Python for scientific research Number crunching using NumPy/SciPy

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June 2017



Researcher Development



What we've done so far

- Declare variables using built-in data types and execute operations on them
- Use flow control commands to dictate the order in which commands are run and when
- 3 Encapsulate programs into reusable functions, modules and packages
- Next: Number crunching using NumPy/SciPy

- We are typically faced by numerical tasks, such as, computing Pearson's correlation coefficient or generating random numbers
- The NumPy (numeric python) package provides a comprehensive set of mathematical data structures (e.g vector, matrix) and functions (e.g trigonometry, random number generator)
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 - Signal processing (e.g Fourier transform, filtering)
 - Solving differential equations
 - Optimisation
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A taste of NumPy

```
import numpy as np
# 1D array/vector
x = np.array([1, 2, 3, 4])
x.min() # return min of array
x.max() # return max of array
x.sum() # sum all elements in array
# 2D array
x = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
x*x # element-by-element multiplication
x.shape # return dimensions of matrix
np.dot(x, x) # matrix multiplication
np.mat(x)*np.mat(x) # matrix multiplication (cast as matrix)
```

A taste of NumPy

```
# Generate random numbers
np.random.rand() # from a uniform distribution
np.random.randn() # from a normal distribution
np.random.randn(5, 5) # 5 x 5 matrix of random numbers

# Create number sequences
np.arange(0, 1, 0.1) # 0 to 1 in steps of 0.1
np.linspace(0, 1, 100) # 100 values between 0 and 1
np.logspace(0, 1, 10) # 10 values between 10°0 and 10°1
```

A taste of SciPy

```
import scipy.stats as sp
# Create two random arrays
x1 = np.random.randn(30)
x2 = np.random.randn(30)
# Correlation coefficientss
sp.pearsonr(x1, x2) # pearson correlation
sp.spearmanr(x1, x2) # spearman correlation
sp.kendalltau(x1, x2) # kendall correlation
# Statistical tests
sp.ttest_ind(x1, x2) # independent t-test
sp.mannwhitneyu(x1, x2) # Mann-Whitney rank test
sp.wilcoxon(x1, x2) # Wilcoxon signed-rank test
# Least-squares regression
sp.linregress(x1, x2)
```

Predator prey equations (Lotka Volterra)

$$\frac{\mathrm{d}u}{\mathrm{d}t} = \alpha u - \beta uv$$

$$\frac{\mathrm{d}v}{\mathrm{d}t} = -\gamma v + \delta u v$$

Where:

- u: is the number of prey (e.g rabbits)
- v: is the number of predators (e.g foxes)
- ullet α : prey growth rate in the absence of predators
- β : dying rate of prey due to predation
- ullet γ : dying rate of predators in the absence of prey
- δ : predator growth rate when consuming prey

Predator prey equations in Python

$$\frac{\mathrm{d}u}{\mathrm{d}t} = \alpha u - \beta u v$$

$$\frac{\mathrm{d}v}{\mathrm{d}t} = -\gamma v + \delta u v$$

```
def predator_prey(x, t):
    Predator prev model (Lotka Volterra)
    # Constants
    alpha = 1
    beta = 0.1
    gamma = 1.5
    delta = 0.075
    # x = [u, v] describes prey and predator populations
    u \cdot v = x
    # Define differential equation (u = x[0], v = x[1])
    du = alpha*u - beta*u*v
    dv = -gamma*v + delta*u*v
    return du, dv
```

Solve differential equations

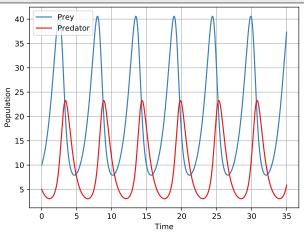
```
from scipy.integrate import odeint

time = np.linspace(0, 35, 1000) # time vector
init = [10, 5] # initial condition: 10 prey, 5 predators
x = odeint(predator_prey, init, time) # solve
```

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Fourier transform

```
from scipy.fftpack import fftfreq, fft

# Create frequency vector
N = len(time)
freq = fftfreq(N, np.mean(np.diff(time)))
freq = freq[range(int(N/2))]

# Compute Fast Fourier Transform
y = fft(x[:, 0])/N # compute and normalise fft
y = y[range(int(N/2))] # keep only positive frequencies
```

Fourier transform

