

Cornell Data Science

Classification

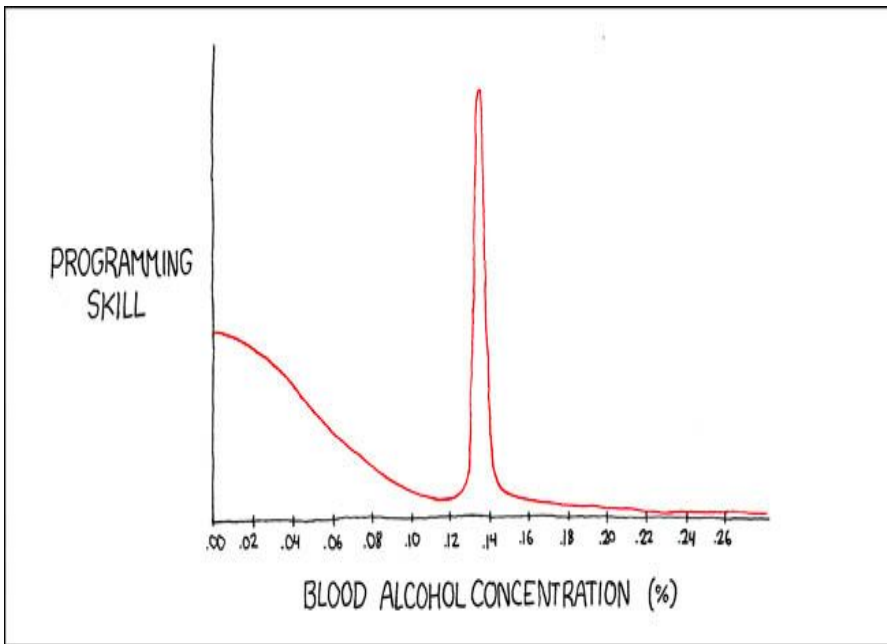


Recap

We have learned regression models to predict numeric continuous variables.

- Linear Regression
- Logistic Regression
- Decision Tree

Ex: Predicting stock value, monthly temperature, etc.



Intro to Classification

“What kind of species is this?”

“How would consumers rate this restaurant?”

“Which Hogwarts House do I belong to?”

“Am I going to pass this class?”



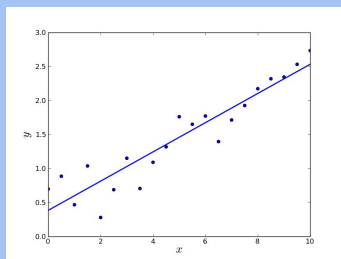
<https://www.bdcwire.com/wp-content/uploads/2015/04/Screen-Shot-2015-04-06-at-1.40.38-PM-e1428342443848-1000x531.png>

Recall: Predictive Modeling Challenges

Regression

“How much?”

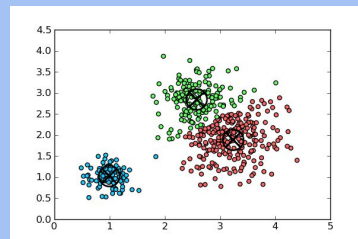
Used for *quantitative* predictions



Classification

“What kind?”

Used for *qualitative* predictions



https://lh3.ggpht.com/-d16xbB_2m94/Uml0Gi76Xtl/AAAAAAI94/5ezC-ZqZWz8/s1600/linearRegression.png

<http://blog.mpacula.com/wp-content/uploads/2011/04/kmeans1.png>

Wait ...

What did I just read?



Classifier 1: k-Nearest Neighbors (KNN)

Simple yet powerful tool

- Very easy to interpret output
- Relatively fast calculation time
- Makes no prior assumptions

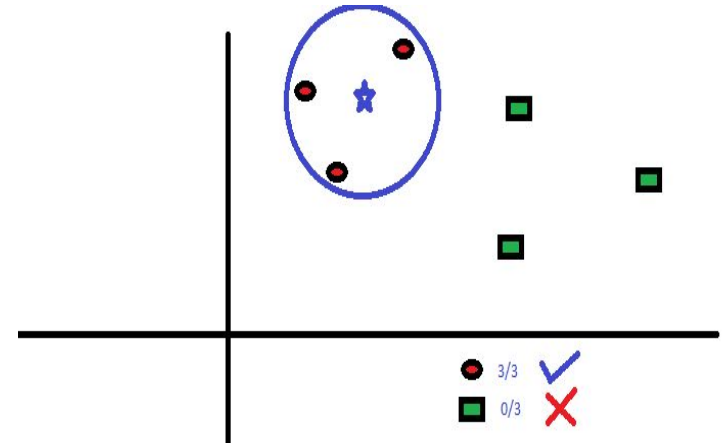
Too simple and only good for coarse analysis



KNN

How does it work?

- *Define* k value (in this case $k = 3$)
- *Pick* a point to predict (blue star)
- *Count* the number of closest types
- *Increase* the radius until the nearest type adds up to 3
- *Predict* the blue star to be a red circle!



<https://www.analyticsvidhya.com/blog/2014/10/introduction-k-neighbours-algorithm-clustering/>



Question:

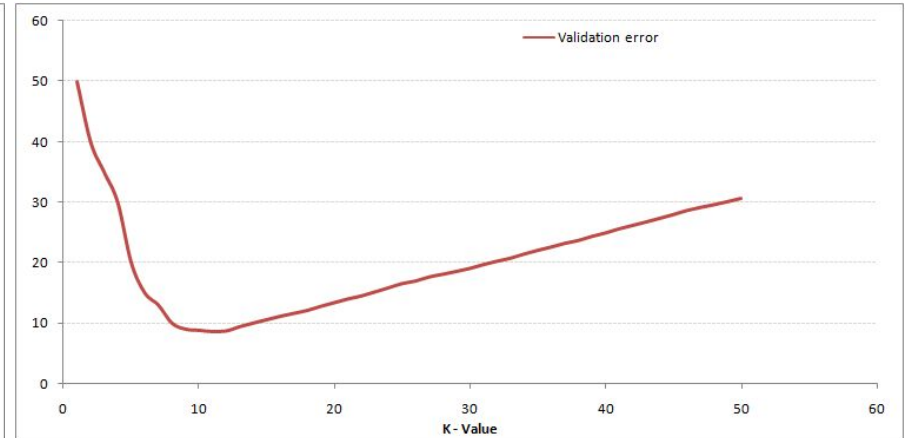
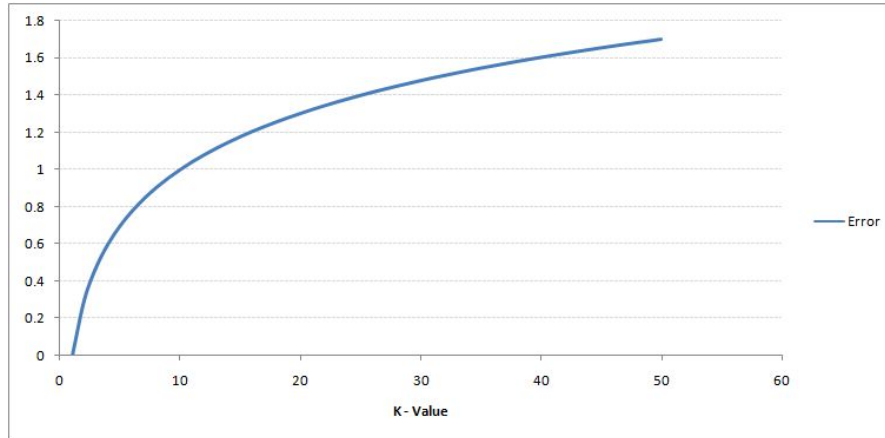
What defines a good k value?

Why is k odd?



KNN

k -value has a relationship to fit!



<https://www.analyticsvidhya.com/blog/2014/10/introduction-k-neighbours-algorithm-clustering/>

KNN in R - Demo Time!

We'll use the `knn` function from the `class` library.



Classifier 2: Naive Bayes

- Use Bayes Theorem
- Easy model to understand
 - Very fast!
 - Robust to outliers
 - Strong prediction even with small datasets
- Assuming every feature is **independent**



Conditional Probability and Independence

Conditional Probability:

Probability of an event A given an event B

Still confusing? Draw diagrams!

Independence:

When 2 events do not affect the probability of the other event occurring.

Assuming independence simplifies the calculation



Bayes' Theorem

$$P(A | B) = \frac{P(B | A)P(A)}{P(B)}$$



Naive Bayes Classifier

Problem: We have k classes and want to predict which class the point x belongs to.

- Represent x with a vector of n features and calculate the probability of x being in each k given the the vector.
- Predict x to be the class with the maximum probability

By using Bayes' Theorem and assuming all n features are independent, this probability can be expressed as

$$p(C_k) \prod_{i=1}^n p(x_i \mid C_k)$$



Naive Bayes (Continued)

Naive Bayes classifiers differ by how they assume the distribution of $P(x_i|C_k)$.

Gaussian Naive Bayes: The likelihood of features is assumed to be Gaussian.

Bernoulli Naive Bayes: The likelihood of features is assumed to follow Bernoulli distribution



Naive Bayes in R - Demo Time!



Classifier 3 - SVM

- Support Vector Machine
- Powerful tool with a badass name
 - Great at classifying data in a high dimensional space
 - Only uses subset of data, hence memory efficient
- Requires large calculation time and not great at noisy datasets

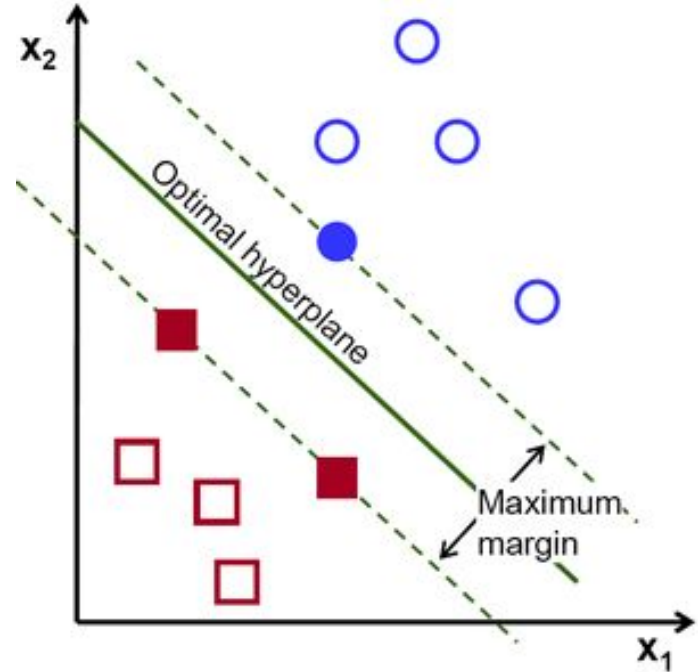


Maximal Margin Classifier

We want to find a **separating hyperplane**.

Once we find some candidates for the hyperplane, we try to maximize the **margin**, the distance from borderline points.

SVM is a maximal margin classifier on a higher dimension using **kernels**.

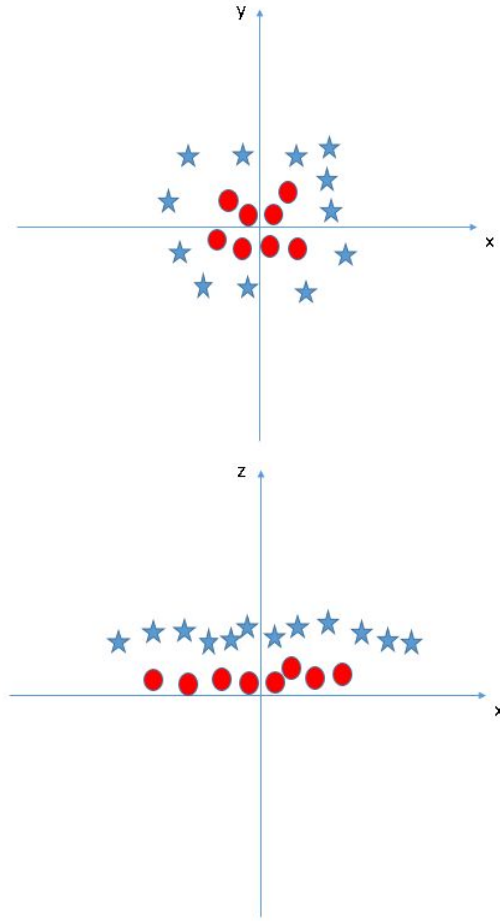


Kernels in Action

You cannot linearly divide the 2 classes on the xy plane at right.

Introduce new feature, $z = x^2 + y^2$ (**radial kernel**)

Map 2 dimensional data onto 3 dimensional data. Now a hyperplane is easy to find. (Imagine slicing a cone!)



Demo Time!

We'll use the `ksvm` function from `kernlab` library.



Coming Up

Your problem set: Continue project 1

Next week: Clustering and unsupervised learning!

