

Analysis and Implementation of 3D Magnetic Field Shaping via A 2D Planar Transmitting Coil Array

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Abstract—Wireless power transfer (WPT) systems operating at several MHz are known to be advantageous for realizing high spatial freedom of power transfer and compact/lightweight designs. The combined use of multiple transmitting (Tx) coils for magnetic field shaping is expected to further increase the spatial freedom. This paper studies an extendable planar Tx-coil array architecture. This architecture provides new conveniences for the MHz WPT systems to efficiently charge devices in 3D space. Time-domain and phasor-domain modelings are carried out in turn to analyze the magnetic field shaping effect under the current phase shift modulation of the Tx coils. An overlap design of the Tx-coil layout is also developed to minimize the cross coupling between the coils, which reduces the interference between Tx coils. Finally, the above concepts are experimentally implemented. The results clearly demonstrate the new advantages of the planar Tx-coil array-based magnetic field shaping, in terms of spatial freedom of the power transfer, efficiency, and output power capability, when charging receivers with six-degrees-of-freedom positions and orientations in 3D space. For instance, a perpendicular receiver in the center of the Tx-coil array can be charged with 82% dc-dc efficiency and 45 W, which is difficult for a conventional single Tx-coil solution.

Index Terms—Cross coupling minimization, magnetic field shaping, planar transmitting-coil array, 3D space, wireless power transfer.

I. INTRODUCTION

Wireless power transfer (WPT) has attracted great interest in recent years due to the significantly enhanced convenience in charging various electronic devices and even electric vehicles. Most commercial WPT systems operate in the kilohertz (kHz) band [1], [2]. Many efforts have been made to improve the performance of the kHz systems through innovations in circuit topology, coil design and control [3]–[5]. At the same time, a higher operating frequency, such as several megahertz (MHz), is promising to achieve a higher degree of spatial freedom in power transfer and a compact and lightweight design [6]–[8]. As same as the kHz WPT, the ever-increasing requirement

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for the spatial freedom also poses challenges for the MHz WPT, especially when charging devices with different positions and orientations in three-dimensional (3D) space. Many investigations have been conducted such as through adopting repeaters, impedance matching networks, new coil structures and switching devices [9]–[12]. In conventional WPT systems, the magnetic field (i.e., B-field) distribution is usually regarded as uncontrollable, which depends mostly on the design of transmitting (Tx) coil. For instance, different single 3D Tx coils have been proposed to generate an omnidirectional magnetic field [13], [14]. In addition, direct-quadrature (DQ) Tx coils with ferrite cores were applied to achieve wide-range omnidirectional inductive power transfer [15], [16]. Specially designed 3D receiving (Rx) coils were also developed to reduce the spatial output power variation [17], [18].

Through multiple Tx coils and appropriate control, it is possible to actively shape the B-field distribution in 3D space. This provides an important new degree of freedom to further enhance the performance (e.g., transfer distance, efficiency and power transfer capability) of today's MHz WPT systems. Majority of existing work on the magnetic field shaping operated in the kHz band, and many of those investigations adopted 3D structures of orthogonal Tx coils, which can straightforwardly avoid cross coupling between Tx coils [18]–[21]. For instance, nonidentical current control for two-dimensional (2D) and 3D omnidirectional WPT has been proposed and implemented [19]. A spherical shape transmitter structure was adopted consisting of two or three separate orthogonal Tx coils and worked at 530 kHz. With the similar transmitter structure, a quadrature-shaped receiving (Rx) coil was further developed to achieve an angular-misalignment insensitive 100 kHz WPT system [18]. Using two orthogonal rectangular Tx coils, a phase-control method was applied to form magnetic fields in 2D directions [20]. Experimental results showed average improvements of power transfer efficiency and distance by 20.1% and 30% with an operating frequency of 60 kHz. Based on a cubic-shaped structure using three orthogonal Tx coils, real-time control of Tx coil currents, i.e., different amplitudes and phases (0 or 180°), was proposed to charge multiple moving receivers with a 20 kHz operating frequency [21]. A current amplitude control scheme was applied to a bowl-shaped omnidirectional 6.78 MHz WPT system, which achieved 60–70% dc-dc efficiency at 3–15 W when charging multiple receiving devices [22].

As mentioned above, the existing work mainly used 3D Tx coil structures to combine the magnetic field generated by individual Tx coils in a direction perpendicular to the coil plane. Meanwhile, this paper also makes full use of the

magnetic field distribution in the horizontal direction to realize the 3D magnetic field shaping through a 2D planar Tx coil array. In addition, compared with the 3D coil structures, a two-dimensional (2D) structure, i.e., a planar Tx-coil array, would be more convenient to integrate in many application scenarios. It also provides more design freedom in number and layout of the Tx coils, especially in terms of extendability. Besides, unlike the existing 3D orthogonal Tx coil structures, the overlap design of the 2D Tx-coil array is developed to largely minimize the cross coupling between the Tx coils. A phasor representation is also proposed to derive the B-field amplitude distribution, which is directly relevant to the spatial power distribution. Further, combining with the MHz operating frequency, the spatial freedom of the power transfer and compactness of the final systems can be obviously improved.

Therefore, this paper studies an extendable planar Tx-coil array architecture for the magnetic field shaping, which has a potential to charge devices with different 3D positions and orientations. First, the B-field distribution is analytically modelled in Section II to clarify the mechanism of the 3D magnetic field shaping through the 2D planar Tx-coil array. Secondly, the cross coupling between two adjacent Tx coils is especially analyzed, which is the unique challenge of adopting the planar array architecture, and is minimized later by optimally designing the layout of the Tx coils, as discussed in Section III. This reduces the interference among the Tx coils (i.e., additional reflected impedances) and thus helps to improve the operating conditions of power amplifiers (PAs) and the performance of the final WPT system. In section IV, calculation results of the B-field amplitude distribution are visualized to verify magnetic field shaping effects through the planar Tx-coil array and phase shift modulation of Tx-coil currents. Finally, Section V explains a complete experimental 6.78 MHz WPT system, implementing a 2×2 planar Tx-coil array. An LED array is fabricated to experimentally visualize the actual magnetic field shaping and verify the consistency with the calculation results. The efficiency and output power are then measured and compared when transferring power to an Rx coil moving in six degrees of freedom. The results show significant improvements through the Tx-coil array-based magnetic shaping and minimized cross coupling design. In Section VI, conclusions and main future works are

addressed.

II. ARCHITECTURE AND MODELING

A. Extendable Planar Tx-coil Array

Fig. 1 illustrates the layout of an extendable planar Tx-coil array, such as using square coils. And Fig. 2 shows the relationship between PAs and Tx coils. Due to its 2D structure, modulating the phase shift in all the Tx coils is especially effective to shape the final magnetic field in 3D space. In the figure, the side length of each square coil is represented by l . Cross coupling between individual Tx coils changes with the distance d between adjacent coils. In this planar coil array, all the Tx coils locate on the XOY plane, and the four corners of a single Tx-coil ($Tx_{i,j}$) in the i -th row and j -th column are:

$$\begin{cases} A_{i,j} & (id + il - l, jd + jl, 0), \\ B_{i,j} & (id + il, jd + jl, 0), \\ C_{i,j} & (id + il, jd + jl - l, 0), \\ D_{i,j} & (id + il - l, jd + jl - l, 0). \end{cases} \quad (1)$$

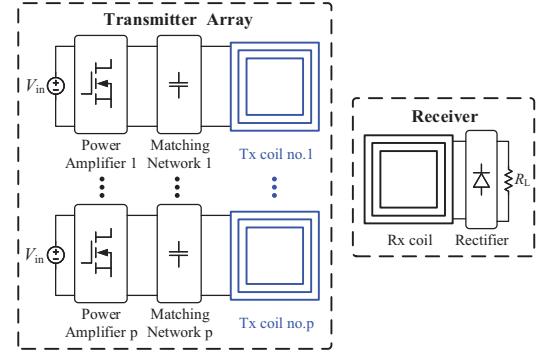


Fig. 2. Typical system configuration.

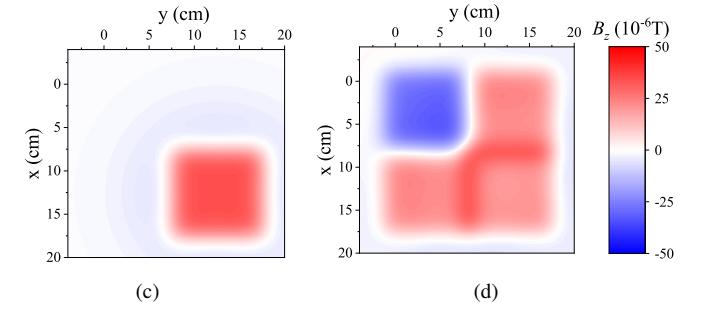
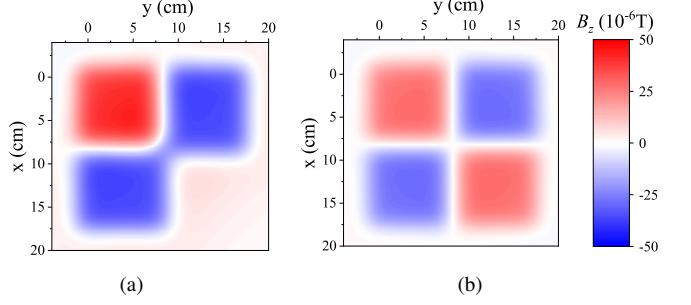
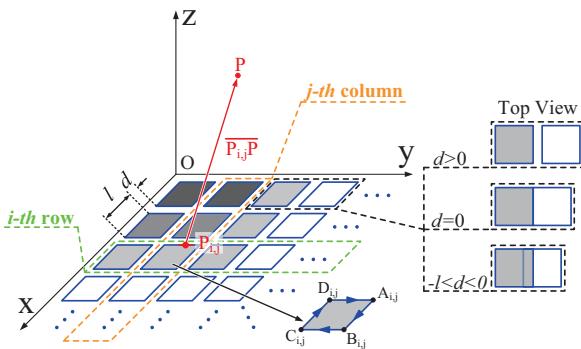


Fig. 3. Calculation results of z -direction B-field generated by a 2×2 Tx-coil array at different observation time t ($z = 2.5 \text{ cm}$). (a) $\omega t = 0$. (b) $\omega t = \frac{\pi}{4}$. (c) $\omega t = \frac{\pi}{2}$. (d) $\omega t = \frac{3\pi}{4}$.

Fig. 1. An extendable planar Tx-coil array.



And it is supposed that the current $I_{i,j}$ of $\text{Tx}_{i,j}$ flows from $A_{i,j}$ to $B_{i,j}$, $C_{i,j}$ and $D_{i,j}$.

In Fig. 1, point $P_{i,j}(x_{i,j}, y_{i,j}, z_{i,j})$ is on the $\text{Tx}_{i,j}$ and an arbitrary point $P(x, y, z)$ is in 3D space. A unity vector from $P_{i,j}$ to P is $\hat{r}_{i,j}$, which can be expressed as

$$\begin{aligned}\hat{r}_{i,j} &= \frac{\overline{\text{P}_{i,j}\text{P}}}{|\overline{\text{P}_{i,j}\text{P}}|} \\ &= \frac{\hat{e}_x(x - x_{i,j}) + \hat{e}_y(y - y_{i,j}) + \hat{e}_z(z - z_{i,j})}{\sqrt{(x - x_{i,j})^2 + (y - y_{i,j})^2 + (z - z_{i,j})^2}},\end{aligned}\quad (2)$$

where \hat{e}_x , \hat{e}_y and \hat{e}_z are unity vectors in x , y and z directions. The current $I_{i,j}$ in $\text{Tx}_{i,j}$ is

$$I_{i,j} = I_{i,j}^m \cos(\omega t + \theta_{i,j}), \quad (3)$$

where $I_{i,j}^m$ is amplitude, $\theta_{i,j}$ is initial phase, and ω is a target operating frequency, such as 6.78 MHz in this paper. Based on the Biot-Savart law and (1)–(3), the magnetic flux density induced by $\text{Tx}_{i,j}$ at an arbitrary point P can be derived as

$$\begin{aligned}\overline{B_{i,j}} &= \oint \frac{\mu_0}{4\pi} \frac{N_{tx} I_{i,j}^m \cos(\omega t + \theta_{i,j})}{r_{i,j}^2} \overline{dl} \times \hat{r}_{i,j} \\ &= \frac{\mu_0 N_{tx} I_{i,j}^m \cos(\omega t + \theta_{i,j})}{4\pi} \\ &\quad \left\{ \int_{A_{i,j}B_{i,j}} \frac{1}{r_{i,j}^3} [\hat{e}_z(y - y_{i,j}) dx - \hat{e}_y(z - z_{i,j}) dx] \right. \\ &\quad - \int_{B_{i,j}C_{i,j}} \frac{1}{r_{i,j}^3} [\hat{e}_x(z - z_{i,j}) dy - \hat{e}_z(x - x_{i,j}) dy] \\ &\quad - \int_{C_{i,j}D_{i,j}} \frac{1}{r_{i,j}^3} [\hat{e}_z(y - y_{i,j}) dx - \hat{e}_y(z - z_{i,j}) dx] \\ &\quad \left. + \int_{D_{i,j}A_{i,j}} \frac{1}{r_{i,j}^3} [\hat{e}_x(z - z_{i,j}) dy - \hat{e}_z(x - x_{i,j}) dy] \right\},\end{aligned}\quad (4)$$

where N_{tx} is the number of turns of $\text{Tx}_{i,j}$; μ_0 is the permeability of vacuum. Note that $\overline{B_{i,j}}$ has its $B_x|_{i,j}$, $B_y|_{i,j}$ and $B_z|_{i,j}$ terms. Detailed derivations of $B_x|_{i,j}$, $B_y|_{i,j}$ and $B_z|_{i,j}$ are listed in the Appendix. The B-field at point P is the sum

of the B-field induced by each coil in an $m \times n$ Tx-coils array,

$$\begin{bmatrix} B_x \\ B_y \\ B_z \end{bmatrix} = \begin{bmatrix} \sum_{i=1}^m \sum_{j=1}^n B_x|_{i,j} \\ \sum_{i=1}^m \sum_{j=1}^n B_y|_{i,j} \\ \sum_{i=1}^m \sum_{j=1}^n B_z|_{i,j} \end{bmatrix}. \quad (5)$$

As shown by the calculation results in Fig. 3, the z -direction B-field induced by a 2×2 coil array, as an example, changes with time. The four coils, namely $\text{Tx}_{1,1}$, $\text{Tx}_{1,2}$, $\text{Tx}_{2,1}$ and $\text{Tx}_{2,2}$, have the same current amplitude and frequency, while the phases of the four coils are 180° , 0° , 0° , and 90° , respectively. The real-time B-field strength at the same position changes with time, but its amplitude is fixed and corresponds to the maximum receiving power.

B. B-field Amplitude Distribution Function

To obtain the B-field Amplitude Distribution Function (ADF), the expression of the B-field can be first simplified as follows:

$$\begin{bmatrix} B_x \\ B_y \\ B_z \end{bmatrix} = \begin{bmatrix} B_x^m \cos(\omega t + \theta_x) \\ B_y^m \cos(\omega t + \theta_y) \\ B_z^m \cos(\omega t + \theta_z) \end{bmatrix}, \quad (6)$$

where B_x^m , B_y^m and B_z^m are the ADFs of x -direction, y -direction, and z -direction components of the B-field; θ_x , θ_y and θ_z are the initial phases. The phasor representation of the B-field at point P is

$$\begin{bmatrix} \mathbf{B}_x \\ \mathbf{B}_y \\ \mathbf{B}_z \end{bmatrix} = \begin{bmatrix} \frac{B_x^m}{\sqrt{2}} / \theta_x \\ \frac{B_y^m}{\sqrt{2}} / \theta_y \\ \frac{B_z^m}{\sqrt{2}} / \theta_z \end{bmatrix} = \begin{bmatrix} \sum_{i=1}^m \sum_{j=1}^n \mathbf{B}_x|_{i,j} \\ \sum_{i=1}^m \sum_{j=1}^n \mathbf{B}_y|_{i,j} \\ \sum_{i=1}^m \sum_{j=1}^n \mathbf{B}_z|_{i,j} \end{bmatrix}. \quad (7)$$

The B-field ADFs in three directions are calculated and give in (8) at the bottom of this page. As shown in the three equations, B_x^m , B_y^m , and B_z^m are jointly determined by the ADFs $B_{\{i,j\}}^m$ and initial phase $\theta_{i,j}$ of all the individual Tx coils. It should be noted that (8) has no time-related variables. This advantage makes it convenient to check the B-field strength in different 3D positions and thus the actual magnetic field shaping effect [see Figs. 9 and 10 in Section IV].

$$\begin{bmatrix} B_x^m \\ B_y^m \\ B_z^m \end{bmatrix} = \begin{bmatrix} \left\{ \left[\sum_{i=1}^m \sum_{j=1}^n B_x^m|_{i,j} \cos(\theta_{i,j}) \right]^2 + \left[\sum_{i=1}^m \sum_{j=1}^n B_x^m|_{i,j} \sin(\theta_{i,j}) \right]^2 \right\}^{\frac{1}{2}} \\ \left\{ \left[\sum_{i=1}^m \sum_{j=1}^n B_y^m|_{i,j} \cos(\theta_{i,j}) \right]^2 + \left[\sum_{i=1}^m \sum_{j=1}^n B_y^m|_{i,j} \sin(\theta_{i,j}) \right]^2 \right\}^{\frac{1}{2}} \\ \left\{ \left[\sum_{i=1}^m \sum_{j=1}^n B_z^m|_{i,j} \cos(\theta_{i,j}) \right]^2 + \left[\sum_{i=1}^m \sum_{j=1}^n B_z^m|_{i,j} \sin(\theta_{i,j}) \right]^2 \right\}^{\frac{1}{2}} \end{bmatrix} \quad (8)$$

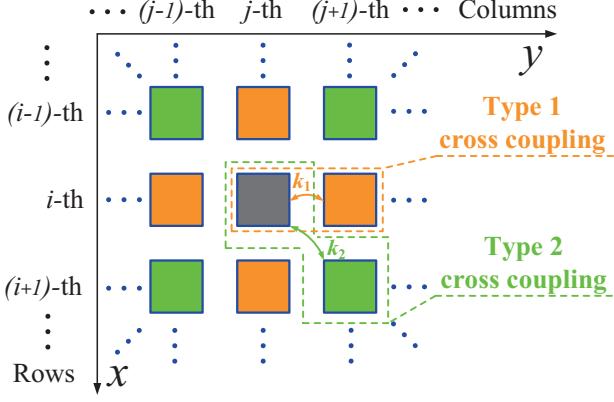


Fig. 4. Two types of cross coupling in a planar Tx-coil array.

III. CROSS COUPLING AND ITS MINIMIZATION

A. Analysis and Modeling

In the planar Tx-coil array, each Tx coil may actually act as an Rx coil to other Tx coils when these coils are cross-coupled. This unique nature, i.e., the cross coupling between the Tx coils, may

- 1) reduce the power that is supposed to be fed into the receiver, which is certainly unfavorable for overall system performance such as efficiency [23];
- 2) impact and complicate the operation of PAs because the cross coupling makes each PA see the impedance reflected by other transmitters. This reflected impedance may also significantly change with different phases of the coil currents [24].
- 3) pose a severe challenge to effective shaping of the final magnetic field [25].

As discussed in next subsection, this cross coupling between the Tx-coils can be properly managed by designing the distance d between the Tx coils [see Fig. 1].

Fig. 4 shows two types of cross coupling in a planar Tx-coil array. k_1 is defined to represent the cross coupling coefficient between two adjacent coils in the same row or column (e.g., gray and orange coils), while k_2 represents the cross coupling coefficient between two adjacent coils in next different row and column (e.g., gray and green coils). Note that only cross-coupling of adjacent coils is considered because the cross-

coupling between other Tx coils is usually negligible [26]. Based on Fig. 4, the mutual inductances of the two types of Tx-coil pairs, M_1 and M_2 , are

$$\frac{\Phi_{i,j-1}}{I_{i,j}} = \frac{\Phi_{i,j+1}}{I_{i,j}} = \frac{\Phi_{i-1,j}}{I_{i,j}} = \frac{\Phi_{i+1,j}}{I_{i,j}} = M_1, \quad (9)$$

$$\frac{\Phi_{i-1,j-1}}{I_{i,j}} = \frac{\Phi_{i+1,j-1}}{I_{i,j}} = \frac{\Phi_{i-1,j+1}}{I_{i,j}} = \frac{\Phi_{i+1,j+1}}{I_{i,j}} = M_2, \quad (10)$$

where $I_{i,j}$ is the current of $Tx_{i,j}$, and Φ 's are the flux linkages. For example, the flux linkage of $Tx_{i,j+1}$, namely $\Phi_{i,j+1}$, can be derived as [refer to Table VI in Appendix]

$$\Phi_{i,j+1}(N_{tx}, d, l) = N_{tx} \iint_{S_{i,j+1}} \lim_{z \rightarrow 0} B_z|_{i,j} dx dy, \quad (11)$$

where N_{tx} is again coil turns and $S_{i,j+1}$ is coil area. For the sake of simplicity, here each coil is assumed to have the same area. Similarly, the maximum values of M_1 and M_2 can also be represented as

$$M_1^{\max} = M_2^{\max} = \frac{\Phi_{i,j}(N_{tx}, d, l)}{I_{i,j}}. \quad (12)$$

From the above equations, the two cross coupling coefficients, k_1 and k_2 , can be calculated as

$$k_1 = \frac{M_1}{M_1^{\max}}, \quad k_2 = \frac{M_2}{M_2^{\max}}. \quad (13)$$

B. Minimization via Overlap Design

Fig. 5(a) shows the relationship between k_1 and d . The calculation results are in good agreement with the simulation results obtained by the High-Frequency Structure Simulator (HFSS). Note that the coil model in HFSS is the same as the actual PCB model [see Fig. 12]. In calculation, the side length l of the coils is 9 cm, which is equal to the average length of each turn in the simulation model. Interestingly, there is an overlap distance (i.e., a negative d) corresponding to the same amount of positive and negative magnetic field fluxes. This overlap distance largely decouples the two Tx coils, namely close-to-zero cross coupling. Similar results can be seen in Fig. 5(b) too (k_2 versus d). It is because that based on the right-hand rule, the direction of the magnetic flux

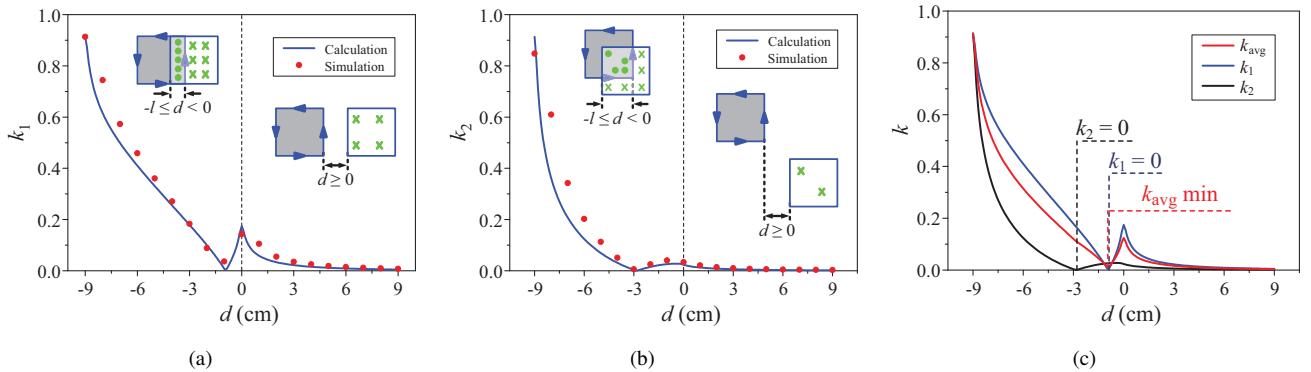


Fig. 5. Cross coupling coefficients k_1 and k_2 versus Tx-coil distance d (coil length $l = 9$ cm). (a) k_1 . (b) k_2 . (c) k_1 , k_2 and k_{avg} in a 2×2 Tx-coil array.

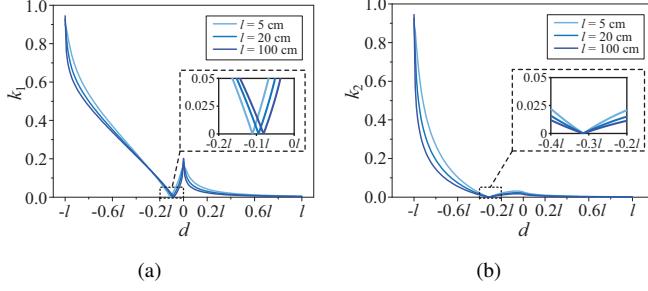


Fig. 6. Cross coupling coefficients versus different d and l . (a) k_1 . (b) k_2 .

inside and outside a coil is opposite. Therefore, there exists an overlap area to cancel the cross coupling between adjacent Tx coils.

The two overlap distances that make k_1 and k_2 equal to zero are not the same. The sum of all cross-coupling coefficients (k_1 's and k_2 's) of the Tx-coil array ($m \times n$ coils) is

$$k_{\text{sum}} = (2mn - m - n)k_1 + 2(m - 1)(n - 1)k_2. \quad (14)$$

Then, an average cross coupling coefficient can be defined to guide the design of d ,

$$k_{\text{avg}} = \frac{k_{\text{sum}}}{4mn - 3m - 3n + 2}, \quad (15)$$

in which the denominator is the total number of the two types of cross coupling in the Tx-coil array. Fig. 5(c) shows a comparison of k_1 , k_2 and k_{avg} in a 2×2 Tx-coil array. The Tx-coil distance d that minimizes k_{avg} is close to the distance that minimizes k_1 , because k_1 changes more drastically with d than k_2 .

Fig. 6(a) and Fig. 6(b) show k_1 and k_2 under different d and l . Despite slight differences, d 's that minimize k_1 and k_2 are almost in the same proportion as l 's. The optimal value of d that minimizes the dominant k_1 can be further fine-tuned using detailed HFSS coil models, as shown in Fig. 7(a). In the above calculation, the optimal k_1 is -1.11 cm [see Fig. 5(c)]. In all the cases in Fig. 7(b)–(e), the average length of each turn l is the same as that calculated above, i.e., 9 cm. As shown in these subfigures, the optimal d 's under different coil turns, trace width, and trace spacing are close with a maximum deviation of 0.2 cm. Note that Fig. 7(e) shows that the optimal d 's under different operating frequencies (f) are identical. It is because f does not impact the 3D magnetic field distribution; f only affects the changing ratio of the magnetic field [refer to Table VI]. Therefore, the optimal overlap design can be conducted through the combination of calculation and HFSS-based simulation:

- 1) calculate theoretically the optimal d using (9) – (15);
- 2) further fine-tune and finalize the optimal d using the detailed HFSS coil models.

For reference purposes, the relationship between overlap distance d_s and cross coupling coefficient k_s is also investigated for spiral coils, as shown in Fig. 8. A similar trend can be observed, and there is a specific d_s to respectively minimize the cross coupling in both pairs of spiral coils.

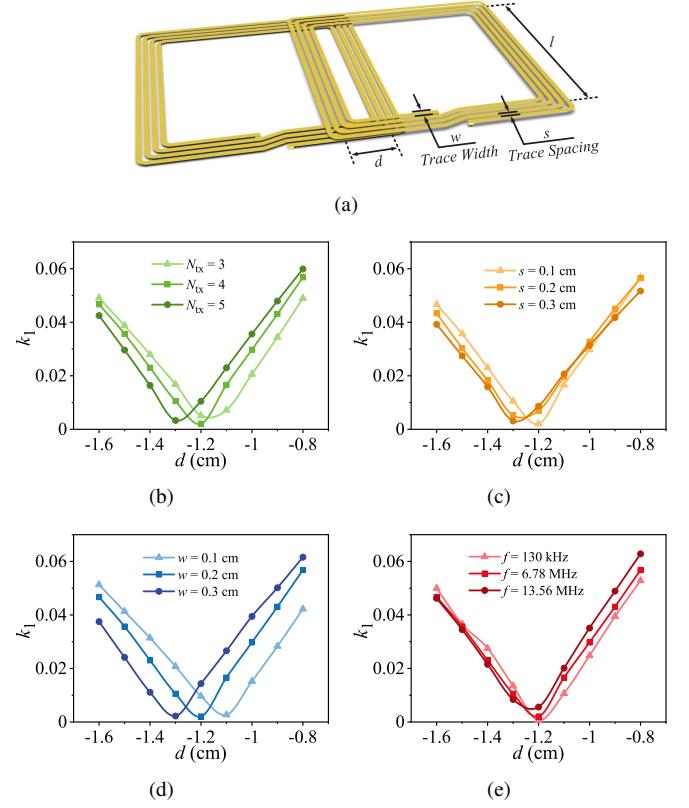


Fig. 7. k_1 versus d through the HFSS simulation. (a) Coil model. (b) Different N_{tx} ($l = 9$ cm, $s = 0.1$ cm, $w = 0.2$ cm, and $f = 6.78$ MHz). (c) Different s ($l = 9$ cm, $N_{\text{tx}} = 4$, $w = 0.2$ cm, and $f = 6.78$ MHz). (d) Different w ($l = 9$ cm, $N_{\text{tx}} = 4$, $s = 0.1$ cm, and $f = 6.78$ MHz). (e) Different f ($l = 9$ cm, $N_{\text{tx}} = 4$, $s = 0.1$ cm, and $w = 0.2$ cm).

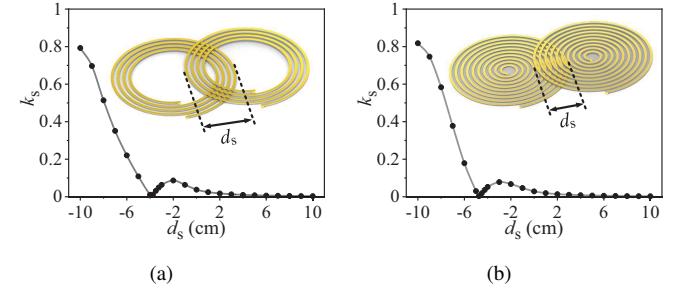


Fig. 8. Cross coupling coefficient versus d_s in spiral coils (10 cm diameter). (a) 4 turns. (b) 10 turns (a coil pattern exists in the center).

IV. MAGNETIC FIELD SHAPING EFFECTS

Fig. 9 and Fig. 10 show magnetic field shaping effects in xy plane and yz plane, taking a 2×2 Tx-coil array as an example. Compared with 3D figures, these 2D figures with B-field amplitude distribution more clearly demonstrate the shaping effects. Here the operating frequency is 6.78 MHz. The currents in the Tx coils have the same amplitude but different phases (i.e., phase shift modulation). The side length of all coils l is 10 cm, and the coil distance d is -1.24 cm to minimize the cross coupling. As a preliminary study, the magnetic field shaping effects are individually verified with phases of 0, 90, 180, 270 degrees in the Tx coils. The combinations of phases in Figs 9 and 10 are especially selected to show an obvious magnetic field shaping effect.

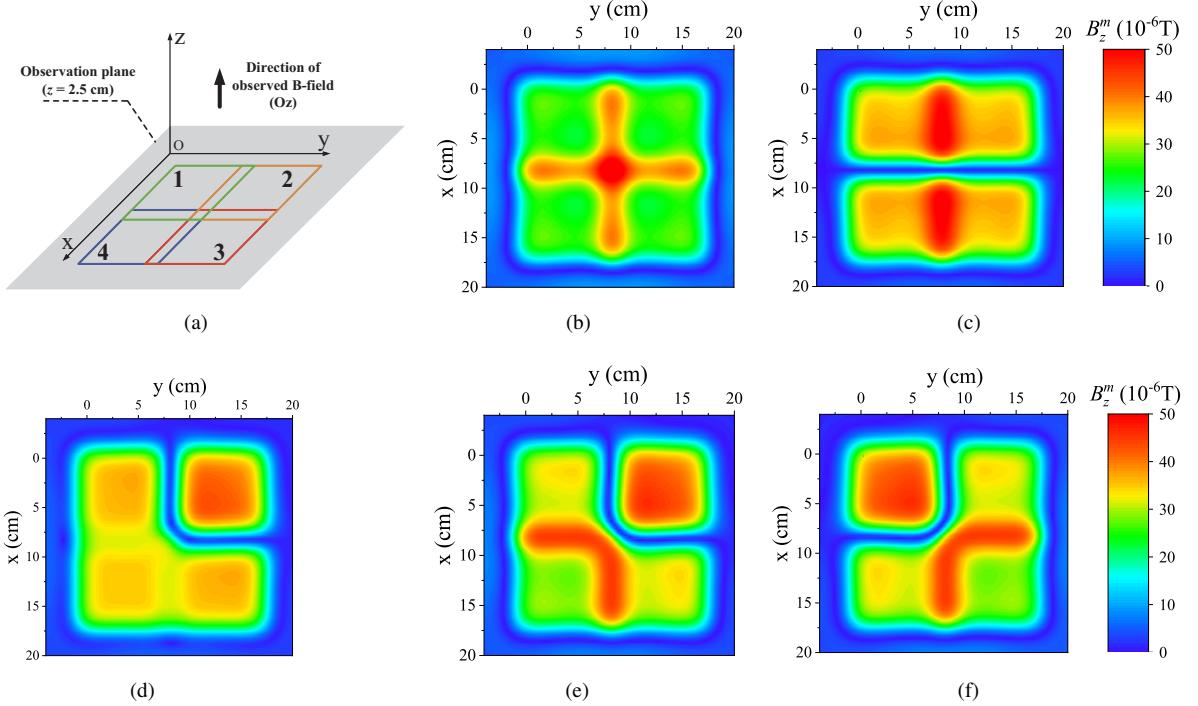


Fig. 9. Calculation results of B-field ADFs generated by a 2×2 planar Tx-coil array ($z=2.5 \text{ cm}$). (a) Layout and coordinates. (b) $\theta_1 = 0^\circ$, $\theta_2 = 0^\circ$, $\theta_3 = 0^\circ$ and $\theta_4 = 0^\circ$. (c) $\theta_1 = 0^\circ$, $\theta_2 = 0^\circ$, $\theta_3 = -180^\circ$ and $\theta_4 = -180^\circ$. (d) $\theta_1 = -180^\circ$, $\theta_2 = 0^\circ$, $\theta_3 = -180^\circ$ and $\theta_4 = -90^\circ$. (e) $\theta_1 = -180^\circ$, $\theta_2 = 0^\circ$, $\theta_3 = -180^\circ$ and $\theta_4 = -180^\circ$. (f) $\theta_1 = 180^\circ$, $\theta_2 = 0^\circ$, $\theta_3 = 0^\circ$ and $\theta_4 = 0^\circ$.

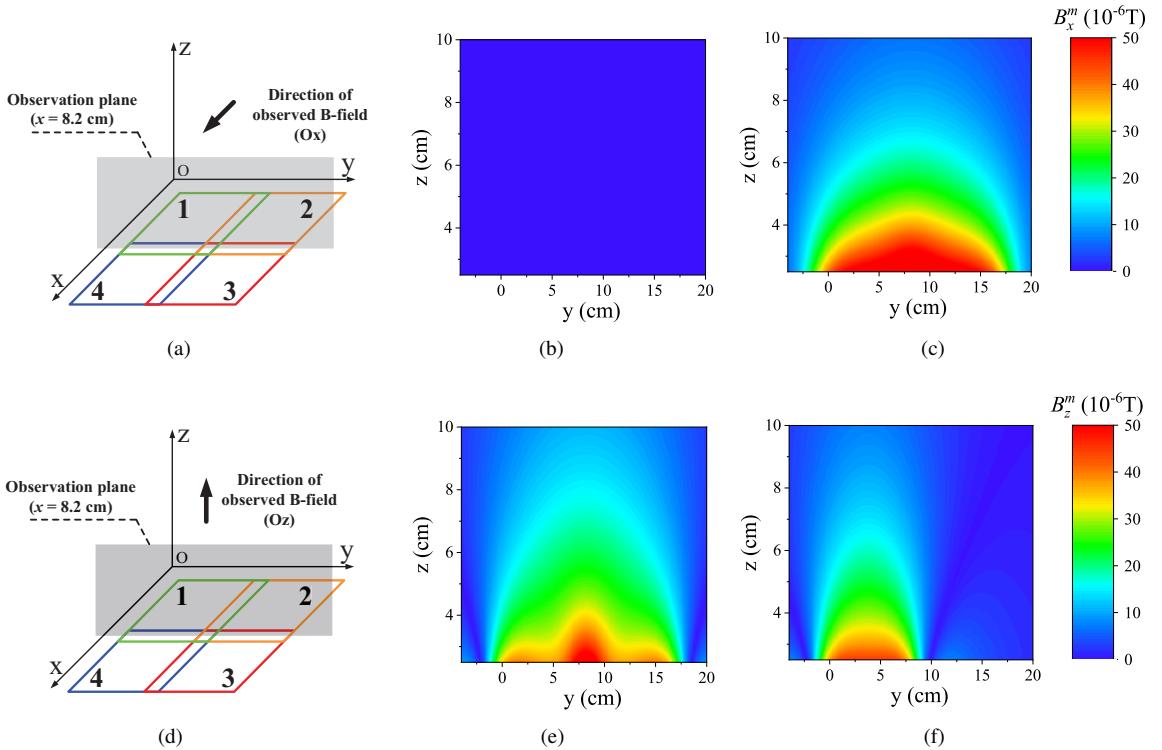


Fig. 10. Calculation results of B-field ADFs generated by a 2×2 planar Tx-coil array ($x=8.2 \text{ cm}$). (a) Layout and coordinates for Fig. 10(b) and Fig. 10(c). (b) $\theta_1 = 0^\circ$, $\theta_2 = 0^\circ$, $\theta_3 = 0^\circ$, and $\theta_4 = 0^\circ$. (c) $\theta_1 = 0^\circ$, $\theta_2 = 0^\circ$, $\theta_3 = 180^\circ$, and $\theta_4 = 180^\circ$. (d) Layout and coordinates for Fig. 10(e) and Fig. 10(f). (e) $\theta_1 = 0^\circ$, $\theta_2 = 0^\circ$, $\theta_3 = 0^\circ$, and $\theta_4 = 0^\circ$. (f) $\theta_1 = 0^\circ$, $\theta_2 = 0^\circ$, $\theta_3 = 180^\circ$, and $\theta_4 = 0^\circ$.

As shown in Fig. 9(b), if there is no phase difference in the Tx-coil currents, the z -direction B-field amplitude distribution on the xy plane (i.e., B_z^m) has its peak at the center of the

observation plane ($z=2.5 \text{ cm}$). If the phase shift is applied, such as in Fig. 9(c), the peak in the xy plane will be split into two peaks along the x axis and be actually further

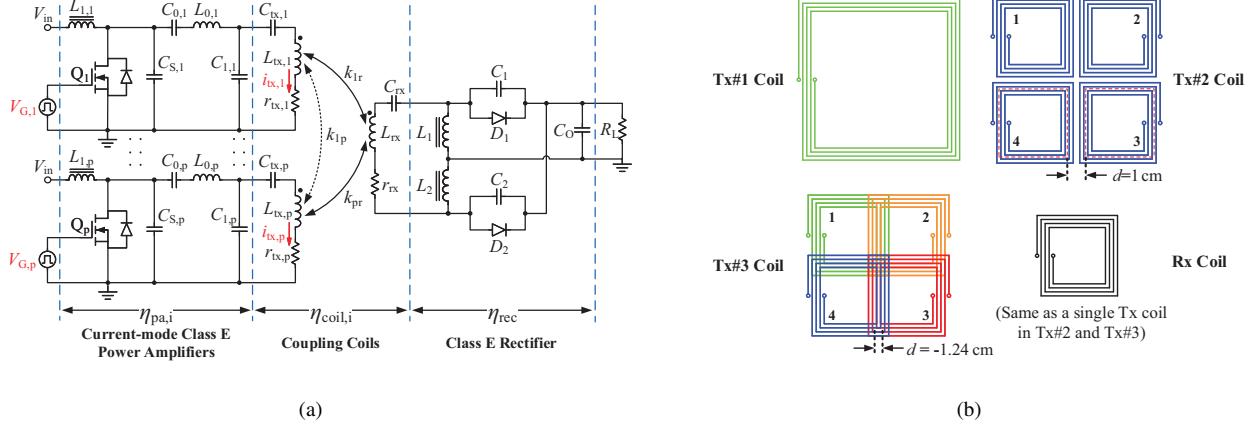


Fig. 11. A 6.78 MHz WPT system with an extendable planar Tx-coil array. (a) Circuit model. (b) Tx coils (#1–3) and Rx coil.

strengthened. Note that the peak can also appear above the non-overlap areas, such as shown in Fig. 9(d). These figures, namely Fig. 9(b)–Fig. 9(d), demonstrate the possibility of controlling the z -direction magnetic field distribution over the xy plane by changing the phases of the Tx-coil currents. This new capability can be utilized to enhance the adaptability of the power transfer to the horizontal misalignment (i.e., over the xy plane) of an Rx coil, as experimentally verified in the following Section V. Fig. 9(e) and Fig. 9(f) further show that the two peaks of the B-field distribution can actually rotate over the xy plane through the coil current phase shift modulation, which proves an additional degree of freedom in the magnetic field shaping.

Similarly, Fig. 10(b) and Fig. 10(c) show the magnetic field shaping effect in x direction over yz plane, namely B_x^m ($x=8.2\text{ cm}$). Both the B-field strength and distribution can be adjusted through the Tx current phase shift modulation. As shown in Fig. 10(c), unlike the conventional signal Tx-coil transmitter, the planar Tx-coil array is able to transfer power to an Rx coil that is perpendicular to the plane of the transmitter. Similar results can be seen in Fig. 10(e) and Fig. 10(f), which show the effect in z direction, namely B_z^m ($x=8.2\text{ cm}$). All the above calculation results indicate a promising aspect of the planar (i.e., 2D) Tx-coil array-based magnetic field shaping, namely the controllable magnetic field distribution in 3D space. This advantage will significantly improve the adaptability of WPT to receivers with 3D positions and orientations in actual environments.

V. EXPERIMENTAL IMPLEMENTATION

A. Configuration and Setup

Fig. 11(a) shows the circuit model of an example WPT system with an extendable planar Tx-coil array and a receiver. The transmitter includes multiple Class E PAs operating at 6.78 MHz to separately drive their corresponding Tx coils. And the receiving side consists of an Rx coil and a Class E full-wave rectifier. The phase shift between the drive signals of the PAs is modulated to generate Tx-coil currents with

different phases. In the present experimental system, there are four PAs and four Tx coils.

Fig. 11(b) shows three types of Tx coils for comparison purposes.

- 1) Tx#1: Single large Tx coil;
- 2) Tx#2: 2×2 Tx-coil array without overlap;
- 3) Tx#3: 2×2 Tx-coil array with overlap to minimize the average cross coupling k_{avg} .

The final experimental 6.78 MHz WPT system in Fig. 12 employs the same configuration in Fig. 11. The PA switches

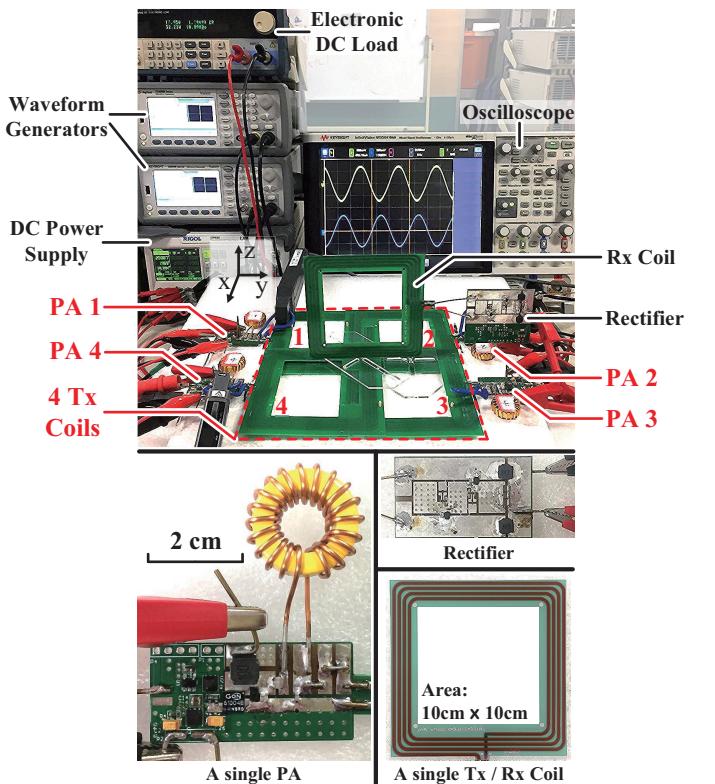


Fig. 12. Final experimental 6.78-MHz WPT system employing the proposed extendable planar Tx-coil array.

Q_{1-4} use GaN transistors (GS61004B). A 10Ω dc load is emulated using an electronic load. Two waveform generators are utilized to generate four-channel phase shifted PA driving signals. In actual scenarios, both FPGA and dedicated phase delay ICs can be applied to implement the phase shift modulation [27], [28]. Note that in Fig. 12, the Rx coil is perpendicular to the Tx-coil array. All the parameters of the three types of Tx PCB coils are listed in Table I. The quality factor of Tx#1 is much lower because the coil parasitic resistance grows faster than inductance when the coil size increases. In Tx#3, the distance d between adjacent Tx coils is determined to minimize the coil cross coupling [refer to Section III-B]. For the sake of simplicity, the Rx coil is as same as a single Tx coil in Tx#2 and Tx#3.

TABLE I
MAJOR PARAMETERS OF THREE TYPES OF TX COILS (6.78 MHz).

| Parameters | Tx#1 | Tx#2 | Tx#3 |
|-----------------------------------|--------------------|--------------------|--------------------|
| Inductance (μ H) | 10.76 | 3.32 | 3.32 |
| Parasitic resistance (Ω) | 3.96 | 0.61 | 0.61 |
| Quality factor | 115.8 | 231.9 | 231.9 |
| Coil array area (cm^2) | 20.0×20.0 | 20.0×20.0 | 17.8×17.8 |
| Coil distance d (cm) | n/a | 1 | -1.24 |
| Number of coils | 1 | 4 | 4 |
| Number of turns | 4 | 4 | 4 |
| Coil trace width (cm) | 0.2 | 0.2 | 0.2 |
| Coils trace spacing (cm) | 0.1 | 0.1 | 0.1 |
| Coils trace thickness (cm) | 0.007 | 0.007 | 0.007 |

Table II lists the measured cross coupling coefficients in the two Tx-coil arrays (Tx#2,3). Consistent with the above analysis via Fig. 5, the type 1 cross coupling (k_1) is dominant and can be dramatically reduced by the optimized Tx-coil overlap design ($d=-1.24$ cm). This leads to a largely minimized average cross coupling coefficient k_{avg} (68.1% reduction). It is known that a reflected impedance seen by an individual Tx coil is proportional to the square of the cross coupling coefficient [7]. For Tx#3 array, the mutual interference among the coils is much smaller than that in Tx#2 array, which helps improve the loading condition of the current-mode Class E PAs. Note that in the present overlap design, k_2 's are actually increased to reduce the more dominant k_1 's.

TABLE II
MEASUREMENT RESULTS OF TX-COIL CROSS COUPLING.

| Tx-coil pair / k_{avg} | Cross coupling type | Tx#2 | Tx#3 |
|---------------------------------|---------------------|-------|-------|
| No. 1 – No. 2 | Type 1 | 0.094 | 0.010 |
| No. 1 – No. 3 | Type 2 | 0.020 | 0.048 |
| No. 1 – No. 4 | Type 1 | 0.092 | 0.006 |
| No. 2 – No. 3 | Type 1 | 0.092 | 0.013 |
| No. 2 – No. 4 | Type 2 | 0.020 | 0.044 |
| No. 3 – No. 4 | Type 1 | 0.094 | 0.009 |
| k_{avg} | n/a | 0.069 | 0.022 |

B. PA Parameter Selection

Thanks to the matching network design (T-type here) developed in Ref. [29], the Class E PAs are possible to maintain

an almost constant output current amplitude (i.e., current-mode) when there are variations in their load impedance, such as due to changes in the position and orientation of the Rx coil [see Fig. 11(a)]. The target variation range of PA load impedance can be first determined by experimental testing. Then, as mentioned in Ref. [29], the classical Class E PA can be designed targeting an intermediate dc load (22Ω here), and the parameters of the T-type matching network are accordingly optimized to transform the varying load impedance to the PA high-efficiency region.

Table III lists the parameters of the PAs that drive Tx#1–3. Note that the two inductors of the T-type matching network are absorbed by L_0 and L_{tx} , respectively. The four PAs for Tx#2 and Tx#3 share the same set of parameters. Because of inevitable manufacturing errors, the combinations of L_0 and C_0 of the PAs are slightly different. In the Tx#2 case, the strong cross coupling between the Tx coils (i.e., without the overlap design) further complicates the loading condition during the phase shift modulation, which makes the PA parameter design especially difficult [24]. As an example, Fig. 13 shows the trajectories of the PA load impedance Z_{PA} when θ_1 and θ_2 are 0, and θ_3 and θ_4 change from 0 to 360 degrees. Here η_{PA} is the efficiency of a single PA. The range of the PA load impedance variation is significantly suppressed with the overlap design (i.e., the case of Tx#3). This certainly helps alleviate the difficulty in PA parameter selection. It again indicates the importance of the overlap design of the Tx-coil array.

TABLE III
PA PARAMETERS FOR TX#1–3.

| | L_1 (μ H) | C_s (pF) | C_0 (pF) | L_0 (μ H) | C_1 (pF) | C_{tx} (pF) |
|-------------------|---------------------|---------------|---------------|---------------------|---------------|-------------------------|
| Tx#1 | 10 | 76 | 938 | 1.793 | 560 | 52 |
| Tx#2 & Tx#3 | 10 | 76 | 760 (PA1) | 1.930 (PA1) | | |
| | | | 751 (PA2) | 1.939 (PA2) | 560 | 182 |
| | | | 750 (PA3) | 1.940 (PA3) | | |
| | | | 774 (PA4) | 1.918 (PA4) | | |

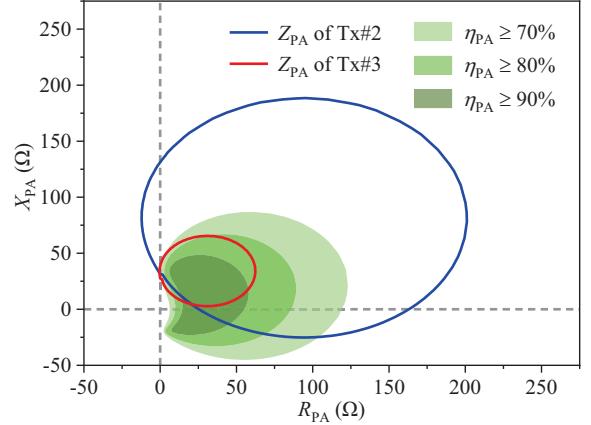


Fig. 13. Example PA load impedance trajectories ($\theta_1=\theta_2=0$, θ_3 and θ_4 are from 0 to 360 degrees).

C. Visualization of Magnetic Field Shaping

To visualize the B-field strength distribution, an LED array with 25 receiving modules is built up. As shown in Fig. 14, each receiving module is $2.5 \text{ cm} \times 2.5 \text{ cm}$, and the entire LED array is $20 \text{ cm} \times 20 \text{ cm}$. The supporting acrylic frame can fix the LED array in different positions and orientations through magnetic docking. Note that the lightness of the LEDs has a nonlinear relationship with the B-field strength.

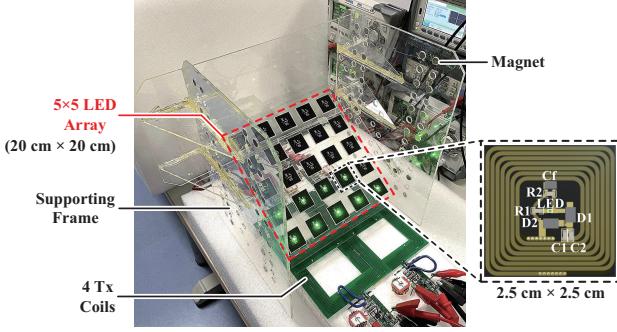


Fig. 14. An LED array to visualize the magnetic field shaping.

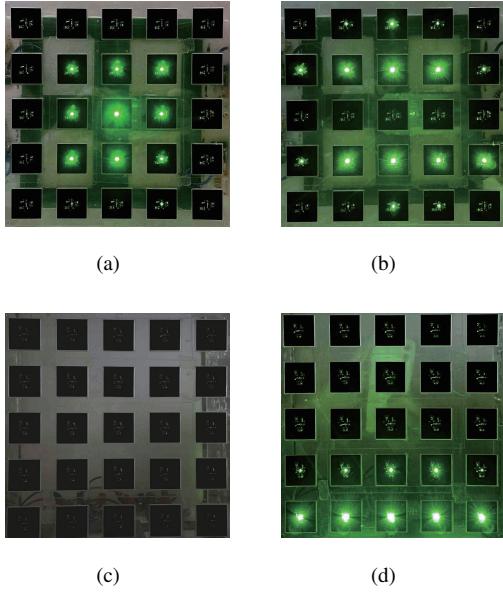


Fig. 15. Illumination of the LED array in horizontal and perpendicular orientations. (a) Visualization corresponding to Fig. 9(b) (horizontal). (b) Visualization corresponding to Fig. 9(c) (horizontal). (c) Visualization corresponding to Fig. 10(b) (perpendicular). (d) Visualization corresponding to Fig. 10(c) (perpendicular).

The four sub-figures in Fig. 15 correspondingly verify the calculation results in Fig. 9(b), Fig. 9(c), Fig. 10(b), and Fig. 10(c). The visualization results well match with their calculation results. Meanwhile, it is natural that there are minor differences, mostly due to the limited number of LED modules and nonlinearity between LED lightness and B-field strength. The above LED array is a convenient tool to directly visualize and confirm the actual magnetic field shaping effect.

D. Rx Coil with Six Degrees of Freedom

Fig. 16 and Fig. 17 show the measured output dc power and dc-dc efficiency using Tx#1, Tx#2 and Tx#3. Note that Tx#2 and Tx#3 are the planar Tx-coil arrays without and with overlap, respectively. Experiments are conducted to investigate the performance when the Rx coil is in six-degrees-of-freedom positions and orientations (i.e., x , y , z , α , β and γ). Due to the symmetry in (x , y) and (α , β), their results are similar. To avoid redundancy, only the results for x , z , α , and γ cases are shown in the two figures. The input dc voltages of the three systems are all 20 V, and the driving signal phases of the four PAs (θ_1 - θ_4) are accordingly modulated to investigate the magnetic field shaping effects.

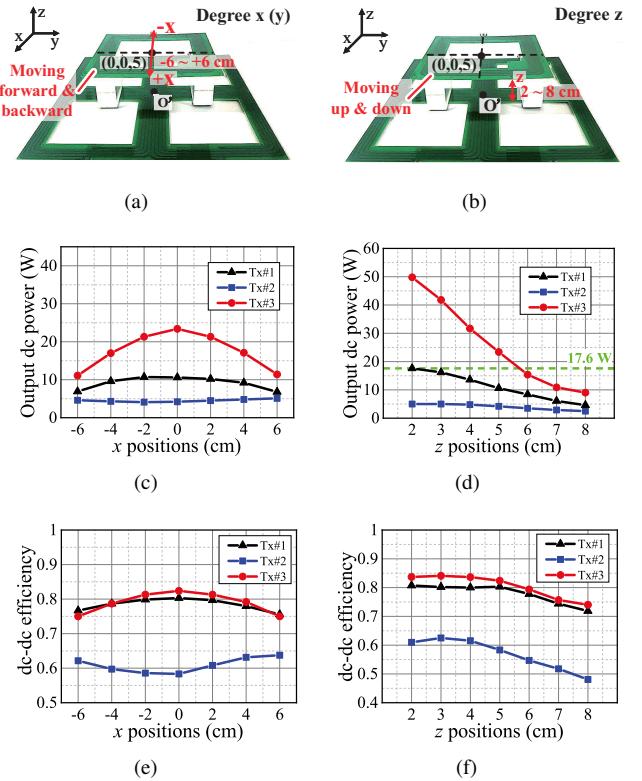


Fig. 16. Experimental results in different x and z positions using Tx#1, Tx#2 and Tx#3. (a) Setup (x positions). (b) Setup (z positions). (c) Output power (x positions). (d) Output power (z positions). (e) Dc-dc efficiency (x positions). (f) Dc-dc efficiency (z positions).

For the case of a moving Rx coil in x direction ($\pm 6 \text{ cm}$), symmetrically placed Tx coils, (no. 1, no. 2) and (no. 3, no. 4), should have the same phase [see Fig. 12]. Therefore, here θ_3 and θ_4 are fixed to 0° , and θ_1 and θ_2 are tuned to change from -180° to 180° . For the movement of Rx in other directions, a similar principle is applied. Fig. 16(c) shows that the output power using the Tx#3 (i.e., the case with the overlap design) is obviously much higher than those using Tx#1 and Tx#2, while Tx#1 (i.e., a single Tx coil) and Tx#3 demonstrate the similar dc-dc efficiency. In Fig. 16(e), the efficiency in Tx#3 case is extraordinary high when comparing with the Tx#2 case (i.e., the case without coil overlap). The above results clearly show the importance of the overlap design for a high-performance MHz WPT system using the planar Tx-coil array. Otherwise, a

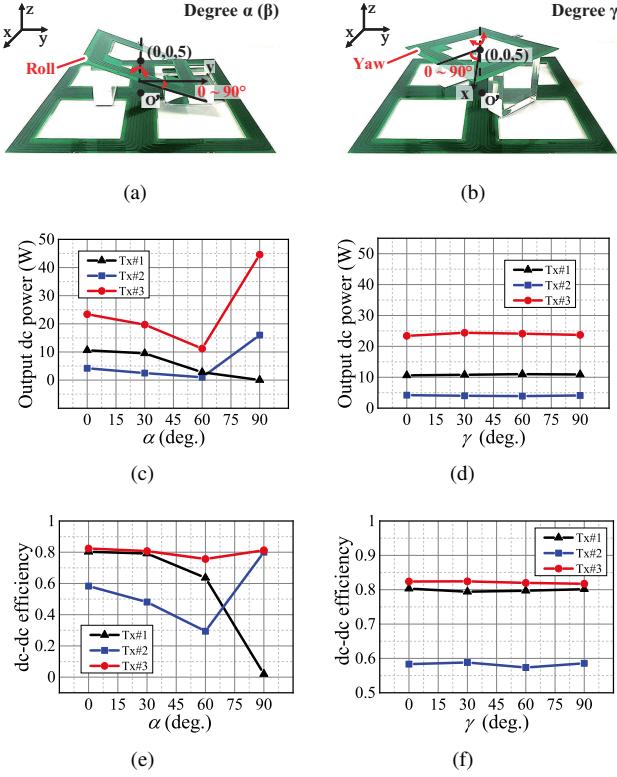


Fig. 17. Experimental results in different α and γ angles using Tx#1, Tx#2 and Tx#3. (a) Setup (α angles). (b) Setup (γ angles). (c) Output power (α angles). (d) Output power (γ angles). (e) Dc-dc efficiency (α angles). (f) Dc-dc efficiency (γ angles).

large amount of power will be transferred among the Tx coils due to the cross coupling, which causes the lowest efficiency and output power in the Tx#2 case. Similarly, the Tx#3 coil array also demonstrated the best performance when the Rx coil moves along the z axis [see Fig. 16(b)(d)(f)]. The Tx#3 WPT system can achieve an 84% dc-dc efficiency at 50 W. It can maintain the same output power 17.6 W as the maximum output power of the single Tx-coil WPT system (i.e., Tx#1) but with a much longer transfer distance, about 6 cm versus 2 cm. Note that in the present scenario, the Rx coil moves vertically in the center. Thus phases $\theta_1-\theta_4$ are all zero [see Fig. 10(e)].

Fig. 17 shows the results when the Rx coil rotates in α and γ angles, i.e., with different orientations. Again, the results in β angles are omitted due to their similarity with the results in α angles. For the case of α angles ($\alpha = 0 - 90^\circ$), θ_2 and θ_3 are changed from 0° to -180° , while θ_1 and θ_4 are fixed to 0° . The results using the Tx#3 coil array, namely Fig. 17(c) and Fig. 17(e), demonstrate consistently the best performance, both in output power and efficiency. It is especially promising to notice that even when the Rx coil is perpendicular to the Tx coil array (i.e., $\alpha = 90^\circ$), 45 W output power and 82% dc-dc efficiency can still be achieved. Meanwhile, the conventional single Tx coil (i.e., Tx#1) becomes completely unfunctional in such an extreme case because no magnetic flux will pass through the Rx coil. Note that the efficiency of the Tx#2 case is also high when the Rx coil is perpendicular [see Fig. 17(e)].

This is mainly because that the PAs happenly see a suitable impedance reflected by other transmitters. The planar Tx-coil array, overlap design and phase shift modulation work together to provide new degrees of freedom in magnetic field shaping. The results using the Tx#3 coil arrays in γ angles are also superior in both output power and efficiency [see Fig. 17(d) and Fig. 17(f)].

TABLE IV
ADDITIONAL FOUR SCENES (TX#3-COIL ARRAY).

| Scenes | Rx Positions/Orientations | Specs and Results |
|--------|--|--|
| | An eccentric perpendicular Rx | $\eta_{dc-dc} = 77.1\%$ $R_L = 10 \Omega$ $P_{out} = 22.2 \text{ W}$ |
| | A randomly placed Rx | $\eta_{dc-dc} = 78.4\%$ $R_L = 10 \Omega$ $P_{out} = 16.3 \text{ W}$ |
| | A perpendicular Rx and a horizontal Rx (Rx#1: red, Rx#2: yellow) | $\eta_{dc-dc} = 80.3\%$ $R_{L,1} = 10 \Omega$ $P_{out,1} = 20.4 \text{ W}$ $R_{L,2} = 5 \Omega$ $P_{out,2} = 14.7 \text{ W}$ |
| | Two horizontal Rxs (Rx#1: red, Rx#2: yellow) | $\eta_{dc-dc} = 81.4\%$ $R_{L,1} = 10 \Omega$ $P_{out,1} = 18.0 \text{ W}$ $R_{L,2} = 5 \Omega$ $P_{out,2} = 12.6 \text{ W}$ |

E. Further discussions

The results of additional four scenes are summarized in Table IV, using the optimally designed Tx#3-coil array to reduce the cross coupling between the Tx coils. Note that for clarity, the circuits (PAs, rectifiers, etc.) are not shown in the figures. Again, the results are promising in terms of efficiency and output power. Especially, in the third scene, the perpendicular Rx#1 and horizontal Rx#2 provide output powers of 20.4 W and 14.7 W, respectively. The overall dc-dc efficiency is as high as 80.3%. In actual scenarios, a perpendicular Rx can be convenient for the wireless charging of smart watches, headsets, hand-held cellphones, etc. In such applications, the charging surface of the mobile devices may be placed upright. All the above results indicate that in a wide range of new applications, a well-designed and controlled planar Tx-coil array could further improve the spatial freedom of today's WPT.

Fig. 18 shows the experimental current waveforms of the four Tx coils in Fig. 12, i.e., with a perpendicular Rx coil in the center. The phases of the driving signals are 0° , 0° , -180° , and -180° . Offsets are observed in the actual Tx current phases, as shown in Fig. 18. This is mainly because that the cross

TABLE V
COMPARISON OF WPT SYSTEMS WITH MAGNETIC FIELD SHAPING.

| Reference | 2014 [19] | 2016 [30] | 2018 [25] | 2020 [18] | 2021 [22] | This Work |
|-----------------------------|------------------|------------------|------------------|------------------|------------|--------------------------|
| Output Power | 3 W | 1.07 W | 13.7 W | 8 - 18 W | 3 - 15 W | 9 - 50 W |
| Efficiency | 50% - 60% | 69.5% | 28.2% | 60% - 65% | 60% - 70%* | 74% - 84%* |
| Operating Frequency | 530 kHz | 550 kHz | 20 kHz | 100 kHz | 6.78 MHz | 6.78 MHz |
| Spatial DoF of Rx | 3 | 3 | 3 | 3 | 6 | 6 |
| Tx-coil Structure | Spherical Shape | Spherical Shape | Cubic Shape | Spherical Shape | Bowl Shape | Extendable 2D Coil Array |
| Cross Coupling Minimization | Orthogonal Coils | Orthogonal Coils | Orthogonal Coils | Orthogonal Coils | - | Overlap Design |

* : dc-dc efficiency.

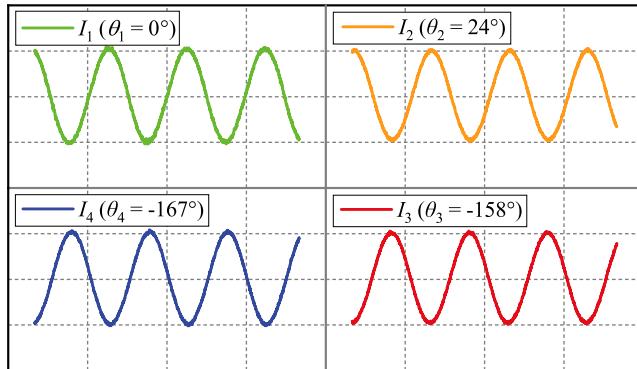


Fig. 18. Experimental current waveforms of the four Tx coils (0.7 A/div, 150 ns/div).

coupling is largely reduced, but is not completely eliminated. Meanwhile, the final MHz WPT system still performs well, as mentioned above. Further reduction of the cross coupling should be investigated in the future, and it is also possible to develop a feedback-based compensation scheme of the driving signals to eventually achieve accurate phase shift modulation of final Tx currents.

Finally, Table V summarizes the specifications and performance of state-of-the-art WPT systems with magnetic field shaping. As shown by the comparison, the developed system in this paper demonstrated improved power transfer capability and dc-dc efficiency at 6.78 MHz. Thanks to the proposed overlap design to minimize the cross coupling between the Tx coils, it becomes possible to realize effective 3D magnetic field shaping using an extendable 2D planar Tx-coil array.

VI. CONCLUSION

This paper studies the planar Tx-coil array architecture and current phase shift modulation technique to realize the magnetic field shaping in 3D space. The B-field amplitude distribution is analytically derived based on the Biot-Savart law and phasor representation. In order to reduce the interference to the PA operation, the influence of the cross coupling between the Tx coils is especially analyzed and minimized. Both the calculation and experimental results have well verified the effect of the magnetic field shaping under different current phases of individual Tx coils, and demonstrated significantly

improved spatial freedom of power transfer to receivers in different 3D positions and orientations.

Based on the above promising results, main future works may include 1) 3D position and orientation detection of Rx coils; 2) real-time phase shift modulation for power transfer to a moving receiver; 3) scheme and analysis of multiple-receiver power transfer in 3D space, etc. Especially, a “scan” mechanism can be developed to drive the Tx coils sequentially in a certain pattern. The different reflected impedances seen by the individual Tx coils could be utilized to reconstruct the 3D location and orientation of an Rx coil. The optimal phase shift in each Tx coil can then be calculated based on the derived B-field amplitude distribution functions (ADFs), following specific design targets such as maximizing power transfer efficiency and capability.

APPENDIX

The x -direction, y -direction and z -direction components of the B-field induced by $Tx_{i,j}$ at $P(x, y, z)$ are derived and listed in Table VI. Here $B_{\{\bullet\}|i,j}$ represents $B_x|_{i,j}$, $B_y|_{i,j}$ or $B_z|_{i,j}$.

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TABLE VI
X-, Y-, AND Z-DIRECTION COMPONENTS OF B-FIELD INDUCED BY $\text{Tx}_{i,j}$ COIL AT $P(x, y, z)$.

| \overline{B} | $B_{\{\bullet\}} _{i,j}$ | Derivation |
|----------------------|--------------------------|---|
| $\overline{B}_{i,j}$ | $B_x _{i,j}$ | $\frac{\mu_0 N_{tx} I_{i,j}^m \cos(\omega t + \theta_{i,j})}{4\pi} \left\{ \frac{z}{[j(d+l)-x]^2+z^2} \left\{ \frac{y-i(d+l)}{\{[j(d+l)-x]^2+[i(d+l)-y]^2+z^2\}^{\frac{1}{2}}} + \frac{i(d+l)-l-y}{\{[j(d+l)-x]^2+[i(d+l)-l-y]^2+z^2\}^{\frac{1}{2}}} \right\} + \right.$ $\left. \frac{z}{[j(d+l)-l-x]^2+z^2} \left\{ \frac{i(d+l)-y}{\{[j(d+l)-l-x]^2+[i(d+l)-y]^2+z^2\}^{\frac{1}{2}}} + \frac{-i(d+l)+l+y}{\{[j(d+l)-l-x]^2+[i(d+l)-l-y]^2+z^2\}^{\frac{1}{2}}} \right\} \right\}$ |
| $B_y _{i,j}$ | $B_y _{i,j}$ | $\frac{\mu_0 N_{tx} I_{i,j}^m \cos(\omega t + \theta_{i,j})}{4\pi} \left\{ \frac{-z}{[i(d+l)-y]^2+z^2} \left\{ \frac{j(d+l)-x}{\{[j(d+l)-x]^2+[i(d+l)-y]^2+z^2\}^{\frac{1}{2}}} + \frac{-j(d+l)+l+x}{\{[j(d+l)-l-x]^2+[i(d+l)-y]^2+z^2\}^{\frac{1}{2}}} \right\} + \right.$ $\left. \frac{z}{[i(d+l)-l-y]^2+z^2} \left\{ \frac{j(d+l)-x}{\{[j(d+l)-x]^2+[i(d+l)-l-y]^2+z^2\}^{\frac{1}{2}}} + \frac{-j(d+l)+l+x}{\{[j(d+l)-l-x]^2+[i(d+l)-l-y]^2+z^2\}^{\frac{1}{2}}} \right\} \right\}$ |
| $B_z _{i,j}$ | $B_z _{i,j}$ | $\frac{\mu_0 N_{tx} I_{i,j}^m \cos(\omega t + \theta_{i,j})}{4\pi} \left\{ \frac{y-i(d+l)}{[i(d+l)-y]^2+z^2} \left\{ \frac{j(d+l)-x}{\{[i(d+l)-y]^2+[j(d+l)-x]^2+z^2\}^{\frac{1}{2}}} + \frac{-j(d+l)+l+x}{\{[i(d+l)-y]^2+[j(d+l)-l-x]^2+z^2\}^{\frac{1}{2}}} \right\} + \right.$ $\left. \frac{j(d+l)-l-x}{[j(d+l)-l-x]^2+z^2} \left\{ \frac{i(d+l)-y}{\{[i(d+l)-y]^2+[j(d+l)-l-x]^2+z^2\}^{\frac{1}{2}}} + \frac{-i(d+l)+l+y}{\{[i(d+l)-l-y]^2+[j(d+l)-l-x]^2+z^2\}^{\frac{1}{2}}} \right\} - \right.$ $\left. \frac{j(d+l)-x}{[j(d+l)-x]^2+z^2} \left\{ \frac{i(d+l)-y}{\{[i(d+l)-y]^2+[j(d+l)-x]^2+z^2\}^{\frac{1}{2}}} + \frac{-i(d+l)+l+y}{\{[i(d+l)-l-y]^2+[j(d+l)-x]^2+z^2\}^{\frac{1}{2}}} \right\} - \right.$ $\left. \frac{-i(d+l)+l+y}{[i(d+l)-l-y]^2+z^2} \left\{ \frac{j(d+l)-x}{\{[i(d+l)-l-y]^2+[j(d+l)-x]^2+z^2\}^{\frac{1}{2}}} + \frac{-j(d+l)+l+x}{\{[i(d+l)-l-y]^2+[j(d+l)-l-x]^2+z^2\}^{\frac{1}{2}}} \right\} \right\}$ |

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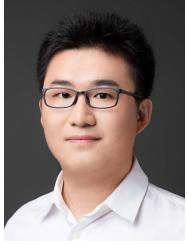
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