

COSC 2436: Final Exam Review

Final Exam Topics

- **Hashing**
- **Binary Search Tree (BST)**
- **AVL Tree**
- **Graphs**
- **Stacks & Queues**
- **Sorting**

Hashing #1

Insert the following values into a hash table using linear probing.

Assume the hash table is of size 10.

{54, 75, 24, 45, 18, 10}

Hashing #1

Insert the following values into a hash table using linear probing.
Assume the hash table is of size 10.

{54, 75, 24, 45, 18, 10}

0	1	2	3	4	5	6	7	8	9
10				54	75	24	45	18	

Hashing #2

Write the function for quadratic probing.

```
void quadraticProbing(int table[], int x, int tableSize){  
    int index = 0;  
    for(int i = 0; i < tableSize; i++){  
        index = ((x%tableSize) + (i*i)) % tableSize;  
        if(table[index] == -1){  
            table[index] = x;  
            break;  
        }  
    }  
}
```

Hashing #3

The code below shows double hashing. What is wrong with the code?


```
73 ▼ void doubleHashing(int table[], int x, int tableSize){  
74 ▼     for(int i = 0; i < tableSize; i++){  
75         int index = (hash1(x, tableSize) + (i * hash2(x, 7))) % tableSize;  
76 ▼         if(table[index] == -1){  
77             table[index] = x;  
78         }  
79     }  
80 }
```

Hashing #3

The code below shows double hashing. What is wrong with the code?

There should be a *break* statement after line 77. If there is no break statement, *x* will keep getting added to the table.

```
73 ▼ void doubleHashing(int table[], int x, int tableSize){  
74 ▼   for(int i = 0; i < tableSize; i++){  
75     int index = (hash1(x, tableSize) + (i * hash2(x, 7))) % tableSize;  
76 ▼     if(table[index] == -1){  
77       table[index] = x;  
78     }  
79   }  
80 }
```

 **add *break*;**

Hashing #4

Match the following hash function with its correct description.

- Direct Hashing _____
 - Linear Probing _____
 - Quadratic Probing _____
 - Separate Chaining _____
 - Double Hashing _____
- a) table never fills up
 - b) data is overwritten during collision
 - c) clustering can occur
 - d) uses two hash functions
 - e) probes by i^2 if collision is found

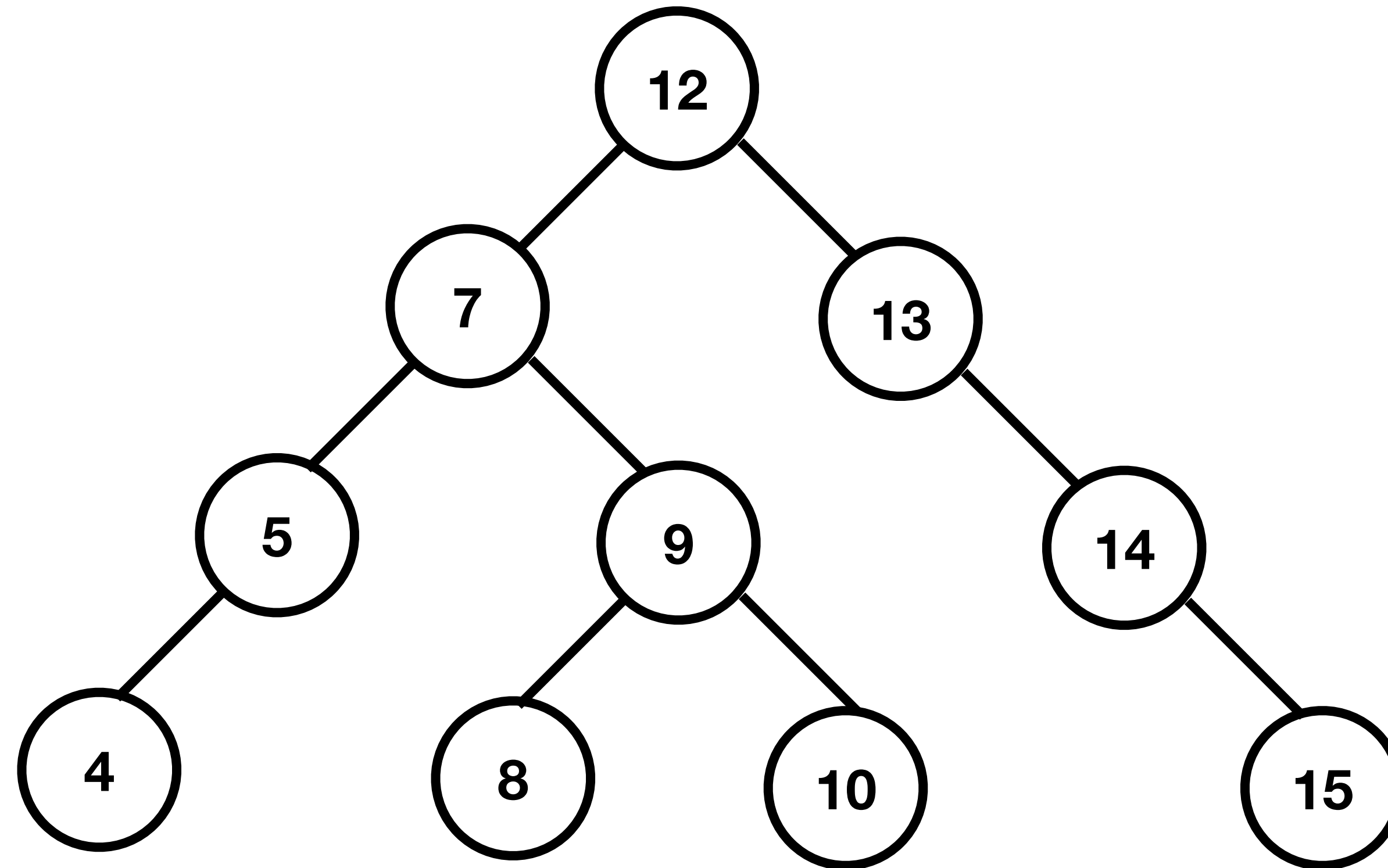
Hashing #4

Match the following hash function with its correct description.

- Direct Hashing __b__
 - Linear Probing __c__
 - Quadratic Probing __e__
 - Separate Chaining __a__
 - Double Hashing __d__
- a) table never fills up
 - b) data is overwritten during collision
 - c) clustering can occur
 - d) uses two hash functions
 - e) probes by i^2 if collision is found

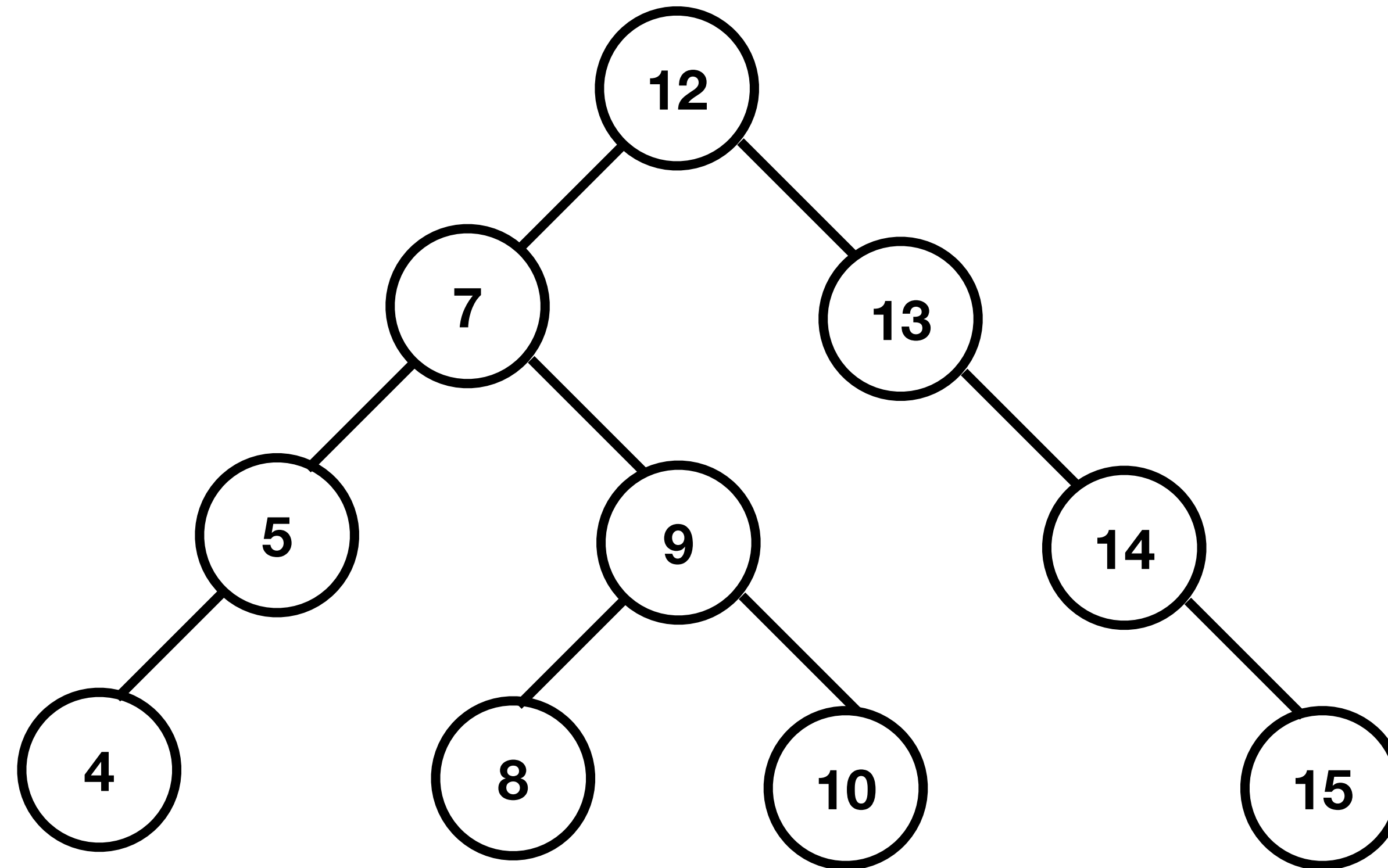
BST #1

Perform preorder traversal on the following BST.



BST #1

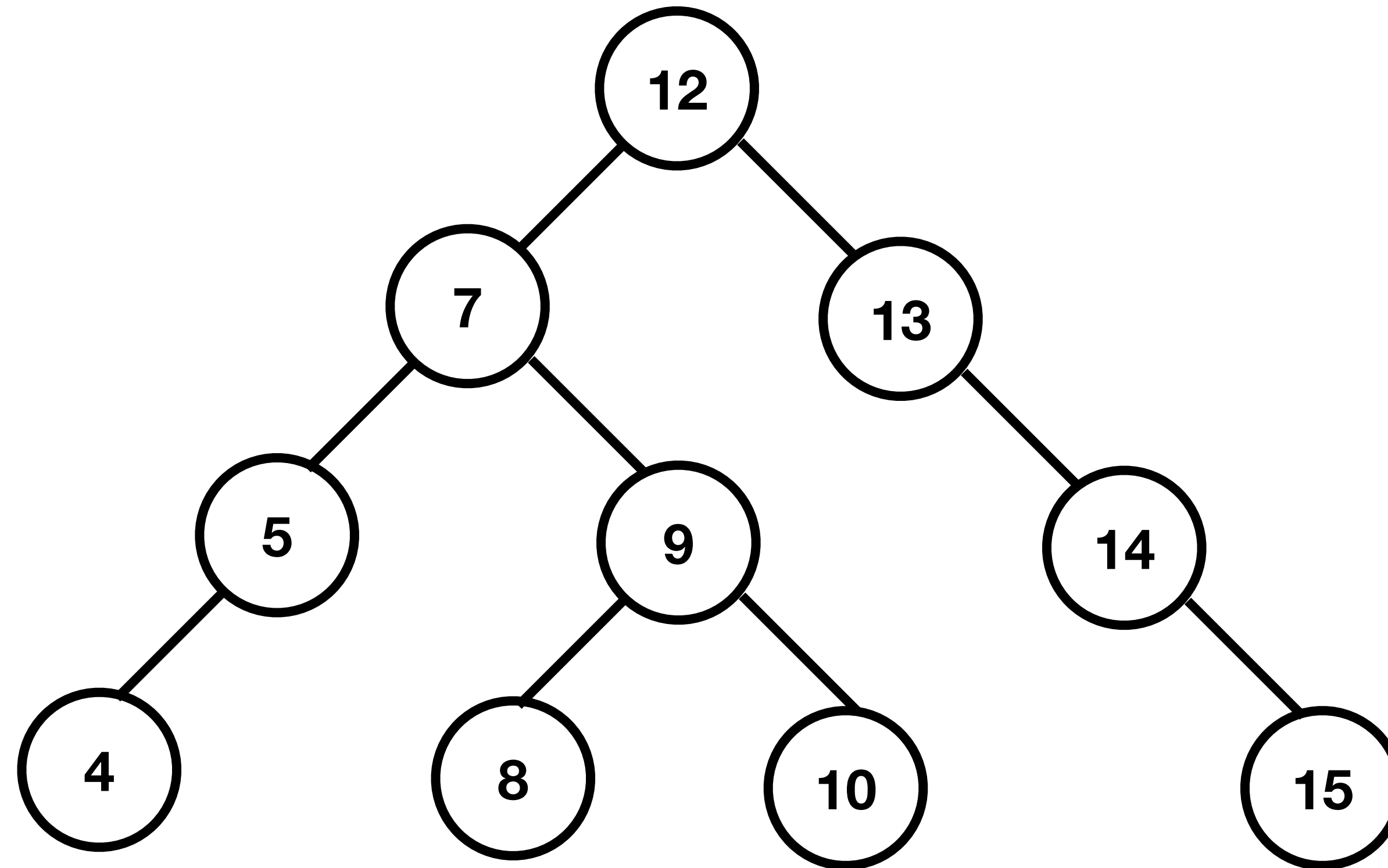
Perform preorder traversal on the following BST.



Preorder: 12 7 5 4 9 8 10 13 14 15

BST #2

Write the function which produced the output below.



Output: 4 5 8 10 9 7 15 14 13 12

BST #2

Write the function which produced the output below.

```
void postorder(node *n){  
    if(n == nullptr)  
        return;  
    postorder(n->left);  
    postorder(n->right);  
    cout << n->value << " ";  
}
```

BST #3

Write the function `getSum()` which returns the sum of all the values in a BST.

```
struct node{  
    int value;  
    node *right;  
    node *left;  
};
```

```
int getSum(node *n) {
```

```
}
```

BST #3

Write the function `getSum()` which returns the sum of all the values in a BST.

```
int getSum(node *n){  
    if(n == nullptr)  
        return 0;  
    return (n->value + getSum(n->right) + getSum(n->left));  
}
```


BST #4

Write the function leafCount() which returns the number of leafs in a BST.

```
struct node{  
    int value;  
    node *left;  
    node *right;  
};
```

```
int leafCount(node *root) {  
  
  
  
  
  
  
  
  
}
```

BST #4

Write the function `leafCount()` which returns the number of leafs in a BST.

```
int leafCount(node *n){  
    if(n == nullptr)  
        return 0;  
    else if(n->left == nullptr && n->right == nullptr)  
        return 1;  
    else  
        return leafCount(n->left) + leafCount(n->right);  
}
```

BST #5

Which of the following is NOT a property of a BST:

- A) Best case time complexity is $O(\log(n))$
- B) Left-Child $<$ Root $<$ Right-Child
- C) Only contains unique values
- D) Can have more than 2 children
- E) None of the above

BST #5

Which of the following is NOT a property of a BST:

- A) Best case time complexity is $O(\log(n))$
- B) Left-Child $<$ Root $<$ Right-Child
- C) Only contains unique values
- D) Can have more than 2 children
- E) None of the above

D) Can have more than 2 children

AVL Tree #1

Perform the following AVL Tree commands.

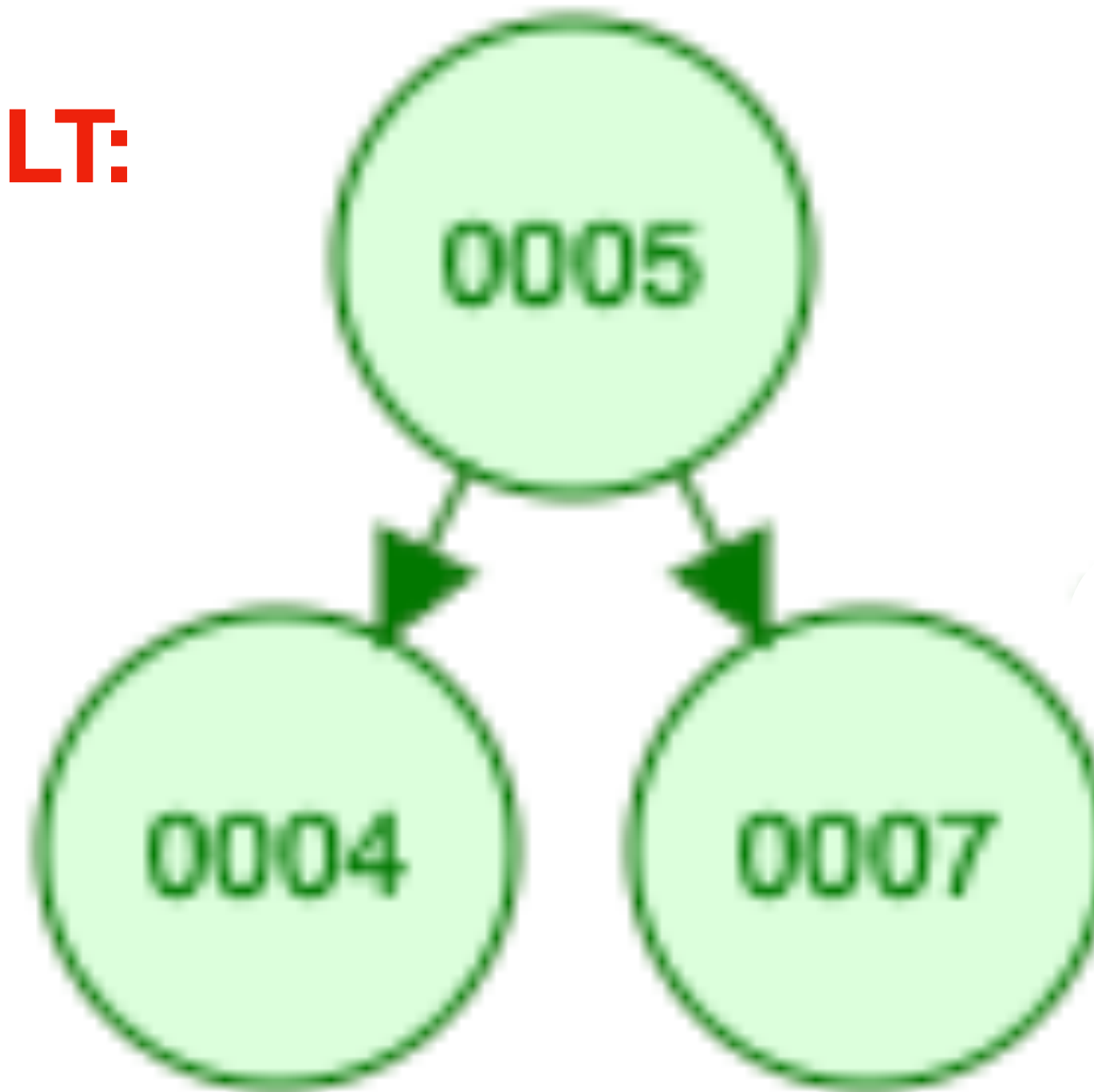
- **Insert(5)**
- **Insert(6)**
- **Insert(7)**
- **Insert(2)**
- **Insert(3)**
- **Insert(4)**
- **Delete(6)**
- **Delete(3)**
- **Delete(2)**

AVL Tree #1

Perform the following AVL Tree commands.

- Insert(5)
- Insert(6)
- Insert(7)
- Insert(2)
- Insert(3)
- Insert(4)
- Delete(6)
- Delete(3)
- Delete(2)

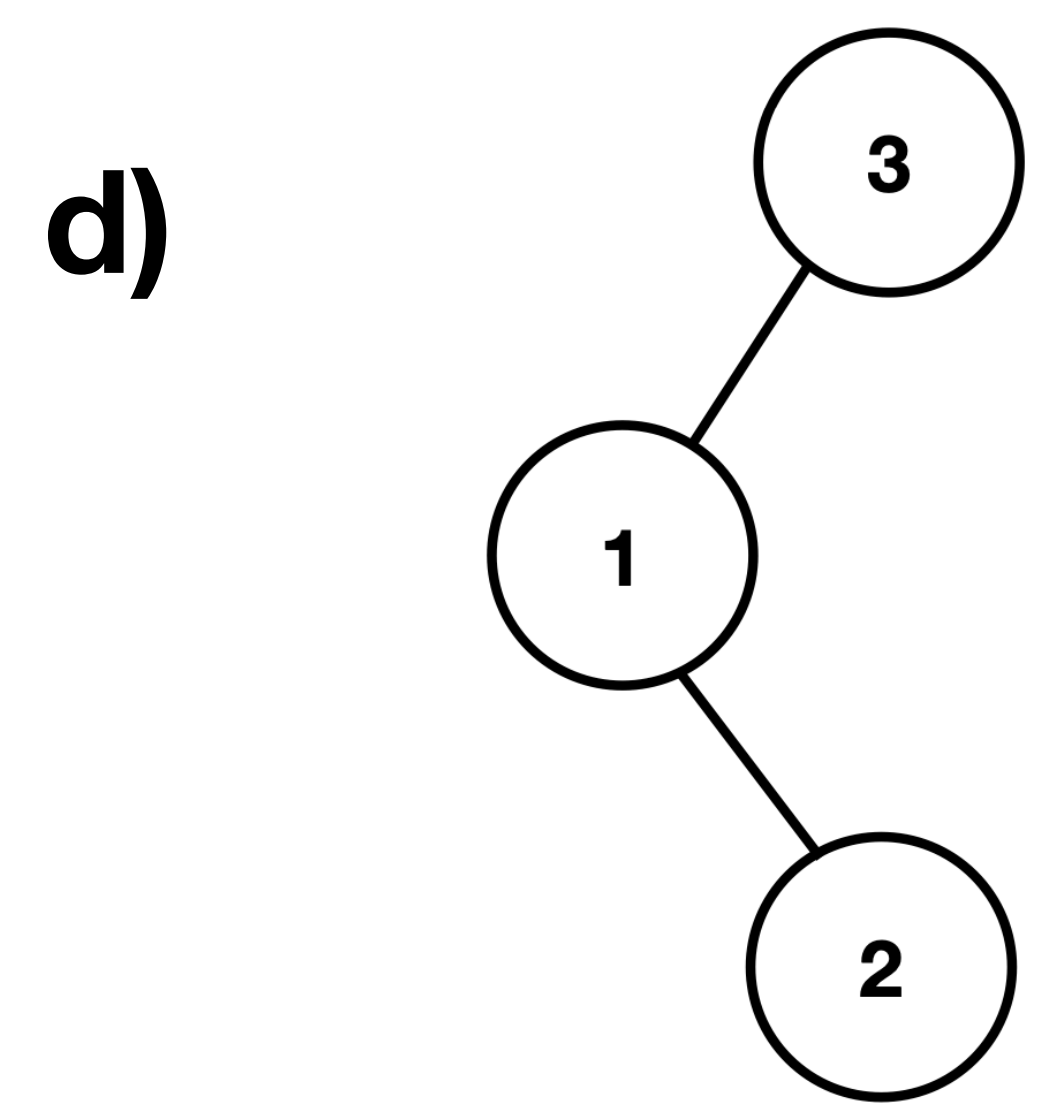
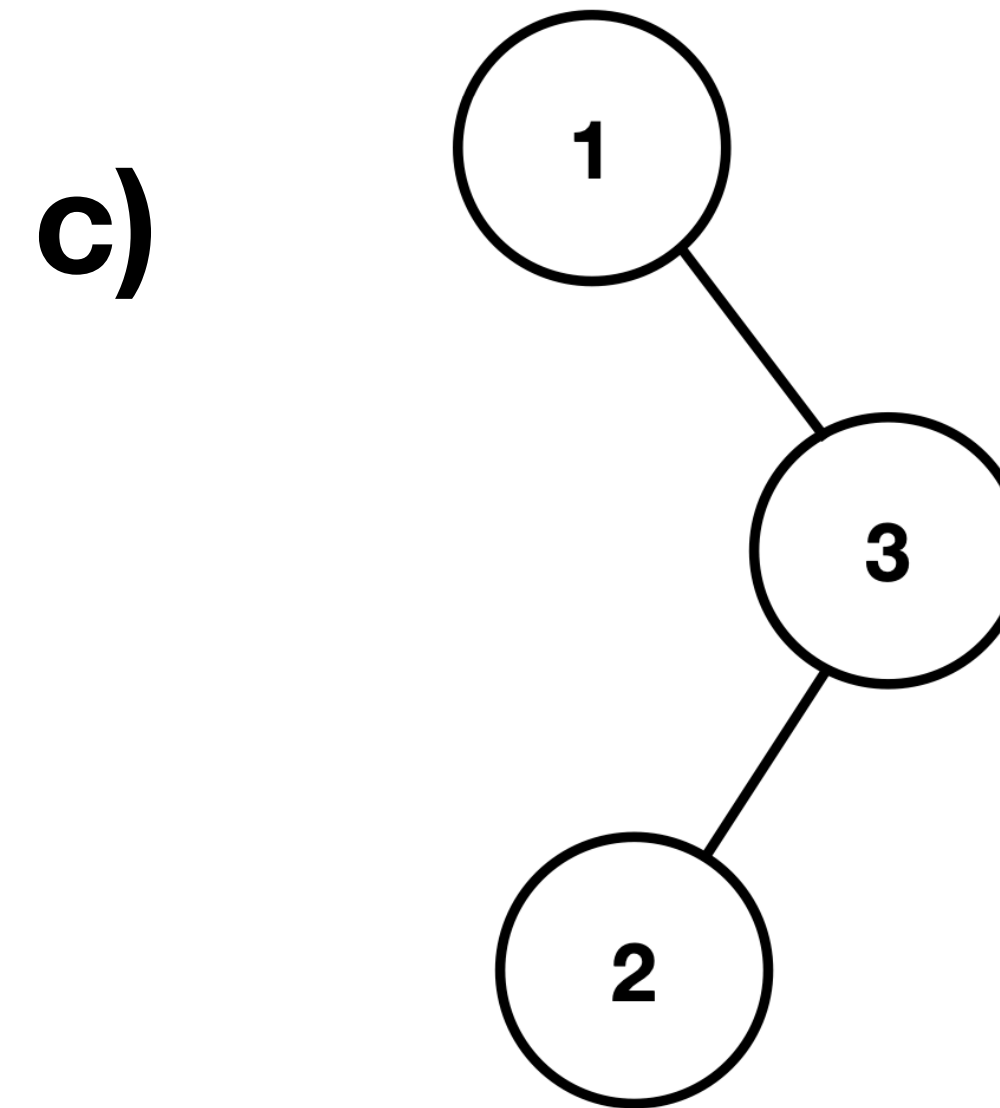
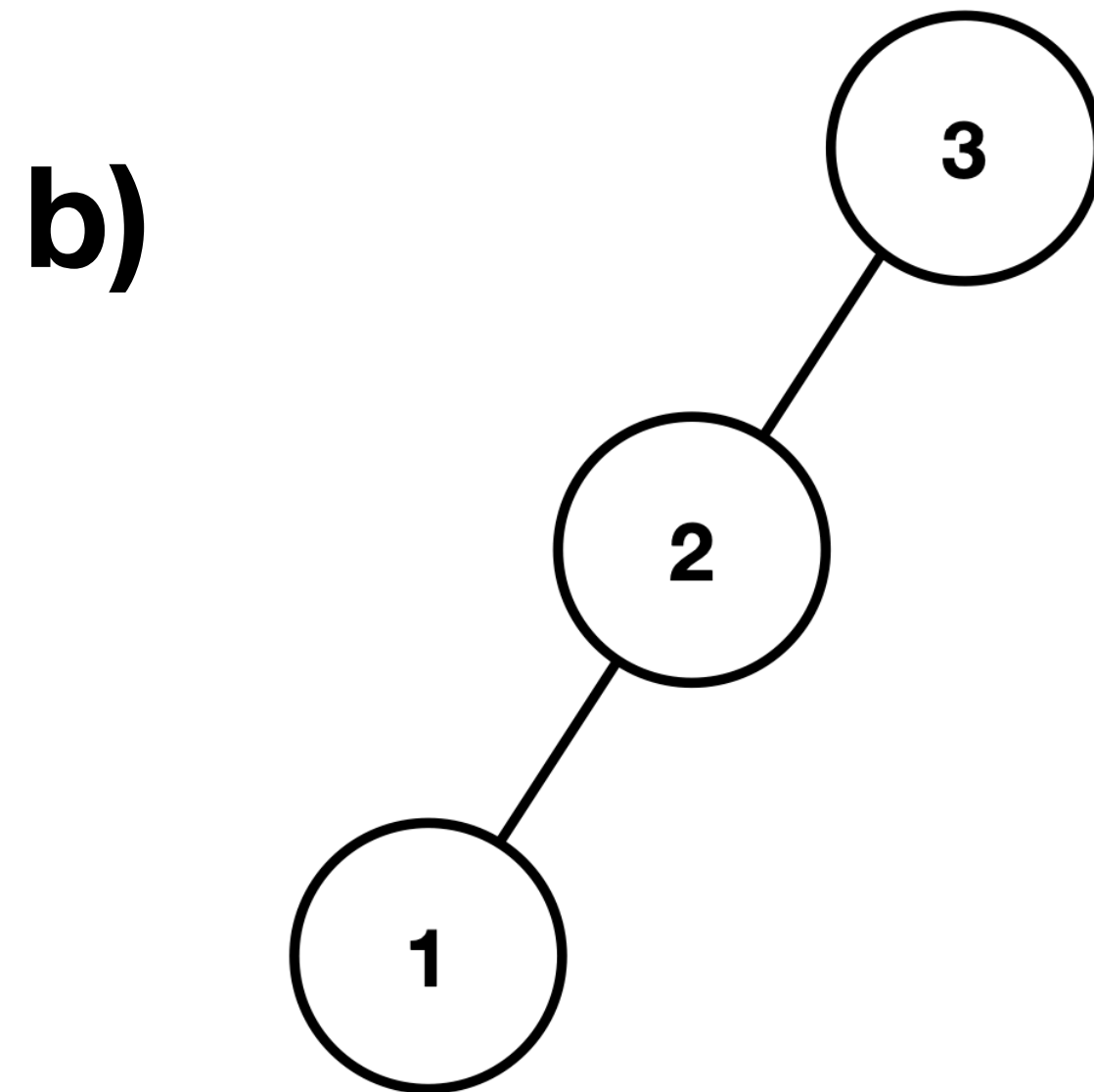
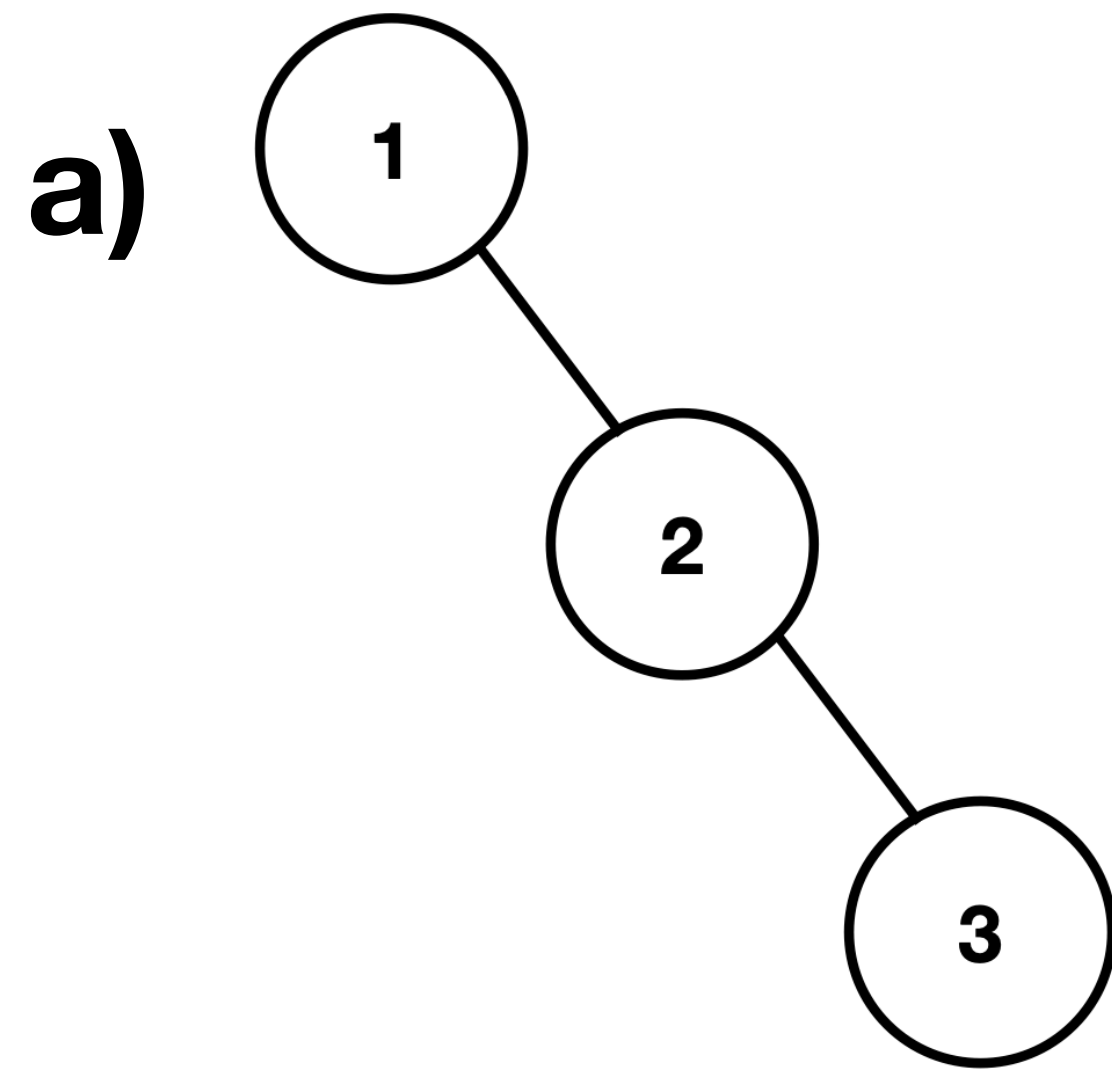
RESULT:



AVL Tree #2

Match the following picture with the rotation that should be performed:

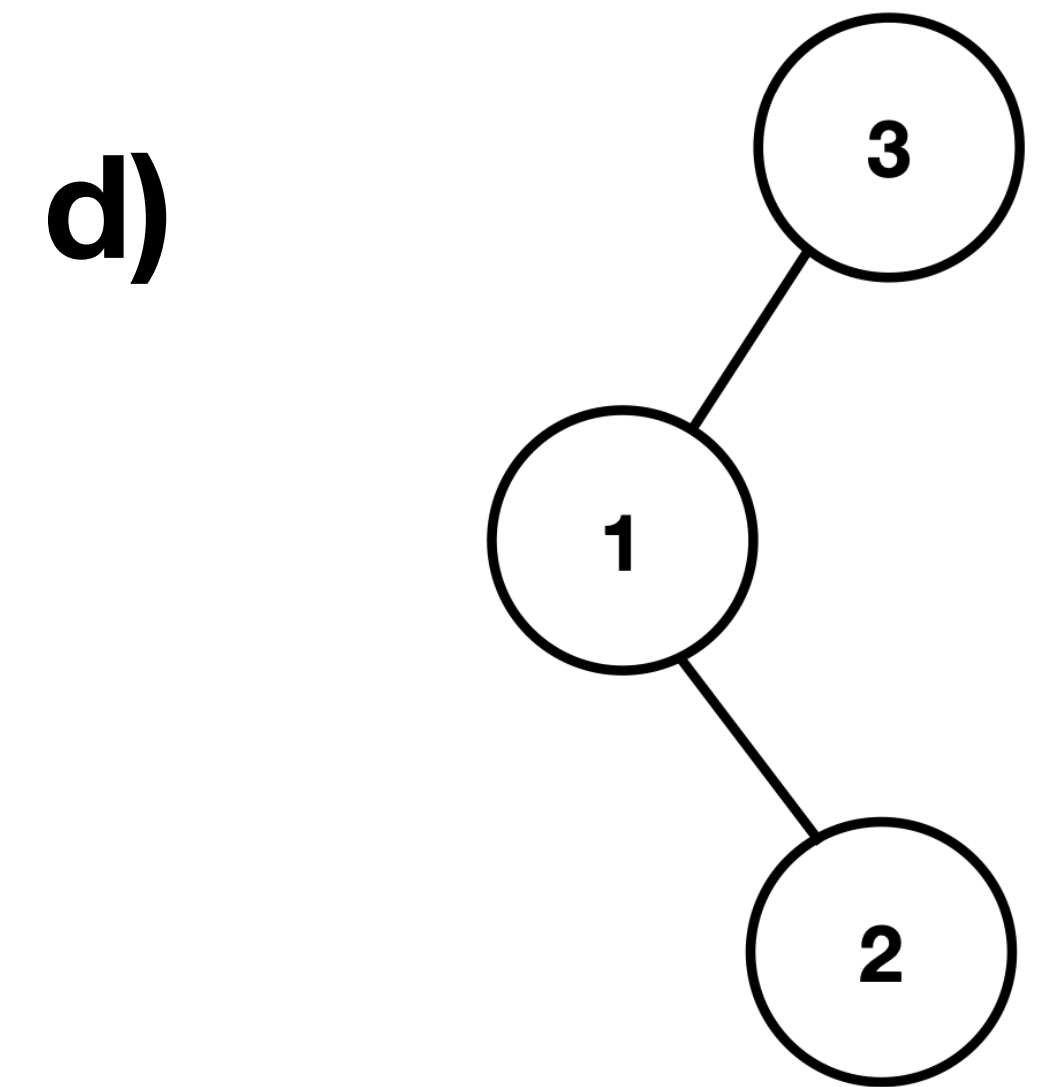
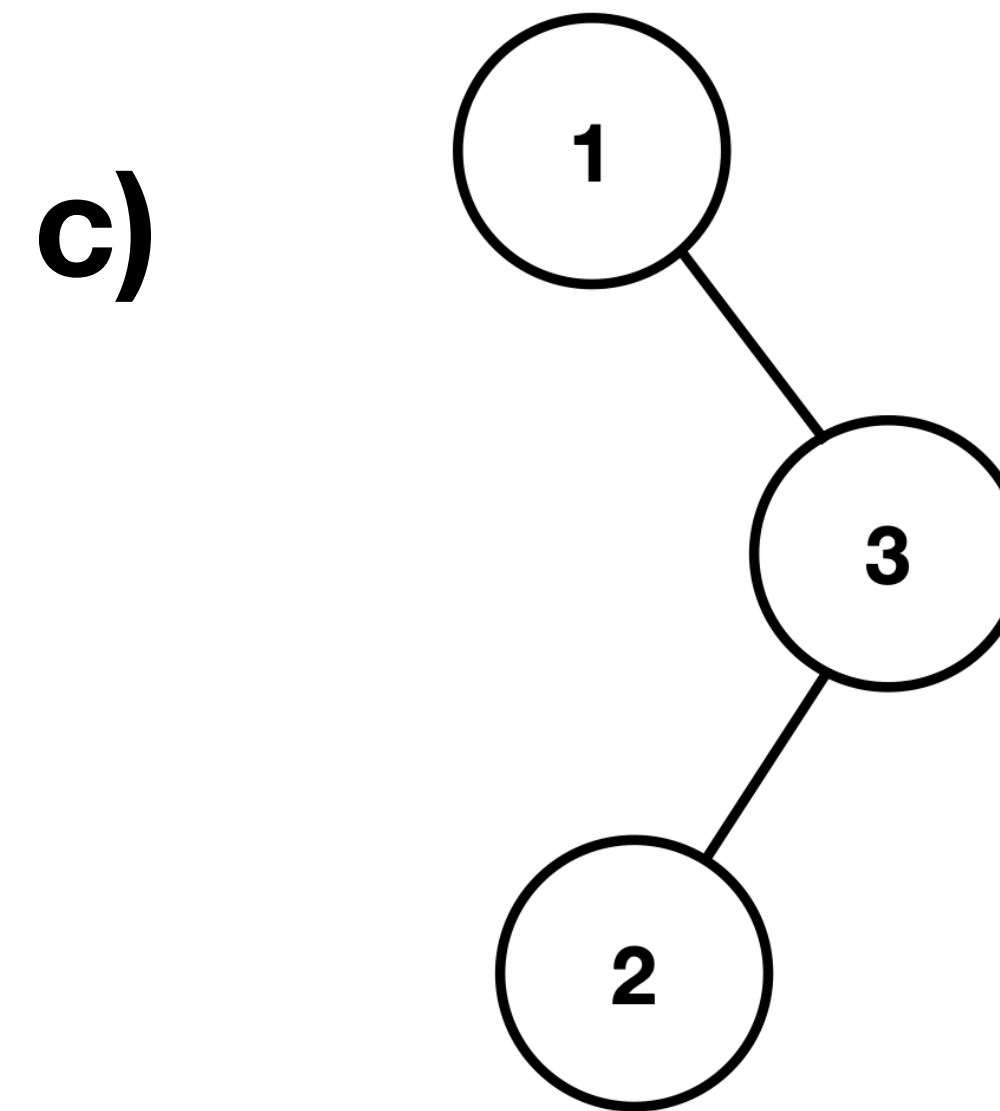
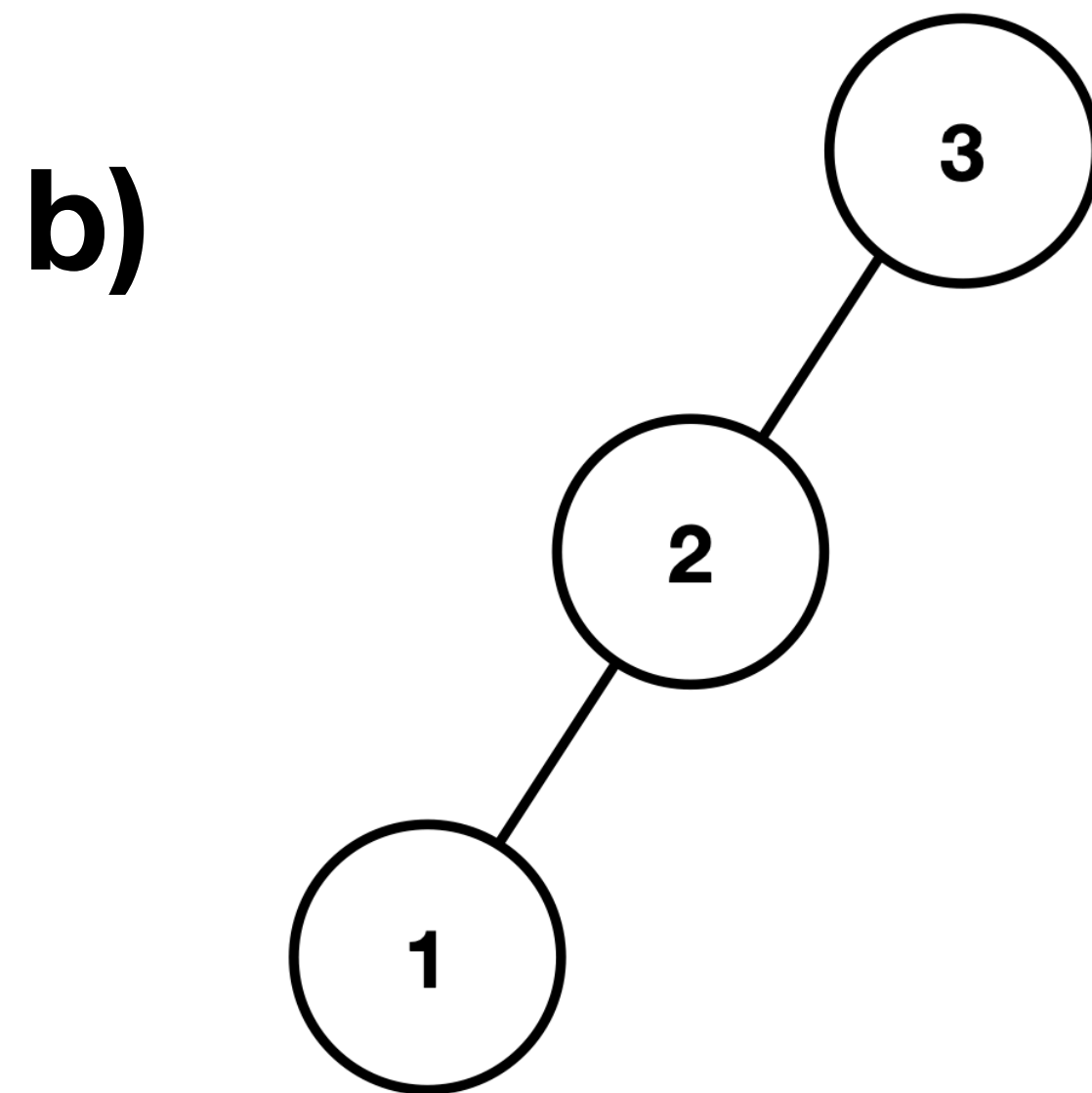
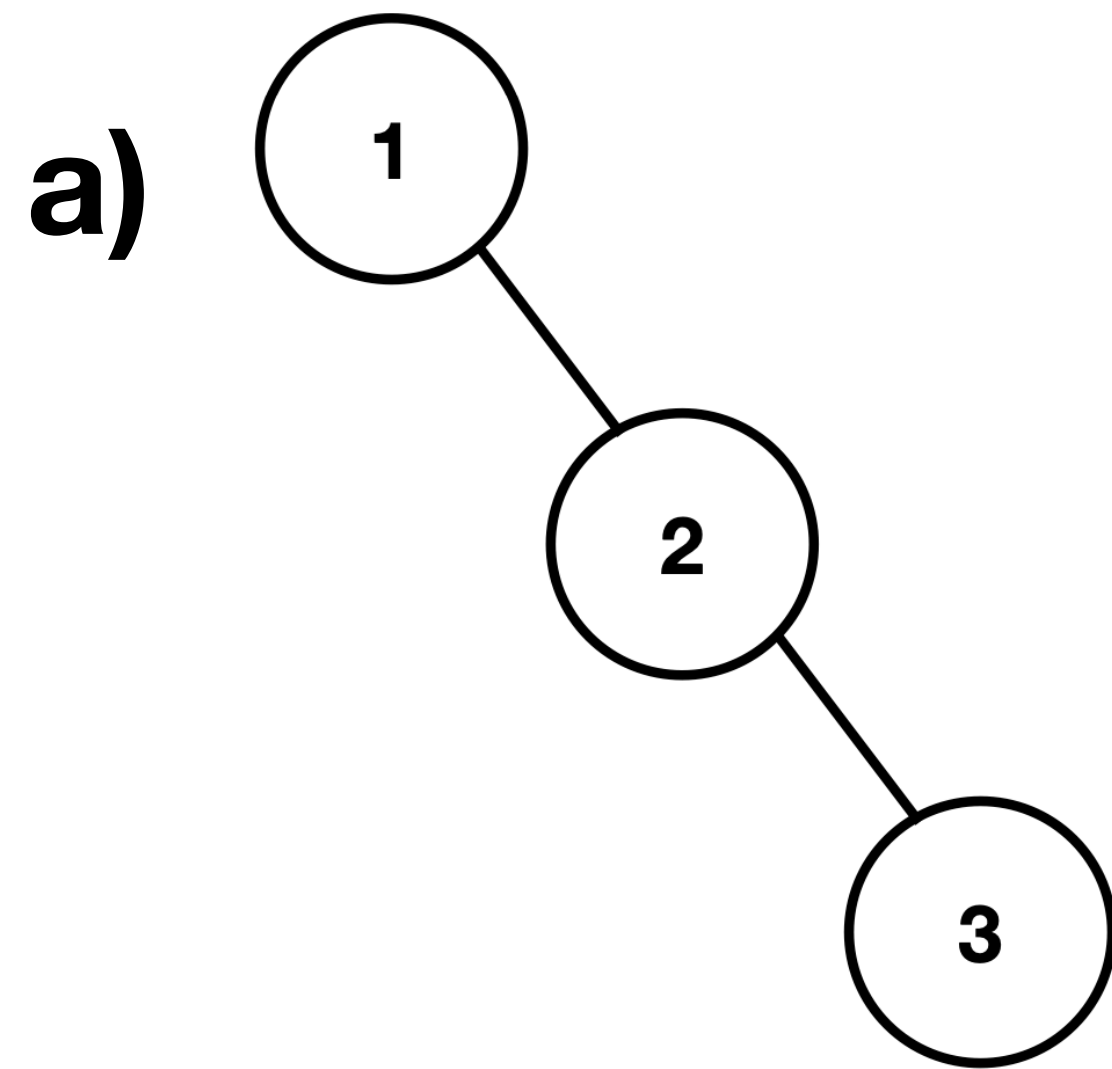
- **Single Right Rotation** _____
- **Single Left Rotation** _____
- **Right Left Rotation** _____
- **Left Right Rotation** _____



AVL Tree #2

Match the following picture with the rotation that should be performed:

- Single Right Rotation **__b__**
- Single Left Rotation **__a__**
- Left Right Rotation **__c__**
- Right Left Rotation **__d__**



AVL Tree #3

Write the function to perform a single left rotation on a given node.

```
node *singleLeftRotation (node *n) {
```

```
}
```

AVL Tree #3

Write the function to perform a single left rotation on a given node.

```
11 ▼ node *singleLeftRotation(node *n){  
12     node *newParent = n->right;  
13     node *newRight = newParent->left;  
14     newParent->left = n;  
15     n->right = newRight;  
16     return newParent;  
17 }
```

AVL Tree #4

Indicate whether the following statements are true or false

- **The acceptable balance factor values for an AVL Tree are: -1, 0, and 1.**
- **The worst case time complexity for an AVL Tree is $O(n)$.**
- **The maximum height of an AVL Tree with 7 nodes is 2.**
- **An AVL Tree is a BST with a self balancing property.**

AVL Tree #4

Indicate whether the following statements are true or false

- The acceptable balance factor values for an AVL Tree are: -1, 0, and 1.

true

- The worst case time complexity for an AVL Tree is $O(n)$.

false

- The maximum height of an AVL Tree with 7 nodes is 2.

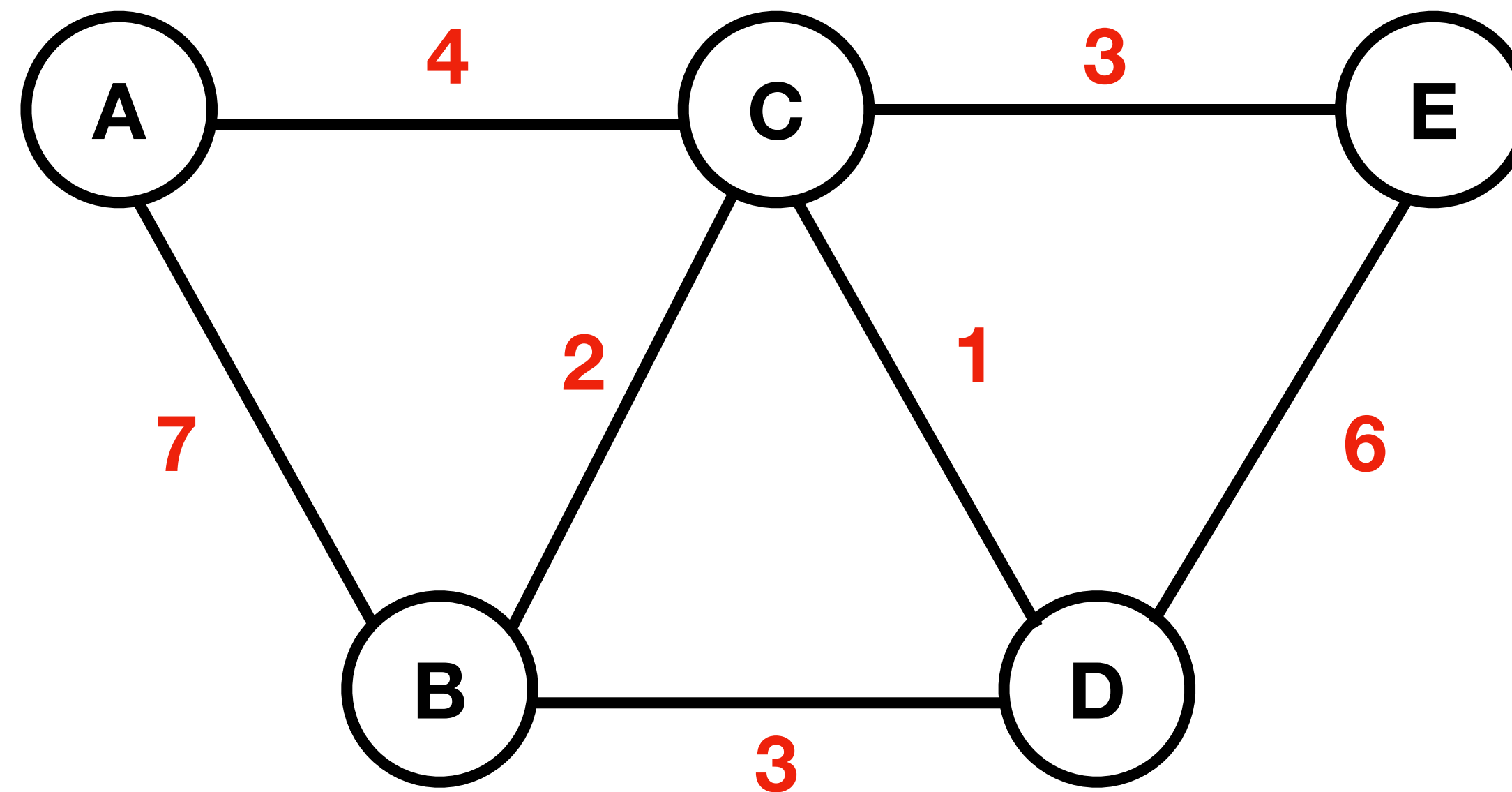
false

- An AVL Tree is a BST with a self balancing property.

true

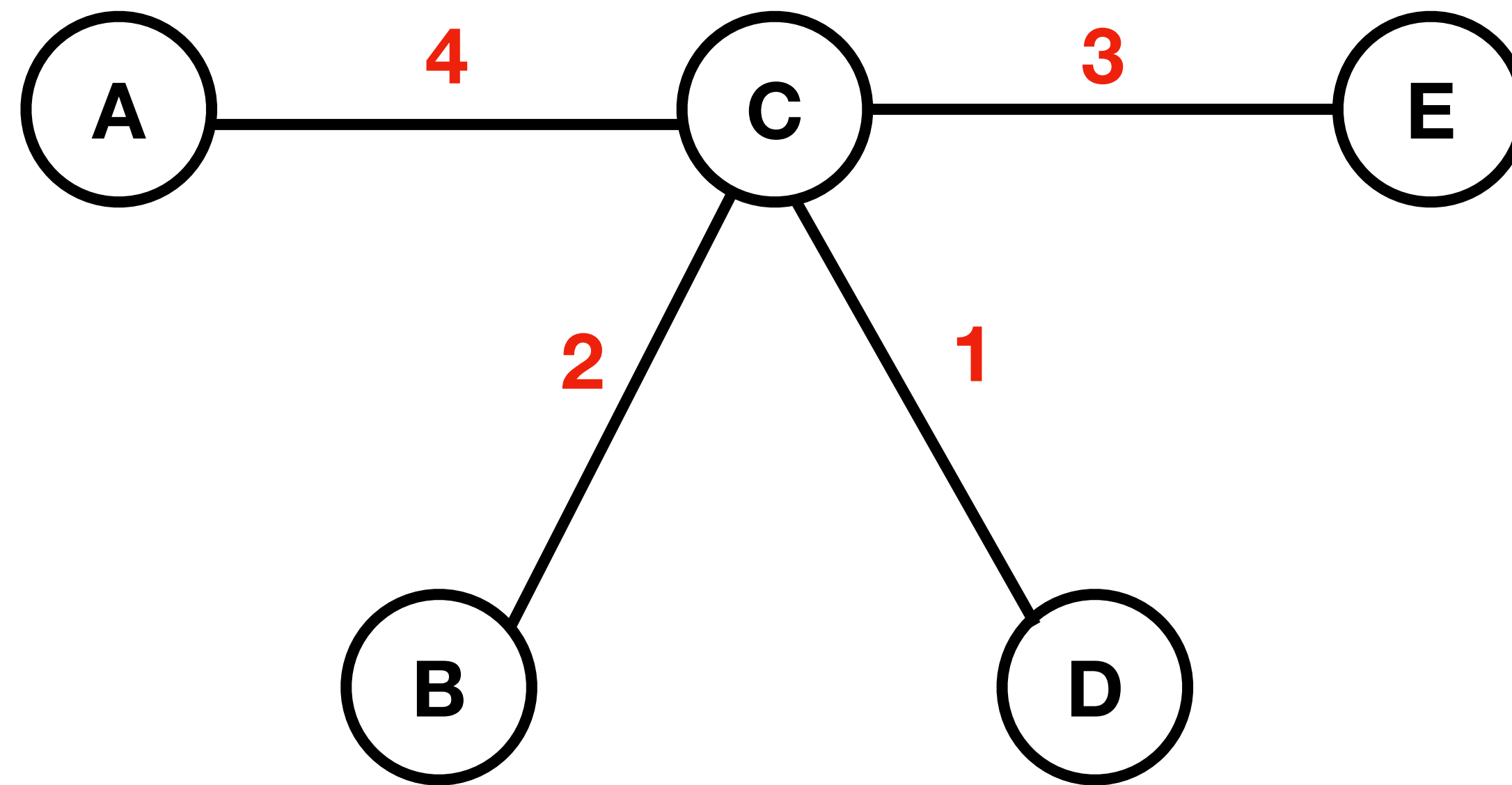
Graphs #1

Find the MST of the following graph using Prim's Algorithm. Start from vertex B.



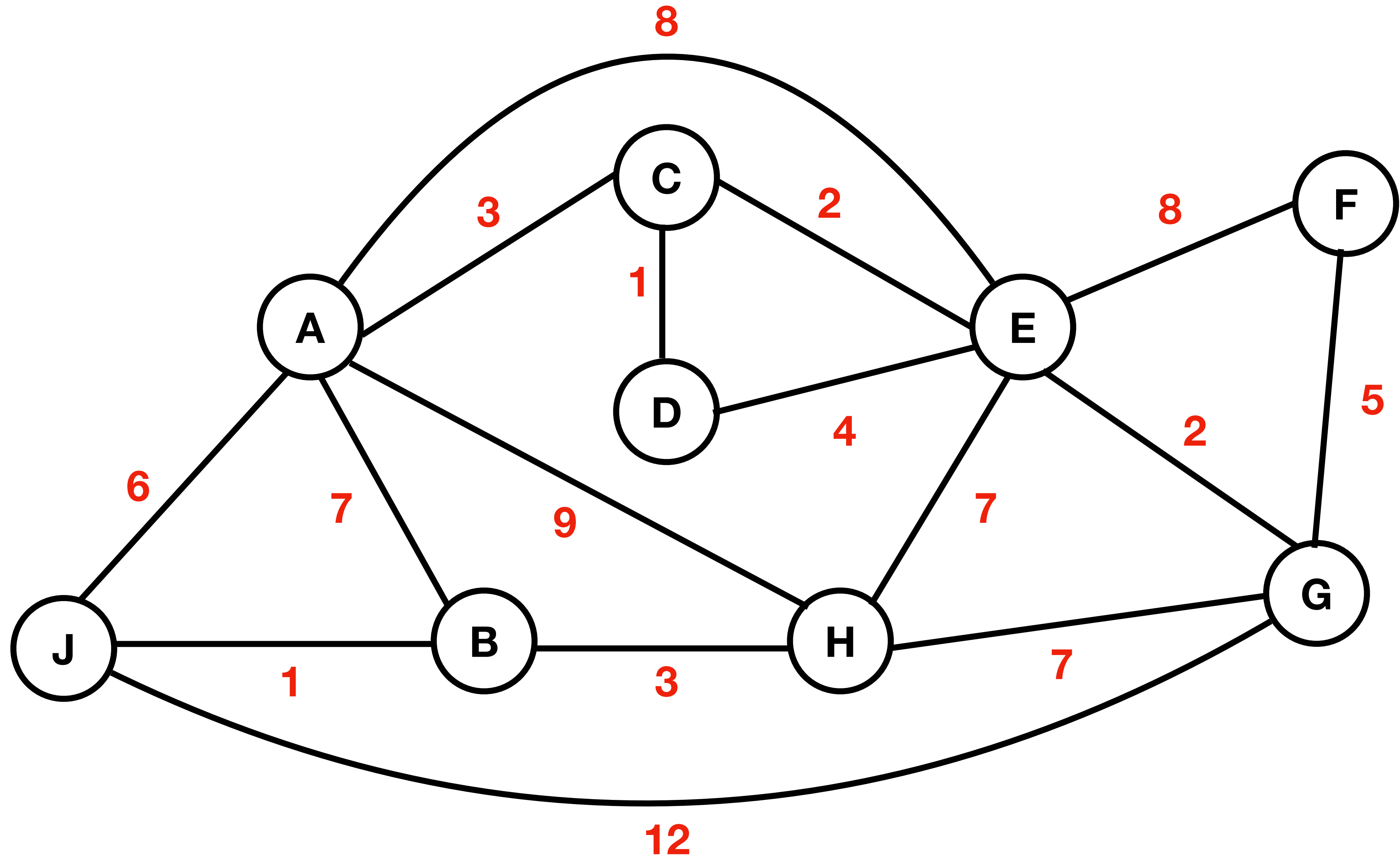
Graphs #1

Find the MST of the following graph using Prim's Algorithm. Start from vertex B.



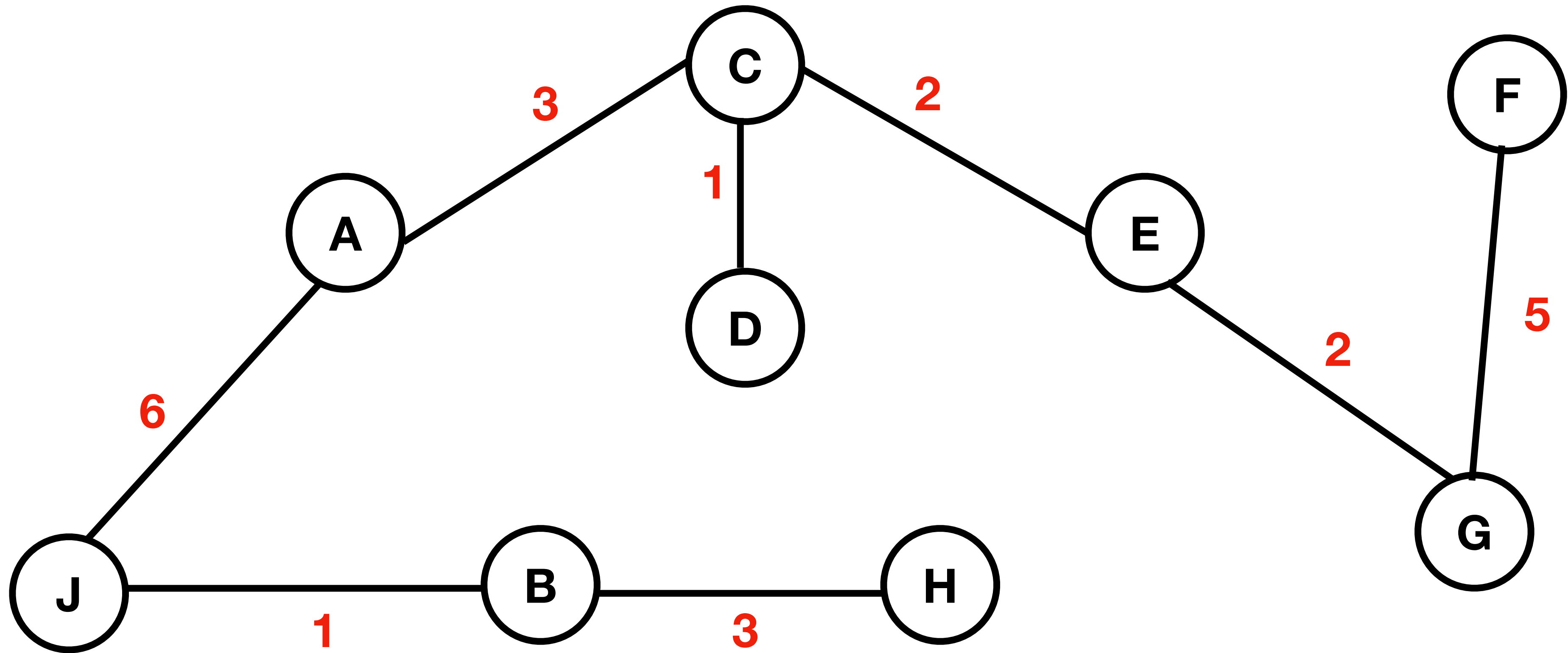
Graphs #2

Find the MST of the following graph using Kruskal's Algorithm.



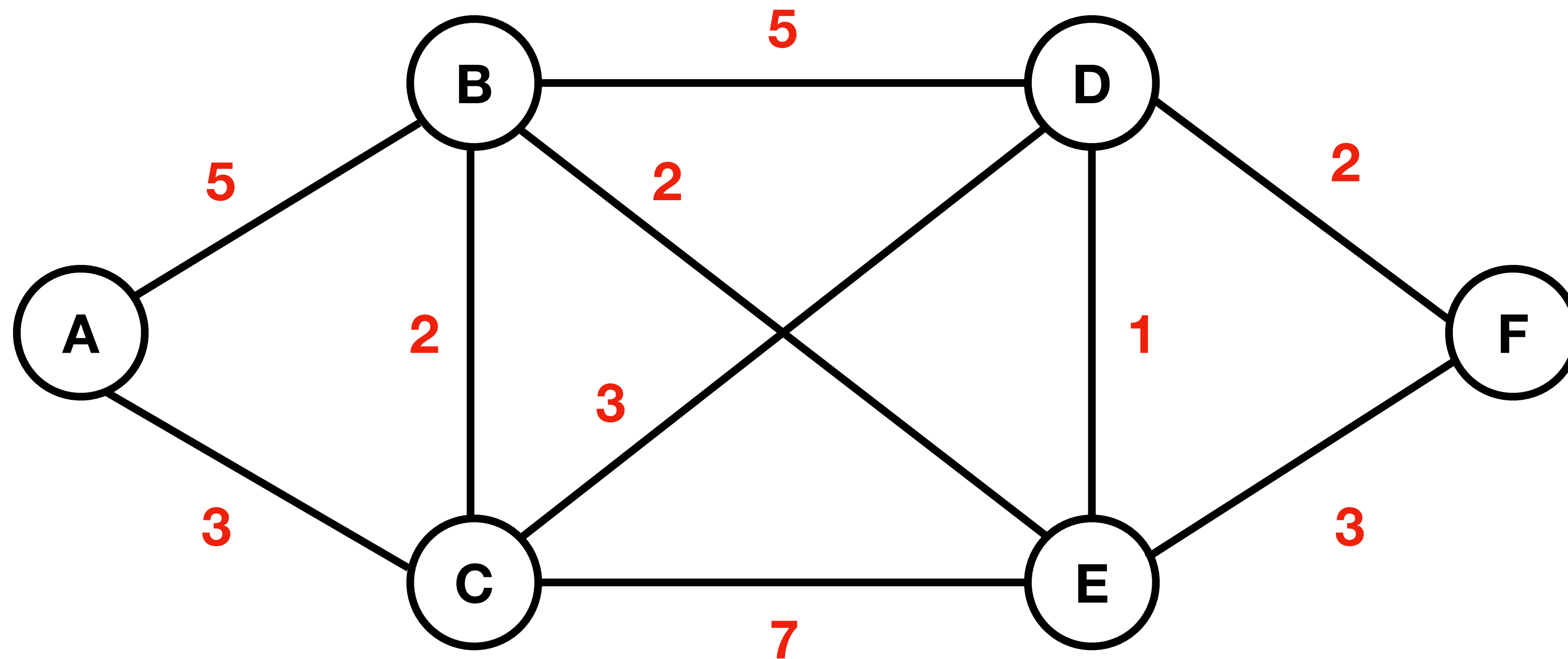
Graphs #2

Find the MST of the following graph using Kruskal's Algorithm.



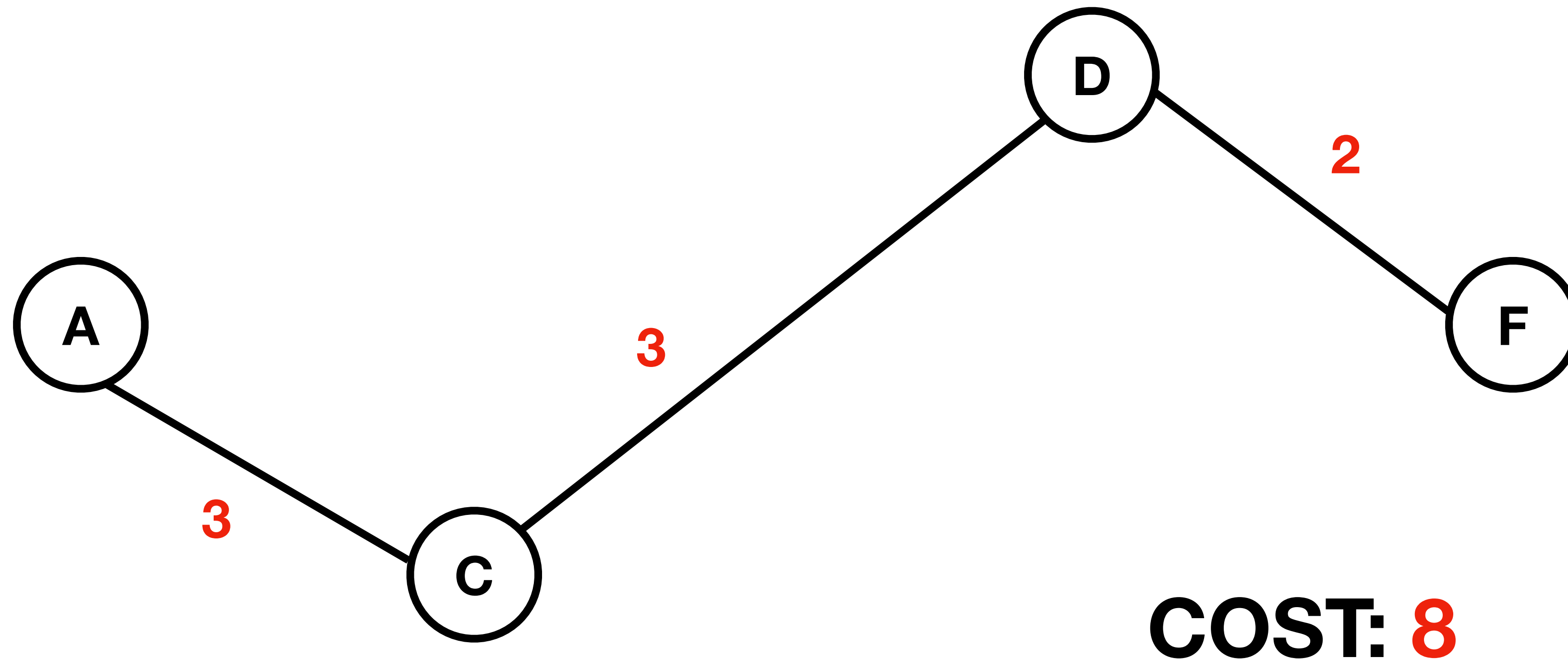
Graphs #3

Find the shortest path from vertex A to vertex F with minimum cost.



Graphs #3

Find the shortest path from vertex A to vertex F with minimum cost.



Graphs #4

Write DFS for an adjacency matrix.

```
void DFS(int **graph, int source, int n) {
```

```
}
```

Graphs #4

```
void DFS(int **graph, int source, int n){
    stack<int> s;
    bool *visited = new bool[n];
    for(int i = 0; i < n; i++)
        visited[i] = false;
    s.push(source);
    while(!s.empty()){
        int v = s.top();
        s.pop();
        if(!visited[v]){
            cout << v << " ";
            visited[v] = true;
        }
        for(int i = 0; i < n; i++){
            if(graph[v][i] != 0 && !visited[i])
                s.push(i);
        }
    }
    cout << endl;
    delete [] visited;
}
```

Graphs #5

Is the following unweighted graph directed or undirected? Explain.

0	1	0	1	0	0	1
1	0	1	0	1	0	0
0	1	0	0	1	0	0
1	0	0	0	0	0	0
0	1	1	0	0	1	0
0	0	0	0	0	1	0
1	0	0	0	1	0	0

Graphs #5

Is the following unweighted graph directed or undirected? Explain.

Directed

0	1	0	1	0	0	1
1	0	1	0	1	0	0
0	1	0	0	1	0	0
1	0	0	0	0	0	0
0	1	1	0	0	1	0
0	0	0	0	0	1	0
1	0	0	0	1	0	0

Stack & Queue #1

Implement an enqueue function using two stacks. No other data structure is allowed.

```
class Queue{
    private:
        stack<int> s1;
        stack<int> s2;
    public:
        void push(int x) ;
};

void Queue::enqueue(int x) {

}
```

Stack & Queue #1

```
void Queue::enqueue(int x) {  
    while(!s1.empty()) {  
        s2.push(s1.top());  
        s1.pop();  
    }  
    s1.push(x);  
    while(!s2.empty()) {  
        s1.push(s2.top());  
        s2.pop();  
    }  
}
```


Stack & Queue #2

Write a function to delete all of the occurrences of a certain value from a queue. You are only allowed one additional variable.

```
void deleteAll(queue<int> &q, int x) {
```

```
}
```

Stack & Queues #2

```
7 ▼ void deleteAll(queue<int> &q, int x){  
8     int size = q.size();  
9 ▼ while(size > 0){  
10         if(q.front() != x)  
11             q.push(q.front());  
12         q.pop();  
13         size--;  
14     }  
15 }
```

Stack & Queue #3

Write a function that returns the minimum value of a stack and has a time complexity of $O(1)$.

```
class Stack{
    private:
        stack<int> s;
    public:
        void push(int x) ;
        int getMin() ;
};

void Stack::push(int x) {

}

int Stack::getMin() {

}
```

Stack & Queue #3

```
int Stack::getMin(){  
    if(!s.empty())  
        return s.top();  
    else  
        return -1000;  
}
```

```
void Stack::push(int x){  
    if(s.empty())  
        s.push(x);  
    else{  
        if(x <= s.top())  
            s.push(x);  
        else{  
            stack<int> tempStack;  
            while(!s.empty() && x > s.top()){  
                tempStack.push(s.top());  
                s.pop();  
            }  
            s.push(x);  
            while(!tempStack.empty()){  
                s.push(tempStack.top());  
                tempStack.pop();  
            }  
        }  
    }  
}
```

Sorting #1

Perform heap sort on the array below. Sort the numbers in ascending order.

{4, 1, 2, 9, 5, 8, 3}

Sorting #1

Perform heap sort on the array below. Sort the numbers in ascending order.

{1, 2, 3, 4, 5, 8, 9}

Sorting #2

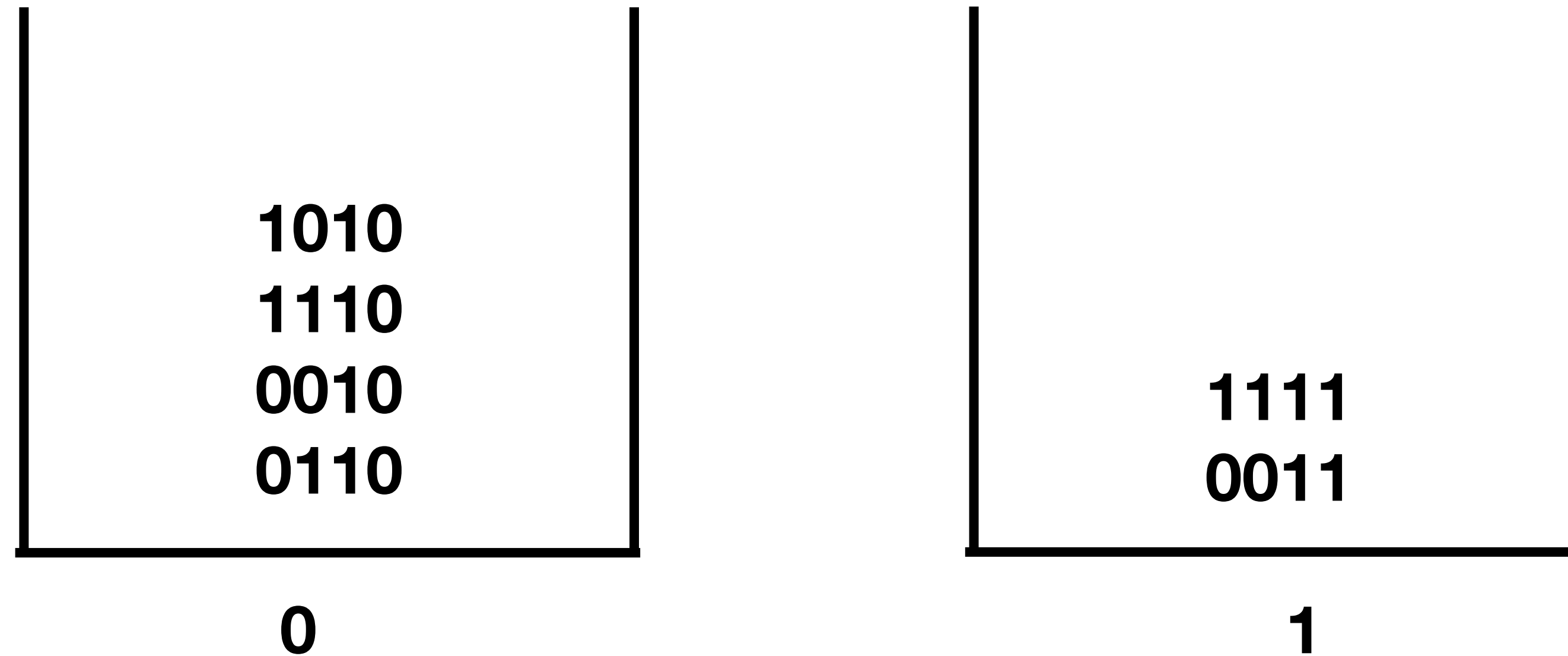
Perform bucket sort on the array of binary numbers below.

{0110, 0010, 0011, 1111, 1110, 1010}

Sorting #2

Perform bucket sort on the array of binary numbers below.

{0110, 0010, 0011, 1111, 1110, 1010}



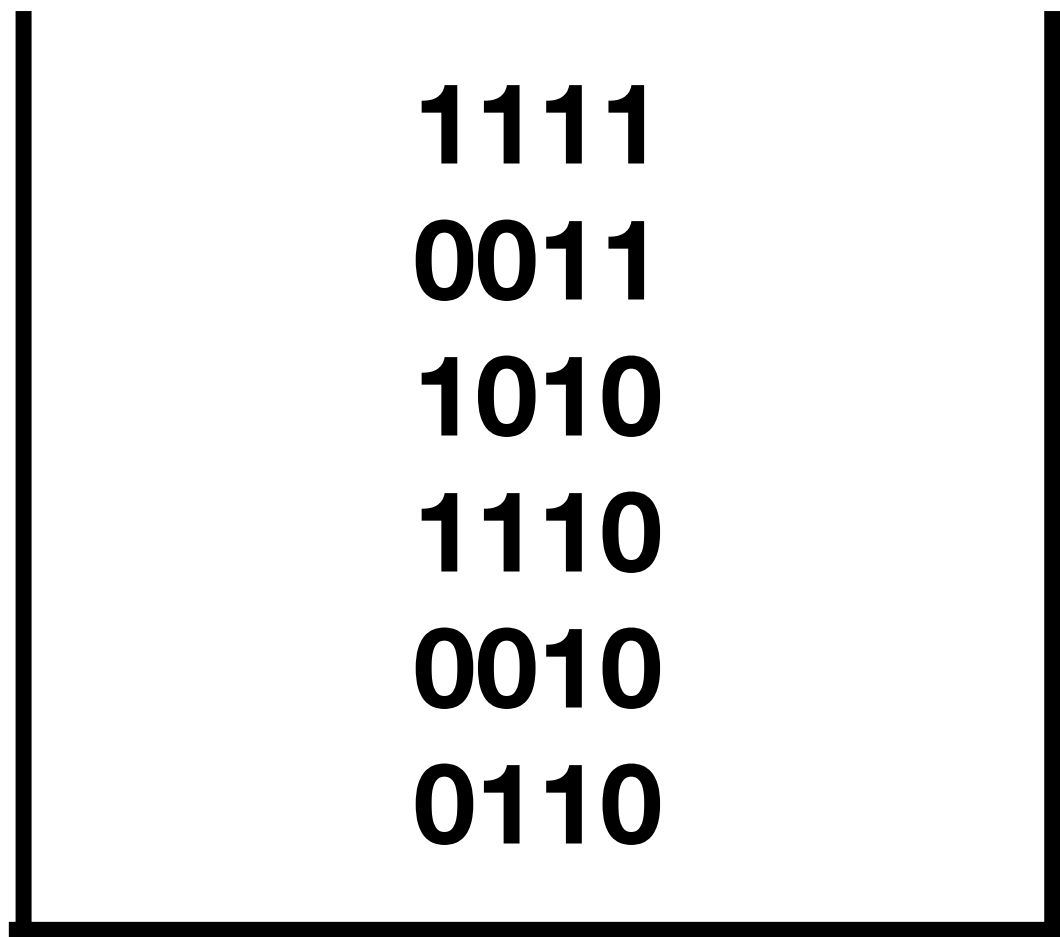
0110, 0010, 1110, 1010, 0011, 1111

Sorting #2

0110, 0010, 1110, 1010, 0011, 1111



0

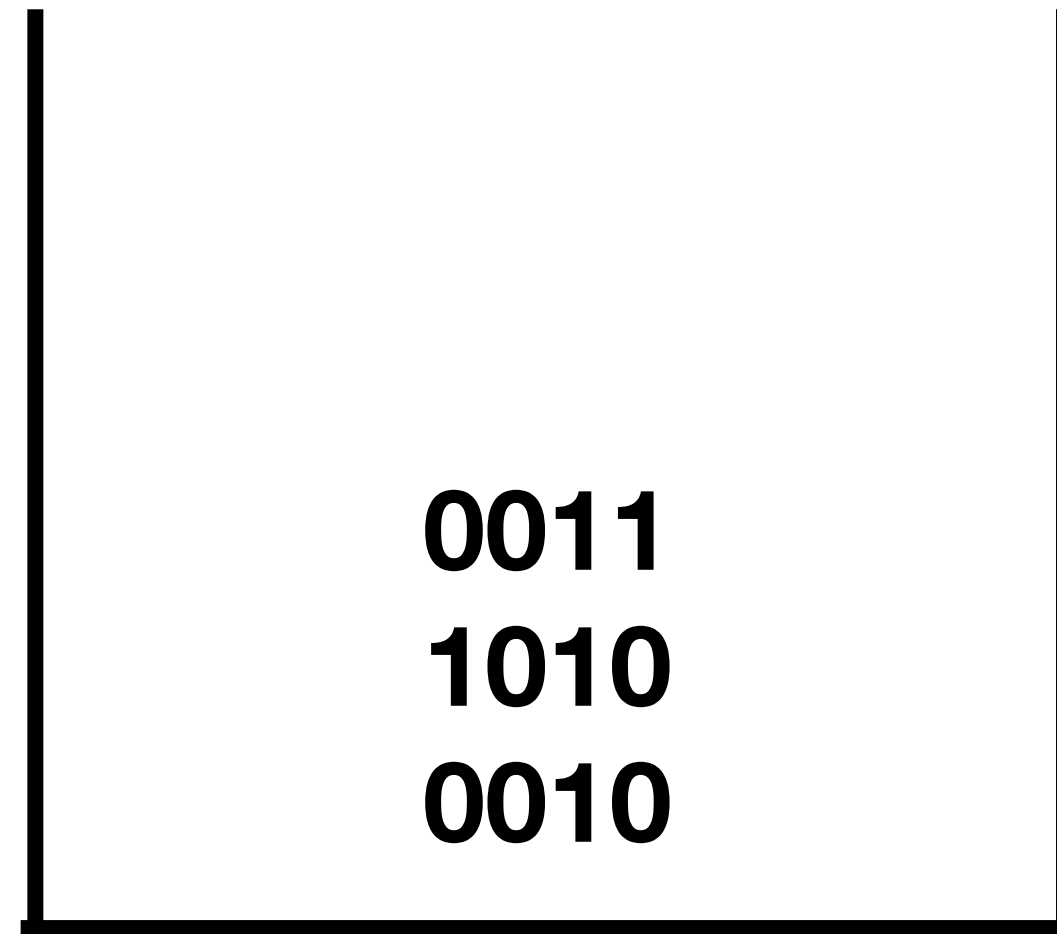


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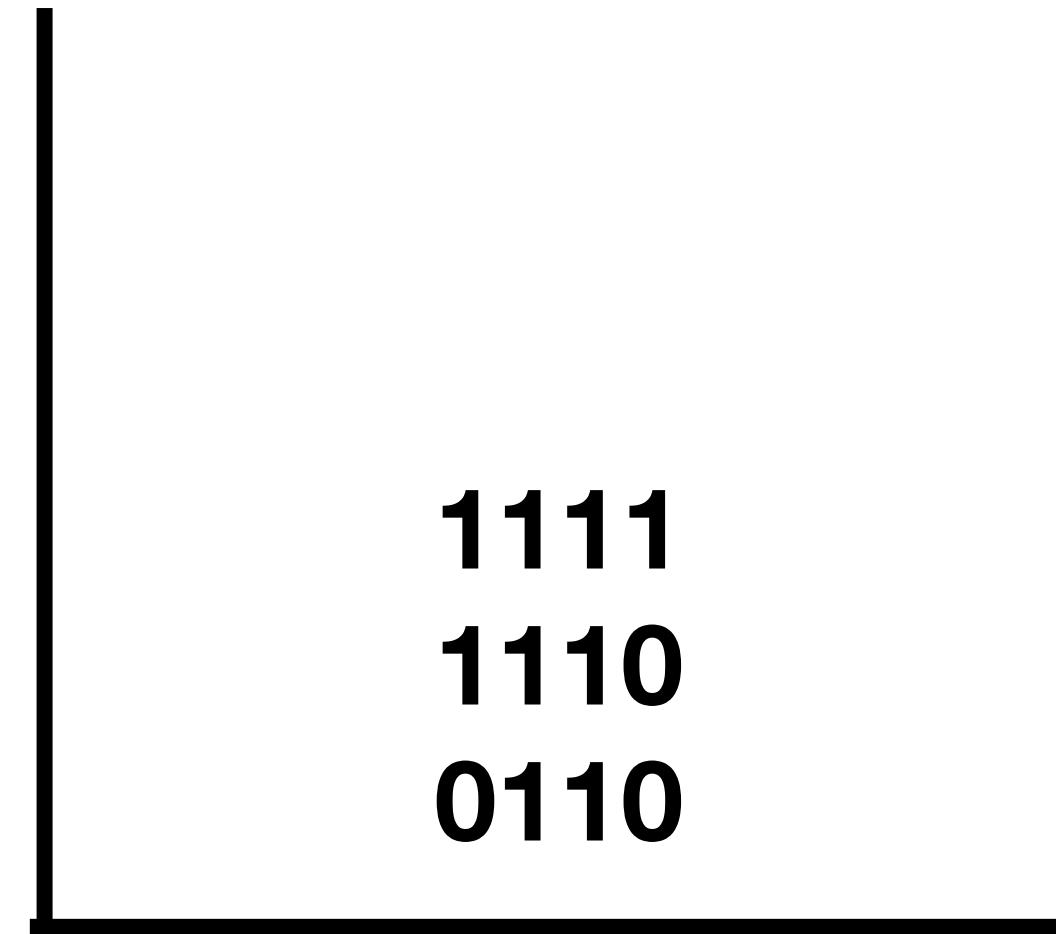
0110, 0010, 1110, 1010, 0011, 1111

Sorting #2

0110, 0010, 1110, 1010, 0011, 1111



0

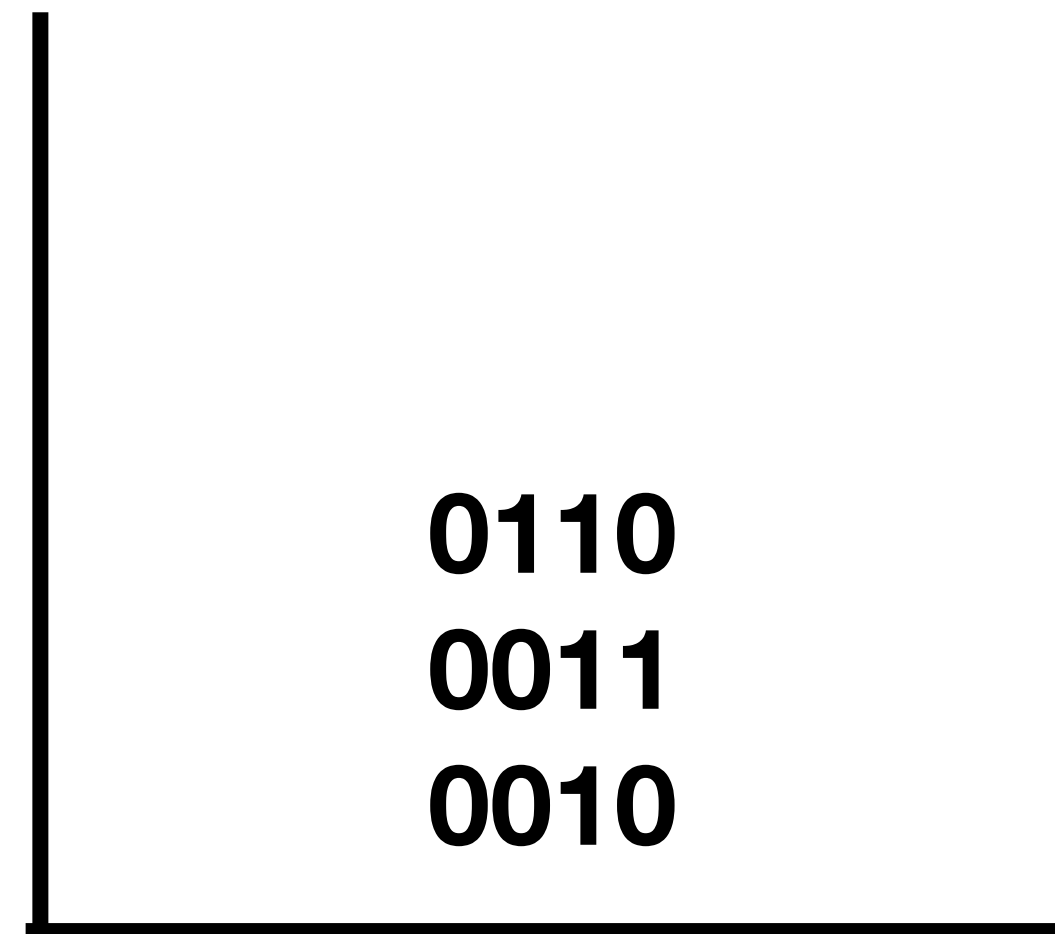


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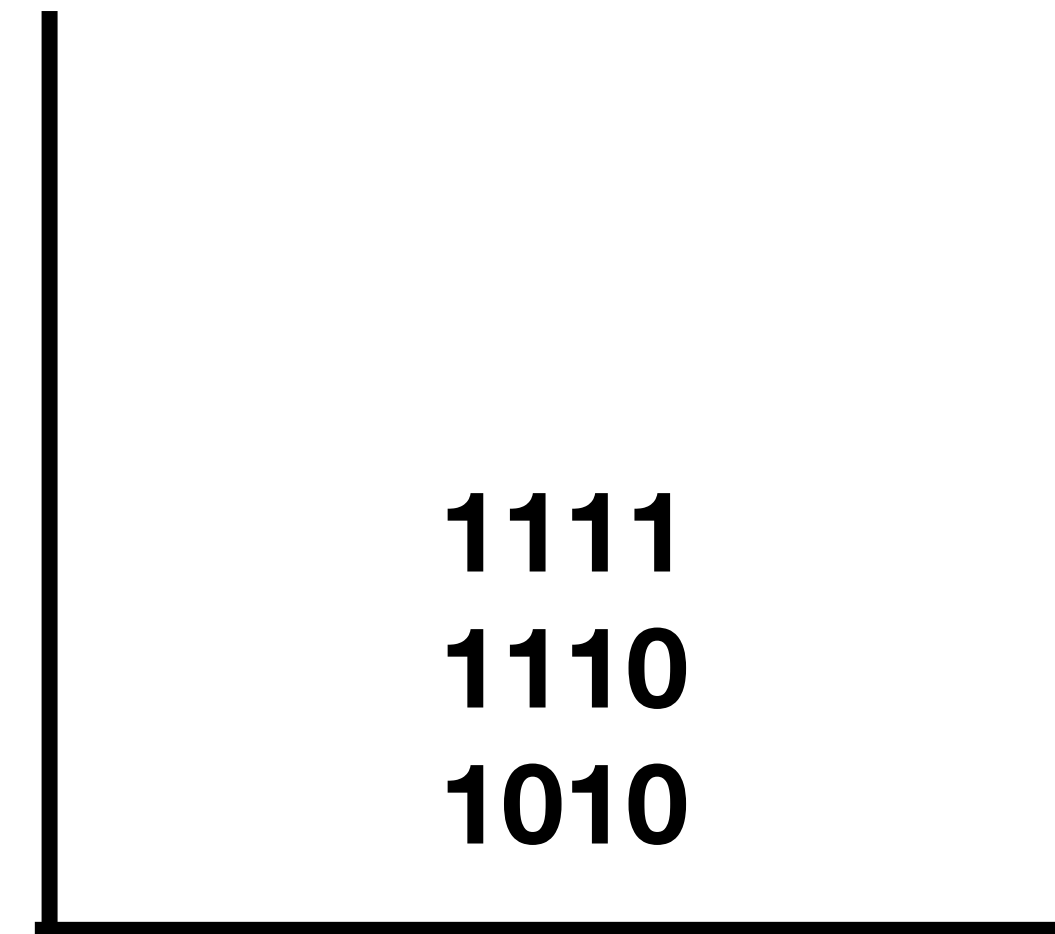
0010, 1010, 0011, 0110, 1110, 1111

Sorting #2

0010, 1010, 0011, 0110, 1110, 1111



0



1

FINAL ANSWER: 0010, 0011, 0110, 1010, 1110, 1111

Hashing Review

- **Know how to trace and code the following hashing methods:**
 - **Quadratic Probing**
 - **Linear Probing**
 - **Direct Hashing**
 - **Double Hashing**
 - **Separate Chaining**

BST & AVL Tree Review

- **Know how to perform inOrder, reverseOrder, postOrder, and preOrder traversals**
- **Know how to do basic BST & AVL Tree functions (insert, search, height, balance, delete, etc.)**
- **Know how to trace insert and delete for AVL tree**
- **Know the rotations for AVL Tree**

Graph Review

- **Know how to trace Prim's, Kruskal's and Dijkstra's**
- **Know how to code BFS and DFS**
- **Know the basics of adjacency matrix and adjacency list**

Stack & Queue Review

- **Know the basic stack and queue functions (push(), pop(), top(), front(), size(), empty(), etc.)**

Sorting Review

- **Know how to trace the different sorting algorithms covered this semester**

Final Remarks

- **You will have 3 hours to take the final exam**
- **Bring your own pencil(s) to take the final exam**
- **For more practice, review the documents found on BlackBoard**