

Analysis of electrical power and energy systems

Practical session 7

25 November 2021

1 Transient stability and primary frequency control

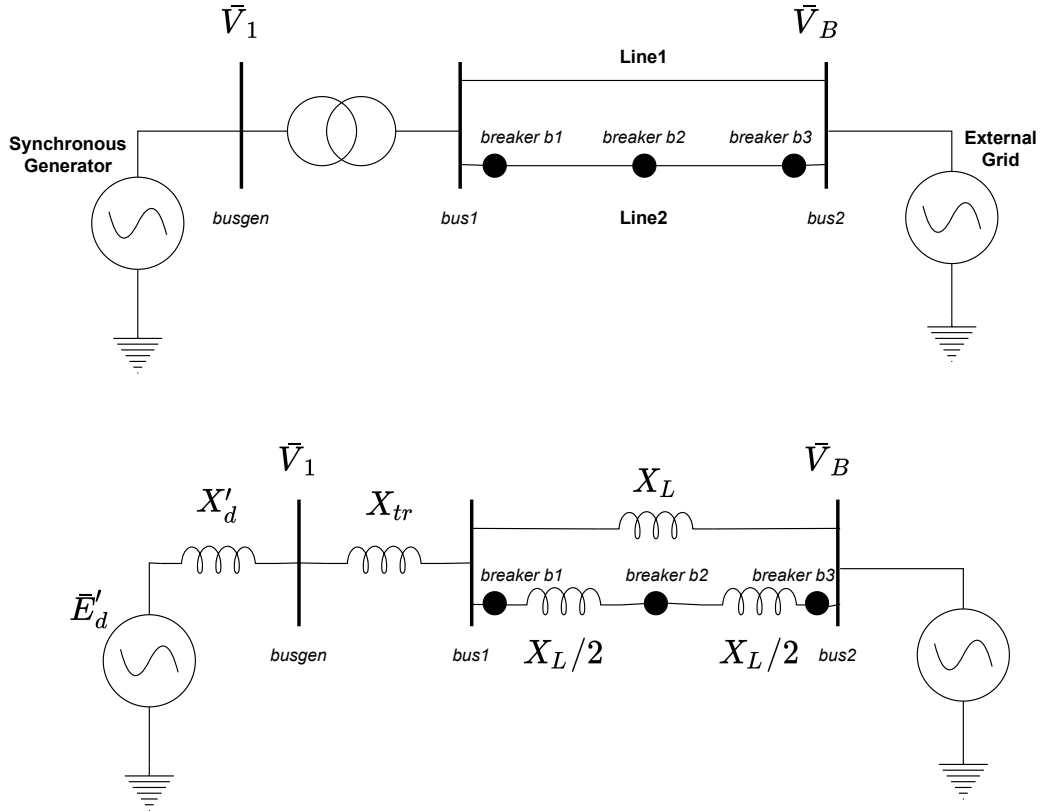


Figure 1: One-Machine-Infinite-Bus system.

1. Consider the one-machine-infinite-bus system shown in Figure 1. A synchronous generator converts a mechanical power P_m into an electrical power P_e (without conversion losses) which is transferred to the network through a step-up transformer and two parallel lines with same impedances. The electrical losses are not considered in this system therefore, the step-up transformer can be represented by an equivalent reactance X_{tr} . The following data are given :

$$X_L = 1pu, X'_d = 0.3pu, X_{tr} = 0.5pu, \bar{V}_B = 1\angle 0^\circ.$$

$$\text{Initial values : } \bar{E}'_d = E'_d \angle \delta, \bar{V}_1 = 1\angle 30^\circ$$

- (a) What is the initial active power transferred P_e ? Calculate the maximal power transmissible \hat{P}_e .
- (b) Consider a three-phase short-circuit close to breaker b_2 cleared by the tripping of line 2. Plot the $P - \delta$ curves for the three situations: before short-circuit, during

short-circuit and after short-circuit. Assume that the voltage magnitude E' is kept constant as well as voltage phasor \bar{V}_B .

- (c) Calculate the critical fault clearing angle δ_{cr} using the equal area criterion.
 - (d) What is the impact on the critical fault clearing angle if the short-circuit occurs close to breaker b_1 ?
2. A power system has a total load of 1260MW at 60Hz. The load varies 1.5% for every 1% change in frequency ($D = 1.5$). The system has 240MW of spinning reserve evenly spread among 500MW of generation capacity with 5% regulation based on this capacity. All other generators are operating with their valves wide open and are capable of down regulation only, also with $R = 5\%$. Find the steady-state frequency deviation when a 60MW load is suddenly tripped.¹

2 Solutions

Link to the Python notebook shown during the session: Python Notebook TP7

- 1. (a) $P_e = 0.5$ pu, $\hat{P}_e = 1.051$ pu
 - (b) See python notebook
 - (c) $\delta_{cr} = 49.37^\circ$
 - (d) $\delta_{cr} = 43.74^\circ$
2. $f_{ss} = 60.1132$ Hz

¹This exercise has been adapted from the course *31750 Stability and control in electric power systems* given at Technical University of Denmark.