Survival Data Analysis for Cancer Data

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Introduction

In this book, there are my notes and exercises from the Ph.D. course on **Survival Data Analysis for Cancer Data** by Prof. Matthieu Resche-Rigon and Prof. Sylvie Chevret from ECSTRA Team, Inserm, University of Paris Diderot, promoted by the Dep. of Mathematical Sciences "G. L. Lagrange" of the Politecnico of Torino (Italy).

From the download button on the top of each (HTML) page you can download both the epub and the PDF versions of the present book.

Contributions

If you find any mistakes, typing errors or if you simply want to contribute, you have two main options:

- 1. Provide a solution proposal by opening a *pull request* to the related git repository (https://github.com/CorradoLanera/SuDACDa/pulls)
- 2. Ask me for a fix by opening an *issue* to the project (https://github.com/CorradoLanera/SuDACDa/issues)

Settings

Here, there are the libraries loaded during the course, with the relative options, plus some packages and options useful to write code more understandable by humans obtaining nicer output.

```
# Packages for the analyses
library(survival)
                                                              # Survival Analysis
library(survminer)
                                       # Drawing Survival Curves using 'ggplot2'
library(rms)
                                                   # Regression Modeling Strategy
  options(datadist = 'dd')
                                             # Distribution Summaries used by rms
# Packages for data management
                                       # Imports the principal tidyverse packages
library(tidyverse)
# Document output options
knitr::opts_chunk$set(
    echo
               = TRUE,
    message
              = FALSE,
             = FALSE,
    warning
    fig.height = 4.4
)
         # by default, render all the code too
```

6 CONTENTS

The following code create the packages.bib files which is the BibTeX lists of all the packages references we have loaded.

```
# Automatically create a bib database for the loaded packages
knitr::write_bib(c(.packages(), 'bookdown', 'knitr', 'rmarkdown'),
    file = 'packages.bib'
)
```

Chapter 1

Monday: Introduction to Survival Analyses and simulation of data

1.1 Simulated Data

- 1. Simulate a sample of n = 100 or 1000 exponential survival times, with mean $\theta = 5$.
- Non censored

```
n <- c(thousand = 1000) # samples
t <- rexp(n, rate = 5) # random exponential times
status_no_cens <- rep(1, times = n) # no censored data --> all are cases
```

• Uniform censoring over [0, a], with a = 1, a = 0.5 or a = 2

```
a <- c(cens_05 = 0.5) # upper bound of the uniform censoring dist

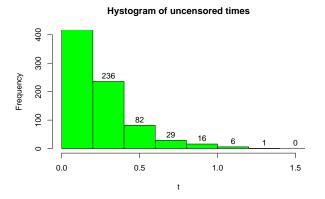
cens <- runif(n, min = 0, max = a) # censored times

t_cens <- pmin(t, cens) # censored times are earlier than event times

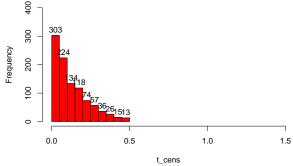
status_cens <- status_no_cens - (t_cens == cens) # remove censored cases
```

- 2. Plot the observed survival times
- Non censored and censored

```
# NOTE: for the plots to be comparable, xlim and ylim have to be the same range
        for both the plots. Moreover to drow well adjusted plots, they were set
#
        a posteriori.
hist(t,
  main = 'Hystogram of uncensored times',
  col = 'green',
 xlim = c(0, 1.5),
 ylim = c(0, 400),
  labels = TRUE
                                       # add the labels over the top of the bars
hist(t_cens,
 main = 'Hystogram of censored times (a = 0.5)',
  col = 'red',
 xlim = c(0, 1.5),
  ylim = c(0, 400),
 labels = TRUE
```



Hystogram of censored times (a = 0.5)



- 3. Parametric estimation of survival function
- Uncensored

```
`?survreg` := "Regression for a Parametric Survival Model"
#
# R formula: y \sim x <--> math formula: y = f(x)
# Here we want to model the response (labelled time) as they are, without any
\# furter investigation on the effect on them from some other variable
survreg(Surv(t, status_no_cens) ~ 1,
  dist = 'exponential'
) %>%
              # here `summary()` add some more statistics to the standard output
  summary
```

```
##
## Call:
## survreg(formula = Surv(t, status_no_cens) ~ 1, dist = "exponential")
               Value Std. Error
## (Intercept) -1.59
                        0.0316 -50.3 0
##
## Scale fixed at 1
##
## Exponential distribution
## Loglik(model) = 590.4 Loglik(intercept only) = 590.4
## Number of Newton-Raphson Iterations: 4
## n= 1000
```

Censored

```
survreg(Surv(t_cens, status_cens) ~ 1,
 dist = 'exponential'
) %>%
  summary
```

```
##
## Call:
## survreg(formula = Surv(t_cens, status_cens) ~ 1, dist = "exponential")
               Value Std. Error
## (Intercept) -1.58
                         0.0403 -39.1 0
```

1.1. SIMULATED DATA 9

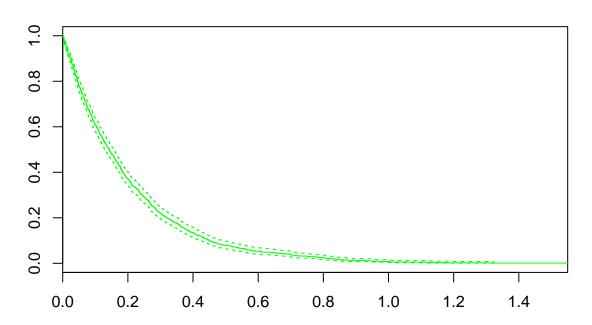
```
##
## Scale fixed at 1
##
## Exponential distribution
## Loglik(model) = 354.6 Loglik(intercept only) = 354.6
## Number of Newton-Raphson Iterations: 4
## n= 1000
```

- 4. Non parametric estimation of survival and the distribution functions
- Uncensored

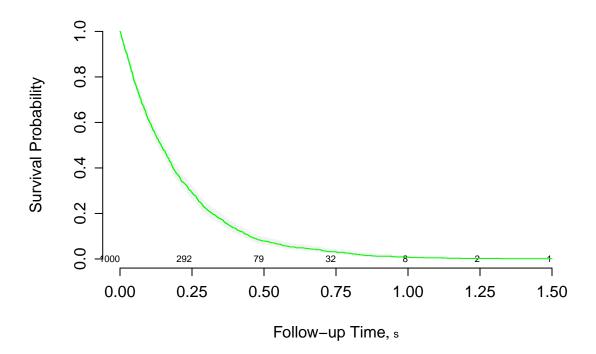
```
# `?survfit` := "Create survival curves"
survfit(Surv(t, status_no_cens) ~ 1)
```

```
## Call: survfit(formula = Surv(t, status_no_cens) ~ 1)
##
         n events
                      median 0.95LCL 0.95UCL
## 1000.000 1000.000
                       0.143
                                 0.129
                                          0.157
# Here we would like to compare to approach to survival plots:
# 1. Using the packege _survival_, so the standard one
\# 2. Uisng the package \_rms\_, a comprehensive package for regression analyses
# Using survival `plot` provided by the _survival_ package
# (`?survival:::plot.survfit`), we can continue to
# use the `survfit()` function for nonparametric survival estimation from the
# same _survival_ package
survfit(Surv(t, status_no_cens) ~ 1) %>%
 plot(
           = c(0, 1.55),
   xlim
   conf.int = TRUE,
   mark.time = TRUE,
         = 'green',
   col
            = 'Uncensored --- survival'
   main
)
# Using the survplot from the _rms_ package (`survplot`), we have to switch to
# the `npsurv()` function for nonparametric survival estimation from the _rms_
# package
npsurv(Surv(t, status_no_cens) ~ 1) %>%
  survplot(
   xlim
            = c(0, 1.5),
   conf.int = TRUE,
   n.risk = TRUE,
   col
           = 'green'
)
title(main = 'Uncensored --- rms') # unfortunally survplot do not have an
                                   # integrated option for the title...
```

Uncensored --- survival



Uncensored --- rms

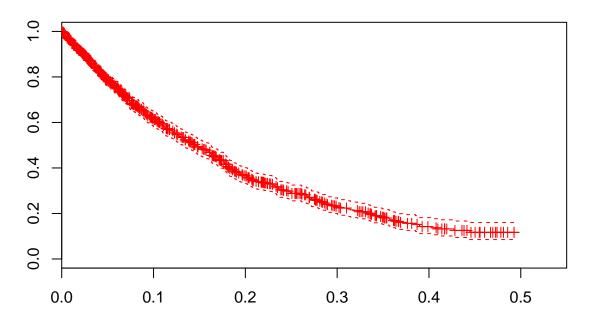


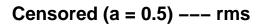
1.1. SIMULATED DATA

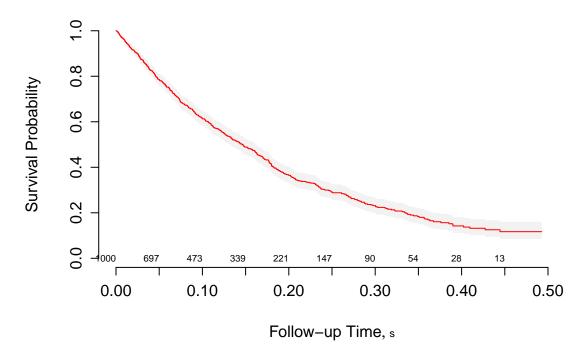
• censored

```
survfit(Surv(t_cens, status_cens) ~ 1)
## Call: survfit(formula = Surv(t_cens, status_cens) ~ 1)
##
                      median 0.95LCL 0.95UCL
         n
             events
## 1000.000 615.000
                       0.146
                                0.133
                                         0.162
survfit(Surv(t_cens, status_cens) ~ 1) %>%
 plot(
            = c(0, 0.55),
   conf.int = TRUE,
   mark.time = TRUE,
   col = 'red',
           = 'Censored (a = 0.5)'
)
npsurv(Surv(t_cens, status_cens) ~ 1) %>%
 survplot(
            = c(0, 0.5),
   xlim
   conf.int = TRUE,
   n.risk = TRUE,
           = 'red'
title(main = 'Censored (a = 0.5) --- rms')
```

Censored (a = 0.5)







1.2 mgus data from survival package

1. Load and explore data

```
data(mgus)
                                                                              # load
head(mgus)
                                                                     # first 10 rows
                sex dxyr pcdx pctime futime death alb creat hgb mspike
##
     id age
                                                  1 2.8
     1
         78 female
                      68 <NA>
                                  NA
                                         748
                                                          1.2 11.5
      2
         73 female
                           LP
                                 1310
                                        6751
                                                    NA
                                                                NA
                                                                       1.3
                      66
                                                           NA
##
     3
         87
              male
                      68 <NA>
                                  NA
                                         277
                                                  1 2.2
                                                          1.1 11.2
                                                                       1.3
     4
         86
              male
                      69 <NA>
                                   NA
                                        1815
                                                  1 2.8
                                                          1.3 15.3
                                                                       1.8
## 5
     5
         74 female
                      68 <NA>
                                  NA
                                        2587
                                                  1 3.0
                                                          0.8 9.8
                                                                       1.4
## 6
     6
         81
                                         563
                                                  1 2.9
              male
                      68 <NA>
                                   NA
                                                          0.9 11.5
                                                                       1.8
dim(mgus)
                                                          # number of rows and cols
## [1] 241
names (mgus)
                                                               # name of the columns
    [1] "id"
                  "age"
                                              "pcdx"
                                                        "pctime" "futime"
                           "sex"
                                     "dxyr"
    [8] "death"
                  "alb"
                           "creat"
                                     "hgb"
                                              "mspike"
str(mgus)
                                               # R internal structure of the object
## 'data.frame':
                     241 obs. of 12 variables:
            : num 1 2 3 4 5 6 7 8 9 10 ...
    $ id
```

```
: atomic 78 73 87 86 74 81 72 79 85 58 ...
##
    ..- attr(*, "label")= chr "AGE AT date_on"
          : Factor w/ 2 levels "female", "male": 1 1 2 2 1 2 1 1 1 2 ...
   ..- attr(*, "label")= chr "Sex"
##
   $ dxyr : num 68 66 68 69 68 68 68 69 70 65 ...
## $ pcdx : Factor w/ 4 levels "AM", "LP", "MA", ...: NA 2 NA ...
   $ pctime: atomic NA 1310 NA NA NA NA NA NA NA NA NA ...
   ..- attr(*, "label")= chr "Progression to Group 4 (days)"
##
   $ futime: atomic 748 6751 277 1815 2587 ...
    ..- attr(*, "label")= chr "Follow-Up Time"
##
   $ death : num 1 1 1 1 1 1 1 1 1 1 ...
##
          : atomic 2.8 NA 2.2 2.8 3 2.9 3 3.1 3.2 3.5 ...
  $ alb
    ..- attr(*, "label")= chr "Serum Albumin"
  $ creat : atomic 1.2 NA 1.1 1.3 0.8 0.9 0.8 0.8 1 1 ...
   ..- attr(*, "label")= chr "Serum Creatinine"
##
          : atomic 11.5 NA 11.2 15.3 9.8 11.5 13.5 15.5 12.4 14.8 ...
   $ hgb
##
    ..- attr(*, "label")= chr "Hemoglobin"
   $ mspike: atomic 2 1.3 1.3 1.8 1.4 1.8 1.3 1.4 1.5 2.2 ...
    ..- attr(*, "label")= chr "Serum M-Spike"
##
##
   - attr(*, "formats")=List of 1
##
    ..$ death:List of 2
    .. .. $ values: num 0 1
    ....$ labels: chr "Alive" "Dead"
summary(mgus)
                                                          # summary from base R
##
                                                   dxyr
                                                               pcdx
         id
                                     sex
                      age
## Min.
         : 1
                 Min.
                        :34.00
                                 female:104
                                                     :56.0
                                                             AM : 8
                                 male :137
                                                             LP : 5
## 1st Qu.: 61
                 1st Qu.:55.00
                                              1st Qu.:66.0
## Median :121
                 Median :63.00
                                              Median:68.0
                                                             MA : 7
                                                     :67.4
## Mean
          :121
                 Mean
                       :62.87
                                              Mean
                                                             MM : 44
  3rd Qu.:181
                 3rd Qu.:72.00
                                              3rd Qu.:70.0
                                                             NA's:177
                        :90.00
                                                     :73.0
##
  Max.
          :241
                 Max.
                                              Max.
##
##
       pctime
                                                         alb
                       futime
                                       death
  Min.
         : 365
                   Min.
                        :
                                   Min.
                                          :0.0000
                                                    Min.
                                                           :1.800
                               6
   1st Qu.: 2469
                   1st Qu.: 2422
                                   1st Qu.:1.0000
##
                                                    1st Qu.:2.900
## Median : 3778
                   Median: 5022
                                   Median :1.0000
                                                    Median :3.200
## Mean
         : 4342
                   Mean : 5425
                                   Mean
                                         :0.9336
                                                    Mean
                                                           :3.204
  3rd Qu.: 5750
                   3rd Qu.: 8264
                                                    3rd Qu.:3.500
                                   3rd Qu.:1.0000
## Max.
          :11685
                   Max.
                          :14325
                                   Max.
                                          :1.0000
                                                    Max.
                                                           :5.100
##
   NA's
          :177
                                                    NA's
                                                          :31
##
                                       mspike
       creat
                        hgb
                   Min. : 7.40
## Min.
          :0.600
                                   Min. :0.300
## 1st Qu.:0.900
                   1st Qu.:12.20
                                   1st Qu.:1.500
## Median :1.000
                   Median :13.20
                                   Median :1.700
## Mean
         :1.095
                   Mean :13.15
                                   Mean
                                         :1.764
## 3rd Qu.:1.100
                   3rd Qu.:14.50
                                   3rd Qu.:2.000
## Max.
           :6.400
                   Max.
                          :16.60
                                   Max. :3.200
## NA's
                   NA's
          :43
                          :1
describe(mgus) # more comprehensive description from _Hisc_ package, loaded by
```

mgus

##

```
## 12 Variables 241 Observations
                                   Gmd .05
80.67 13
                                                 .10
##
     n missing distinct Info Mean
                             121
         0 241 1
##
     241
                                                    25
          .50 .75
121 181
                        .90
##
     .25
                              .95
                 181 217 229
     61
##
## lowest : 1 2 3 4 5, highest: 237 238 239 240 241
## age : AGE AT date_on
                                         .05 .10
     n missing distinct Info Mean
                                     Gmd
     241 0 53 0.999 62.87 13.42
                                            44
##
                                                    48
                 .75
                       .90 .95
##
    . 25
            .50
           63 72
##
     55
                         78
##
## lowest : 34 35 36 37 38, highest: 84 85 86 87 90
## sex : Sex
## n missing distinct
##
     241 0 2
##
## Value female male
## Frequency 104 137
## Proportion 0.432 0.568
## -----
## dxyr
     n missing distinct Info Mean Gmd .05
241 0 17 0.97 67.4 3.073 61
                                                .10
##
                                                    63
     .25 .50 .75 .90
66 68 70 70
                              .95
##
                               70
##
##
## Value 56 58 59 60 61 62 63 64 65 ## Frequency 1 1 5 5 2 7 7 10 10
                                                   18
## Proportion 0.004 0.004 0.021 0.021 0.008 0.029 0.029 0.041 0.041 0.075
## Value
           67 68 69 70 71 72 73
## Frequency 24 40 45 62 2 1 1
## Proportion 0.100 0.166 0.187 0.257 0.008 0.004 0.004
## -----
## pcdx
     n missing distinct
     64 177
##
##
          AM LP MA
## Value
## Frequency 8 5 7
## Proportion 0.125 0.078 0.109 0.688
## -----
## pctime : Progression to Group 4 (days)
    .. missing distinct Info Mean Gmd .05 .10 64 177 63 1 4342 3030 1223 1409 .25 .50 .75 .90 .95 2469 3778 5750 8946 10051
##
##
##
##
```

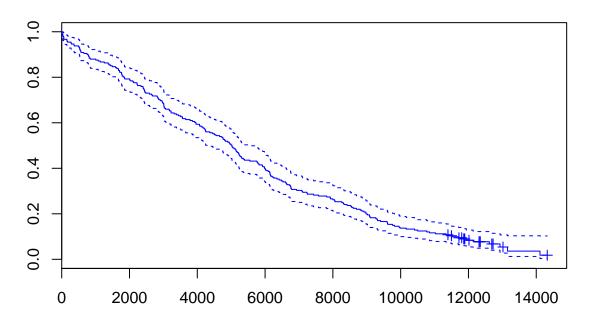
```
## lowest: 365 700 954 1218 1249, highest: 9723 10109 10359 11354 11685
## -----
## futime : Follow-Up Time
                                Gmd .05
4222 283
   n missing distinct
                     Info Mean
                                               .10
          0 237 1 5425
.50 .75 .90 .95
     241
         0 237
                                               779
##
    .25
    2422 5022 8264 11425 12140
##
##
## lowest: 6 7 31 32 39, highest: 12931 13019 13152 14111 14325
## death
                     Info Sum
0.186 225
     n missing distinct
##
                                 Mean
                                         Gmd
     241 0 2
                             225 0.9336 0.1245
##
##
## -----
## alb : Serum Albumin
                                 Gmd .05
0.5293 2.3
                     Info Mean
##
     n missing distinct
                                               .10
     210 31 26 0.995 3.204 0.5293
##
                                              2.6
     . 25
##
           .50
                .75 .90 .95
           3.2 3.5
##
     2.9
                       3.8
                             3.9
##
## lowest : 1.8 1.9 2.1 2.2 2.3, highest: 4.0 4.1 4.3 4.5 5.1
## -----
## creat : Serum Creatinine
## n missing distinct Info Mean Gmd .05
                                              .10
    198 43 19 0.978 1.095 0.39 0.700 0.800
##
     . 25
          .50 .75 .90 .95
  0.900 1.000 1.100 1.300 1.615
##
##
## Value 0.6 0.7 0.8 0.9 1.0 1.1 1.2 1.3 1.4 1.5
## Frequency 4 13
                 26 42
                          35 29 18
                                      12
                                          4 4
## Proportion 0.020 0.066 0.131 0.212 0.177 0.146 0.091 0.061 0.020 0.020
##
## Value 1.6 1.7 2.0 2.5 2.6 3.5 3.6 3.7 6.4
          1 3 1 1
                                  1
## Frequency
                          1 1
## Proportion 0.005 0.015 0.005 0.005 0.005 0.005 0.005 0.005 0.005
## -----
## hgb : Hemoglobin
     n missing distinct Info Mean Gmd .05 .10
##
     ##
##
    . 25
   12.20 13.20 14.50 15.11 15.51
##
## lowest : 7.4 7.7 8.4 9.5 9.6, highest: 15.9 16.1 16.2 16.5 16.6
## mspike : Serum M-Spike
     n missing distinct Info Mean Gmd .05
241 0 23 0.993 1.764 0.4687 1.1
                                              .10
##
##
                                              1.3
     . 25
                 .75 .90 .95
##
           .50
           1.7 2.0
                       2.3
##
     1.5
                             2.5
## lowest : 0.3 0.8 0.9 1.0 1.1, highest: 2.5 2.6 2.7 2.9 3.2
```

```
## # A tibble: 241 x 12
                  sex dxyr
                            pcdx pctime futime death
                                                   alb creat
           age
                                       <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
##
  * <dbl> <fctr> <dbl> <fctr> <dbl> <fctr> <dbl>
## 1
        1
            78 female
                        68
                            <NA>
                                   NA
                                        748
                                               1
                                                   2.8
                                                       1.2 11.5
## 2
        2
            73 female
                        66
                            LP
                                  1310
                                        6751
                                                   NA
                                                         NΑ
                                               1
                                                             NA
## 3
        3
            87
                male
                        68 <NA>
                                  NA
                                       277
                                              1
                                                   2.2
                                                       1.1 11.2
## 4
            86 male 69 <NA>
        4
                                  NA 1815
                                               1 2.8
                                                        1.3 15.3
## 5
        5
            74 female 68
                           <NA>
                                   NA 2587
                                               1 3.0
                                                        0.8
                                                            9.8
                                              1 2.9
## 6
                                   NA 563
                                                       0.9 11.5
        6
            81
                male 68 <NA>
## 7
            72 female 68 <NA>
                                   NA 1135
                                              1 3.0
                                                       0.8 13.5
        7
            79 female 69
                                   NA 2016
                                                        0.8 15.5
## 8
        8
                            <NA>
                                               1 3.1
## 9
        9
            85 female
                       70
                            <NA>
                                   NA
                                       2422
                                               1
                                                   3.2
                                                       1.0 12.4
                            <NA>
                                   NA
                                        6155
                                               1
                                                       1.0 14.8
## 10
       10
            58 male 65
                                                   3.5
## # ... with 231 more rows, and 1 more variables: mspike <dbl>
```

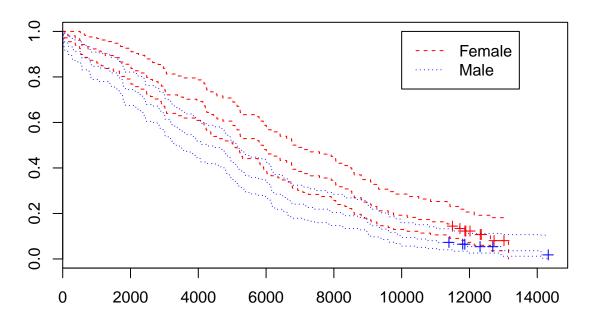
- 2. Non parametric Kaplan-Meyer estimation of the survival function
- Estimate the survival function from randomization overall and according to sex.

```
survfit(Surv(futime, death) ~ 1,
  data = mgus_df
) %>%
 plot(
   conf.int = TRUE,
   mark.time = TRUE,
          = 'blue',
   col
            = 'Survival function for mgus data'
)
survfit(Surv(futime, death) ~ sex,
 data = mgus df
) %>%
 plot(
   conf.int = TRUE,
   mark.time = TRUE,
           = 'Survival function for mgus data according to sex',
             = c('red', 'blue'),
    col
   lty
             = c(2, 3)
)
legend(
 x = 10000, y = 1,
 legend = c("Female", "Male"),
 col = c('red', 'blue'),
        = c(2, 3)
 lty
```

Survival function for mgus data



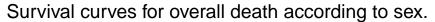
Survival function for mgus data according to sex

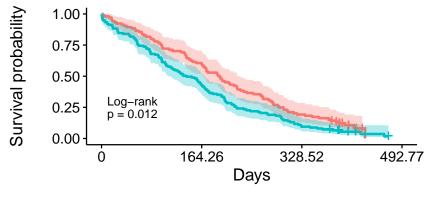


Sex

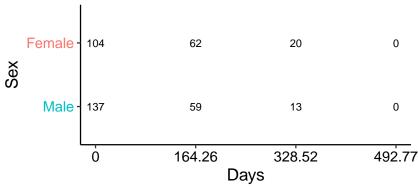
- Female

Male

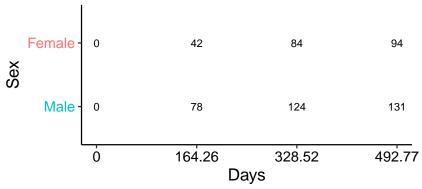




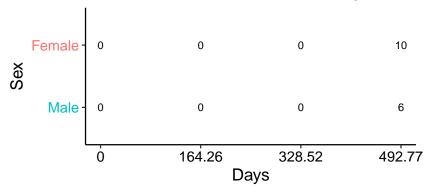
Number at risk



Cumulative number of events



Cumulative number of censoring



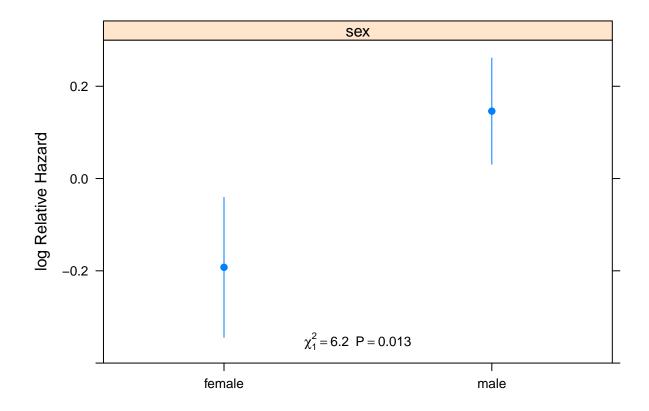
Note: No female reaches the end of the f-up!

• Test the effect of sex

```
# Using __survival__ (no plot method is provided for this solution)
survdiff(Surv(futime, death) ~ sex,
  data = mgus_df
)
```

```
## Call:
## survdiff(formula = Surv(futime, death) ~ sex, data = mgus_df)
##
                N Observed Expected (O-E)^2/E (O-E)^2/V
                        94
                                113
                                         3.08
                                                    6.25
## sex=female 104
## sex=male 137
                       131
                                112
                                         3.08
                                                    6.25
##
## Chisq= 6.2 on 1 degrees of freedom, p= 0.0124
# usinq __rms__
dd <- datadist(mgus_df) # To evaluate cph, _rms_ needs this object which simply
                         # store statistics about the data.
                         # Note: the name of the object (i.e. "dd") has to be
                                 exactly the same as the one specified into the
                                 option set just after the `library(rms)` call.
                         #
                                 (See: Chapter settings)
cox_model <- cph(Surv(futime, death) ~ sex,</pre>
 data = mgus_df
summary(cox_model)
                                              # return effect size and HR with CI
```

```
##
               Effects
                                    Response : Surv(futime, death)
##
## Factor
                     Low High Diff. Effect S.E.
                                                     Lower 0.95 Upper 0.95
                                    -0.33853 0.13603 -0.60514 -0.071916
## sex - female:male 2
                        1
                              NA
                                                  NA 0.54600
    Hazard Ratio
                                     0.71282
                                                                 0.930610
                              NA
Predict(cox_model) %>%
                               # Compute predicted values and confidence limits
                               # Note: pay attention to Title-case "P"redict
 plot(
   groups = 'sex',
   anova = anova(cox model),
                                    # Compute and print the $\chi^2$ statistics
          = TRUE
                                    # print the pvalue
   pval
```



1.3 Non parametric Kaplan-Meier estimation of the survival function

1. Let consider a sample of n = 500

```
n <- 500
```

2. Simulate the dates of entry in the cohort, from January, 2010 to January, 2017

3. Simulate the data-set of death, assuming exponential death times of mean 2 years

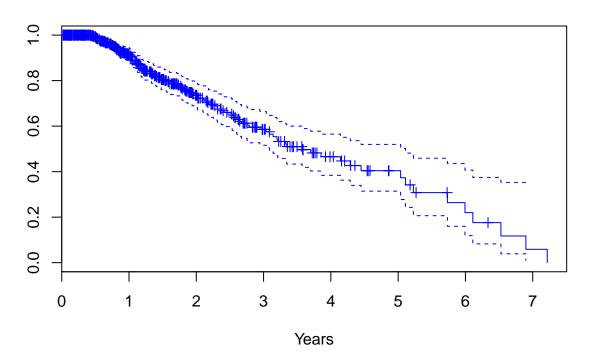
4. Let fix the reference date of the analyses of June, 2017

```
end_date <- as.Date('2017-06-01') # Fixed date for the end of f-up
death_r_cens <- pmin(death_t, end_date - time_start)
status_cens <- status_no_cens - (death_t == death_r_cens)</pre>
```

5. Estimate the survival function from randomization

```
survfit(Surv(death_r_cens, status_cens) ~ 1) %>%
plot(
   conf.int = TRUE,
   mark.time = TRUE,
   main = 'Survival curve from randomization (right censored at 2017-06-01)',
   col = 'blue',
   xlab = 'Years',
   xscale = 365.25
)
```

Survival curve from randomization (right censored at 2017–06–01)



Software

Packages

All the exercise are solved using R (ver. 3.4.2) has been used provided with packages: survival (Therneau (2017)) for the survival data analyses (reference package), survminer (Kassambara and Kosinski (2017)) for advance survival plot using ggplot2 (Wickham and Chang (2016)) package, rms (Harrell, Jr. (2017)) for additional features on regression modeling strategies (survival ones included).

With regards to the data management, the collection of package tidyverse (Wickham (2017)) is loaded, which includes: dplyr (Wickham et al. (2017)) for data manipulation, purrr (Henry and Wickham (2017)) for functional programming, readr (R-readr) for data import, tidyr (R-tidyr) for funtions to tidy the data, tibble (R-tibble) to take advantage of the *tible* data frame class and ggplot2 as a interface for the Gramar of Grahics.

The present book was written in RMarkdown (R-rmarkdown), compiled using knitr (Xie (2017b)) and rendered as an HTML book by bookdown (Xie (2017a)).

System Information

All the code is compiled on a system with the following overall characteristics and loaded packages.

devtools::session_info()

```
##
    setting value
##
    version R version 3.4.2 (2017-09-28)
##
    system
             x86_64, mingw32
##
    ui
             RTerm
##
    language (EN)
##
    collate
             English_United States.1252
##
    tz
             Europe/Berlin
             2017-10-03
##
    date
##
##
    package
                  * version date
                                        source
                            2016-10-29 CRAN (R 3.4.1)
##
    acepack
                    1.4.1
##
                    0.2.0
                            2017-04-11 CRAN (R 3.4.1)
    assertthat
##
                    1.1.0
                            2017-05-22 CRAN (R 3.4.0)
    backports
                  * 3.4.2
                            2017-09-28 local
##
    base
                    0.1 - 3
##
    base64enc
                            2015-07-28 CRAN (R 3.4.0)
##
    bindr
                    0.1
                            2016-11-13 CRAN (R 3.4.1)
##
    bindrcpp
                    0.2
                            2017-06-17 CRAN (R 3.4.1)
                            2017-08-20 CRAN (R 3.4.1)
    bookdown
                    0.5
                            2017-02-13 CRAN (R 3.4.0)
##
    broom
                    0.4.2
```

```
2016-07-27 CRAN (R 3.4.1)
   cellranger
                 1.1.0
##
   checkmate
                1.8.3
                         2017-07-03 CRAN (R 3.4.1)
## cluster
                2.0.6 2017-03-16 CRAN (R 3.4.1)
## cmprsk
                2.2-7 2014-06-17 CRAN (R 3.4.1)
                0.2-15 2016-10-05 CRAN (R 3.4.0)
## codetools
## colorspace 1.3-2 2016-12-14 CRAN (R 3.4.1)
## compiler
                3.4.2 2017-09-28 local
## data.table 1.10.4 2017-02-01 CRAN (R 3.4.0)
   datasets
##
               * 3.4.2
                         2017-09-28 local
              1.13.3 2017-08-02 CRAN (R 3.4.1)
## devtools
## digest
                0.6.12 2017-01-27 CRAN (R 3.4.1)
               * 0.7.3
                         2017-09-09 CRAN (R 3.4.1)
## dplyr
              0.10.1 2017-06-24 CRAN (R 3.4.1)
## evaluate
## forcats
                         2017-01-23 CRAN (R 3.4.1)
                0.2.0
             0.2.0
0.8-69
* 1.2-2
                0.8-69 2017-06-21 CRAN (R 3.4.0)
## foreign
## Formula
                         2017-07-10 CRAN (R 3.4.1)
               * 2.2.1
##
   ggplot2
                         2016-12-30 CRAN (R 3.4.1)
               * 0.1.5 2017-08-22 CRAN (R 3.4.1)
##
   ggpubr
                1.1.1 2017-06-21 CRAN (R 3.4.1)
##
   glue
               * 3.4.2 2017-09-28 local
##
   graphics
             * 3.4.2 2017-09-28 local
##
   grDevices
   grid
                3.4.2 2017-09-28 local
                2.3
                         2017-09-09 CRAN (R 3.4.1)
##
   gridExtra
                0.2.0 2016-02-26 CRAN (R 3.4.1)
##
   gtable
## haven
                1.1.0 2017-07-09 CRAN (R 3.4.1)
## Hmisc
               * 4.0-3 2017-05-02 CRAN (R 3.4.1)
## hms 0.3 2016-11-22 CRAN (R 3.4.1)
## htmlTable 1.9 2017-01-26 CRAN (R 3.4.1)
## htmltools 0.3.6 2017-04-28 CRAN (R 3.4.1)
## htmlwidgets 0.9
                         2017-07-10 CRAN (R 3.4.1)
              1.3.1
1.5
                         2017-08-20 CRAN (R 3.4.1)
## httr
##
  jsonlite
                         2017-06-01 CRAN (R 3.4.1)
## km.ci
                0.5-2 2009-08-30 CRAN (R 3.4.1)
                0.1-5 2012-12-03 CRAN (R 3.4.0)
## KMsurv
                1.17
                         2017-08-10 CRAN (R 3.4.1)
## knitr
## labeling
                0.3
                         2014-08-23 CRAN (R 3.4.0)
             * 0.20-35 2017-03-25 CRAN (R 3.4.1)
## lattice
## latticeExtra 0.6-28 2016-02-09 CRAN (R 3.4.1)
             0.2.0
                         2016-06-12 CRAN (R 3.4.1)
## lazyeval
                1.6.0
                         2016-09-13 CRAN (R 3.4.1)
## lubridate
## magrittr
               * 1.5
                         2014-11-22 CRAN (R 3.4.1)
## MASS
                 7.3-47 2017-04-21 CRAN (R 3.4.1)
## Matrix
                1.2-11 2017-08-16 CRAN (R 3.4.1)
## MatrixModels 0.4-1
                         2015-08-22 CRAN (R 3.4.1)
## memoise
              1.1.0 2017-04-21 CRAN (R 3.4.1)
               * 3.4.2 2017-09-28 local
## methods
               1.5-5 2016-10-15 CRAN (R 3.4.0)
##
   mnormt
##
   modelr
                0.1.1
                         2017-07-24 CRAN (R 3.4.1)
                1.4-7
                         2017-09-07 CRAN (R 3.4.1)
## multcomp
                 0.4.3 2016-02-13 CRAN (R 3.4.1)
## munsell
                1.0-6
## mvtnorm
                         2017-03-02 CRAN (R 3.4.0)
## nlme
                3.1-131 2017-02-06 CRAN (R 3.4.1)
## nnet
                7.3-12 2016-02-02 CRAN (R 3.4.1)
            3.4.2 2017-09-28 local
## parallel
```

```
2017-03-21 CRAN (R 3.4.1)
   pkgconfig
                 2.0.1
## plyr
                 1.8.4
                        2016-06-08 CRAN (R 3.4.1)
## polspline
                1.1.12 2015-07-14 CRAN (R 3.4.0)
                 1.7.8
                        2017-09-09 CRAN (R 3.4.1)
## psych
               * 0.2.3
##
   purrr
                        2017-08-02 CRAN (R 3.4.1)
## quantreg
                 5.33
                        2017-04-18 CRAN (R 3.4.1)
                 2.2.2
                        2017-06-17 CRAN (R 3.4.1)
## RColorBrewer 1.1-2
                        2014-12-07 CRAN (R 3.4.0)
## Rcpp
                 0.12.12 2017-07-15 CRAN (R 3.4.1)
## readr
               * 1.1.1
                        2017-05-16 CRAN (R 3.4.1)
## readxl
                1.0.0
                        2017-04-18 CRAN (R 3.4.1)
                 1.4.2 2016-10-22 CRAN (R 3.4.1)
## reshape2
                0.1.2 2017-08-09 CRAN (R 3.4.1)
## rlang
## rmarkdown
                1.6
                        2017-06-15 CRAN (R 3.4.1)
               * 5.1-1
## rms
                         2017-05-03 CRAN (R 3.4.1)
                 4.1-11 2017-04-21 CRAN (R 3.4.1)
##
   rpart
## rprojroot
                1.2
                         2017-01-16 CRAN (R 3.4.1)
## rstudioapi
                0.7
                         2017-09-07 CRAN (R 3.4.1)
## rvest
                0.3.2
                        2016-06-17 CRAN (R 3.4.1)
                2.4-0 2017-07-26 CRAN (R 3.4.1)
## sandwich
## scales
                0.5.0 2017-08-24 CRAN (R 3.4.1)
## SparseM
               * 1.77
                        2017-04-23 CRAN (R 3.4.0)
                3.4.2
                        2017-09-28 local
## splines
               * 3.4.2
##
   stats
                        2017-09-28 local
## stringi
              1.1.5
                        2017-04-07 CRAN (R 3.4.0)
## stringr
                1.2.0
                        2017-02-18 CRAN (R 3.4.1)
## survival
               * 2.41-3 2017-04-04 CRAN (R 3.4.1)
## survminer
               * 0.4.0
                        2017-06-07 CRAN (R 3.4.1)
## survMisc
                 0.5.4
                        2016-11-23 CRAN (R 3.4.1)
## TH.data
                        2017-01-23 CRAN (R 3.4.1)
                1.0-8
## tibble
               * 1.3.4
                        2017-08-22 CRAN (R 3.4.1)
## tidyr
               * 0.7.1
                        2017-09-01 CRAN (R 3.4.1)
## tidyverse
                        2017-01-27 CRAN (R 3.4.1)
               * 1.1.1
## tools
                 3.4.2
                        2017-09-28 local
               * 3.4.2
## utils
                        2017-09-28 local
## withr
                2.0.0
                        2017-07-28 CRAN (R 3.4.1)
## xml2
                1.1.1
                        2017-01-24 CRAN (R 3.4.1)
## xtable
               1.8-2
                        2016-02-05 CRAN (R 3.4.1)
                2.1.14 2016-11-12 CRAN (R 3.4.1)
##
   yaml
## zoo
                1.8-0 2017-04-12 CRAN (R 3.4.1)
```

 $26 CHAPTER\ 1.\ \ MONDAY: INTRODUCTION\ TO\ SURVIVAL\ ANALYSES\ AND\ SIMULATION\ OF\ DATA$

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