

## Single Positive Multi-label Learning



	person	dog	bus	bicycle	apple	boat
(a)	✓	✗	✓	✓	✗	✗
(b)	✓	✗	?	✓	?	✗
(c)	✓	?	?	?	?	?

✓: positive labels ✗: negative labels  
?: unknown Labels

(a): Multi-label Learning (b): Multi-label Learning with Missing Labels (MLML) (c): Single Positive Multi-label Learning (SPML)

In SPML, each multi-label training image has **only one positive label** and **other labels remain unannotated**.

## Traditional Solution

**Assuming-Negative (AN) Loss:** assumes all unannotated labels are negative and follows BCE loss.

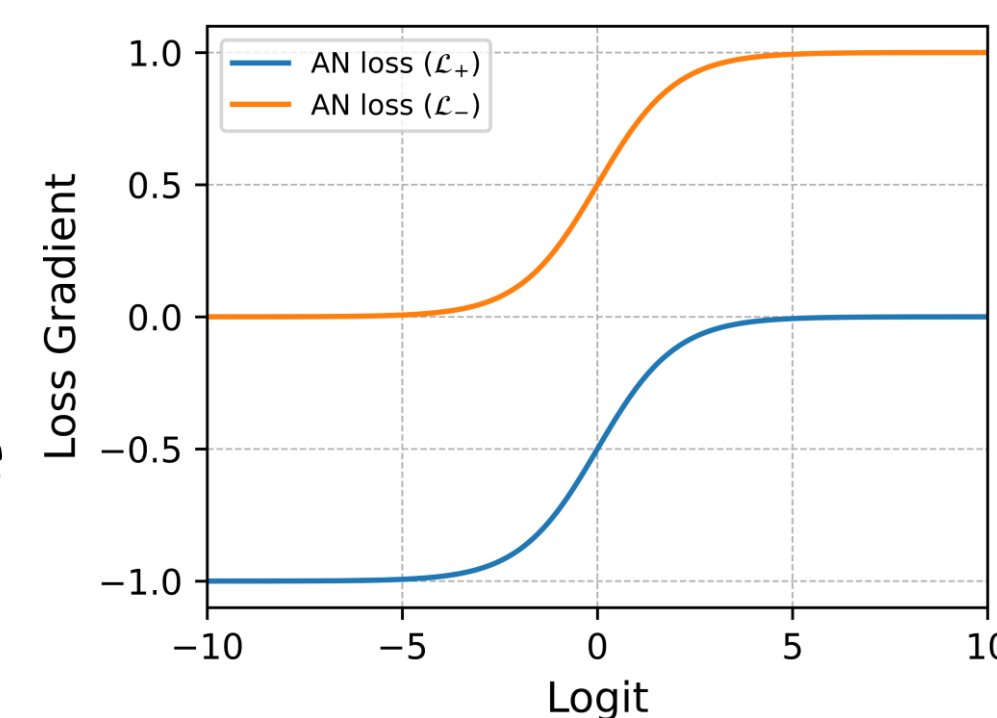
$$\mathcal{L}_{AN}(\mathbf{f}^{(n)}, \mathbf{y}^{(n)}) = -\frac{1}{C} \sum_{c=1}^C [\mathbb{1}_{[y_c^{(n)}=1]} \log(f_c^{(n)}) + \mathbb{1}_{[y_c^{(n)}=0]} \log(1 - f_c^{(n)})]$$

The gradient regime of AN loss:

$$\begin{aligned} \mathcal{L}_+ &= -\log(p) \\ \mathcal{L}_- &= -\log(1 - p) \end{aligned} \Rightarrow \begin{cases} \frac{\partial \mathcal{L}_+}{\partial g} = \frac{\partial \mathcal{L}_+}{\partial p} \frac{\partial p}{\partial g} = \frac{-e^{-g}}{1 + e^{-g}}, & y_c^{(n)} = 1 \\ \frac{\partial \mathcal{L}_-}{\partial g} = \frac{\partial \mathcal{L}_-}{\partial p} \frac{\partial p}{\partial g} = \frac{1}{1 + e^{-g}}, & y_c^{(n)} = 0 \end{cases}$$

It results in three issues:

1. Dominance of Assumed Negative Labels
2. Introduced Label Noise
3. Over-Suppression for Confident Positive Predictions



## Motivation

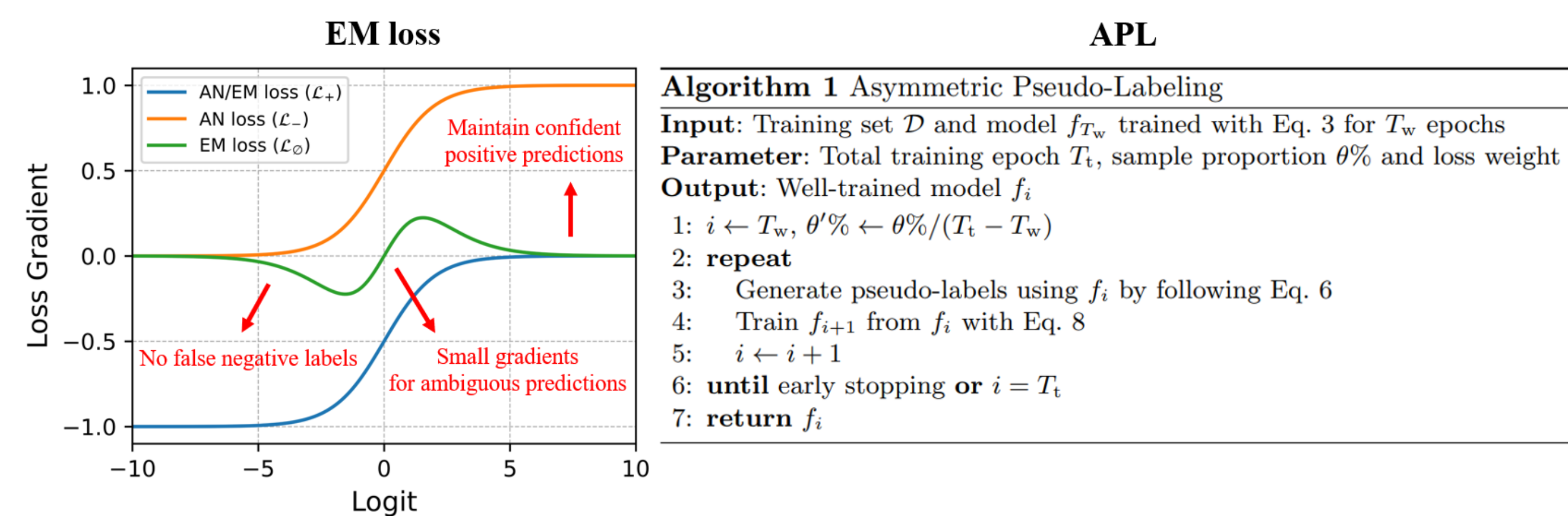
Una. labels need to be treated with a **better gradient regime**. Instead making any unrealistic assumptions, we choose to **acknowledge the fact that they are unknown**.

## Acknowledging the Unknown

1. **Entropy-Maximization (EM) Loss:** maximizes the entropy of predicted probabilities for una. labels.
2. **Asymmetric Pseudo-Labeling (APL):** adopts asymmetric-tolerance PL strategies.

$$\mathcal{L}_{EM}(\mathbf{f}^{(n)}, \mathbf{y}^{(n)}) = -\frac{1}{C} \sum_{c=1}^C [\mathbb{1}_{[y_c^{(n)}=1]} \log(f_c^{(n)}) + \mathbb{1}_{[y_c^{(n)}=0]} \alpha H(f_c^{(n)})]$$

$$H(f_c^{(n)}) = -[f_c^{(n)} \log(f_c^{(n)}) + (1 - f_c^{(n)}) \log(1 - f_c^{(n)})]$$



## Benchmark Results

Experimental results with mAP on four large-scale multi-label datasets

Ann. Labels	Methods	VOC	COCO	NUS	CUB
All P. & All N.	BCE loss	89.42±0.27	76.78±0.13	52.08±0.20	30.90±0.64
1 P. & All N.	BCE loss	87.60±0.31	71.39±0.19	46.45±0.27	20.65±1.11
1 P. & 0 N.	AN loss	85.89±0.38	64.92±0.19	42.27±0.56	18.31±0.47
	DW	86.98±0.36	67.59±0.11	45.71±0.23	19.15±0.56
	L1R	85.97±0.31	64.44±0.20	42.15±0.46	17.59±1.82
	L2R	85.96±0.36	64.41±0.24	42.72±0.12	17.71±1.79
	LS	87.90±0.21	67.15±0.13	43.77±0.29	16.26±0.45
	N-LS	88.12±0.32	67.15±0.10	43.86±0.54	16.82±0.42
	EntMin	53.16±2.81	32.52±5.55	19.38±3.64	13.08±0.15
	Focal loss	87.59±0.58	68.79±0.14	47.00±0.14	19.80±0.30
	ASL	87.76±0.51	68.78±0.32	46.93±0.30	18.81±0.48
	ROLE	87.77±0.22	67.04±0.19	41.63±0.35	13.66±0.24
1 P. & 0 N.	ROLE+LI	88.26±0.21	69.12±0.13	45.98±0.26	14.86±0.72
	EM loss	89.09±0.17	70.70±0.31	47.15±0.11	20.85±0.42
	EM loss+APL	89.19±0.31	70.87±0.23	47.59±0.22	21.84±0.34

→ Oracles

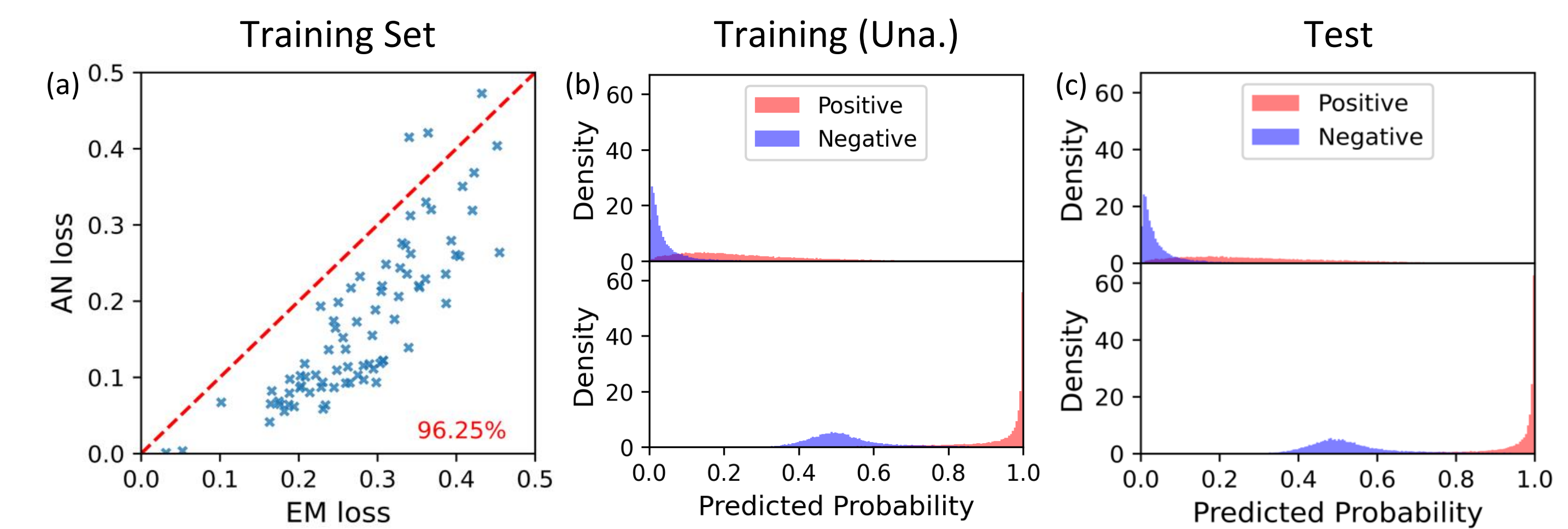
→ AN Loss and Improved AN Loss

→ Other Comprising Methods

→ Ours

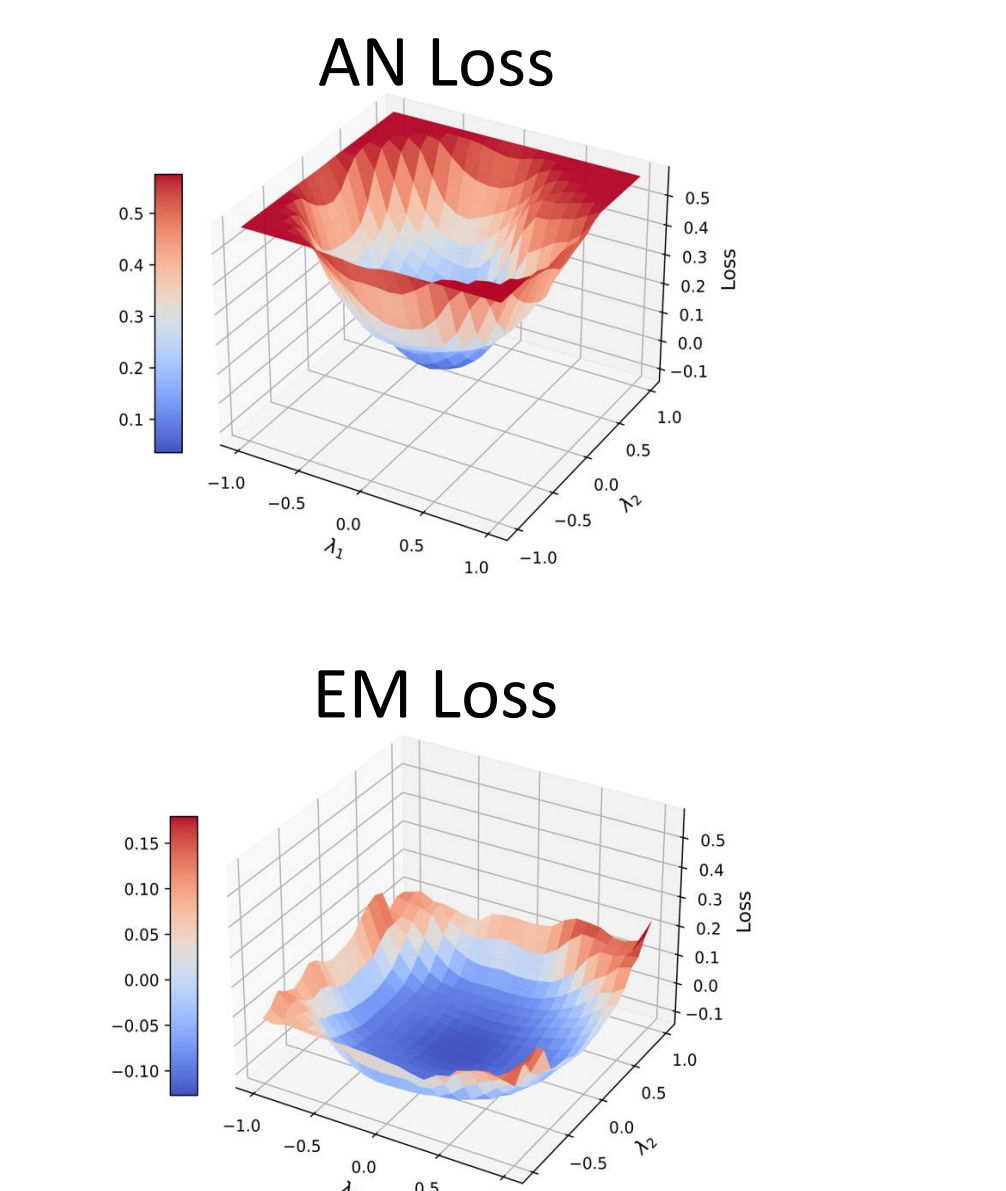
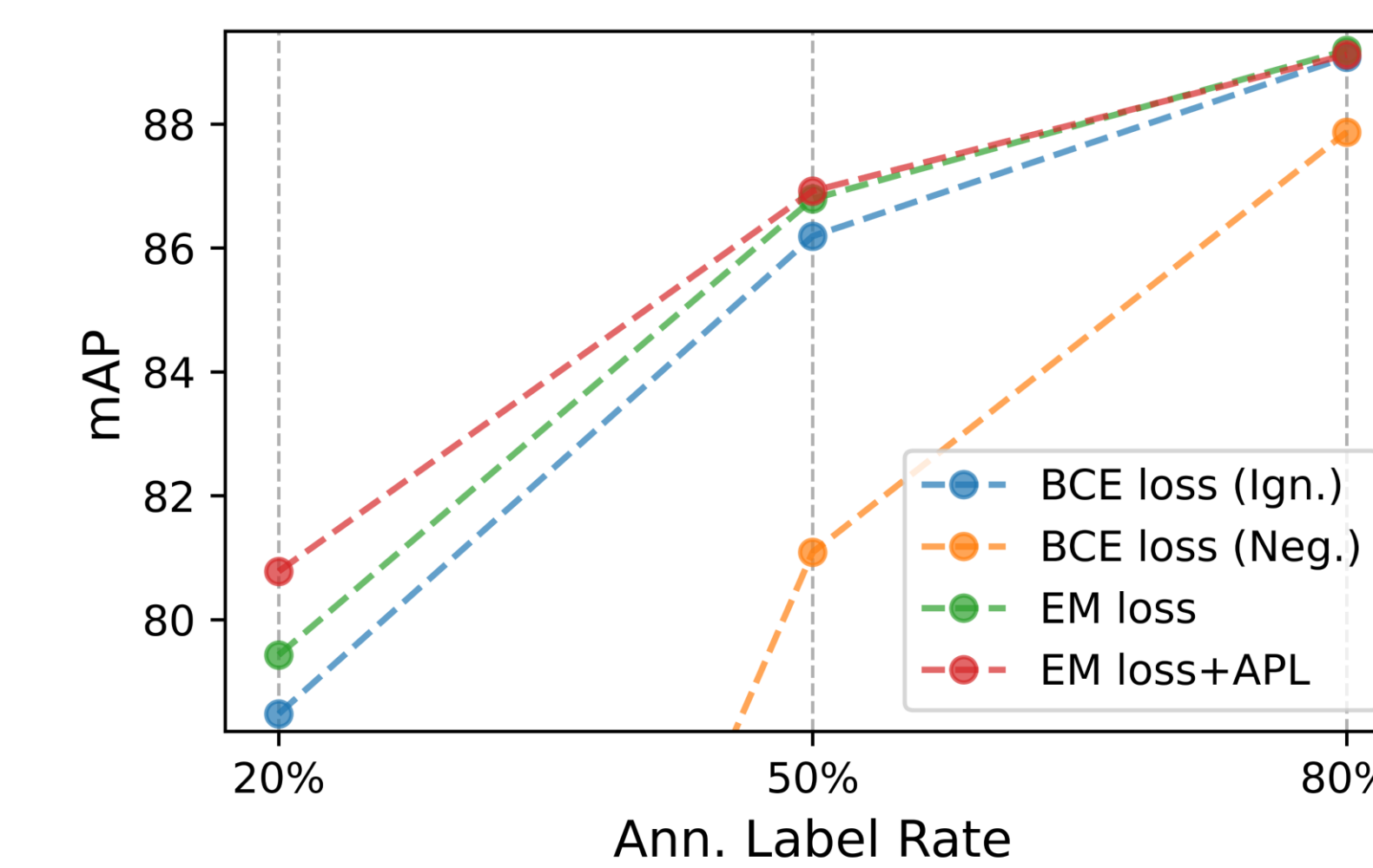
## Further Analysis

Distinguishability of the predictions for pos. and neg. labels  
(a): Wass. distances (b)&(c): Densities of an example class



Performance in a more general scenario (MLML)

Generalization Evaluation by Loss Landscapes



## Qualitative Results



Paper and Code are publicly available:

<https://github.com/Correr-Zhou/SPML-AckTheUnknown>



The proposed method achieves **SOTA results** on all four benchmarks, and even **approaches to the results of training with full annotations** in some cases.