Linear-Time Suffix-Sorting Proseminar Datenkompression

WS 16/17 - Clemens Damke

Problemstellung

Problemstellung

Lösungsansätze

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GSACA

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Performance

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Performance

Rückblick

Problemstellung

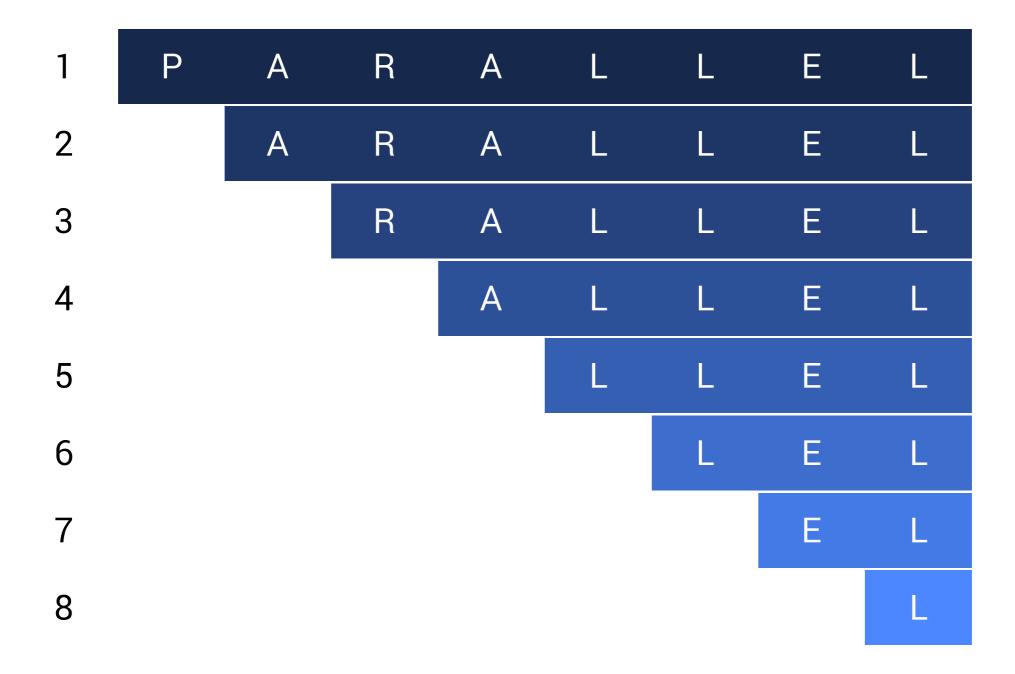
Konstruktion eines Suffix Arrays mit

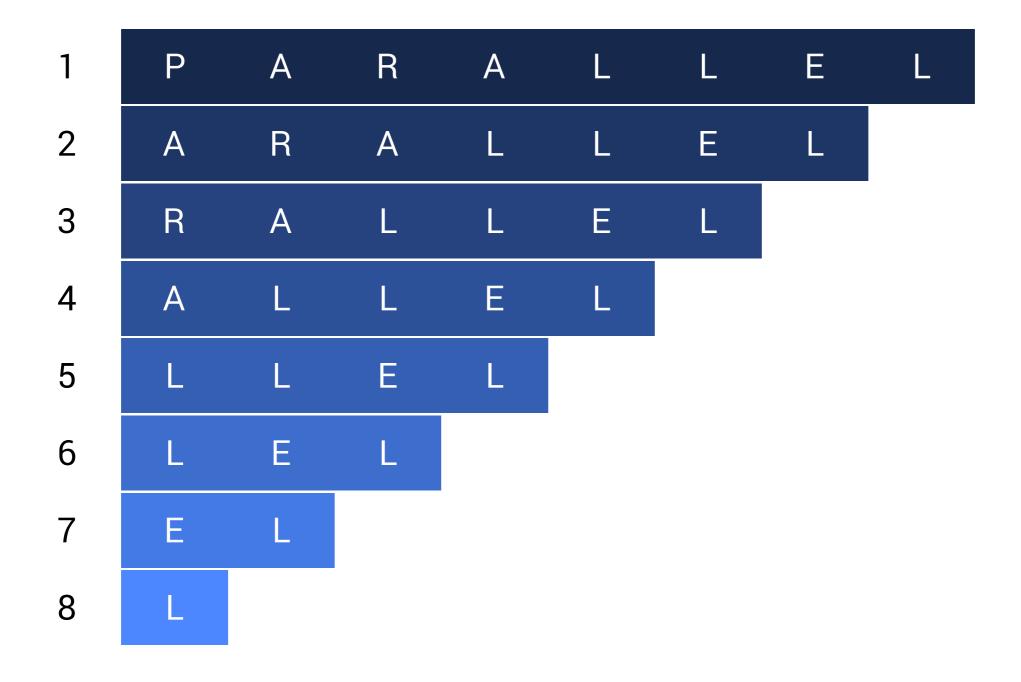
einem rekursionsfreien Linearzeit-Algorithmus.

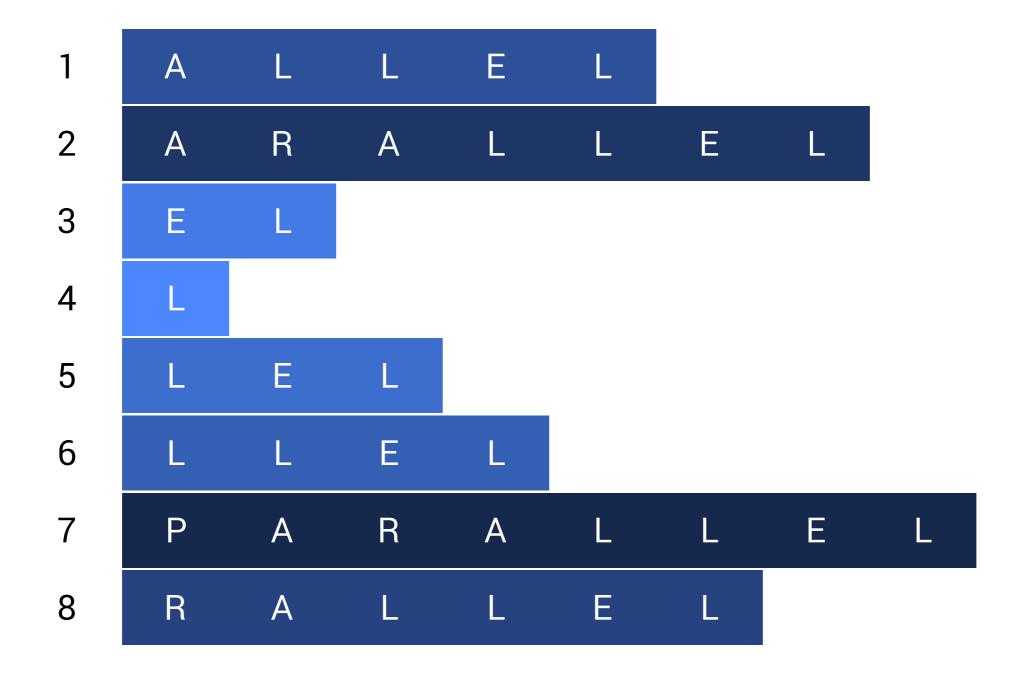
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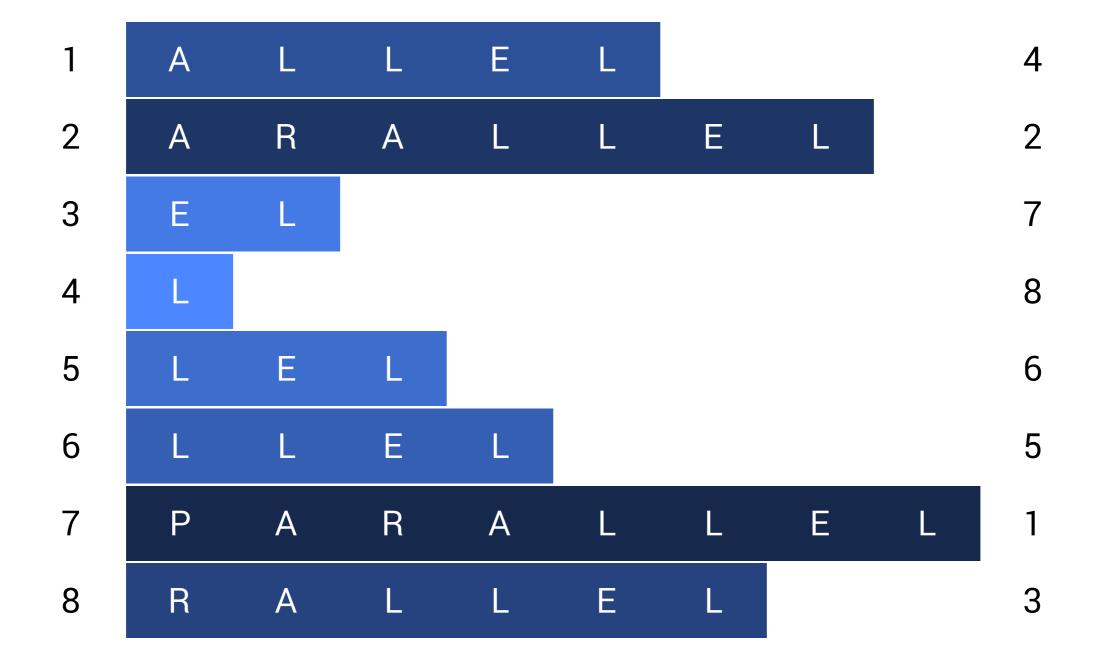
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P A R A L L E L



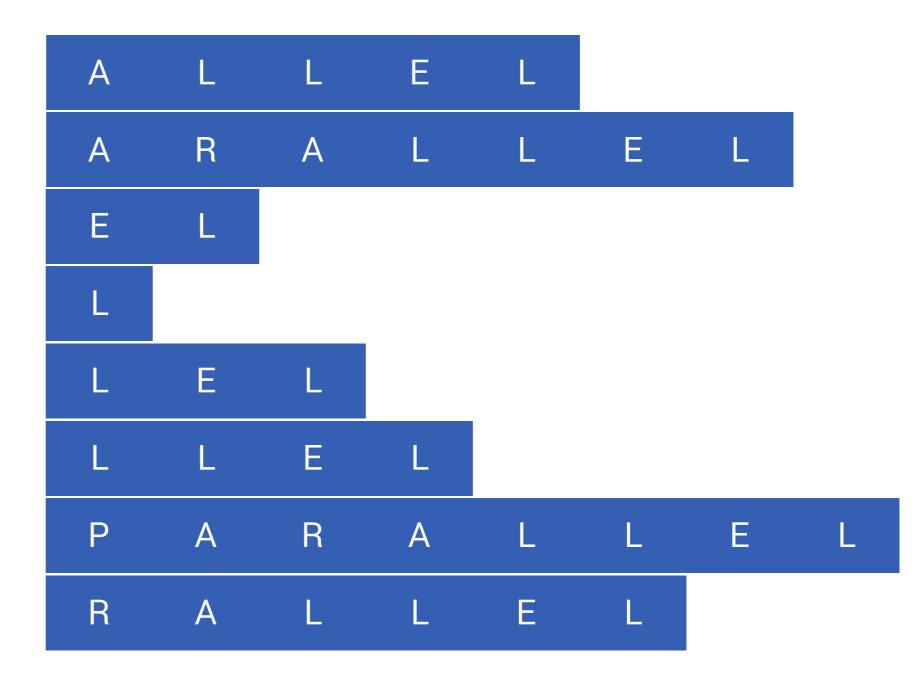






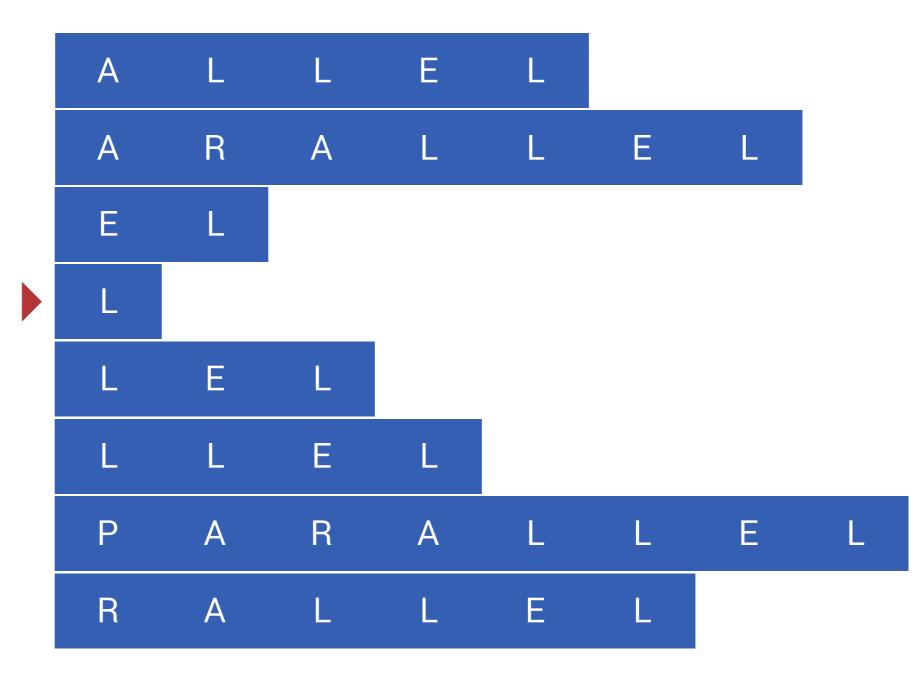
Substringsuche

Ist *alle* in *parallel* enthalten?



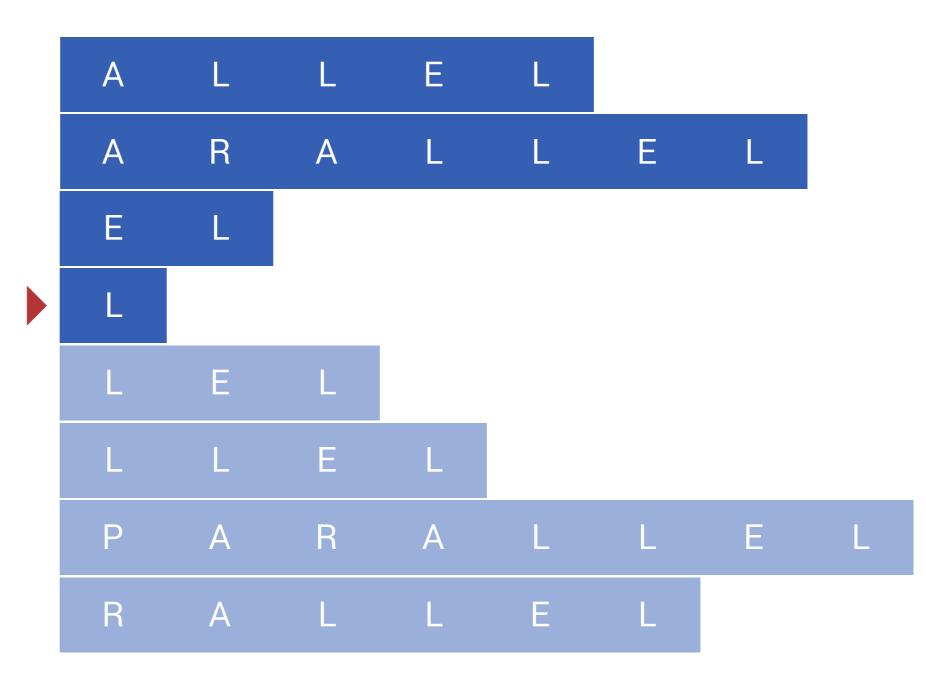
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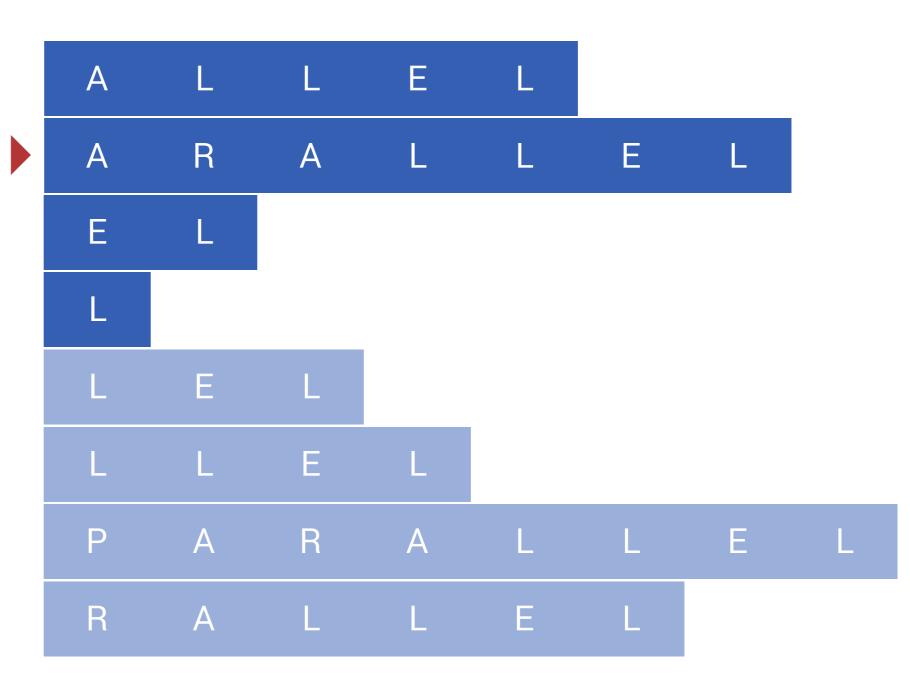
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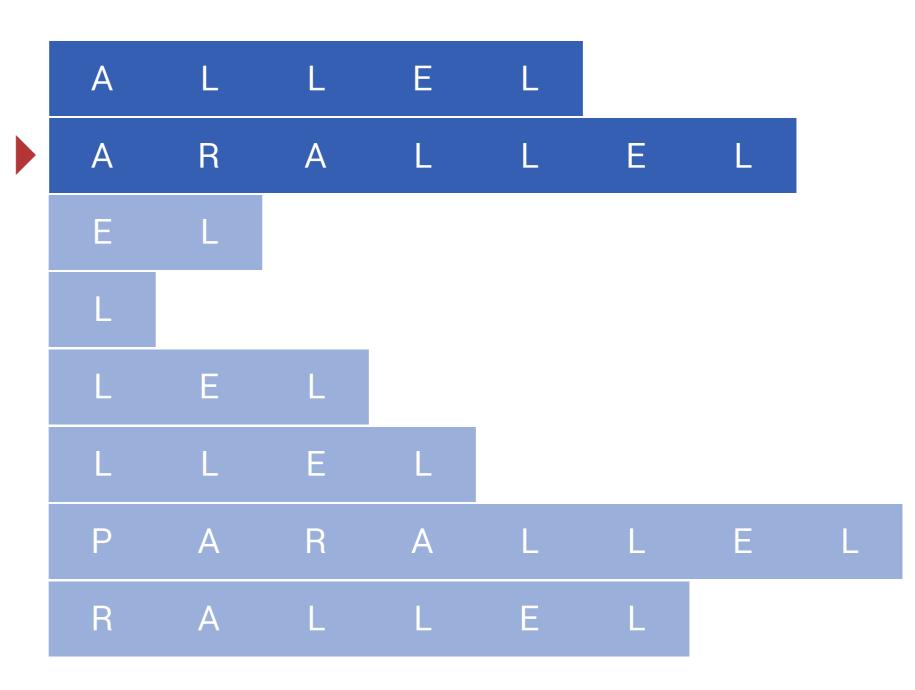
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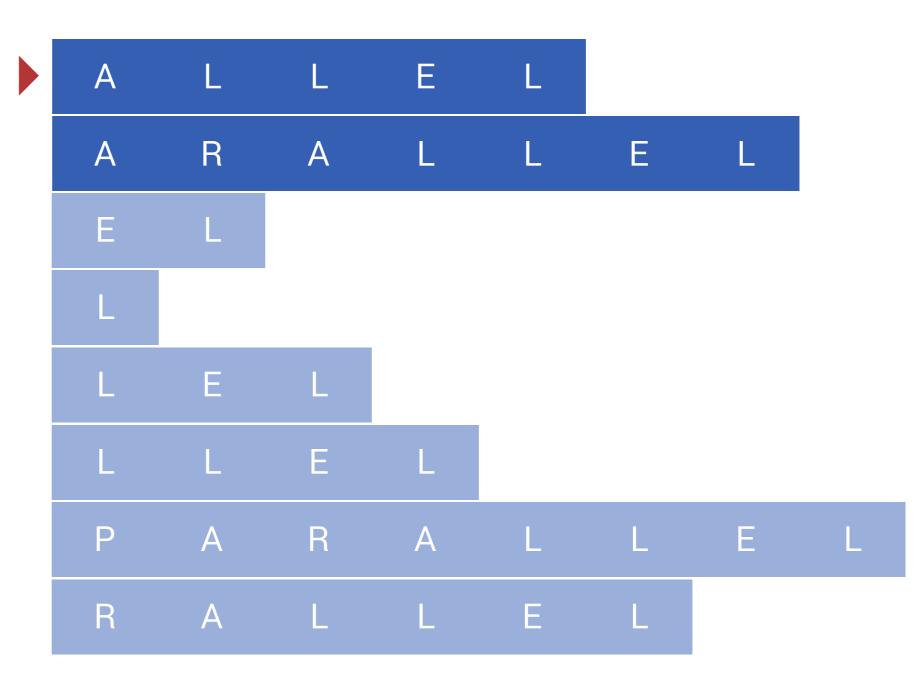
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Substringsuche

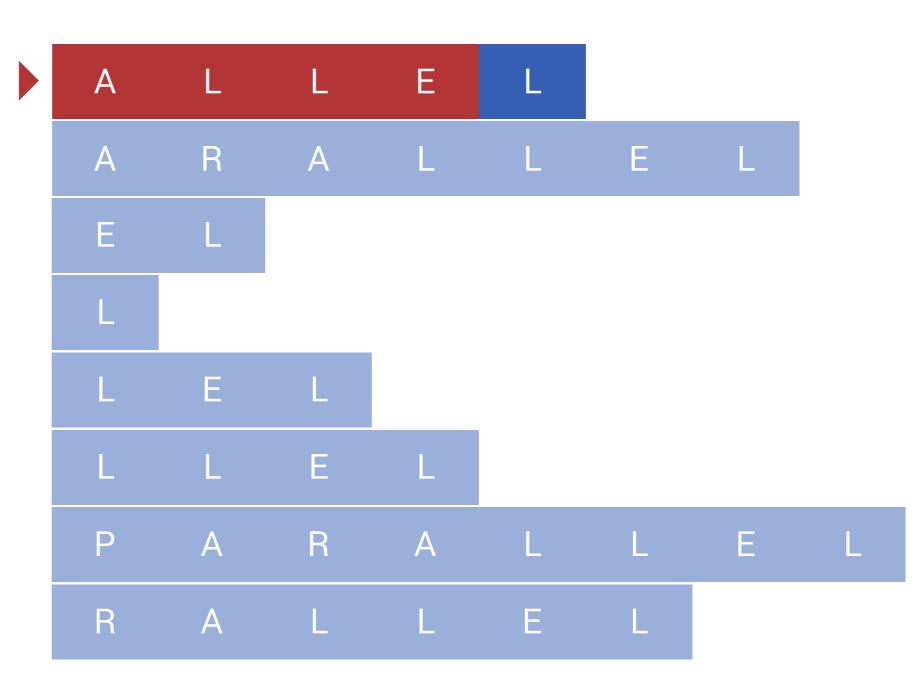
Ist *alle* in *parallel* enthalten?



Substringsuche

Ist *alle* in *parallel* enthalten?

Ja, an Stelle 4.



Verwendet in Implementationen

des LZ77-Kompressionsalgorithmus

Konstruktion eines Suffix Arrays mit

einem rekursionsfreien Linearzeit-Algorithmus.

Konstruktion eines Suffix Arrays mit

einem rekursionsfreien Linearzeit-Algorithmus)

Lösungsansätze

Naiver Ansatz

Verwendung eines allgemeinen Sortierverfahrens (z. B. Quicksort)

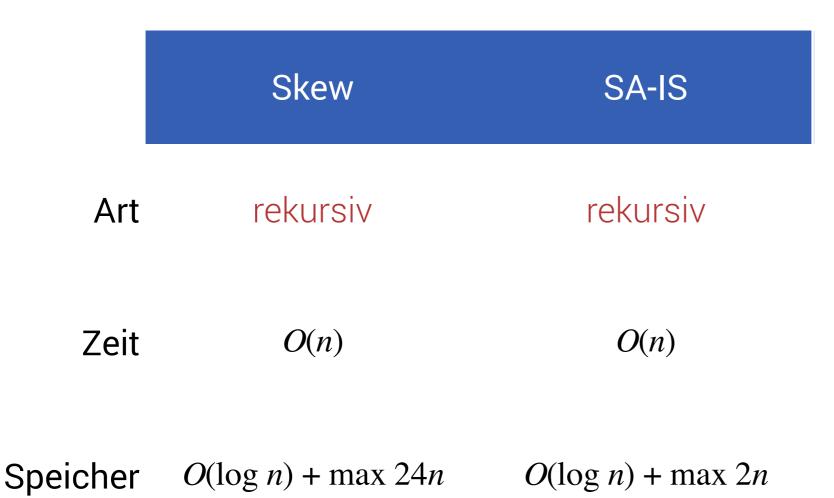
$$O(n \log n) \cdot O(n) = O(n^2 \log n)$$

Naiver Ansatz

Verwendung eines allgemeinen Sortierverfahrens (z. B. Quicksort)

$$O(n \log n) \cdot O(n) = O(n^2 \log n) \neq O(n)$$

Linearzeit Ansätze



Linearzeit Ansätze

| | Skew | SA-IS | ? | | |
|----------|------------------------|-----------------------|------------------|--|--|
| Art | rekursiv | rekursiv | iterativ | | |
| Zeit | O(n) | O(n) | O(n) | | |
| Speicher | $O(\log n) + \max 24n$ | $O(\log n) + \max 2n$ | <i>O</i> (1) + ? | | |

?

iterativ

O(n)

O(1) +?

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iterativ

O(n)

O(1) +?

GSACA

Greedy Suffix Array Construction Algorithm

Definitionen

| Р | Α | R | Α | L | L | Е | L | \$ |
|---|---|---|---|---|---|---|---|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |

Definitionen

S := Eingabe, eine mit \$ terminierte Zeichenkette der Länge n

Definitionen

S[4]



S := Eingabe, eine mit \$ terminierte Zeichenkette der Länge n

S[i] := i-tes Zeichen von S

| S = | Р | Α | R | Α | L | L | Е | L | \$ | |
|-----|---|---|-------|---|---|---|---|-----|-------|--|
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 1 | 7 = 9 | |
| | | | S[48) | | | | | | | |

S := Eingabe, eine mit \$ terminierte Zeichenkette der Länge n

S[i] := i-tes Zeichen von S

$$S[i ... j + 1) := S[i ... j] := S[i] ... S[j]$$

S₄

| S = | Р | Α | R | Α | L | L | Е | L | \$ |
|-----|---|---|---|---|---|---|---|-----|-----|
| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 n | = 9 |

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$$S_i := S[i ... n]$$

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| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 n | = 9 |

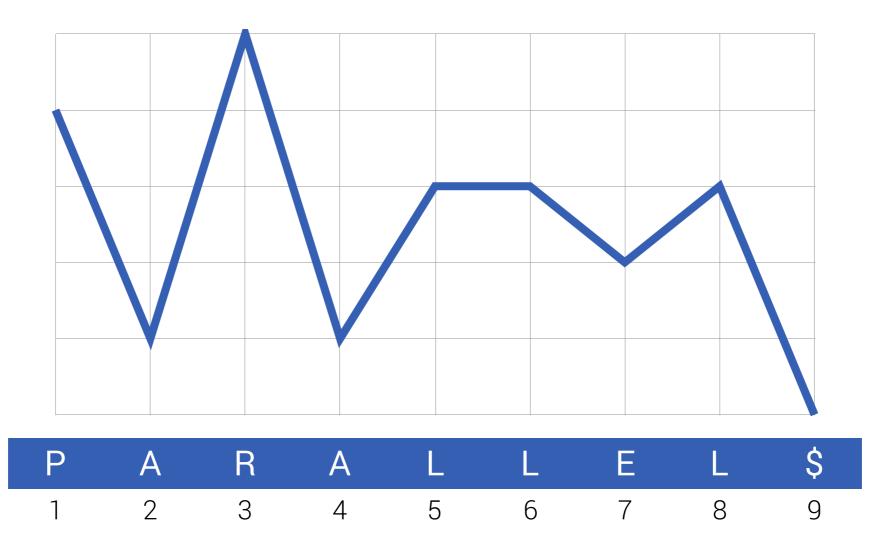
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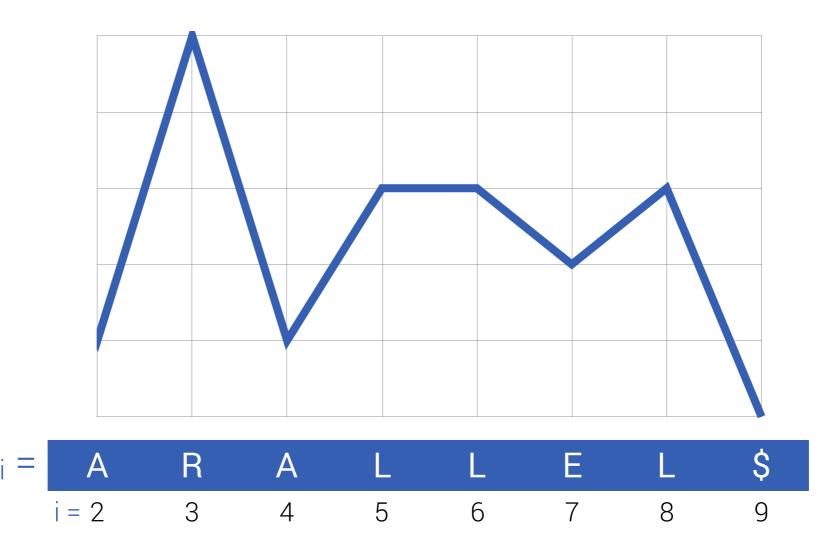
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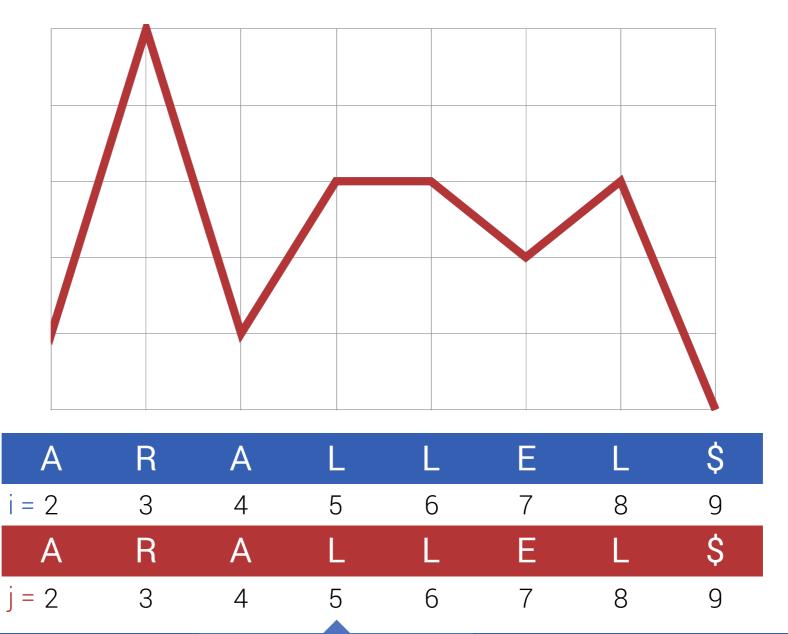
$$S[i ... j + 1) := S[i ... j] := S[i] ... S[j]$$

$$S_i := S[i ... n]$$

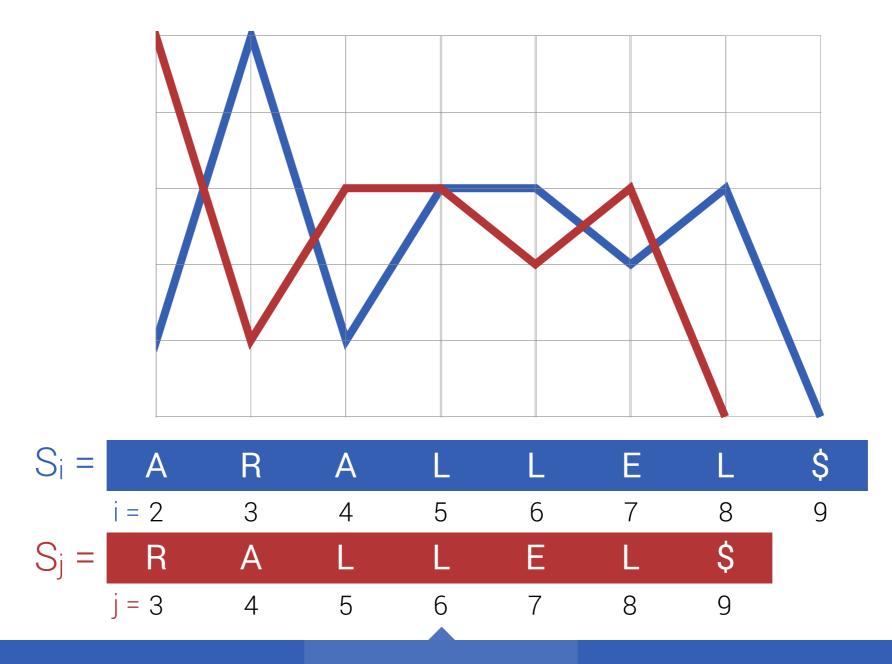
$$\hat{i} := min \{ j \in [i .. n]: S_j <_{lex} S_i \}$$

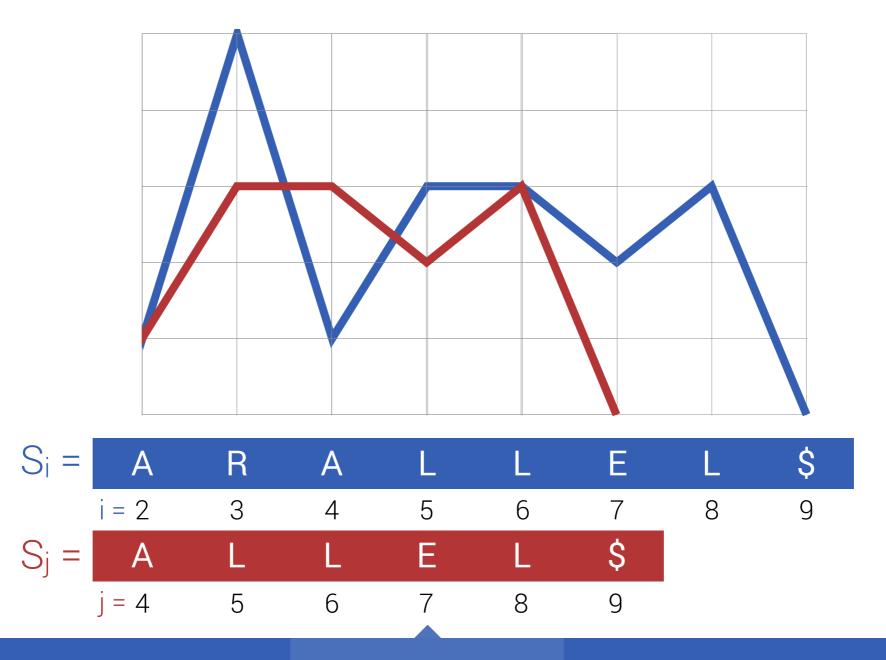




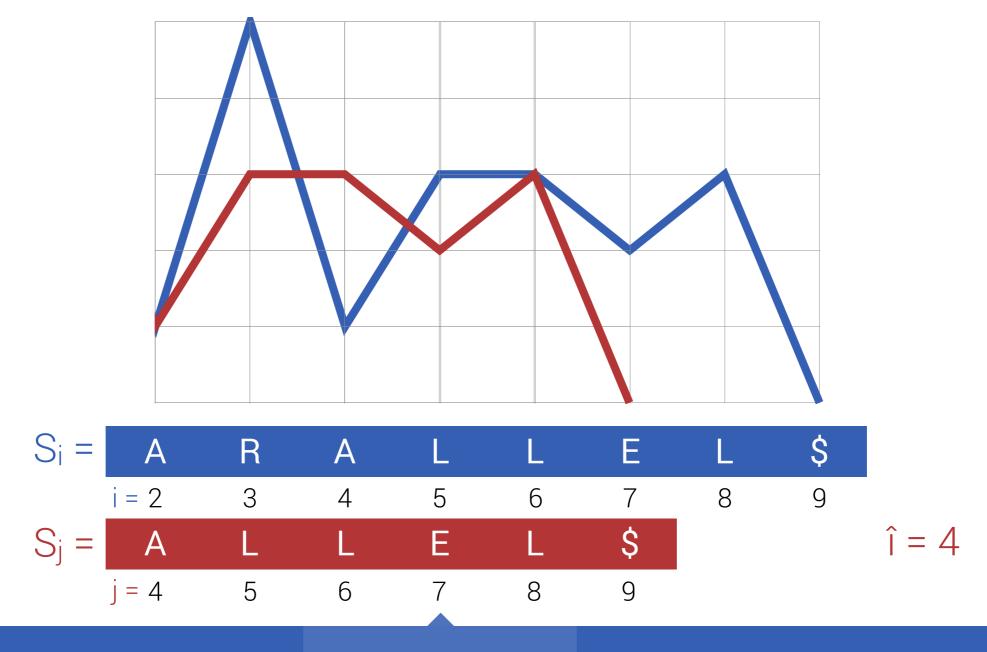


 $\hat{i} := min \{ j \in [i .. n] : S_j <_{lex} S_i \}$





$$\hat{i} := min \{ j \in [i .. n] : S_j <_{lex} S_i \}$$



Problemstellung

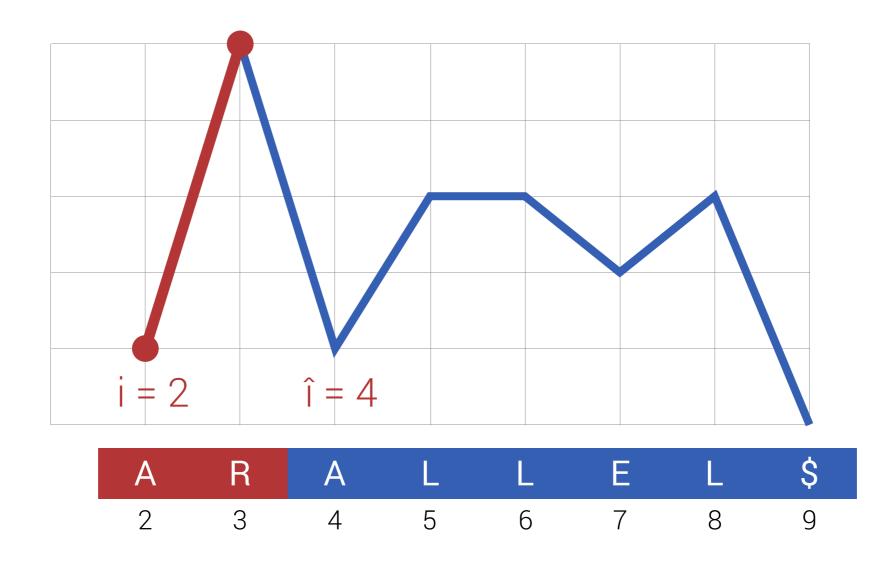
Lösungsansätze

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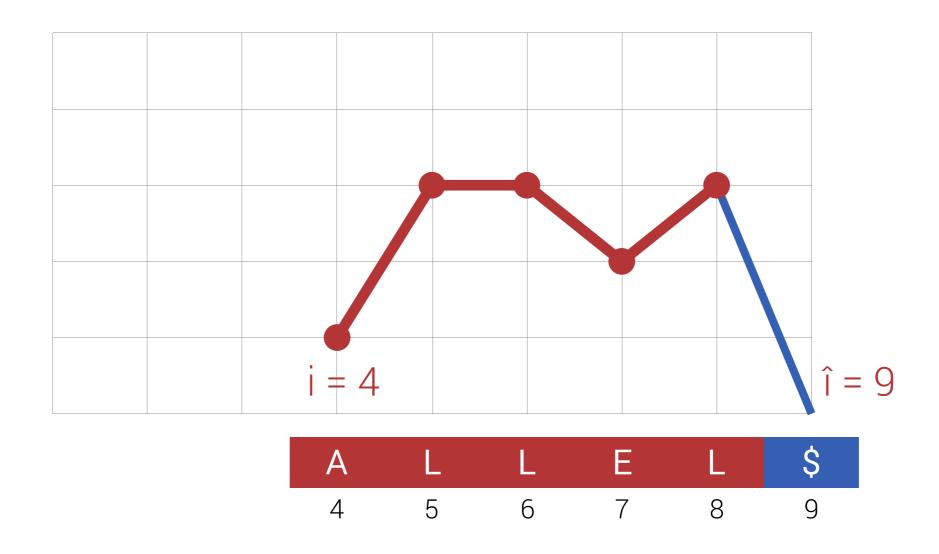
Performance

Rückblick

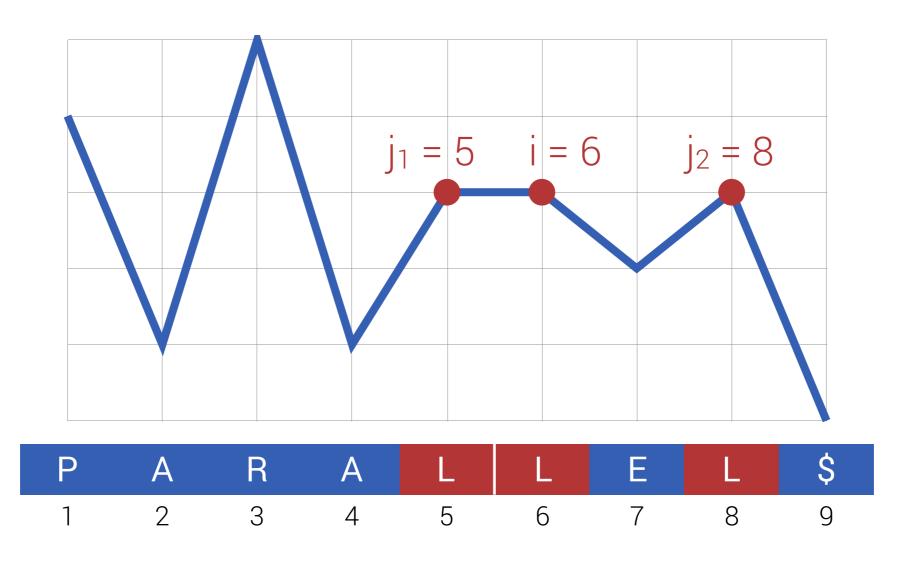
Gruppenkontext von $S_i := S[i .. \hat{i})$



Gruppenkontext von $S_i := S[i .. \hat{i})$



Gruppe von $S_i := \{ S_j : Gr.kontext S_j = Gr.kontext S_i \}$

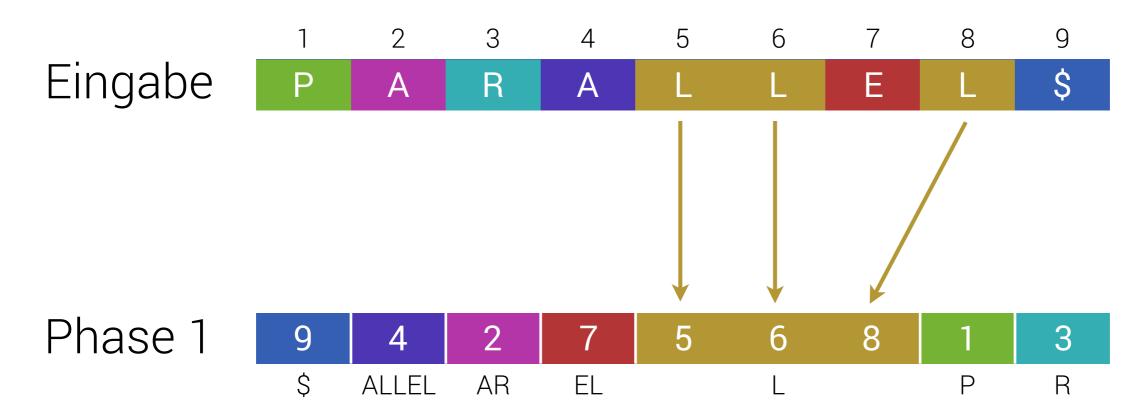


Eingabe

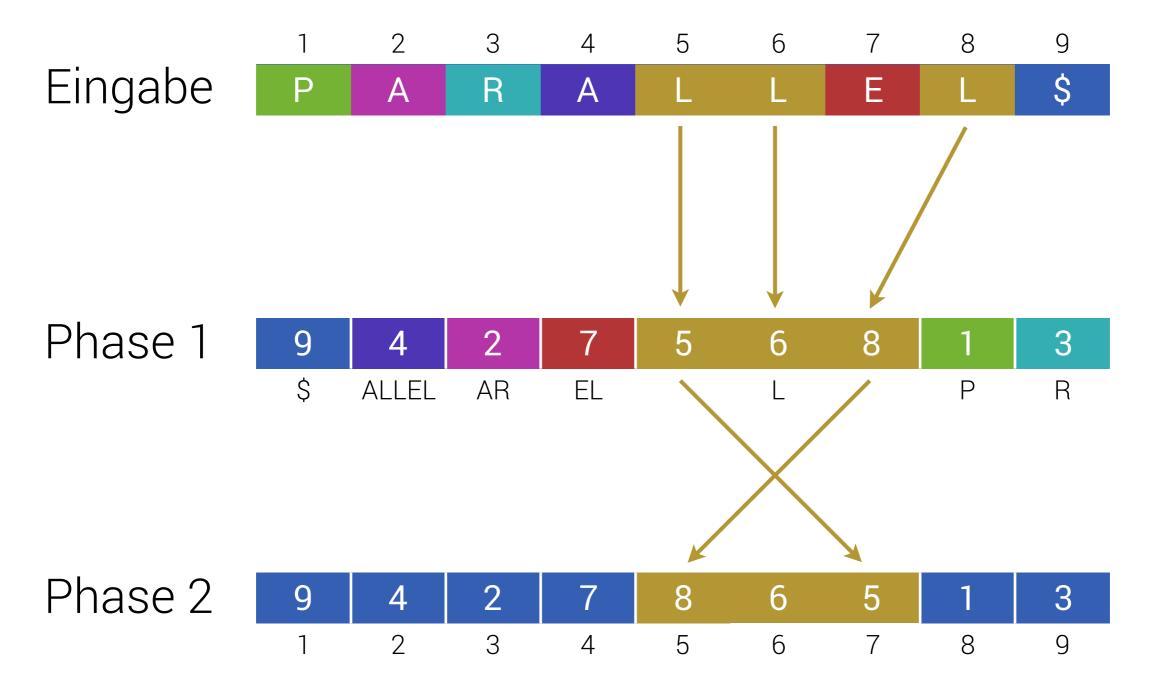
1 2 3 4 5 6 7 8 9

P A R A L L E L \$

Problemstellung Lösungsansätze GSACA Performance Rückblick

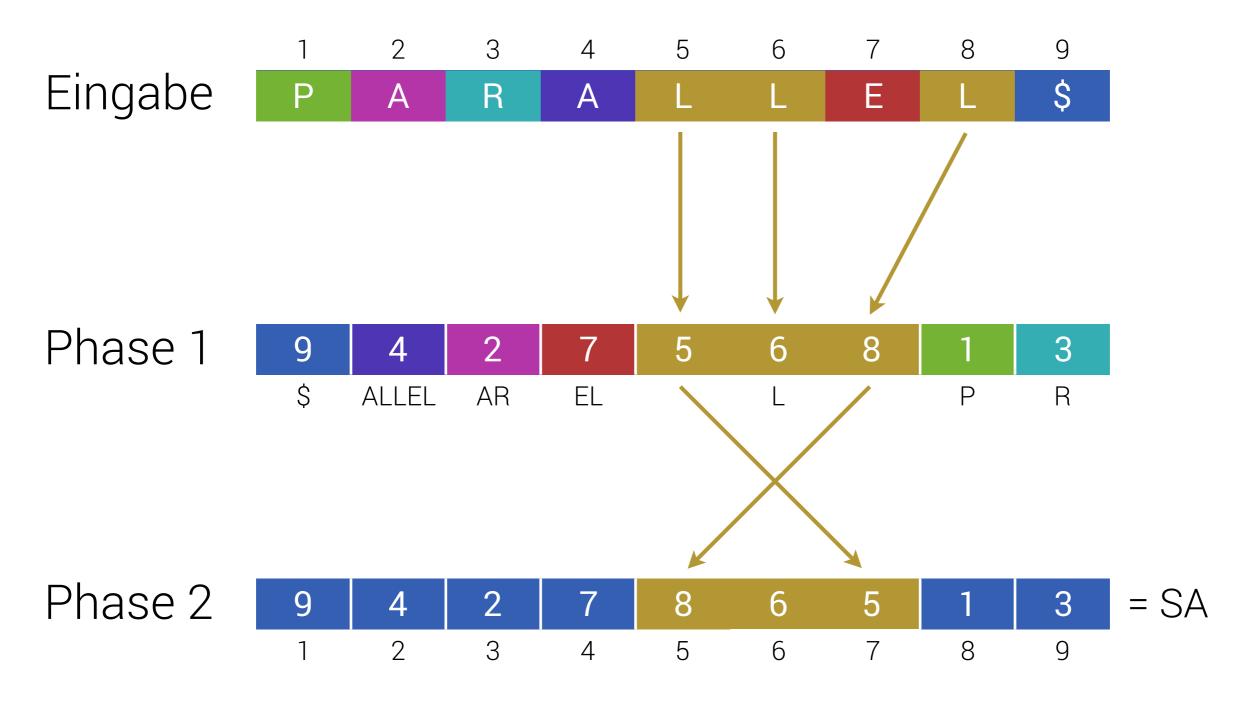


Problemstellung Lösungsansätze GSACA Performance Rückblick

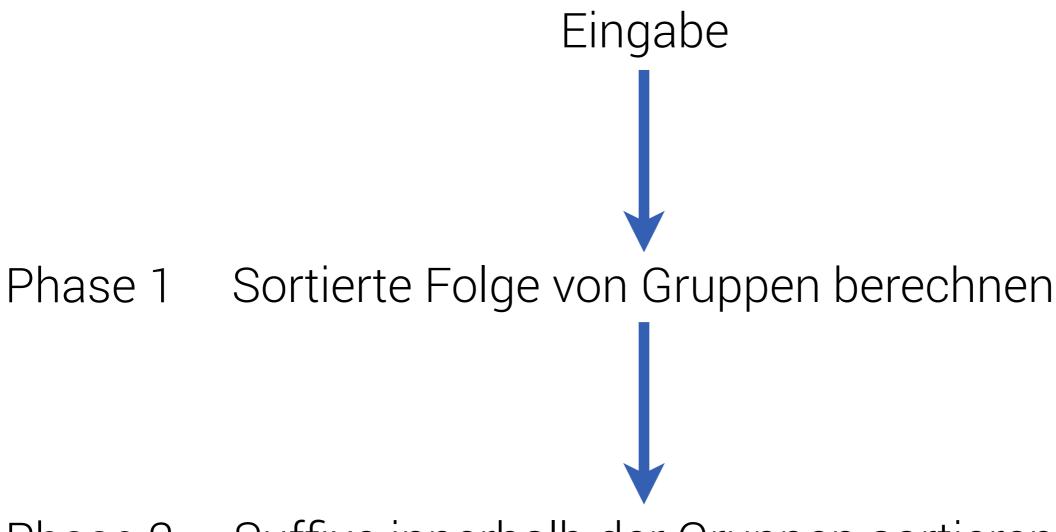


Problemstellung Lösungsansätze

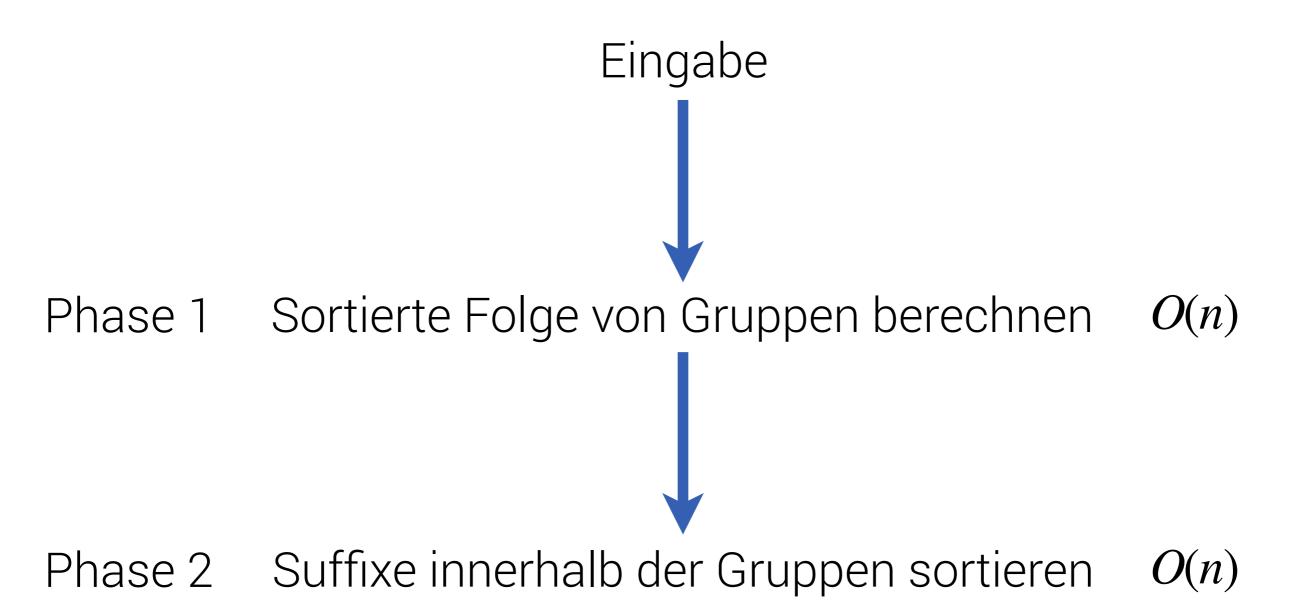
GSACA



Problemstellung Lösungsansätze



Phase 2 Suffixe innerhalb der Gruppen sortieren



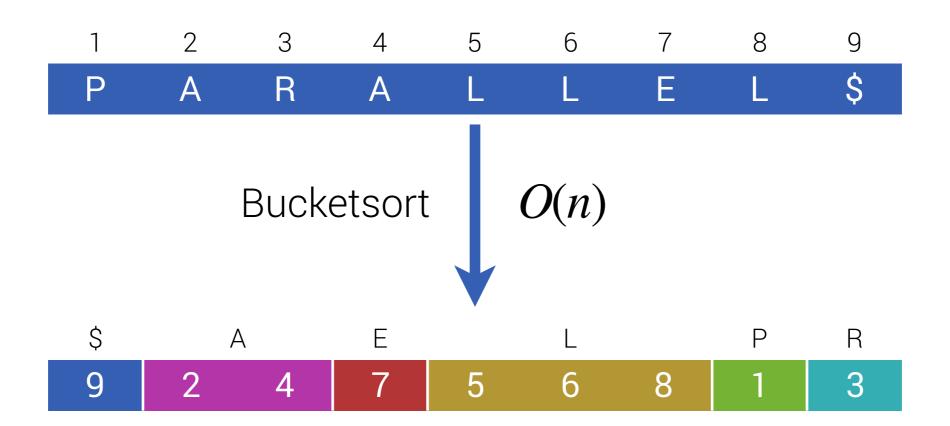
Problemstellung Lösungsansätze GSACA Performance Rückblick

Sortierte Folge von Gruppen berechnen

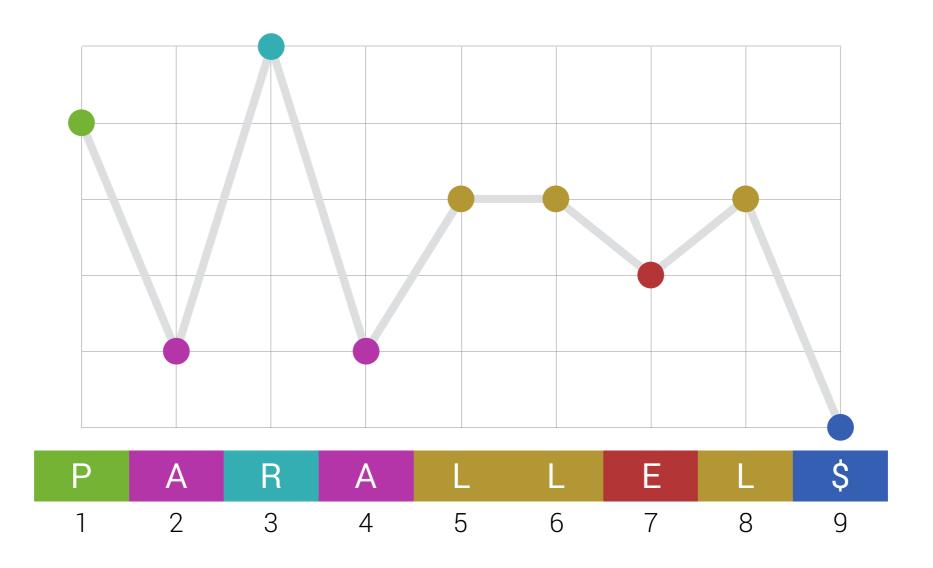


Problemstellung Lösungsansätze GSACA Performance Rückblick

Sortierte Folge von Gruppen berechnen







Problemstellung

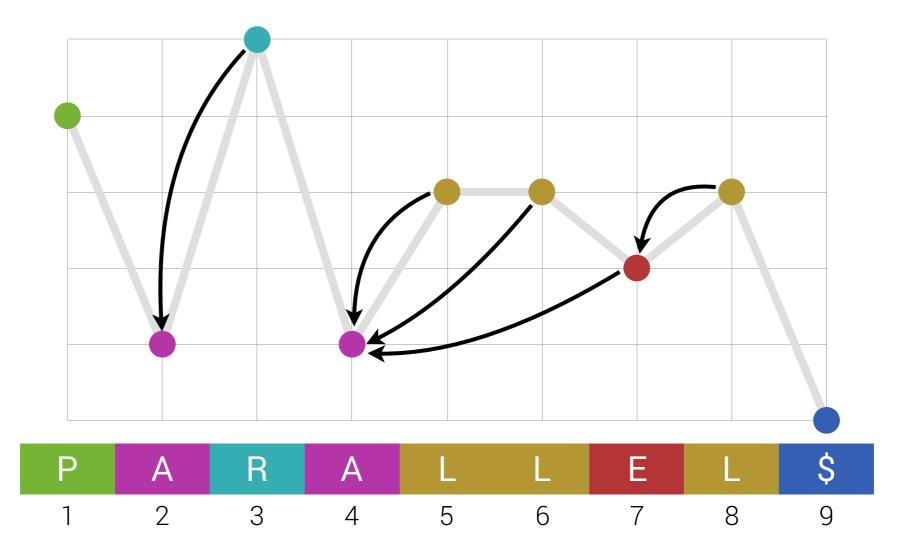
Lösungsansätze

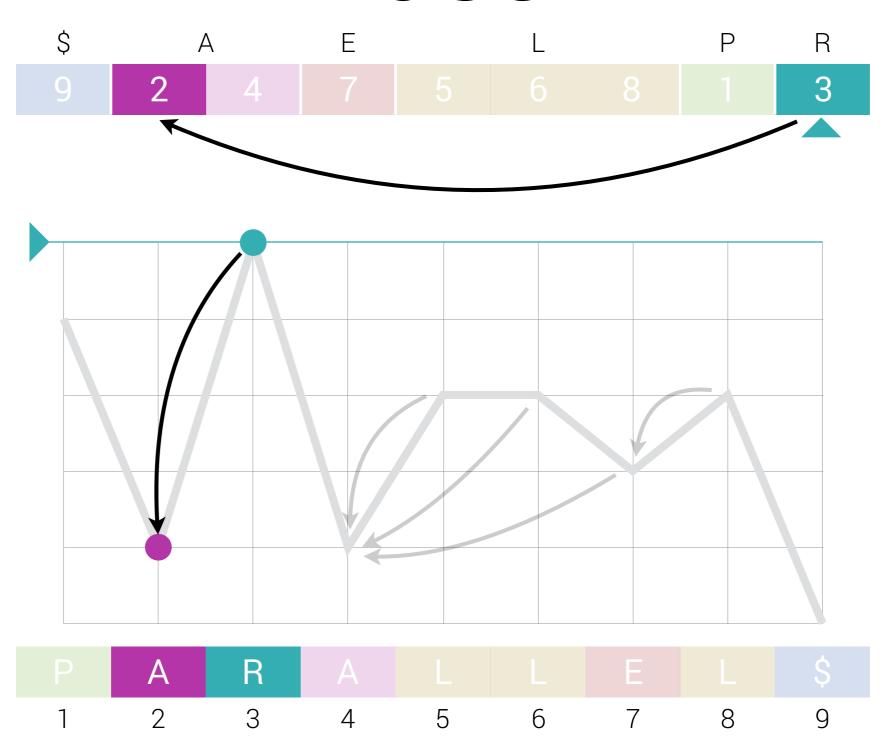
GSACA

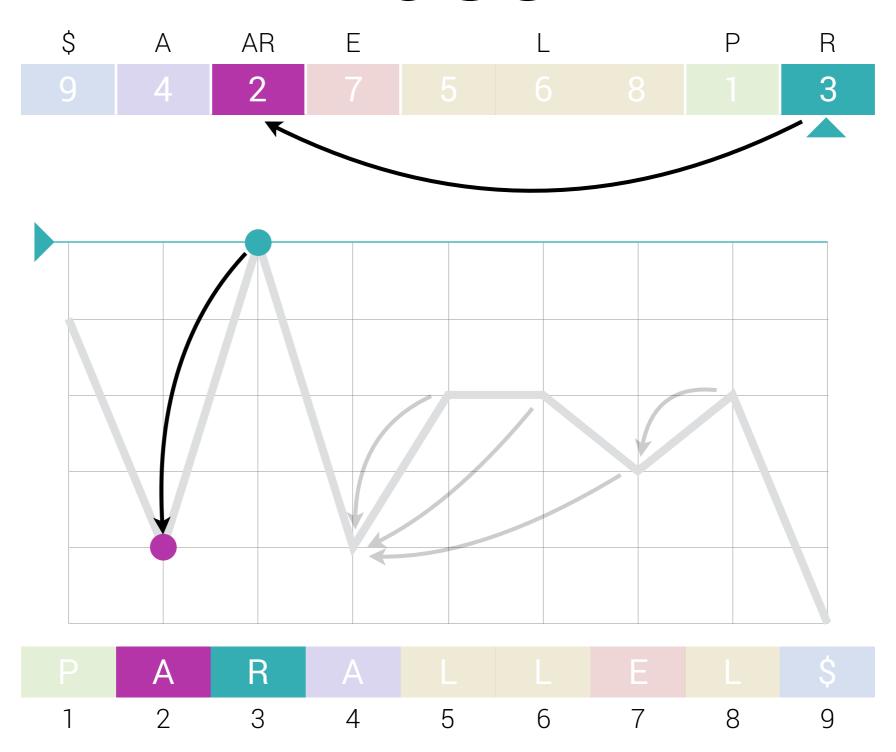
Performance

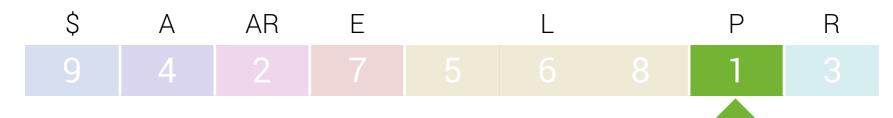
Rückblick

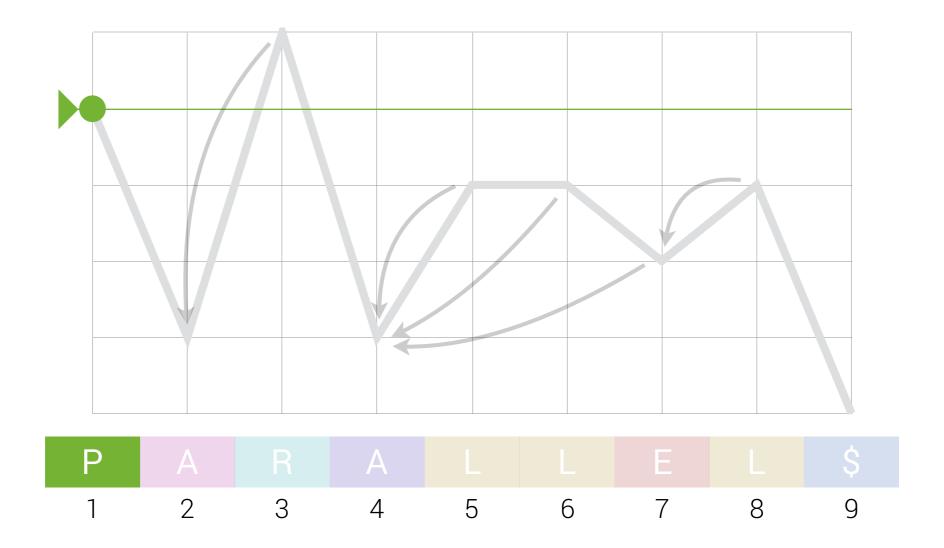












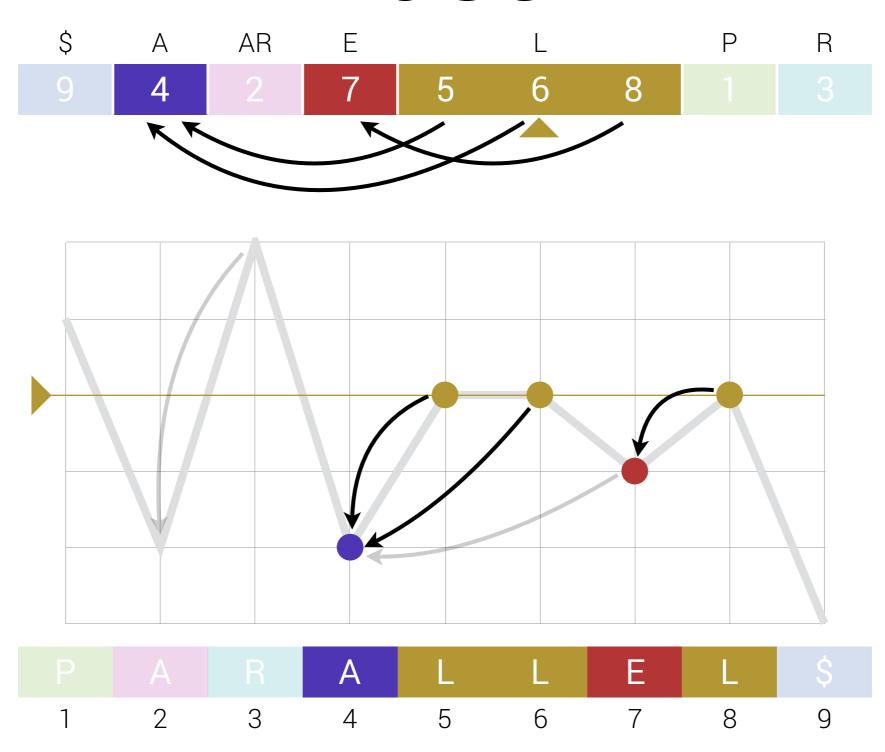
Problemstellung

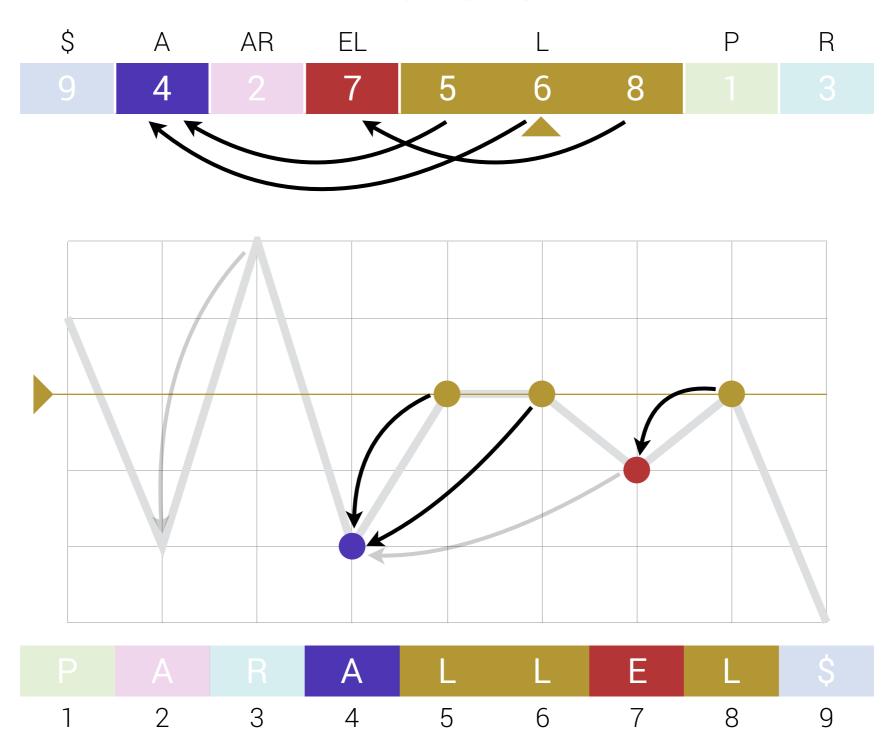
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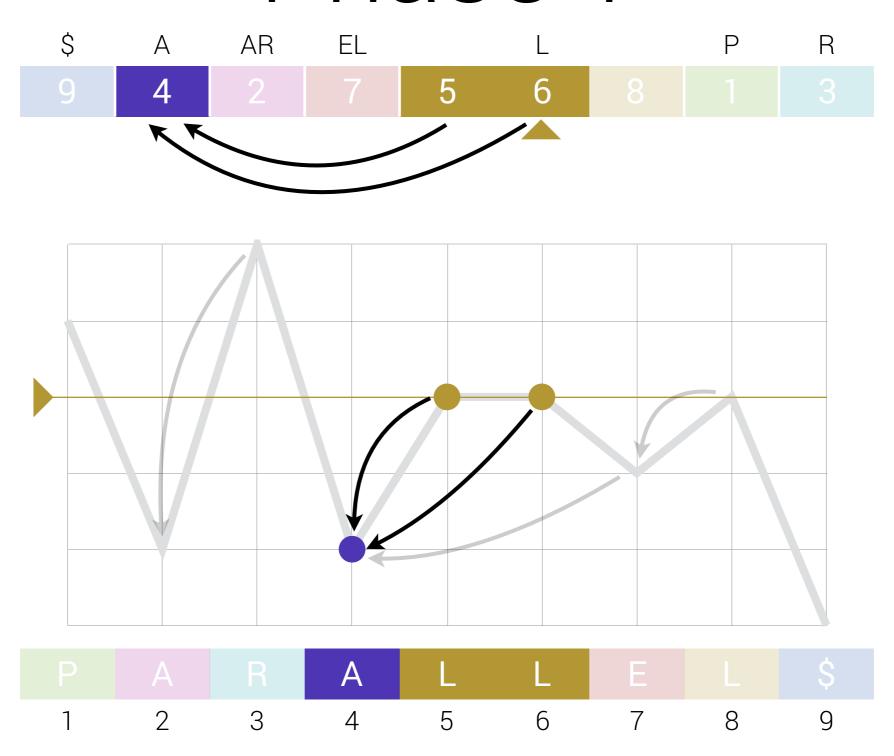
GSACA

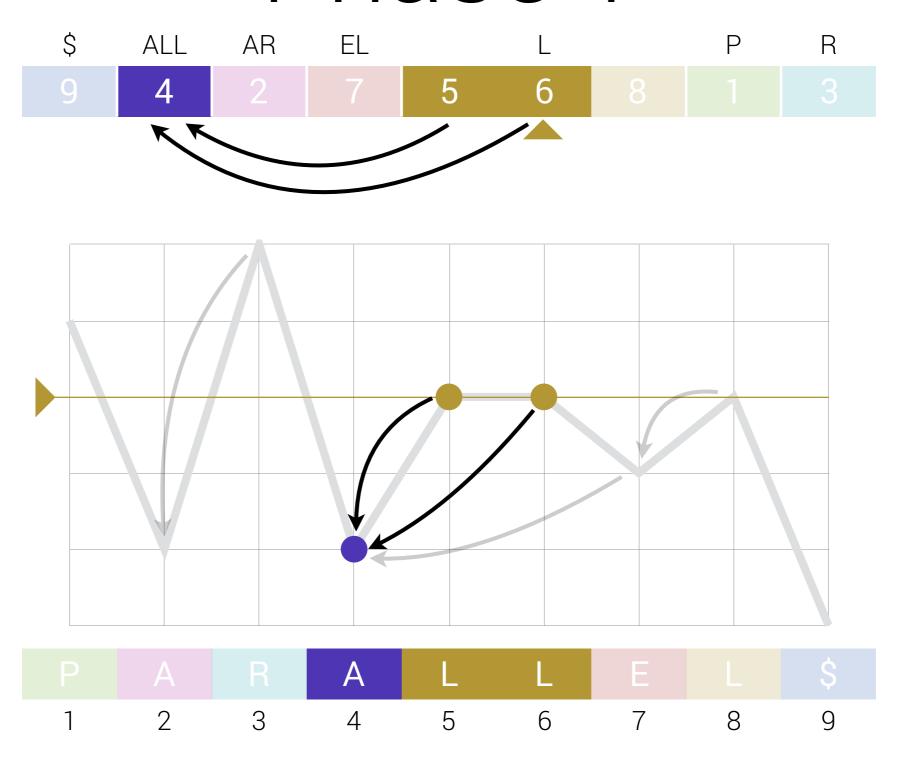
Performance

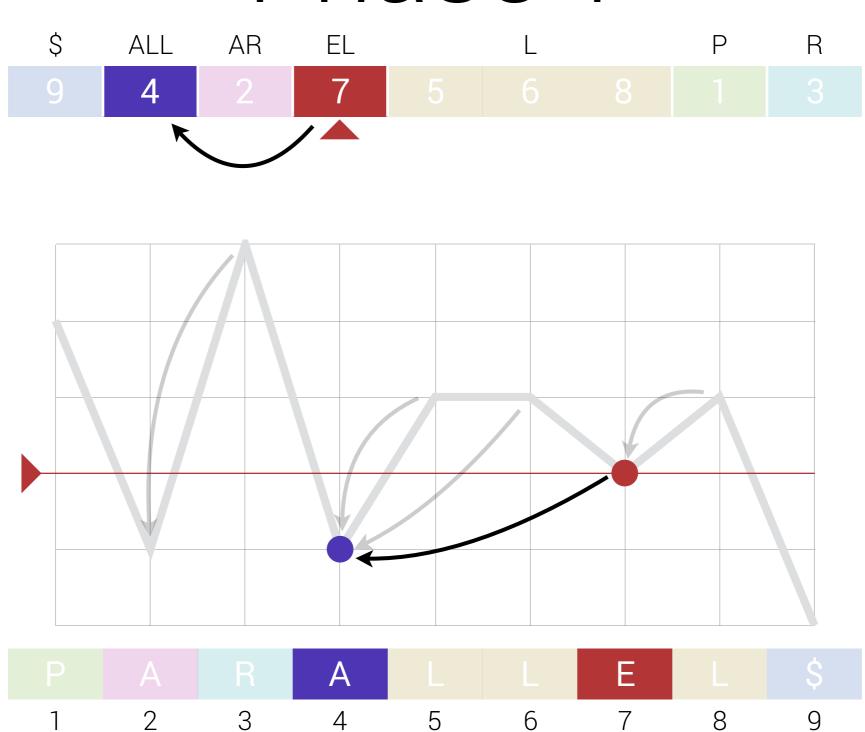
Rückblick

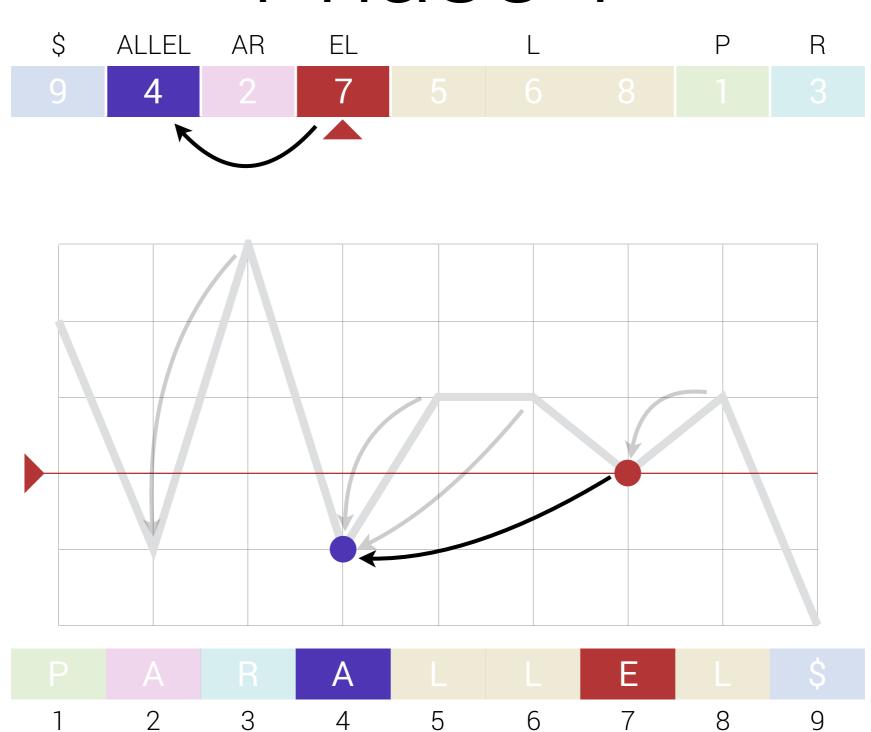




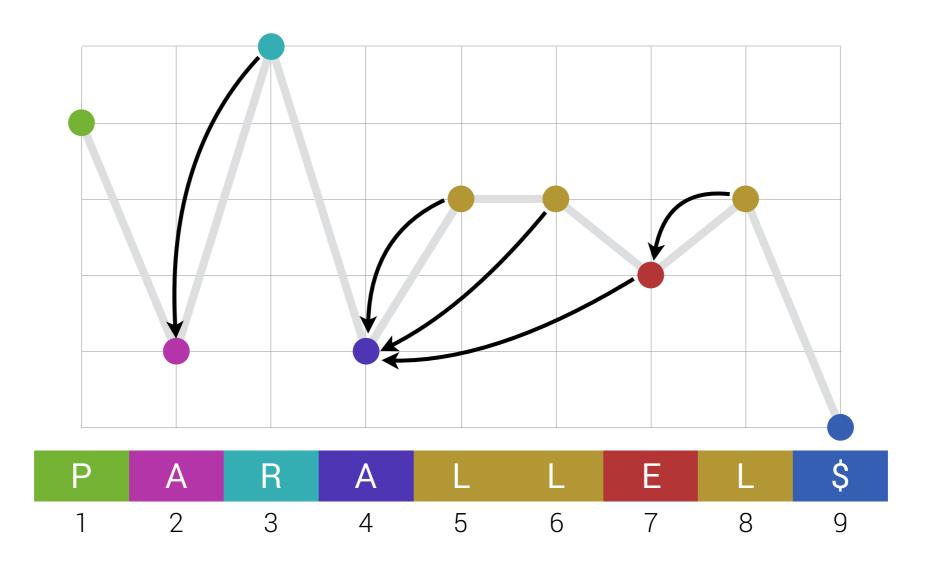




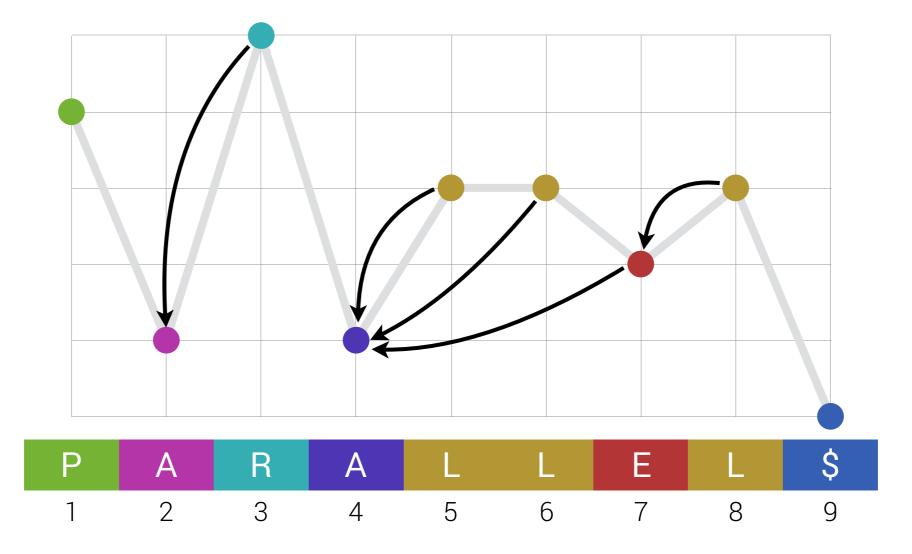


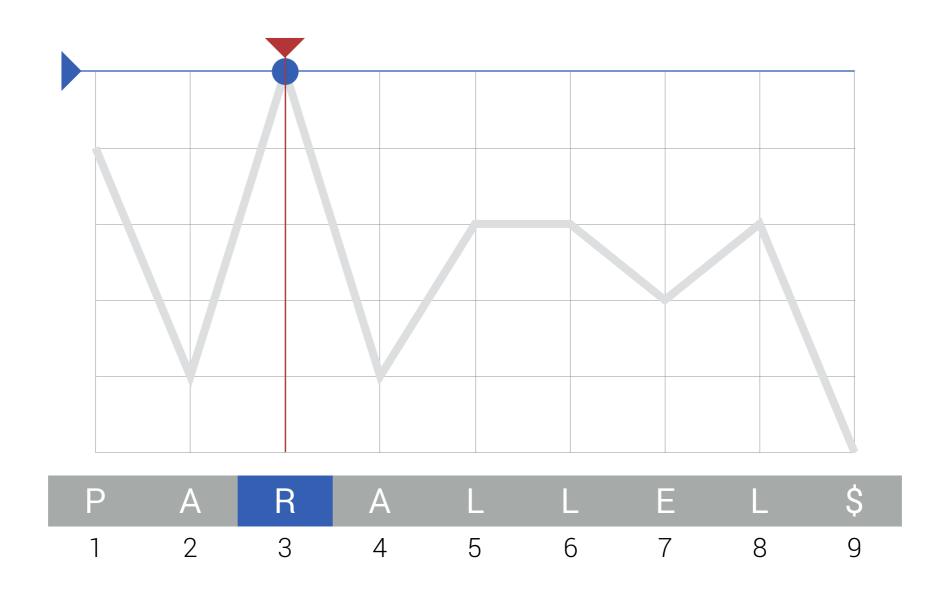


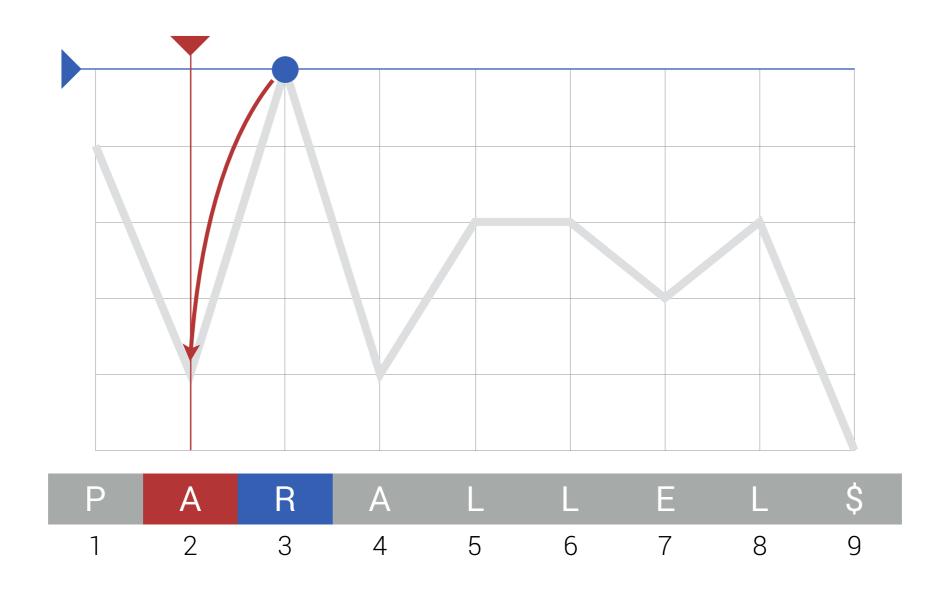


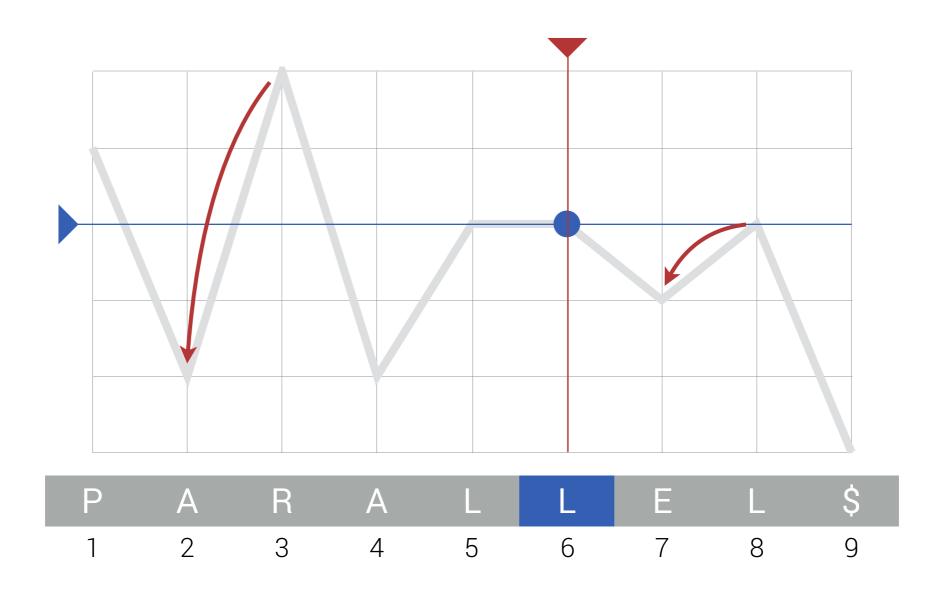




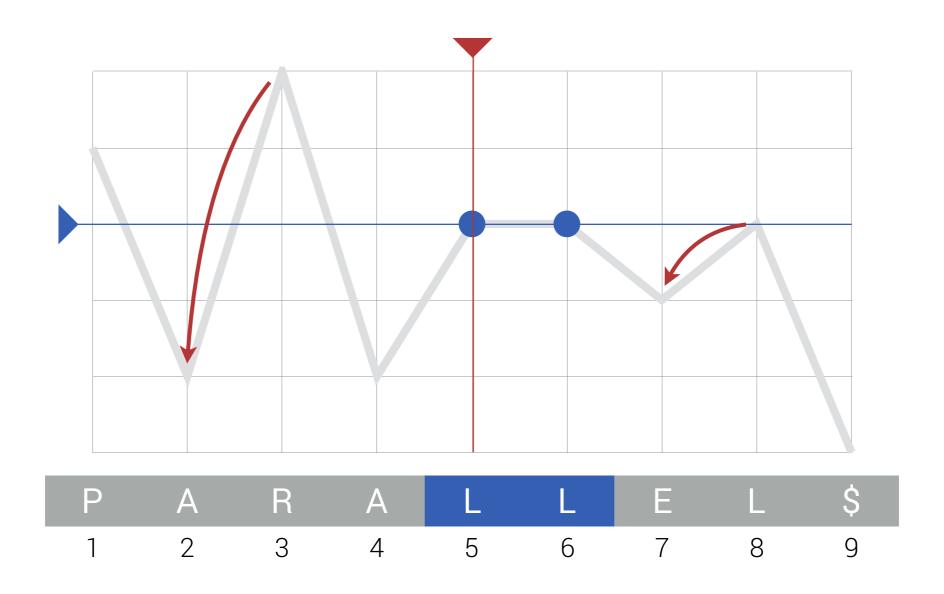








 $prev(i) := max \{ j \in [1 .. i]: Gr.kontext S_j <_{lex} Gr.kontext S_i \}$

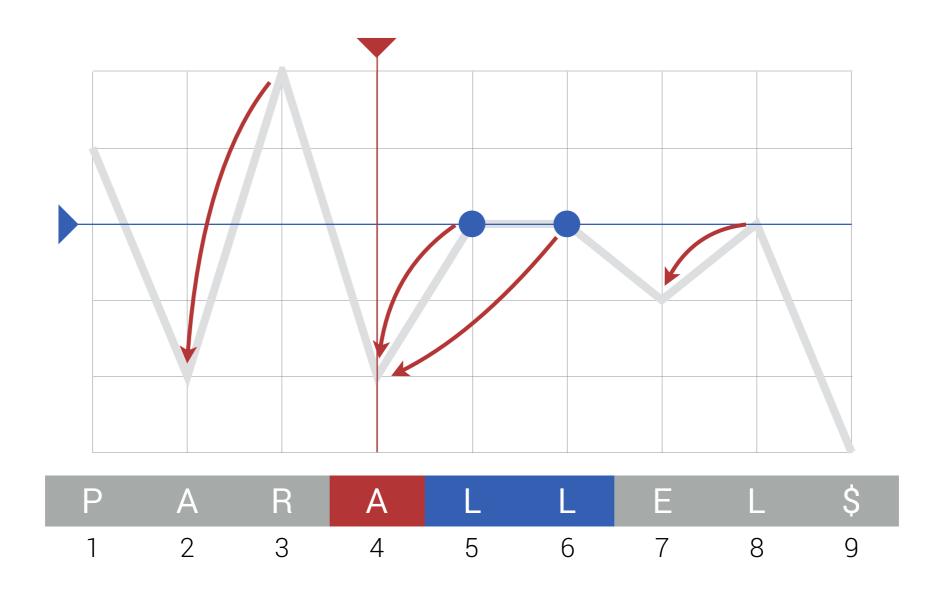


Problemstellung Lösungsansätze

GSACA

Performance

 $prev(i) := max \{ j \in [1 .. i]: Gr.kontext S_j <_{lex} Gr.kontext S_i \}$

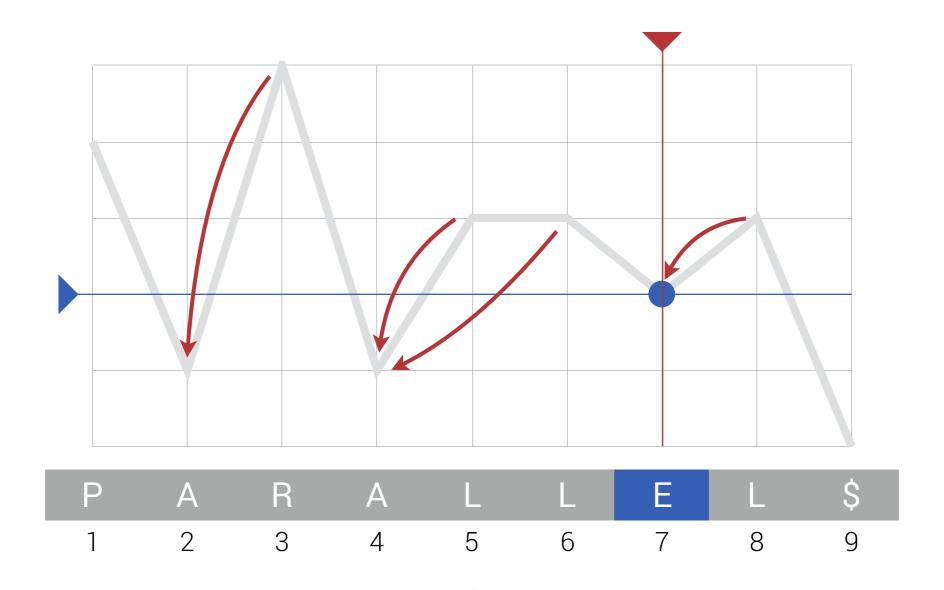


Problemstellung Lösungsansätze

GSACA

Performance

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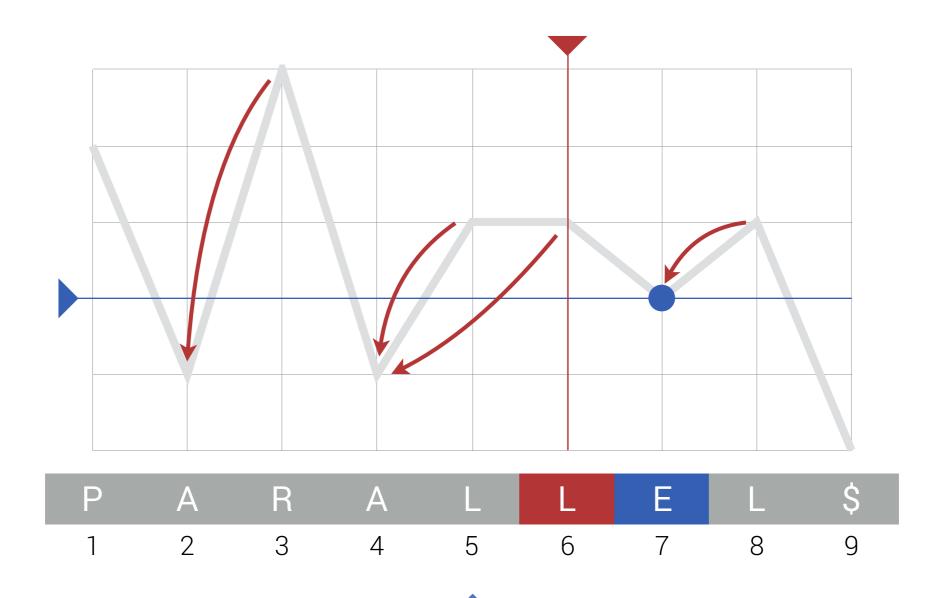
Problemstellung Li

Lösungsansätze

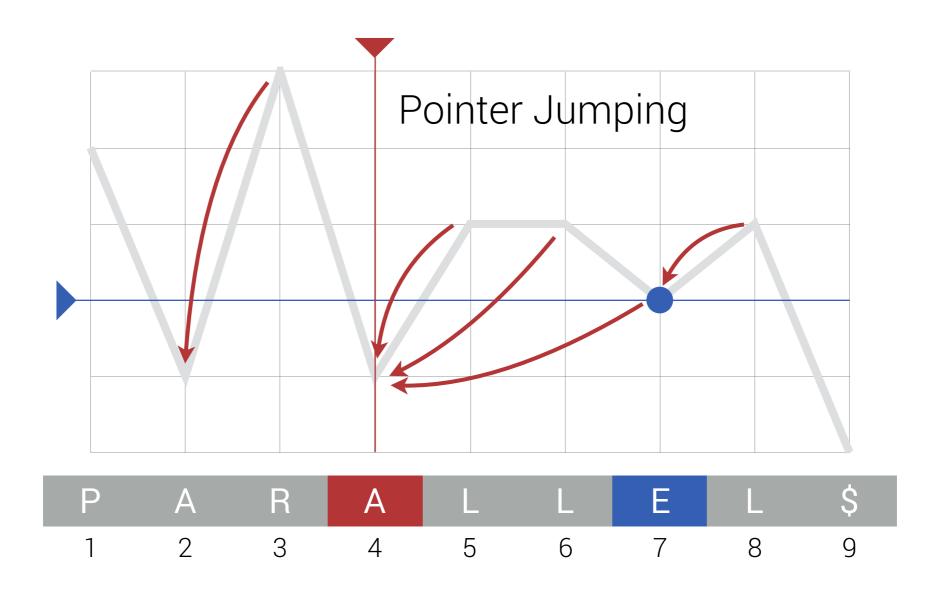
GSACA

Performance

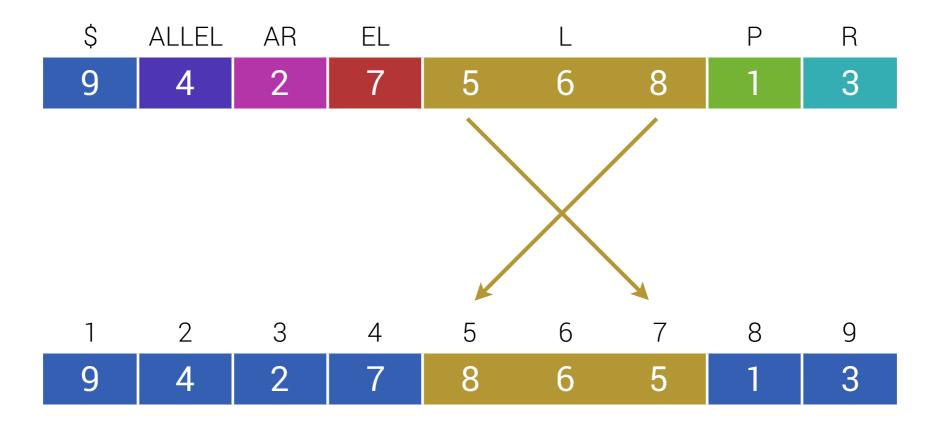
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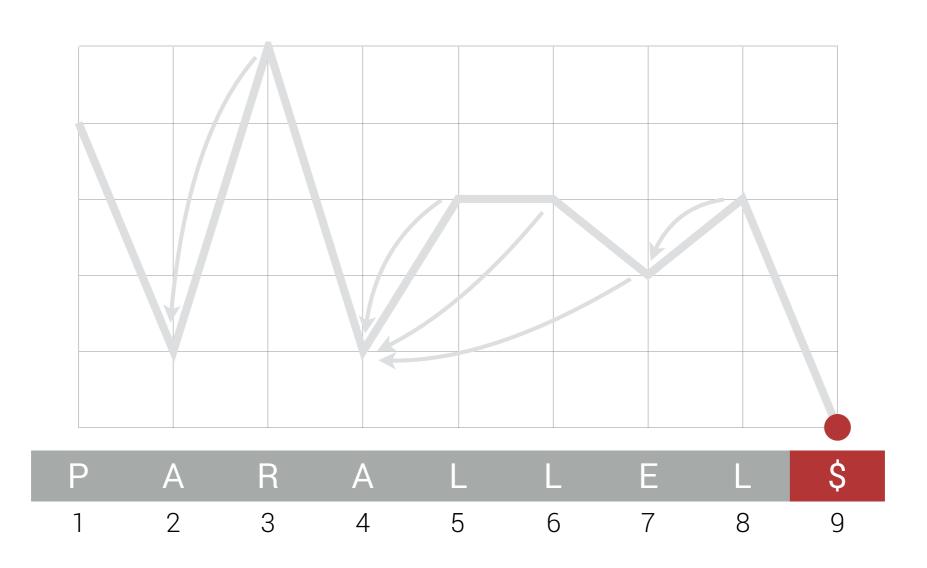
 $prev(i) := max \{ j \in [1 .. i]: Gr.kontext S_j <_{lex} Gr.kontext S_i \}$



Suffixe innerhalb der Gruppen sortieren







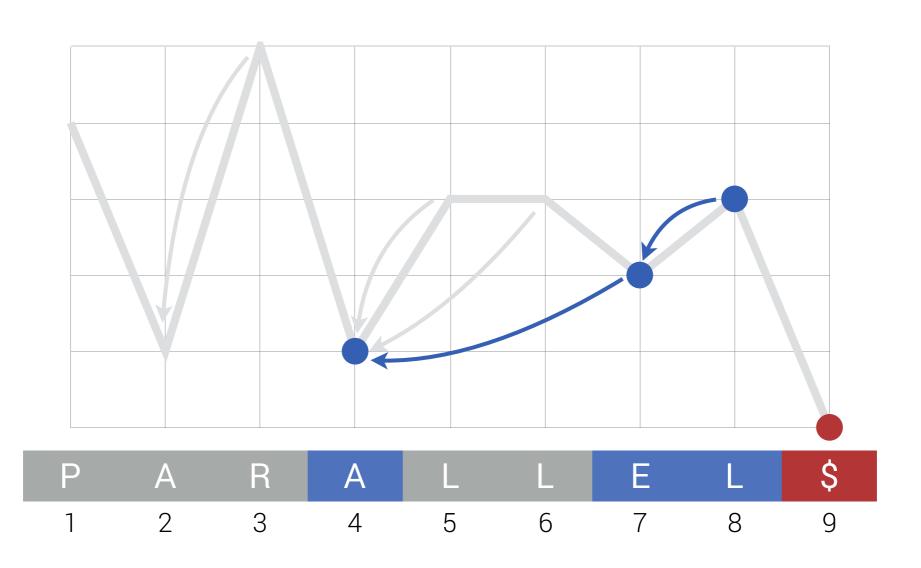
Problemstellung

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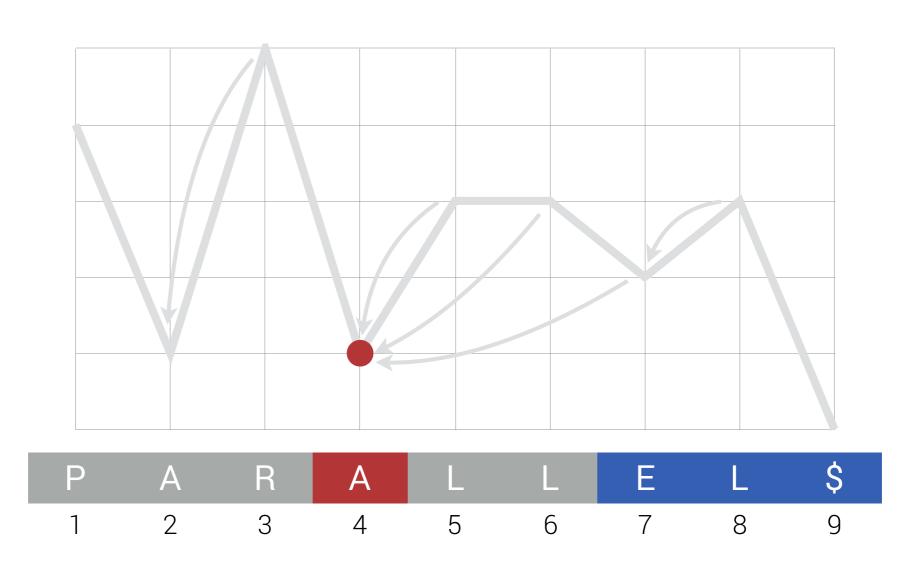
Problemstellung

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Performance



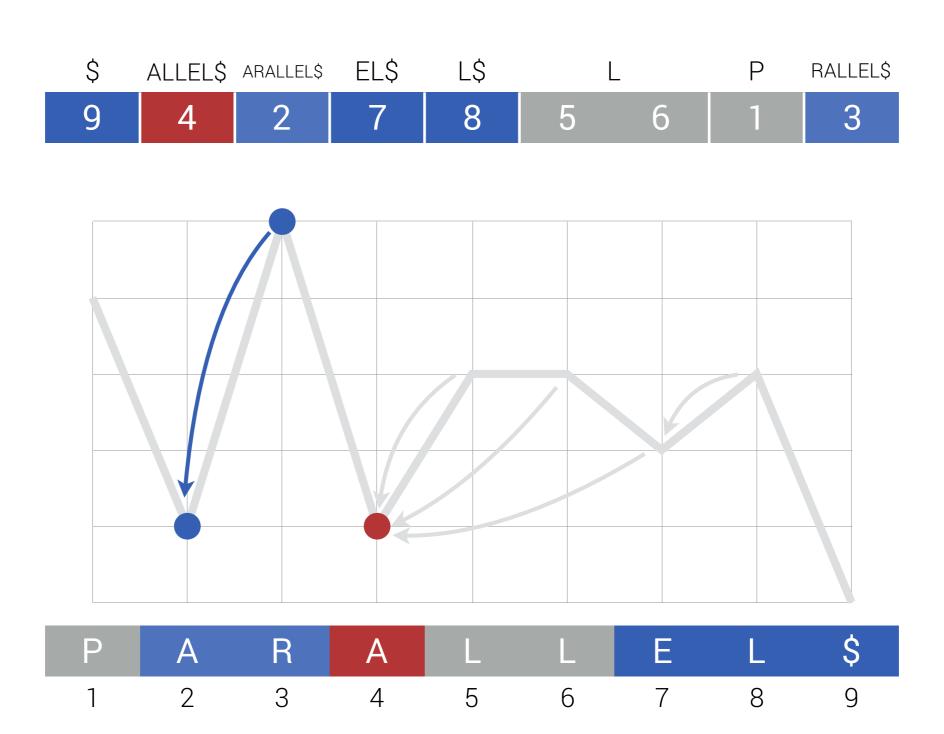


Problemstellung

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Performance

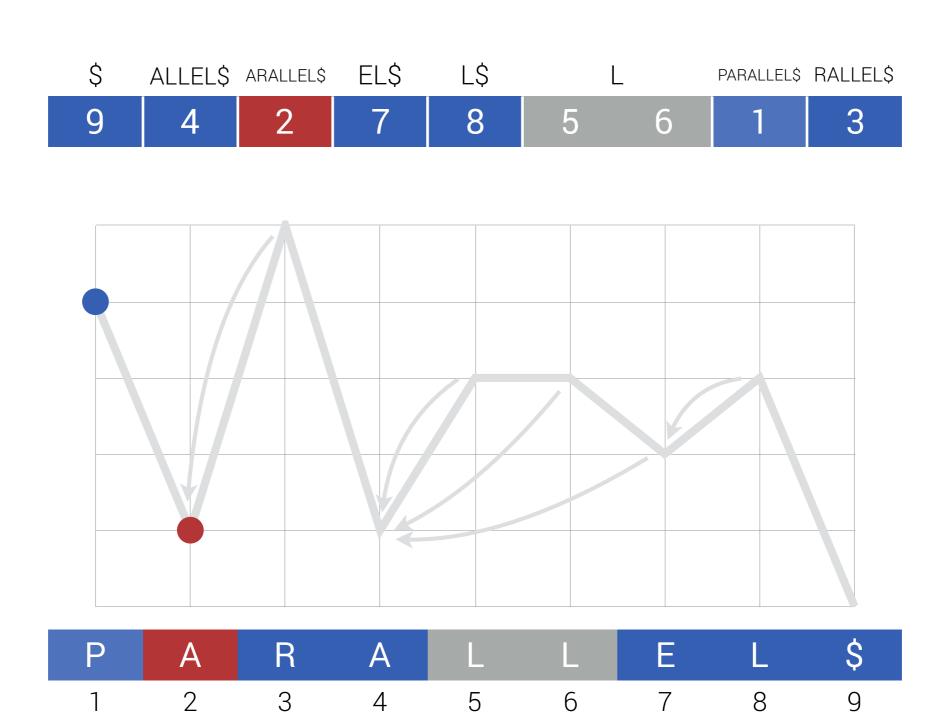


Problemstellung

Lösungsansätze

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Performance

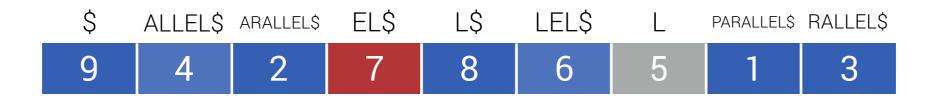


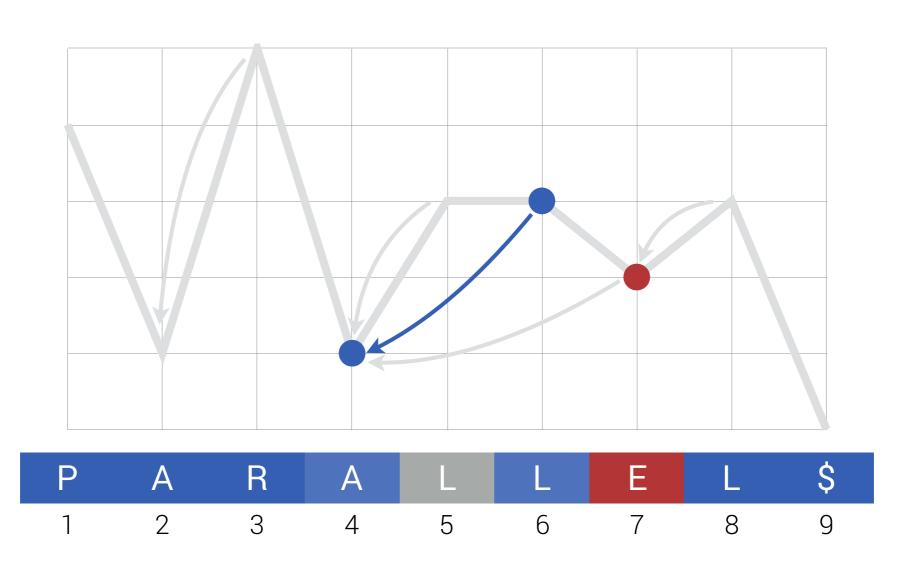
Problemstellung

Lösungsansätze

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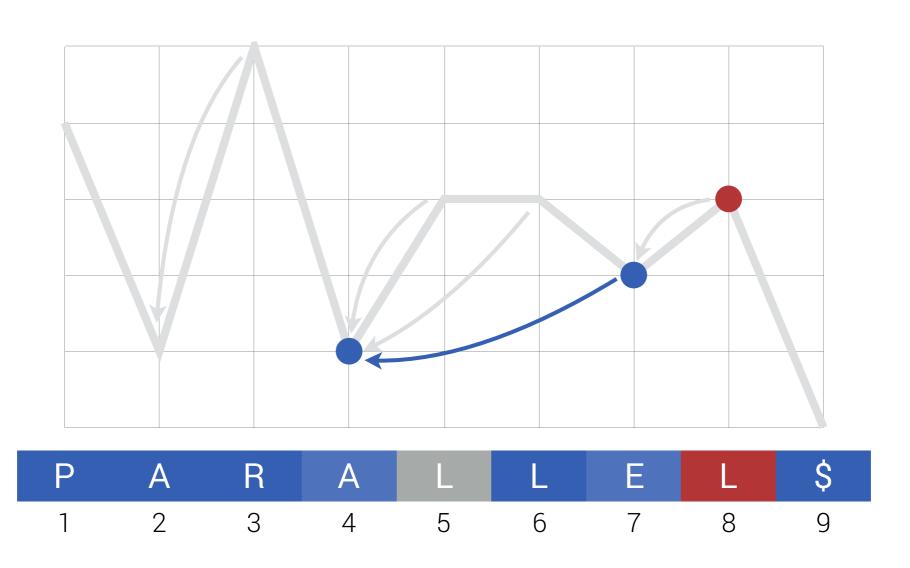
Problemstellung

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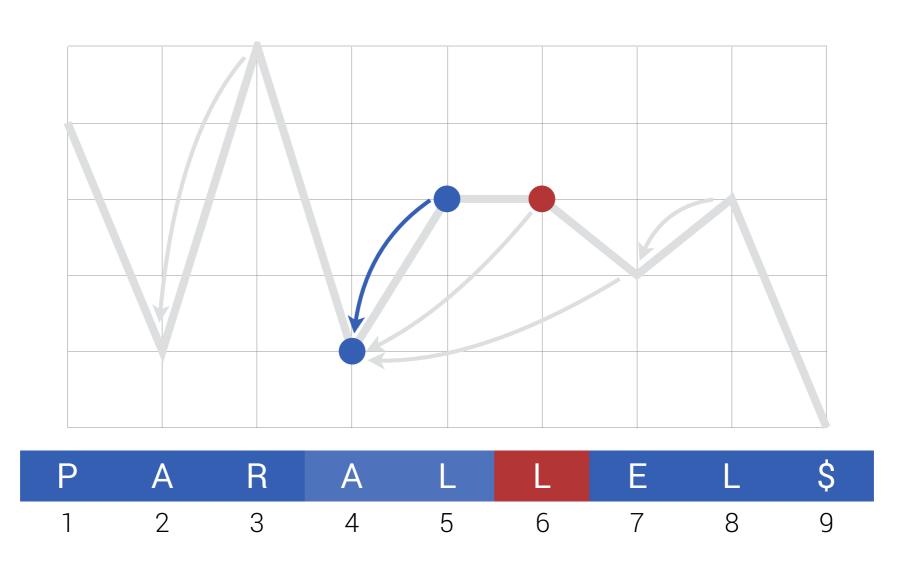
Problemstellung

Lösungsansätze

GSACA

Performance





Problemstellung

Lösungsansätze

GSACA

Performance

```
$ ALLEL$ ARALLEL$ EL$ L$ LEL$ LLEL$ PARALLEL$ RALLEL$

SA = 9 4 2 7 8 6 5 1 3
```

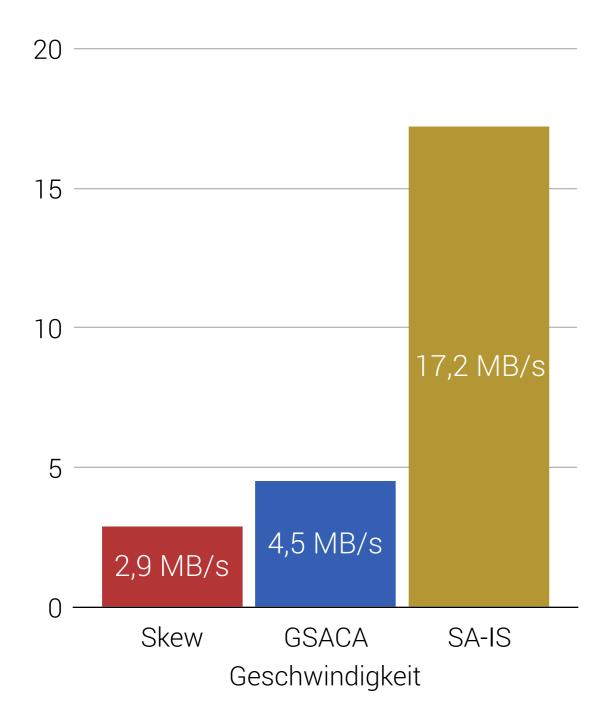
Linearzeit Ansätze

| | Skew | SA-IS | GSACA |
|----------|------------------------|-----------------------|------------------|
| Art | rekursiv | rekursiv | iterativ |
| Zeit | O(n) | O(n) | O(n) |
| Speicher | $O(\log n) + \max 24n$ | $O(\log n) + \max 2n$ | <i>O</i> (1) + ? |

Linearzeit Ansätze

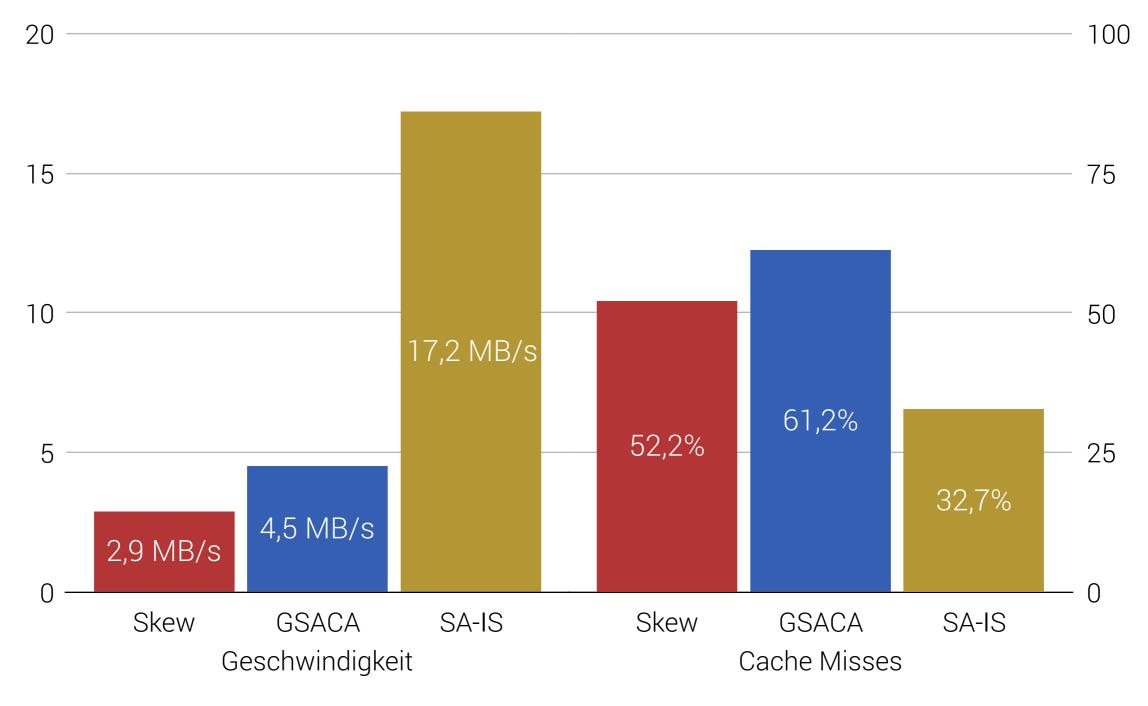
| | Skew | SA-IS | GSACA |
|----------|------------------------|-----------------------|------------|
| Art | rekursiv | rekursiv | iterativ |
| Zeit | O(n) | O(n) | O(n) |
| Speicher | $O(\log n) + \max 24n$ | $O(\log n) + \max 2n$ | O(1) + 12n |

GSACA im Vergleich



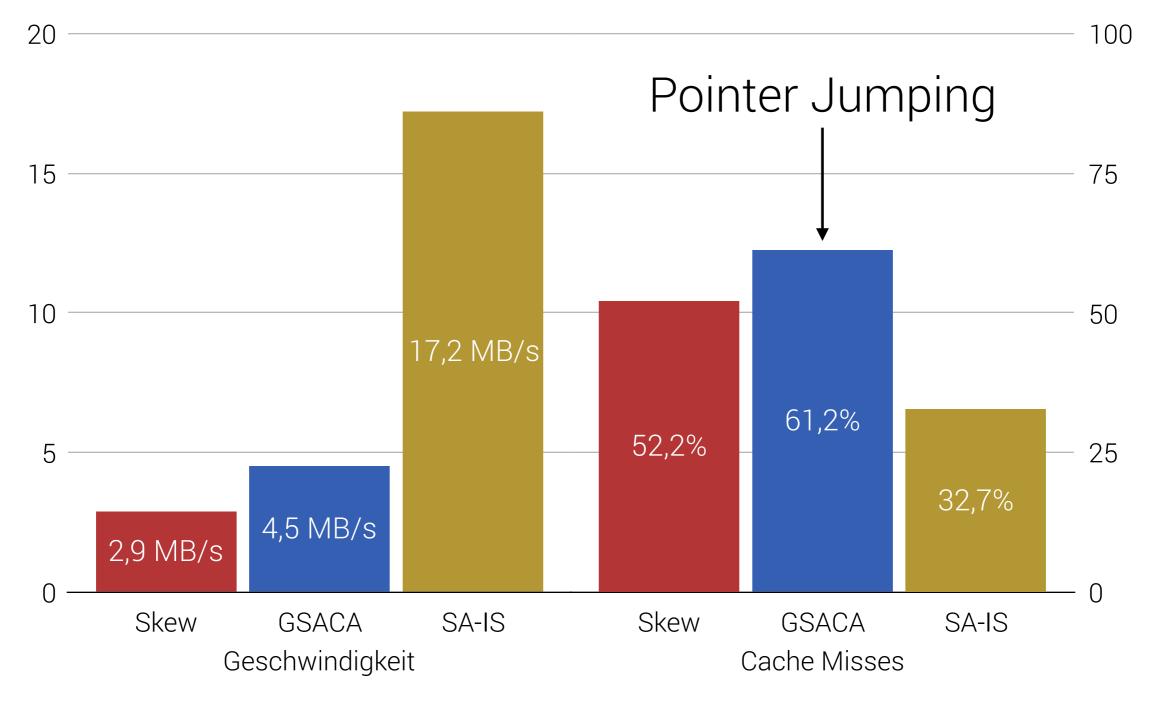
Testdaten: <u>Silesia Corpus</u>

GSACA im Vergleich



Testdaten: <u>Silesia Corpus</u>

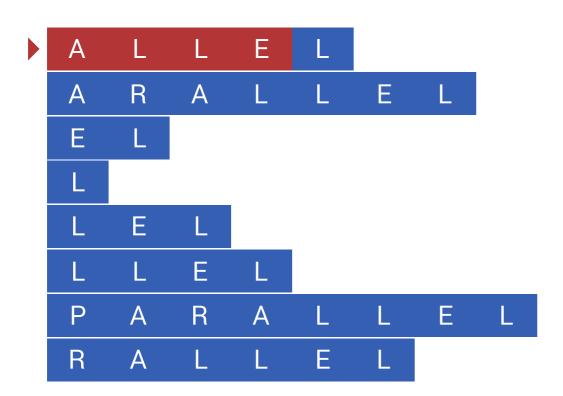
GSACA im Vergleich



Testdaten: <u>Silesia Corpus</u>

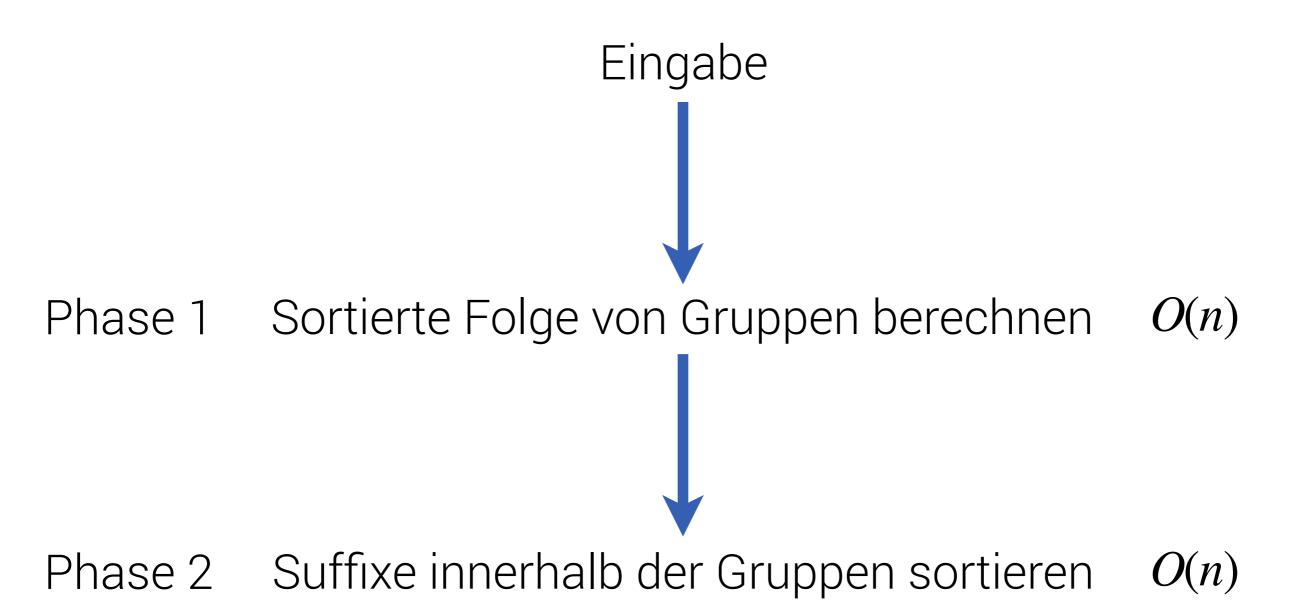
Einsatzgebiete

Substringsuche



LZ77 Kompression

GSACA



Noch nicht praxistauglich.

Noch nicht praxistauglich.

Noch nicht praxistauglich.

Neuartiges Konzept mit vielen spannenden noch zu lösenden Problemen...

Danke!