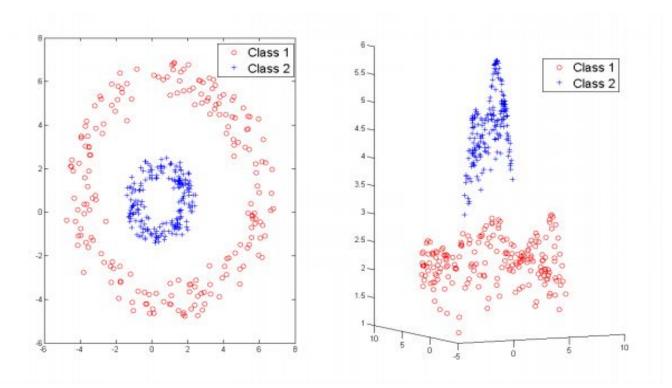
### Kernels

- You cannot linearly divide the 2 classes on the xy plane at right
- Introduce new feature,  $z = x^2 + y^2$  (radial kernel)
- Map 2 dimensional data onto 3 dimensional data. Now a hyperplane is easy to find.





# Kernels





### **SVM** has **MANY** Hyperparameters

### **SVM**

#### C

The "penalty cost" for misclassifications (soft margins)

#### Gamma

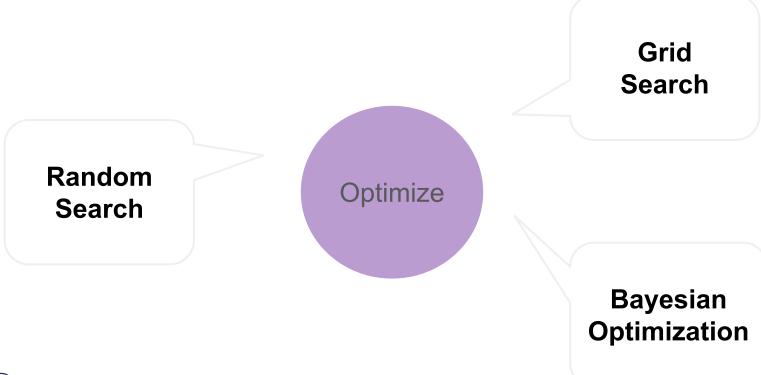
How far the influence of a single training example reaches

### Kernels

Method of transforming our data set



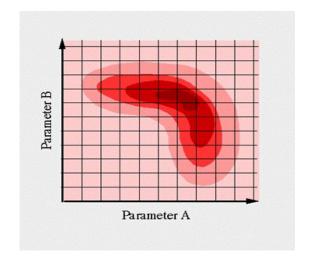
### **Finding the Best Hyper Parameters**

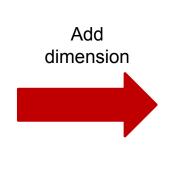


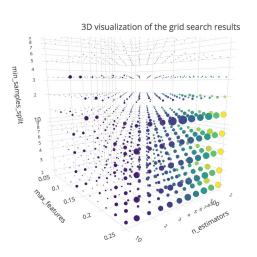


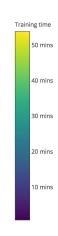
### **Curse of Dimensionality**

Our search space for the optimal hyper-parameters increases **exponentially** as the number of hyper parameters we are considering increases











## **Overview**

Perceptron	SVM
<ul> <li>A very simple model</li> <li>Will perform poorly if data is not linearly separable</li> </ul>	<ul> <li>More complex model because we have to choose the "penalty cost" associated with misclassifications</li> <li>Can transform feature space by choosing a Kernel</li> </ul>



# **Demo**



# **Cross Validation**





Often used in practice with k=5 or k=10.

Create equally sized *k* partitions, or **folds**, of training data

#### For each fold:

- Treat the *k-1* other folds as training data.
- Test on the chosen fold.

The average of these errors is the validation error



### **Dataset**



Fold 1 Fold 2 Fold 3 Fold 4 Fold 5



**Test Sample** 

**Training Sample** 

**Training Sample** 

**Training Sample** 

**Training Sample** 

Calculate MSE = mse1



**Training Sample** 

**Test Sample** 

**Training Sample** 

**Training Sample** 

**Training Sample** 

Calculate MSE = mse2



**Training Sample** 

**Training Sample** 

**Test Sample** 

**Training Sample** 

**Training Sample** 

Calculate MSE = mse3



# And so on



Fold 1 Fold 2 Fold 3 Fold 4 Fold 5

MSE = Avg(mse1...5)



Matters less how we divide up

Selection bias not present



### **Leave-1-Out Cross Validation**

For each sample:

- Treat all other data as training data.
- Test on that one sample

The average of these errors is the validation error

Pro: Better on small datasets

**Pro:** More realistic (trained on most of the data)

**Con:** Takes longer to run



### **Coming Up**

- Assignment 6: Due tonight at 11:59pm
- Assignment 7: Due next Wednesday at 11:59pm
- Mid-Semester Check-Ins: Due today! Please get them done ASAP:)
- Next Lecture: More Supervised Learning! (Decision Trees & Logistic Regression)

