

IB DIPLOMA PROGRAMME

Mathematics Standard Level SL  
Test on Common core material

## Test 2 P1

December 2019

40 minutes

Instructions to candidates:

- Write down your name in the space provided.
- Do not open this examination paper until instructed to do so.
- A graphic display calculator is **not allowed** for this test
- Answer all the questions
- Write your answers in the spaces provided.
- You are advised to show all working, where possible. Where an answer is wrong, some marks may be given for correct method, provided this is shown by written working.
- Unless otherwise stated in the question, all numerical **answers** must be given **exactly** or rounded to 3 significant figures.

Points: \_\_\_\_\_/40

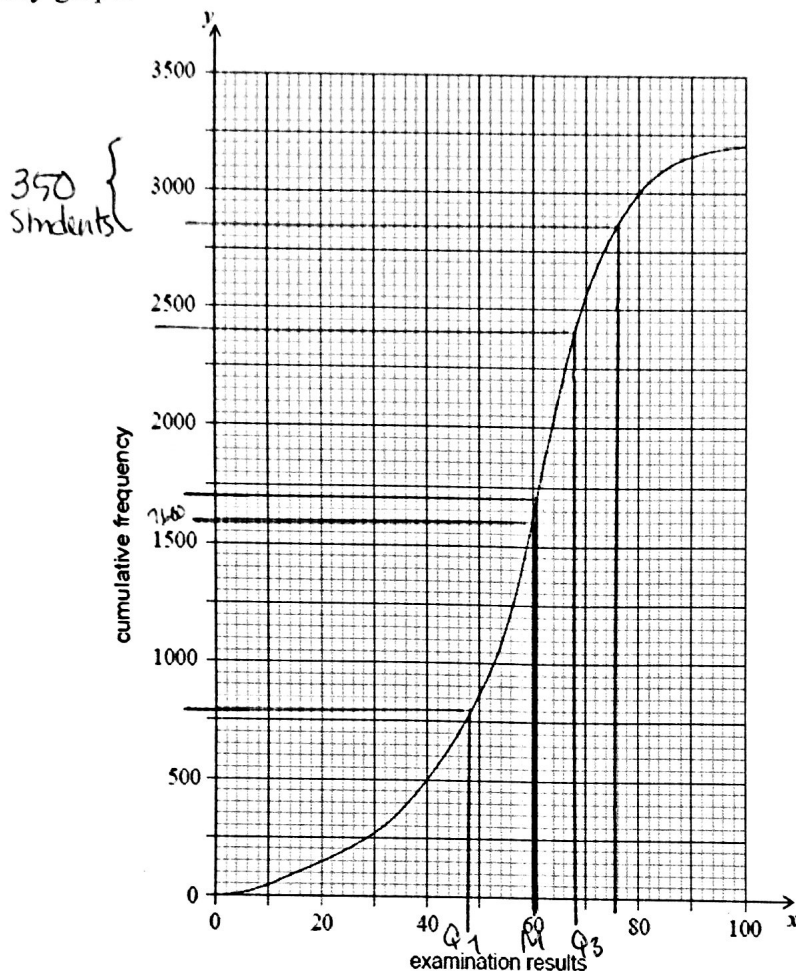
Grade:

Name: WORKED SOLUTIONS

Teacher: (AA, ARC or ANU) \_\_\_\_\_

**Question 1. [total marks: 8]**

The final examination results obtained by a group of 3200 Biology students are summarized on the cumulative frequency graph.



- a) Find the median of the examination results.

[2 marks]

median is 60 (M1) A1

- b) Find the interquartile range.

[3 marks]

$$IQR = Q_3 - Q_1$$

$$= 68 - 48 = 20$$

COULD BE SEEN ON GRAPH → M1 A1 A1

- c) 350 of the group obtained the highest possible grade in the examination.

Find the final examination result required to obtain the highest possible grade.

[3 marks]

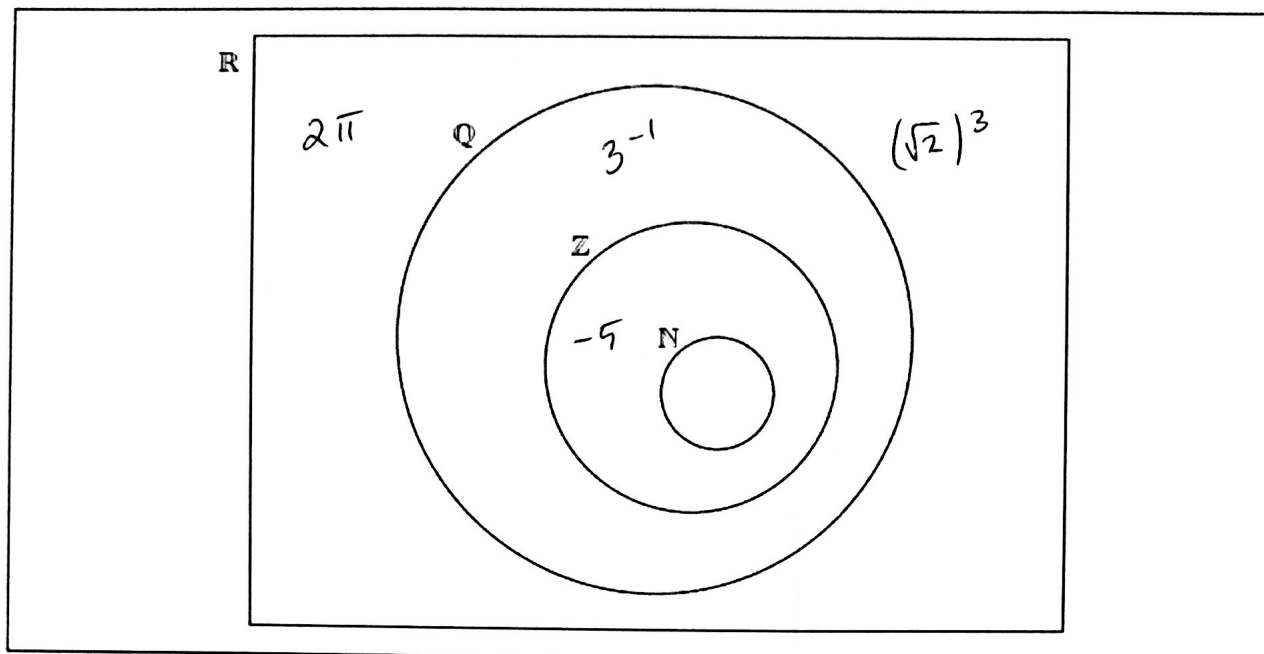
$$3200 - 350 = 2850 \quad (M1) \quad (\text{Drawing lines M1})$$

76 A1

**Question 2. [total marks: 6]**

- a) Place the numbers  $2\pi$ ,  $-5$ ,  $3^{-1}$  and  $(\sqrt{2})^3$  in the correct position on the Venn diagram.

[4 marks]



A1  
for each  
correct  
value  
on  
correct  
area

- b) In the table indicate which **two** of the given statements are true by placing a tick (✓) in the right hand column.

[2 marks]

Statement	True
$Z \subset Q$	✓
$N \subset Q'$	
$N \cap Z = N$	✓
$Q \cup R = Z'$	

A1

A1

A2 2 correct  
values

A1 1 correct  
value  
or 2 correct  
and 1 wrong

**Question 3. [total marks: 15]**

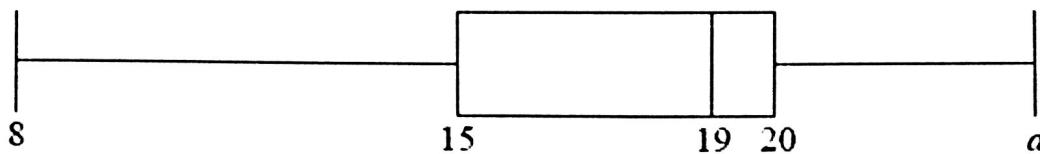
A group of 10 girls is to be sampled from all the girls in a school with 500 girls. The girls are selected for the sample from a list of all the 500 girls in a random order numbered from 1 to 500 by a systematic sampling method, starting with the 13<sup>th</sup> girl.

- (a) Write down the numbers of first 5 girls who are sampled.

[2 marks]

..... 13<sup>th</sup>, 53<sup>th</sup>, 113<sup>th</sup>, 163<sup>rd</sup>, 213<sup>th</sup> ..... A2 All 5 correct  
 ..... A1 3 or 4 correct

The group of 10 girls recorded the number of hours they spent watching television during a particular week. Their results are summarized in the box-and-whisker plot below.



- (b) The range of the data is 16. Find the value of  $a$ .

[2 marks]

..... range = max - min  
 ..... =  $a - 8 = 16 \Rightarrow a = 24$  ..... (M1) A1

- (c) Find the value of the interquartile range.

[2 marks]

..... IQR =  $Q_3 - Q_1$   
 ..... =  $20 - 15 = 5$  ..... (M1) A1

The group of girls watched a total of 180 hours of television.

- (d) Find the mean number of hours that the girls in this group spent watching television that week.

[2 marks]

.....  
 .....  $\bar{x} = \frac{180h}{10} = 18h$  ..... (M1) A1

A group of 20 boys also recorded the number of hours they spent watching television that same week. Their results are summarized in the table below.

$\bar{x} = 21$	$\sigma = 3$
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- (e) Find the total number of hours the group of boys spent watching television that week. [2 marks]

$$\begin{aligned} \text{total number of hours} &= 20(21) && \text{(M1)} \\ &= 420 \text{ h} && \text{A1} \end{aligned}$$

The following week, the group of boys had exams. During this exam week, the boys spent half as much time watching television compared to the previous week.

- (f) For this exam week, find
- (i) the mean number of hours that the group of boys spent watching television. [2 marks]

$$\bar{x} = 21\left(\frac{1}{2}\right) = 10.5 \text{ h} \quad \text{(M1) A1}$$

- (ii) the variance in the number of hours the group of boys spent watching television. [3 marks]

$$\begin{aligned} \text{original } \sigma &= 3 \\ \text{new } \sigma &= \frac{3}{2} \quad \text{(M1)} \quad \text{new variance } \left(\frac{3}{2}\right)^2 = \frac{9}{4} \quad \text{A1} \\ &\quad \text{(M1)} \end{aligned}$$

Question 4. [total marks: 6]

Line  $L_1$  passes through the points  $A(-3, 0.5)$  and  $B(9, -3.5)$ .

- (a) Find the gradient of  $L_1$ .

[2 marks]

$$m = \frac{\Delta y}{\Delta x} = \frac{-3.5 - 0.5}{9 - (-3)} = \frac{-4}{12} = -\frac{1}{3} \quad \text{M1} \quad \text{A1}$$

Line  $L_2$  passes through the point  $C(3, 1)$  and is parallel to  $L_1$ .

- (b) Determine the equation of  $L_2$ .

[2 marks]

Give your answer in the form  $ax + by + d = 0$ , where  $a$ ,  $b$ , and  $d$  are integers.

$$\begin{aligned} y - y_0 &= m(x - x_0) \\ y - 1 &= -\frac{1}{3}(x - 3) \\ y - 1 &= -\frac{1}{3}x + 1 \quad \text{M1} \\ y + \frac{1}{3}x - 2 &= 0 \quad / \times 3 \Rightarrow 3y + x - 6 = 0 \quad \text{A1} \end{aligned}$$

- (c) Find the coordinates of the  $x$ -intercept of  $L_2$ .

[2 marks]

$$\begin{aligned} x\text{-intercept is where } y &= 0 \\ 3y + x - 6 &= 0 \quad \text{M1} \\ 0 + x - 6 &= 0 \\ x &= 6 \quad \text{A1} \end{aligned}$$

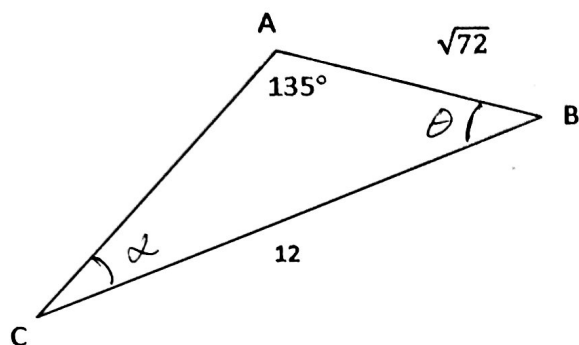
**Question 5. [total marks: 5]**

In triangle ABC, sides  $AB = \sqrt{72}$  and  $BC = 12$ . Angle  $CAB = 135^\circ$ .

You are given that  $\sin 135^\circ = \frac{1}{\sqrt{2}}$  and that  $\sin 30^\circ = \frac{1}{2}$ .

**Find angle ABC.**

The diagram is NOT to scale



$$\frac{\sin \alpha}{\sqrt{72}} = \frac{\sin 135^\circ}{12} \quad M1$$

$$\sin \alpha = \frac{\sqrt{72} \left( \frac{1}{\sqrt{2}} \right)}{12} \quad M1$$

$$= \frac{\frac{\sqrt{72}}{\sqrt{2}}}{12} = \frac{\sqrt{\frac{72}{2}}}{12}$$

$$= \frac{\sqrt{36}}{12} = \frac{6}{12} = \frac{1}{2}$$

$$\sin \alpha = \frac{1}{2} \quad \therefore \alpha = 30^\circ \quad A1$$

$$\theta + \alpha + 135^\circ = 180^\circ \quad M1$$

$$\theta = 180^\circ - 135^\circ - 30^\circ$$

$$\angle ABC \quad \theta = 15^\circ \quad A1$$