

Loiane Groner

Learning JavaScript Data Structures and Algorithms

Third Edition

Write complex and powerful JavaScript code using the latest ECMAScript



Packt

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Loiane Groner



BIRMINGHAM - MUMBAI

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Indexer: Rekha Nair

Graphics: Jason Monteiro

Production Coordinator: Arvindkumar Gupta

First published: October 2014

Second edition: June 2016

Third edition: April 2018

Production reference: 1250418

Published by Packt Publishing Ltd.

Livery Place

35 Livery Street

Birmingham

B3 2PB, UK.

ISBN 978-1-78862-387-2

www.packtpub.com

*To my parents, for their love and support and for guiding me throughout all these years.
To my husband, for his support and for being my loving partner throughout our life journey.*

– Loiane Groner



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Loiane Groner has over 10 years of experience in developing enterprise applications. Currently, she works as a business analyst and a Java/HTML5/JavaScript developer at an American financial institution.

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I would like to thank my parents, for giving me education, guidance, and advices through all these years, and my husband, for being patient and supportive and giving me encouragement so that I keep doing what I love.

I also would like to thank the readers of this book and other books that I have written for their support and feedback. Thank you very much!

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Preface

JavaScript is one of the most popular programming language nowadays. It is known as the internet language due the fact that the browser understands JavaScript natively, without installing any plugins in it. JavaScript has grown so much that is no longer just a frontend language; it is also present now on the server (NodeJS), database (MongoDB), and mobile devices and is also used in embedded and **Internet of Things (IoT)** devices.

Learning data structures is very important for any technology professional. Working as a developer means you are able to solve problems with the help of programming languages, and data structures are an indispensable piece of the solutions we need to create to solve these problems. Choosing a wrong data structure can also have an impact on the performance of the program we are writing. That is why, it's important to get to know different data structures and how to apply them properly.

Algorithms are the state of art of computer science. There are so many ways of solving the same problem, and some approaches are better than the others. That is why, it's also very important to know the most famous algorithms.

This book was written for beginners who want to learn data structures and algorithms and also for those who are already familiar with data structures and algorithms, but want to learn it using JavaScript.

Happy coding!

Who this book is for

If you are a student of computer science or are at the start of your technology career and want to explore JavaScript's optimum ability, this book is for you. If you are already familiar with programming, but want to hone your skills on algorithms and data structures, this book is also for you.

You just need a basic knowledge of JavaScript and programming logic to start having fun with algorithms.

What this book covers

Chapter 1, *JavaScript - A Quick Overview*, covers the basics of JavaScript needed prior to learning data structures and algorithms. It also covers the setup of the development environment needed for this book.

Chapter 2, *ECMAScript and TypeScript Overview*, covers some new JavaScript functionalities introduced since 2015 and also covers the basic functionalities of TypeScript, a JavaScript superset.

Chapter 3, *Arrays*, explains how to use the most basic and most used data structure, which are the arrays. This chapter demonstrates how to declare, initialize, add, and remove elements from an array. It also covers how to use native JavaScript Array methods.

Chapter 4, *Stacks*, introduces the stack data structure, demonstrating how to create a stack and add and remove elements. It also demonstrates how to use stack to solve some computer science-related problems.

Chapter 5, *Queues and Deques*, covers the queue data structure, demonstrating how to create a queue and add and remove its elements. It covers the deque data structure, a special type of the queue. It also demonstrates how to use queue to solve some computer science-related problems and the major differences between queues and stacks.

Chapter 6, *Linked Lists*, explains how to create the linked list data structure from scratch using objects and "pointer" concept. Besides covering how to declare, create, add, and remove elements, it also covers the various types of linked lists, such as the doubly linked list and circular linked list.

Chapter 7, *Sets*, introduces the set data structure and how it can be used to store non-repeated elements. It also explains the different types of set operations and how to implement and use them.

Chapter 8, *Dictionaries and Hashes*, explains the dictionary and hash data structures and the differences between them. This chapter covers how to declare, create, and use both data structures. It also explains how to handle collisions in hash and techniques for creating better hash functions.

Chapter 9, *Recursion*, introduces the concept of recursion and demonstrates the differences between declarative and recursive algorithms.

Chapter 10, *Trees*, covers the tree data structure, its terminology, focusing on Binary Search Tree data—its methods to search, traverse, add, and remove nodes. It also introduces self-balancing trees, such as the AVL and Red-Black trees.

Chapter 11, *Binary Heap and Heap Sort*, covers the min heap and max heap data structures, how to use the heap as a priority queue, and discusses the famous heap sort algorithm.

Chapter 12, *Graphs*, introduces the amazing world of graphs and its application in real-world problems. This chapter covers the most common graph terminology, the different way of representing a graph, how to traverse graphs using the Breadth-First Search and Depth-First Search algorithms and its applications.

Chapter 13, *Sorting and Searching Algorithms*, explores the most used sorting algorithms, such as the Bubble sort (and its improved version), Selection sort, Insertion sort, Merge sort, and Quick sort. It also covers the counting and radix sort, two distributed sorting algorithms. It also covers how to search algorithms, such as the sequential and binary search, and how to shuffle arrays.

Chapter 14, *Algorithm Designs and Techniques*, introduces some algorithm techniques and some of the most famous algorithms. It also covers an introduction to functional programming in JavaScript.

Chapter 15, *Algorithm Complexity*, introduces the Big-O notation and its concepts along with a cheat sheet of the complexity of the algorithms implemented in this book. It covers an introduction to NP-Completeness problems and heuristic solutions. At last, it explains how to take your algorithm knowledge to the next level.

To get the most out of this book

Although this book provides a brief introduction on JavaScript in its first chapter, you will need a basic knowledge of JavaScript and programming logic.

To test the code examples provided by this book, you will need a code editor (such as Atom or Visual Studio Code) so that you can read the code and also a browser (Chrome, Firefox, or Edge).

You can also test the examples online by accessing <https://javascript-ds-algorithms-book.firebaseioapp.com/>. Also, remember to open the developer tools of the browser so that you can see what is being outputted in the browser's console.

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Conventions used

There are a number of text conventions used throughout this book.

CodeInText: Indicates code words in text, database table names, folder names, filenames, file extensions, pathnames, dummy URLs, user input, and Twitter handles. Here is an example: "Mount the downloaded WebStorm-10*.dmg disk image file as another disk in your system."

A block of code is set as follows:

```
class Stack {  
    constructor() {  
        this.items = []; // {1}  
    }  
}
```

When we wish to draw your attention to a particular part of a code block, the relevant lines or items are set in bold:

```
const stack = new Stack();  
console.log(stack.isEmpty()); // outputs true
```

Any command-line input or output is written as follows:

```
npm install http-server -g
```

Bold: Indicates a new term, an important word, or words that you see onscreen. For example, words in menus or dialog boxes appear in the text like this. Here is an example: "Select **System info** from the **Administration** panel."

Warnings or important notes appear like this.



Tips and tricks appear like this.



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1

JavaScript – A Quick Overview

JavaScript is a very powerful language. It is one of the most popular languages in the world and is one of the most prominent languages on the internet. For example, GitHub (the world's largest code host, available at <https://github.com>) hosts over 400,000 JavaScript repositories (the largest number of projects available is in JavaScript; refer to <http://githut.info>). The number of projects in JavaScript and GitHub grows every year.

JavaScript is not a language that can only be used in the frontend. It can also be used in the backend, and Node.js is the technology responsible for this. The number of **Node Package Modules (npm)**, <https://www.npmjs.org>, has also grown exponentially. JavaScript can also be used for mobile development and is one of the most popular frameworks in Apache Cordova (<https://cordova.apache.org>), which is a mobile hybrid framework that allows developers to code using HTML, CSS, and JavaScript, which allows you to build an app and generate an APK file for Android and IPA file for iOS (Apple). And of course, let's not forget about desktop applications. We can write desktop applications compatible with Linux, Mac OS, and Windows using a JavaScript framework called Electron (<https://electron.atom.io>). JavaScript is also used in embedded and **Internet of Things (IoT)** devices. As you can see, JavaScript is everywhere!

JavaScript is a must-have on your resume if you are or are becoming a web developer.

In this chapter, you will learn the syntax and some necessary basic functionalities of JavaScript so that we can start developing our own data structures and algorithms. We will cover:

- Setting up the environment and JavaScript basics
- Controlling structures and functions
- Object-oriented programming in JavaScript
- Debugging and tools

JavaScript data structure and algorithms

In this book, you will learn about the most-used data structures and algorithms. Why should we use JavaScript to learn about data structures and algorithms? We have already answered this question. JavaScript is very popular and is appropriate for learning about data structures because it is a functional language. Also, this can be a very fun way of learning something new, as it is very different from (and easier than) learning about data structures with a standard language such as **C**, **Java**, or **Python**. And who said data structures and algorithms were only made for languages such as C and Java? You might need to implement some of these languages while developing for the frontend as well.

Learning about data structures and algorithms is very important. The first reason is that data structures and algorithms can solve the most common problems efficiently. This will make a difference to the quality of the source code you write in the future (including performance; if you choose the incorrect data structure or algorithm, depending on the scenario, you may have some performance issues). Secondly, algorithms are studied in college together with the introductory concepts of computer science. And finally, if you are planning on getting a job with one of the greatest **Information Technology (IT)** companies (such as Google, Amazon, Microsoft, eBay, and so on) data structures, and algorithms are the subjects of interview questions.

Let's get started!

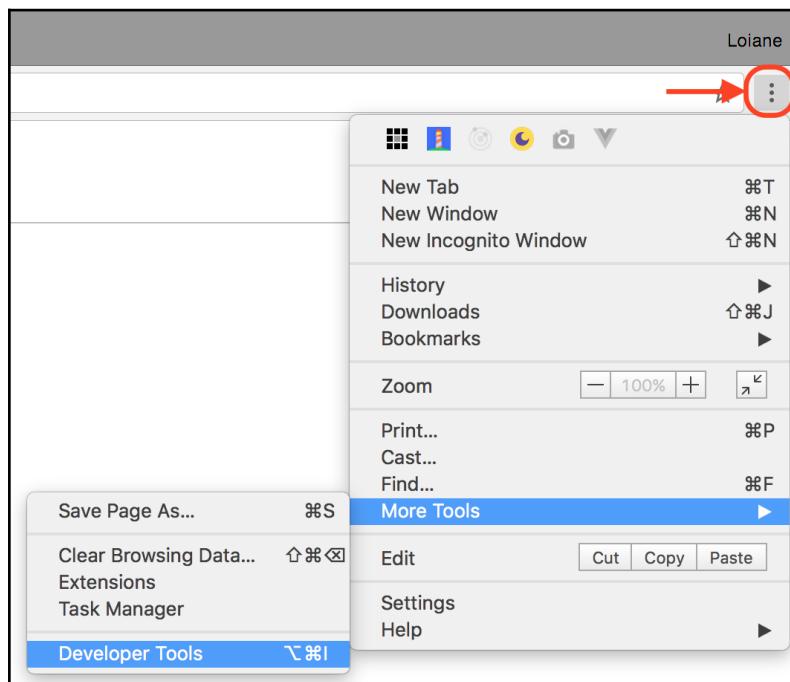
Setting up the environment

One of the pros of the JavaScript language compared to other languages is that you do not need to install or configure a complicated environment to get started with it. Every computer has the required environment already, even though the user may never write a single line of source code. All we need is a browser!

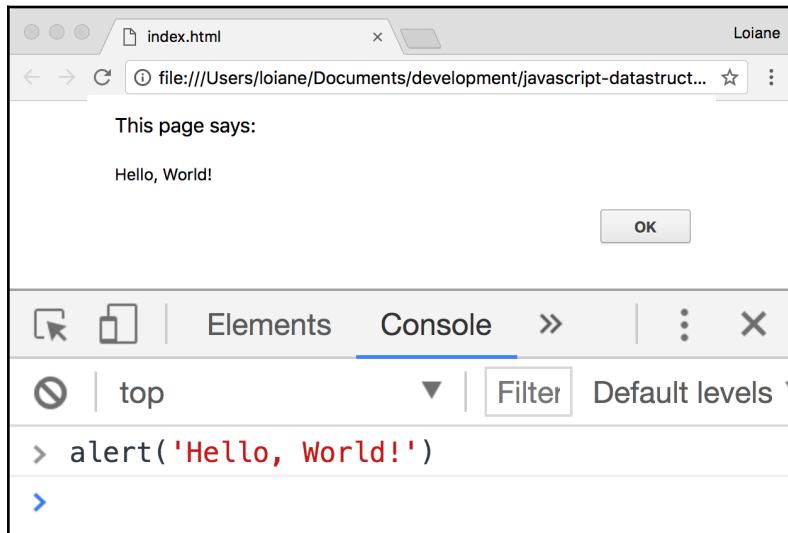
To execute the examples in this book, it is recommended that you have a modern browser installed such as Google Chrome or Firefox (you can use the one you like the most), an editor of your preference (such as Visual Studio Code), and a web server (XAMPP or any other of your preference, but this step is optional). Chrome, Firefox, VS Code, and XAMPP are available for Windows, Linux, and Mac OS.

The minimum setup to work with JavaScript

The simplest environment that you can use for JavaScript development is a browser. The modern browsers (Chrome, Firefox, Safari, and Edge) have a functionality called **Developer Tools**. To access the DevTools in Chrome, you can click on the menu in the upper-right corner, **More Tools** | **Developer Tools**:



When you open the DevTools, you will see the **Console** tab, and you will be able to write all your JavaScript code in its command-line area, as demonstrated in the following screenshot (to execute the source code, you need to press *Enter*):

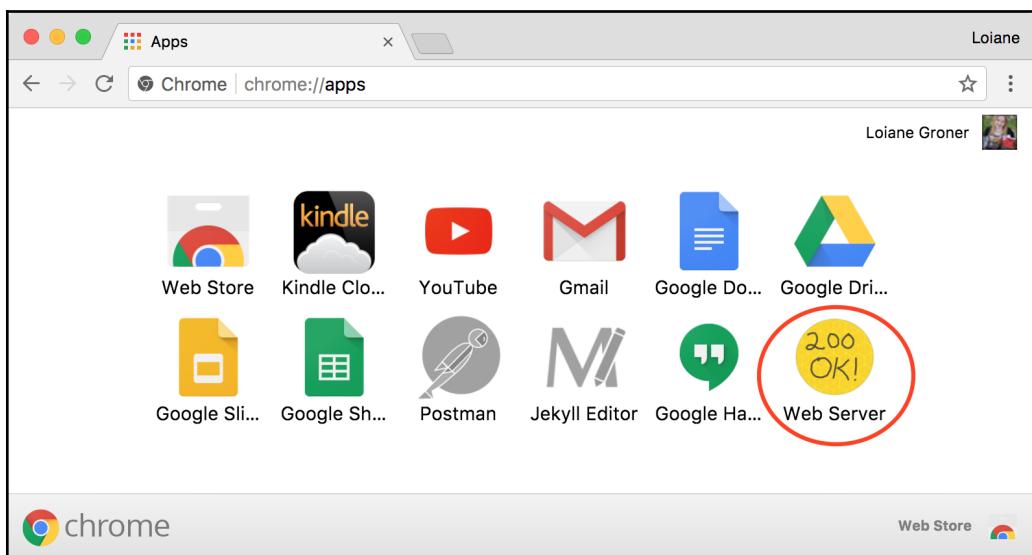


Using web servers

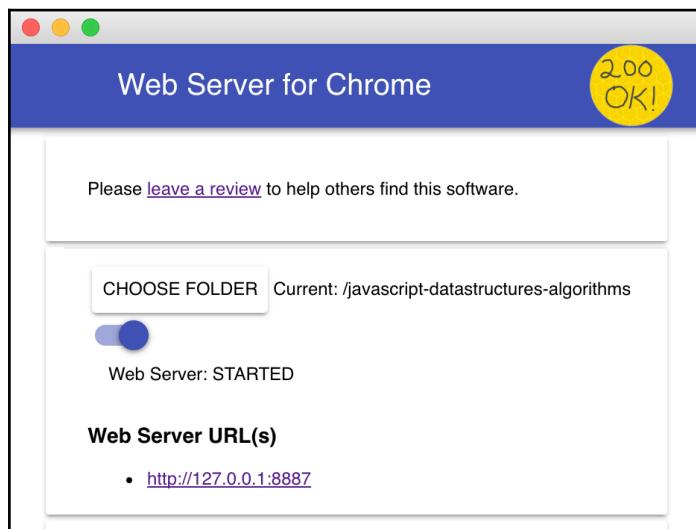
The second environment option you might want to install on your computer is also simple, but it requires installing a web server. If an HTML file contains only simple JavaScript code that does not require any request to a server (**Ajax** calls), it can be executed in the browser by right-clicking on the HTML file and selecting the **Open with** option. The code we will develop throughout this book is simple and it can be executed using this approach. However, it is always nice to have a web server installed.

There are many open source and free options available to you. If you are familiar with **PHP**, **XAMPP** (<https://www.apachefriends.org>) is a good option, and it is available for Linux, Windows, and Mac OS.

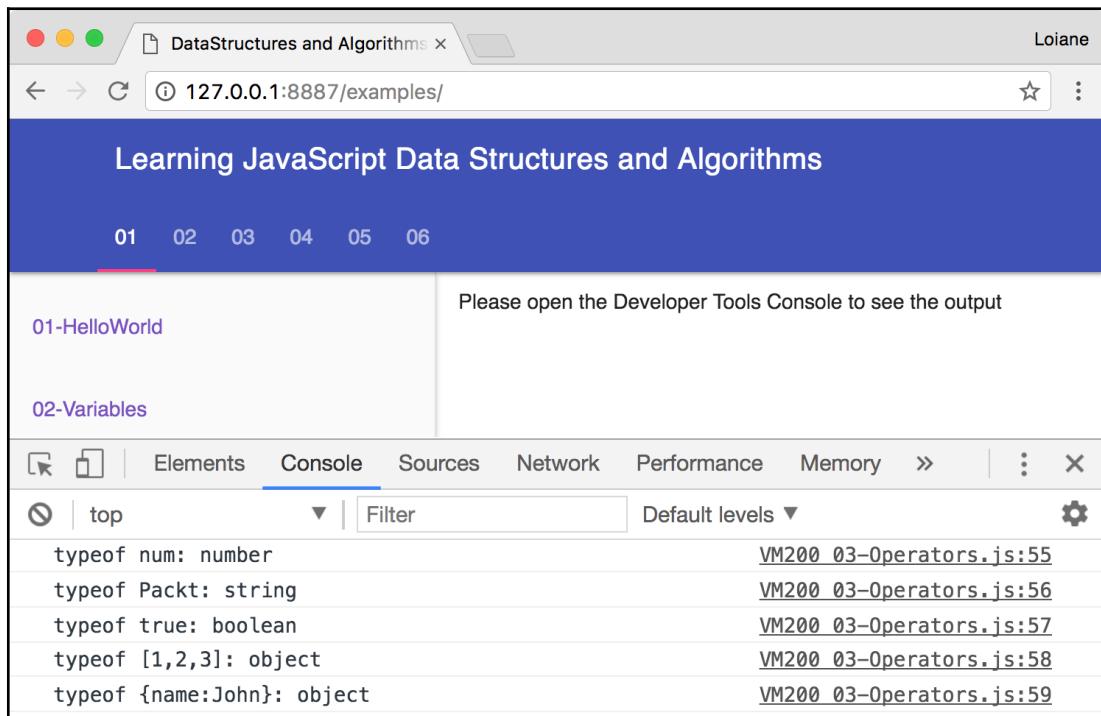
Since we will be focusing on JavaScript for the server side and the browser, there is also a simpler web server you can install in Chrome. It is the **Web Server for Chrome** extension, and this can be downloaded at <https://goo.gl/pxqLmU>. After installing it, you can access it through the Chrome URL `chrome://apps:`



After opening the **Web Server** extension, you can **CHOOSE FOLDER** you want to serve in the browser. You can create a new folder in which you can execute the source code we will implement throughout this book, or you can download the source code from this book and extract it to a directory of your preference and access it through the informed URL (the default is <http://127.0.0.1:8887>):



All examples from this book can be executed by accessing <http://127.0.0.1:8887/examples>. You will find an `index.html` with a list of all examples, as demonstrated in the following screenshot:



When executing the examples, always remember to have the **Developer Tools** enabled and the **Console** tab open to see the output. The Web Server for Chrome extension was also developed using JavaScript. For better experience, it is recommended to use this extension to execute the examples from this book or install the Node.js `http-server` we will learn in the next section.



Node.js http-server

The third option is having an environment that is 100 percent JavaScript! For this environment, we need to have Node.js installed. Go to <http://nodejs.org>, and download and install Node.js. After installing it, open the Terminal application (if you are using Windows, open the Command Prompt with Node.js, which was installed with Node.js) and run the following command:

```
npm install http-server -g
```

Make sure you type the command and don't copy and paste it. Copying the command might give you some errors. You can also execute the command as an administrator. For Linux and Mac systems, use the following command:

```
sudo npm install http-server -g
```

This command will install `http-server`, which is a JavaScript server. To start a server and run the examples from this book in the Terminal application, change the directory to the folder that contains the book's source code and type `http-server`, as displayed in the following screenshot:



A screenshot of a terminal window titled "javascript-datastructures-algorithms — node /usr/local/bin/http-server — 94x8". The terminal shows the following command being run:

```
loiane:~ loiane$ cd /Users/loiane/Documents/development/javascript-datastructures-algorithms
[loiane:javascript-datastructures-algorithms loiane$ http-server
Starting up http-server, serving .
Available on:
  http://127.0.0.1:8080
  http://192.168.0.11:8080
Hit CTRL-C to stop the server
```

To execute the examples, open the browser and access the localhost on the port specified by the `http-server` command.



Detailed steps to download the code bundle and run the examples are mentioned in the preface of this book. Please have a look. The code bundle for the book is also hosted on GitHub at <https://github.com/loiane/javascript-datastructures-algorithms>. We also have other code bundles from our rich catalog of books and videos available at <https://github.com/PacktPublishing>. Check them out!

JavaScript basics

Before we start diving in to the various data structures and algorithms, let's have a quick overview of the JavaScript language. This section will present the JavaScript basics required to implement the algorithms we will create in the subsequent chapters.

To start, let's look at the two different ways we can use JavaScript code on an HTML page. The first example is demonstrated by the following code. We need to create an HTML file (`01-HelloWorld.html`) and write this code in it. In this example, we are declaring the `script` tag inside the HTML file and, inside the `script` tag, we have the JavaScript code:

```
<!DOCTYPE html>
<html>
  <head>
    <meta charset="UTF-8">
  </head>
  <body>
    <script>
      alert('Hello, World!');
    </script>
  </body>
</html>
```



Try using the Web Server for Chrome extension or the `http-server` to run the preceding code and see its output in the browser.

For the second example, we need to create a JavaScript file (we can save it as `01-HelloWorld.js`) and, inside this file, we will insert the following code:

```
alert('Hello, World!');
```

Then, our HTML file will look similar to this:

```
<!DOCTYPE html>
<html>
  <head>
    <meta charset="UTF-8">
    <title></title>
  </head>
  <body>
    <script src="01-HelloWorld.js"></script>
  </body>
</html>
```

The second example demonstrates how to include a JavaScript file inside an HTML file.

By executing any of these two examples, the output will be the same. However, the second example is the most used by JavaScript developers.



You may find JavaScript `include` statements or JavaScript code inside the `head` tag in some examples on the internet. As a best practice, we will include any JavaScript code at the end of the `body` tag. This way, the HTML will be parsed by the browser and displayed before the scripts are loaded. This boosts the performance of the page.

Variables

Variables store data that can be set, updated, and retrieved whenever necessary. Values that are assigned to a variable belong to a type. In JavaScript, the available types are **number**, **string**, **boolean**, **function**, and **object**. We also have **undefined** and **null**, along with arrays, dates, and regular expressions.

Although JavaScript has different available variable types, it is not a **strongly typed** language such as C/C++, C#, and Java. In strongly typed languages, we need to declare the type of the variable along with its declaration (for example, in Java, to declare an integer variable, we use `int num = 1;`). In JavaScript, we only need to use the keyword `var`, and we do not need to declare the variable type. For this reason, JavaScript is not a strongly typed language. However, there are discussions and a specification in draft mode for optional static typing (<https://github.com/ds1omov/typed-objects-es7>) that can become part of the JavaScript specification (**ECMAScript**) in the future. We can also use **TypeScript** in case we want to type our variables when working with JavaScript. We will learn more about ECMAScript and TypeScript later in this chapter.

The following is an example of how to use variables in JavaScript:

```
var num = 1; // {1}
num = 3; // {2}
var price = 1.5; // {3}
var myName = 'Packt'; // {4}
var trueValue = true; // {5}
var nullVar = null; // {6}
var und; // {7}
```

- In line {1}, we have an example of how to declare a variable in JavaScript (we are declaring a number). Although it is not necessary to use the `var` keyword declaration, it is a good practice to always specify when we declare a new variable.
- In line {2}, we updated an existing variable. JavaScript is not a strongly typed language. This means you can declare a variable, initialize it with a number, and then update it with a string or any other datatype. Assigning a value to a variable that is different from its original type is also not a good practice.
- In line {3}, we also declared a number, but this time it is a decimal floating point. In line {4}, we declared a string; in line {5}, we declared a boolean. In line {6}, we declared a `null` value, and in line {7}, we declared an `undefined` variable. A `null` value means no value, and `undefined` means a variable that has been declared but not yet assigned a value.

If we want to see the value of each variable we declared, we can use `console.log` to do so, as listed in the following code snippet:

```
console.log('num: ' + num);
console.log('myName: ' + myName);
console.log('trueValue: ' + trueValue);
console.log('price: ' + price);
console.log('nullVar: ' + nullVar);
console.log('und: ' + und);
```

The `console.log` method also accepts more than just arguments. Instead of `console.log('num: ' + num)`, we can also use `console.log('num: ', num)`. While the first option is going to concatenate the result into a single string, the second option allows us to add a description and also visualize the variable content in case it is an object.



We have three ways of outputting values in JavaScript that we can use with the examples of this book. The first one is `alert('My text here')`, which outputs an alert window on the browser, and the second one is `console.log('My text here')`, which outputs text on the **Console** tab of the debug tool (Google Developer Tools or Firebug, depending on the browser you are using). The third way is outputting the value directly on the HTML page that is rendered by the browser using `document.write('My text here')`. You can use the option that you feel most comfortable with.

We will discuss functions and objects later in this chapter.

Scope variable

The scope refers to where in the algorithm we can access the variable (it can also be a function when we work with function scopes). There are local and global variables.

Let's look at an example:

```
var myVariable = 'global';
myOtherVariable = 'global';

function myFunction() {
    var myVariable = 'local';
    return myVariable;
}

function myOtherFunction() {
    myOtherVariable = 'local';
    return myOtherVariable;
}

console.log(myVariable); // {1}
console.log(myFunction()); // {2}

console.log(myOtherVariable); // {3}
console.log(myOtherFunction()); // {4}
console.log(myOtherVariable); // {5}
```

The above code can be explained as follows:

- Line {1} will output `global` because we are referring to a global variable.
- Line {2} will output `local` because we declared the `myVariable` variable inside the `myFunction` function as a local variable, so the scope will only be inside `myFunction`.
- Line {3} will output `global` because we are referencing the global variable named `myOtherVariable` that was initialized on the second line of the example.
- Line {4} will output `local`. Inside the `myOtherFunction` function, we referenced the `myOtherVariable` global variable and assigned the value `local` to it because we are not declaring the variable using the `var` keyword.
- For this reason, line {5} will output `local` (because we changed the value of the variable inside `myOtherFunction`).

You may hear that global variables in JavaScript are evil, and this is true. Usually, the quality of JavaScript source code is measured by the number of global variables and functions (a large number is bad). So, whenever possible, try avoiding global variables.

Operators

We need operators when performing any operation in a programming language. JavaScript also has arithmetic, assignment, comparison, logical, bitwise, and unary operators, among others. Let's take a look at these:

```
var num = 0; // {1}
num = num + 2;
num = num * 3;
num = num / 2;
num++;
num--;

num += 1; // {2}
num -= 2;
num *= 3;
num /= 2;
num %= 3;

console.log('num == 1 : ' + (num == 1)); // {3}
console.log('num === 1 : ' + (num === 1));
console.log('num != 1 : ' + (num != 1));
console.log('num > 1 : ' + (num > 1));
console.log('num < 1 : ' + (num < 1));
console.log('num >= 1 : ' + (num >= 1));
console.log('num <= 1 : ' + (num <= 1));

console.log('true && false : ' + (true && false)); // {4}
console.log('true || false : ' + (true || false));
console.log('!true : ' + (!true));
```

In line {1}, we have the arithmetic operators. In the following table, we have the operators and their descriptions:

Arithmetic operator	Description
+	Addition
-	Subtraction
*	Multiplication

/	Division
%	Modulus (remainder of a division operation)
++	Increment
--	Decrement

In line { 2 }, we have the assignment operators. In the following table, we have the operators and their descriptions:

Assignment operator	Description
=	Assignment
+=	Addition assignment ($x += y$) == ($x = x + y$)
-=	Subtraction assignment ($x -= y$) == ($x = x - y$)
*=	Multiplication assignment ($x *= y$) == ($x = x * y$)
/=	Division assignment ($x /= y$) == ($x = x / y$)
%=	Remainder assignment ($x %= y$) == ($x = x \% y$)

In line { 3 }, we have the comparison operators. In the following table, we have the operators and their descriptions:

Comparison operator	Description
==	Equal to
===	Equal to (both value and object type)
!=	Not equal to
>	Greater than
>=	Greater than or equal to
<	Less than
<=	Less than or equal to

Finally, in line { 4 }, we have the logical operators. In the following table, we have the operators and their descriptions:

Logical operator	Description
&&	And
	Or
!	Not

JavaScript also supports bitwise operators, which are shown as follows:

```
console.log('5 & 1:', (5 & 1));
console.log('5 | 1:', (5 | 1));
console.log('~ 5:', (~5));
console.log('5 ^ 1:', (5 ^ 1));
console.log('5 << 1:', (5 << 1));
console.log('5 >> 1:', (5 >> 1));
```

The following table contains a more detailed description of the bitwise operators:

Bitwise operator	Description
&	And
	Or
~	Not
^	Xor
<<	Left shift
>>	Right shift

The `typeof` operator returns the type of the variable or expression. For example, have a look at the following code:

```
console.log('typeof num:', typeof num);
console.log('typeof Packt:', typeof 'Packt');
console.log('typeof true:', typeof true);
console.log('typeof [1,2,3]:', typeof [1,2,3]);
console.log('typeof {name:John}:', typeof {name:'John'});
```

The output will be as follows:

```
typeof num: number
typeof Packt: string
typeof true: boolean
typeof [1,2,3]: object
typeof {name:John}: object
```

According to the specification, there are two data types in JavaScript:

- **Primitive data types:** Null, undefined, string, number, boolean, and symbol
- **Derived data types/objects:** JavaScript objects, including functions, arrays, and regular expressions

JavaScript also supports the `delete` operator, which deletes a property from an object:

```
var myObj = {name: 'John', age: 21};
delete myObj.age;
console.log(myObj); //outputs Object {name: "John"}
```

In this book's algorithms, we will be using some of these operators.

Truthy and falsy

In JavaScript, `true` and `false` are a little bit tricky. In most languages, the boolean values `true` and `false` represent the true/false results. In JavaScript, a string such as `Packt` evaluates to `true`.

The following table can help us better understand how `true` and `false` work in JavaScript:

Value Type	Result
<code>undefined</code>	<code>false</code>
<code>null</code>	<code>false</code>
<code>Boolean</code>	<code>true</code> is <code>true</code> and <code>false</code> is <code>false</code>
<code>Number</code>	The result is <code>false</code> for <code>+0</code> , <code>-0</code> , or <code>NaN</code> ; otherwise, the result is <code>true</code>
<code>String</code>	The result is <code>false</code> if the string is empty (<code>length</code> is 0); otherwise, the result is <code>true</code> (<code>length</code> ≥ 1)
<code>Object</code>	<code>true</code>

Let's consider some examples and verify their output:

```
function testTruthy(val) {
    return val ? console.log('truthy') : console.log('falsy');
}

testTruthy(true); // true
testTruthy(false); // false
testTruthy(new Boolean(false)); // true (object is always true)

testTruthy(''); // false
testTruthy('Packt'); // true
testTruthy(new String('')); // true (object is always true)

testTruthy(1); // true
testTruthy(-1); // true
testTruthy(NaN); // false
testTruthy(new Number(NaN)); // true (object is always true)

testTruthy({}); // true (object is always true)

var obj = { name: 'John' };
testTruthy(obj); // true
testTruthy(obj.name); // true
testTruthy(obj.age); // age (property does not exist)
```

Functions of the equals operators (== and ===)

The two equals operators supported by JavaScript can cause a little bit of confusion when working with them.

When using ==, values can be considered equal even when they are of different types. This can be confusing even for a senior JavaScript developer. Let's analyze how == works using the following table:

Type(x)	Type(y)	Result
null	undefined	true
undefined	null	true
Number	String	x == toNumber(y)
String	Number	toNumber(x) == y
Boolean	Any	toNumber(x) == y

Any	Boolean	<code>x == toNumber(y)</code>
String or Number	Object	<code>x == toPrimitive(y)</code>
Object	String or number	<code>toPrimitive(x) == y</code>

If `x` and `y` are of the same type, then JavaScript will use the `equals` method to compare the two values or objects. Any other combination that is not listed in the table gives a `false` result.

The `toNumber` and `toPrimitive` methods are internal and evaluate the values according to the tables that follow.

The `toNumber` method is as follows:

Value type	Result
<code>undefined</code>	This is <code>Nan</code>
<code>null</code>	This is <code>+0</code>
<code>Boolean</code>	If the value is <code>true</code> , the result is <code>1</code> ; if the value is <code>false</code> , the result is <code>+0</code>
<code>Number</code>	This is the value of the number

Finally, `toPrimitive` is as follows:

Value Type	Result
<code>Object</code>	If <code>valueOf</code> returns a primitive value, it returns the primitive value; otherwise, if <code>toString</code> returns a primitive value, it returns the primitive value and otherwise returns an error

Let's verify the results of some examples. First, we know that the output of the following code is `true` (`string length > 1`):

```
console.log('packt' ? true : false);
```

Now, what about the following code? Let's take a look:

```
console.log('packt' == true);
```

The output is `false`, so let's understand why:

- First, it converts the boolean value using `toNumber`, so we have `packt == 1`.
- Then, it converts the string value using `toNumber`. Since the string consists of alphabetical characters, it returns `Nan`, so we have `Nan == 1`, which is `false`.

What about the following code? Let's take a look:

```
console.log('packt' == false);
```

The output is also `false`, and the following is why:

- First, it converts the boolean value using `toNumber`, so we have `packt == 0`.
- Then, it converts the string value using `toNumber`. Since the string consists of alphabetical characters, it returns `Nan`, so we have `Nan == 0`, which is `false`.

What about the `==` operator? This is much easier. If we are comparing two values of different types, the result is always `false`. If they have the same type, they are compared according to the following table:

Type(x)	Values	Result
Number	x has the same value as y (but not <code>Nan</code>)	true
String	x and y are identical characters	true
Boolean	x and y are both <code>true</code> or both <code>false</code>	true
Object	x and y reference the same object	true

If `x` and `y` are different types, then the result is `false`. Let's consider some examples:

```
console.log('packt' === true); //false
console.log('packt' === 'packt'); //true
var person1 = {name:'John'};
var person2 = {name:'John'};
console.log(person1 === person2); //false, different objects
```

Control structures

JavaScript has a similar set of control structures as the C and Java languages. Conditional statements are supported by `if...else` and `switch`. Loops are supported by the `while`, `do...while`, and `for` constructs.

Conditional statements

The first conditional statement we will take a look at is the `if...else` construct. There are a few ways we can use the `if...else` construct.

We can use the `if` statement if we want to execute a block of code only if the condition (expression) is `true`, as follows:

```
var num = 1;
if (num === 1) {
    console.log('num is equal to 1');
}
```

We can use the `if...else` statement if we want to execute a block of code and the condition is `true` or another block of code just in case the condition is `false` (`else`), as follows:

```
var num = 0;
if (num === 1) {
    console.log('num is equal to 1');
} else {
    console.log('num is not equal to 1, the value of num is ' + num);
}
```

The `if...else` statement can also be represented by a ternary operator. For example, take a look at the following `if...else` statement:

```
if (num === 1) {
    num--;
} else {
    num++;
}
```

It can also be represented as follows:

```
(num === 1) ? num-- : num++;
```

Also, if we have several expressions, we can use `if...else` several times to execute different blocks of code based on different conditions, as follows:

```
var month = 5;
if (month === 1) {
    console.log('January');
} else if (month === 2) {
    console.log('February');
} else if (month === 3) {
    console.log('March');
} else {
    console.log('Month is not January, February or March');
}
```

Finally, we have the `switch` statement. If the condition we are evaluating is the same as the previous one (however, it is being compared to different values), we can use the `switch` statement:

```
var month = 5;
switch (month) {
    case 1:
        console.log('January');
        break;
    case 2:
        console.log('February');
        break;
    case 3:
        console.log('March');
        break;
    default:
        console.log('Month is not January, February or March');
}
```

One thing that is very important in a `switch` statement is the use of the `case` and `break` keywords. The `case` clause determines whether the value of `switch` is equal to the value of the `case` clause. The `break` statement stops the `switch` statement from executing the rest of the statement (otherwise, it will execute all the scripts from all `case` clauses below the matched case until a `break` statement is found in one of the `case` clauses). Finally, we have the `default` statement, which is executed by default if none of the `case` statements are true (or if the executed `case` statement does not have the `break` statement).

Loops

Loops are often used when we work with arrays (which are the subject of the next chapter). Specifically, we use the `for` loop in our algorithms.

The `for` loop is the same as in C and Java. It consists of a loop counter that is usually assigned a numeric value, then the variable is compared against another value (the script inside the `for` loop is executed while this condition is true), and finally, the numeric value is increased or decreased.

In the following example, we have a `for` loop. It outputs the value of `i` on the console, where `i` is less than 10; `i` is initiated with 0, so the following code will output the values 0 to 9:

```
for (var i = 0; i < 10; i++) {  
    console.log(i);  
}
```

The next loop construct we will look at is the `while` loop. The block of code inside the `while` loop is executed while the condition is true. In the following code, we have a variable, `i`, initiated with the value 0, and we want the value of `i` to be output while `i` is less than 10 (or less than or equal to 9). The output will be the values from 0 to 9:

```
var i = 0;  
while (i < 10) {  
    console.log(i);  
    i++;  
}
```

The `do...while` loop is similar to the `while` loop. The only difference is that in the `while` loop, the condition is evaluated before executing the block of code, and in the `do...while` loop, the condition is evaluated after the block of code is executed. The `do...while` loop ensures that the block of code is executed at least once. The following code also outputs the values from 0 to 9:

```
var i = 0;  
do {  
    console.log(i);  
    i++;  
} while (i < 10);
```

Functions

Functions are very important when working with JavaScript. We will also use functions in our examples.

The following code demonstrates the basic syntax of a function. It does not have arguments or the `return` statement:

```
function sayHello() {  
    console.log('Hello!');  
}
```

To execute this code, we simply use the following statement:

```
sayHello();
```

We can also pass arguments to a function. Arguments are variables with which a function is supposed to do something. The following code demonstrates how to use arguments with functions:

```
function output(text) {  
    console.log(text);  
}
```

To use this function, we can use the following code:

```
output('Hello!');
```

You can use as many arguments as you like, as follows:

```
output('Hello!', 'Other text');
```

In this case, only the first argument is used by the function, and the second one is ignored. A function can also return a value, as follows:

```
function sum(num1, num2) {  
    return num1 + num2;  
}
```

This function calculates the sum of two given numbers and returns its result. We can use it as follows:

```
var result = sum(1, 2);  
output(result); // outputs 3
```

Object-oriented programming in JavaScript

JavaScript objects are very simple collections of name-value pairs. There are two ways of creating a simple object in JavaScript. The first way is as follows:

```
var obj = new Object();
```

And the second way is as follows:

```
var obj = {};
```

We can also create an entire object, as follows:

```
obj = {
  name: {
    first: 'Gandalf',
    last: 'the Grey'
  },
  address: 'Middle Earth'
};
```

As we can see, to declare a JavaScript object, *[key, value]* pairs are used, where the key can be considered an attribute of the object and the value is the property value. All classes that we will create in this book are JavaScript objects, such as `Stack`, `Set`, `LinkedList`, `Dictionary`, `Tree`, `Graph`, and so on.

In **Object-oriented programming (OOP)**, an object is an instance of a class. A class defines the characteristics of the object. For our algorithms and data structures, we will create some classes that will represent them. This is how we can declare a class (constructor) that represents a book:

```
function Book(title, pages, isbn) {
  this.title = title;
  this.pages = pages;
  this.isbn = isbn;
}
```

To instantiate this class, we can use the following code:

```
var book = new Book('title', 'pag', 'isbn');
```

Then, we can access its properties and update them as follows:

```
console.log(book.title); // outputs the book title
book.title = 'new title'; // update the value of the book title
console.log(book.title); // outputs the updated value
```

A class can also contain functions (generally also referred to as **methods**). We can declare and use a function/method as the following code demonstrates:

```
Book.prototype.printTitle = function() {  
    console.log(this.title);  
};  
  
book.printTitle();
```

We can declare functions directly inside the class definition as well:

```
function Book(title, pages, isbn) {  
    this.title = title;  
    this.pages = pages;  
    this.isbn = isbn;  
    this.printIsbn = function() {  
        console.log(this.isbn);  
    };  
}  
book.printIsbn();
```



In the prototype example, the `printTitle` function will be shared between all the instances and only one copy will be created. When we use a class-based definition, as in the previous example, each instance will have its own copy of the functions. Using the `prototype` method saves memory and processing cost regarding assigning the functions to the instance. However, you can only declare `public` functions and properties using the `prototype` method. With a class-based definition, you can declare `private` functions and properties, and the other methods inside the class can also access them. ECMAScript 2015 (ES6) introduces a simplified syntax like the class-based example and it is `prototype`-based. We will discuss more on this later in this chapter.

Debugging and tools

Knowing how to program with JavaScript is important, but so is knowing how to debug your code. Debugging is very useful in helping you find bugs in your code, but it can also help you execute your code at a lower speed so that you can see everything that is happening (the stack of methods called, variable assignment, and so on). It is highly recommended that you spend some time debugging the source code of this book to see every step of the algorithm (it might help you understand it better as well).

Firefox, Safari, Edge, and Chrome support debugging. A great tutorial from Google that shows you how to use Google Developer Tools to debug JavaScript can be found at <https://developer.chrome.com/devtools/docs/javascript-debugging>.

You can use any text editor of your preference. However, there are other great tools that can help you be more productive when working with JavaScript as well, which are listed as follows:

- **WebStorm:** This is a very powerful JavaScript IDE with support for the latest web technologies and frameworks. It is a paid IDE, but you can download a 30-day trial version (<http://www.jetbrains.com/webstorm>).
- **Sublime Text:** This is a lightweight text editor and you can customize it by installing plugins. You can buy the license to support the development team, but you can also use it for free (the trial version does not expire) at <http://www.sublimetext.com>.
- **Atom:** This is also a free text editor created by GitHub. It has great support for JavaScript and it can also be customized by installing plugins (<https://atom.io>).
- **Visual Studio Code:** This is a free and open source code editor created by Microsoft, written with TypeScript. It has JavaScript autocomplete functionality with IntelliSense and provides built-in debug capability directly from the editor. It can also be customized by installing plugins (<https://code.visualstudio.com>).

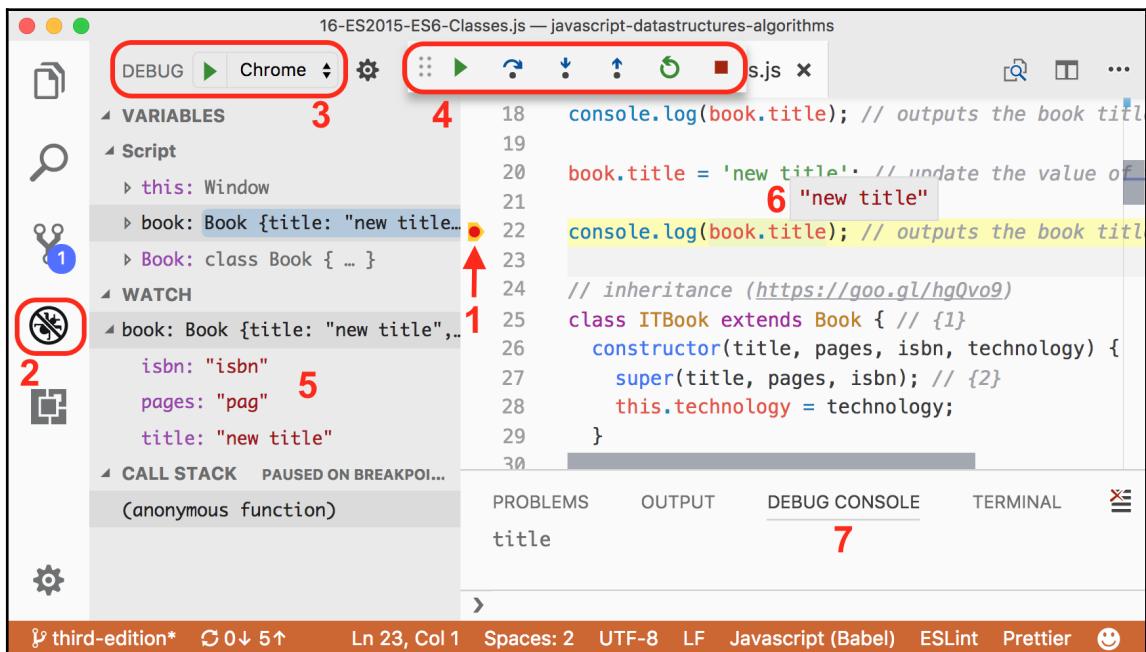
All of the aforementioned editors are available for Windows, Linux, and Mac OS.

Debugging with VSCode

To debug JavaScript or ECMAScript code directly from VSCode, first, we need to install the Debugger for Chrome extension (<https://goo.gl/QpxWGM>).

Next, open the Web Server for Chrome extension and open the link to see the book examples in the browser (the default URL is <http://127.0.0.1:8887/examples>).

The following screenshot demonstrates how to debug directly from the editor:



1. In the editor, open the JavaScript file you want to debug, pass the mouse pointer near the line numbers, and click on the line to add a breakpoint (as demonstrated by 1 in the preceding screenshot). This is where the debugger will stop so we can analyze the code.
2. Once the Web Server is up and running, click on the Debug view (2), select Chrome (3), and click on the Play icon to initiate the debugging process.
3. Chrome will be opened automatically. Navigate to the desired example to evoke the code we want to debug. Once the line we added the breakpoint to is reached by the debugger, the process will stop and the editor will receive the focus.
4. We can control how the code is debugged using the top toolbar (4). We can resume the process, go to a method call, go to the next line, and restart and stop the process. It is the same behavior we have in the debugger in Chrome and other browsers.
5. The advantage of using this built-in debug functionality is that we can do everything from the editor (coding, debugging, and testing). And we also have the variables declared and call stack, we can watch variables and expressions (5), hover the mouse over a variable to see its current value (6), and see the console output as well (7).

The source code of this book was developed using Visual Studio Code and the code bundle also contains configured launch tasks so you can debug the code and the tests directly from the **VSCODE** (all details are in the `.vscode/launch.json` file). All extensions recommended to run the source code from this book are also listed in the `.vscode/extensions.json` file.

Summary

In this chapter, we learned how to set up the development environment to be able to create or execute the examples in this book.

We also covered the basics of the JavaScript language that are needed prior to getting started with developing the algorithms and data structures covered in this book.

In the next chapter, we will learn about new functionalities introduced to JavaScript since 2015 and also how to leverage static typing and error checking using TypeScript.

2

ECMAScript and TypeScript Overview

The JavaScript language evolves every year. Since 2015, there has been a new version released every year, which we call **ECMAScript**, and as JavaScript is a very powerful language, it is also used for enterprise development. One of the capabilities that really helps in this type of development (among other types of application) is typed variables, which we now have, thanks to **TypeScript**, a superset of JavaScript.

In this chapter, you will learn some functionalities that were introduced to JavaScript since 2015, and also the advantages of using a typed version of JavaScript in our projects. We will cover the following:

- Introduction to ECMAScript
- JavaScript in the browser versus in the server
- Introduction to TypeScript

ECMAScript or JavaScript?

When working with JavaScript, we find the term ECMAScript very often in books, blog posts, video courses, and so on. What does ECMAScript have to do with JavaScript, and is there a difference?

ECMA is an organization that standardizes information. Long story short, a long time ago, JavaScript was submitted to ECMA for standardization. This resulted in a new language standard, which we know as ECMAScript. JavaScript is an implementation of this specification (the most popular), which is known as **ActionScript**.

ES6, ES2015, ES7, ES2016, ES8, ES2017, and ES.Next

As we already know, JavaScript is a language that runs mostly on browsers (as well as in servers using NodeJS, and in desktop and mobile devices), and each browser can implement its own version of the available functionalities of JavaScript (as you will learn later on in this book). This specific implementation is based on ECMAScript. Thus, the browsers offer mostly the same functionalities (our JavaScript code will run in all browsers); however, each functionality's behavior may be a little bit different from browser to browser.

All the code presented in this chapter so far is based on ECMAScript 5 (ES5 - ES is simply short for ECMAScript), which became a standard in December 2009. ECMAScript 2015 (ES2015) was standardized in June 2015, almost 6 years after its previous edition. The name ES6 became popular before the release of ES2015.

The committee responsible for drafting the ECMAScript specifications made the decision to move to a yearly model to define new standards, where new features would be added as they were approved. For this reason, ECMAScript sixth edition was renamed to ECMAScript 2015 (ES6).

In June 2016, ECMAScript seventh edition was standardized. We know this edition as **ECMAScript 2016 or ES2016 (ES7)**.

In June 2017, ECMAScript eighth edition was standardized. We know this edition as **ECMAScript 2017 or ES2017 (ES8)**. At the time of writing this book, this is the most recent edition of ES.

You also might see **ES.Next** in some resources. This term is a reference to the next edition of ECMAScript.

In this topic, we will cover some of the new functionalities introduced in ES2015 onwards, which will be helpful when we develop our data structures and algorithms.

The compatibility table

It is important to know that, even though ES2015 - ES2017 have already been released, its features might not be supported by all browsers. For a better experience, it is always best to use the latest version available for the browser you choose to use.

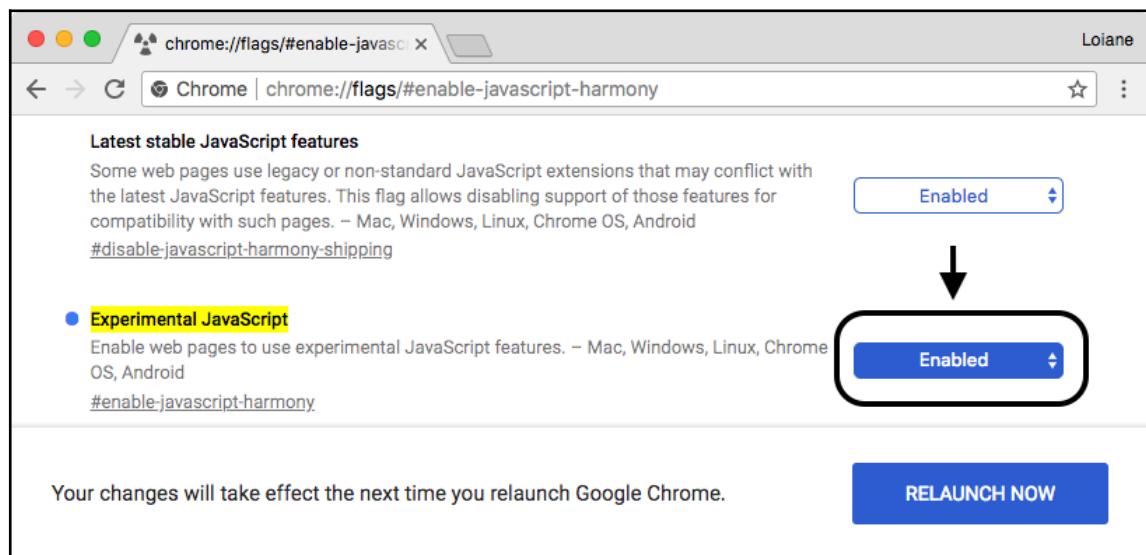
At the following links, you can verify which features are available in each browser:

- **ES2015 (ES6):** <http://kangax.github.io/compat-table/es6/>
- **ES2016+:** <http://kangax.github.io/compat-table/es2016plus/>

After ES5, the biggest ES release was ES2015. According to the compatibility table in the preceding link, most of its features are available in modern browsers. Even if some of the features of ES2016+ are not yet available, we can start using new syntax and new functionalities today.

By default, Firefox adds support for ES as their team ships the implementation of the functionalities.

In Google Chrome, you can enable these functionalities by enabling the **Experimental JavaScript** flag by opening the URL `chrome://flags/#enable-javascript-harmony`, as demonstrated in the following image:



In Microsoft Edge, you can navigate to `about:flags` and select the **Enable experimental JavaScript features** flag (a similar process to Chrome).



Even with the **Enable Experimental JavaScript** flag enabled, some of the ES2016+ features might not be supported in Chrome or Edge. The same can be applied to Firefox. To know exactly which features are already supported in each browser, please verify the compatibility table.

Using Babel.js

Babel (<https://babeljs.io>) is a JavaScript transpiler, also known as a source-to-source compiler. It converts JavaScript code with ECMAScript language features to equivalent code that uses only language features from the widely supported ES5 specification.

There are many ways of using Babel.js. One of them is installing it according to its setup (<https://babeljs.io/docs/setup>). Another one is using it directly in the browser through its **Try it out** option (<https://babeljs.io/repl>), as demonstrated in the following screenshot:

The screenshot shows a web browser window titled "Babel · The compiler for writing..." with the URL "https://babeljs.io/repl#?babili=false&browsers=...". The main area is yellow and displays the word "BABEL" in large, stylized letters. Below this is a code editor with two columns. The left column contains the following code:

```
1 console.log('Babel');
```

The right column contains the generated ES5 code:

```
1 'use strict';
2
3 console.log('Babel');
```

Along with each example that will be presented in the following topics, we will also provide a link so that you can run and test the examples in Babel.

ECMAScript 2015+ functionalities

In this topic, we will demonstrate how to use some of the functionalities of ES2015, which may be useful in everyday JavaScript coding and which will also be useful to simplify the examples presented in the following chapters of this book.

Among the functionalities, we will cover the following:

- Variables with `let` and `const`
- Template literals
- Destructuring
- Spread operator
- Arrow functions using `=>`
- Classes
- Modules

let and const instead of var

Until ES5, we could declare variables in any place in our code, even if we overwrote the variables declaration, as in the following code:

```
var framework = 'Angular';
var framework = 'React';
console.log(framework);
```

The output of the preceding code is `React`, as the last variable declared, named `framework`, was assigned this value. In the previous code, we had two variables with the same name; this is very dangerous and might drive the code to an incorrect output.

Other languages, such as C, Java, and C#, do not allow this behavior. With ES2015, a new keyword was introduced, called `let`. `let` is the new `var` keyword, meaning we can simply substitute the keyword `var` for `let`. In the following code, we have an example:

```
let language = 'JavaScript!'; // {1}
let language = 'Ruby!'; // {2} - throws error
console.log(language);
```

Line {2} will throw an error because a variable named `language` has already been declared in the same scope (line {1}). We will discuss the `let` and scope of the variables in the next topic.



The preceding code can be tested and executed at <https://goo.gl/he0udz>.

ES2015 also introduced the keyword `const`. Its behavior is the same as the keyword `let`; the only difference is that a variable defined as `const` has a read-only value, meaning a constant value.

Consider the following code:

```
const PI = 3.141593;
PI = 3.0; //throws error
console.log(PI);
```

When we try to assign a new value to `PI` or even try to declare it again as `var PI` or `let PI`, the code will throw an error saying that `PI` is read-only.

Let's take a look at another example of `const`. We will declare an object as `const`:

```
const jsFramework = {
  name: 'Angular'
};
```

Let's try changing the name of the `jsFramework` variable:

```
jsFramework.name = 'React';
```

If we try to run this code, it will work. But `const` variables are read-only! So why is it possible to run the preceding code? For non-object types such as `number`, `boolean`, and even `string`, this means we cannot change the variable values. When working with objects, a read-only `const` allows the properties of the object to be reassigned or updated, but the reference to the variable itself (the memory reference address) cannot be changed, meaning it cannot be reassigned.

If we try to assign a new reference to the `jsFramework` variable as follows, the compiler will complain and throw an error ("`jsFramework`" is read-only):

```
// error, cannot reassign object reference
jsFramework = {
  name: 'Vue'
};
```

The preceding code can be executed at <https://goo.gl/YUQj3r>.



Variables scope with let and const

To understand how variables declared with the `let` or `const` keywords work, let's use the following example (you can run the example using the following URL: <https://goo.gl/NbsVvg>):

```
let movie = 'Lord of the Rings'; // {1}
//var movie = 'Batman v Superman'; // error movie already declared

function starWarsFan() {
    const movie = 'Star Wars'; // {2}
    return movie;
}

function marvelFan() {
    movie = 'The Avengers'; // {3}
    return movie;
}

function blizzardFan() {
    const isFan = true;
    let phrase = 'Warcraft'; // {4}
    console.log('Before if: ' + phrase);
    if (isFan) {
        let phrase = 'initial text'; // {5}
        phrase = 'For the Horde!'; // {6}
        console.log('Inside if: ' + phrase);
    }
    phrase = 'For the Alliance!'; // {7}
    console.log('After if: ' + phrase);
}

console.log(movie); // {8}
console.log(starWarsFan()); // {9}
console.log(marvelFan()); // {10}
console.log(movie); // {11}
blizzardFan(); // {12}
```

This will be the output from the previous code:

```
Lord of the Rings
Star Wars
The Avengers
The Avengers
Before if: Warcraft
Inside if: For the Horde!
After if: For the Alliance!
```

The following is an explanation of why we got this output:

- In line {1}, we declared a `movie` variable with the value `Lord of the Rings`, and we output its value in line {8}. This variable has a global scope, as you learned in the *Variable scope* section of this chapter.
- In line {9}, we executed the `starWarsFan` function. Inside this function, we also declared a variable named `movie` in line {2}. The output from this function is `Star Wars` because the variable from line {2} has a local scope, meaning it is only valid inside this function.
- In line {10}, we executed the `marvelFan` function. Inside this function, we changed the value of the `movie` variable (line {3}). This variable made a reference to the global variable declared in line {1}. Therefore, we got the output `The Avengers` in line {10} and in line {11}, where we output the global variable.
- Finally, we executed the `blizzardFan` function in line {12}. Inside this function, we declared a variable named `phrase` (line {4}) with the scope of the function. Then, in line {5}, again, we will declare a variable named `phrase`, but this time, this variable will only have a scope inside the `if` statement.
- In line {6}, we changed the value of `phrase`. As we are still inside the `if` statement, only the variable declared in line {5} would have its value changed.
- Then, in line {7}, we again changed the value of `phrase`, but as we are not inside the block of the `if` statement, the value of the variable declared in line {4} is changed.

This scope behavior is the same as in other programming languages, such as Java or C. However, this was only introduced in JavaScript through ES2015 (ES6).



Note that in the code presented in the section, we are mixing `let` and `const`. Which one should we use? Some developers (and also some lint tools) prefer using `const` if the reference of the variable does not change. However, this is a matter of personal preference; there is no wrong choice!

Template literals

Template literals are a nice functionality because we can create strings without the need to concatenate the values.

For example, consider the following examples written with ES5:

```
const book = {
    name: 'Learning JavaScript DataStructures and Algorithms'
};
console.log('You are reading ' + book.name + '.,\n and this is a new line\n and so is this.');
```

We can improve the syntax of the previous `console.log` output with the following code:

```
console.log(`You are reading ${book.name}.,
    and this is a new line
    and so is this.`);
```

Template literals are enclosed by backticks (`). To interpolate a variable value, we will simply set the variable value inside a dollar sign and curly braces (\${ }), as we did with `book.name`.

Template literals can also be used for multiline strings. There is no need to use \n anymore. Simply hit *Enter* on the keyboard to take the string to a new line, as was done with `and this is a new line` in the previous example.

This functionality will be very useful in our examples to simplify the output!

The preceding examples can be executed at <https://goo.gl/4N36CS>.



Arrow functions

Arrow functions are a great way of simplifying the syntax of functions in ES2015. Consider the following example:

```
var circleAreaES5 = function circleArea(r) {
    var PI = 3.14;
    var area = PI * r * r;
    return area;
};
console.log(circleAreaES5(2));
```

We can simplify the syntax of the preceding code to the following code:

```
const circleArea = r => { // {1}
  const PI = 3.14;
  const area = PI * r * r;
  return area;
};
console.log(circleArea(2));
```

The main difference is in line {1} of the example, on which we can omit the keyword `function` using `=>`.

If the function has a single statement, we can use a simpler version, by omitting the keyword `return` and the curly brackets as demonstrated in the following code snippet:

```
const circleArea2 = r => 3.14 * r * r;
console.log(circleArea2(2));
```

If the function does not receive any argument, we use empty parentheses, which we would usually use in ES5:

```
const hello = () => console.log('hello!');
hello();
```

The preceding examples can be executed at <https://goo.gl/nM414v>.



Default parameter values for functions

With ES2015, it is also possible to define default parameter values for functions. The following is an example:

```
function sum(x = 1, y = 2, z = 3) {
  return x + y + z;
}
console.log(sum(4, 2)); // outputs 9
```

As we are not passing `z` as a parameter, it will have a value of 3 by default. So, $4 + 2 + 3 == 9$.

Before ES2015, we would have to write the preceding function as in the following code:

```
function sum(x, y, z) {  
    if (x === undefined) x = 1;  
    if (y === undefined) y = 2;  
    if (z === undefined) z = 3;  
    return x + y + z;  
}
```

Or, we could also write the code as follows:

```
function sum() {  
    var x = arguments.length > 0 && arguments[0] !== undefined ? arguments[0]  
    : 1;  
    var y = arguments.length > 1 && arguments[1] !== undefined ? arguments[1]  
    : 2;  
    var z = arguments.length > 2 && arguments[2] !== undefined ? arguments[2]  
    : 3;  
    return x + y + z;  
}
```



JavaScript functions also have a built-in object called the `arguments` object. The `arguments` object is an array of the arguments used when the function is called. We can dynamically access and use the arguments even if we do not know the argument name.

With ES2015, we can save a few lines of code using the default parameter values functionality.



The preceding example can be executed at <https://goo.gl/AP5EYb>.

Declaring the spread and rest operators

In ES5, we can turn arrays into parameters using the `apply()` function. ES2015 has the spread operator (`...`) for this purpose. For example, consider the `sum` function we declared in the previous topic. We can execute the following code to pass the `x`, `y`, and `z` parameters:

```
let params = [3, 4, 5];  
console.log(sum(...params));
```

The preceding code is the same as the code written in ES5, as follows:

```
console.log(sum.apply(undefined, params));
```

The spread operator (...) can also be used as a rest parameter in functions to replace arguments. Consider the following example:

```
function restParamaterFunction(x, y, ...a) {
    return (x + y) * a.length;
}
console.log(restParamaterFunction(1, 2, 'hello', true, 7));
```

The preceding code is the same as the following (also outputs 9 in the console):

```
function restParamaterFunction(x, y) {
    var a = Array.prototype.slice.call(arguments, 2);
    return (x + y) * a.length;
}
console.log(restParamaterFunction(1, 2, 'hello', true, 7));
```



The spread operator example can be executed at <https://goo.gl/8equk5>, and the rest parameter example can be executed at <https://goo.gl/LaJZqU>.

Enhanced object properties

ES6 introduces a concept called **array destructuring**, which is a way of initializing variables at once. For example, consider the following:

```
let [x, y] = ['a', 'b'];
```

Executing the preceding code is the same as doing the following:

```
let x = 'a';
let y = 'b';
```

Array destructuring can also be performed to swap values at once without the need to create temp variables, as follows:

```
[x, y] = [y, x];
```

The preceding code is the same as the following one:

```
var temp = x;
x = y;
y = temp;
```

This will be very useful when you learn sorting algorithms as these swap values are very common.

There is also another functionality, called **property shorthand**, which is another way of destructuring objects. For example, consider the following example:

```
let [x, y] = ['a', 'b'];
let obj = { x, y };
console.log(obj); // { x: "a", y: "b" }
```

The preceding code is the same as doing the following:

```
var x = 'a';
var y = 'b';
var obj2 = { x: x, y: y };
console.log(obj2); // { x: "a", y: "b" }
```

The last functionality that we will discuss in this topic is called the **shorthand method names**. This allows developers to declare functions inside objects as if they were properties. The following is an example:

```
const hello = {
  name: 'abcdef',
  printHello() {
    console.log('Hello');
  }
};
console.log(hello.printHello());
```

The preceding code can also be written as follows:

```
var hello = {
  name: 'abcdef',
  printHello: function printHello() {
    console.log('Hello');
  }
};
console.log(hello.printHello());
```

The three examples presented can be executed at:

- **Array destructuring:** <https://goo.gl/VsLecp>
- **Variable swap:** <https://goo.gl/EyFAII>
- **Property shorthand:** <https://goo.gl/DKU2PN>

Object-oriented programming with classes

ES2015 also introduced a cleaner way of declaring classes. You learned that we can declare a class named `Book` in the object-oriented programming section this way:

```
function Book(title, pages, isbn) { // {1}
    this.title = title;
    this.pages = pages;
    this.isbn = isbn;
}
Book.prototype.printTitle = function() {
    console.log(this.title);
};
```

With ES2015, we can simplify the syntax and use the following code:

```
class Book { // {2}
    constructor(title, pages, isbn) {
        this.title = title;
        this.pages = pages;
        this.isbn = isbn;
    }
    printIsbn() {
        console.log(this.isbn);
    }
}
```

We can simply use the keyword `class` and declare a class with a `constructor` function and other functions as well—for example, the `printIsbn` function. ES2015 classes are syntactical sugar over the prototype-based syntax. The code for the `Book` class declared in line {1} has the same behavior and output as the code declared in line {2}:

```
let book = new Book('title', 'pag', 'isbn');
console.log(book.title); // outputs the book title
book.title = 'new title'; // update the value of the book title
console.log(book.title); // outputs the book title
```

The preceding example can be executed at <https://goo.gl/UhK1n4>.



Inheritance

With ES2015, there is also a simplified syntax to use inheritance between classes. Let's look at an example:

```
class ITBook extends Book { // {1}
    constructor(title, pages, isbn, technology) {
        super(title, pages, isbn); // {2}
        this.technology = technology;
    }

    printTechnology() {
        console.log(this.technology);
    }
}
let jsBook = new ITBook('Learning JS Algorithms', '200', '1234567890',
'JavaScript');
console.log(jsBook.title);
console.log(jsBook.printTechnology());
```

We can extend another class and inherit its behavior using the keyword `extends` (line {1}). Inside the constructor, we can also refer to the `constructor` superclass using the keyword `super` (line {2}).

Although the syntax of this new way of declaring classes in JavaScript is very similar to other programming languages such as Java and C/C++, it is good to remember that JavaScript object-oriented programming is done through a prototype.

The preceding example can be executed at <https://goo.gl/hgQvo9>.



Working with getters and setters

It is also possible to create getter and setter functions for the class attributes with ES2015. Although class attributes are not private as in other object-oriented languages (the encapsulation concept), it is good to follow a naming pattern.

The following is an example of a class declaring a `get` and `set` function along with its use:

```
class Person {  
    constructor(name) {  
        this._name = name; // {1}  
    }  
    get name() { // {2}  
        return this._name;  
    }  
    set name(value) { // {3}  
        this._name = value;  
    }  
}  
  
let lotrChar = new Person('Frodo');  
console.log(lotrChar.name); // {4}  
lotrChar.name = 'Gandalf'; // {5}  
console.log(lotrChar.name);  
lotrChar._name = 'Sam'; // {6}  
console.log(lotrChar.name);
```

To declare a `get` and `set` function, we simply need to use the keyword `get` or `set` in front of the function name (lines `{2}` and `{3}`), which is the name we want to expose and to be used. We can declare the class attributes with the same name, or we can use an underscore in front of the attribute name (line `{1}`) to make it feel like the attribute is private.

Then, to use the `get` or `set` functions, we can simply refer to their names as if it was a simple attribute (lines `{4}` and `{5}`).

The `_name` attribute is not private, and we can still access it (line `{6}`). However, we will talk about this later on in this book.

This example can be executed at <https://goo.gl/SMRYsv>.



Exponentiation operator

The exponentiation operator may come in handy when working with math. Let's use the formula to calculate the area of a circle as an example:

```
const area = 3.14 * r * r;
```

We could also use the `Math.pow` function to write the same code:

```
const area = 3.14 * Math.pow(r, 2);
```

ES2016 introduced `**`, where `**` is designed to be the new exponentiation operator. We can calculate the area of a circle using the exponentiation operator as follows:

```
const area = 3.14 * (r ** 2);
```

This example can be executed at <https://goo.gl/z6dCFB>.



ES2015+ also has some other functionalities; among them, we can list iterators, typed arrays, `Set`, `Map`, `WeakSet`, `WeakMap`, tail calls, `for..of`, `Symbol`, `Array.prototype.includes`, trailing commas, string padding, object static methods, and so on. We will cover some of these other functionalities in other chapters of this book.



You can check the list of all available JavaScript and ECMAScript functionalities at <https://developer.mozilla.org/en-US/docs/Web/JavaScript>.

Modules

Node.js developers are already familiar with working with modules by using the `require` statement (**CommonJS** modules). There is also another popular JavaScript standard for modules which is the **Asynchronous Module Definition (AMD)**. **RequireJS** is the most popular AMD implementation. ES2015 introduced an official module feature in the JavaScript specification. Let's create and use some modules.

The first module we will create contains two functions to calculate the area of geometric figures. In a file (`17-CalcArea.js`), add the following code:

```
const circleArea = r => 3.14 * (r ** 2);

const squareArea = s => s * s;

export { circleArea, squareArea }; // {1}
```

This means we are exposing both functions so other files can use them ({1}). Only exported members are visible by other modules or files.

In our main file for this example (`17-ES2015-ES6-Modules.js`), we will use the functions declared in the `17-CalcArea.js` file. The following snippet is the code that consumes the two functions:

```
import { circleArea, squareArea } from './17-CalcArea'; // {2}

console.log(circleArea(2));
console.log(squareArea(2));
```

First, we need to import the functions we want to use in this file ({2}), and after importing them, we can evoke them.

If we wanted to use the `circleArea` function, we could import only this function as well:

```
import { circleArea } from './17-CalcArea';
```

Basically, modules are JavaScript code declared in separate files. We can import the functions, variables, and classes from other files directly in the JavaScript code (without the need to import several files in the HTML first—and in the correct order—as we used to do a few years ago before JavaScript was modern and popular). Modules allow us to better organize our code in case we are creating a library or working on a big project.

There is also the option to use the exported member with a different name when we do the import, as follows:

```
import { circleArea as circle } from './17-CalcArea';
```

Or, we can rename the name of the exported functions while exporting them:

```
export { circleArea as circle, squareArea as square };
```

In this case, the exported members need to be imported with the exposed name, not the name used internally, as follows:

```
import { circle, square } from './17-CalcArea';
```

There are also a few different ways we can import the functions in a different module:

```
import * as area from './17-CalcArea';

console.log(area.circle(2));
console.log(area.square(2));
```

In this case, we can import the entire module as a single variable and evoke the exported members as if they were attributes or methods of a class.

It is also possible to add the `export` keyword in front of each function or variable we want to expose. We do not need to have an `export` declaration at the end of the file:

```
export const circleArea = r => 3.14 * (r ** 2);
export const squareArea = s => s * s;
```

Suppose we only have a single member in the module and we want to export it. We can use the `export default` keyword as follows:

```
export default class Book {
    constructor(title) {
        this.title = title;
    }
    printTitle() {
        console.log(this.title);
    }
}
```

To import the preceding class in a different module, we can use the following code:

```
import Book from './17-Book';

const myBook = new Book('some title');
myBook.printTitle();
```

Note that in this case, we do not need to use the curly brackets (`{ }`) around the name of the class. We only use curly brackets in case the module has more than one member exported.

We will use modules when we create our data structures and algorithms library later on in this book.



For more information about ES2015 modules, please read at http://exploringjs.com/es6/ch_modules.html. You can also check out the complete source code for this example by downloading the source code bundle of this book.

Running ES2015 modules in the browser and with Node.js

Let's try to run the `17-ES2015-ES6-Modules.js` file with Node.js by changing the directory and then executing the node command as follows:

```
cd path-source-bundle/examples/chapter01  
node 17-ES2015-ES6-Modules
```

We will get an error, `SyntaxError: Unexpected token import`. This is because at the time of writing this book, Node.js does not support ES2015 native modules. Node.js uses **CommonJS** module require syntax, and this means we need to transpile our ES2015 so Node can understand it. There are different tools we can use for this task. To keep things simple, we will use Babel CLI.



The complete setup and detailed use of Babel can be found at <https://babeljs.io/docs/setup> and <https://babeljs.io/docs/usage/cli/>.

The best approach would be to create a local project and configure it to use Babel. Unfortunately, all of these details are not in the scope of this book (this is a subject for a Babel book). For our example, and to keep things simple, we will use Babel CLI globally by installing it using `npm`:

```
npm install -g babel-cli
```

If you use Linux or Mac OS, you might want to use `sudo` in the front of the command for admin access (`sudo npm install -g babel-cli`).

From inside the `chapter01` directory, we will compile the three JavaScript files with modules we created previously to CommonJS transpile code with Babel, so we can use the code using Node.js. We will transpile the file to the `chapter01/lib` folder using the following commands:

```
babel 17-CalcArea.js --out-dir lib
babel 17-Book.js --out-dir lib
babel 17-ES2015-ES6-Modules.js --out-dir lib
```

Next, let's create a new JavaScript file named `17-ES2015-ES6-Modules-node.js` so we can use the `area` functions and the `Book` class:

```
const area = require('./lib/17-CalcArea');
const Book = require('./lib/17-Book');

console.log(area.circle(2));
console.log(area.square(2));

const myBook = new Book('some title');
myBook.printTitle();
```

The code is basically the same, but the difference is that since Node.js does not support the `import` syntax (for now), we need to use the `require` keyword.

To execute the code, we can use the following command:

```
node 17-ES2015-ES6-Modules-node
```

In the following screenshot, we can see the commands and the output, so we can confirm that the code works with Node.js:

```
loiane:javascript-datastructures-algorithms loiane$ cd examples/chapter01
loiane:chapter01 loiane$ babel 17-CalcArea.js --out-dir lib
17-CalcArea.js -> lib/17-CalcArea.js
loiane:chapter01 loiane$ babel 17-Book.js --out-dir lib
17-Book.js -> lib/17-Book.js
loiane:chapter01 loiane$ babel 17-ES2015-ES6-Modules.js --out-dir lib
17-ES2015-ES6-Modules.js -> lib/17-ES2015-ES6-Modules.js
loiane:chapter01 loiane$ node 17-ES2015-ES6-Modules-node
12.56
4
some title
loiane:chapter01 loiane$
```

Using native ES2015 imports in Node.js

It would be nice if we could use the ES2015 imports in Node.js so that we don't need to transpile our code. Starting with Node 8.5, we can use ES2015 imports in Node.js as an experimental feature.

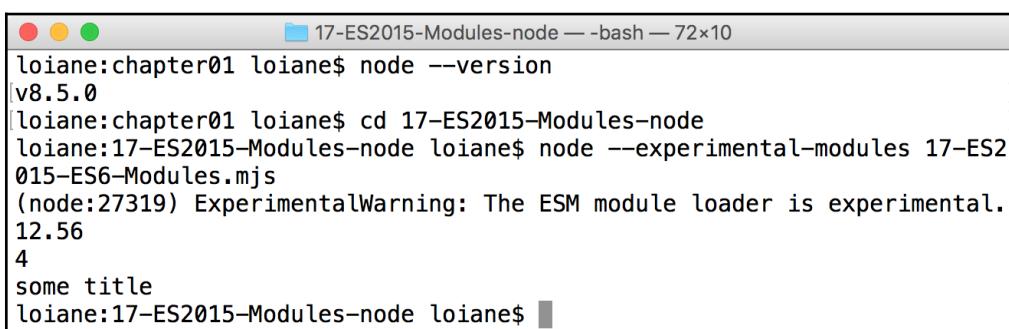
For this example, we will create a new folder inside chapter01 called 17-ES2015-Modules-node. We will copy the files 17-CalcArea.js, 17-Book.js, and 17-ES2015-ES6-Modules.js to this folder and we will change the extension from js to mjs (the .mjs extension is a requirement so that this can work). In the 17-ES2015-ES6-Modules.mjs file, we will update the imports, adding the .mjs extension to it as follows:

```
import * as area from './17-CalcArea.mjs';
import Book from './17-Book.mjs';
```

To execute the code, we will run the node command, passing the --experimental-modules to it as in the following code:

```
cd 17-ES2015-Modules-node
node --experimental-modules 17-ES2015-ES6-Modules.mjs
```

In the following screenshot, we can see the commands and the output:



The screenshot shows a terminal window titled "17-ES2015-Modules-node — bash — 72x10". The user runs "node --version" which outputs "v8.5.0". Then, they change directory to "17-ES2015-Modules-node" and run "node --experimental-modules 17-ES2015-ES6-Modules.mjs". A warning message appears: "(node:27319) ExperimentalWarning: The ESM module loader is experimental." followed by "12.56". The user then types "4" and "some title". The command ends with "loiane\$".

At the time of writing this book, the target for Node.js to support ES2015 import feature is Node 10 LTS.



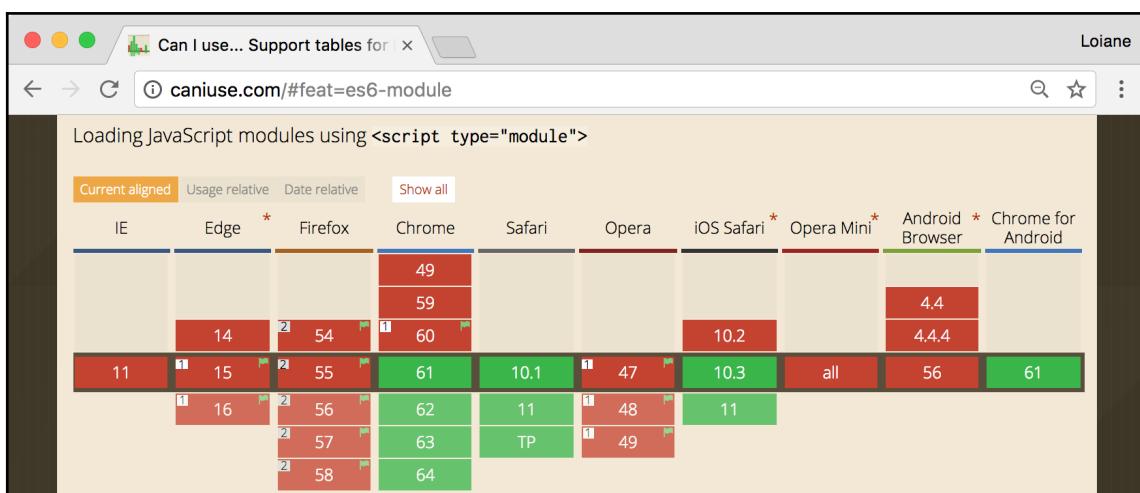
More examples and information about ES2015 import native support in Node.js can be found at <https://github.com/nodejs/node-eps/blob/master/002-es-modules.md>.

Running ES2015 modules in the browser

There are different approaches to run the code with ES2015 in the browser. The first one is to ship the traditional bundle (a JavaScript file with our code transpiled to ES5). We can create a bundle using popular tools such as **Browserify** or **Webpack**. In this case, we create the distribution file (bundle), and in our HTML file, we import it as any other JavaScript code:

```
<script src="./lib/17-ES2015-ES6-Modules-bundle.js"></script>
```

The ES2015 modules support finally landed in browsers at the beginning of 2017. At the time of writing this book, it is still experimental and not supported by all modern browsers. The current support for this feature (and how to enable it in an experimental mode) can be verified at <http://caniuse.com/#feat=es6-module>, as shown in the following screenshot:



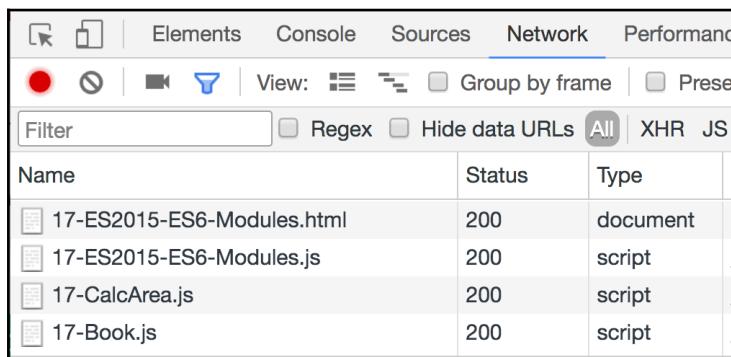
To use the `import` keyword in the browser, first, we need to update our code by adding the `.js` extension in the `import` as follows:

```
import * as area from './17-CalcArea.js';
import Book from './17-Book.js';
```

Secondly, to import the modules we created, we simply need to add `type="module"` inside the `script` tag:

```
<script type="module" src="17-ES2015-ES6-Modules.js"></script>
```

If we execute the code and open the **Developer Tools | Network** tab, we will be able to see that all the files we created were loaded:



Name	Status	Type
17-ES2015-ES6-Modules.html	200	document
17-ES2015-ES6-Modules.js	200	script
17-CalcArea.js	200	script
17-Book.js	200	script

To keep backward compatibility with browsers that do not support this functionality, we can use `nomodule`:

```
<script nomodule src=". /lib/17-ES2015-ES6-Modules-bundle.js"></script>
```

Until this feature is officially supported by most modern browsers, we still need to use a bundler tool to transpile ES2015+.



To learn more about ES2015 modules in browser, please read
<https://goo.gl/cf1cGW> and <https://goo.gl/wBUJUo>.

ES2015+ backward compatibility

Do I need to update my current JavaScript code to ES2015? The answer is only if you would like to! ES2015+ are supersets of the JavaScript language. Everything that was standardized as ES5 will continue working as it does today. However, you can start using ES2015+ to leverage the new syntax and make your code simpler and easier to read.

In the following chapters of this book, we will use ES2015+ as much as we can. Suppose we want to create a data structures and algorithms library from this book, and by default, we want to support developers that want to use our library in the browser (ES5) and in the Node.js environment. For now, the option we have is transpiling our code to **Universal Module Definition (UMD)**. For more information about UMD, please go to <https://github.com/umdjs/umd>. We will learn more about how to transpile ES2015 code with Babel to UMD in Chapter 4, *Stacks*.

Along with the ES2015+ syntax, for the examples that use modules, the source code bundle also provides a transpiled version of the source code so that you can run the code in any browser.

Introducing TypeScript

TypeScript is an open source, **gradually typed** superset of JavaScript created and maintained by Microsoft. It was created to allow developers to supercharge the JavaScript language and to also make it easier to scale applications. Among its main capabilities is providing typing to JavaScript variables. Types in JavaScript enable static checking, thus making it easier to refactor the code and find bugs. And at the end, TypeScript compiles to simple JavaScript code!

Regarding the scope of this book, with TypeScript, we can use some object-oriented concepts that are not available in JavaScript such as interfaces and private properties (this can be useful when working with data structures and sorting algorithms). And of course, we can also leverage the typing functionality, which is very important for some data structures.

All of these functionalities are available at **compile time**. Once we write our code, we compile it to plain JavaScript (ES5, ES2015+, and CommonJS, among other options).

To get started with TypeScript, we need to install it using npm:

```
npm install -g typescript
```

Next, we need to create a file with the .ts extension, such as `hello-world.ts`:

```
let myName = 'Packt';
myName = 10;
```

The preceding code is a simple ES2015 code. Now, let's compile it using the `tsc` command:

```
tsc hello-world
```

On the Terminal, we will get the following warning:

```
hello-world.ts(2,1): error TS2322: Type '10' is not assignable to type  
'string'.
```

But if we verify the folder where we created the file, we will see it created a `hello-world.js` file with the following content:

```
var myName = 'Packt';  
myName = 10;
```

The previously generated code is ES5 code. Even with the error in the Terminal (which is in fact a warning, not an error), the TypeScript compiler generated the ES5 code as it should. This reinforces the fact that although TypeScript does all the type and error checking during compile time, it does not prevent the compiler from generating the JavaScript code. This means that developers can leverage all these validations while we write the code and get a JavaScript code with less chances of errors or bugs.

Type inference

While working with TypeScript, it is very common to find code as follows:

```
let age: number = 20;  
let existsFlag: boolean = true;  
let language: string = 'JavaScript';
```

TypeScript allows us to assign a type to a variable. But the preceding code is verbose. TypeScript has type inference, meaning TypeScript will verify and apply a type to the variable automatically based on the value that was assigned to it. Let's rewrite the preceding code with a cleaner syntax:

```
let age = 20; // number  
let existsFlag = true; // boolean  
let language = 'JavaScript'; // string
```

With the preceding code, TypeScript still knows that `age` is a `number`, `existsFlag` is a `boolean`, and `language` is a `string`, so we don't need to explicitly assign a type to these variables.

So, when do we type a variable? If we declare the variable and do not initialize it with a value, then it is recommended to assign a type, as demonstrated by the following code:

```
let favoriteLanguage: string;
let langs = ['JavaScript', 'Ruby', 'Python'];
favoriteLanguage = langs[0];
```

If we do not type a variable, then it is automatically typed as `any`, meaning it can receive any value, as it is in JavaScript.

Interfaces

In TypeScript, there are two concepts for interfaces. The first one is related to assigning a type to a variable. Consider the following code:

```
interface Person {
    name: string;
    age: number;
}

function printName(person: Person) {
    console.log(person.name);
}
```

The first concept for the TypeScript interface is that an interface is a thing. It is a description of the attributes and methods an object must have.

This allows editors such as VSCode to have autocomplete with IntelliSense, as shown in the following screenshot:



Now, let's try using the `printName` function:

```
const john = { name: 'John', age: 21 };
const mary = { name: 'Mary', age: 21, phone: '123-45678' };
printName(john);
printName(mary);
```

The preceding code does not have any compilation errors. The variable `john` has a name and age as expected by the `printName` function. The variable `mary` has a name and age, but also has phone information.

So, why does this code work? TypeScript has a concept called **Duck Typing**. If it looks like a duck, swims like a duck, and quacks like a duck, then it must be a duck! In the example, the variable `mary` behaves like the `Person` interface, so it must be a `Person`. This is a powerful feature of TypeScript.

And after running the `tsc` command again, we will get the following output in the `hello-world.js` file:

```
function printName(person) {
    console.log(person.name);
}
var john = { name: 'John', age: 21 };
var mary = { name: 'Mary', age: 21, phone: '123-45678' };
```

The preceding code is just plain JavaScript. The code completion and type and error checking are available in compile time only.

The second concept for the TypeScript interface is related to object-oriented programming. This is the same concept as in other object-oriented languages such as Java, C#, Ruby, and so on. An interface is a contract. In this contract, we can define what behavior the classes or interfaces that will implement this contract should have. Consider the ECMAScript standard. ECMAScript is an interface for the JavaScript language. It tells the JavaScript language what functionalities it should have, but each browser might have a different implementation of it.

Consider the following code:

```
interface Comparable {
    compareTo(b): number;
}

class MyObject implements Comparable {
    age: number;
```

```
compareTo(b): number {
    if (this.age === b.age) {
        return 0;
    }
    return this.age > b.age ? 1 : -1;
}
```

The `Comparable` interface tells the `MyObject` class that it should implement a method called `compareTo` that receives an argument. Inside this method, we can code the required logic. In this case, we are comparing two numbers, but we could use a different logic for comparing two strings or even a more complex object with different attributes. This interface behavior does not exist in JavaScript, but it is very helpful when working with sorting algorithms, as an example.

Generics

Another powerful feature of TypeScript that is useful to data structures and algorithms is the generic concept. Let's modify the `Comparable` interface so that we can define the type of the object the `compareTo` method should receive as an argument:

```
interface Comparable<T> {
    compareTo(b: T): number;
}
```

By passing the `T` type dynamically to the `Comparable` interface, between the diamond operator `<>`, we can specify the argument type of the `compareTo` function:

```
class MyObject implements Comparable<MyObject> {
    age: number;

    compareTo(b: MyObject): number {
        if (this.age === b.age) {
            return 0;
        }
        return this.age > b.age ? 1 : -1;
    }
}
```

This is useful so that we can make sure we are comparing objects of the same type, and by using this functionality, we also get code completion from the editor.

Other TypeScript functionalities

This was a very quick introduction to TypeScript. The TypeScript documentation is a great place for learning all the other functionalities and to dive into the details of the topics we quickly covered in this chapter; it can be found at <https://www.typescriptlang.org/docs/home.html>.

TypeScript also has an online playground (similar to Babel) that we can use to play with some code examples, at <https://www.typescriptlang.org/play/index.html>.



The source code bundle of this book also contains a TypeScript version of the JavaScript data structures and algorithms library we will develop throughout this book as an extra resource!

TypeScript compile-time checking in JavaScript files

Some developers still prefer using plain JavaScript to develop their code instead of TypeScript. But it would be nice if we could use some of the type and error checking features in JavaScript as well!

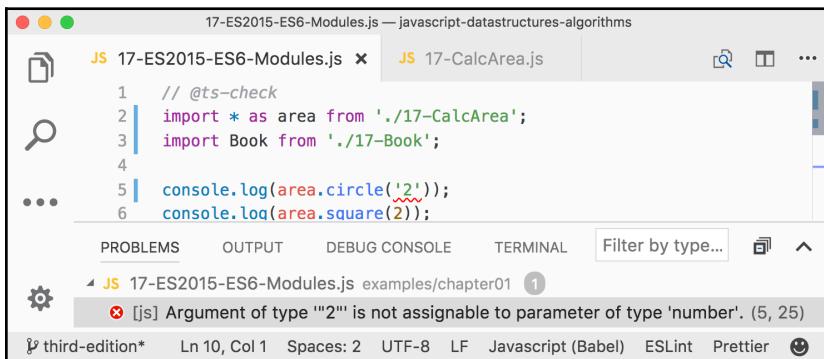
The good news is that TypeScript has a special functionality that allows us to have this compile-time error and type checking! To use it, we need to have TypeScript installed globally on our computer. In the first line of the JavaScript files, we want to use type and error checking, so we simply need to add `// @ts-check`, as demonstrated in the following screenshot:

A screenshot of a code editor window titled "17-CalcArea.js — javascript-datastructures-algorithms". The file content is as follows:

```
1 // @ts-check
2
3 /**
4 * Calculates the area of a circle
5 * @param {number} r (radius of the circle)
6 */
7 export const circleArea = r => 3.14 * (r ** 2);
```

The code editor interface includes tabs for "ES2015-ES6-Modules.js" and "JS 17-CalcArea.js x". At the bottom, there are status indicators for "third-edition*", ESLint, Prettier, and a smiley face icon.

The type checking is enabled when we add JSDoc (JavaScript documentation) to our code. Then, if we try to pass a string to our circle (or `circleArea`) method, we will get a compilation error:



A screenshot of a code editor window titled "17-ES2015-ES6-Modules.js — javascript-datastructures-algorithms". It shows two tabs: "17-ES2015-ES6-Modules.js" and "17-CalcArea.js". The code in "17-ES2015-ES6-Modules.js" includes imports from "17-CalcArea" and "17-Book", and calls to "area.circle('2')". A tooltip indicates a type error: "[ts] Argument of type '\"2\"' is not assignable to parameter of type 'number'. (5, 25)". The status bar at the bottom shows "third-edition*" and various file details.

Summary

In this chapter, we did an overview of some of the ECMAScript 2015+ functionalities that will help us simplify the syntax of our upcoming examples. We also introduced TypeScript to help us leverage static typing and error checking.

In the next chapter, we will look at our first data structure, which is the array, the most basic data structure that many languages support natively, including JavaScript.

3 Arrays

An **array** is the simplest memory data structure. For this reason, all programming languages have a built-in array datatype. JavaScript also supports arrays natively, even though its first version was released without array support. In this chapter, we will dive into the array data structure and its capabilities.

An array stores values that are all of the same datatype sequentially. Although JavaScript allows us to create arrays with values from different datatypes, we will follow best practices and assume that we cannot do this (most languages do not have this capability).

Why should we use arrays?

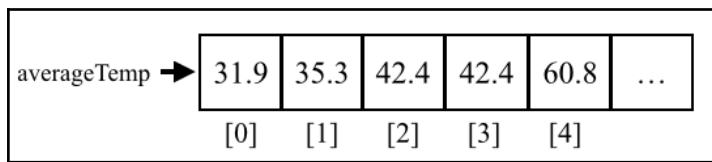
Let's consider that we need to store the average temperature of each month of the year for the city that we live in. We could use something similar to the following to store this information:

```
const averageTempJan = 31.9;
const averageTempFeb = 35.3;
const averageTempMar = 42.4;
const averageTempApr = 52;
const averageTempMay = 60.8;
```

However, this is not the best approach. If we store the temperature for only one year, we can manage 12 variables. However, what if we need to store the average temperature for more than one year? Fortunately, this is why arrays were created, and we can easily represent the same information mentioned earlier as follows:

```
const averageTemp = [];
averageTemp[0] = 31.9;
averageTemp[1] = 35.3;
averageTemp[2] = 42.4;
averageTemp[3] = 52;
averageTemp[4] = 60.8;
```

We can also represent the `averageTemp` array graphically:



Creating and initializing arrays

Declaring, creating, and initializing an array in JavaScript is really simple, as the following shows:

```
let daysOfWeek = new Array(); // {1}
daysOfWeek = new Array(7); // {2}
daysOfWeek = new Array('Sunday', 'Monday', 'Tuesday', 'Wednesday',
'Thursday', 'Friday', 'Saturday'); // {3}
```

We can simply declare and instantiate a new array using the keyword `new` (line {1}). Also, using the keyword `new`, we can create a new array specifying the length of the array (line {2}). A third option would be passing the array elements directly to its constructor (line {3}).

However, using the `new` keyword is not considered best practice. If we want to create an array in JavaScript, we can assign empty brackets (`[]`), as in the following example:

```
let daysOfWeek = [];
```

We can also initialize the array with some elements, as follows:

```
let daysOfWeek = ['Sunday', 'Monday', 'Tuesday', 'Wednesday', 'Thursday',
'Friday', 'Saturday'];
```

If we want to know how many elements are in the array (its size), we can use the `length` property. The following code will give an output of 7:

```
console.log(daysOfWeek.length);
```

Accessing elements and iterating an array

To access a specific position of the array, we can also use brackets, passing the index of the position we would like to access. For example, let's say we want to output all the elements from the `daysOfWeek` array. To do so, we need to loop the array and print the elements, starting from index 0 as follows:

```
for (let i = 0; i < daysOfWeek.length; i++) {  
    console.log(daysOfWeek[i]);  
}
```

Let's take a look at another example. Let's say that we want to find out the first 20 numbers of the Fibonacci sequence. The first two numbers of the Fibonacci sequence are 1 and 2, and each subsequent number is the sum of the previous two numbers:

```
const fibonacci = []; // {1}  
fibonacci[1] = 1; // {2}  
fibonacci[2] = 1; // {3}  
  
for (let i = 3; i < 20; i++) {  
    fibonacci[i] = fibonacci[i - 1] + fibonacci[i - 2]; // // {4}  
}  
  
for (let i = 1; i < fibonacci.length; i++) { // {5}  
    console.log(fibonacci[i]); // {6}  
}
```

The following is the explanation for the preceding code:

1. In line {1}, we declared and created an array.
2. In lines {2} and {3}, we assigned the first two numbers of the Fibonacci sequence to the second and third positions of the array (in JavaScript, the first position of the array is always referenced by 0 (zero), and as there is no zero in the Fibonacci sequence, we will skip it).
3. Then, all we need to do is create the third to the 20th number of the sequence (as we know the first two numbers already). To do so, we can use a loop and assign the sum of the previous two positions of the array to the current position (line {4}, starting from index 3 of the array to the 19th index).
4. Then, to take a look at the output (line {6}), we just need to loop the array from its first position to its length (line {5}).



We can use `console.log` to output each index of the array (lines `{5}` and `{6}`), or we can also use `console.log(fibonacci)` to output the array itself. Most browsers have a nice array representation in `console.log`.

If you would like to generate more than 20 numbers of the Fibonacci sequence, just change the number `20` to whatever number you like.

Adding elements

Adding and removing elements from an array is not that difficult; however, it can be tricky. For the examples we will create in this section, let's consider that we have the following numbers array initialized with numbers from 0 to 9:

```
let numbers = [0, 1, 2, 3, 4, 5, 6, 7, 8, 9];
```

Inserting an element at the end of the array

If we want to add a new element to this array (for example, the number 10), all we have to do is reference the latest free position of the array and assign a value to it:

```
numbers[numbers.length] = 10;
```



In JavaScript, an array is a mutable object. We can easily add new elements to it. The object will grow dynamically as we add new elements to it. In many other languages, such as C and Java, we need to determine the size of the array, and if we need to add more elements to the array, we need to create a completely new array; we cannot simply add new elements to it as we need them.

Using the push method

JavaScript API also has a method called `push` that allows us to add new elements to the end of an array. We can add as many elements as we want as arguments to the `push` method:

```
numbers.push(11);
numbers.push(12, 13);
```

The output of the `numbers` array will be the numbers from 0 to 13.

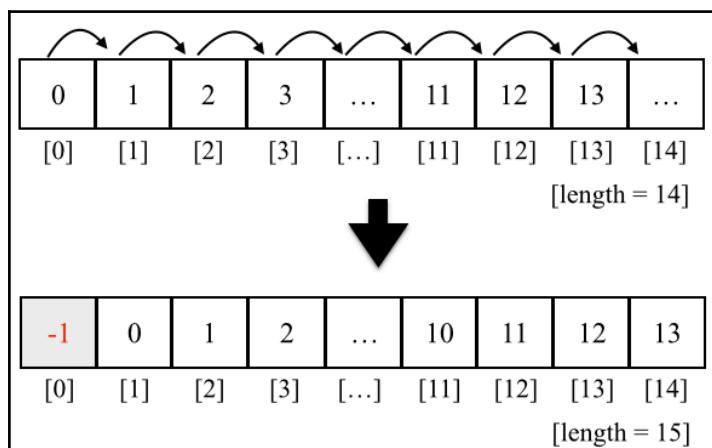
Inserting an element in the first position

Suppose we need to add a new element to the array (number `-1`) and would like to insert it in the first position, not the last one. To do so, first we need to free the first position by shifting all the elements to the right. We can loop all the elements of the array, starting from the last position (value of `length` will be the end of the array) and shifting the previous element (`i-1`) to the new position (`i`) to finally assign the new value we want to the first position (index `0`). We can create a function to represent this logic or even add a new method directly to the `Array` prototype, making the `insertFirstPosition` method available to all array instances. The following code represents the logic described here:

```
Array.prototype.insertFirstPosition = function(value) {
    for (let i = this.length; i >= 0; i--) {
        this[i] = this[i - 1];
    }
    this[0] = value;
};

numbers.insertFirstPosition(-1);
```

We can represent this action with the following diagram:



Using the unshift method

The JavaScript `Array` class also has a method called `unshift`, which inserts the values passed in the method's arguments at the start of the array (the logic behind-the-scenes has the same behavior as the `insertFirstPosition` method):

```
numbers.unshift(-2);  
numbers.unshift(-4, -3);
```

So, using the `unshift` method, we can add the value `-2` and then `-3` and `-4` to the beginning of the `numbers` array. The output of this array will be the numbers from `-4` to `13`.

Removing elements

So far, you have learned how to add elements in the array. Let's take a look at how we can remove a value from an array.

Removing an element from the end of the array

To remove a value from the end of an array, we can use the `pop` method:

```
numbers.pop();
```



The `push` and `pop` methods allow an array to emulate a basic `stack` data structure, which is the subject of the next chapter.

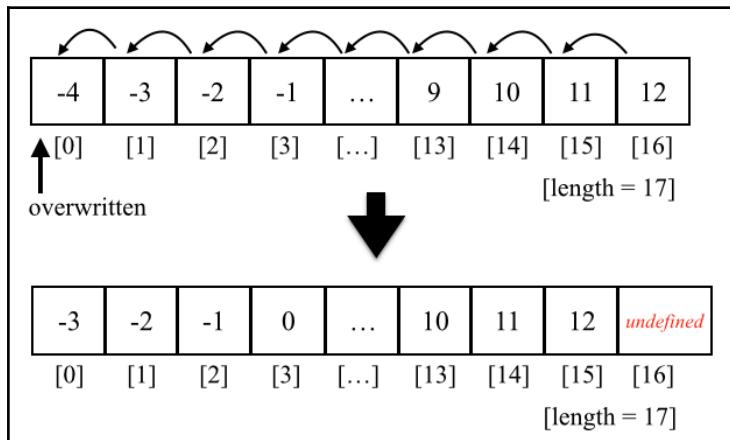
The output of our array will be the numbers from `-4` to `12`. The length of our array is `17`.

Removing an element from the first position

To remove a value from the beginning of the array, we can use the following code:

```
for (let i = 0; i < numbers.length; i++) {  
    numbers[i] = numbers[i + 1];  
}
```

We can represent the previous code using the following diagram:



We shifted all the elements one position to the left. However, the length of the array is still the same (17), meaning we still have an extra element in our array (with an `undefined` value). The last time the code inside the loop was executed, `i+1` was a reference to a position that does not exist. In some languages, such as Java, C/C++, or C#, the code would throw an exception, and we would have to end our loop at `numbers.length - 1`.

We have only overwritten the array's original values, and we did not really remove the value (as the length of the array is still the same and we have this extra `undefined` element).

To remove the value from the array, we can also create a `removeFirstPosition` method with the logic described in this topic. However, to really remove the element from the array, we need to create a new array and copy all values other than `undefined` values from the original array to the new one and assign the new array to our array. To do so, we can also create a `reIndex` method as follows:

```
Array.prototype.reIndex = function(myArray) {
  const newArray = [];
  for(let i = 0; i < myArray.length; i++ ) {
    if (myArray[i] !== undefined) {
      // console.log(myArray[i]);
      newArray.push(myArray[i]);
    }
  }
  return newArray;
}
```

```
// remove first position manually and reIndex
Array.prototype.removeFirstPosition = function() {
    for (let i = 0; i < this.length; i++) {
        this[i] = this[i + 1];
    }
    return this.reIndex(this);
};

numbers = numbers.removeFirstPosition();
```



The preceding code should be used only for educational purposes and should not be used in real projects. To remove the first element from the array, we should always use the `shift` method, which is presented in the next section.

Using the `shift` method

To remove an element from the beginning of the array, we can use the `shift` method, as follows:

```
numbers.shift();
```

If we consider that our array has the value -4 to 12 and a length of 17 after we execute the previous code, the array will contain the values -3 to 12 and have a length of 16.



The `shift` and `unshift` methods allow an array to emulate a basic queue data structure, which is the subject of Chapter 5, *Queues and Deques*.

Adding and removing elements from a specific position

So far, we have learned how to add elements at the end and at the beginning of an array, and we have also learned how to remove elements from the beginning and end of an array. What if we also want to add or remove elements from any position in our array? How can we do this?

We can use the `splice` method to remove an element from an array by simply specifying the position/index that we would like to delete from and how many elements we would like to remove, as follows:

```
numbers.splice(5, 3);
```

This code will remove three elements, starting from index 5 of our array. This means `numbers[5]`, `numbers[6]`, and `numbers[7]` will be removed from the `numbers` array. The content of our array will be `-3, -2, -1, 0, 1, 5, 6, 7, 8, 9, 10, 11, and 12` (as the numbers 2, 3, and 4 have been removed).



As with JavaScript arrays and objects, we can also use the `delete` operator to remove an element from the array, for example, `delete numbers[0]`. However, position 0 of the array will have the value `undefined`, meaning that it would be the same as doing `numbers[0] = undefined` and we would need to re-index the array. For this reason, we should always use the `splice`, `pop`, or `shift` methods to remove elements.

Now, let's say we want to insert numbers 2 to 4 back into the array, starting from position 5. We can again use the `splice` method to do this:

```
numbers.splice(5, 0, 2, 3, 4);
```

The first argument of the method is the index we want to remove elements from or insert elements into. The second argument is the number of elements we want to remove (in this case, we do not want to remove any, so we will pass the value 0 (zero)). And from the third argument onward we have the values we would like to insert into the array (the elements 2, 3, and 4). The output will be values from `-3` to `12` again.

Finally, let's execute the following code:

```
numbers.splice(5, 3, 2, 3, 4);
```

The output will be values from `-3` to `12`. This is because we are removing three elements, starting from the index 5, and we are also adding the elements 2, 3, and 4, starting at index 5.

Two-dimensional and multi-dimensional arrays

At the beginning of this chapter, we used a temperature measurement example. We will now use this example one more time. Let's consider that we need to measure the temperature hourly for a few days. Now that we already know we can use an array to store the temperatures, we can easily write the following code to store the temperatures over 2 days:

```
let averageTempDay1 = [72, 75, 79, 79, 81, 81];
let averageTempDay2 = [81, 79, 75, 75, 73, 72];
```

However, this is not the best approach; we can do better! We can use a **matrix** (a two-dimensional array or an *array of arrays*) to store this information, in which each row will represent the day, and each column will represent an hourly measurement of temperature, as follows:

```
let averageTemp = [];
averageTemp[0] = [72, 75, 79, 79, 81, 81];
averageTemp[1] = [81, 79, 75, 75, 73, 73];
```

JavaScript only supports one-dimensional arrays; it does not support matrices. However, we can implement matrices or any multi-dimensional array using an array of arrays, as in the previous code. The same code can also be written as follows:

```
// day 1
averageTemp[0] = [];
averageTemp[0][0] = 72;
averageTemp[0][1] = 75;
averageTemp[0][2] = 79;
averageTemp[0][3] = 79;
averageTemp[0][4] = 81;
averageTemp[0][5] = 81;
// day 2
averageTemp[1] = [];
averageTemp[1][0] = 81;
averageTemp[1][1] = 79;
averageTemp[1][2] = 75;
averageTemp[1][3] = 75;
averageTemp[1][4] = 73;
averageTemp[1][5] = 73;
```

In the previous code, we specified the value of each day and hour separately. We can also represent this two-dimensional array as the following diagram:

	[0]	[1]	[2]	[3]	[4]	[5]
[0]	72	75	79	79	81	81
[1]	81	79	75	75	73	73

Each row represents a day, and each column represents the temperature for each hour of the day.

Iterating the elements of two-dimensional arrays

If we want to verify the output of the matrix, we can create a generic function to log its output:

```
function printMatrix(myMatrix) {
    for (let i = 0; i < myMatrix.length; i++) {
        for (let j = 0; j < myMatrix[i].length; j++) {
            console.log(myMatrix[i][j]);
        }
    }
}
```

We need to loop through all the rows and columns. To do this, we need to use a nested `for` loop, in which the variable `i` represents rows, and `j` represents the columns. In this case, each `myMatrix[i]` also represents an array, therefore we also need to iterate each position of `myMatrix[i]` in the nested `for` loop.

We can output the contents of the `averageTemp` matrix using the following code:

```
printMatrix(averageTemp);
```



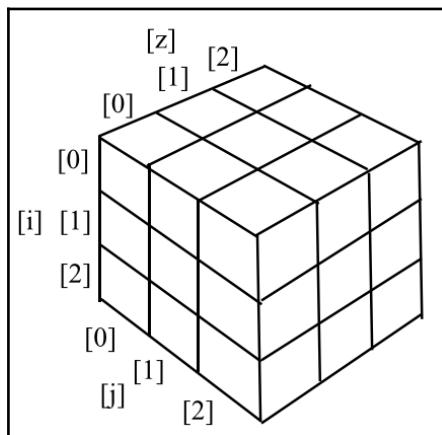
To output a two-dimensional array in the browser console, we can also use the `console.table(averageTemp)` statement. This will provide a more user-friendly output.

Multi-dimensional arrays

We can also work with multi-dimensional arrays in JavaScript. For example, let's create a 3×3 matrix. Each cell contains the sum i (row) + j (column) + z (depth) of the matrix, as follows:

```
const matrix3x3x3 = [];
for (let i = 0; i < 3; i++) {
    matrix3x3x3[i] = []; // we need to initialize each array
    for (let j = 0; j < 3; j++) {
        matrix3x3x3[i][j] = [];
        for (let z = 0; z < 3; z++) {
            matrix3x3x3[i][j][z] = i + j + z;
        }
    }
}
```

It does not matter how many dimensions we have in the data structure; we need to loop each dimension to access the cell. We can represent a $3 \times 3 \times 3$ matrix with a cube diagram, as follows:



To output the content of this matrix, we can use the following code:

```
for (let i = 0; i < matrix3x3x3.length; i++) {
    for (let j = 0; j < matrix3x3x3[i].length; j++) {
        for (let z = 0; z < matrix3x3x3[i][j].length; z++) {
            console.log(matrix3x3x3[i][j][z]);
        }
    }
}
```

If we had a $3 \times 3 \times 3 \times 3$ matrix, we would have four nested `for` statements in our code and so on. You rarely will need a four-dimensional array in your career as a developer. Two-dimensional arrays are most common.

References for JavaScript array methods

Arrays in JavaScript are modified objects, meaning that every array we create has a few methods available to be used. JavaScript arrays are very interesting because they are very powerful and have more capabilities available than primitive arrays in other languages. This means that we do not need to write basic capabilities ourselves, such as adding and removing elements in/from the middle of the data structure.

The following is a list of the core available methods in an array object. We have covered some methods already:

Method	Description
<code>concat</code>	Joins multiple arrays and returns a copy of the joined arrays.
<code>every</code>	Iterates every element of the array, verifying the desired condition (function) until <code>false</code> is returned.
<code>filter</code>	Creates an array with each element that evaluates to <code>true</code> in the function provided.
<code>forEach</code>	Executes a specific function on each element of the array.
<code>join</code>	Joins all the array elements into a string.
<code>indexOf</code>	Searches the array for specific elements and returns its position.
<code>lastIndexOf</code>	Returns the position of the last item in the array that matches the search criterion.
<code>map</code>	Creates a new array from a function that contains the criterion/condition and returns the elements of the array that match the criterion.
<code>reverse</code>	Reverses the array so that the last item becomes the first and vice versa.
<code>slice</code>	Returns a new array from the specified index.
<code>some</code>	Iterates every element of the array, verifying the desired condition (function) until <code>true</code> is returned.
<code>sort</code>	Sorts the array alphabetically or by the supplied function.

<code>toString</code>	Returns the array as a string.
<code>valueOf</code>	Similar to the <code>toString</code> method, returns the array as a string.

We have already covered the `push`, `pop`, `shift`, `unshift`, and `splice` methods. Let's take a look at these new ones. These methods will be very useful in the subsequent chapters of this book, where we will code our own data structure and algorithms. Some of these methods are very useful when we work with **functional programming**, which we will cover in Chapter 14, *Algorithm Designs and Techniques*.

Joining multiple arrays

Consider a scenario where you have different arrays and you need to join all of them into a single array. We could iterate each array and add each element to the final array.

Fortunately, JavaScript already has a method that can do this for us, named the `concat` method, which looks as follows:

```
const zero = 0;
const positiveNumbers = [1, 2, 3];
const negativeNumbers = [-3, -2, -1];
let numbers = negativeNumbers.concat(zero, positiveNumbers);
```

We can pass as many arrays and objects/elements to this array as we desire. The arrays will be concatenated to the specified array in the order that the arguments are passed to the method. In this example, `zero` will be concatenated to `negativeNumbers`, and then `positiveNumbers` will be concatenated to the resulting array. The output of the `numbers` array will be the values `-3, -2, -1, 0, 1, 2, and 3`.

Iterator functions

Sometimes, we need to iterate the elements of an array. We have learned that we can use a loop construct to do this, such as the `for` statement, as we saw in some previous examples.

JavaScript also has some built-in iterator methods that we can use with arrays. For the examples in this section, we will need an array and a function. We will use an array with values from 1 to 15 and a function that returns `true` if the number is a multiple of 2 (even) and `false` otherwise. The code is presented as follows:

```
function isEven(x) {
  // returns true if x is a multiple of 2.
```

```
        console.log(x);
        return x % 2 === 0 ? true : false;
    }
let numbers = [1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15];

return (x % 2 == 0) ? true : false can also be represented as
return (x % 2 == 0).
```



To simplify our code, instead of declaring functions using the **ES5** syntax, we will use the **ES2015 (ES6)** syntax as we learned in [Chapter 2, ECMAScript and TypeScript Overview](#). We can rewrite the `isEven` function using **arrow functions**:

```
const isEven = x => x % 2 === 0;
```

Iterating using the `every` method

The first method we will take a look at is the `every` method. The `every` method iterates each element of the array until the function returns `false`, as follows:

```
numbers.every(isEven);
```

In this case, our first element of the `numbers` array is the number `1`. `1` is not a multiple of `2` (it is an odd number), so the `isEven` function will return `false`, and this will be the only time the function will be executed.

Iterating using the `some` method

Next, we have the `some` method. It has the opposite behavior to the `every` method; however, the `some` method iterates each element of the array until the return of the function is `true`:

```
numbers.some(isEven);
```

In our case, the first even number of our `numbers` array is `2` (the second element). The first element that will be iterated is the number `1`; it will return `false`. Then, the second element that will be iterated is the number `2`, which will return `true`, and the iteration will stop.

Iterating using forEach

If we need the array to be completely iterated no matter what, we can use the `forEach` function. It has the same result as using a `for` loop with the function's code inside it, as follows:

```
numbers.forEach(x => console.log(x % 2 === 0));
```

Using map and filter

JavaScript also has two other iterator methods that return a new array with a result. The first one is the `map` method, which is as follows:

```
const myMap = numbers.map(isEven);
```

The `myMap` array will have the following values: [false, true, false, true, false, true, false, true, false, true, false, true, false]. It stores the result of the `isEven` function that was passed to the `map` method. This way, we can easily know whether a number is even or not. For example, `myMap[0]` returns `false` because 1 is not even, and `myMap[1]` returns `true` because 2 is even.

We also have the `filter` method. It returns a new array with the elements for which the function returned `true`, as follows:

```
const evenNumbers = numbers.filter(isEven);
```

In our case, the `evenNumbers` array will contain the elements that are multiples of 2: [2, 4, 6, 8, 10, 12, 14].

Using the reduce method

Finally, we have the `reduce` method. The `reduce` method receives a function with the following parameters: `previousValue`, `currentValue`, `index`, and `array`. The `index` and `array` are optional parameters, so we do not need to pass them if we do not need to use them. We can use this function to return a value that will be added to an accumulator, which will be returned after the `reduce` method stops being executed. It can be very useful if we want to sum up all the values in an array. Here's an example:

```
numbers.reduce((previous, current) => previous + current);
```

The output will be 120.



These three methods (`map`, `filter`, and `reduce`) are the basis of functional programming in JavaScript, which we will explore in Chapter 14, *Algorithm Designs and Techniques*.

ECMAScript 6 and new array functionalities

As you learned in Chapter 1, *JavaScript – A Quick Overview*, the JavaScript language has new functionalities according to the **ECMAScript 2015** (ES6 or ES2015) and newer specifications (2015+).

The following is a list of the new methods added in ES2015 and ES2016:

Method	Description
<code>@@iterator</code>	Returns an iterator object that contains the key/value pairs of the array that can be synchronously called to retrieve key/value of the array elements.
<code>copyWithin</code>	Copies a sequence of values of the array into the position of a start index.
<code>entries</code>	Returns <code>@@iterator</code> , which contains key/value pairs.
<code>includes</code>	Returns <code>true</code> if an element is found in the array, and <code>false</code> otherwise. This was added in ES2016.
<code>find</code>	Searches for an element in the array given the desired condition (callback function) and returns the element if it is found.
<code>findIndex</code>	Searches for an element in the array given the desired condition (callback function) and returns the element index if it is found.
<code>fill</code>	Fills the array with a static value.
<code>from</code>	Creates a new array from an existing one.
<code>keys</code>	Returns <code>@@iterator</code> , which contains the keys of the array.
<code>of</code>	Creates a new array from the arguments passed to the method.
<code>values</code>	Returns <code>@@iterator</code> , which contains the values of the array.

Along with these methods, the `Array` API also provides a way of iterating the array which uses the `Iterator` object that can be retrieved from the array instance and used in the `for...of` loop.

Iterating using the `for...of` loop

You have learned that we can iterate an array using the `for` loop and the `forEach` method. ES2015 introduced the `for...of` loop, which iterates through the values of an array. We can take a look at an example of how to use the `for...of` loop:

```
for (const n of numbers) {  
    console.log(n % 2 === 0 ? 'even' : 'odd');  
}
```

Using the `@@iterator` object

The `Array` class also has a property named `@@iterator` that was introduced in ES2015. To use this, we need to access the `Symbol.iterator` property of the array as follows:

```
let iterator = numbers[Symbol.iterator]();  
console.log(iterator.next().value); // 1  
console.log(iterator.next().value); // 2  
console.log(iterator.next().value); // 3  
console.log(iterator.next().value); // 4  
console.log(iterator.next().value); // 5
```

Then, we can individually call the `next` method of the iterator to retrieve the next value of the array. For the `numbers` array, we need to call the `iterator.next().value` 15 times because we have 15 values in the array.

We can output all 15 values from the `numbers` array using the following code:

```
iterator = numbers[Symbol.iterator]();  
for (const n of iterator) {  
    console.log(n);  
}
```

When the array is iterated and there are no more values to be iterated, the `iterator.next()` code will return `undefined`.

Array entries, keys, and values

ES2015 also introduced three ways of retrieving iterators from an array. The first one you will learn is the `entries` method.

The `entries` method returns `@@iterator`, which contains key/value pairs. The following is an example of how we can use this method:

```
let aEntries = numbers.entries(); // retrieve iterator of key/value
console.log(aEntries.next().value); // [0, 1] - position 0, value 1
console.log(aEntries.next().value); // [1, 2] - position 1, value 2
console.log(aEntries.next().value); // [2, 3] - position 2, value 3
```

As the `numbers` array only contains numbers, key will be the position of the array, and value will be the value stored in the array index.

We can also use the following code as an alternative to the preceding code:

```
aEntries = numbers.entries();
for (const n of aEntries) {
    console.log(n);
}
```

To be able to retrieve key/value pairs is very useful when we are working with sets, dictionaries, and hash maps. This functionality will be very useful to us in the later chapters of this book.

The `keys` method returns `@@iterator`, which contains the keys of the array. The following is an example of how we can use this method:

```
const aKeys = numbers.keys(); // retrieve iterator of keys
console.log(aKeys.next()); // {value: 0, done: false}
console.log(aKeys.next()); // {value: 1, done: false}
console.log(aKeys.next()); // {value: 2, done: false}
```

For the `numbers` array, the keys will be the indexes of the array. Once there are no values to be iterated, the code `aKeys.next()` will return `undefined` as `value` and `true` as `done`. When `done` has the value `false`, it means that there are still more keys of the array to be iterated.

The `values` method returns `@@iterator`, which contains the values of the array. The following is an example of how we can use this method:

```
const aValues = numbers.values();
console.log(aValues.next()); // {value: 1, done: false}
console.log(aValues.next()); // {value: 2, done: false}
console.log(aValues.next()); // {value: 3, done: false}
```



It is valid to remember that not all functionalities from ES2015 work on browsers yet. Because of this, the best way to test this code is using **Babel**. Examples can be executed at <https://goo.gl/eojEGk>.

Using the `from` method

The `Array.from` method creates a new array from an existing one. For example, if we want to copy the array `numbers` into a new one, we can use the following code:

```
let numbers2 = Array.from(numbers);
```

It is also possible to pass a function so that we can determine which values we want to map. Consider the following code:

```
let evens = Array.from(numbers, x => (x % 2 == 0));
```

The preceding code created a new array named `evens`, and a value `true` if in the original array the number is even, and `false` otherwise.

Using the `Array.of` method

The `Array.of` method creates a new array from the arguments passed to the method. For example, let's consider the following example:

```
let numbers3 = Array.of(1);
```

```
let numbers4 = Array.of(1, 2, 3, 4, 5, 6);
```

The preceding code would be the same as performing the following:

```
let numbers3 = [1];
let numbers4 = [1, 2, 3, 4, 5, 6];
```

We can also use this method to make a copy of an existing array. The following is an example:

```
let numbersCopy = Array.of(...numbers4);
```

The preceding code is the same as using `Array.from(numbers4)`. The difference here is that we are using the spread operator that you learned in Chapter 1, *JavaScript – A Quick Overview*. The spread operator (...) will spread each of the values of the `numbers4` array into arguments.

Using the `fill` method

The `fill` method fills the array with a value. For example, consider the following array:

```
let numbersCopy = Array.of(1,2,3,4,5,6);
```

The `numbersCopy` array has the length 6, meaning we have six positions. Let's use the following code:

```
numbersCopy.fill(0);
```

Here, the `numbersCopy` array will have all its positions with value `[0,0,0,0,0,0]`. We can also pass the start index that we want to fill the array with, as follows:

```
numbersCopy.fill(2, 1);
```

In the preceding example, all the positions of the array will have the value 2, starting from position 1 `[0,2,2,2,2,2]`.

It is also possible to pass the end index that we want to fill the array with:

```
numbersCopy.fill(1, 3, 5);
```

In the preceding example, we will fill the array with value 1 from index 3 to 5 (not inclusive), resulting in the following array: `[0,2,2,1,1,2]`.

The `fill` method is great when we want to create an array and initialize its values, as demonstrated:

```
let ones = Array(6).fill(1);
```

The preceding code will create an array of length 6 and all its values as 1 `[1,1,1,1,1,1]`.

Using the `copyWithin` method

The `copyWithin` method copies a sequence of values of the array into the position of a start index. For example, let's consider the following array:

```
let copyArray = [1, 2, 3, 4, 5, 6];
```

Now, let's say we want to copy the values 4, 5, and 6 to the first three positions of the array, resulting in the `[4, 5, 6, 4, 5, 6]` array. We can use the following code to achieve this result:

```
copyArray.copyWithin(0, 3);
```

Now, consider that we want to copy the values 4 and 5 (the positions 3 and 4) to the positions 1 and 2. We can use the following code to do this:

```
copyArray = [1, 2, 3, 4, 5, 6];
copyArray.copyWithin(1, 3, 5);
```

In this case, we will copy the elements starting in position 3 and ending in position 5 (not inclusive) to the position 1 of the array, resulting in the `[1, 4, 5, 4, 5, 6]` array.

Sorting elements

Throughout this book, you will learn how to write the most-used searching and sorting algorithms. However, JavaScript also has a sorting method and a couple of search methods available. Let's take a look at them.

First, let's take our `numbers` array and put the elements out of order (`1, 2, 3, ... 15` are already sorted). To do this, we can apply the `reverse` method, in which the last item will be the first and vice versa, as follows:

```
numbers.reverse();
```

So now, the output for the `numbers` array will be `[15, 14, 13, 12, 11, 10, 9, 8, 7, 6, 5, 4, 3, 2, 1]`. Then, we can apply the `sort` method as follows:

```
numbers.sort();
```

However, if we output the array, the result will be `[1, 10, 11, 12, 13, 14, 15, 2, 3, 4, 5, 6, 7, 8, 9]`. This is not ordered correctly. This is because the `sort` method sorts the elements lexicographically, and it assumes all the elements are strings.

We can also write our own comparison function. As our array has numeric elements, we can write the following code:

```
numbers.sort((a, b) => a - b);
```

This code will return a negative number if `b` is bigger than `a`, a positive number if `a` is bigger than `b`, and 0 (zero) if they are equal. This means that if a negative value is returned, it implies that `a` is smaller than `b`, which is further used by the `sort` function to arrange the elements.

The previous code can be represented by the following code as well:

```
function compare(a, b) {
  if (a < b) {
    return -1;
  }
  if (a > b) {
    return 1;
  }
  // a must be equal to b
  return 0;
}
numbers.sort(compare);
```

This is because the `sort` function from the JavaScript `Array` class can receive a parameter called `compareFunction`, which is responsible for sorting the array. In our example, we declared a function that will be responsible for comparing the elements of the array, resulting in an array sorted in ascending order.

Custom sorting

We can sort an array with any type of object in it, and we can also create `compareFunction` to compare the elements as required. For example, suppose we have an object, `Person`, with `name` and `age`, and we want to sort the array based on the `age` of the person. We can use the following code:

```
const friends = [
  { name: 'John', age: 30 },
  { name: 'Ana', age: 20 },
  { name: 'Chris', age: 25 }, // trailing comma ES2017
];
function comparePerson(a, b) {
  if (a.age < b.age) {
    return -1;
```

```
        }
        if (a.age > b.age) {
            return 1;
        }
        return 0;
    }
    console.log(friends.sort(comparePerson));
```

In this case, the output from the previous code will be Ana (20), Chris (25), and John (30).

Sorting strings

Suppose we have the following array:

```
let names = ['Ana', 'ana', 'john', 'John'];
console.log(names.sort());
```

What do you think would be the output? The answer is as follows:

```
["Ana", "John", "ana", "john"]
```

Why does ana come after John when a comes first in the alphabet? The answer is because JavaScript compares each character according to its **ASCII** value. For example, A, J, a, and j have the decimal ASCII values of A: 65, J: 74, a: 97, and j: 106.

Therefore, J has a lower value than a, and because of this, it comes first in the alphabet.



For more information about the ASCII table, visit

<http://www.asciitable.com>.

Now, if we pass compareFunction, which contains the code to ignore the case of the letter, we will have the output ["Ana", "ana", "john", "John"], as follows:

```
names = ['Ana', 'ana', 'john', 'John']; // reset array original state
console.log(names.sort((a, b) => {
    if (a.toLowerCase() < b.toLowerCase()) {
        return -1;
    }
    if (a.toLowerCase() > b.toLowerCase()) {
        return 1;
    }
    return 0;
});
```

```
});
```

In this case, the `sort` function will not have any effect; it will obey the current order of lower and uppercase letters.

If we want lowercase letters to come first in the sorted array, then we need to use the `localeCompare` method:

```
names.sort((a, b) => a.localeCompare(b));
```

The output will be `["ana", "Ana", "john", "John"]`.

For accented characters, we can use the `localeCompare` method as well:

```
const names2 = ['Maëve', 'Maeve'];
console.log(names2.sort((a, b) => a.localeCompare(b)));
```

The output will be `["Maeve", "Maëve"]`.

Searching

We have two search options: the `indexOf` method, which returns the index of the first element that matches the argument passed, and `lastIndexOf`, which returns the index of the last element found that matches the argument passed. Let's go back to the `numbers` array that we were using before:

```
console.log(numbers.indexOf(10));
console.log(numbers.indexOf(100));
```

In the previous example, the output in the console would be `9` for the first line and `-1` (because it does not exist in our array) for the second line. We can get the same result with the following code:

```
numbers.push(10);
console.log(numbers.lastIndexOf(10));
console.log(numbers.lastIndexOf(100));
```

We added a new element with the value `10`, so the second line will output `15` (our array now has values from `1` to `15` and `10`), and the third line will output `-1` (because the element `100` does not exist in our array).

ECMAScript 2015 - the find and findIndex methods

Consider the following example:

```
let numbers = [1,2,3,4,5,6,7,8,9,10,11,12,13,14,15];
function multipleOf13(element, index, array) {
return (element % 13 == 0);
}
console.log(numbers.find(multipleOf13));
console.log(numbers.findIndex(multipleOf13));
```

The `find` and `findIndex` methods receive a callback function that will search for a value that satisfies the condition presented in the testing function (callback). For this example, we are looking to see whether the array `numbers` contain any multiple of 13.

The difference between `find` and `findIndex` is that the `find` method returns the first value of the array that satisfies the proposed condition. The `findIndex` method, on the other hand, returns the index of the first value of the array that satisfies the condition. If the value is not found, it returns `undefined`.

ECMAScript 2016 - using the includes method

The `includes` method returns `true` if an element is found in the array, and `false` otherwise. The following code is an example of how to use this method:

```
console.log(numbers.includes(15));
console.log(numbers.includes(20));
```

In this example, the `includes(15)` will return `true` and `includes(20)` will return `false` because the element 20 does not exist in the `numbers` array.

It is also possible to pass a starting index where we want the array to start searching for the value:

```
let numbers2 = [7,6,5,4,3,2,1];
console.log(numbers2.includes(4,5));
```

The output from the preceding example will be `false` because the element 4 does not exist after position 5.

Outputting the array into a string

Finally, we come to the final two methods: `toString` and `join`.

If we want to output all the elements of the array into a single string, we can use the `toString` method as follows:

```
console.log(numbers.toString());
```

This will output the values 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, and 10 to the console.

If we want to separate the elements by a different separator, such as `-`, we can use the `join` method to do just this, as follows:

```
const numbersString = numbers.join('-');
console.log(numbersString);
```

The output will be as follows:

```
1-2-3-4-5-6-7-8-9-10-11-12-13-14-15-10
```

This can be useful if we need to send the array's content to a server or to be decoded (and then, knowing the separator, it is easy to decode).



There are some great resources that you can use to boost your knowledge about arrays and their methods. Mozilla has a great page about arrays and their methods with great examples at https://developer.mozilla.org/en-US/docs/Web/JavaScript/Reference/Global_Objects/Array (<http://goo.gl/vu1diT>). The **Lo-Dash library** is also very useful when working with arrays in JavaScript projects: <http://lodash.com>.

The `TypedArray` class

We can store any datatype in JavaScript arrays. This is because JavaScript arrays are not strongly typed as in other languages such as C and Java.

`TypedArray` was created so that we could work with arrays with a single datatype. Its syntax is `let myArray = new TypedArray(length)`, where `TypedArray` needs to be replaced with one `TypedArray` class, as specified in the following table:

TypedArray	Description
Int8Array	8-bit two's complement signed integer
Uint8Array	8-bit unsigned integer
Uint8ClampedArray	8-bit unsigned integer
Int16Array	16-bit two's complement signed integer
Uint16Array	16-bit unsigned integer
Int32Array	32-bit two's complement signed integer
Uint32Array	32-bit unsigned integer
Float32Array	32-bit IEEE floating point number
Float64Array	64-bit IEEE floating point number

The following is an example:

```
let length = 5;
let int16 = new Int16Array(length);

let array16 = [];
array16.length = length;

for (let i=0; i<length; i++) {
int16[i] = i+1;
}
console.log(int16);
```

Typed arrays are great for working with WebGL APIs, manipulating bits, and manipulating files and images. Typed arrays work exactly like simple arrays, and we can also use the same methods and functionalities that we have learned in this chapter.

At the following link, you can find a good tutorial on how to use typed arrays to manipulate binary data and its applications in real-world projects: <http://goo.gl/kZBsGx>.

Arrays in TypeScript

All the source code from this chapter is valid TypeScript code. The difference is that TypeScript will do type checking at compile time to make sure we are only manipulating arrays in which all values have the same datatype.

If we take a look at the preceding code, it is the same `numbers` array as we declared in previous sections of this chapter:

```
const numbers = [1, 2, 3, 4, 5, 6, 7, 8, 9, 10];
```

Due to the type inference, TypeScript understands that the declaration of the `numbers` array is the same as `const numbers: number[]`. For this reason, we do not need to always explicitly declare the variable type if we initialize it during its declaration.

If we go back to the sorting example of the `friends` array, we can refactor the code to the following in TypeScript:

```
interface Person {
    name: string;
    age: number;
}

// const friends: {name: string, age: number}[];
const friends = [
    { name: 'John', age: 30 },
    { name: 'Ana', age: 20 },
    { name: 'Chris', age: 25 }
];

function comparePerson(a: Person, b: Person) {
    // content of the comparePerson function
}
```

By declaring the `Person` interface, we make sure the `comparePerson` function receives only objects that have `name` and `age`. The `friends` array does not have an explicit type, so in this case, if we wanted, we could explicitly declare its type using `const friends: Person[]`.

In summary, if we want to type our JavaScript variables using TypeScript, we simply need to use `const` or `let` `variableName: <type>[]` or, when using files with a `.js` extension, we can also have the type checking by adding the comment `// @ts-check` in the first line of the JavaScript file as we learned in Chapter 1, *JavaScript – A Quick Overview*.

At runtime, the output will be exactly the same as if we were using pure JavaScript.

Summary

In this chapter, we covered the most-used data structure: arrays. We learned how to declare, initialize, and assign values as well as add and remove elements. We learned about two-dimensional and multi-dimensional arrays as well as the main methods of an array, which will be very useful when we start creating our own algorithms in later chapters.

We also learned the new methods and functionalities that were added to the `Array` class in the ECMAScript 2015 and 2016 specifications.

And finally, we also learned how to make sure the array only contains values of the same type by using TypeScript or the TypeScript compile-time checking capability for JavaScript files.

In the next chapter, we will learn about stacks, which can be treated as arrays with a special behavior.

4 Stacks

We learned in the previous chapter how to create and use arrays, which are the most common type of data structure in computer science. As we learned, we can add and remove elements from an array at any index desired. However, sometimes we need some form of data structure where we have more control over adding and removing items. There are two data structures that have some similarities to arrays, but which give us more control over the addition and removal of elements. These data structures are **stacks** and **queues**.

In this chapter, we will cover the following topics:

- Creating our own JavaScript data structure library
- The stack data structure
- Adding elements to a stack
- Popping elements from a stack
- How to use the `Stack` class
- The decimal to binary problem

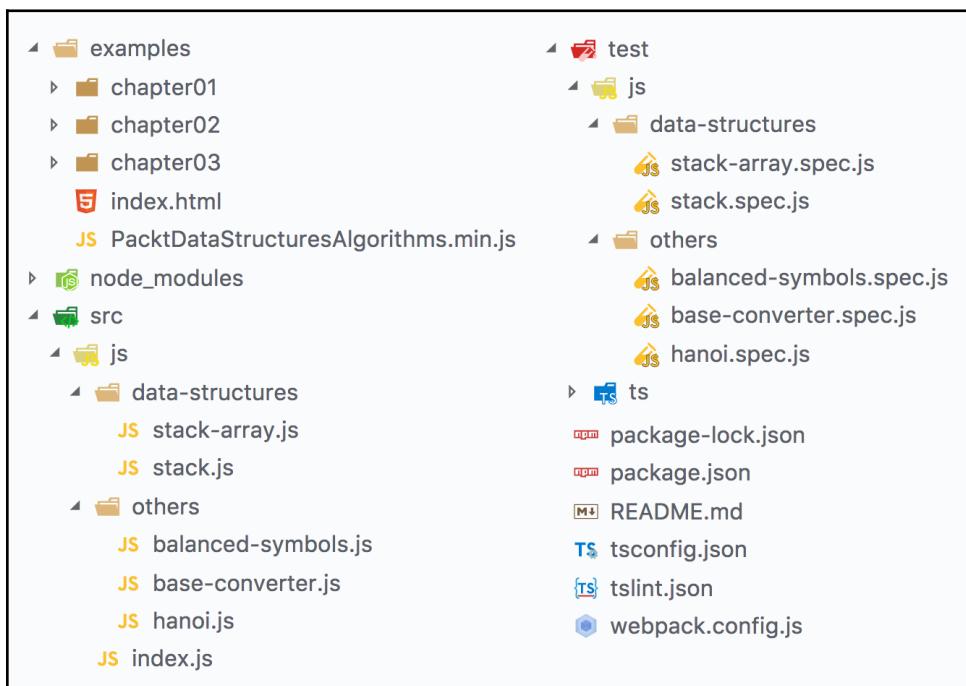
Creating a JavaScript data structure and algorithm library

Starting in this chapter, we are going to create our own JavaScript data structure and algorithm library. The source code bundle of this book has been prepared for this task.

After downloading the source code, and with Node.js installed on your computer as instructed in Chapter 1, *JavaScript – A Quick Overview*, change the directory to the project's folder and execute the command `npm install`, as demonstrated in the following screenshot:

```
[loiane:development loiane$ cd javascript-datastructures-algorithms
[loiane:javascript-datastructures-algorithms loiane$ npm install
> fsevents@1.1.2 install /Users/loiane/Documents/development/javascript-datastructures-algorithms/node_modules/fsevents
> node install
```

With all dependencies installed (`node_modules`), you will have access to scripts that will allow you to test, generate a test coverage report, and also generate a file named `PacktDataStructuresAlgorithms.min.js` that contains all the source code we will create, starting from this chapter. The following are the files from our library and some of the files we will create in this chapter:



The source code we will create in this chapter can be found in the `src/js` directory, organized by category. There is also a `test` folder, where you will find a `spec.js` file that matches its original file from the `src` folder. These files contain the test code written with a testing JavaScript test framework called **Mocha** (<https://mochajs.org>). And for every JavaScript file, you will also find a correspondent TypeScript file inside the `ts` folder. To run the tests, you can execute the command `npm run test`, and to run the tests and see the test coverage report (the percentage of the source code that is being covered by the tests), you can run `npm run dev`. If you are using **Visual Studio Code** as your editor, you will also find scripts to debug the test codes. Simply add your breakpoints where desired and run the Mocha TS or Mocha JS debug tasks. Inside the `package.json` file, you will also find the `npm run webpack` script which is responsible for generating the `PacktDataStructuresAlgorithms.min.js` file that is being used by our HTML examples. This script uses **Webpack** (<https://webpack.github.io>), a tool that will resolve all the ECMAScript 2015+ module dependencies, transpile the source code using Babel, bundle all the JavaScript files into a single one, and also make the code compatible with the browser or Node.js, as we learned in *Chapter 2, ECMAScript and TypeScript Overview*. More information about other available scripts can also be found in the `README.md` file.



Detailed steps to download the code bundle are mentioned in the *Preface* of this book. Please have a look. The code bundle for the book is also hosted on GitHub at <https://github.com/loiane/javascript-datastructures-algorithms>.

The stack data structure

A stack is an ordered collection of items that follows the last in, first out (**LIFO**) principle. The addition of new items or the removal of existing items takes place at the same end. The end of the stack is known as the top, and the opposite side is known as the base. The newest elements are near the top, and the oldest elements are near the base.

We have several examples of stacks in real life, for example, a pile of books, as we can see in the following image, or a stack of trays in a cafeteria or food court:



A stack is also used by compilers in programming languages, by the computer memory to store variables and method calls, and also by the browser history (the browser's back button).

Creating an array-based Stack class

We are going to create our own class to represent a stack. Let's start with the basics by creating a `stack-array.js` file and declaring our `Stack` class:

```
class Stack {  
    constructor() {  
        this.items = []; // {}  
    }  
}
```

We need a data structure that will store the elements of the stack. We can use an array to do it ({}). The array data structure allows us to add or remove elements from any position in the data structure. Since the stack follows the LIFO principle, we will limit the functionalities that will be available for the insertion and removal of elements. The following methods will be available in the `Stack` class:

- `push(element(s))`: This method adds a new element (or several elements) to the top of the stack.
- `pop()`: This method removes the top element from the stack. It also returns the removed element.

- `peek()`: This method returns the top element from the stack. The stack is not modified (it does not remove the element; it only returns the element for information purposes).
- `isEmpty()`: This method returns `true` if the stack does not contain any elements, and `false` if the size of the stack is bigger than 0.
- `clear()`: This method removes all the elements of the stack.
- `size()`: This method returns the number of elements that the stack contains. It is similar to the `length` property of an array.

Pushing elements to the stack

The first method that we will implement is the `push` method. This method is responsible for adding new elements to the stack, with one very important detail: we can only add new items to the top of the stack, meaning at the end of the stack. The `push` method is represented as follows:

```
push(element) {  
    this.items.push(element);  
}
```

As we are using an array to store the elements of the stack, we can use the `push` method from the JavaScript `Array` class that we covered in the previous chapter.

Popping elements from the stack

Next, we are going to implement the `pop` method. This method is responsible for removing the items from the stack. As the stack uses the LIFO principle, the last item that we added is the one that is removed. For this reason, we can use the `pop` method from the JavaScript `Array` class that we also covered in the previous chapter. The `pop` method is represented as follows:

```
pop() {  
    return this.items.pop();  
}
```

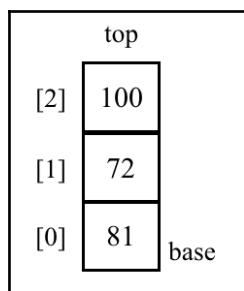
With the `push` and `pop` methods being the only methods available for adding and removing items from the stack, the LIFO principle will apply to our own `Stack` class.

Peeking the element from the top of the stack

Now, let's implement additional helper methods in our class. If we would like to know what the last element added to our stack was, we can use the `peek` method. This method will return the item from the top of the stack:

```
peek() {  
    return this.items[this.items.length - 1];  
}
```

As we are using an array to store the items internally, we can obtain the last item from an array using `length - 1` as follows:



For example, in the previous diagram, we have a stack with three items; therefore, the length of the internal array is 3. The last position used in the internal array is 2. As a result, the `length - 1` ($3 - 1$) is 2!

Verifying whether the stack is empty

The next method we will create is the `isEmpty` method, which returns `true` if the stack is empty (no element has been added), and `false` otherwise:

```
isEmpty() {  
    return this.items.length === 0;  
}
```

Using the `isEmpty` method, we can simply verify whether the length of the internal array is 0.

Similar to the `length` property from the `array` class, we can also implement `length` for our `Stack` class. For collections, we usually use the term `size` instead of `length`. And again, as we are using an array to store the elements internally, we can simply return its `length`:

```
size() {
    return this.items.length;
}
```

Clearing the elements of the stack

Finally, we are going to implement the `clear` method. The `clear` method simply empties the stack, removing all its elements. The simplest way of implementing this method is as follows:

```
clear() {
    this.items = [];
}
```

An alternative implementation would be calling the `pop` method until the stack is empty.

And we are done! Our `Stack` class is implemented.

Using the Stack class

In this topic, we will learn how to use the `Stack` class. The first thing we need to do is instantiate the `Stack` class we just created. Next, we can verify whether it is empty (the output is `true`, because we have not added any elements to our stack yet):

```
const stack = new Stack();
console.log(stack.isEmpty()); // outputs true
```

Next, let's add some elements to it (let's push the numbers 5 and 8; you can add any element type to the stack):

```
stack.push(5);
stack.push(8);
```

If we call the `peek` method, it is going to return the element 8, because it was the last element that was added to the stack:

```
console.log(stack.peek()); // outputs 8
```

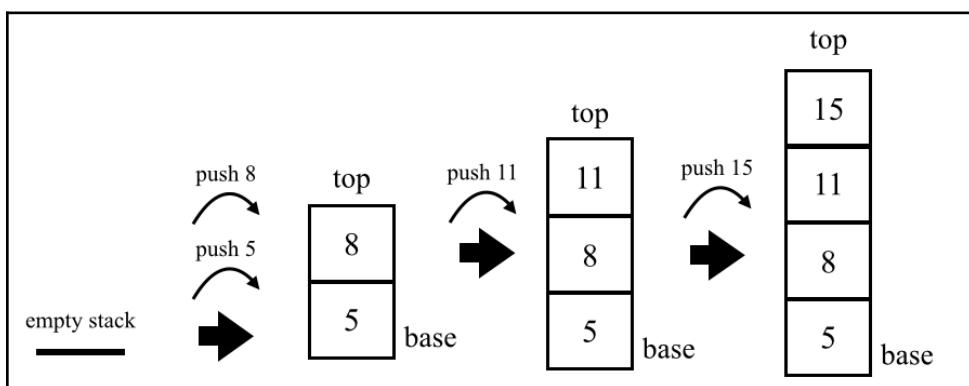
Let's also add another element:

```
stack.push(11);
console.log(stack.size()); // outputs 3
console.log(stack.isEmpty()); // outputs false
```

We added the element 11. If we call the `size` method, it will give the output as 3, because we have three elements in our stack (5, 8, and 11). Also, if we call the `isEmpty` method, the output will be `false` (we have three elements in our stack). Finally, let's add another element:

```
stack.push(15);
```

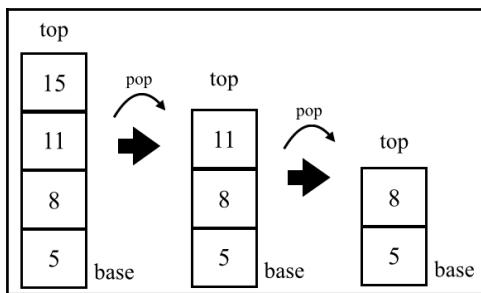
The following diagram shows all the `push` operations we have executed so far, and the current status of our stack:



Next, let's remove two elements from the stack by evoking the `pop` method twice:

```
stack.pop();
stack.pop();
console.log(stack.size()); // outputs 2
```

Before we evoked the `pop` method twice, our stack had four elements in it. After the execution of the `pop` method twice, the stack now has only two elements: 5 and 8. The following diagram exemplifies the execution of the `pop` method:



Creating a JavaScript object-based Stack class

The easiest way of creating a `Stack` class is using an array to store its elements. When working with a large set of data (which is very common in real-world projects), we also need to analyze what is the most efficient way of manipulating the data. When working with arrays, most methods have a complexity of time $O(n)$; we will learn more algorithm complexity in the last chapter of this book, Chapter 15, *Algorithm Complexity*. What this means is that, for most methods, we need to iterate through the array until we find the element we are looking for and, in the worst-case scenario, we will iterate through all the positions of the array, where n is the size of the array. If the array has more elements, it will take longer to iterate through all elements compared to an array with fewer elements. In addition, an array is an ordered set of the elements, and to keep the elements in order, it would need more space in the memory as well.

Wouldn't it be better if we could access the element directly, use less memory space, and still have all the elements organized the way we need to? For the scenario of a stack data structure in the JavaScript language, it is also possible to use a JavaScript object to store the stack elements, keep them in order, and also comply with the LIFO principle. Let's see how we can achieve this behavior.

We will start by declaring the `Stack` class (`stack.js` file) as follows:

```
class Stack {
  constructor() {
    this.count = 0;
    this.items = {};
  }
  // methods
}
```

For this version of the `Stack` class, we will use a `count` property to help us keep track of the size of the stack (and, consequently, also help us add and remove elements in the data structure).

Pushing elements to the stack

In the array-based version, we were able to add multiple elements to the `Stack` class at the same time. Since we are working with an object, this version of the `push` method only allows us to push a single element at a time. We can see the `push` method code below:

```
push(element) {  
    this.items[this.count] = element;  
    this.count++;  
}
```

In JavaScript, an object is a set of **key** and **value** pairs. To add an `element` to the stack, we will use the `count` variable as the key of the `items` object and the `element` will be its value. After pushing the element to the stack, we increment the `count`.

We can use the same example as before to use the `Stack` class and push the elements 5 and 8:

```
const stack = new Stack();  
stack.push(5);  
stack.push(8);
```

Internally, we will have the following values inside the `items` and `count` properties:

```
items = {  
    0: 5,  
    1: 8  
};  
count = 2;
```

Verifying whether the stack is empty and its size

The `count` property also works as the size of the stack. So, for the `size` method, we can simply return the `count` property:

```
size() {  
    return this.count;  
}
```

And to verify whether the stack is empty, we can compare if the `count` value is 0 as follows:

```
isEmpty() {
    return this.count === 0;
}
```

Popping elements from the stack

As we are not using an array to store the elements, we will need to implement the logic to remove an element manually. The `pop` method also returns the element that was removed from the stack. The `pop` method is as follows:

```
pop() {
    if (this.isEmpty()) { // {1}
        return undefined;
    }
    this.count--; // {2}
    const result = this.items[this.count]; // {3}
    delete this.items[this.count]; // {4}
    return result; // {5}
}
```

First, we need to verify whether the stack is empty ({1}) and, if so, we return the value `undefined`. If the stack is not empty, we will decrement the `count` property ({2}) and we will store the value from the top of the stack ({3}) so we can return it ({5}) after the element has been removed ({4}).

As we are working with a JavaScript object, to remove a specific value from the object, we can use the JavaScript `delete` operator.

Let's use the following internal values to emulate the `pop` action:

```
items = {
  0: 5,
  1: 8
};
count = 2;
```

To access the element from the top of the stack (latest element added: 8), we need to access the key with value 1. So we decrement the `count` variable from 2 to 1. We are able to access `items[1]`, delete it, and return its value.

Peeking the top of the stack and clearing it

In the last section, we learned that, in order to access the element that is stored at the top of the stack, it is necessary to decrement the `count` property by 1. So let's see the code for the `peek` method:

```
peek() {
    if (this.isEmpty()) {
        return undefined;
    }
    return this.items[this.count - 1];
}
```

And to clear the stack, we can simply reset it to the same values we used in the constructor:

```
clear() {
    this.items = {};
    this.count = 0;
}
```

We could also use the following logic to remove all elements from the stack, respecting the LIFO behavior:

```
while (!this.isEmpty()) {
    this.pop();
}
```

Creating the `toString` method

In the array version, we do not need to worry about a `toString` method because the data structure will use the one already provided by the array. For this object version, we will create a `toString` method so we can print the content of the stack similar to an array:

```
toString() {
    if (this.isEmpty()) {
        return '';
    }
    let objString = `${this.items[0]}`; // {1}
    for (let i = 1; i < this.count; i++) { // {2}
        objString = `${objString},${this.items[i]}`; // {3}
    }
    return objString;
}
```

If the stack is empty, we simply return an empty string. If it is not empty, we will initialize the string with the first element, from the base of the stack ({}1). Then, we will iterate through all the keys of the stack ({}2) until its top, adding a comma (,) followed by the next element ({}3). If the stack contains only one element, the code from lines {}2 and {}3 will not be executed.

With the `toString` method, we complete this version of the `Stack` class. This is also an example of how to have different versions of code. For the developer who uses the `Stack` class, it does not matter whether the array or the object version is used; both have the same functionality, but the behavior internally is very different.



With the exception of the `toString` method, all other methods we created have complexity $O(1)$, meaning we can access the element we are interested in directly and perform an action with it (`push`, `pop`, or `peek`).

Protecting the internal elements of the data structure

When we are creating a data structure or object that other developers might also use, we want to protect the internal elements so only the methods we exposed are used to modify the internal structure. In the case of the `Stack` class, we want to make sure the elements are added to the top of the stack and it is not possible to add elements in the base of the stack or any other random position (in the middle of the stack). Unfortunately, the `items` and the `count` properties we declared in the `Stack` class are not protected and this behavior is due to how JavaScript classes work.

Try running the following code:

```
const stack = new Stack();
console.log(Object.getOwnPropertyNames(stack)); // {1}
console.log(Object.keys(stack)); // {2}
console.log(stack.items); // {3}
```

We will get `["count", "items"]` as the output for lines {}1 or {}2. This means the `count` and `items` variables are public, as we easily access them, as demonstrated in line {}3. With this behavior, we can assign a new value to the `count` or `items` properties.

In this chapter, we used the **ES2015 (ES6)** syntax to create the `Stack` class. ES2015 classes are prototype-based. Although a prototype-based class saves memory and escalates better than function-based classes, this approach does not allow us to declare `private` properties (variables) or methods. And, in this case, we want the user of the `Stack` class to have access only to the methods we are exposing in the class. Let's take a look at other approaches that can allow us to have `private` properties in JavaScript.

The underscore naming convention

Some developers prefer using the underscore naming convention to mark an attribute as `private` in JavaScript:

```
class Stack {  
    constructor() {  
        this._count = 0;  
        this._items = {};  
    }  
}
```

It consists of prefixing an underscore (`_`) before the name of the attribute. But this option is just a convention; it does not protect the data and we depend on the common sense of the developer who will use our code.

ES2015 classes with scoped symbols

ES2015 introduced a new primitive type called `Symbol` that is immutable, and it can be used as an object property. Let's see how we can use it to declare the `items` property in the `Stack` class (we will use an array for storage to simplify the code):

```
const _items = Symbol('stackItems'); //{1}  
class Stack {  
    constructor () {  
        this[_items] = []; //{2}  
    }  
    //Stack methods  
}
```

In the preceding code, we declared the variable `_items` as a `Symbol` (line `{1}`), and initiated its value inside the class `constructor` (line `{2}`). To access the variable `_items`, we simply need to replace all `this.items` occurrences with `this[_items]`.

This approach provides a false class `private` property, because the method `Object.getOwnPropertySymbols` was also introduced in ES6, and it can be used to retrieve all the property symbols declared in the class. An example of how we can explore and hack the `Stack` class is given as follows:

```
const stack = new Stack();
stack.push(5);
stack.push(8);
let objectSymbols = Object.getOwnPropertySymbols(stack);
console.log(objectSymbols.length); // outputs 1
console.log(objectSymbols); // [Symbol()]
console.log(objectSymbols[0]); // Symbol()
stack[objectSymbols[0]].push(1);
stack.print(); //outputs 5, 8, 1
```

As we can see from the preceding code, it is possible to retrieve the `_items` symbol by accessing `stack[objectSymbols[0]]`. And, as the `_items` property is an array, we can do any array operation such as removing or adding an element to the middle of the array (the same would happen if we were using an object to store the elements). But this is not what we want as we are working with a stack.

So let's see a third option.

ES2015 classes with WeakMap

There is one datatype we can use to ensure that the property will be `private` in a class, and it is called `WeakMap`. We will explore the `map` data structure in detail in Chapter 8, *Dictionaries and Hashes*, but, for now, we need to know that a `WeakMap` can store a key value pair, where the key is an object and the value can be any datatype.

Let's see what the `Stack` class would look like if we used `WeakMap` to store the `items` attribute (array version):

```
const items = new WeakMap(); // {1}

class Stack {
  constructor () {
    items.set(this, []); // {2}
  }
  push(element) {
    const s = items.get(this); // {3}
    s.push(element);
  }
  pop() {
```

```
    const s = items.get(this);
    const r = s.pop();
    return r;
}
//other methods
}
```

The above code snippet can be interpreted as follows:

- In line {1}, we declare the `items` variable as a `WeakMap`.
- In line {2}, we set the `items` value inside the constructor by setting `this` (reference to the `Stack` class) as the key of the `WeakMap` and the array that represents the stack as its value.
- In line {3}, we retrieve the value of the `items` by retrieving the value from the `WeakMap`, that is, by passing `this` as the key (that we set in line {2}).

Now we know that the `items` property is truly private in the `Stack` class. With this approach, the code is not easy to read and it is not possible to inherit the `private` properties if we extend this class; we cannot have it all!

ECMAScript class field proposal

TypeScript has a `private` modifier for class properties and methods. However, this modifier works only during compilation time (as the TypeScript type and error checking that we have already discussed in previous chapters). After the code is transpiled to JavaScript, the attribute will be public as well.

The truth is we cannot declare `private` properties or methods as is possible in other programming languages. There are different approaches with which we can achieve the same result, but each one has its pros and cons regarding a simpler syntax or performance.

Which approach is better? It depends on how you use the algorithms presented in this book in real-life projects. It depends on the volume of data you will be dealing with, on the number of instances that you need of the classes we create, among other constraints. Ultimately, the decision is yours.

At the time of writing, there is a proposal to add `private` properties to JavaScript classes. With this proposal, we will be able to declare JavaScript class fields directly in the class body and also initialize the properties. The following is an example:

```
class Stack {
  #count = 0;
```

```
#items = 0;  
  
// stack methods  
}
```

We will be able to declare `private` properties by prefixing the properties with the hash symbol (#). This behavior is very similar to the privacy of attributes with `WeakMap`. So hopefully, in the near future, we will not need to apply hacks or compromise the readability of the code to use `private` class attributes.



For more information about the class field proposal, please access: <https://github.com/tc39/proposal-class-fields>.

Solving problems using stacks

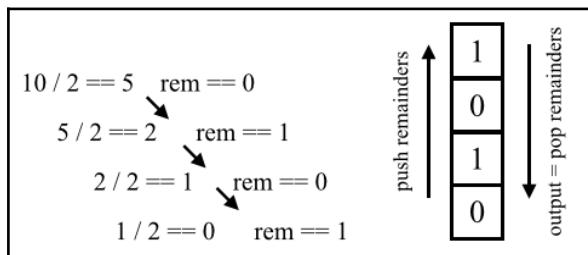
Stacks have a variety of applications in real-world problems. They can be used for backtracking problems to remember tasks or paths visited, and to undo actions (we will learn how to apply this example when we discuss graphs and backtracking problems later in this book). The Java and C# programming languages use stacks to store variables and method calls and there is a stack overflow exception that can be thrown, especially when working with recursive algorithms (which we will cover later in this book as well).

Now that we know how to use the `Stack` class, let's use it to solve some computer science problems. In this section, we will cover the decimal to binary problem, where we will also transform the algorithm into a base converter algorithm.

Converting decimal numbers to binary

We are already familiar with the decimal base. However, binary representation is very important in computer science, as everything in a computer is represented by binary digits (0 and 1). Without the ability to convert back and forth between decimal and binary numbers, it would be a little difficult to communicate with a computer.

To convert a decimal number into a binary representation, we can divide the number by 2 (binary is a base 2 number system) until the division result is 0. As an example, we will convert the number 10 into binary digits:



This conversion is one of the first things you learn in college (computer science classes). The following is our algorithm:

```
function decimalToBinary(decNumber) {
    const remStack = new Stack();
    let number = decNumber;
    let rem;
    let binaryString = '';

    while (number > 0) { // {1}
        rem = Math.floor(number % 2); // {2}
        remStack.push(rem); // {3}
        number = Math.floor(number / 2); // {4}
    }

    while (!remStack.isEmpty()) { // {5}
        binaryString += remStack.pop().toString();
    }

    return binaryString;
}
```

In the preceding code, while the division result is not zero (line {1}), we get the remainder of the division (modulo - mod), and push it to the stack (lines {2} and {3}) and, finally, we update the number that will be divided by 2 (line {4}). An important observation: JavaScript has a numeric datatype, but it does not distinguish integers from floating points. For this reason, we need to use the `Math.floor` function to obtain only the integer value from the division operations. Finally, we pop the elements from the stack until it is empty, concatenating the elements that were removed from the stack into a string (line {5}).

We can try the previous algorithm and output its result on the console using the following code:

```
console.log(decimalToBinary(233)); // 11101001
console.log(decimalToBinary(10)); // 1010
console.log(decimalToBinary(1000)); // 1111101000
```

The base converter algorithm

We can modify the previous algorithm to make it work as a converter from decimal to the bases between 2 and 36. Instead of dividing the decimal number by 2, we can pass the desired base as an argument to the method and use it in the division operations, as shown in the following algorithm:

```
function baseConverter(decNumber, base) {
    const remStack = new Stack();
    const digits = '0123456789ABCDEFGHIJKLMNOPQRSTUVWXYZ'; // {6}
    let number = decNumber;
    let rem;
    let baseString = '';

    if (!(base >= 2 && base <= 36)) {
        return '';
    }

    while (number > 0) {
        rem = Math.floor(number % base);
        remStack.push(rem);
        number = Math.floor(number / base);
    }

    while (!remStack.isEmpty()) {
        baseString += digits[remStack.pop()]; // {7}
    }

    return baseString;
}
```

There is one more thing we need to change. In the conversion from decimal to binary, the remainders will be 0 or 1; in the conversion from decimal to octagonal, the remainders will be from 0 to 8; and in the conversion from decimal to hexadecimal, the remainders can be 0 to 9 plus the letters A to F (values 10 to 15). For this reason, we need to convert these values as well (lines {6} and {7}). So, starting at base 11, each letter of the alphabet will represent its base. The letter A represents base 11, B represents base 12, and so on.

We can use the previous algorithm and output its result on the console as follows:

```
console.log(baseConverter(100345, 2)); // 110000111111001  
console.log(baseConverter(100345, 8)); // 303771  
console.log(baseConverter(100345, 16)); // 187F9  
console.log(baseConverter(100345, 35)); // 2BW0
```



You will also find the balanced parentheses (palindrome problem) and the Hanoi Tower examples when you download the source code of this book.

Summary

In this chapter, we learned about the stack data structure. We implemented our own algorithm that represents a stack using arrays and a JavaScript object, and we learned how to add and remove elements from it using the `push` and `pop` methods.

We compared different syntaxes that can be used to create the `Stack` class, and presented the pros and cons of each one. We also covered how to solve one of the most famous problems in computer science using stacks.

In the next chapter, we will learn about queues, which are very similar to stacks, but use a principle different from LIFO.

5

Queues and Deques

We have learned how stacks work. Queues are a very similar data structure, but instead of LIFO, they use a different principle that we will learn about in this chapter. We will also learn how deques, a data structure that mixes the stack and queue principles, work.

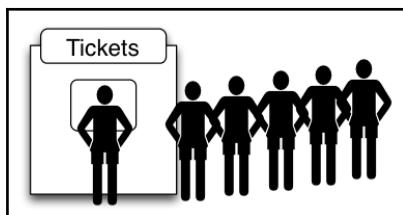
In this chapter, we will cover the following topics:

- The queue data structure
- The deque data structure
- Adding elements to a queue and a deque
- Removing elements from a queue and a deque
- Simulating circular queues with the Hot Potato game
- Checking whether a phrase is a palindrome with a deque

The queue data structure

A **queue** is an ordered collection of items that follows the **first in, first out (FIFO)**, also known as the **first come, first served**, principle. The addition of new elements in a queue is at the tail, and the removal is from the front. The newest element added to the queue must wait at the end of the queue.

The most popular example of a queue in real life is the typical line that we form from time to time:



We have lines for movies, the cafeteria, and a checkout line at a grocery store, among other examples. The first person in the line is the first one who will be attended to.

A very popular example in computer science is the printing line. Let's say we need to print five documents. We open each document and click on the Print button. Each document will be sent to the print line. The first document that we asked to be printed is going to be printed first and so on, until all the documents are printed.

Creating the Queue class

We are now going to create our own class to represent a queue. Let's start with the basics and declare our class:

```
class Queue {  
    constructor() {  
        this.count = 0; // {1}  
        this.lowestCount = 0; // {2}  
        this.items = {}; // {3}  
    }  
}
```

First, we need a data structure that will store the elements of the queue. We can use an array to do it, just like we did for the `Stack` class in one of the examples in the previous chapter; however, we will use an object to store our elements ({3}); this will allow us to write a more efficient data structure when accessing its elements. You will also notice the `Queue` and `Stack` classes are very similar, just the principles for adding and removing the elements are different.

To help us control the size of the queue, we declare a `count` property as well ({1}). And, since we will be removing elements from the front of the queue, we also need a variable to help us track the first element. For this purpose, we declare the `lowestCount` variable ({2}).

Next, we need to declare the methods available for a queue:

- `enqueue (element)` : This method adds a new element at the back of the queue.
- `dequeue ()` : This method removes the first element from the queue (the item that is in the front of the queue). It also returns the removed element.
- `peek ()` : This method returns the first element from the queue, the first one added, and the first one that will be removed from the queue. The queue is not modified (it does not remove the element; it only returns the element for information purposes - very similar to the `peek` method from the `Stack` class). This method also works as the `front` method, as it is known in other languages.
- `isEmpty ()` : This method returns `true` if the queue does not contain any elements, and `false` if the queue size is bigger than 0.
- `size ()` : This method returns the number of elements the queue contains. It is similar to the `length` property of the array.

Enqueuing elements to the queue

The first method that we will implement is the `enqueue` method. This method will be responsible for adding new elements to the queue, with one very important detail: we can only add new elements to the end of the queue:

```
enqueue(element) {  
    this.items[this.count] = element;  
    this.count++;  
}
```

The `enqueue` method has the same implementation as the `push` method from the `Stack` class. As the `items` property is a JavaScript object, it is a collection of **key** and **value** pairs. To add an element to the queue, we will use the `count` variable as the key of the `items` object and the `element` will be its value. After pushing the element to the stack, we increment the `count`.

Dequeuing elements from the queue

Next, we are going to implement the `dequeue` method. This method is responsible for removing items from the queue. As the queue uses the FIFO principle, the first item that we added in the queue is the one that is removed:

```
dequeue() {
    if (this.isEmpty()) {
        return undefined;
    }
    const result = this.items[this.lowestCount]; // {1}
    delete this.items[this.lowestCount]; // {2}
    this.lowestCount++; // {3}
    return result; // {4}
}
```

First, we need to verify whether the queue is empty and, if so, we return the value `undefined`. If the queue is not empty, we will store the value from the front of the queue ({1}) so we can return it ({4}) after the element has been removed ({2}). We also need to increase the `lowestCount` property by 1 ({2}).

Let's consider the following internal values to emulate the `dequeue` action:

```
items = {
    0: 5,
    1: 8
};
count = 2;
lowestCount = 0;
```

To access the element from the front of the queue (the first element added: 5), we need to access the key with value 0. We are able to access `items[0]`, delete it, and return its value. In this scenario, after removing the first element, the `items` property will contain only one element (1: 8), which will be the next to be removed if we evoke the `dequeue` method. So we increment the `lowestCount` variable from 0 to 1.

With the `enqueue` and `dequeue` methods being the only methods available for adding and removing items from the queue, we have ensured the FIFO principle operates for our own `Queue` class.

Peeking the element from the front of the queue

Now, let's implement some additional helper methods for our class. If we want to know what the front element of our queue is, we can use the `peek` method. This method will return the item from the front of the queue (using the `lowestCount` as a key to retrieve the element value):

```
peek() {
    if (this.isEmpty()) {
        return undefined;
    }
    return this.items[this.lowestCount];
}
```

Verifying whether the queue is empty and its size

The next method is the `isEmpty` method, which returns `true` if the queue is empty, and `false` otherwise:

```
isEmpty() {
    return this.count - this.lowestCount === 0;
}
```

To calculate how many elements there are in the queue, we simply calculate the difference between the `count` property and the `lowestCount`.

Suppose the `count` property has value 2 and the `lowestCount` has value 0. This means we have two elements in the queue. Next, we remove one element from the queue. The property `lowestCount` will be updated to value 1 and `count` will continue with value 2. Now the queue has only one element, and so on.

So to implement the `size` method, we simply return this difference:

```
size() {
    return this.count - this.lowestCount;
}
```

We can also write the `isEmpty` method as follows:

```
isEmpty() {
    return this.size() === 0;
}
```

Clearing the queue

To clear all the elements from the queue, we can evoke the `dequeue` method until it returns `undefined` or we can simply reset the value of the `Queue` class properties to the same values as declared in its constructor:

```
clear() {
    this.items = {};
    this.count = 0;
    this.lowestCount = 0;
}
```

Creating the `toString` method

And we are done! Our `Queue` class is implemented. Just like we did for the `Stack` class, we can also add the `toString` method:

```
toString() {
    if (this.isEmpty()) {
        return '';
    }
    let objString = `${this.items[this.lowestCount]}`;
    for (let i = this.lowestCount + 1; i < this.count; i++) {
        objString = `${objString},${this.items[i]}`;
    }
    return objString;
}
```

In the `Stack` class, we started to iterate the items values from index zero. As the first index of the `Queue` class might not be zero, we start iterating it from the `lowestCount` index.

And now we are really done!



The `Queue` and `Stack` classes are very similar. The main difference comes with the `dequeue` and `peek` methods, which is because of the difference between the FIFO and LIFO principles.

Using the Queue class

First, we need to instantiate the Queue class that we created. Next, we can verify that it is empty (the output is `true` because we have not added any elements to our queue yet):

```
const queue = new Queue();
console.log(queue.isEmpty()); // outputs true
```

Next, let's add some elements to it (let's enqueue the elements '`John`' and '`Jack`'; you can add any element type to the queue):

```
queue.enqueue('John');
queue.enqueue('Jack');
console.log(queue.toString()); // John, Jack
```

Let's add another element:

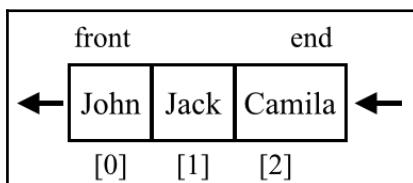
```
queue.enqueue('Camila');
```

Let's also execute some other commands:

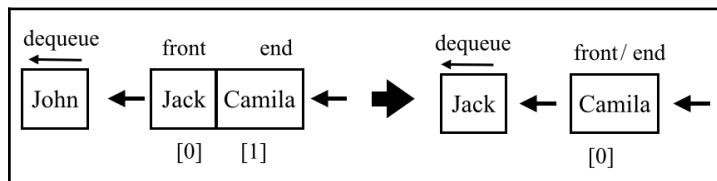
```
console.log(queue.toString()); // John, Jack, Camila
console.log(queue.size()); // outputs 3
console.log(queue.isEmpty()); // outputs false
queue.dequeue(); // remove John
queue.dequeue(); // remove Jack
console.log(queue.toString()); // Camila
```

If we ask to output the contents of the queue, we will get `John`, `Jack`, and `Camila`. The size of the queue will be `3`, because we have three elements queued in it (and it is also not going to be empty).

The following diagram exemplifies all the `enqueue` operations we executed so far, and the current status of our queue:



Next, we asked to `dequeue` two elements (the `dequeue` method is executed twice). The following diagram exemplifies the `dequeue` method execution:



And when we finally ask to output the contents of the queue again, we only have the element `Camila`. The first two queued elements were dequeued; the final element queued to the data structure is the last one that will be dequeued from it. That is, we follow the FIFO principle.

The deque data structure

The `deque` data structure, also known as the **double-ended queue**, is a special queue that allows us to insert and remove elements from the end or from the front of the queue.

An example of a deque in real life is the typical line for movie theaters, cafeterias, and so on. For example, a person who has just bought a ticket can come back to the front of the queue just to ask for some quick information. And if the person who is at the back of the queue is in a hurry, this person can also leave the queue.

In computer science, a common application of a deque is storing a list of undo operations. Each time a user performs an operation in the software, the operation is pushed to the deque (just like in a stack). When the user clicks on the Undo button, the operation is popped from the deque, meaning it is removed from the back. After a predefined number of operations, the older ones are removed from the front of the deque. Because the deque implements both principles, FIFO and LIFO, we can also say that the deque is a merger between the queue and the stack data structures.

Creating the Deque class

As usual, we will start by declaring the `Deque` class and its constructor:

```
class Deque {  
    constructor() {  
        this.count = 0;  
        this.lowestCount = 0;  
        this.items = {};  
    }  
}
```

Since a deque is a special queue, we will notice that it shares some code snippets with the constructor, the same internal properties, and the following methods: `isEmpty`, `clear`, `size`, and `toString`.

Since the deque allows inserting and removing from both ends, we will also have the following methods:

- `addFront (element)`: This method adds a new element at the front of the deque
- `addBack (element)`: This method adds a new element at the back of the deque (same implementation as the `enqueue` method from the `Queue` class)
- `removeFront ()`: This method removes the first element from the deque (the same implementation as the `dequeue` method from the `Queue` class)
- `removeBack ()`: This method removes the last element from the deque (the same implementation as the `pop` method from the `Stack` class)
- `peekFront ()`: This method returns the first element from the deque (the same implementation as the `peek` method from the `Queue` class)
- `peekBack ()`: This method returns the last element from the deque (the same implementation as the `peek` method from the `Stack` class)



The `Deque` class also implements the `isEmpty`, `clear`, `size`, and `toString` methods (you can check the complete source code by downloading the source code bundle from this book).

Adding elements to the front of the deque

As we have implemented the logic for some methods already, we will focus only on the logic for the `addFront` method. The code for the `addFront` method is presented as follows:

```
addFront(element) {  
    if (this.isEmpty()) { // {1}  
        this.addBack(element);  
    } else if (this.lowestCount > 0) { // {2}  
        this.lowestCount--;  
        this.items[this.lowestCount] = element;  
    } else {  
        for (let i = this.count; i > 0; i--) { // {3}  
            this.items[i] = this.items[i - 1];  
        }  
        this.count++;  
        this.lowestCount = 0;  
        this.items[0] = element; // {4}  
    }  
}
```

When adding an element to the front of the deque, there are three scenarios.

The first scenario is when the deque is empty ({1}). In this case, we can evoke the `addBack` method. The element will be added at the back of the deque, which, in this case, will also be the front of the deque. The `addBack` method already has the logic required to increase the `count` property, so we can reuse it to avoid duplicating code.

The second scenario is when an element is removed from the front of the deque ({2}), meaning the `lowestCount` property will have value 1 or higher. In this case, we simply need to decrease the `lowestCount` property and assign the element to that object key (position).

Consider the following internal values for the `Deque` class:

```
items = {  
    1: 8,  
    2: 9  
};  
count = 3;  
lowestCount = 1;
```

If we want to add the element 7 to the front of the deque, we will match the second scenario. In this example, the `lowestCount` value will be decreased (new value will be 0 - zero), and we will add value 7 to the key 0.

The third and last scenario is when the `lowestCount` is equals to 0 (zero). We could assign a key with a negative value, and update the logic used to calculate the size of the deque to also evaluate negative keys. In this case, the operation to add a new value would continue to have the lowest computational cost. For educational purposes, we will treat this scenario as if we were working with arrays. To add a new element in the first key or position, we need to move all elements to the next position (`{3}`) to free the first `index`. Because we do not want to lose any existing value, we start to iterate the existing values of the `items` property by its last index, assigning the element from `index - 1`. After all elements have been moved, the first position will be free and we can overwrite any exiting value with the element we want to add to the deque (`{4}`).

Using the Deque class

After instantiating the `Deque` class, we can evoke its methods:

```
const deque = new Deque();
console.log(deque.isEmpty()); // outputs true
deque.addBack('John');
deque.addBack('Jack');
console.log(deque.toString()); // John,Jack
deque.addBack('Camila');
console.log(deque.toString()); // John,Jack,Camila
console.log(deque.size()); // outputs 3
console.log(deque.isEmpty()); // outputs false
deque.removeFront(); // remove John
console.log(deque.toString()); // Jack,Camila
deque.removeBack(); // Camila decides to leave
console.log(deque.toString()); // Jack
deque.addFront('John'); // John comes back for information
console.log(deque.toString()); // John,Jack
```

With the `Deque` class, we can evoke operations from the `Stack` and `Queue` classes. We could also use the `Deque` class to implement a priority queue, but we will explore this topic in Chapter 11, *Binary Heap and Heap Sort*.

Solving problems using queues and deques

Now that we know how to use the `Queue` and `Deque` classes, let's use them to solve some computer science problems. In this section, we will cover a simulation of the Hot Potato game with queues and also how to check whether a phrase is a palindrome with deques.

The circular queue – Hot Potato

As queues are often applied in computer science and also in our lives, there are some modified versions of the default queue we implemented in this chapter. One of the modified versions is the **circular queue**. An example of a circular queue is the Hot Potato game. In this game, children are organized in a circle, and they pass the hot potato to their neighbor as fast as they can. At a certain point of the game, the hot potato stops being passed around the circle of children, and the child that has the hot potato is removed from the circle. This action is repeated until there is only one child left (the winner).

For this example, we will implement a simulation of the Hot Potato game:

```
function hotPotato(elementsList, num) {  
    const queue = new Queue(); // {1}  
    const eliminatedList = [];  
  
    for (let i = 0; i < elementsList.length; i++) {  
        queue.enqueue(elementsList[i]); // {2}  
    }  
  
    while (queue.size() > 1) {  
        for (let i = 0; i < num; i++) {  
            queue.enqueue(queue.dequeue()); // {3}  
        }  
        eliminatedList.push(queue.dequeue()); // {4}  
    }  
  
    return {  
        eliminated: eliminatedList,  
        winner: queue.dequeue() // {5}  
    };  
}
```

To implement a simulation of this game, we will use the `Queue` class we implemented at the beginning of this chapter ({1}). We will get a list of names, and queue all of them ({2}). Given a number, we need to iterate the queue. We will remove an item from the beginning of the queue, and add it to the end of the queue ({3}) to simulate the hot potato (if you have passed the hot potato to your neighbor, you are not threatened with elimination right away). Once we reach the number, the person that has the hot potato is eliminated (removed from the queue {4}). When there is only one person left, this person is declared the winner (line {5}).

We can use the following code to try the `hotPotato` algorithm:

```
const names = ['John', 'Jack', 'Camila', 'Ingrid', 'Carl'];
const result = hotPotato(names, 7);

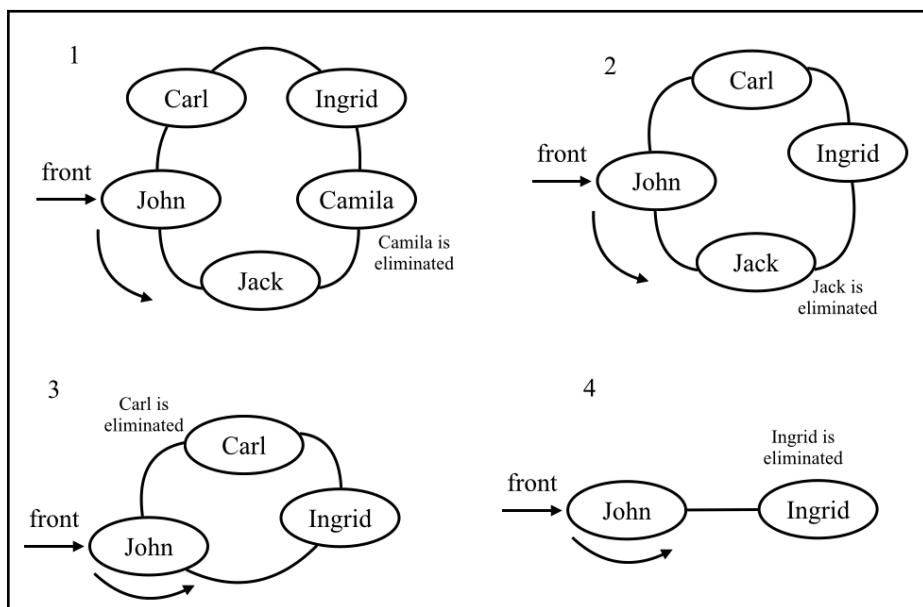
result.eliminated.forEach(name => {
  console.log(`\$${name} was eliminated from the Hot Potato game.`);
});

console.log(`The winner is: ${result.winner}`);
```

The output from the previous algorithm is as follows:

```
Camila was eliminated from the Hot Potato game.
Jack was eliminated from the Hot Potato game.
Carl was eliminated from the Hot Potato game.
Ingrid was eliminated from the Hot Potato game.
The winner is: John
```

This output is simulated in the following diagram:



You can change the number passed to the `hotPotato` function to simulate different scenarios.

Palindrome checker

The following is the definition of a **palindrome** according to Wikipedia:

A palindrome is a word, phrase, number, or other sequence of characters which reads the same backward as forward, such as madam or racecar.

There are different algorithms we can use to verify whether a phrase or string is a palindrome. The easiest way is reversing the string and comparing it with the original string. If both strings are equal, then we have a palindrome. We can also use a stack to do this, but the easiest way of solving this problem using a data structure is using a deque.

The following algorithm uses a deque to solve this problem:

```
function palindromeChecker(aString) {  
    if (aString === undefined || aString === null ||  
        (aString !== null && aString.length === 0)) { // {1}  
        return false;  
    }  
    const deque = new Deque(); // {2}  
    const lowerString = aString.toLocaleLowerCase().split(' ').join(''); //  
    {3}  
    let isEqual = true;  
    let firstChar, lastChar;  
  
    for (let i = 0; i < lowerString.length; i++) { // {4}  
        deque.addBack(lowerString.charAt(i));  
    }  
  
    while (deque.size() > 1 && isEqual) { // {5}  
        firstChar = deque.removeFront(); // {6}  
        lastChar = deque.removeBack(); // {7}  
        if (firstChar !== lastChar) {  
            isEqual = false; // {8}  
        }  
    }  
  
    return isEqual;  
}
```

Before we start with the algorithm logic, we need to verify whether the string that was passed as a parameter is valid ({1}). If it is not valid, then we return `false`.

For this algorithm, we will use the `Deque` class we implemented in this chapter ({2}). As we can receive a string with both lowercase and capital letters, we will transform all letters to lowercase and we will also remove all the spaces ({3}). If you want to, you can also remove all special characters such as ! ? - () and so on. To keep this algorithm simple, we will skip this part.

Next, we will enqueue all characters of the string to the `deque` ({4}). While we will have elements in the `deque` (if only one character is left, it is a palindrome) and the string is a palindrome ({5}), we will remove one element from the front ({6}) and one from the back ({7}). To be a palindrome, both characters removed from the `deque` need to match. If the characters do not match, then the string is not a palindrome ({8}).

We can use the following code to try the `palindromeChecker` algorithm:

```
console.log('a', palindromeChecker('a'));
console.log('aa', palindromeChecker('aa'));
console.log('kayak', palindromeChecker('kayak'));
console.log('level', palindromeChecker('level'));
console.log('Was it a car or a cat I saw', palindromeChecker('Was it a car
or a cat I saw'));
console.log('Step on no pets', palindromeChecker('Step on no pets'));
```

The output for all the preceding examples is `true`.

JavaScript task queues

Since we are using JavaScript in this book, why not explore a little bit further how the language works?

When we open a new tab in the browser, a task queue is created. This is because only a single thread handles all the tasks for a single tab, and it is called an **event loop**. The browser is responsible for several tasks, such as rendering the HTML, executing JavaScript code commands, handling user interaction (user input, mouse clicks, and so on), and executing and processing asynchronous requests. You can learn more about event loops at the following link: <https://goo.gl/ayF840>.

It is really nice to know that a popular and powerful language such as JavaScript uses such a basic data structure to handle internal control.

Summary

In this chapter, we learned about the queue data structure. We implemented our own algorithm that represents a queue, and we learned how to add and remove elements from it using the `enqueue` and `dequeue` methods following the FIFO principle. We also learned about the deque data structure, how to add elements to the front and the back of the deque, and how to remove elements from the front or the back of the deque.

We also covered how to solve two famous problems using the queue and deque data structures: the Hot Potato game (using a modified queue: the circular queue) and a palindrome checker using a deque.

In the next chapter, we will learn about linked lists, a dynamic and more complex data structure.

6 Linked Lists

In Chapter 3, *Arrays*, you learned about the array data structure. An array (we can also call it a list) is a very simple data structure that stores a sequence of data. In this chapter, you will learn how to implement and use a linked list, which is a dynamic data structure, meaning that we can add or remove items from it at will and it will grow as required.

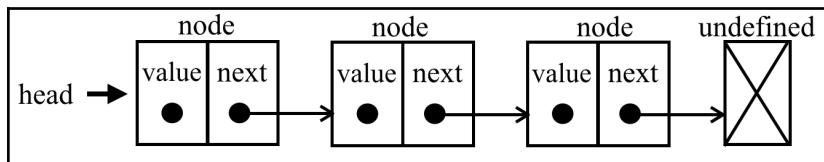
In this chapter, we will cover the following topics:

- The linked list data structure
- Adding elements to a linked list
- Removing elements from a linked list
- How to use the `LinkedList` class
- Doubly linked lists
- Circular linked lists
- Sorted linked list
- Implementing a stack with linked lists

The linked list data structure

Arrays (or lists) are probably the most common data structure used to store a collection of elements. As we mentioned previously in this book, each language has its own implementation of arrays. This data structure is very convenient and provides a handy `[]` syntax to access its elements. However, this data structure has a disadvantage: the size of the array is fixed (in most languages), and inserting or removing items from the beginning or from the middle of the array is expensive, because the elements need to be shifted over (even though we learned that JavaScript has methods from the `Array` class that will do that for us; this is what happens behind the scenes as well).

Linked lists store a sequential collection of elements but, unlike arrays, in linked lists the elements are not placed contiguously in memory. Each element consists of a node that stores the element itself and also a reference (also known as a pointer or link) that points to the next element. The following diagram demonstrates the structure of a linked list:

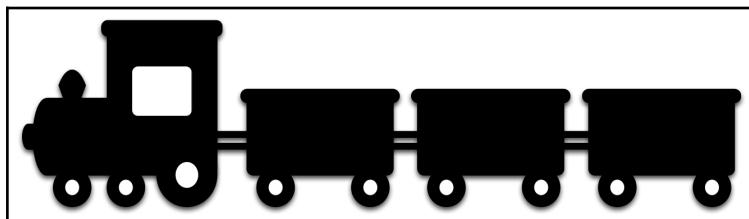


One of the benefits of a linked list over a conventional array is that we do not need to shift elements over when adding or removing them. However, we need to use pointers when working with a linked list and, because of this, we need to pay some extra attention when implementing a linked list. In the array, we can directly access any element at any position; in the linked list, if we want to access an element from the middle, we need to start from the beginning (**head**) and iterate the list until we find the desired element.

We have some real-world examples for linked lists. The first example is a conga line. Each person is an element, and the hands would be the pointer that links to the next person in the conga line. You can add people to the line—you just need to find the spot where you want to add the person, decouple the connection, then insert the new person and make the connection again.

Another example would be a scavenger hunt. You have a clue, and this clue is the pointer to the place where you can find the next clue. With this link, you go to the next place and get another clue that will lead to the next one. The only way to get a clue from the middle of the list is to follow the list from the beginning (from the first clue).

We have another example—which might be the most popular one used to exemplify linked lists—that of a train. A train consists of a series of vehicles (also known as wagons). Each vehicle or wagon is linked to each other. You can easily decouple a wagon, change its place, or add or remove it. The following figure demonstrates a train. Each wagon is an element of the list and the link between the wagons is the pointer:



In this chapter, we will cover the linked list as well as some of its variations, but let's start with the easiest data structure first.

Creating the LinkedList class

Now that you understand what a linked list is, let's start implementing our data structure. This is the skeleton of our `LinkedList` class:

```
import { defaultEquals } from '../util';
import { Node } from './models/linked-list-models'; // {1}

export default class LinkedList {
    constructor>equalsFn = defaultEquals) {
        this.count = 0; // {2}
        this.head = undefined; // {3}
        this.equalsFn = equalsFn; // {4}
    }
}
```

For the `LinkedList` data structure, we start by declaring the `count` property ({2}), which stores the number of elements we have in the list.

We are going to implement a method named `indexOf`, which will allow us to find a specific element in the linked list. To compare equality between elements of the linked list, we will use a function that will be internally evoked as `equalsFn` ({4}). The developer that will use the `LinkedList` class, so that they will be able to pass a custom function that compares two JavaScript objects or values. If no custom function is passed, this data structure will use the `defaultEquals` function that is declared in the `util.js` file (so we can reuse it for other data structures and algorithms we will create in the subsequent chapters) as the default equality comparison function. The `defaultEquals` function is presented as follows:

```
export function defaultEquals(a, b) {
    return a === b;
}
```



The default parameter value and the module import for the `defaultEquals` function are part of the **ECMAScript 2015 (ES6)** functionalities, as we learned in Chapter 2, *ECMAScript and TypeScript Overview*.

Since this data structure is dynamic, we also need to store a reference to the first element as well. To do this, we can store the `this` reference inside a variable that we will call `head` ({3}).

To represent the head and other elements of the linked list, we need a helper class called `Node` ({}1). The `Node` class represents the item that we want to add to the list. It contains an `element` attribute, which is the value that we want to add to the list, and a `next` attribute, which is the pointer that contains the link to the next node item in the list. The `Node` class is declared in the `models/linked-list-models.js` file (for reuse purposes) and its code is presented as follows:

```
export class Node {  
    constructor(element) {  
        this.element = element;  
        this.next = undefined;  
    }  
}
```

Then, we have the methods of the `LinkedList` class. Let's see what each method will be responsible for before we implement each one:

- `push(element)`: This method adds a new element to the end of the list.
- `insert(element, position)`: This method inserts a new element at a specified position in the list.
- `getElementAt(index)`: This method returns the element of a specific position in the list. If the element does not exist in the list, it returns `undefined`.
- `remove(element)`: This method removes an element from the list.
- `indexOf(element)`: This method returns the index of the element in the list. If the element does not exist in the list, it returns `-1`.
- `removeAt(position)`: This method removes an item from a specified position in the list.
- `isEmpty()`: This method returns `true` if the linked list does not contain any elements, and `false` if the size of the linked list is bigger than `0`.
- `size()`: This method returns the number of elements the linked list contains. It is similar to the `length` property of the array.
- `toString()`: This method returns a string representation of the linked list. As the list uses a `Node` class as an element, we need to overwrite the default `toString` method inherited from the JavaScript `Object` class to output only the element values.

Pushing elements to the end of the linked list

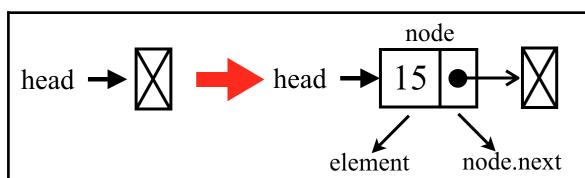
When adding an element at the end of a `LinkedList` object, there can be two scenarios: one where the list is empty and we are adding its first element, or one where the list is not empty and we are appending elements to it.

The following is the implementation of the `push` method:

```
push(element) {
  const node = new Node(element); // {1}
  let current; // {2}
  if (this.head == null) { // {3}
    this.head = node;
  } else {
    current = this.head; // {4}
    while (current.next != null) { // {5} get last item
      current = current.next;
    }
    // and assign next to new element to make the link
    current.next = node; // {6}
  }
  this.count++; // {7}
}
```

The first thing we need to do is create a new `Node` passing `element` as its value ({1}).

Let's implement the first scenario: adding an element when the list is empty. When we create a `LinkedList` object, the `head` will point to `undefined` (or it could be `null` as well):



If the `head` element is `undefined` or `null` (the list is empty {3}), it means we are adding the first element to the list. So, all we have to do is assign the `node` to the `head`. The next node element will be `undefined` automatically.



The last node from the list always has an `undefined` or `null` value as the next element.

So, we have covered the first scenario. Let's go to the second one, which is adding an element to the end of the list when it is not empty.

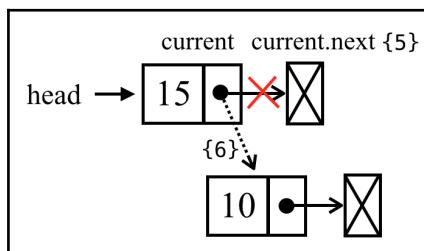
To add an element to the end of the list, we first need to find the last element. Remember that we only have a reference to the first element (`{4}`), so we need to iterate through the list until we find the last item. To do so, we need a variable that points to the current item of the list (`{2}`).

When looping through the list, we know we have reached its end when the `current.next` pointer is `undefined` or `null` (`{5}`). Then, all we have to do is link the `current` element's (which is the last one) `next` pointer to the node we want to add to the list (line `{6}`).



`this.head == null` (`{3}`) is equivalent to `(this.head === undefined || head === null)`, and `current.next != null` (`{5}`) is equivalent to `(current.next !== undefined && current.next !== null)`. For more information about JavaScript `==` and `===` equal operators, please refer to Chapter 1, *JavaScript – A Quick Overview*.

The following diagram exemplifies pushing an element to the end of a linked list when it is not empty:



When we create a `Node` instance, its `next` pointer will always be `undefined`. We are OK with this because we know that it is going to be the last item on the list.

And finally, we cannot forget to increment the size of the list so that we can control it and easily get the list size (`{7}`).

We can use and test the data structure we have created so far with the following code:

```
const list = new LinkedList();
list.push(15);
list.push(10);
```

Removing elements from the linked list from a specific position

Now, let's see how we can remove elements from the `LinkedList`. We are going to implement two methods: the first one removes an element from a specified position (`removeAt`), and the second one is based on the element value (we will present the `remove` method later). As in the case of the `push` method, there are two scenarios when removing elements from the linked list. The first scenario is removing the first element, and the second one is removing any element but the first one.

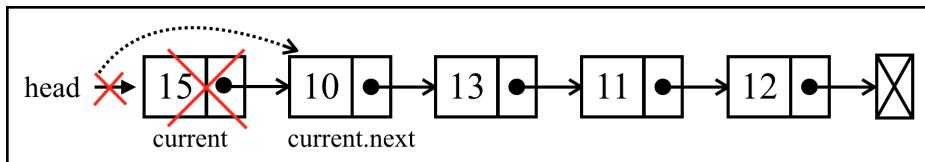
The `removeAt` code is presented as follows:

```
removeAt(index) {
    // check for out-of-bounds values
    if (index >= 0 && index < this.count) { // {1}
        let current = this.head; // {2}

        //removing first item
        if (index === 0) { // {3}
            this.head = current.next;
        } else {
            let previous; // {4}
            for (let i = 0; i < index; i++) { // {5}
                previous = current; // {6}
                current = current.next; // {7}
            }
            // link previous with current's next: skip it to remove
            previous.next = current.next; // {8}
        }
        this.count--; // {9}
        return current.element;
    }
    return undefined; // {10}
}
```

We will delve into this code step by step. As the method is going to receive the `index` (position) of the node that needs to be removed, we need to verify whether the `index` is valid ({1}). A valid position would be from `index 0` (included) to the size of the list (`count - 1`, as the `index` starts from zero). If it is not a valid position, we return `undefined` ({10}), meaning no element was removed from the list.

Let's write the code for the first scenario—we want to remove the first element from the list (`index === 0- {3}`). The following diagram exemplifies this action:



So, if we want to remove the first element, all we have to do is point `head` to the second element of the list. We will make a reference to the first element of the list using the `current` variable ({2}); we will also use this to iterate the list, but we will get there in a minute). So, the `current` variable is a reference to the first element of the list. If we assign `head` to `current.next`, we will be removing the first element. We could also assign `head` to `head.next` directly (without using the `current` variable as an alternative).

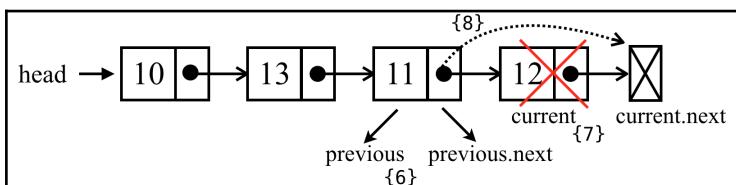
Now, let's say we want to remove the last item of the list, or an item from the middle of the list. To do so, we need to iterate through the nodes of the linked list until we get to the desired position ({5}). An important detail: the `current` variable will always make a reference to the current element of the list that we are looping through ({7}). We also need to make a reference to the element that comes before the `current` ({6}); we will name it `previous` ({4}).

After we iterate to the desired position, the `current` variable will hold the node we want to remove from the linked list. So, to remove the `current` node, all we have to do is link `previous.next` with `current.next` ({8}). This way, the `current` node will be lost in the computer memory and will be available for cleaning by the garbage collector.



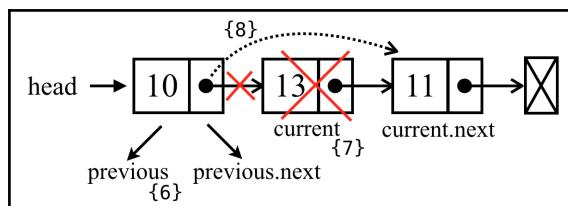
To better understand how the JavaScript garbage collector works, please read https://developer.mozilla.org/en-US/docs/Web/JavaScript/Memory_Management.

Let's try to understand this code with some diagrams. Suppose we want to remove the last element:



In the case of the last element, when we get off the loop in line {8}, the `current` variable will be a reference to the last node of the list (the one we want to remove). The `current.next` value will be `undefined` (because it is the last node). As we also keep a reference to the previous node (one node before the current one), `previous.next` will point to `current`, so to remove `current` all we have to do is change the value of `previous.next` to `current.next`.

Now, let's see whether the same logic applies to an element from the middle of the list:



The `current` variable is a reference to the node that we want to remove. The `previous` variable is a reference to the node that comes before the element we want to remove; thus, to remove the `current` node, all we need to do is link `previous.next` to `current.next`, and so our logic works for both cases.

Looping through the list until we get to the desired position

In the `remove` method, we need to loop through the list until we get to the desired `index` (position). The code snippet to loop until the desired `index` is common in the `LinkedList` class methods. For this reason, we can refactor the code and extract the logic to a separate method so we can reuse it in different places. So, let's create the `getElementAt` method:

```
getElementAt(index) {
  if (index >= 0 && index <= this.count) { // {1}
    let node = this.head; // {2}
    for (let i = 0; i < index && node != null; i++) { // {3}
      node = node.next;
    }
    return node; // {4}
  }
  return undefined; // {5}
}
```

Just to make sure we will loop through the list until we find a valid position, we need to verify whether the `index` passed as a parameter is a valid position (`{1}`). If an invalid position is passed as a parameter, we return `undefined`, since the position does not exist in the `LinkedList` (`{5}`). Next, we will initialize the variable `node` that will iterate through the list with the first element, which is the `head` (`{2}`). You can also rename the variable `node` to `current` if you want to keep the same pattern as the other methods of the `LinkedList` class.

Next, we will loop through the list until the desired `index` (`{3}`). When we get out of the loop, the `node` element (`{4}`) will be referencing the element at the `index` position. You can also use `i = 1; i <= index` in the for loop to achieve the same result.

Refactoring the remove method

We can refactor the `remove` method and use the `getElementAt` method that has been created. To do so, we can replace lines `{4}` to `{8}` as follows:

```
if (index === 0) {  
    // logic for first position  
} else {  
    const previous = this.getElementAt(index - 1);  
    current = previous.next;  
    previous.next = current.next;  
}  
this.count--; // {9}
```

Inserting an element at any position

Next, we are going to implement the `insert` method. This method provides you with the capability to insert an element at any position. Let's take a look at its implementation:

```
insert(element, index) {  
    if (index >= 0 && index <= this.count) { // {1}  
        const node = new Node(element);  
        if (index === 0) { // add on first position  
            const current = this.head;  
            node.next = current; // {2}  
            this.head = node;  
        } else {  
            const previous = this.getElementAt(index - 1); // {3}  
            const current = previous.next; // {4}  
            node.next = current; // {5}  
            previous.next = node; // {6}
```

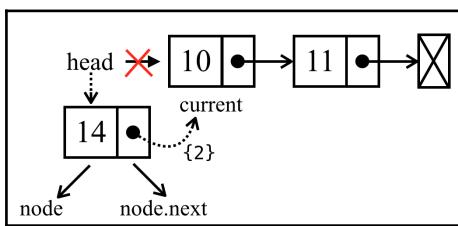
```

    }
    this.count++; // update size of list
    return true;
}
return false; // {7}
}

```

As we are handling positions (indexes), we need to check the out-of-bound values ({1}), just like we did in the `remove` method. If it is out-of-bounds, we return the value `false` to indicate that no item was added to the list ({7}).

If the position is valid, we are going to handle the different scenarios. The first scenario is the case where we need to add an element at the beginning of the list, meaning the *first position*. The following diagram exemplifies this scenario:

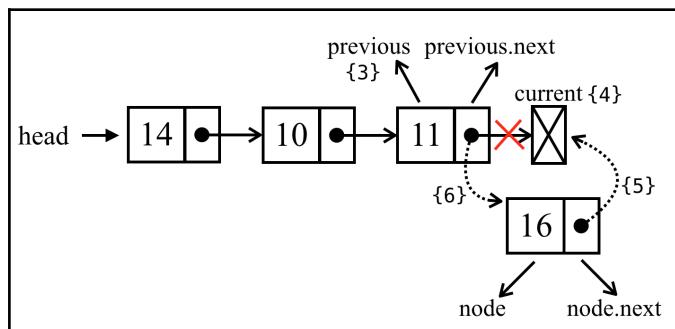


In the preceding diagram, we have the `current` variable making a reference to the first element of the list. What we need to do is set the value `node.next` to `current` (the first element of the list or simply to `head` directly). Now, we have `head` and also `node.next` pointing to `current`. Next, all we have to do is change the `head` reference to `node` ({2}), and we have a new element in the list.

Now, let's handle the second scenario: adding an element in the middle or at the end of the list. First, we need to loop through the list until we reach the desired position ({3}). In this case, we will loop to `index - 1`, meaning one position before where we desire to insert the new node.

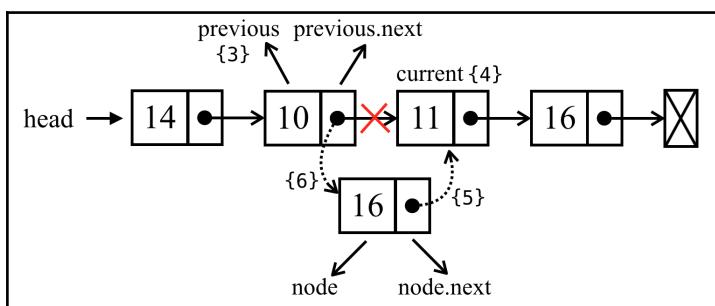
When we get out of the loop, the `previous` variable will be a reference to an element before the `index` where we would like to insert the new element, and the `current` variable ({4}) will be a reference to an element present after the position where we would like to insert the new element. In this case, we want to add the new item between `previous` and `current`. So, first we need to make a link between the new (`node`) and the `current` ({5}), and then we need to change the link between `previous` and `current`. We need `previous.next` to point to `node` ({6}) instead of `current`.

Let's see the code in action using a diagram:



If we try to add a new element to the last position, `previous` will be a reference to the last item of the list and `current` will be `undefined`. In this case, `node.next` will point to `current`, `previous.next` will point to `node`, and we have a new element in the list.

Now, let's see how we can add a new element in the middle of the list with the help of the following diagram:



In this case, we are trying to insert the new element (`node`) between the `previous` and `current` elements. First, we need to set the value of the `node.next` pointer to `current`. Then, we need to set the value of `previous.next` to `node`. Finally, we have a new element in the list!



It is very important to have variables referencing the nodes we need to control so that we do not lose the link between the nodes. We could work with only one variable (`previous`), but it would be harder to control the links between the nodes. For this reason, it is better to declare an extra variable to help us with these references.

The `indexOf` method: returning the position of an element

The next method that we will implement is the `indexOf` method. The `indexOf` method receives the value of an element and returns the position of this element if it is found. Otherwise, it returns `-1`.

Let's take a look at its implementation:

```
indexOf(element) {  
    let current = this.head; // {1}  
    for (let i = 0; i < this.count && current != null; i++) { // {2}  
        if (this.equalsFn(element, current.element)) { // {3}  
            return i; // {4}  
        }  
        current = current.next; // {5}  
    }  
    return -1; // {6}  
}
```

As always, we need a variable that will help us iterate through the list; this variable is `current`, and its first value is the `head` ({1}).

Next, we iterate through the elements ({2}), starting from the `head` (index 0) until the list size (the `count` variable) is reached. Just to make sure, we can verify whether the `current` variable is `null` or `undefined` to avoid runtime errors as well.

In each iteration, we will verify whether the element we are looking for is the element in the `current` node ({3}). In this case, we will use the `equals` function that we passed to the `LinkedList` class constructor. The default value of `equalFn` is presented as follows:

```
function defaultEquals(a, b) {  
    return a === b;  
}
```

So it would be the same as using `element === current.element` at line {3}. However, if the element is a complex object, we allow the developer to pass a customized function to the `LinkedList` to compare the elements.

If the element we are looking for is the element of `current`, we return its position ({4}). If not, we iterate to the next node of the list ({5}).

The loop will not be executed if the list is empty, or if we reach the end of the list. If we do not find the value, we return `-1` ({6}).

Removing an element from the linked list

With the `indexOf` method created, we can implement other methods such as the `remove` method:

```
remove(element) {
    const index = this.indexOf(element);
    return this.removeAt(index);
}
```

We have already written a method that removes an element at a given position (`removeAt`). Now that we have the `indexOf` method, if we pass the element's value we can find its position and call the `removeAt` method, passing the position that we found. It is very simple, and it is also easier if we need to change the code from the `removeAt` method—it will be changed for both methods (this is what's nice about reusing code). This way, we do not need to maintain two methods to remove an item from the list—we need only one! Also, the bounds constraints will be checked by the `removeAt` method as well.

The `isEmpty`, `size`, and `getHead` methods

The `isEmpty` and `size` methods are the same as the ones we implemented for the classes we created in previous chapters. Let's take a look at them anyway:

```
size() {
    return this.count;
}
```

The `size` method returns the number of elements of the list. Unlike the classes we implemented in earlier chapters, the `length` variable of the list is controlled internally, since `LinkedList` is a class built from scratch.

The `isEmpty` method returns `true` if there is no element in the list, and `false` otherwise. Its code is presented as follows:

```
isEmpty() {
    return this.size() === 0;
}
```

And finally, we have the `getHead` method:

```
getHead() {
    return this.head;
}
```

The `head` variable is a *private* variable from the `LinkedList` class (as we learned, JavaScript does not support real private properties yet, but for our learning purposes we are considering instance properties as private, since the developers that will use our classes are supposed to only access the classes, methods). So, if we need to iterate the list outside the class implementation, we can provide a method to get the first element of the class.

The `toString` method

The `toString` method converts the `LinkedList` object into a string. The following is the implementation of the `toString` method:

```
toString() {
    if (this.head == null) { // {1}
        return '';
    }
    let objString = `${this.head.element}`; // {2}
    let current = this.head.next; // {3}
    for (let i = 1; i < this.size() && current != null; i++) { // {4}
        objString = `${objString},${current.element}`;
        current = current.next;
    }
    return objString; // {5}
}
```

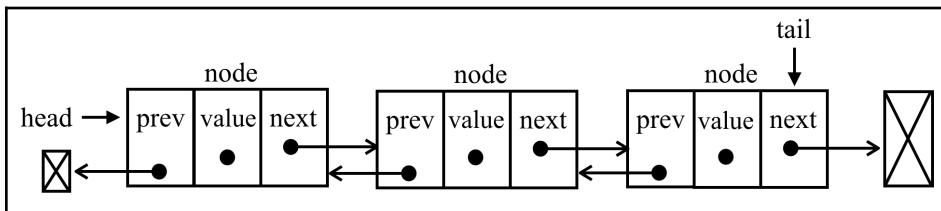
First, if the list is empty (`head` will be `null` or `undefined`), we return an empty string ({1}). We can also use `if (this.isEmpty())` for this verification.

If the list is not empty, we will initialize the string that will be returned at the end of the method (`objString`) with the first element's value ({2}). Next, we will iterate through all the other elements of the list ({4}), adding the values to our string. If the list has only one element, the `current != null` validation will fail because the `current` variable will have a value of `undefined` (or `null`), so the algorithm will not add any other values to `objString`.

Finally, we return the string with the list's content ({5}).

Doubly linked lists

There are different types of linked list. In this section, we are going to cover the **doubly linked list**. The difference between a doubly linked list and a normal linked list is that in a linked list we make the link from one node to the next one only, while in a doubly linked list, we have a double link: one for the next element and one for the previous element, as shown in the following diagram:



Let's get started with the changes that are needed to implement the `DoublyLinkedList` class:

```

class DoublyNode extends Node { // {1}
  constructor(element, next, prev) {
    super(element, next); // {2}
    this.prev = prev; // {3} NEW
  }
}

class DoublyLinkedList extends LinkedList { // {4}
  constructor>equalsFn = defaultEquals) {
    super>equalsFn); // {5}
    this.tail = undefined; // {6} NEW
  }
}
  
```

As the `DoublyLinkedList` class is a special type of `LinkedList`, we will extend the `LinkedList` class ({4}). This means the `DoublyLinkedList` class will inherit (will have access to) all the properties and methods from the `LinkedList` class. So to get started, in the `DoublyLinkedList` constructor, we need to evoke ({5}) the `LinkedList` constructor, which will initialize the `equalsFn`, `count`, and `head` properties. In addition, we will also need to keep the reference to the last element of the list (`tail - {6}`).

The doubly linked list provides us with two ways to iterate the list: from the beginning to its end or vice versa. We can also go to the next element or the previous element of a particular node. Because of this behavior, for each node we will need to track its previous node as well. So in addition to the `element` and the `next` properties from the `Node` class, the `DoublyLinkedList` will use a special node called `DoublyNode` with a property named `prev` ({3}). The `DoublyNode` extends the `Node` class so we can inherit the `element` and `next` properties ({1}). Because we are also using inheritance, we also need to evoke the `Node` constructor inside the `DoublyNode` class constructor ({2}).

In the singly linked list, when you are iterating the list and you miss the desired element, you need to go back to the beginning of the list and start iterating it again. This is one of the advantages of the doubly linked list.



As we can see in the preceding code, the differences between the `LinkedList` class and the `DoublyLinkedList` class are marked by NEW.

Inserting a new element at any position

Inserting a new element in a doubly linked list is very similar to a linked list. The difference is that in the linked list, we only control one pointer (`next`), and in the doubly linked list we have to control both the `next` and `prev` (previous) properties. For the `DoublyLinkedList` class, we will overwrite the `insert` method, meaning we will apply a different behavior than the one from the `LinkedList` class.

Here, we have the algorithm to insert a new element at any position:

```
insert(element, index) {
  if (index >= 0 && index <= this.count) {
    const node = new DoublyNode(element);
    let current = this.head;
    if (index === 0) {
      if (this.head == null) { // {1} NEW
        this.head = node;
        this.tail = node;
      } else {
        node.next = this.head; // {2}
        current.prev = node; // {3} NEW
        this.head = node; // {4}
      }
    } else if (index === this.count) { // last item NEW
      current = this.tail; // {5}
    }
  }
}
```

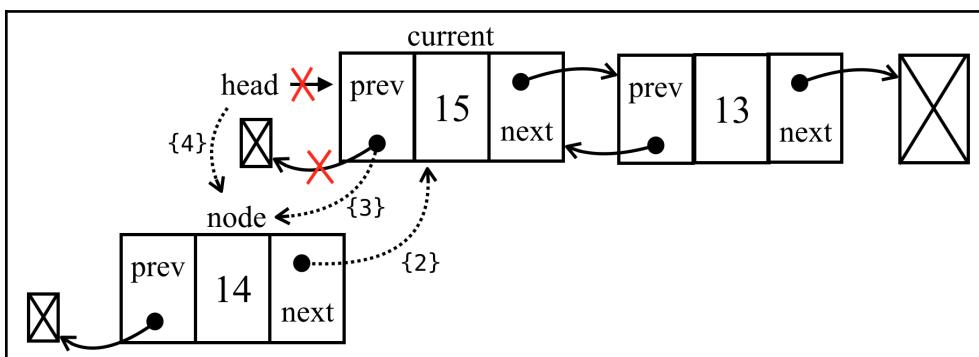
```

        current.next = node; // {6}
        node.prev = current; // {7}
        this.tail = node; // {8}
    } else {
        const previous = this.getElementAt(index - 1); // {9}
        current = previous.next; // {10}
        node.next = current; // {11}
        previous.next = node; // {12}
        current.prev = node; // {13} NEW
        node.prev = previous; // {14} NEW
    }
    this.count++;
    return true;
}
return false;
}

```

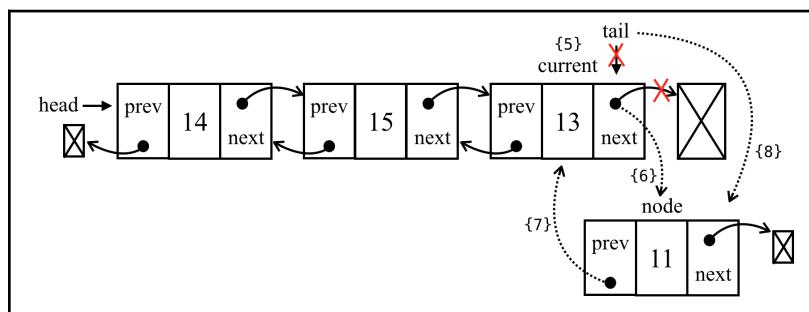
Let's analyze the first scenario: insert a new element at the first position in the list (the beginning of the list). If the list is empty ({1}), we simply need to point `head` and `tail` to the new node. If not, the `current` variable will be a reference to the first element of the list. As we did for the linked list, we set `node.next` to `current` ({2}) and `head` will point to the `node` ({4}) - it will be the first element of the list). The difference now is that we also need to set a value for the previous pointer of the elements. The `current.prev` pointer will point to the new element (`node`—{3}) instead of `undefined`. Since the `node.prev` pointer is already `undefined`, we do not need to update anything.

The following diagram demonstrates this process:

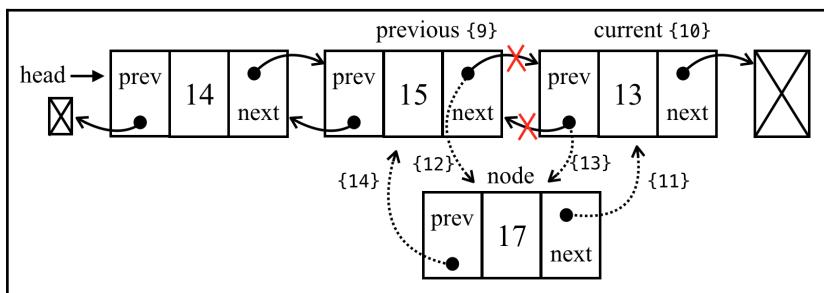


Now, let's analyze another scenario: suppose we want to add a new element as the last element of the list. As we are also controlling the pointer to the last element, this is a special case. The `current` variable will reference the last element (`{5}`). Then, we start making the links: the `current.next` pointer (which points to `undefined`) will point to node (`{6}`): `node.next` will be pointing to `undefined` already because of the constructor). The `node.prev` pointer will reference `current` (`{7}`). Then, there is only one thing left to be done, and that is updating `tail`, which will point to `node` instead of `current` (`{8}`).

The following diagram demonstrates all of these actions:



Then, we have the third scenario: inserting a new element in the middle of the list. As we did for the previous methods, we will iterate the list until we get to the desired position (`{9}`). The `getElementAt` method is inherited from the `LinkedList` class and we do not need to overwrite its behavior. We will insert the new element between the `current` (`{10}`) and `previous` elements. First, `node.next` will point to `current` (`{11}`), and `previous.next` will point to `node` (`{12}`) so that we do not lose the link between the nodes. Then, we need to fix all the links: `current.prev` will point to `node` (`{13}`) and `node.prev` will point to `previous` (`{14}`). The following diagram exemplifies this process:





We can make some improvements in both the methods that we implemented: `insert` and `remove`. In the case of a negative result, we could insert elements at the end of the list. There is also a performance improvement: for example, if `position` is greater than `length/2`, it is best to iterate from the end than start from the beginning (by doing so, we will have to iterate fewer elements from the list).

Removing elements from any position

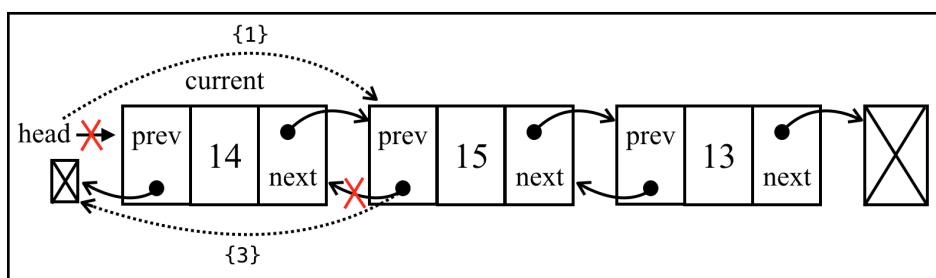
Removing elements from a doubly linked list is also very similar to a linked list. The only difference is that we need to set the previous pointer as well. Let's take a look at the implementation:

```
removeAt(index) {
    if (index >= 0 && index < this.count) {
        let current = this.head;
        if (index === 0) {
            this.head = current.next; // {1}
            // if there is only one item, then we update tail as well NEW
            if (this.count === 1) { // {2}
                this.tail = undefined;
            } else {
                this.head.prev = undefined; // {3}
            }
        } else if (index === this.count - 1) { // last item NEW
            current = this.tail; // {4}
            this.tail = current.prev; // {5}
            this.tail.next = undefined; // {6}
        } else {
            current = this.getElementAt(index); // {7}
            const previous = current.prev; // {8}
            // link previous with current's next - skip it to remove
            previous.next = current.next; // {9}
            current.next.prev = previous; // {10} NEW
        }
        this.count--;
        return current.element;
    }
    return undefined;
}
```

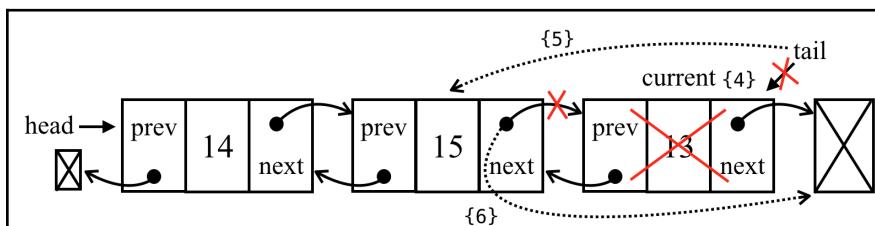
We need to handle three scenarios: removing an element from the beginning of the list, removing an element from the middle of the list, and removing the last element.

Let's take a look at how to remove the first element. The `current` variable is a reference to the first element of the list, the one we want to remove. All we need to do is change the reference from `head`; instead of `current`, it will be the next element (`current.next - {1}`). However, we also need to update the `current.next` previous pointer (as the first element `prev` pointer is a reference to `undefined`), so we change the reference of `head.prev` to `undefined` (`{3}`)—as `head` also points to the new first element of the list; or we can also use `current.next.prev`. As we also need to control the `tail` reference, we can check whether the element we are trying to remove is the first one, and if it's positive, all we need to do is set `tail` to `undefined` as well (`{2}`).

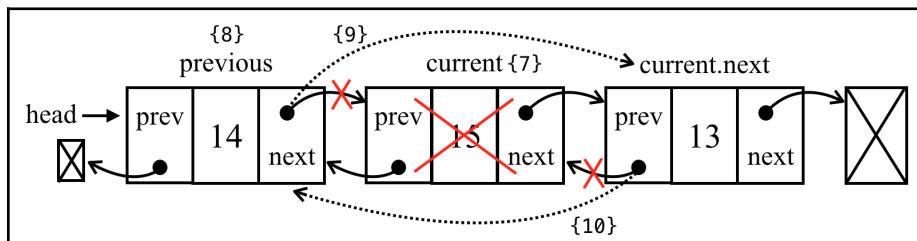
The following diagram illustrates the removal of the first element from a doubly linked list:



The following scenario removes an element from the last position. As we have the reference to the last element already (`tail`), we do not need to iterate the list to get to it, so we can assign the `tail` reference to the `current` variable as well (line `{4}`). Next, we need to update the `tail` reference to the second-last element of the list (`{5}`) - `current.prev` or `tail.prev` works as well). Now that `tail` is pointing to the second-last element, all we need to do is update the `next` pointer to `undefined` (`{6}`) - `tail.next = undefined`). The following diagram demonstrates this action:



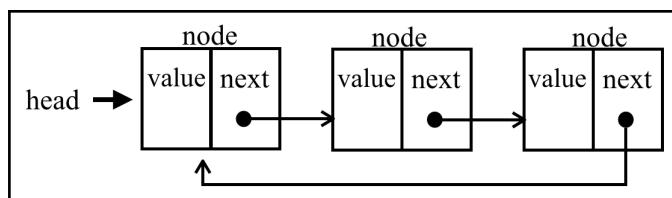
The third and final scenario removes an element from the middle of the list. First, we need to iterate until we get to the desired position (`{7}`). The element we want to remove will be referenced by the `current` variable (`{7}`). So, to remove it, we can skip it in the list by updating the references of `previous.next` and `current.next.prev`. So, `previous.next` will point to `current.next` (`{9}`), and `current.next.prev` will point to `previous` (`{10}`), as demonstrated by the following diagram:



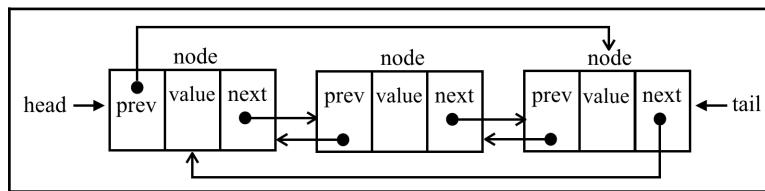
To check the implementation of other methods of the doubly linked list, refer to the source code of the book. The download link of the source code is mentioned in the *Preface* of the book, and it can also be accessed at: <http://github.com/loiane/javascript-datastructures-algorithms>.

Circular linked lists

A **circular linked list** can have only one reference direction (as with a linked list) or a double reference (as with a doubly linked list). The only difference between a circular linked list and a linked list is that the last element's `next` (`tail.next`) pointer does not make a reference to `undefined`, but to the first element (`head`), as we can see in the following diagram:



A **doubly circular linked list** has `tail.next` pointing to the `head` element, and `head.prev` pointing to the `tail` element:



Let's check the code to create the `CircularLinkedList` class:

```
CircularLinkedList extends LinkedList {
    constructor>equalsFn = defaultEquals) {
        super>equalsFn);
    }
}
```

The `CircularLinkedList` class does not need any additional properties, so we can simply extend the `LinkedList` class and overwrite the required methods to apply the special behavior.

We will overwrite the implementation of the `insert` and `removeAt` methods in the following topics.

Inserting a new element at any position

The logic to insert an element in a circular linked list is the same as to insert an element in a normal linked list. The difference in the circular linked list is that we also need to link the last node's `next` reference to the `head` node. The following is the `insert` method for the `CircularLinkedList` class:

```
insert(element, index) {
    if (index >= 0 && index <= this.count) {
        const node = new Node(element);
        let current = this.head;
        if (index === 0) {
            if (this.head == null) {
                this.head = node; // {1}
                node.next = this.head; // {2} NEW
            } else {
                node.next = current; // {3}
                current = this.getElementAt(this.size()); // {4}
            }
        } else {
            let prev = this.getElementAt(index - 1);
            node.next = current;
            prev.next = node;
        }
    }
}
```

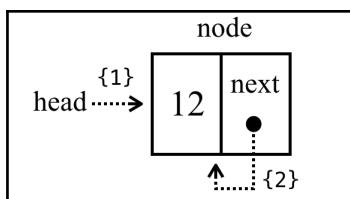
```

        // update last element
        this.head = node; // {5}
        current.next = this.head; // {6} NEW
    }
} else { // no changes in this scenario
    const previous = this.getElementAt(index - 1);
    node.next = previous.next;
    previous.next = node;
}
this.count++;
return true;
}
return false;
}

```

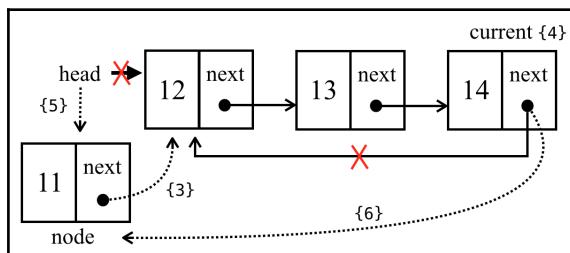
Let's break down the different scenarios. The first one is when we want to insert a new element in the first position of the list. If the list is empty, we assign the `head` node to the new element created ({1}), as we did in the `LinkedList` class, and we also need to link the last node to the head ({2}). In this case, the last element of the list is the node we created that will point to itself, because it is also the head.

The following diagram exemplifies the first scenario:



The second scenario is inserting an element in the first position in a non-empty list, so the first thing we need to do is assign `node.next` to the `head` reference (`current` variable). This is the logic we used in the `LinkedList` class. However, in the `CircularLinkedList`, we still need to make the last node of the list point to the new head element, so we need to get the reference to the last element. To do so, we will use the `get ElementType` method, passing the list size as a parameter ({2}). We update the `head` element to the new element and we link the last node (`current`) to the new head ({3}).

The following diagram exemplifies the second scenario:



If we want to insert a new element in the middle of the list, the code is the same as the `LinkedList` class since no changes will be applied to the last or first nodes of the list.

Removing elements from any position

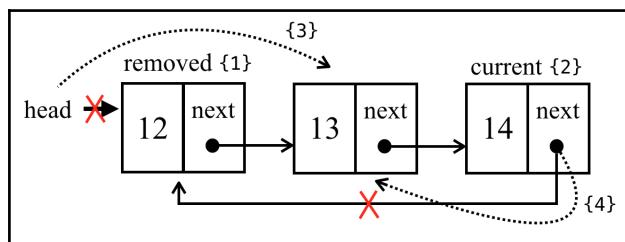
To remove an element from a circular linked list, we only need to worry about the second scenario, which changes the `head` element of the list. The code for the `removeAt` method is presented as follows:

```
removeAt(index) {
    if (index >= 0 && index < this.count) {
        let current = this.head;
        if (index === 0) {
            if (this.size() === 1) {
                this.head = undefined;
            } else {
                const removed = this.head; // {1}
                current = this.getElementAt(this.size()); // {2} NEW
                this.head = this.head.next; // {3}
                current.next = this.head; // {4}
                current = removed; // {5}
            }
        } else {
            // no need to update last element for circular list
            const previous = this.getElementAt(index - 1);
            current = previous.next;
            previous.next = current.next;
        }
        this.count--;
        return current.element; // {6}
    }
    return undefined;
}
```

The first scenario to remove an element is removing the element of the list with a single node. In this case, we simply assign `undefined` to the `head`. There are no changes here when we compare this to the `LinkedList` class.

The second scenario is removing the first element of a non-empty list. As the `head` reference will change, we also need to update the reference to the last node's `next` property; thus, we first keep a reference to the current `head` element, which is going to be removed from the list (`{1}`). As we did in the insert method, we also need to get the reference to the last node of the list (`{2}`), which will be stored in the `current` variable. After we have a reference to all the required nodes, we can start making the new links. We update the `head` element, linking the `head` to the second element (`head.next - {3}`), and then we link the last element (`current.next`) to the new `head` (`{4}`). We can update the reference of the `current` variable (`{5}`) so that we can return its value (`{6}`) for information purposes.

The following diagram exemplifies these actions:



Sorted linked lists

A **sorted linked list** is a list that keeps its elements sorted. To keep all elements sorted, instead of applying a sorting algorithm, we will insert the element at its correct position so as to keep the list always sorted.

Let's start by declaring the `SortedLinkedList` class:

```
const Compare = {
    LESS_THAN: -1,
    BIGGER_THAN: 1
};

function defaultCompare(a, b) {
    if (a === b) { // {1}
        return 0;
    }
    else if (a < b) { // {2}
        return -1;
    }
    else { // {3}
        return 1;
    }
}

function compare(a, b, compareFn) {
    if (compareFn === undefined) {
        compareFn = defaultCompare;
    }
    const result = compareFn(a, b);
    if (result === 0) {
        return 0;
    }
    else if (result === -1) {
        return -1;
    }
    else if (result === 1) {
        return 1;
    }
    else {
        throw new Error('Unknown result');
    }
}
```

```

        }
        return a < b ? Compare.LESS_THAN : Compare.BIGGER_THAN; // {2}
    }

    class SortedLinkedList extends LinkedList {
        constructor>equalsFn = defaultEquals, compareFn = defaultCompare) {
            super>equalsFn);
            this.compareFn = compareFn; // {3}
        }
    }
}

```

The `SortedLinkedList` class will inherit all the properties and methods from the `LinkedList` class, but since this class has a special behavior, we will need a function to compare the elements. For this reason, we also need to declare `compareFn ({3})`, which will be used to compare the elements. This function will use the `defaultCompare` function by default. If the elements have the same reference, it returns 0 ({1}). If the first element is less than the second element, it returns -1 and 1 otherwise. To keep the code more elegant, we can declare a constant `Compare` to represent each of these values. If the element that is being compared is more complex, we can create a custom comparison function and pass it to the `SortedLinkedList` class constructor as well.

Inserting elements in order

We will overwrite the `insert` method with the code presented as follows:

```

insert(element, index = 0) { // {1}
    if (this.isEmpty()) {
        return super.insert(element, 0); // {2}
    }
    const pos = this.getIndexNextSortedElement(element); // {3}
    return super.insert(element, pos); // {4}
}

getIndexNextSortedElement(element) {
    let current = this.head;
    let i = 0;
    for (; i < this.size() && current; i++) {
        const comp = this.compareFn(element, current.element); // {5}
        if (comp === Compare.LESS_THAN) { // {6}
            return i;
        }
        current = current.next;
    }
    return i; // {7}
}

```

```
}
```

As we do not want to allow inserting elements at any index, we will start assigning a default value to the `index` parameter (`{1}`), so we can simply evoke `list.insert(myElement)` without the need to pass the `index` parameter. If the `index` parameter is passed to the method, its value is going to be ignored as the position to insert the element will be controlled internally. The reason why we need to do it this way is that we do not want to rewrite the entire `LinkedList` class methods again, so we are only overwriting the `insert` method's behavior. If you want to, you can create a `SortedLinkedList` class from scratch, copying all the code from the `LinkedList` class however, this will make maintaining the code a little bit more difficult since we will need to make the changes in two classes instead of only one.

If the list is empty, we can simply evoke the `LinkedList insert` method passing 0 (zero) as the `index` (`{2}`). If the list is not empty, we will get what's known as the correct `index` to insert the `element` (`{3}`) and evoke the `LinkedList insert` method, passing the position in order to keep the list sorted (`{4}`).

To retrieve the correct index to insert the `element`, we will create a new method called `getIndexNextSortedElement`. Inside this method, we will iterate through the list until we find a position to insert the `element` or until all the elements have been iterated. In this last scenario, the `index` returned (`{7}`) will be the `size` of the list (the `element` will be inserted at the end of the list). To compare the elements, we will use `compareFn` (`{5}`), passed to the class constructor. When the `element` we want to insert in the list is less than the `element` of the current list, we have found the position to insert (`{6}`).

And that's it! We can reuse the `LinkedList insert` method internally. All the other methods such as `remove`, `indexOf`, and on are the same as the `LinkedList`.

Creating the StackLinkedList class

We can also use the `LinkedList` class and its variations as internal data structures to create other data structures such as `stack`, `queue`, and `deque`. In this topic, we will learn how to create the `stack` data structure (covered in Chapter 4, *Stacks*).

The `StackLinkedList` class structure and the methods `push` and `pop` are declared as follows:

```
class StackLinkedList {
    constructor() {
        this.items = new DoublyLinkedList(); // {1}
    }
    push(element) {
        this.items.push(element); // {2}
    }
    pop() {
        if (this.isEmpty()) {
            return undefined;
        }
        return this.items.removeAt(this.size() - 1); // {3}
    }
}
```

For the `StackLinkedList` class, instead of using an array or a JavaScript object to store the `items`, we will use a `DoublyLinkedList` ({1}). The reason for using the doubly linked list instead of the linked list is that for the stack, we will be inserting elements at the end of the list ({2}) and also removing elements from the end of the list ({3}). Our `DoublyLinkedList` class keeps a reference of the last `element` of the list (`tail`), so it does not need to iterate throughout all the list elements to access it; it has direct access to the first and last elements, decreasing the processing effort, and keeping the cost at **O(1)**, which is our original `Stack` implementation.



We could also enhance the `LinkedList` class, keeping a reference to the `tail` element and using the enhanced version instead of the `DoublyLinkedList`.

We can inspect the code for the other `Stack` methods as follows:

```
peek() {
    if (this.isEmpty()) {
        return undefined;
    }
    return this.items.getElementAt(this.size() - 1).element;
}
isEmpty() {
    return this.items.isEmpty();
}
size() {
    return this.items.size();
```

```
    }
    clear() {
        this.items.clear();
    }
    toString() {
        return this.items.toString();
    }
}
```

We are evoking the methods from the `DoublyLinkedList` class for every other method. Using the linked list data structure internally in the stack implementation is easier since we do not need to create the code from scratch with the same processing cost, and it also makes the code easier to read!



We can apply the same logic and create a `Queue` and `Deque` class using the `DoublyLinkedList` or even the `LinkedList` class!

Summary

In this chapter, you learned about the linked list data structure and its variants: the doubly linked list, the circular linked list, and the sorted linked list. You learned how to add and remove elements at any position, and how to iterate through a linked list. You also learned that the most important advantage of a linked list over an array is that you can easily add and remove elements from a linked list without shifting over its elements. So, whenever you need to add and remove lots of elements, the best option will be a linked list instead of an array.

You also learned how to create a stack using an internal linked list to store its elements instead of an array or an object, and you also learned the benefits of using another data structure to leverage its available operations instead of writing all the logic from scratch.

In the next chapter, you will learn about sets, a data structure that stores unique elements.

7 Sets

Sequential data structures such as arrays (lists), stacks, queues, and linked lists should sound familiar to you by now. In this chapter, we will cover a data structure called sets, which is also a sequential data structure that does not allow duplicated values. We will learn how to create a set data structure, add and remove values, and search for whether a value already exists. We will also learn how to perform mathematical operations such as union, intersection, and difference. Finally, we will learn how to use the native **ECMAScript 2015 (ES2015)** Set class.

In this chapter, we will cover:

- Creating a Set class from scratch
- Performing mathematical operations with a Set
- ECMAScript 2015 native Set class

Structuring a dataset

A **set** is a collection of items that are unordered and consists of unique elements (meaning they cannot be repeated). This data structure uses the same mathematical concept as finite sets, but it is applied to a computer science data structure.

Let's take a look at the mathematical concept of sets before we dive into the computer science implementation of it. In mathematics, a set is a collection of distinct objects.

For example, we have a set of natural numbers, which consists of integer numbers greater than or equal to 0—that is, $N = \{0, 1, 2, 3, 4, 5, 6, \dots\}$. The list of the objects within the set is surrounded by {} (curly braces).

There is also the null set concept. A set with no element is called a **null set** or an **empty set**. An example would be a set of prime numbers between 24 and 29. Since there is no prime number (a natural number greater than 1 that has no positive divisors other than 1 and itself) between 24 and 29, the set will be empty. We will represent an empty set with {}.

You can also imagine a set as an array with no repeated elements and no concept of order.

In mathematics, a set also has some basic operations such as union, intersection, and difference. We will also cover these operations in this chapter.

Creating a Set class

ECMAScript 2015 introduced the `Set` class as part of the JavaScript API, and you will learn how to use this later on in this chapter. We will create our own implementation of the `Set` class based on the **ES2015** `Set` class. We will also implement some set operations such as union, intersection, and difference, that are not present in the ES2015 native class.

To get started, the following is the `Set` class declaration with its constructor:

```
class Set {  
    constructor() {  
        this.items = {};  
    }  
}
```

A very important detail here is that we are using an object to represent our set (`items`) instead of an array. However, we could also use an array in this implementation. The approach we will follow in this chapter is very similar to the `items` object approach we used in Chapter 4, *Stacks*, and Chapter 5, *Queues and Deques*. Also, objects in JavaScript do not allow you to have two different properties on the same key, which guarantees unique elements in our set.

Next, we need to declare the methods available for a set (we will try to simulate the same `Set` class implemented in ECMAScript 2015):

- `add(element)`: This adds a new `element` to the set.
- `delete(element)`: This removes the `element` from the set.
- `has(element)`: This returns `true` if the `element` exists in the set and `false` otherwise.

- `clear()`: This removes all the elements from the set.
- `size()`: This returns how many elements the set contains. It is similar to the `length` property of an array.
- `values()`: This returns an array of all the values (elements) of the set.

The `has(element)` method

The first method we will implement is the `has(element)` method. We will implement this method first because it will be used in other methods, such as `add` and `remove`, to verify whether the element already exists in the set. We can take a look at its implementation here:

```
has(element){  
    return element in items;  
};
```

Since we are using an object to store all the elements of the set, we can use JavaScript's `in` operator to verify that the given element is a property of the `items` object.

However, there is a better way of implementing this method, which is as follows:

```
has(element) {  
    return Object.prototype.hasOwnProperty.call(this.items, element);  
}
```

The `Object` prototype has the `hasOwnProperty` method. This method returns a boolean indicating whether the object has the specified property directly in the object or not, while the `in` operator returns a boolean indicating whether the object has the specified property in the object chain.



We could also use `this.items.hasOwnProperty(element)` in our code. However, some lint tools such as **ESLint** (<https://eslint.org>) throw an error when trying to use this code. The error is because not all objects inherit from `Object.prototype` and even for objects which inherit from `Object.prototype`, the `hasOwnProperty` method could be shadowed by something else and the code may not work. To avoid any issues, it is safer to use the `Object.prototype.hasOwnProperty.call`.

The add method

The next method we will implement is the `add` method, as follows:

```
add(element) {  
    if (!this.has(element)) {  
        this.items[element] = element; // {1}  
        return true;  
    }  
    return false;  
}
```

Given an `element`, we can check whether the `element` already exists in the set. If not, we add the `element` to the set ({1}) and return `true` to indicate that the `element` was added. If the `element` already exists in the set, we simply return `false` to indicate that the `element` was not added.



We are adding the `element` as the key and value because it will help us search for the `element` if we store it as the key as well.

The delete and clear methods

Next, we will implement the `delete` method:

```
delete(element) {  
    if (this.has(element)) {  
        delete this.items[element]; // {1}  
        return true;  
    }  
    return false;  
}
```

In the `delete` method, we will verify whether the given `element` exists in the set. If `this` is positive, we will remove the `element` from the set ({1}) and return `true` to indicate that the `element` was removed; otherwise, we will return `false`.

Since we are using an object to store the `items` object of the set, we can simply use the `delete` operator to remove the property from the `items` object ({1}).

To use the `Set` class, we can use the following code as an example:

```
const set = new Set();
set.add(1);
set.add(2);
```

Just out of curiosity, if we output the `this.items` property on the console (`console.log`) after executing the previous code, this will be the output in Google Chrome:

```
Object {1: 1, 2: 2}
```



We can note that this is an object with two properties. The property name is the value we added to the set and its value, as well.

If we want to remove all the elements from the set, we can use the `clear` method, as follows:

```
clear() {
  this.items = {};
}
```

All we need to do to reset the `items` object is assign it to an empty object again (`{}`). We could also iterate the set and remove all the elements one by one using the `remove` method, but this is too much work, as we have an easier way of doing it.

The size method

The next method we will implement is the `size` method (which returns how many elements are in the set). There are three ways of implementing this method.

The first method is to use a `length` variable and control it whenever we use the `add` or `remove` method, as we used in the `LinkedList`, `Stack`, and `Queue` classes in the previous chapters.

In the second method, we use a built-in method from the `Object` class in JavaScript (ECMAScript 2015+), as follows:

```
size() {
  return Object.keys(this.items).length; // {1}
};
```

The `Object` class in JavaScript contains a method called `keys` that returns an array of all the properties of a given object. In this case, we can use the `length` property of this array (`{1}`) to return how many properties we have in the `items` object. This code will only work in modern browsers (such as IE9+, FF4+, Chrome5+, Opera12+, Safari5+, and so on).

The third method is to extract each property of the `items` object manually, count how many properties there are, and return this number. This method will work in any browser and is the equivalent of the previous code, as follows:

```
sizeLegacy() {  
    let count = 0;  
    for(let key in this.items) { // {2}  
        if(this.items.hasOwnProperty(key)) { // {3}  
            count++; // {4}  
        }  
    }  
    return count;  
};
```

So, first, we will iterate through all the properties of the `items` object (`{2}`) and check whether this property is really a property of our object (so that we do not count it more than once - `{3}`). If it's positive, we will increment the `count` variable (`{4}`) and at the end of the method, we will return this number.



We cannot simply use the `for-in` statement, iterate through the properties of the `items` object, and increment the `count` variable's value. We also need to use the `has` method (to verify that the `items` object has this property) because the object's prototype contains additional properties for the object as well (properties are inherited from the base JavaScript `Object` class, but it still has properties of the object, which are not used in this data structure).

The values method

To implement the `values` method, we can also use a built-in method from the `Object` class named `values` as follows:

```
values() {  
    return Object.values(this.items);  
}
```



The `Object.values()` method returns an array of all of the properties' values of a given object. It was added in **ECMAScript 2017** and it is only available in modern browsers.

If we want to write a code that can be executed in any browser, we can use the following code, which is equivalent to the previous code:

```
valuesLegacy() {  
    let values = [];  
    for(let key in this.items) { // {1}  
        if(this.items.hasOwnProperty(key)) { // {2}  
            values.push(key);  
        }  
    }  
    return values;  
};
```

So, first, we will iterate through all the properties of the `items` object ({1}), add them to an array ({2}), and return this array. This method is similar to the `sizeLegacy` method we developed, but instead of counting the properties, we are adding in an array.

Using the Set class

Now that we have finished implementing our set data structure, let's take a look at how we can use it. Let's give it a try and execute some commands to test our `Set` class, as follows:

```
const set = new Set();  
  
set.add(1);  
console.log(set.values()); // outputs [1]  
console.log(set.has(1)); // outputs true  
console.log(set.size()); // outputs 1  
  
set.add(2);  
console.log(set.values()); // outputs [1, 2]  
console.log(set.has(2)); // true  
console.log(set.size()); // 2  
  
set.delete(1);  
console.log(set.values()); // outputs [2]  
  
set.delete(2);  
console.log(set.values()); // outputs []
```

So, now we have a very similar implementation of the `Set` class, as in ECMAScript 2015.

Set operations

Set is one of the most basic concepts in mathematics and it is very important in computer science as well. One of the main applications in computer science is in **databases**, which are the roots of most applications. Sets are used in query design and processing. When we create a query to retrieve a set of data in a relational database (Oracle, Microsoft SQL Server, MySQL, and so on), we design the query using set notation and the database will also return a set of data. When we create an SQL query, we can specify whether we want to retrieve all the data from a table or only a subset. We can also retrieve data that is common to two tables, data that exists only in one table (and not in the other table), or data that exists in both tables (among other operations). These operations are known in the SQL world as **joins**, and the base of **SQL joins** are set operations.



To learn more about SQL join operations, please read at <http://www.sqljoin.com/sql-join-types>.

We can perform the following operations on sets:

- **Union:** Given two sets, this returns a new set of elements from both of the given sets
- **Intersection:** Given two sets, this returns a new set with the elements that exist in both sets
- **Difference:** Given two sets, this returns a new set with all the elements that exist in the first set and do not exist in the second set
- **Subset:** This confirms whether a given set is a subset of another set

Set union

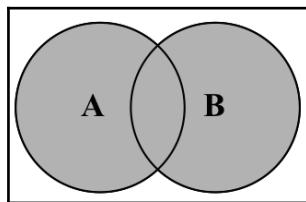
In this topic, we will cover the mathematical concept of union. The union of sets **A** and **B** is denoted by:

$$A \cup B$$

And is defined as:

$$A \cup B = x | x \in A \vee x \in B$$

This means that **x** (the element) exists in **A** or **x** exists in **B**. The following diagram exemplifies the union operation:



Now, let's implement the `union` method in our `Set` class with the following code:

```
union(otherSet) {  
    const unionSet = new Set(); // {1}  
    this.values().forEach(value => unionSet.add(value)); // {2}  
    otherSet.values().forEach(value => unionSet.add(value)); // {3}  
    return unionSet;  
}
```

First, we need to create a new set to represent the union of two sets ({1}). Next, we will get all the `values` from the first set (the current instance of the `Set` class), iterate through them, and add all the values to the set that represents the `union` ({2}). Then, we will do the exact same thing but with the second set ({3}). Finally, we will return the result.



Since the `values` method we implemented returns an array, we can use the `Array` classes `forEach` method to iterate through all elements of the array. Just a reminder that the `forEach` method was introduced in ECMAScript 2015. The `forEach` method receives a parameter (`value`) that represents each value of the array and also has a callback function that executes a programming logic. In the preceding code, we are also using **arrow functions** (`=>`) instead of explicitly declaring `function(value) { unionSet.add(value) }`. The code looks modern and succinct using the ES2015 functionalities we learned in Chapter 2, *ECMAScript and TypeScript Overview*.

We can also write the `union` method as follows, without using the `forEach` method and arrow functions, but whenever possible, we will try using the ES2015+ functionalities:

```
union(otherSet) {
    const unionSet = new Set(); // {1}

    let values = this.values(); // {2}
    for (let i = 0; i < values.length; i++) {
        unionSet.add(values[i]);
    }

    values = otherSet.values(); // {3}
    for (let i = 0; i < values.length; i++) {
        unionSet.add(values[i]);
    }

    return unionSet;
};
```

Let's test the previous code as follows:

```
const setA = new Set();
setA.add(1);
setA.add(2);
setA.add(3);

const setB = new Set();
setB.add(3);
setB.add(4);
setB.add(5);
setB.add(6);

const unionAB = setA.union(setB);
console.log(unionAB.values());
```

The output will be [1, 2, 3, 4, 5, 6]. Note that the element 3 is present in both `setA` and `setB`, and it appears only once in the result set.



It is important to note that the `union`, `intersection`, and `difference` methods we are implementing in this chapter do not modify the current instance of the `Set` class nor the `otherSet` that is being passed as a parameter. Methods or functions that do not have collateral effects are called **pure functions**. A pure function does not modify the current instance nor the parameters; it only produces a new result. This is a very important concept of the **functional programming** paradigm that we will introduce later in this book.

Set intersection

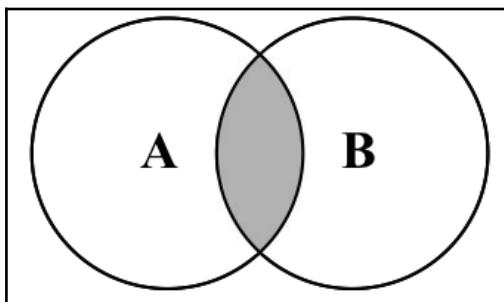
In this topic, we will cover the mathematical concept of intersection. The intersection of sets **A** and **B** is denoted by:

$$A \cap B$$

And is defined as:

$$A \cap B = x | x \in A \wedge x \in B$$

This means that **x** (the element) exists in both **A** and **B**, thus sharing a or some of its elements with both **A** and **B**. The following diagram exemplifies the intersection operation:



Now, let's implement the `intersection` method in our `Set` class, as follows:

```
intersection(otherSet) {
    const intersectionSet = new Set(); // {1}

    const values = this.values();
    for (let i = 0; i < values.length; i++) { // {2}
        if (otherSet.has(values[i])) { // {3}
            intersectionSet.add(values[i]); // {4}
        }
    }
    return intersectionSet;
}
```

For the `intersection` method, we need to find all the elements from the current instance of the `Set` class that also exist in the given `Set` instance (`otherSet`). So, first, we will create a new `Set` instance so that we can return it with the common elements (`{1}`). Next, we will iterate through all the values of the current instance of the `Set` class (`{2}`), and we will verify that the value exists in the `otherSet` instance as well (`{3}`). We can use the `has` method, which we implemented earlier in this chapter to verify that the element exists in the `Set` instance. Then, if the value exists in the other `Set` instance as well, we will add it to the created `intersectionSet` variable (`{4}`) and return it.

Let's do some testing, as follows:

```
const setA = new Set();
setA.add(1);
setA.add(2);
setA.add(3);

const setB = new Set();
setB.add(2);
setB.add(3);
setB.add(4);

const intersectionAB = setA.intersection(setB);
console.log(intersectionAB.values());
```

The output will be `[2, 3]`, as the values 2 and 3 exist in both sets.

Improving the intersection method

Suppose we have the following two sets:

- setA with values [1, 2, 3, 4, 5, 6, 7]
- setB with values [4, 6]

Using the `intersection` method we created, we would need to iterate the values of `setA` seven times, which is the number of elements in `setA`, and compare these seven values with only two elements from `setB`. It would be better if we had the same result if we only had to iterate `setB` two times. Fewer iterations means a cheaper processing cost, so let's optimize our code in order to iterate the set with fewer elements, as follows:

```
intersection(otherSet) {
    const intersectionSet = new Set(); // {1}
    const values = this.values(); // {2}
    const otherValues = otherSet.values(); // {3}
    let biggerSet = values; // {4}
    let smallerSet = otherValues; // {5}
    if (otherValues.length - values.length > 0) { // {6}
        biggerSet = otherValues;
        smallerSet = values;
    }
    smallerSet.forEach(value => { // {7}
        if (biggerSet.includes(value)) {
            intersectionSet.add(value);
        }
    });
    return intersectionSet;
}
```

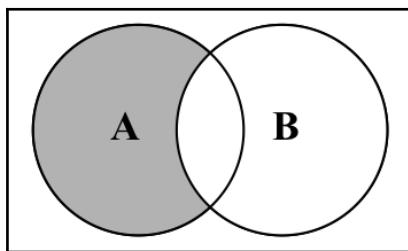
So, first, we will create a new set to store our `intersection` result ({1}). We will also retrieve the values of the current set instance ({2}) and the given set passed as a parameter to the `intersection` method ({3}). Next, we will presume that the current instance is the set with more elements ({4}) and the given set is the set of smaller elements ({5}). We will compare the size of both sets ({6}), and in case the given set has more elements than the current instance, we switch the values of `biggerSet` and `smallerSet`. Finally, we will iterate the smaller set ({7}) in order to calculate the common values between the two sets and return the result.

Set difference

In this topic, we will cover the mathematical concept of difference. The difference between sets **A** and **B** is denoted by $A - B$, which is defined as:

$$A - B = x | x \in A \wedge x \notin B$$

This means that **x** (the element) exists in **A**, but **x** does not exist in **B**. The following diagram exemplifies the difference operation between sets **A** and **B**:



Now, let's implement the difference method in our `Set` class using the following code:

```
difference(otherSet) {  
    const differenceSet = new Set(); // {1}  
    this.values().forEach(value => { // {2}  
        if (!otherSet.has(value)) { // {3}  
            differenceSet.add(value); // {4}  
        }  
    });  
    return differenceSet;  
}
```

The `intersection` method will return all the elements that exist in both sets. The `difference` method will return all the elements that exist in **A** but not in **B**. First, we will create our result set (`{1}`) as we do not want to modify the current set or the given set. Then, we will iterate all the values of the current set instance (`{2}`). We will verify whether the `value` (element) exists in the given set (`{3}`), and if the element does not exist in the `otherSet`, we will add the `value` to the resultant set.

Let's do some testing (with the same sets we used in the `intersection` section):

```
const setA = new Set();
setA.add(1);
setA.add(2);
setA.add(3);

const setB = new Set();
setB.add(2);
setB.add(3);
setB.add(4);

const differenceAB = setA.difference(setB);
console.log(differenceAB.values());
```

The output will be [1] because 1 is the only element that exists in `setA`. If we do `setB.difference(setA)`, we will get [4] as the output because 4 is the only element that only exists in `setB`.



We cannot optimize the `difference` method as we did with the `intersection` method, since the difference between `setA` and `setB` might be different than the difference between `setB` and `setA`.

Subset

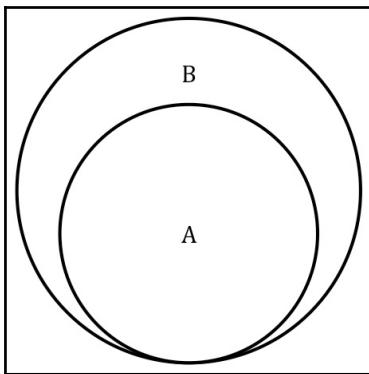
The last set operation we will cover is the subset. An example of the mathematical concept of subset is that **A** is a subset of (or is included in) **B**, and this is denoted by:

$$A \subseteq B$$

The set is defined as:

$$\forall x x \in A \Rightarrow x \in B$$

This means that for every **x** (element) that exists in **A**, it also *needs to exist* in **B**. The following diagram exemplifies when **A** is a subset of **B**:



Now, let's create the `isSubsetOf` method in our `Set` class using the following code:

```
isSubsetOf(otherSet) {  
    if (this.size() > otherSet.size()) { // {1}  
        return false;  
    }  
    let isSubset = true; // {2}  
    this.values().every(value => { // {3}  
        if (!otherSet.has(value)) { // {4}  
            isSubset = false; // {5}  
            return false;  
        }  
        return true; // {6}  
    });  
    return isSubset; // {7}  
}
```

The first verification that we need to do is to check the size of the current instance of the `Set` class. If the current instance has more elements than the `otherSet` instance, it is not a subset ({1}). A subset needs to have less or the same number of elements as the compared set.

Next, we presume that the current instance is a subset of the given set ({2}). We will iterate through all the current set elements ({3}), and we will verify that the element also exists in `otherSet` ({4}). If any element does not exist in `otherSet`, it means that it is not a subset, so we will return `false` ({5}). If all the elements also exist in `otherSet`, line {5} will not be executed, and then we will return `true` ({7}) since the `isSubset` flag will not be changed.

In the `isSubsetMethod`, we are not using the `forEach` method which we used in `union`, `intersection`, and `difference`. We are using the `every` method instead, which is also part of the JavaScript Array class and was introduced in ES2015. We learned in Chapter 3, *Arrays*, that the `forEach` method is evoked for every value of the array. In the case of the subset logic, we can stop iterating the values in case we find a value that is not in the `otherSet`, meaning it is not a subset. The `every` method will be evoked as long as the callback function returns `true` ({ 6 }). If the callback function returns `false`, it breaks the loop, so that is why we are also changing the value of the `isSubset` flag in line { 5 }.

Let's try the previous code:

```
const setA = new Set();
setA.add(1);
setA.add(2);

const setB = new Set();
setB.add(1);
setB.add(2);
setB.add(3);

const setC = new Set();
setC.add(2);
setC.add(3);
setC.add(4);

console.log(setA.isSubsetOf(setB));
console.log(setA.isSubsetOf(setC));
```

We have three sets: `setA` is a subset of `setB` (so the output is `true`); however, `setA` is not a subset of `setC` (`setC` only contains the value 2 from `setA` and not the values 1 and 2), so the output will be `false`.

ECMAScript 2015 – the Set class

ECMAScript 2015 introduced a `Set` class as part of the JavaScript API. We developed our `Set` class based on the ES2015 `Set` class.



You can see the details of the ECMAScript 2015 `Set` class implementation at https://developer.mozilla.org/en-US/docs/Web/JavaScript/Reference/Global_Objects/Set (or <http://goo.gl/2li2a5>).

Now, let's take a look at how we can use the native Set class, as well.

Let's use the same examples we used to test our Set class, as follows:

```
const set = new Set();
set.add(1);
console.log(set.values()); // outputs @Iterator
console.log(set.has(1)); // outputs true
console.log(set.size); // outputs 1
```

The difference between our Set class and the ES2015 Set class is that the `values` method returns `Iterator` (which you learned in Chapter 3, *Arrays*) instead of the array with the values. Another difference is that we developed a `size` method to return the number of values the Set stores. The ES2015 Set class has a property named `size`.

We can also call the `delete` method to remove an element from `set` with the following code:

```
set.delete(1);
```

The `clear` method also resets the Set data structure. It is the same functionality we implemented.

ES2015 Set class operations

We developed the mathematical operations such as union, intersection, difference, and also subset in our Set class. Unfortunately, the ES2015 native Set class does not contain these functionalities. However, we can write our own functions with similar functionality in case it is needed.

We will use the following two sets in our examples:

```
const setA = new Set();
setA.add(1);
setA.add(2);
setA.add(3);

const setB = new Set();
setB.add(2);
setB.add(3);
setB.add(4);
```

Simulating the union operation

To add all the elements from two sets, we can create a function that will return a new set with all elements from `set1` and `set2`. We need to iterate `set1` ({1}) and `set2` ({2}) and add all their elements into the union set using `add`, as demonstrated by the following code:

```
const union = (set1, set2) => {
  const unionAb = new Set();
  set1.forEach(value => unionAb.add(value));
  set2.forEach(value => unionAb.add(value));
  return unionAb;
};
console.log(union(setA, setB)); // {1, 2, 3, 4}
```

Simulating the intersection operation

To simulate the intersection operation, we can also create a function to help us create a new set of the common elements that both `setA` and `setB` demonstrated as follows:

```
const intersection = (set1, set2) => {
  const intersectionSet = new Set();
  set1.forEach(value => {
    if (set2.has(value)) {
      intersectionSet.add(value);
    }
  });
  return intersectionSet;
};
console.log(intersection(setA, setB)); // {2, 3}
```

The preceding code does the same thing as the `intersection` function we developed, however, the preceding code is not optimized (as we also developed an optimized version).

Simulating the difference operation

While the intersection operation is achieved by creating a new set with the common elements that both `setA` and `setB` have, the difference operation is achieved by creating a new set with the elements that `setA` has but `setB` does not. Take a look at the following code:

```
const difference = (set1, set2) => {
  const differenceSet = new Set();
  set1.forEach(value => {
    if (!set2.has(value)) { // {1}
```

```
        differenceSet.add(value);
    }
});
return differenceSet;
};
console.log(difference(setA, setB));
```

The only difference between the `intersection` function and the `difference` simulations is line `{1}` as we only want to add the different `Set` elements that `setA` has and `setB` does not.

Using the spread operator

There is a simpler way of simulating the union, intersection, and difference operations by using the **spread operator**, also introduced in ES2015 that we learned in [Chapter 2, ECMAScript and TypeScript Overview](#).

The process consists of three steps:

1. Converting the sets to arrays.
2. Performing the desired operation.
3. Converting the result back to a set.

Let's see how we can perform the `set union` operation using the spread operator:

```
console.log(new Set([...setA, ...setB]));
```

The ES2015 `Set` class also accepts passing an array directly in its constructor to initialize the `Set` with values, so we apply the spread operator in `setA(...setA)`, which will transform its values in an array (will spread its values) and we do the same to `setB`.

As `setA` has values `[1, 2, 3]` and `setB` has values `[2, 3, 4]`, the preceding code is the same as doing `new Set([1, 2, 3, 2, 3, 4])`, but it will only add the unique values.

Now, let's see how we can perform the `set intersection` operation using the spread operator:

```
console.log(new Set([...setA].filter(x => setB.has(x))));
```

The preceding code will also transform `setA` into an array and will use the `filter` method, which returns a new array with the values that match the callback function—which in this case verifies whether the element also exists in `setB`. The returned array will be used to initialize the constructor of the resultant `Set`.

Finally, let's see how we can perform the *set difference* operation using the spread operator:

```
console.log(new Set([...setA].filter(x => !setB.has(x))));
```

It is the same code as the intersection operation, however, we are only interested in the elements that do not exist in `setB`.

You can use the version of your preference to perform the set operations using the native ES2015 `Set` class!

Multisets or bags

As we have already learned, the set data structure does not allow duplicated elements. However, in mathematics, there is a concept called multi-set, which allows the same element to be inserted into the set even if the element has already been inserted before.

Multisets (or **bags**) can be very useful for counting how many times the element is present in a set. It is also largely applied in database systems.



We will not cover the bag data structure in this book. However, you can check the source code and examples by downloading the code bundle of this book or accessing <https://github.com/loiane/javascript-datastructures-algorithms>.

Summary

In this chapter, you learned how to implement a `Set` class from scratch, which is similar to the `Set` class defined in the definition of ECMAScript 2015. We also covered some methods that are not usually present in other programming language implementations of the set data structure, such as union, intersection, difference, and subset. We implemented a complete `Set` class compared to the current implementation of `Set` in other programming languages.

In the next chapter, we will cover hashes and dictionaries, which are non-sequential data structures.

8

Dictionaries and Hashes

In the previous chapter, we learned about sets. In this chapter, we will continue our discussion about data structures that store unique values (non-repeated values) using dictionaries and hashes.

In a set, we are interested in the value itself as the primary element. In a dictionary (or map), we store values in pairs as [key, value]. The same goes for hashes (they store values in pairs, such as [key, value]); however, the way that we implement these data structures is a little bit different as dictionaries can only store a single value per key, as we will learn in this chapter.

In this chapter, we will cover:

- The dictionary data structure
- The hash table data structure
- Handling collisions in hash tables
- The **ECMAScript 2015** Map, WeakMap, and WeakSet classes

The dictionary data structure

As we have already learned, a set is a collection of distinct elements (non-repeated elements). A **dictionary** is used to store [key, value] pairs, where the key could be used to find a particular element. A dictionary is very similar to a set; a set stores a [key, key] collection of elements, and a dictionary stores a [key, value] collection of elements. A dictionary is also known as a **map**, **symbol table**, and an **associative array**.

In computer science, dictionaries are often used to store the reference address of objects. For example, if we open the **Chrome | Developer tools** in the **Memory** tab and run a **snapshot**, we will be able to see some objects and their respective address references in the memory (represented by @<number>). We can see this scenario in the following screenshot:

	Constructor	Distance	Objects Count	Shallow Size	Retained Size
Profiles	▶ 13 :: [] @182773	6		3 096 0 %	12 120 0 %
HEAP SNAPSHOTS	▶ map :: system / Map @847	5		88 0 %	88 0 %
Snapshot 4 Save 4.3 MB	▶ name :: "http://127.0.0.1:8887/Pack	6		40 0 %	40 0 %
	▶ source :: "!!function(e,t){\"object\"=	6		40 0 %	40 0 %
	line_ends :: (script line ends) [] @	6		24 0 %	24 0 %
	▶ 16 :: !!! @57	3		24 0 %	24 0 %
	▶ 7 :: system @182771	6		24 0 %	24 0 %
	Retainers				
	Object	Distance	Count	Shallow Size	Retained Size
	▼ get HashTableLinearProbingLazy in @167693	2		24 0 %	4 488 0 %
	▼ PacktDataStructuresAlgorithms in Window / 127.	1		64 0 %	193 952 4 %
	▼ extension in system / NativeContext @163829	2		2 240 0 %	117 928 3 %
	native_context in Window / 127.0.0.1:8887	1		64 0 %	193 952 4 %
	▶ context in Array() @189499	2		72 0 %	616 0 %
	▶ context in Boolean() @192427	2		72 0 %	808 0 %
	▶ context in Date() @190901	2		72 0 %	5 344 0 %
	▶ context in Error() @189897	2		72 0 %	576 0 %

In this chapter, we will also cover some examples of how to use the dictionary data structure in real world projects: a dictionary itself (the words and their definitions) and an address book.

Creating the Dictionary class

Similar to the `Set` class, ECMAScript 2015 also contains an implementation of the `Map` class, also known as a dictionary.

The class we will implement in this chapter is based on the `Map` implementation of ECMAScript 2015. You will notice that it is very similar to the `Set` class (but instead of storing a `[key, key]` pair, we will store a `[key, value]` pair).

The following is the base structure of our `Dictionary` class:

```
import { defaultToString } from '../util';

export default class Dictionary {
    constructor(toStrFn = defaultToString) {
        this.toStrFn = toStrFn; // {1}
        this.table = {}; // {2}
    }
}
```

Similar to the `Set` class, we will also store the elements of the `Dictionary` class in an `Object` instance instead of an array (`table` property—{2}). We will store the `[key, value]` pairs as `table[key] = {key, value}`.



JavaScript lets us access an object property by using brackets `([])`, passing the name of the property as "**position**". This is why it is called an associative array! We have used dictionaries before in this book in Chapter 4, *Stacks*, Chapter 5, *Queues and Deques*, and Chapter 7, *Sets*.

In a dictionary, the ideal would be to store keys of type string and any type of value (from primitive type such as numbers, a string, to complex objects). However, because JavaScript is not strongly typed, we cannot guarantee the `key` will be a string. For this reason, we need to transform whatever object is passed as the `key` into a string to make it easier to search and retrieve values from the `Dictionary` class (this same logic can also be applied to the `Set` class from the previous chapter). To do so, we will need a function to transform the `key` into a string ({1}). By default, we will use the `defaultToString` function declared in the `utils.js` file (we can reuse the functions from this file in any data structure we create).



Since we are using the ES2015 **default parameter** functionality, `toStrFn` is an optional parameter. If needed, we can also pass a custom function to specify how we would like to transform the `key` into a string.

The `defaultToString` function is declared as follows:

```
export function defaultToString(item) {  
    if (item === null) {  
        return 'NULL';  
    } else if (item === undefined) {  
        return 'UNDEFINED';  
    } else if (typeof item === 'string' || item instanceof String) {  
        return `${item}`;  
    }  
    return item.toString(); // {1}  
}
```



Please note that it is important that if the `item` variable is an object, it needs to have a `toString` method implemented, otherwise it will lead to unexpected results such as `[object Object]`, which is not very user-friendly.

If the `key (item)` is a string, then we simply return it, otherwise, we evoke the `toString` method of the `item`.

Next, we need to declare the methods available for a map/dictionary, which are:

- `set (key, value)`: This method adds a new element to the dictionary. If the `key` already exists, the existing `value` will be overwritten with the new one.
- `remove (key)`: This method removes the `value` from the dictionary using the `key` as the search parameter.
- `hasKey (key)`: This method returns `true` if the `key` exists in the dictionary and `false` otherwise.
- `get (key)`: This method returns a specific `value` from the dictionary using the `key` as the search parameter.
- `clear ()`: This method removes all the values from the dictionary.
- `size ()`: This method returns how many values the dictionary contains. It is similar to the `length` property of the `Array` class.
- `isEmpty ()`: This method returns `true` if the `size` equals to zero and `false` otherwise.
- `keys ()`: This method returns an array of all the keys the dictionary contains.
- `values ()`: This method returns an array of all the values of the dictionary.

- `keyValues()`: This method returns an array of all value pairs [key, value] of the dictionary.
- `forEach(callbackFn)`: This method iterates every value pair in the dictionary. The `callbackFn` function has two parameters: `key` and `value`. This method can also be interrupted in case the callback function returns `false` (similar to the `every` method from the `Array` class).

Verifying whether a key exists in the dictionary

The first method we will implement is the `hasKey(key)` method. We will implement this method first because it will be used in other methods, such as `set` and `remove`. We can see its code as follows:

```
hasKey(key) {
    return this.table[this.toStrFn(key)] != null;
}
```

JavaScript only allows us to use strings as the `key`/property of objects. In case we have a complex object passed as a `key`, we will need to transform it into a string. For this reason, we will always invoke the `toStrFn` function. In case there is a value pair for the given `key` (a position in the table not `null` or `undefined`), then we return `true`, otherwise, we return `false`.

Setting a key and value in the dictionary and the ValuePair class

Next, we have the `set` method, as declared in the following code:

```
set(key, value) {
    if (key != null && value != null) {
        const tableKey = this.toStrFn(key); // {1}
        this.table[tableKey] = new ValuePair(key, value); // {2}
        return true;
    }
    return false;
}
```

This method receives a `key` and a `value` parameter. If the `key` and `value` are not `undefined` or `null`, then we get the string that represents the `key` ({}1) and we create a new value pair and assign it to the `key` string (`tableKey`) property in the `table` object ({}2). If the `key` and `value` are valid, we also return `true`, indicating the dictionary was able to store the `key` and `value`, otherwise, we return `false`.

This method can be used to add a new value or update an existing one.

In line {}2{}, we are instantiating the class `ValuePair`. The `ValuePair` class declaration is as follows:

```
class ValuePair {  
    constructor(key, value) {  
        this.key = key;  
        this.value = value;  
    }  
    toString() {  
        return `#${this.key}: ${this.value}`;  
    }  
}
```

Because we are transforming the `key` into a string to store the `value` in the dictionary, we are also going to store the original key for informational purposes. For this reason, instead of simply storing the `value` in the dictionary, we will store both values: the original `key` and the `value`. To make it easier to output the dictionary in the `toString` method later, we are also going to create a `toString` method for the `ValuePair` class.

Removing a value from the dictionary

Next, we will implement the `remove` method. It is very similar to the `remove` method from the `Set` class; the only difference is that we will first search for the `key` (instead of `value`), as follows:

```
remove(key) {  
    if (this.hasKey(key)) {  
        delete this.table[this.toStrFn(key)];  
        return true;  
    }  
    return false;  
}
```

Then, we will use the JavaScript `delete` operator to remove the `key` (transformed into a string) from the `table` object. In case we are able to remove the `value` from the dictionary, we will also return `true`, otherwise, we will return `false`.

Retrieving a value from the dictionary

If we want to search for a particular `key` from the dictionary and retrieve its `value`, we can use the following method:

```
get(key) {  
    const valuePair = this.table[this.toStrFn(key)]; // {1}  
    return valuePair == null ? undefined : valuePair.value; // {2}  
}
```

The `get` method will retrieve the object that is stored in the given `key` property ({1}). If the `value` pair object exists, then we return its `value`, otherwise, we return `undefined` ({2}).

A different way of implementing this same method would be verifying whether the `value` that we would like to retrieve exists (by searching for its `key`) first, and if the result is positive, we access the `table` object and return the desired value. The second option of the `get` method is as follows:

```
get(key) {  
    if (this.hasKey(key)) {  
        return this.table[this.toStrFn(key)];  
    }  
    return undefined;  
}
```

However, in this second approach, we would be retrieving the string for the `key` and accessing the `table` object twice: the first time in the `hasKey` method and the second time inside the `if` statement. It is a small detail, but the first approach has a cheaper processing cost.

The `keys`, `values`, and `valuePairs` methods

Now that we have created the most important methods for the `Dictionary` class, let's create some auxiliary, but very useful methods.

Next, we will create the `valuePairs` method, which is going to return an array with all `ValuePair` objects present in the dictionary. The code is as follows:

```
keyValues() {  
    return Object.values(this.table);  
}
```

The code is very simple—we are evoking the built-in `values` method from the JavaScript `Object` class introduced in the ECMAScript 2017 which we learned in Chapter 1, *JavaScript – A Quick Overview*.

Since the `Object.values` method might not be available in all browsers yet, we can also use the following code as an alternative:

```
keyValues() {  
    const valuePairs = [];  
    for (const k in this.table) { // {1}  
        if (this.hasKey(k)) {  
            valuePairs.push(this.table[k]); // {2}  
        }  
    }  
    return valuePairs;  
};
```

In the preceding code, we need to iterate through all the properties of the `table` object ({1}). Just to make sure the key exists, we will use the `hasKey` function for this verification, and then, we will add the `ValuePair` from the `table` object ({2}) into the resultant array. In this method, since we are already retrieving the property (`key`) from the `table` object directly, we do not need to transform it into a string with the `toString` function.



We cannot simply use the `for-in` statement and iterate through the properties of the `table` object. We also need to use the `hasKey` method (to verify whether the `table` object has this property) because the object's prototype contains additional properties of the object, as well. (Properties are inherited from the base JavaScript `Object` class, but it still has properties of the object that we are not interested in for this data structure.)

The next method we will create is the `keys` method. This method returns all the keys (the original ones) used to identify a value in the `Dictionary` class, as follows:

```
keys() {  
    return this.keyValues().map(valuePair => valuePair.key);  
}
```

We will evoke the `keyValues` method we created that returns an array of `ValuePair` instances. Then, we will iterate each `ValuePair`. Since we are only interested in the `ValuePair` `key` property, we will only return its `key`.

In the preceding code, we are using the `map` method from the `Array` class to iterate each `ValuePair`. The `map` method transforms a given value into something else. In this case, we are transforming each `ValuePair` into its `key`. The logic used inside the `keys` method can also be written as follows:

```
const keys = [];
const valuePairs = this.keyValues();
for (let i = 0; i < valuePairs.length; i++) {
    keys.push(valuePairs[i].key);
}
return keys;
```

The `map` method allows us to execute the same logic and obtain the same result as the five lines of the preceding code, and once we get used to its syntax, it is even easier to read the code and understand what it is doing.



The `map` method was introduced in ES2015 (ES6) as we learned in Chapter 3, *Arrays*. The `keys` method we created is also using the **functional programming paradigm**, which we will learn more about later in this book.

Similar to the `keys` method, we also have the `values` method. The `values` method returns an array of all values stored in the dictionary. Its code is very similar to the `keys` method, however, instead of returning the `key` property of the `ValuePair` class, we return the `value` property as follows:

```
values() {
    return this.keyValues().map(valuePair => valuePair.value);
}
```

Iterating each `ValuePair` of the dictionary with `forEach`

So far, we have not created a method that allows us to iterate through each value stored in the data structures. We are going to implement the `forEach` method for the `Dictionary` class, but we can use this same logic for the other data structures we created previously in the book as well.

The `forEach` method is as follows:

```
forEach(callbackFn) {
    const valuePairs = this.keyValues(); // {1}
    for (let i = 0; i < valuePairs.length; i++) { // {2}
        const result = callbackFn(valuePairs[i].key, valuePairs[i].value); // {3}
        if (result === false) {
            break; // {4}
        }
    }
}
```

First, we will retrieve the `ValuePair` array from the dictionary ({1}). Next, we will iterate each `ValuePair` ({2}) and we will evoke the `callbackFn` function ({3}) passed as a parameter to the `forEach` method and will also store its result. In case the callback function returns `false`, we will interrupt the execution of the `forEach` method ({4}), breaking the `for` loop that is iterating the `valuePairs`.

The `clear`, `size`, `isEmpty`, and `toString` methods

The `size` method returns how many values are stored in the dictionary. We can retrieve all the keys from the `table` object using the `Object.keys` method (the same as we did in the `keyValues` method). The code for the `size` method is declared as follows:

```
size() {
    return Object.keys(this.table).length;
}
```

We could also evoke the `keyValues` method and return the `length` of the returned array (`return this.keyValues().length`).

To verify whether the dictionary is empty, we can retrieve its `size` and see whether it is zero. If the `size` is zero, it means the dictionary is empty. This logic is implemented in the `isEmpty` method as follows:

```
isEmpty() {
    return this.size() === 0;
}
```

To clear the dictionary, we can simply assign a new object instance to the `table` object:

```
clear() {
  this.table = {};
}
```

Finally, we will also create the `toString` method as follows:

```
toString() {
  if (this.isEmpty()) {
    return '';
  }
  const valuePairs = this.keyValues();
  let objString = `${valuePairs[0].toString()}`; // {1}
  for (let i = 1; i < valuePairs.length; i++) {
    objString = `${objString}, ${valuePairs[i].toString()}`; // {2}
  }
  return objString; // {3}
}
```

For the `toString` method, in case the dictionary is empty, we return an empty string. Otherwise, we add its first `ValuePair` to the resultant string by evoking the `ValuePair` `toString` method ({1}). Then, if there is any `value` in the array, we also add it to the resultant string ({2}), returning it at the end of the method ({3}).

Using the Dictionary class

To use the `Dictionary` class, first we need to create an instance, and then we will add three emails to it. We will use this `dictionary` instance to exemplify an email address book.

Let's execute some code using the class we created:

```
const dictionary = new Dictionary();
dictionary.set('Gandalf', 'gandalf@email.com');
dictionary.set('John', 'johnsnow@email.com');
dictionary.set('Tyrion', 'tyrion@email.com');
```

If we execute the following code, we will get the output as true:

```
console.log(dictionary.hasKey('Gandalf'));
```

The following code will output 3 because we added three elements to our dictionary instance:

```
console.log(dictionary.size());
```

Now, let's execute the following lines of code:

```
console.log(dictionary.keys());
console.log(dictionary.values());
console.log(dictionary.get('Tyrion'));
```

The output will be as follows, in the respective order:

```
["Gandalf", "John", "Tyrion"]
["gandalf@email.com", "johnsnow@email.com", "tyrion@email.com"]
tyrion@email.com
```

Finally, let's execute some more lines of code:

```
dictionary.remove('John');
```

Let's also execute the following ones:

```
console.log(dictionary.keys());
console.log(dictionary.values());
console.log(dictionary.keyValues());
```

The output will be as follows:

```
["Gandalf", "Tyrion"]
["gandalf@email.com", "tyrion@email.com"]
[{"key": "Gandalf", "value": "gandalf@email.com"}, {"key": "Tyrion", "value": "tyrion@email.com"}]
```

Since we removed one value, the dictionary instance now contains only two value types. The highlighted line exemplifies how the table object is structured internally.

To evoke the `forEach` method, we can use the following code:

```
dictionary.forEach((k, v) => {
  console.log('forEach: ', `key: ${k}, value: ${v}`);
});
```

And we will get the following output:

```
forEach: key: Gandalf, value: gandalf@email.com
forEach: key: Tyrion, value: tyrion@email.com
```

The hash table

In this section, we will learn about the `HashTable` class, also known as `HashMap`, a hash implementation of the `Dictionary` class.

Hashing consists of finding a value in a data structure in the shortest time possible. You learned in previous chapters that if we want to get a value from a data structure (using a `get` method), we need to iterate through the structure until we find it. When we use a hash function, we already know which position the value is in, so we can simply retrieve it. A hash function is a function that, given a `key`, will return an address in the table where the value is.

In computer science, the hash table has several use cases. It can be used as associative arrays, since it is an implementation of the dictionary. It can also be used to index a database. When we create a new table in a relational database such as MySQL, Microsoft SQL Server, Oracle, and so on, it is always a good practice to create an `index` to allow for faster searching of the record `key`. In this case, a hash table can be created to store the key and the reference to the record in the table. Another very common use is using hash tables to represent objects. The JavaScript language uses a hash table internally to represent each object. In this case, each property and method (members) of the object are stored as `key` object types, and each `key` points to the respective member of the object.

As an example, let's continue using the email address book we used in the previous section. The hash function we will use in this book is the most common one, called a **lose-lose hash** function, in which we simply sum up the ASCII values of each character of the key length:

Name/Key	Hash Function	Hash Value	Hash Table
Gandalf	$71 + 97 + 110 + 100 + 97 + 108 + 102$	685	[...]
John	$74 + 111 + 104 + 110$	399	[399]
Tyrion	$84 + 121 + 114 + 105 + 111 + 110$	645	[645]

Creating a HashTable class

We will also use an associative array (object) to represent our data structure as we did in the Dictionary class.

As usual, let's start with the structure of our class using the following code:

```
class HashTable {  
    constructor(toStrFn = defaultToString) {  
        this.toStrFn = toStrFn;  
        this.table = {};  
    }  
}
```

Next, we need to add some methods into our class. We will implement three basic methods for every class:

- `put(key, value)`: This method adds a new item to the hash table (or it can also update it)
- `remove(key)`: This method removes the `value` from the hash table using the `key`
- `get(key)`: This method returns a specific `value` searched by the `key`

Creating a hash function

The first method that we will implement before we implement these three methods is the `hashCode` method. The code is as follows:

```
loseloseHashCode(key) {  
    if (typeof key === 'number') { // {1}  
        return key;  
    }  
    const tableKey = this.toStrFn(key); // {2}  
    let hash = 0; // {3}  
    for (let i = 0; i < tableKey.length; i++) {  
        hash += tableKey.charCodeAt(i); // {4}  
    }  
    return hash % 37; // {5}  
}  
  
hashCode(key) {  
    return this.loseloseHashCode(key);  
}
```

The `hashCode` method simply evokes the `loseloseHashCode` method, passing the key as the parameter.

In the `loseloseHashCode` method, we will first verify whether the key is a number ({1}). If it is a number, we simply return it. Next, we will generate a number based on the sum of each char ASCII value that composes the key. So, first, we need to transform the key into a string ({2}) in case the key is an object and not a string. We will initialize the hash variable that will store the sum ({3}). Then, we will iterate through each character of the key and add the ASCII value of the corresponding character value from the ASCII table to the hash variable ({3}). To do so, we can use the `charCodeAt` method from the JavaScript `String` class. Finally, we will return the hash value. To work with lower numbers, we must use the rest of the division (%) of the hash number using an arbitrary number ({5}) - this will avoid risking working with very big numbers that do not fit in a numeric variable.



For more information about the ASCII table,
refer to: <http://www.asciitable.com>.

Putting a key and a value in the hash table

Now that we have our `hashCode` function, we can implement the `put` method, as follows:

```
put(key, value) {
    if (key != null && value != null) { // {1}
        const position = this.hashCode(key); // {2}
        this.table[position] = new ValuePair(key, value); // {3}
        return true;
    }
    return false;
}
```

The `put` method has a similar logic as the `set` method from the `Dictionary` class. We could name this method `set` as well, however, most of the programming languages use the `put` method for the `HashTable` data structure, so we will follow the same naming convention.

First, we will verify whether the `key` and `value` are valid ({1}), and in case they are not valid, we return `false` to indicate the value was not added (or updated). For the given `key` parameter, we need to find a position in the table using the `hashCode` function we created ({2}). Then, all we have to do is create a `ValuePair` instance with the `key` and `value` ({3}). Similar to the `Dictionary` class, we will also store the original `key` for information purposes.

Retrieving a value from the hash table

Retrieving a `value` from the `HashTable` instance is also simple. We will implement the `get` method for this purpose, as follows:

```
get(key) {
    const valuePair = this.table[this.hashCode(key)];
    return valuePair == null ? undefined : valuePair.value;
}
```

First, we will retrieve the position of the given `key` parameter using the `hashCode` method we created. This function will return the position of the `value`, and all we have to do is access this position from the `table` array and return its `value`.



The `HashTable` and `Dictionary` classes are very similar. The difference is that in the `Dictionary` class, we store the `ValuePair` in the `key` property of the `table` (after it was transformed to a string), and in the `HashTable` class, we generate a number from the `key` (`hash`) and store the `ValuePair` in the `hash` position (or property).

Removing a value from the hash table

The last method we will implement for the `HashTable` is the `remove` method, which is as follows:

```
remove(key) {
    const hash = this.hashCode(key); // {1}
    const valuePair = this.table[hash]; // {2}
    if (valuePair != null) {
        delete this.table[hash]; // {3}
        return true;
    }
    return false;
}
```

To remove a value from the `HashTable`, first, we need to know what position we need to access, so we retrieve the hash using the `hashCode` function ({1}). We retrieve the `valuePair` stored in the hash position ({2}) and in case the `valuePair` is not null or undefined, we remove it using the JavaScript `delete` operator ({3}). We also return `true` if the removal was successful and `false` otherwise.



Instead of using the `delete` JavaScript operator, we can also assign `null` or `undefined` to the removed hash position.

Using the `HashTable` class

Let's test the `HashTable` class by executing some examples:

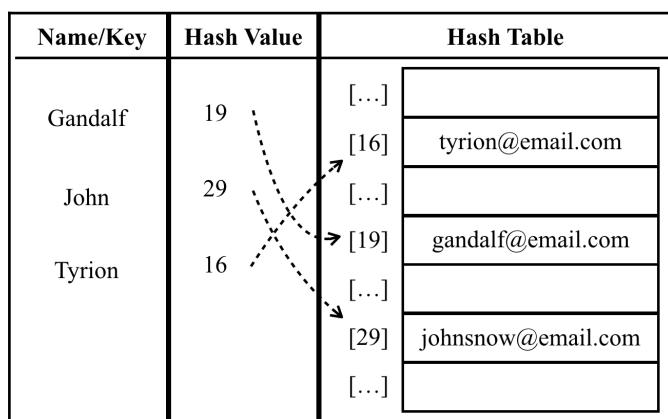
```
const hash = new HashTable();
hash.put('Gandalf', 'gandalf@email.com');
hash.put('John', 'johnsnow@email.com');
hash.put('Tyrion', 'tyrion@email.com');

console.log(hash.hashCode('Gandalf') + ' - Gandalf');
console.log(hash.hashCode('John') + ' - John');
console.log(hash.hashCode('Tyrion') + ' - Tyrion');
```

When we inspect the contents of the hash table after running the previous code, we get the following output:

```
19 - Gandalf
29 - John
16 - Tyrion
```

The following diagram represents the `HashTable` data structure with these three elements in it:



Now, let's test the `get` method by executing the following code:

```
console.log(hash.get('Gandalf')); // gandalf@email.com
console.log(hash.get('Loiane')); // undefined
```

Since `Gandalf` is a key that exists in `HashTable`, the `get` method will return its value. Since `Loiane` is not an existing key, when we try to access its position in the array (a position generated by the hash function), its value will be `undefined` (non-existent).

Next, let's try to remove `Gandalf` from `HashTable`, as follows:

```
hash.remove('Gandalf');
console.log(hash.get('Gandalf'));
```

The `hash.get('Gandalf')` method will return `undefined` as the output on the console since `Gandalf` no longer exists in the table.

Hash table versus hash set

A hash table is the same thing as a hash map. We have covered this data structure in this chapter.

In some programming languages, we also have the **hash set** implementation. The hash set data structure consists of a set, but to insert, remove, or get elements, we use a `hashCode` function. We can reuse all the code we implemented in this chapter for a hash set; the difference is that instead of adding a key-value pair, we will insert only the value, not the key. For example, we could use a hash set to store all the English words (without their definitions). Similar to the `set` data structure, the hash set also stores only unique values, not repeated ones.

Handling collisions between hash tables

Sometimes, different keys can have the same hash value. We will call it a **collision** since we will try to set different key-value pairs to the same position of the `HashTable` instance. For example, let's take a look at what we get in the output with the following code:

```
const hash = new HashTable();
hash.put('Ygritte', 'ygritte@email.com');
hash.put('Jonathan', 'jonathan@email.com');
hash.put('Jamie', 'jamie@email.com');
hash.put('Jack', 'jack@email.com');
hash.put('Jasmine', 'jasmine@email.com');
hash.put('Jake', 'jake@email.com');
hash.put('Nathan', 'nathan@email.com');
hash.put('Athelstan', 'athelstan@email.com');
hash.put('Sue', 'sue@email.com');
hash.put('Aethelwulf', 'aethelwulf@email.com');
hash.put('Sargeras', 'sargeras@email.com');
```

By evoking the `hash.hashCode` method for each name mentioned, we will get the following output:

```
4 - Ygritte
5 - Jonathan
5 - Jamie
7 - Jack
8 - Jasmine
9 - Jake
10 - Nathan
7 - Athelstan
5 - Sue
5 - Aethelwulf
10 - Sargeras
```



Note that Nathan has the same hash value as Sargeras (10). Jack has the same hash value as Athelstan (7). Jonathan, Jamie, Sue, and Aethelwulf (5) have the same hash value as well.

What will happen to the `HashTable` instance? Which values do we have inside it after executing the previous code?

To help us find out, let's implement the `toString` method:

```
toString() {
  if (this.isEmpty()) {
    return '';
  }
  const keys = Object.keys(this.table);
  let objString = `${keys[0]} => ${this.table[keys[0]].toString()} `;
  for (let i = 1; i < keys.length; i++) {
    objString = `${objString}, ${keys[i]} =>
${this.table[keys[i]].toString()} `;
  }
  return objString;
}
```

Since we don't know which positions from the table array have values, we can use a similar logic to the `Dictionary` `toString` method.

After evoking `console.log(hashTable.toString())`, we will have the following output on the console:

```
{ 4 => [#Ygritte: ygritte@email.com] }
{ 5 => [#Aethelwulf: aethelwulf@email.com] }
```

```
{7 => [#Athelstan: athelstan@email.com] }
{8 => [#Jasmine: jasmine@email.com] }
{9 => [#Jake: jake@email.com] }
{10 => [#Sargerias: sargerias@email.com] }
```

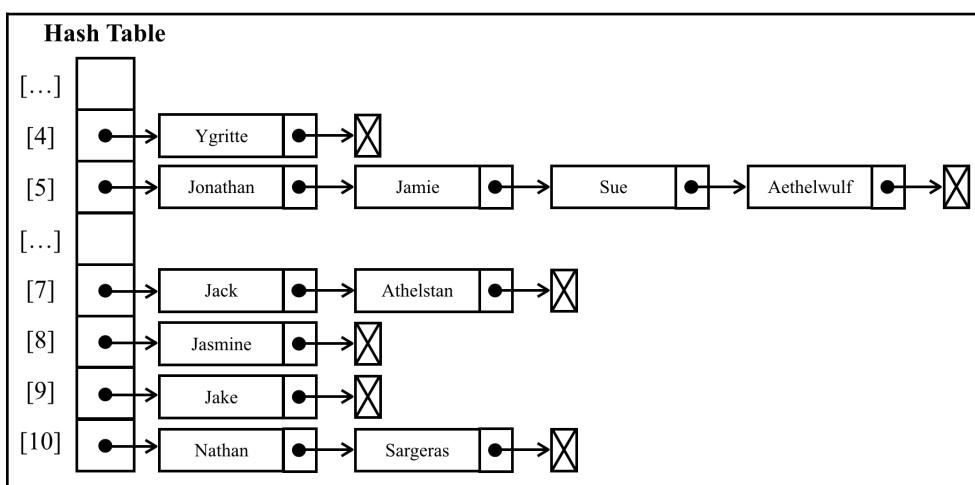
Jonathan, Jamie, Sue, and Aethelwulf have the same hash value—that is, 5. Since Aethelwulf was the last one to be added, Aethelwulf will be the one to occupy position 5 of HashTable. First, Jonathan will occupy it, then Jamie will overwrite it, next Sue will overwrite it one more time, and finally, Aethelwulf will overwrite it again. The same will happen to the other elements that have a collision.

The idea of using a data structure to store all these values is obviously not to lose these values; it is to keep them all, one way or another. For this reason, we need to handle this situation when it happens. There are a few techniques to handle collisions: separate chaining, linear probing, and double hashing. We will cover the first two techniques in this book.

Separate chaining

The **separate chaining** technique consists of creating a linked list for each position of the table and storing the elements in it. It is the simplest technique to handle collisions; however, it requires additional memory outside the HashTable instance.

For example, if we use separate chaining in the code we used to do some testing in the previous topic and represented it in a diagram, this would be the output (the values have been omitted from the diagram to simplify it):



At position **5**, we would have a `LinkedList` instance with four elements in it, at positions **7**, and **10**, we would have `LinkedList` instances with two elements in it, and at positions **4**, **8**, and **9**, we would have `LinkedList` instances with a single element in it.

For separate chaining and linear probing, we need to replace three methods: `put`, `get`, and `remove`. These three methods will be different for each different technique we decide to implement.

As usual, let's start declaring the basic structure of the `HashTableSeparateChaining`:

```
class HashTableSeparateChaining {  
    constructor(toStrFn = defaultToString) {  
        this.toStrFn = toStrFn;  
        this.table = {};  
    }  
}
```

The put method

Let's implement the first method, the `put` method, as follows:

```
put(key, value) {  
    if (key != null && value != null) {  
        const position = this.hashCode(key);  
        if (this.table[position] == null) { // {1}  
            this.table[position] = new LinkedList(); // {2}  
        }  
        this.table[position].push(new ValuePair(key, value)); // {3}  
        return true;  
    }  
    return false;  
}
```

In this method, we will verify whether the position we are trying to add the value to already has other values in it ({1}). If this is the first time we are adding an element in this position, we will initialize it with an instance of the `LinkedList` class ({2} - which we learned in Chapter 6, *Linked Lists*). Then, we will add the `ValuePair` instance to the `LinkedList` instance using the `push` method ({3}), which we also implemented in Chapter 6, *Linked Lists*.

The get method

Next, we will implement the `get` method to retrieve a value given a key with the following code:

```
get(key) {  
    const position = this.hashCode(key);  
    const linkedList = this.table[position]; // {1}  
    if (linkedList != null && !linkedList.isEmpty()) { // {2}  
        let current = linkedList.getHead(); // {3}  
        while (current != null) { // {4}  
            if (current.element.key === key) { // {5}  
                return current.element.value; // {6}  
            }  
            current = current.next; // {7}  
        }  
    }  
    return undefined; // {8}  
}
```

The first verification we need to do is to check whether there is any value at the desired position. To do this, we retrieve the `linkedList` at the hash position ({1}) and we verify whether there is an instance of the `linkedList` or if it is empty ({2}). If there is no value, we return `undefined` to represent that the value was not found in the `HashTable` instance ({8}). If there is an object in the position, we know that the instance of this object is a `LinkedList` instance. Now, all we have to do is search for the `element` we want to find by iterating through the list. To do so, we need to get the reference of the head of the list ({3}), which is the first `element` of the `linkedList`, and then we can iterate through it until we find the end of the list ({4}, in the last iteration `current.next` will be `null`).

The Node of `linkedList` contains the `next` pointer and the `element` properties. The `element` property is an instance of `ValuePair`, so it has the `value` and `key` properties. To access the `key` property of the Node of `LinkedList`, we can use the `current.element.key` and compare it to see whether it is the `key` we are searching for ({5}). If it is the same `key` attribute, we must return the `Node` value ({6}), and if not, we should continue iterating through the list by going to the next `element` of the list ({7}). This logic allows us to search for all `key` attributes at any position of the `LinkedList`.

Another approach for this algorithm is the following: instead of doing the search of the `key` inside the `get` method, we could instantiate the `LinkedList` in the `put` method, passing a custom `equalsFn` to the `LinkedList` constructor that compares only the `key` property of the element (which is an instance of `ValuePair`). Just so we remember, by default, the `LinkedList` will use the `==` operator to compare its `element` instances, meaning it will compare the reference of the `ValuePair` instance. In this case, in the `get` method, we would use the `indexOf` method to search for the desired `key`, which returns a position bigger or equals zero in case the element exists in the `LinkedList`. With the position, we can use the `getElementAt` to retrieve the `ValuePair` instance from the `LinkedList`.

The remove method

Removing a value from the `HashTableSeparateChaining` instance is a little bit different from the `remove` method we implemented earlier in this chapter. Now that we are using `LinkedList`, we need to remove the `element` from `LinkedList`. Let's take a look at the `remove` method implementation:

```
remove(key) {
    const position = this.hashCode(key);
    const linkedList = this.table[position];
    if (linkedList != null && !linkedList.isEmpty()) {
        let current = linkedList.getHead();
        while (current != null) {
            if (current.element.key === key) { // {1}
                linkedList.remove(current.element); // {2}
                if (linkedList.isEmpty()) { // {3}
                    delete this.table[position]; // {4}
                }
                return true; // {5}
            }
            current = current.next; // {6}
        }
    }
    return false; // {7}
}
```

In the `remove` method, we will do the same thing we did in the `get` method to find the element we are looking for. When iterating through the `LinkedList` instance, if the current element in the list is the key we are looking for ({1}), we will use the `remove` method to remove the element from `LinkedList` ({2}). Then, we will perform an additional validation: if the list is empty ({3}, there are no elements in it anymore), we will remove the position from the table using the `delete` operator ({4}), so we can skip this position whenever we look for an element. Finally, we will return `true` to indicate that the element was removed ({5}), or we will return `false` at the end to indicate that the element was not present in `HashTableSeparateChaining` ({7}). If it is not the element we are looking for, then we iterate to the next `LinkedList` element ({6}), as we did for the `get` method.

By replacing these three methods, we have a `HashTableSeparateChaining` instance with a separate chaining technique to handle collisions.

Linear probing

Another technique of collision resolution is **linear probing**. It is called linear because the collision is handled in a way the values will be stored directly in the table, not in a separate data structure.

When we try to add a new element, if the position of the hash is already occupied, then we will try position +1. If position +1 is occupied, then we will try position + 2, and so on, until we find a free position in the hash table. Let's imagine we have a hash table with some values already in it and we want to add a new key and value. We calculate the hash for this new key and we check whether the position for the hash is already occupied. If it is not occupied, we add the value in the correct position. If it is occupied, then we iterate the hash until we find a free spot.

The following diagram demonstrates this process:

#1: add **Jamie** - hash 5

index	key-value	hash
4	Ygritte	4
5	Jonathan	5
6		
7	Jack	7
8	Jasmine	8
9	Jake	9
10	Nathan	10
11		

#2: add **Athelstan** - hash 7

index	key-value	hash
4	Ygritte	4
5	Jonathan	5
6	Jamie	5
7	Jack	7
8	Jasmine	8
9	Jake	9
10	Nathan	10
11		

When we remove a key-value from the hash table, it is not enough to simply remove the element from the position which we implemented in the previous data structures of this chapter. If we only remove the element, it might result in finding an empty spot when searching for another element with the same hash (position), resulting in a bug in the algorithm.

There are two options for the linear probing technique. The first one is the *soft delete* approach. We use a special value (flag) to indicate that the key-value was deleted (*lazy or soft deletion*) instead of actually deleting the element. However, over time, the hash table will be manipulated and we might end up with a hash table with several deleted spots. This will gradually deteriorate the hash table's efficiency, as searching for key-values will become slower over time. To be able to quickly access and find a key is one of the main reasons we would use a hash table. The following diagram demonstartes this process:

index	key-value	hash	
4	Ygritte	4	
5	Deleted		# find Athelstan - hash 7
6	Deleted		Deleted, go to next position
7	Deleted		Occupied, and not the key, go to next position
8	Jasmine	8	Deleted, go to next position
9	Deleted		Deleted, go to next position
10	Deleted		Deleted, go to next position
11	Athelstan	7	Found it!

The second approach requires verifying whether it is necessary to move one or more elements to a backward position. When searching for a key, this approach prevents finding an empty spot, but if it is necessary to move elements, this means we will need to shift key-values within the hash table. The following diagram exemplifies this process:

index	key-value	hash
4	Ygritte	4
5	Jonathan	5
6	Jamie	5
7	Jack	7
8	Jasmine	8
9	Jake	9
10	Nathan	10
11	Athelstan	7
12	Sue	5
13	Aethelwulf	5
14	Sargeras	10
15		



Both approaches have their pros and cons. For this chapter, we will implement the second approach (move one or more elements to a backward position). To check the implementation of the lazy deletion approach (`HashTableLinearProbingLazy` class), please refer to the source code of this book. The download link for the source code is mentioned in the *Preface* of the book, or it can also be accessed at <http://github.com/loiane/javascript-datastructures-algorithms>.

The put method

Let's go ahead and implement the three methods we need to overwrite. The first one will be the `put` method, as follows:

```
put(key, value) {
    if (key != null && value != null) {
        const position = this.hashCode(key);
        if (this.table[position] == null) { // {1}
            this.table[position] = new ValuePair(key, value); // {2}
        } else {
            let index = position + 1; // {3}
            while (this.table[index] != null) { // {4}
                index++; // {5}
            }
            this.table[index] = new ValuePair(key, value); // {6}
        }
        return true;
    }
    return false;
}
```

As usual, we will start by getting the hash `position` generated by the `hashCode` method. Next, we will verify that the `position` has an element in it ({1}). If not (this is the easiest scenario), we will add the element to it ({2} - which is an instance of the `ValuePair` class).

If the `position` is already occupied, we need to find the next `position` that is free (`position` is `undefined` or `null`), so we will create an `index` variable and assign `position + 1` to it ({3}). Then, we will verify whether the `position` is occupied ({4}), and if it is, we will increment `index` ({5}) until we find a `position` that is not occupied. After the `while` loop, the `index` will point to a free position. Then, all we have to do is assign the value we want to this `position` ({6}).



In some languages, we need to define the size of the array. One of the concerns of using linear probing is when the array is out of available positions. When the algorithm reaches the end of the array, it needs to loop back to its beginning and continue iterating its elements - and if necessary, we also need to create a new bigger array and copy the elements to the new array. We do not need to worry about this in JavaScript as we do not need to define a size for the array (and we are using an associative array), and it can grow as needed automatically. This is part of JavaScript's built-in functionality.

Let's simulate the insertions in the hash table:

1. We will try to insert Ygritte. The hash value is 4, and since the hash table was just created, position 4 is empty, so we can insert the name here.
2. We will try to insert Jonathan at position 5. It is also empty, so we can insert the name.
3. We will try to insert Jamie at position 5, which also has a hash value of 5. Position 5 is already occupied by Jonathan, so we need to go to position + 1 ($5 + 1$). Position 6 is free, so we can insert Jamie at 6.
4. We will try to insert Jack at position 7. It is empty, so we can insert the name, no collisions.
5. We will try to insert Jasmine at position 8. It is empty, so we can insert the name, no collisions.
6. We will try to insert Jake at position 9. It is empty, so we can insert the name, no collisions.
7. We will try to insert Nathan at position 10. It is empty, so we can insert the name, no collisions.
8. We will try to insert Athelstan at position 7. Position 7 is already occupied by Jack, so we need to go to position + 1 ($7 + 1$). Position 8 is also not free, so we iterate until the next free position, which is 11, and insert Athelstan.
9. We will try to insert Sue at position 5. 5 to 11 are all occupied, so we go to position 12 and insert Sue.
10. We will try to insert Aethelwulf at position 5. 5 to 12 are all occupied, so we go to position 13 and insert Aethelwulf.
11. We will try to insert Sargeras at position 10. 10 to 13 are all occupied, so we go to position 14 and insert Sargeras.

The get method

Now that we have added our elements, let's implement the `get` function so that we can retrieve their values, as follows:

```
get(key) {
    const position = this.hashCode(key);
    if (this.table[position] != null) { // {1}
        if (this.table[position].key === key) { // {2}
            return this.table[position].value; // {3}
        }
        let index = position + 1; // {4}
        while (this.table[index] != null && this.table[index].key !== key) { //
{5}
            index++;
        }
        if (this.table[index] != null && this.table[index].key === key) { // //
{6}
            return this.table[position].value; // {7}
        }
    }
    return undefined; // {8}
}
```

To retrieve a key's value, we first need to verify whether the key exists ({1}). If it does not exist, it means that the value is not in the hash table, so we can return `undefined` ({8}). If it does exist, we need to check whether the value we are looking for is the one at the original hash position ({2}). If positive, we will simply return its value ({3}).

If not, we will iterate through the `HashTableLinearProbing` elements starting for the next hash position ({4}). We will continue searching the increasing positions of the `HashTableLinearProbing` instance until we find a position that contains an element that is the element we are looking for, or we find an empty spot ({5}). When we get out of the `while` loop, we verify whether the element's key matches the key we are searching for ({6}), and if positive, we will return its value ({7}). If after we iterate through the table the `index` position is `undefined` or `null`, it means the key does not exist and we return `undefined` ({8}).

The remove method

The `remove` method is very similar to the `get` method, and it is declared as follows:

```
remove(key) {
    const position = this.hashCode(key);
    if (this.table[position] != null) {
```

```

        if (this.table[position].key === key) {
            delete this.table[position]; // {1}
            this.verifyRemoveSideEffect(key, position); // {2}
            return true;
        }
        let index = position + 1;
        while (this.table[index] != null && this.table[index].key !== key) {
            index++;
        }
        if (this.table[index] != null && this.table[index].key === key) {
            delete this.table[index]; // {3}
            this.verifyRemoveSideEffect(key, index); // {4}
            return true;
        }
    }
    return false;
}

```

In the `get` method, when we find the `key` we are looking for, we return its value. In the `remove` method, we will `delete` the element from the hash table. We can find the element directly in the original hash `position` ({1}) or in a different spot if the collision has handled ({3}). Since we do not know if there are more elements with the same hash in a different `position`, we need to verify whether the removal has any side effects. If so, we need to move the collided element to a backward `position` so we do not end up with empty spots ({2} and {4}). To do so, we will create a helper method with this logic, which is declared as follows:

```

verifyRemoveSideEffect(key, removedPosition) {
    const hash = this.hashCode(key); // {1}
    let index = removedPosition + 1; // {2}
    while (this.table[index] != null) { // {3}
        const posHash = this.hashCode(this.table[index].key); // {4}
        if (posHash <= hash || posHash <= removedPosition) { // {5}
            this.table[removedPosition] = this.table[index]; // {6}
            delete this.table[index];
            removedPosition = index;
        }
        index++;
    }
}

```

The `verifyRemoveSideEffect` method received two parameters: the key that was removed and the position in which the key was removed. First, we will retrieve the hash of the key that was removed ({1} - we could also pass this value as a parameter to this method). Then, we will start iterating the table starting from the next position ({2}) until we find an empty spot ({3}). When a free spot is found, it means the elements are in place and no moves (or more moves) are necessary. While iterating the following elements, we need to calculate the hash for the element of the current position ({4}). If the hash of the current element is lesser or equal to the original hash ({5}) or if the hash of the current element is lesser or equal to the `removedPosition` (which is the hash of the last removed key), it means we need to move the current element to the `removedPosition` ({6}). Doing so, we can delete the current element (since it was copied to the `removedPosition`). We also need to update the `removedPosition` to the current index, and we repeat the process.

Let's consider the hash table we created to exemplify the `put` method. Suppose we want to remove Jonathan from the hash table. Let's simulate this removal in the hash table:

1. We will find and remove Jonathan from position 5. 5 is now free. We will verify the side effects.
2. We go to position 6 where we stored Jamie, also with hash 5. His hash $5 \leq$ hash 5, so we will copy Jamie to position 5 and delete Jamie. Position 6 is now free and we will verify the next position.
3. We go to position 7 where we stored Jack with hash 7. His hash $7 > 5$, and $7 > 6$, so there's no need to move him. The next position is also occupied, so we will verify the next position.
4. We go to position 8 where we stored Jasmine with hash 8. hash $8 > 5$ of Jasmine, and $8 > 6$, so there's no need to move her. The next position is also occupied, so we will verify the next position.
5. We go to position 9 where we stored Jake with hash 9. His hash $9 > 5$, and $9 > 6$, so there's no need to move him. The next position is also occupied, so we will verify the next position.
6. We will repeat this same process until position 12.
7. We go to position 12 where we stored Sue with hash 5. Her hash $5 \leq 5$, and $5 \leq 6$, so we will copy Sue to position 6 and delete Sue at position 12. Position 12 is now free. The next position is also occupied, so we will verify the next position.

8. We go to position 13 where we stored Aethelwulf with hash 5. His hash $5 \leq \text{hash} \leq \text{removedPosition}$ 12, so we will copy Aethelwulf to position 12 and delete position 13. Position 13 is now free. The next position is also occupied, so we will verify the next position.
9. We go to position 14 where we stored Sargeras with hash $10 > \text{hash} \leq \text{removedPosition}$ 13, but $\text{hash} 10 \leq \text{removedPosition}$ 13, so we will copy Sargeras to position 13 and delete position 14. Position 14 is now free. The next position is free, so the execution is completed.

Creating better hash functions

The lose-lose hash function we implemented is not a good hash function, as we have concluded (too many collisions). We would have multiple collisions if we used this function. A good hash function is composed of certain factors: the time to insert and retrieve an element (performance) and also a low probability of collisions. We can find several different implementations on the internet, or we can create our own.

Another simple hash function that we can implement and which is better than the lose-lose hash function is djb2, which is as follows:

```
djb2HashCode(key) {
  const tableKey = this.toStrFn(key); // {1}
  let hash = 5381; // {2}
  for (let i = 0; i < tableKey.length; i++) { // {3}
    hash = (hash * 33) + tableKey.charCodeAt(i); // {4}
  }
  return hash % 1013; // {5}
}
```

After transforming the key to a string ({1}), the `djb2HashCode` method consists of initializing the `hash` variable with a prime number ({2}, most implementations use 5381); then, we will iterate each character of the string that represents the key ({3}), multiply the `hash` value by 33 (used as a magical number), and sum it with the ASCII value of the character ({4}).

Finally, we will use the rest of the division of the total by another random prime number ({5}), greater than the size we think the `HashTable` instance can have. In our scenario, let's consider 1,000 as the size.

If we run the inserts from the *linear probing* section again, this will be the result we will get using `djb2HashCode` instead of `loseloseHashCode`:

```
807 - Ygritte
288 - Jonathan
962 - Jamie
619 - Jack
275 - Jasmine
877 - Jake
223 - Nathan
925 - Athelstan
502 - Sue
149 - Aethelwulf
711 - Sargeras
```

No collisions!

This is not the best hash function that exists, but it is one of the most highly recommended hash functions by the community.



There are also a few techniques to create hash functions for numeric keys.
You can find a list and implementations at: <http://goo.gl/VtdN2x>.

The ES2015 Map class

ECMAScript 2015 introduced a `Map` class as part of the JavaScript API. We developed our `Dictionary` class based on the ES2015 `Map` class.



You can take a look at the details of the ECMAScript 2015 `Map` class implementation
at: https://developer.mozilla.org/en-US/docs/Web/JavaScript/Reference/Global_Objects/Map (or <http://goo.gl/dm8VP6>).

Let's learn how we can use the native `Map` class, as well. Let's use the same examples we used to test our `Dictionary` class:

```
const map = new Map();

map.set('Gandalf', 'gandalf@email.com');
map.set('John', 'johnsnow@email.com');
map.set('Tyrion', 'tyrion@email.com');
```

```
console.log(map.has('Gandalf')); // true
console.log(map.size); // 3
console.log(map.keys()); // MapIterator {"Gandalf", "John", "Tyrion"}
console.log(map.values()); // MapIterator {"gandalf@email.com",
"johnsnow@email.com", "tyrion@email.com"}
console.log(map.get('Tyrion')); // tyrion@email.com
```

The difference between our `Dictionary` class and the ES2015 `Map` class is that the `values` and `keys` methods return an `Iterator` (which we learned in Chapter 3, *Arrays*) instead of the array with the values or the keys. Another difference is that we developed a `size` method to return the number of values the map is storing. The ES2015 `Map` class has a property named `size`.

We can also call the `delete` method to remove an element from the map, as follows:

```
map.delete('John');
```

The `clear` method also resets the `map` data structure. This is the same functionality we implemented in the `Dictionary` class.

The ES2015 WeakMap and WeakSet classes

Along with the two new data structures `Set` and `Map`, ES2015 also introduced a weak type version of these classes: `WeakMap` and `WeakSet`.

Basically, the only difference between the `Map` or `Set` classes and their weak versions are:

- The `WeakSet` or `WeakMap` classes do not have the `entries`, `keys`, and `values` methods
- It is only possible to use objects as keys

The reason for creating and using these two classes is performance-related. Since `WeakSet` and `WeakMap` are weakly typed (using the object as a key), there is no strong reference to the keys. This behavior allows the JavaScript garbage collector to clean an entire entry from the map or set.

Another advantage of the weak versions is we can only retrieve a value if you have its key. Since these classes do not have the iterator methods (`entries`, `keys`, and `values`), there is no way to retrieve a value unless you know what the key is. This confirms our choice in using the `WeakMap` class to encapsulate the private properties of the ES2015 classes, as we learned in Chapter 4, *Stacks*.

The following code is an example of what we can do with the `WeakMap` class:

```
const map = new WeakMap();

const ob1 = { name: 'Gandalf' }; // {1}
const ob2 = { name: 'John' };
const ob3 = { name: 'Tyrion' };

map.set(ob1, 'gandalf@email.com'); // {2}
map.set(ob2, 'johnsnow@email.com');
map.set(ob3, 'tyrion@email.com');

console.log(map.has(ob1)); // true {3}
console.log(map.get(ob3)); // tyrion@email.com {4}
map.delete(ob2); // {5}
```

We can still use the `set` method of the `WeakMap` class ({2}). However, since it does not allow us to use string or any other primitive datatype (numeric, string, or boolean values), we need to transform the name into an object ({1}).

To search for a specific value ({3}), retrieve it ({4}), and also delete it ({5}), we need to pass the created object as a key.

The same logic is applied to the `WeakSet` class.

Summary

In this chapter, we learned about dictionaries and how to add, remove, and get elements, among other methods. We also learned the difference between a dictionary and a set.

We covered hashing, how to create a hash table (or hash map) data structure, how to add, remove, and get elements, and also how to create hash functions. We learned how to handle collisions in a hash table using two different techniques.

We also covered how to use the ES2015 `Map` class as well as the `WeakMap` and `WeakSet` classes.

In the next chapter, we will learn a new data structure called tree.

9 Recursion

In previous chapters, we learned about different iterative data structures. Starting with next chapter, we will start using a special method to make it easier to write the algorithms used to access the **tree** and **graph** data structures, which is **recursion**. But before we start diving into trees and graphs, we need to understand how recursion works.

In this chapter, we will cover:

- Understanding recursion
- Calculating the factorial of a number
- The Fibonacci sequence
- JavaScript call stack

Understanding recursion

There is a famous programming wisdom quote that says:

“To understand recursion, one must first understand recursion.”

- Unknown

Recursion is a method to solve problems that consist of solving smaller portions of the same problem until you solve the original, larger problem. It usually involves calling the function itself.

A method or function is recursive if it can call itself directly, as follows:

```
function recursiveFunction(someParam) {  
    recursiveFunction(someParam);  
}
```

A function is also called recursive if it can call itself indirectly, as follows:

```
function recursiveFunction1(someParam) {
    recursiveFunction2(someParam);
}

function recursiveFunction2(someParam) {
    recursiveFunction1(someParam);
}
```

Suppose we have to execute `recursiveFunction`. What would the result be? In this case, it would be executed indefinitely. For this reason, every recursive function must have a **base case**, which is a condition in which no recursive call is made (a **stopping point**) to prevent infinite recursion.

Going back to the mentioned programming wisdom, by understanding what recursion is, we solve the original problem. If we translate this programming wisdom into JavaScript code, we can write it as follows:

```
function understandRecursion(doIunderstandRecursion) {
    const recursionAnswer = confirm('Do you understand recursion?');
    if (recursionAnswer === true) { // base case or stop point
        return true;
    }
    understandRecursion(recursionAnswer); // recursive call
}
```

The `understandRecursion` function will keep calling itself until the `recursionAnswer` is yes (`true`). Having the `recursionAnswer` as yes is the base case in the preceding code.

Let's take a look at some famous recursive algorithms in the following section.

Calculating the factorial of a number

For our first example of recursion, let's take a look at how to compute the factorial of a number. A factorial of a number, n , is defined by $n!$ and it is the result of multiplying the numbers from 1 to n .

The factorial of 5 is represented by $5!$ and it is equal to $5 * 4 * 3 * 2 * 1$, resulting in 120.

Iterative factorial

If we try to represent the steps to compute the factorial of any number n , we can define the steps as follows: $(n) * (n - 1) * (n - 2) * (n - 3) * \dots * 1$.

We can write a function to compute the factorial of a number using a loop as demonstrated:

```
function factorialIterative(number) {
  if (number < 0) return undefined;
  let total = 1;
  for (let n = number; n > 1; n--) {
    total = total * n;
  }
  return total;
}
console.log(factorialIterative(5)); // 120
```

We can start computing the factorial starting at the given number, and decrease n until it has a value of 2 since the factorial of 1 is 1 and it is already included in the `total` variable. The factorial of zero is also 1. The factorial of negative numbers will not be computed.

Recursive factorial

Now, let's try rewriting the `factorialIterative` function using recursion. But first, let's define all the steps using a recursive definition.

The factorial of 5 is computed by $5 * 4 * 3 * 2 * 1$. The factorial of 4 ($n - 1$) is computed by $4 * 3 * 2 * 1$. Computing $(n - 1)$ is a subproblem we solve to compute $n!$, which is the original problem, so we can define the factorial of 5 as follows:

1. `factorial(5) = 5 * factorial(4)`: We can compute $5!$ as $5 * 4!$.
2. `factorial(5) = 5 * (4 * factorial(3))`: We need to solve the subproblem of computing $4!$, which we can compute as $4 * 3!$.
3. `factorial(5) = 5 * 4 * (3 * factorial(2))`: We need to solve the subproblem of computing $3!$, which we can compute as $3 * 2!$.
4. `factorial(5) = 5 * 4 * 3 * (2 * factorial(1))`: We need to solve the subproblem of computing $2!$, which we can compute as $2 * 1!$.
5. `factorial(5) = 5 * 4 * 3 * 2 * (1)`: We need to solve the subproblem of computing $1!$.
6. `factorial(1)` or `factorial(0)` returns 1. $1!$ is equal to 1. We could also say that $1! = 1 * 0!$ and $0!$ is also 1.

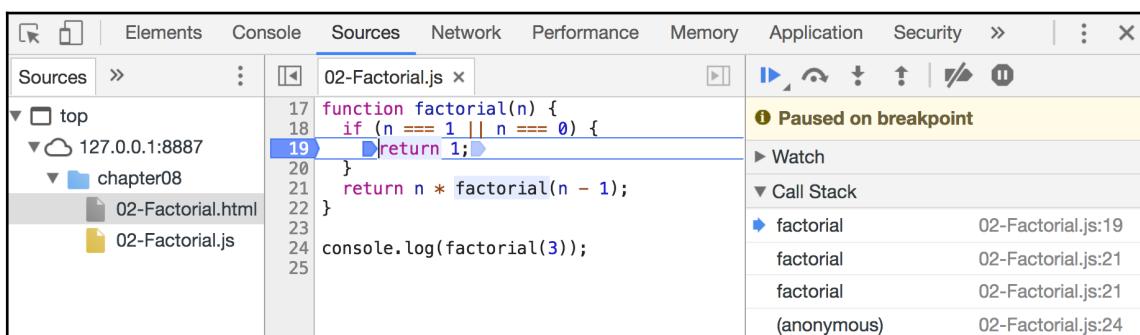
The factorial function using recursion is declared as follows:

```
function factorial(n) {
  if (n === 1 || n === 0) { // base case
    return 1;
  }
  return n * factorial(n - 1); // recursive call
}
console.log(factorial(5)); // 120
```

The call stack

We learned about the stack data structure in [Chapter 4, Stacks](#). We will see it in action in a real application using recursion. Whenever a function is called by an algorithm, the function goes on the top of the **call stack**. When using recursion, each function call will be stacked on top of each other, due to the possibility of one call depending on the result of the previous invocation itself.

We can see the **Call Stack** in action using the browser, as demonstrated in the following screenshot:



If we execute `factorial(3)`, open the developer tools of the browser, go to **Sources**, and add a breaking point in the `Factorial.js` file, when `n` has a value of 1, we will be able to see the **Call Stack** with three calls to the `factorial` function. If we continue the execution, we will also see that as a result of `factorial(1)` being returned, the **Call Stack** will start to pop the `factorial` calls.

We can also add `console.trace()` at the beginning of the function to see the result in the browser's console as well:

```
function factorial(n) {
  console.trace();
  // function logic
}
```

When `factorial(3)` is evoked, we will get the following output in the console:

```
factorial @ 02-Factorial.js:18
(anonymous) @ 02-Factorial.js:25 // console.log(factorial(3)) call
```

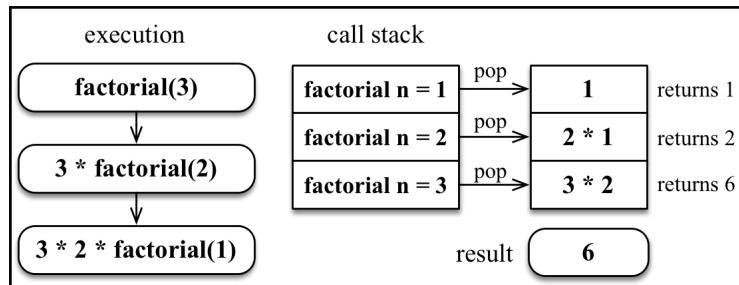
When `factorial(2)` is evoked, we will get the following output in the console:

```
factorial @ 02-Factorial.js:18
factorial @ 02-Factorial.js:22 // factorial(3) is waiting factorial(2)
(anonymous) @ 02-Factorial.js:25 // console.log(factorial(3)) call
```

Finally, when `factorial(1)` is evoked, we will get the following output in the console:

```
factorial @ 02-Factorial.js:18
factorial @ 02-Factorial.js:22 // factorial(2) is waiting factorial(1)
factorial @ 02-Factorial.js:22 // factorial(3) is waiting factorial(2)
(anonymous) @ 02-Factorial.js:25 // console.log(factorial(3)) call
```

We can represent the steps executed and the actions in the call stack in the following diagram:



When `factorial(1)` returns 1, the stack will start to pop the calls, returning the results until `3 * factorial(2)` is computed.

JavaScript limitation on the call stack size

What happens when we forget to add a base case to stop the recursive calls of a function? It will not be executed indefinitely; the browser will throw an error, which is known as a **stack overflow error**.

Each browser has its own limitations, and we can use the following code to do some testing:

```
let i = 0;
function recursiveFn() {
    i++;
    recursiveFn();
}

try {
    recursiveFn();
} catch (ex) {
    console.log('i = ' + i + ' error: ' + ex);
}
```

In **Chrome version 65**, the function is executed 15,662 times, and the browser throws the error `RangeError: Maximum call stack size exceeded`. In **Firefox version 59**, the function is executed 188,641 times, and the browser throws the error `InternalError: too much recursion`. In **Edge version 41**, the function is executed 17,654 times.



Depending on your operating system and browser, the values might be different, but they will be close.

ECMAScript 2015 has **tail call optimization**. If a function call is the last action inside a function (in our example, the highlighted line), and it is handled via a “jump”, not via a “subroutine call”. This means that our code can be executed forever in ECMAScript 2015. This is why it is very important to have a base case to stop the recursion.



For more information about tail call optimization, visit <https://goo.gl/3Rxq7L>.

The Fibonacci sequence

The **Fibonacci sequence** is another problem that we can solve using recursion. It is a series of the numbers 0, 1, 1, 2, 3, 5, 8, 13, 21, 34, and so on. The number 2 is found by adding 1 + 1. The number 3 is found by adding 1 + 2, 5 is found by adding 2 + 3, and so on! The Fibonacci sequence can be defined as follows:

1. The Fibonacci number at position 0 is 0.
2. The Fibonacci number at position 1 or 2 is 1.
3. The Fibonacci number at position n (for $n > 2$) is the Fibonacci of $(n - 1)$ + Fibonacci of $(n - 2)$.

Iterative Fibonacci

We implement the `fibonacci` function in an iterative way, as follows:

```
function fibonacciIterative(n) {  
    if (n < 1) return 0;  
    if (n <= 2) return 1;  
  
    let fibNMinus2 = 0;  
    let fibNMinus1 = 1;  
    let fibN = n;  
    for (let i = 2; i <= n; i++) { // n >= 2  
        fibN = fibNMinus1 + fibNMinus2; // f(n-1) + f(n-2)  
        fibNMinus2 = fibNMinus1;  
        fibNMinus1 = fibN;  
    }  
    return fibN;  
}
```

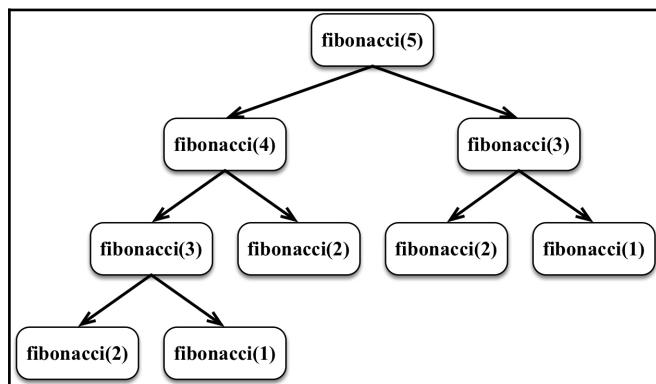
Recursive Fibonacci

The `fibonacci` function can be written as follows:

```
function fibonacci(n){  
    if (n < 1) return 0; // {1}  
    if (n <= 2) return 1; // {2}  
    return fibonacci(n - 1) + fibonacci(n - 2); // {3}  
}
```

In the preceding code, we have the base cases ({1} and {2}) and the logic to compute the Fibonacci for $n > 2$ ({3}).

If we try to find the `fibonacci(5)`, the following will be the result of the calls that are made:



Fibonacci with memoization

There is also a third approach, called **memoization**, that we can use to write the `fibonacci` function. Memoization consists of an optimization technique that stores the values of previous results, similar to a cache. If we analyze the calls made to compute `fibonacci(5)`, we will notice that `fibonacci(3)` was computed twice, so we can store its result so that when we compute it again, we already have it.

The following code represents the `fibonacci` function written with memoization:

```

function fibonacciMemoization(n) {
  const memo = [0, 1]; // {1}
  const fibonacci = (n) => {
    if (memo[n] != null) return memo[n]; // {2}
    return memo[n] = fibonacci(n - 1, memo) + fibonacci(n - 2, memo); // {3}
  };
  return fibonacci;
}
  
```

In the preceding code, we are declaring a `memo` array that will cache all the computed results ({1}). If the result has been computed, we return it ({2}), otherwise, we compute the result and add it to the cache ({3}).

Why use recursion? Is it faster?

Let's run a benchmark between the three different `fibonacci` functions we wrote in this chapter:

Test		Ops/sec
Iterative	<code>fibonacciIterative(25)</code>	38,699,512 ±2.11% fastest
Recursive	<code>fibonacci(25)</code>	1,420 ±1.01% 100% slower
Memoization	<code>fibonacciMemoization(25)</code>	27,697,365 ±3.16% 29% slower

The **Iterative** version is much faster than the **Recursive** versions, so this means recursion is slower. However, take another look at the code of the three different versions. Recursion is easier to understand, and it usually requires less code as well. Also, for some algorithms, an **Iterative** solution may not even be available, and with tail call elimination, the recursion penalty may even be removed.

So, we usually use recursion because it is easier to solve problems using it.



The `fibonacci` function tests are available at <https://jsperf.com/fibonacci-comparison-jsbook>.

Summary

In this chapter, we learned how to write iterative and recursive versions of two famous algorithms: the factorial of a number and the Fibonacci sequence. We learned that in case a recursive algorithm needs to compute the same result more than once, we can use an optimization technique called memoization.

We also compared the performance of the iterative and recursive versions of the Fibonacci algorithm, and we learned that even though the iterative version might be faster, a recursive algorithm is easier to read and understand what it is doing.

In the next chapter, we will learn the tree data structure and we will create the `Tree` class, where most of its methods use recursion.

10 Trees

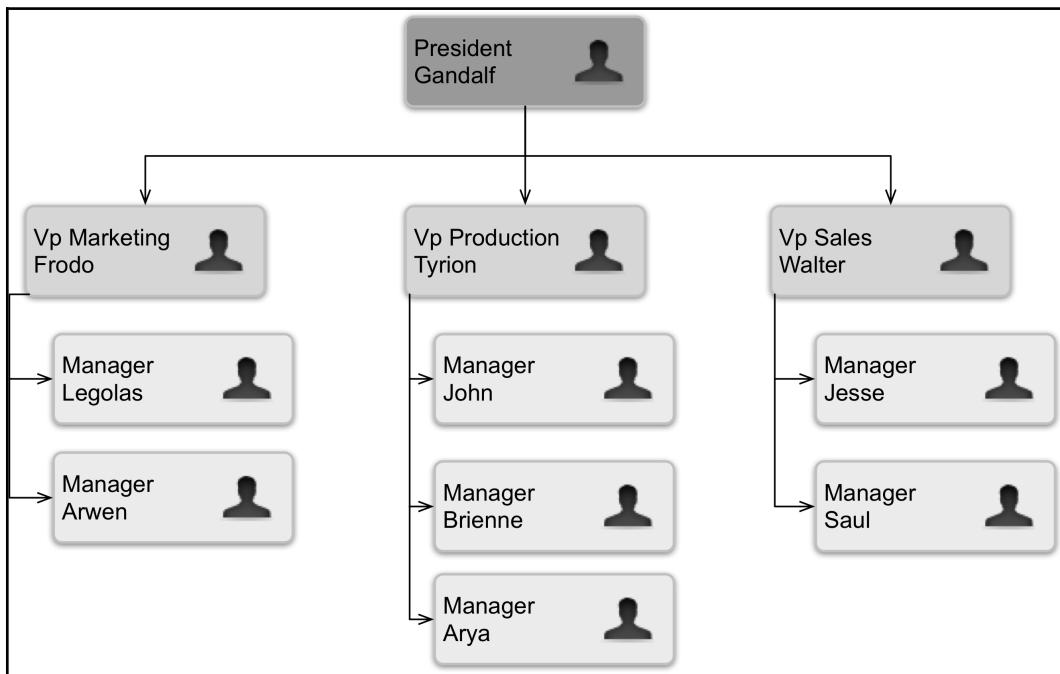
So far in this book, we have covered some sequential data structures. The first non-sequential data structure we covered in this book was the **Hash Table**. In this chapter, you will learn about another non-sequential data structure called a **tree**, which is very useful for storing information that needs to be found easily.

In this chapter, we will cover:

- Tree terminology
- Creating a binary search tree
- Traversing a tree
- Adding and removing nodes
- The AVL tree

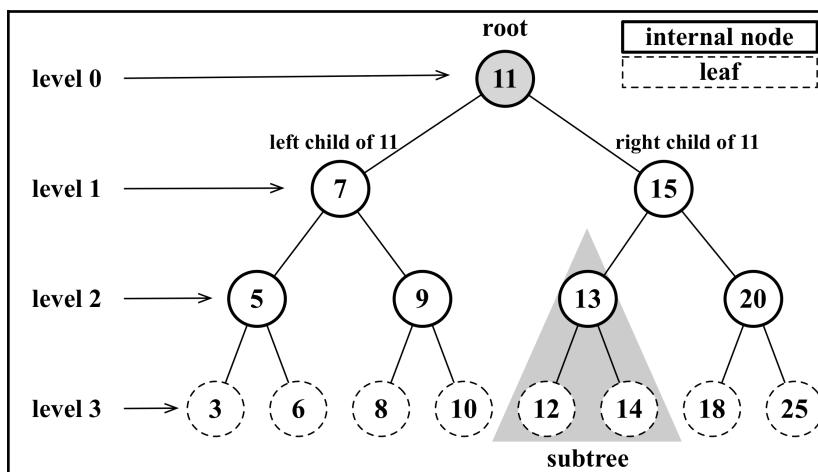
The tree data structure

A tree is an abstract model of a hierarchical structure. The most common example of a tree in real life would be a family tree or a company organizational chart, as we can see in the following figure:



Tree terminology

A tree consists of **nodes** with a parent-child relationship. Each node has a parent (except for the first node at the top) and zero or more children, as in the following figure:



The top node of a tree is called the **root** (11). It is the node that does not have a parent. Each element of the tree is called a node. There are **internal nodes** and **external nodes**. An internal node is a node with at least one child (7, 5, 9, 15, 13, and 20 are internal nodes). A node that does not have children is called an external node or a **leaf** (3, 6, 8, 10, 12, 14, 18, and 25 are leaves).

A node can have ancestors and descendants. The ancestors of a node (except the root) are the parent, grandparent, great-grandparent, and so on. The descendants of a node are children (child), grandchildren (grandchild), great-grandchildren (great-grandchild), and so on. For example, node 5 has 7 and 11 as its ancestors and 3 and 6 as its descendants.

Another terminology used with trees is the **subtree**. A subtree consists of a node and its descendants. For example, the nodes 13, 12, and 14 constitute a subtree from the tree of the preceding diagram.

The depth of a node consists of the number of ancestors. For example, node 3 has a depth of 3 because it has three ancestors (5, 7, and 11).

The height of a tree consists of the maximum depth of any node. A tree can also be broken down into levels. The root is on **level 0**, its children are on **level 1**, and so on. The tree from the preceding diagram has a height of 3 (the maximum depth is 3, as shown in the preceding figure on **level 3**).

Now that we know the most important terms related to trees, we can start learning more about trees.

The binary and binary search trees

A node in a **binary tree** has two children at most: one left child and one right child. This definition allows us to write more efficient algorithms to insert, search, and delete nodes to/from a tree. Binary trees are largely used in computer science.

A **binary search tree (BST)** is a binary tree, but it only allows you to store nodes with lesser values on the left-hand side and nodes with greater values on the right-hand side. The diagram in the previous topic exemplifies a binary search tree.

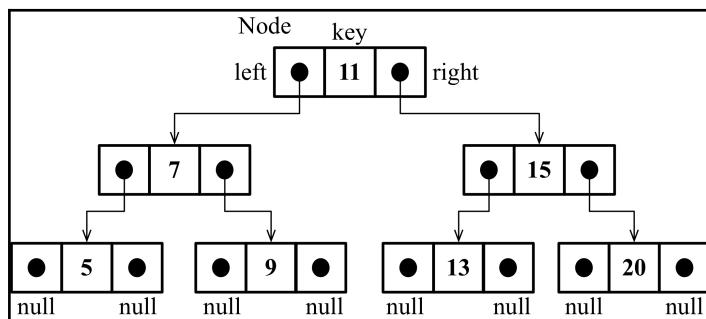
This will be the data structure that we will work on in this chapter.

Creating the Node and BinarySearchTree classes

Let's start by creating our `Node` class that will represent each node of our binary search tree using the following code:

```
export class Node {
  constructor(key) {
    this.key = key; // {1} node value
    this.left = null; // left child node reference
    this.right = null; // right child node reference
  }
}
```

The following diagram exemplifies how a **binary search tree (BST)** is organized in terms of the data structure:



Just as in linked lists, we will work with pointers (references) again to represent the connection between the nodes (called **edges** in tree terminology). When we worked with doubly linked lists, each node had two pointers: one to indicate the next node and another one to indicate the previous node. When working with trees, we will use the same approach, meaning we will also work with two pointers. However, one pointer will point to the **left** child, and the other one will point to the **right** child. For this reason, we will need a **Node** class that will represent each node of the tree. A small detail that is worth noting is that instead of calling the node itself as a node or item, as we did in the previous chapters, we will call it as **key** ({1}). A key is what a tree node is known as in tree terminology.

Next, we will declare the basic structure of our **BinarySearchTree** class:

```
import { Compare, defaultCompare } from '../util';
import { Node } from './models/node';

export default class BinarySearchTree {
  constructor(compareFn = defaultCompare) {
    this.compareFn = compareFn; // used to compare node values
    this.root = null; // {1} root node of type Node
  }
}
```

We will follow the same pattern we used in the **LinkedList** class (from Chapter 6, *Linked Lists*). This means that we will also declare a variable so that we can control the first node of the data structure. In the case of a tree, instead of the **head**, we have the **root** ({1}).

Next, we need to implement some methods. The following are the methods we create in our **BinarySearchTree** class:

- **insert (key)**: This method inserts a new key in the tree
- **search (key)**: This method searches for the key in the tree and returns **true** if it exists and **false** if the node does not exist
- **inOrderTraverse ()**: This method visits all nodes of the tree using in-order traverse
- **preOrderTraverse ()**: This method visits all nodes of the tree using pre-order traverse
- **postOrderTraverse ()**: This method visits all the nodes of the tree using post-order traverse
- **min ()**: This method returns the minimum value/key in the tree
- **max ()**: This method returns the maximum value/key in the tree
- **remove (key)**: This method removes the key from the tree

We will implement each of these methods in the subsequent sections.

Inserting a key into the BST

The methods we will create in this chapter are a little bit more complex than the ones we implemented in previous chapters. We will use a lot of recursion in our methods. If you are not familiar with recursion, please refer to Chapter 9, *Recursion*.

The following code is the first piece of the algorithm used to insert a new key in a tree:

```
insert(key) {  
    if (this.root == null) { // {1}  
        this.root = new Node(key); // {2}  
    } else {  
        this.insertNode(this.root, key); // {3}  
    }  
}
```

To insert a new node (or `key`) into a tree, there are two steps that we need to follow.

The first step is verifying whether the insertion is a special case. The special case for the BST is if the node we are trying to add is the first one in the tree ({1}). If it is, all we have to do is point the `root` to this new node ({2}) by creating an instance of the `Node` class and assigning it to the `root` property. Because of the `Node` constructor properties, we only need to pass the value we want to add to the tree (`key`), and its `left` and `right` pointers will have a `null` value automatically.

The second step is to add the node to a different position than the `root`. In this case, we will need a helper ({3}) method to help us to do this, which is declared as follows:

```
insertNode(node, key) {  
    if (this.compareFn(key, node.key) === Compare.LESS_THAN) { // {4}  
        if (node.left == null) { // {5}  
            node.left = new Node(key); // {6}  
        } else {  
            this.insertNode(node.left, key); // {7}  
        }  
    } else {  
        if (node.right == null) { // {8}  
            node.right = new Node(key); // {9}  
        } else {  
            this.insertNode(node.right, key); // {10}  
        }  
    }  
}
```

```
}
```

The `insertNode` method will help us find out where the correct place to insert a new node is. The following list describes what this method does:

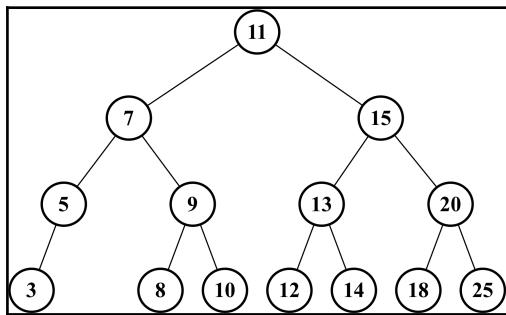
- If the tree is not empty, we need to find a place to add a new node. For this reason, we will call the `insertNode` method by passing the root node and the key we want to insert as parameters ({3}).
- If the node's key is lesser than the current node key (in this case, it is the root ({4})), then we need to check the left child of the node. Note that here, we are using the `compareFn` function that can be passed in the BST class constructor to compare the values since the key can be a complex object instead of a number. If there is no left node ({5}), then we will insert the new key as the left node ({6}). If not, we need to descend a level in the tree by calling `insertNode` recursively ({7}). In this case, the node we will compare next time will be the left child of the current node (left node subtree).
- If the node's key is greater than the current node key and there is no right child ({8}), then we will insert the new key as the right child ({9}). If not, we will also need to call the `insertNode` method recursively, but the new node to be compared will be the right child ({10} - right node subtree).

Let's apply this logic in an example so that we can understand this process better. Consider the scenario—we have a new tree, and we are trying to insert its first key. In this case, we will run the following code:

```
const tree = new BinarySearchTree();
tree.insert(11);
```

In this case, we will have a single node in our tree, and the `root` property will be pointing to it. The code that will be executed is in lines {1} and {2} of our source code.

Now, consider that we already have the following tree:



The code to create the tree seen in the preceding diagram is a continuation of the previous code (in which we inserted the 11 key), as follows:

```
tree.insert(7);
tree.insert(15);
tree.insert(5);
tree.insert(3);
tree.insert(9);
tree.insert(8);
tree.insert(10);
tree.insert(13);
tree.insert(12);
tree.insert(14);
tree.insert(20);
tree.insert(18);
tree.insert(25);
```

We would also like to insert a new key with the value 6, so we will execute the following code as well:

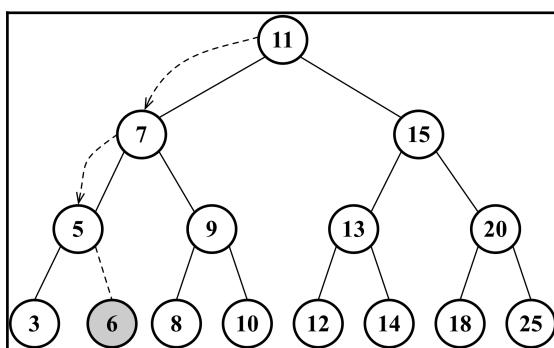
```
tree.insert(6);
```

The following steps will be executed:

1. The tree is not empty, so the code from line {3} will be executed. The code will call the `insertNode` method (`root, key[6]`).
2. The algorithm will check line {4} (`key[6] < root[11]` is `true`), then it will check line {5} (`node.left[7]` is `not null`), and finally, it will go to line {7} by calling `insertNode(node.left[7], key[6])`.

3. We will go inside the `insertNode` method again, but with different parameters. It will check line {4} again (`key[6] < node[7]` is `true`), then it will check line {5} (`node.left[5]` is not `null`), and finally, it will go to line {7} by calling `insertNode(node.left[5], key[6])`.
4. We will go into the `insertNode` method once more. It will check line {4} again (`key[6] < node[5]` is `false`), then it will go to line {8} (`node.right` is `null` — node 5 does not have any right child descendants), and finally, it will execute line {9} by inserting key 6 as the right child of node 5.
5. After this, the stack of method calls will pop up, and the execution will end.

This will be the result after key 6 is inserted in the tree:



Tree traversal

Traversing (or walking) a tree is the process of visiting all the nodes of a tree and performing an operation at each node. However, how should we do this? Should we start from the top of the tree or from the bottom? From the left-hand or the right-hand side? There are three different approaches that can be used to visit all the nodes in a tree: in-order, pre-order, and post-order.

In the following sections, we will dive into the uses and implementations of these three types of tree traversals.

In-order traversal

An **in-order** traversal visits all the nodes of a BST in an ascending order, meaning it will visit the nodes from the smallest to the largest. An application of in-order traversal would be to sort a tree. Let's check out its implementation:

```
inOrderTraverse(callback) {  
    this.inOrderTraverseNode(this.root, callback); // {1}  
}
```

The `inOrderTraverse` method receives a `callback` function as a parameter. This function can be used to perform the action we want to execute when the node is visited (this is known as the visitor pattern; for more information on this, refer to: http://en.wikipedia.org/wiki/Visitor_pattern). Since most of the algorithms we are implementing for the BST are recursive, we will use a helper method that will receive the `root` node of the tree (or subtree) and the `callback` function ({1}). The helper method is listed as follows:

```
inOrderTraverseNode(node, callback) {  
    if (node != null) { // {2}  
        this.inOrderTraverseNode(node.left, callback); // {3}  
        callback(node.key); // {4}  
        this.inOrderTraverseNode(node.right, callback); // {5}  
    }  
}
```

To traverse a tree using the in-order approach, first we need to check whether the tree node that was passed as a parameter is `null` ({2}) - this is the point where the recursion stops being executed, which is the base case of the recursive algorithm).

Next, we will visit the left node ({3}) by evoking the same function recursively. Then, we will visit the root node ({4}) by performing an action with it (`callback`), and then we will visit the right node ({5}).

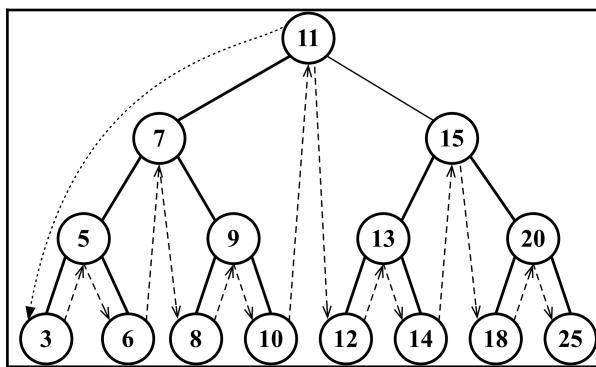
Let's try to execute this method using the tree from the previous topic as an example, as follows:

```
const printNode = (value) => console.log(value); // {6}  
tree.inOrderTraverse(printNode); // {7}
```

First, we need to create a callback function (§ 6). All we will do is print the node's value on the browser's console. Then, we can call the `inOrderTraverse` method by passing our callback function as a parameter (§ 7). When we execute this code, the following will be the output in the console (each number will be an output on a different line):

```
3 5 6 7 8 9 10 11 12 13 14 15 18 20 25
```

The following diagram illustrates the path that the `inOrderTraverse` method followed:



Pre-order traversal

A **pre-order** traversal visits the node prior to its descendants. An application of pre-order traversal could be to print a structured document.

Let's take a look at its implementation:

```
preOrderTraverse(callback) {
    this.preOrderTraverseNode(this.root, callback);
}
```

The `preOrderTraverseNode` method implementation is declared as follows:

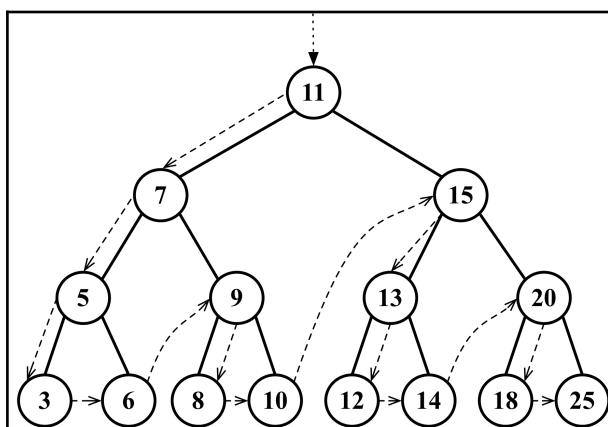
```
preOrderTraverseNode(node, callback) {
    if (node != null) {
        callback(node.key); // {1}
        this.preOrderTraverseNode(node.left, callback); // {2}
        this.preOrderTraverseNode(node.right, callback); // {3}
    }
}
```

The difference between the in-order and pre-order traversals is that the pre-order one visits the root node first (`{1}`), then the left node (`{2}`), and finally the right node (`{3}`), while the in-order traversal executes the lines in the following order: lines `{2}`, `{1}`, and `{3}`.

The following will be the output in the console (each number will be printed on a different line):

```
11 7 5 3 6 9 8 10 15 13 12 14 20 18 25
```

The following diagram illustrates the path followed by the `preOrderTraverse` method:



Post-order traversal

A **post-order** traversal visits the node after it visits its descendants. An application of post-order traversal could be computing the space used by a file in a directory and its subdirectories.

Let's take a look at its implementation:

```
postOrderTraverse(callback) {
    this.postOrderTraverseNode(this.root, callback);
}
```

The `postOrderTraverseNode` implementation is declared as follows:

```
postOrderTraverseNode(node, callback) {
    if (node != null) {
        this.postOrderTraverseNode(node.left, callback); // {1}
        this.postOrderTraverseNode(node.right, callback); // {2}
        callback(node.key); // {3}
    }
}
```

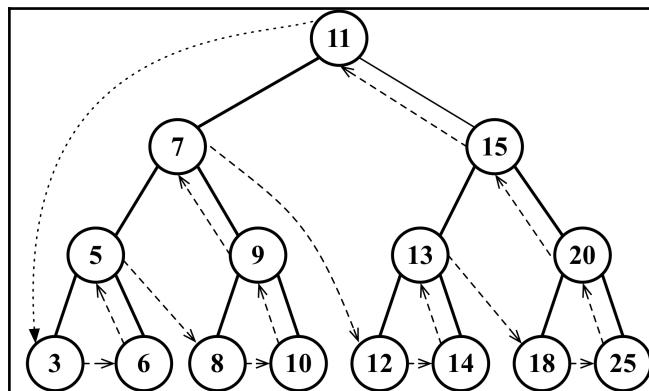
In this case, the post-order traversal will visit the left node ({1}), then the right node ({2}), and finally, the root node ({3}).

The algorithms for the in-order, pre-order, and post-order approaches are very similar; the only thing that changes is the order in which lines {1}, {2}, and {3} are executed in each method.

This will be the output in the console (each number will be printed on a different line):

```
3 6 5 8 10 9 7 12 14 13 18 25 20 15 11
```

The following diagram illustrates the path the `postOrderTraverse` method followed:



Searching for values in a tree

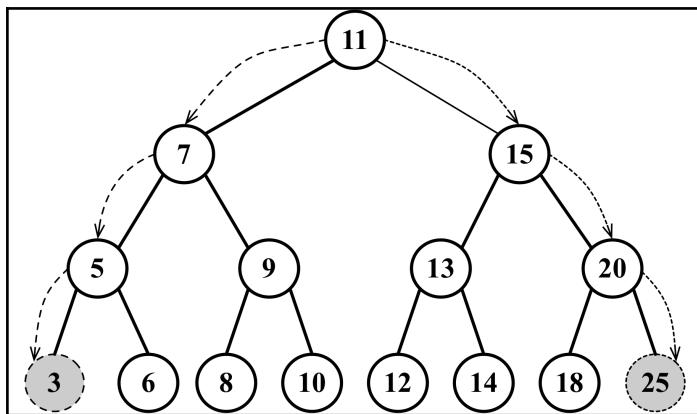
There are three types of searches that are usually performed in trees:

- Searching for minimum values
- Searching for maximum values
- Searching for a specific value

Let's take a look at each one in the following topics.

Searching for minimum and maximum values

Consider the following tree for our examples:



Just looking at the preceding figure, could you easily find the minimum and maximum values of the tree?

If you take a look at the leftmost node in the last level of the tree, you will find the value **3**, which is the lowest key from this tree, and if you take a look at the node that is furthest to the right (also in the last level of the tree), you will find the value **25**, which is the highest key in this tree. This information helps us a lot when implementing methods that will find the minimum and maximum nodes of the tree.

First, let's take a look at the method that will find the minimum key of the tree, as follows:

```
min() {  
    return this.minNode(this.root); // {1}  
}
```

The `min` method will be the method exposed to the user. This method calls the `minNode` method ({1}), which is declared as follows:

```
minNode(node) {  
    let current = node;  
    while (current != null && current.left != null) { // {2}  
        current = current.left; // {3}  
    }  
    return current; // {4}  
}
```

The `minNode` method allows us to find the minimum key starting from any node of the tree. We can use it to find the minimum key from a subtree or from the tree itself. For this reason, we will call the `minNode` method by passing the tree root node ({1}) because we want to find the minimum key of the whole tree.

Inside the `minNode` method, we will traverse the left edge of the tree (lines {2} and {3}) until we find the node at the highest level of the tree (the leftmost end).



The logic used in the `minNode` method is very similar to the code we used to iterate until the last node of a linked list in Chapter 6, *Linked Lists*. The difference here is that we are iterating until we find the leftmost node of the tree.

In a similar way, we also have the `max` method, which looks similar to the following:

```
max() {  
    return this.maxNode(this.root);  
}  
maxNode(node) {  
    let current = node;  
    while (current != null && current.right != null) { // {5}  
        current = current.right;  
    }  
    return current;  
}
```

To find the maximum key, we will traverse the right-hand edge of the tree ({5}) until we find the last node at the right-hand end of the tree.

So, for the minimum value, we will always go to the left-hand side of the tree, and for the maximum value, we will always navigate to the right-hand side of the tree.

Searching for a specific value

In previous chapters, we also implemented the `find`, `search`, and `get` methods to find a specific value in the data structure. We will implement the `search` method for the BST as well. Let's take a look at its implementation:

```
search(key) {  
    return this.searchNode(this.root, key); // {1}  
}  
searchNode(node, key) {  
    if (node == null) { // {2}  
        return false;  
    }  
    if (this.compareFn(key, node.key) === Compare.LESS_THAN) { // {3}  
        return this.searchNode(node.left, key); // {4}  
    } else if (  
        this.compareFn(key, node.key) === Compare.BIGGER_THAN  
    ) { // {5}  
        return this.searchNode(node.right, key); // {6}  
    } else {  
        return true; // {7}  
    }  
}
```

The first thing we need to do is declare the `search` method. Following the pattern of other methods declared for BST, we will use a helper method to help us with the recursion logic ({1}).

The `searchNode` method can be used to find a specific key in the tree or any of its subtrees. This is the reason we will call this method in line {1} by passing the `root` node of the tree as a parameter.

Before we start the algorithm, we will validate that the `node` passed as a parameter is valid (is not `null` or `undefined`). If it is, it means that the key was not found, and it will return `false`.

If the node is not `null`, we need to continue the search. If the key we are looking for is lower than the current node ({3}), then we will continue the search using the left child subtree ({4}). If the value we are looking for is greater than the current node ({5}), then we will continue the search starting from the right child of the current node ({6}). Otherwise, it means that the key we are looking for is equal to the current node's key, and we will return `true` to indicate that we found the key ({7}).

We can test this method using the following code:

```
console.log(tree.search(1) ? 'Key 1 found.' : 'Key 1 not found.');
console.log(tree.search(8) ? 'Key 8 found.' : 'Key 8 not found.');
```

It will output the following:

```
Value 1 not found.
Value 8 found.
```

Let's go into more detail on how the method was executed to find key 1:

1. We called the `searchNode` method, passing the tree `root` as a parameter ({1}).
The `node[root[11]]` is not null ({2}), so we will go to line {3}.
2. The `key[1] < node[11]` is true ({3}), so we will go to line {4} and call the `searchNode` method again, passing `node[7], key[1]` as parameters.
3. The `node[7]` is not null ({2}), so we will go to line {3}.
4. The `key[1] < node[7]` is true ({3}), so we will go to line {4} and call the `searchNode` method again, passing `node[5], key[1]` as parameters.
5. The `node[5]` is not null ({2}), so we will go to line {3}.
6. The `key[1] < node[5]` is true ({3}), so we will go to line {4} and call the `searchNode` method again, passing `node[3], key[1]` as parameters.
7. The `node[3]` is not null ({2}), so we will go to line {3}.
8. The `key[1] < node[3]` is true ({3}), so we will go to line {4} and call the `searchNode` method again, passing `null, key[1]` as parameters.
The `null` was passed as a parameter because `node[3]` is a leaf (it does not have children, so the left child will be `null`).
9. The `node` is `null` (line {2}), the `node` to search in this case is `null`), so we will return `false`.
10. After this, the stack of method calls will pop up, and the execution will end.

Let's do the same exercise to search for value 8, as follows:

1. We called the `searchNode` method, passing `root` as a parameter ({1}).
The `node[root[11]]` is not null ({2}), so we will go to line {3}.
2. The `key[8] < node[11]` is true ({3}), so we will go to line {4} and call the `searchNode` method again, passing `node[7], key[8]` as parameters.
3. The `node[7]` is not null ({2}), so we will go to line {3}.

4. The `key[8] < node[7]` is `false` ({3}), so we will go to line {5}.
5. The `key[8] > node[7]` is `true` ({5}), so we will go to line {6} and call the `searchNode` method again, passing `node[9], key[8]` as parameters.
6. The `node[9]` is not `null` ({2}), so we will go to line {3}.
7. The `key[8] < node[9]` is `true` ({3}), so we will go to line {4} and call the `searchNode` method again, passing `node[8], key[8]` as parameters.
8. The `node[8]` is not `null` ({2}), so we will go to line {3}.
9. The `key[8] < node[8]` is `false` ({3}), so we will go to line {5}.
10. The `key[8] > node[8]` is `false` ({5}), so we will go to line {7} and return `true` because `node[8]` is the key we are looking for.
11. After this, the stack of method calls will pop up, and the execution will end.

Removing a node

The next and last method we will create for our BST is the `remove` method. This is the most complex method we will create in this book. Let's start with the method that will be available to be called from a tree instance, as follows:

```
remove(key) {
    this.root = this.removeNode(this.root, key); // {1}
}
```

This method receives the desired `key` to be removed, and it also calls `removeNode`, passing the `root` and `key` to be removed as parameters ({1}). One very important detail to note is that the `root` receives the return of the `removeNode` method. We will understand why in a second.

The complexity of the `removeNode` method is due to the different scenarios that we need to handle and also because it is recursive.

Let's take a look at the `removeNode` implementation, as follows:

```
removeNode(node, key) {
    if (node == null) { // {2}
        return null;
    }
    if (this.compareFn(key, node.key) === Compare.LESS_THAN) { // {3}
        node.left = this.removeNode(node.left, key); // {4}
        return node; // {5}
    } else if (
        this.compareFn(key, node.key) === Compare.BIGGER_THAN
    }
```

```
    ) { // {6}
    node.right = this.removeNode(node.right, key); // {7}
    return node; // {8}
} else {
    // key is equal to node.item
    // case 1
    if (node.left == null && node.right == null) { // {9}
        node = null; // {10}
        return node; // {11}
    }
    // case 2
    if (node.left == null) { // {12}
        node = node.right; // {13}
        return node; // {14}
    } else if (node.right == null) { // {15}
        node = node.left; // {16}
        return node; // {17}
    }
    // case 3
    const aux = this.minNode(node.right); // {18}
    node.key = aux.key; // {19}
    node.right = this.removeNode(node.right, aux.key); // {20}
    return node; // {21}
}
```

As a stopping point, we have line {2}. If the node we are analyzing is `null`, it means the key does not exist in the tree, and for this reason, we will return `null`.

If not `null`, we need to find the key in the tree. So, if the key we are looking for has a lower value than the current node ({3}), then we will go to the next node at the left-hand side edge of the tree ({4}). If the key is greater than the current node ({6}), then we will go the next node at the right-hand side edge of the tree ({7}), which means we will be analyzing the subtrees.

If we find the key we are looking for (`key is equal to node.key`), then we will have three different scenarios to handle.

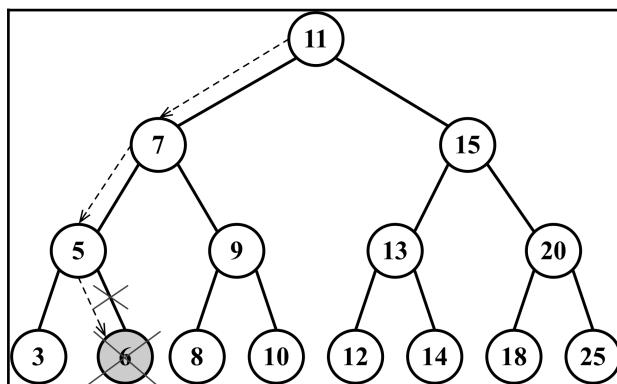
Removing a leaf node

The first scenario is a leaf node that does not have a left or right child (lines {9}). In this case, all we have to do is remove the node by assigning `null` to it (line {9}). However, as you learned during the implementation of linked lists, we know that assigning `null` to the node is not enough, and we also need to take care of the references (pointers). In this case, the node does not have any children, but it has a parent node. We need to assign `null` to its parent node, and this can be done by returning `null` (line {11}).

As the node already has the value `null`, the parent reference to the node will receive `null` as well, and this is the reason we are returning the `node` value in the method `removeNode`. The parent node will always receive the value returned from the method. An alternative to this approach could be passing the parent and the `node` as a parameter of the method.

If we take a look back at the first lines of the code of this method, we will notice that we are updating the references of the left and right pointers of the nodes in lines {4} and {7}, and we are also returning the updated node in lines {5} and {8}.

The following diagram exemplifies the removal of a leaf node:

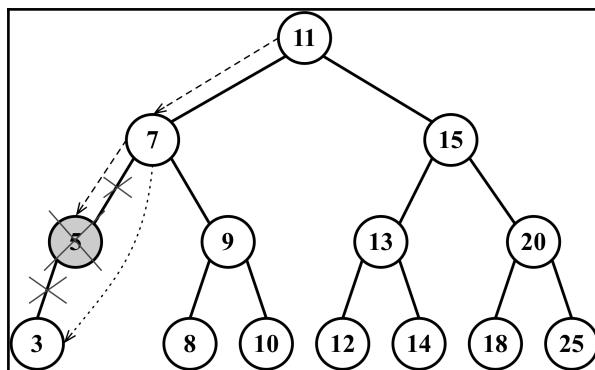


Removing a node with a left or right child

Now, let's review the second scenario, which is a node that has a left or right child. In this case, we need to skip this node and assign the parent pointer to the child node.

If the node does not have a left child (12), it means it has a right child, so we will change the reference of the node to its right child (13) and return the updated node (14). We will do the same if the node does not have a right child (15); we will update the node reference to its left child (16) and return the updated value (17).

The following diagram exemplifies the removal of a node with only a left or right child:



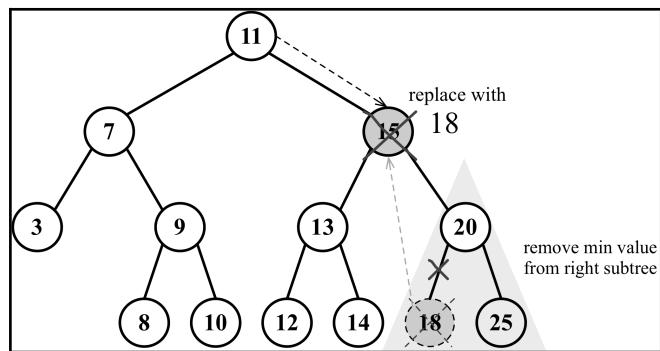
Removing a node with two children

Now comes the third scenario and the most complex one, which is the scenario where the node we are trying to remove has two children: the right and left one. To remove a node with two children, there are four steps that need to be performed, as follows:

1. Once we find the node we want to remove, we need to find the minimum node from its right-hand side edge subtree (its successor, 18).
2. Then, we will update the value of the node with the key of the minimum node from its right-hand side subtree (19). With this action, we are replacing the key of the node, which means it was removed.
3. However, now we have two nodes in the tree with the same key, and this cannot happen. What we need to do now is remove the minimum node from the right subtree since we moved it to the place of the removed node (20).
4. Finally, we will return the updated node reference to its parent (21).

The implementation of the `findMinNode` method is exactly the same as the `min` method. The only difference is that in the `min` method, we are returning only the key, and in the `findMinNode` method, we are returning the node.

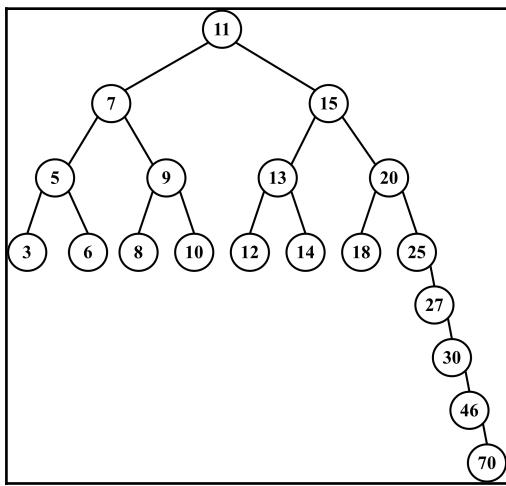
The following diagram exemplifies the removal of a node with only a left child and a right child:



Self-balancing trees

Now that you have learned how to work with BST, you can dive into the study of trees if you want to.

BST has a problem: depending on how many nodes you add, one of the edges of the tree can be very deep, meaning a branch of the tree can have a high level and another branch can have a low level, as shown in the following diagram:



This can cause performance issues when adding, removing, and searching for a node on a particular edge of the tree. For this reason, there is a tree called the **Adelson-Velskii and Landi's tree (AVL tree)**. The AVL tree is a self-balancing BST, which means the height of both the left and right subtrees of any node differ by 1 at most. You will learn more about the AVL tree in the following topic.

Adelson-Velskii and Landi's tree (AVL tree)

The AVL tree is a self-balancing tree, meaning the tree tries to self-balance whenever a node is added to it or removed from it. The height of the left or right subtree of any node (and any level) differs by 1 at most. This means the tree will try to become a complete tree whenever possible while adding or removing a node.

Let's start by creating our `AVLTree` class, which is declared as follows:

```
class AVLTree extends BinarySearchTree {  
    constructor(compareFn = defaultCompare) {  
        super(compareFn);  
        this.compareFn = compareFn;  
        this.root = null;  
    }  
}
```

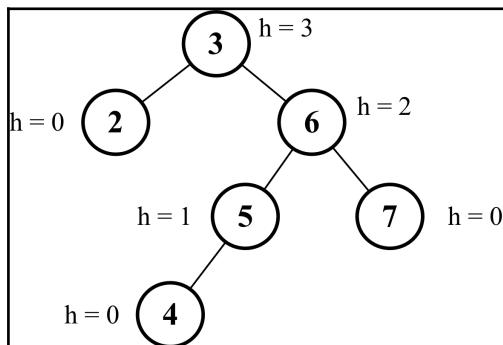
Since the AVL tree is a BST, we can extend the BST class we created and only overwrite the methods which are needed to maintain the AVL tree's balance, which are the `insert`, `insertNode`, and `removeNode` methods. All the other BST methods will be inherited by the `AVLTree` class.

Inserting and removing nodes in an AVL tree works the same way as in BST. However, the difference in the AVL tree is that we will need to verify its **balance factor**, and if needed, we will apply the logic to self-balance the tree.

We will learn how to create the `remove` and `insert` methods, but first, we need to learn about the AVL tree's terminology and its rotation operations.

Height of a node and the balancing factor

As we learned at the beginning of this chapter, the height of a node is defined as the maximum number of edges from the node to any of its leaf nodes. The following diagram exemplifies a tree with the height of each node:



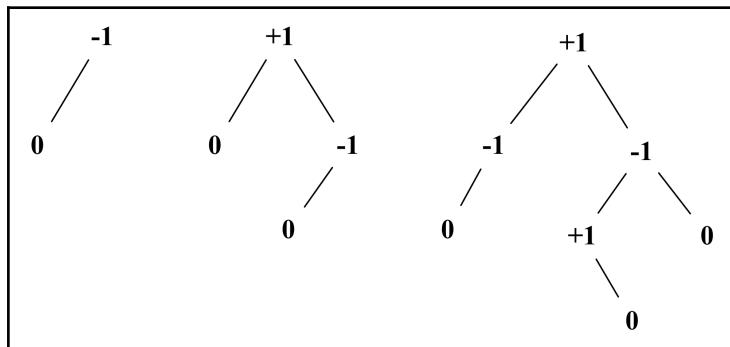
The code to calculate the height of a node is as follows:

```

getNodeHeight(node) {
  if (node == null) {
    return -1;
  }
  return Math.max(
    this.getNodeHeight(node.left), this.getNodeHeight(node.right)
  ) + 1;
}
  
```

In an AVL tree, whenever we insert or remove a node from the tree, we will need to calculate the difference between the height of the right-hand side subtree (hr) and the left-hand side subtree (hl). The result of $hr - hl$ needs to be 0, 1, or -1. If the result is different from these values, it means the tree needs to be balanced. This concept is called the **balance factor**.

The following diagram exemplifies the balance factor of some trees (all trees are balanced):



The code which follows calculates the balance factor of a node and return its state:

```

getBalanceFactor(node) {
  const heightDifference = this.getNodeHeight(node.left) -
  this.getNodeHeight(node.right);
  switch (heightDifference) {
    case -2:
      return BalanceFactor.UNBALANCED_RIGHT;
    case -1:
      return BalanceFactor.SLIGHTLY_UNBALANCED_RIGHT;
    case 1:
      return BalanceFactor.SLIGHTLY_UNBALANCED_LEFT;
    case 2:
      return BalanceFactor.UNBALANCED_LEFT;
    default:
      return BalanceFactor.BALANCED;
  }
}
  
```

To avoid working with the balance factor numbers directly in the code, we will also create a constant in JavaScript that is going to work as an enumerator:

```

const BalanceFactor = {
  UNBALANCED_RIGHT: 1,
  SLIGHTLY_UNBALANCED_RIGHT: 2,
  BALANCED: 3,
  SLIGHTLY_UNBALANCED_LEFT: 4,
  UNBALANCED_LEFT: 5
};
  
```

We will learn what each `heightDifference` means in the following topic.

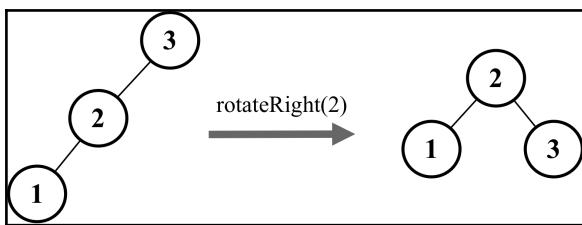
Balancing operations– AVL rotations

After inserting or removing nodes from the AVL tree, we will calculate the height of the nodes and will verify whether the tree needs to be balanced. There are two balancing processes that can be used: simple rotation or double rotation. Between simple rotation and double rotation, there are four scenarios:

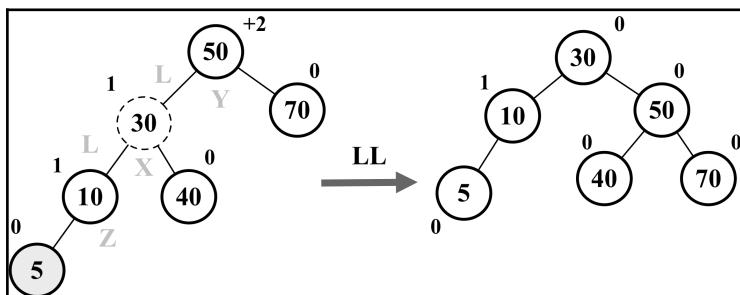
- **Left-Left (LL):** This is a single rotation to the right
- **Right-Right (RR):** This is a single rotation to the left
- **Left-Right (LR):** This is a double rotation to the right (rotate left then right)
- **Right-Left (RL):** This is a double rotation to the left (rotate right then left)

Left-left case: single rotation to the right

This case occurs when the height of a node's left child becomes greater than the height of the right child, and the left child is either balanced and left-heavy, as demonstrated in the following diagram:



Let's use a practical example. Consider the following diagram:



Suppose node 5 was the last one inserted in the AVL tree. This would make the tree unbalanced (node 50-Y has a height of +2), so we would need to balance it.

These are the steps we need to perform to balance the tree:

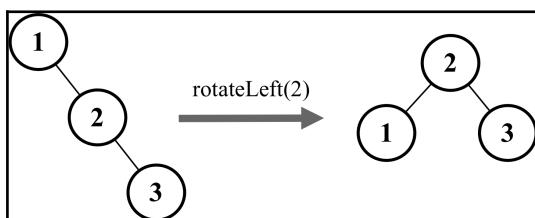
- Node **X**, which is in the middle of the three nodes involved in the balancing (**X**, **Y**, and **Z**), will take the place of node **Y**, which has a balance factor of **+2** ({1})
- Node **X**, the left-hand side subtree, will not be changed
- Node **X**, the right-hand side subtree (node **Z**), will be placed at the left-hand side subtree of node **Y** ({2})
- Node **X**, the right-hand side child, will reference node **Y** ({3})

The following code exemplifies this process:

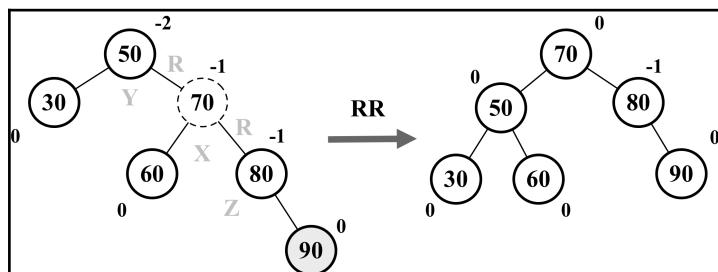
```
rotationLL(node) {
    const tmp = node.left; // {1}
    node.left = tmp.right; // {2}
    tmp.right = node; // {3}
    return tmp;
}
```

Right-right case: single rotation to the left

The right-right case is the inverse of the left-left case. It occurs when the height of a node's right child becomes greater than that of the left child, and the right child is either balanced or right-heavy, as demonstrated by the following diagram:



Let's use a practical example. Consider the following diagram:



Suppose node **90** was the last one inserted in the AVL tree. This would make the tree unbalanced (node **50** -Y has a height of **-2**), so we would need to balance it. These are the steps we will perform to balance the tree:

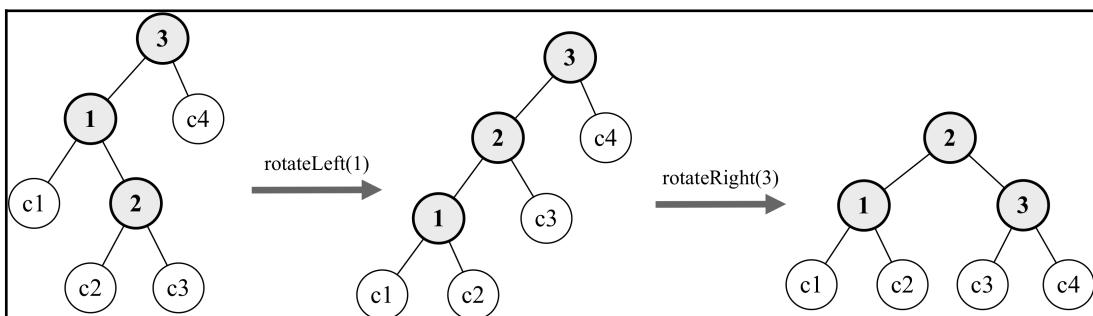
- Node **X**, which is in the middle of the three nodes involved in the balancing (**X**, **Y**, and **Z**), will take place in the node **Y**, which has a balance factor of **-2** (**{1}**)
- Node **X**, the right-hand side subtree, will not be changed
- Node **X**, the left-hand side subtree (node **Z**), will be placed at the right-hand side subtree of node **Y** (**{2}**)
- Node **X**, the left-hand side child, will reference node **Y** (**{3}**)

The following code exemplifies this process:

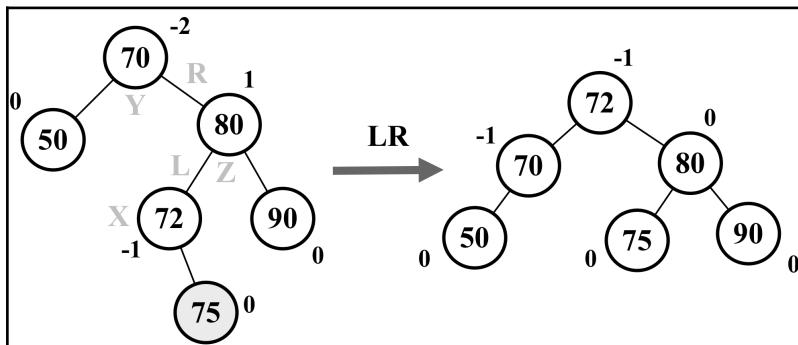
```
rotationRR(node) {
    const tmp = node.right; // {1}
    node.right = tmp.left; // {2}
    tmp.left = node; // {3}
    return tmp;
}
```

Left-right case: double rotation to the right

This case occurs when the height of a node's left child becomes greater than that of the right child, and the left child is right-heavy. In this case, we can fix it by doing a left rotation on the left child, which results in the left-left case, then we fix it again by doing a right rotation on the unbalanced node ,as demonstrated by the following diagram:



Let's use a practical example. Consider the following diagram:



Suppose node **75** was the last one inserted in the AVL tree. This would make the tree unbalanced (node **70-Y** has a height of **-2**), so we would need to balance it. These are the steps we will perform to balance the tree:

- Node **X** will take the place of node **Y**, which has a balance factor of **-2**
- Node **X**, the right-hand side subtree (node **Z**), will be placed at the left-hand side subtree of node **Z**
- Node **X**, the left-hand side subtree, will be placed at the right-hand side subtree of node **Y**
- Node **X**, the right-hand side child, will reference node **Y**
- Node **X**, the left-hand side child, will reference node **Z**

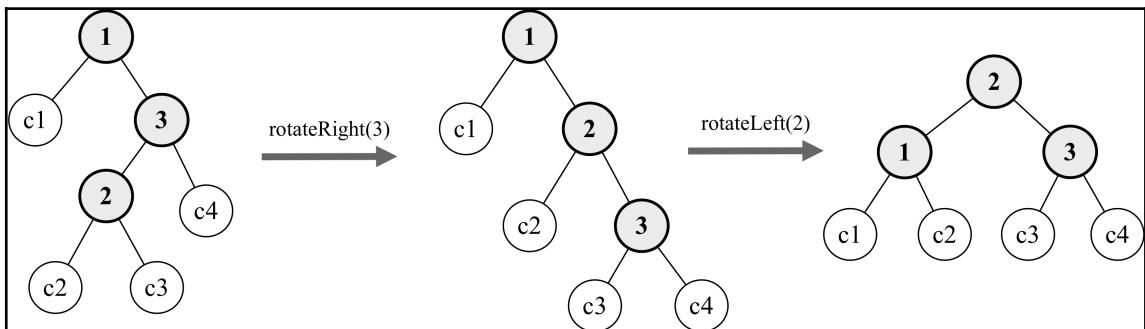
So basically, we are doing an LL rotation first and then an RR rotation.

The following code exemplifies this process:

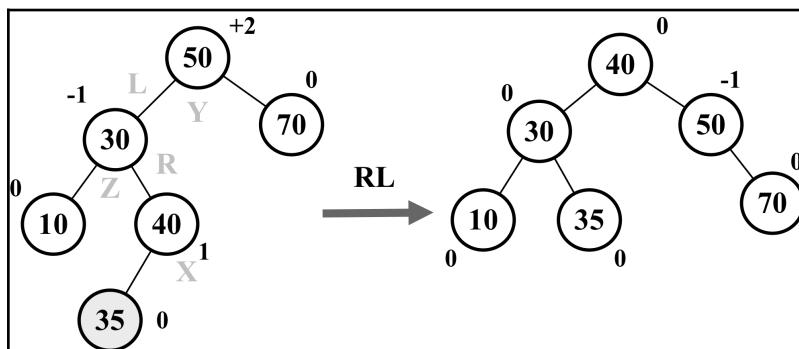
```
rotationLR(node) {
    node.left = this.rotationRR(node.left);
    return this.rotationLL(node);
}
```

Right-left case – double rotation to the left

The right-left case is the inverse of the left-right case. It occurs when the height of a node's right child becomes greater than that of the left child, and the right child is left-heavy. In this case, we can fix it by doing a right rotation on the right child, which results in the right-right case, then we fix it again by doing a left rotation on the unbalanced node, as demonstrated in the following diagram:



Let's use a practical example. Consider the following diagram:



Suppose node **35** was the last one inserted in the AVL tree. This would make the tree unbalanced (node **50** -Y has a height of **+2**), so we would need to balance it. These are the steps we will perform to balance the tree:

- Node **X** will take place of node **Y**, which has a balance factor of **+2**
- Node **X**, the right-hand side subtree (node **Z**), will be placed at the left-hand side subtree of node **Y**

- Node **X**, the left-hand side subtree, will be placed at the right-hand side subtree of node **Z**
- Node **X**, the right-hand side child, will reference node **Y**
- Node **X**, the left-hand side child, will reference node **Z**

So basically, we are doing an RR rotation first and then an LL rotation.

The following code exemplifies this process:

```
rotationRL(node) {
    node.right = this.rotationLL(node.right);
    return this.rotationRR(node);
}
```

With these concepts in place, we can now focus on the code for inserting and removing nodes in/from the AVL tree.

Inserting a node in the AVL tree

Inserting a node in an AVL tree works the same way as in BST. In addition to inserting the node, we will also verify whether the tree is still balanced after the insertion, and if not, we will apply the rotation operations as needed.

The following code inserts a new node in an AVL tree:

```
insert(key) {
    this.root = this.insertNode(this.root, key);
}
insertNode(node, key) {
    // insert node as in BST tree
    if (node == null) {
        return new Node(key);
    } else if (this.compareFn(key, node.key) === Compare.LESS_THAN) {
        node.left = this.insertNode(node.left, key);
    } else if (this.compareFn(key, node.key) === Compare.BIGGER_THAN) {
        node.right = this.insertNode(node.right, key);
    } else {
        return node; // duplicated key
    }
    // balance the tree if needed
    const balanceFactor = this.getBalanceFactor(node); // {1}
    if (balanceFactor === BalanceFactor.UNBALANCED_LEFT) { // {2}
        if (this.compareFn(key, node.left.key) === Compare.LESS_THAN) { // {3}
            node = this.rotationLL(node); // {4}
        } else {
    }
```

```

        return this.rotationLR(node); // {5}
    }
}

if (balanceFactor === BalanceFactor.UNBALANCED_RIGHT) { // {6}
    if (
        this.compareFn(key, node.right.key) === Compare.BIGGER_THAN
    ) { // {7}
        node = this.rotationRR(node); // {8}
    } else {
        return this.rotationRL(node); // {9}
    }
}
return node;
}

```

After inserting the node in the AVL tree, we need to check whether the tree needs to be balanced, so we will calculate the balance factor ({1}) for every node from the node that was inserted to the tree root recursively, and we will apply the correct rotation for each case.

If after inserting a node in the left-hand side subtree the tree is unbalanced ({2}), we need to compare whether the inserted key is lesser than the left child's key ({3}). If so, we will do an LL rotation ({4}). Otherwise, we will do an LR rotation ({5}).

If after inserting a node in the right-hand side subtree the tree is unbalanced ({6}), we need compare whether the inserted key is bigger than the right child's key ({7}). If so, we will do an RR rotation ({8}). Otherwise, we will do an RL rotation ({9}).

Removing a node from the AVL tree

Removing a node from an AVL tree works the same way as in BST. In addition to removing the node, we will also verify whether the tree is still balanced after the removal, and if not, we will apply the rotation operations as needed.

The following code removes a node from an AVL tree:

```

removeNode(node, key) {
    node = super.removeNode(node, key); // {1}
    if (node == null) {
        return node; // null, no need to balance
    }
    // verify if tree is balanced
    const balanceFactor = this.getBalanceFactor(node); // {2}
    if (balanceFactor === BalanceFactor.UNBALANCED_LEFT) { // {3}

```

```

const balanceFactorLeft = this.getBalanceFactor(node.left); // {4}
if (
  balanceFactorLeft === BalanceFactor.BALANCED ||
  balanceFactorLeft === BalanceFactor.SLIGHTLY_UNBALANCED_LEFT
) { // {5}
  return this.rotationLL(node); // {6}
}
if (
  balanceFactorLeft === BalanceFactor.SLIGHTLY_UNBALANCED_RIGHT
) { // {7}
  return this.rotationLR(node.left); // {8}
}
}
if (balanceFactor === BalanceFactor.UNBALANCED_RIGHT) { // {9}
  const balanceFactorRight = this.getBalanceFactor(node.right); // {10}
  if (
    balanceFactorRight === BalanceFactor.BALANCED ||
    balanceFactorRight === BalanceFactor.SLIGHTLY_UNBALANCED_RIGHT
) { // {11}
  return this.rotationRR(node); // {12}
}
if (
  balanceFactorRight === BalanceFactor.SLIGHTLY_UNBALANCED_LEFT
) { // {13}
  return this.rotationRL(node.right); // {14}
}
}
return node;
}

```

Since the `AVLTree` is a child class of the `BinarySearchTree` class, we can use the `BST removeNode` method to remove the node from the AVL tree as well {1}. After removing the node from the AVL tree, we need to check whether the tree needs to be balanced, so we will calculate the balance factor ({1}) for every node from the node that was removed to the tree root recursively, and we will apply the correct rotation for each case.

If after removing a node in the left-hand side subtree the tree is unbalanced ({3}), we will calculate the balance factor of the left subtree ({4}). If the left subtree is unbalanced to the left ({5}), we will do an LL rotation ({6}), or if the left subtree is unbalanced to the right ({7}), we will do an LR rotation ({8}).

The final last case is if after removing a node in the right-hand side subtree the tree is unbalanced ({9}), we will calculate the balance factor of the right subtree ({10}). If the right subtree is unbalanced to the right ({11}), we will do an RR rotation ({12}), or if the right subtree is unbalanced to the left ({13}), we will do an LR rotation ({14}).

Red-Black tree

Like the AVL tree, the **Red-Black tree** is also a self-balancing binary search tree. We learned that inserting or removing a node from the AVL tree might cause rotations, so if we need a self-balancing tree that involves many frequent insertions or deletions, then the Red-Black tree is preferred. If the insertions and deletions are less frequent (we are interested in frequent search operations), then the AVL tree is preferred over the Red-Black tree.

In the Red-Black tree, every node follows the rules which are listed as follows:

1. As the name of the tree suggests, each node is either red or black.
2. The root of the tree is black.
3. All of the leaves are black (nodes represented with the `NULL` reference).
4. If a node is red, then both of its children are black.
5. There cannot be two adjacent red nodes. A red node cannot have a red parent or child.
6. Every path from a given node to any of its descendants (`NULL` leaves) contains the same number of black nodes.

Let's start by creating our `RedBlackTree` class, which is declared as follows:

```
class RedBlackTree extends BinarySearchTree {  
    constructor(compareFn = defaultCompare) {  
        super(compareFn);  
        this.compareFn = compareFn;  
        this.root = null;  
    }  
}
```

Since the Red-Black tree is also a BST tree, we can extend the BST class we created and only overwrite the methods which are needed to maintain the Red-Black tree properties. We will start with the `insert` and `insertNode` methods.

Inserting a node in the Red-Black tree

Inserting a node in a Red-Black tree works the same way as in BST. In addition to inserting the code, we will also apply a color to the node and after the insertion, we will verify whether the tree still meets the rules of the Red-Black tree and that it is still balanced.

The following code inserts a new node in a Red-Black tree:

```
insert(key: T) {
    if (this.root == null) { // {1}
        this.root = new RedBlackNode(key); // {2}
        this.root.color = Colors.BLACK; // {3}
    } else {
        const newNode = this.insertNode(this.root, key); // {4}
        this.fixTreeProperties(newNode); // {5}
    }
}
```

If the tree is empty ({1}), then we will create a new Red-Black tree node ({2}) and to comply with rule 2, we will set the `root` color as black ({3}). By default, the node will be created with the color red ({6}). If the tree is not empty, we will insert the node in its correct place by using the same logic applied to insert a node in a BST ({4}).

The `insertNode` method, in this case, needs to return the newly inserted node so we can verify if after the insertion; the Red-Black tree rules are still satisfied ({5}).

For the Red-Black tree, the node will need a couple of additional properties compared to the node class we used previously: the color of the node {6} and a reference to its parent ({7}). The code is presented as follows:

```
class RedBlackNode extends Node {
    constructor(key) {
        super(key);
        this.key = key;
        this.color = Colors.RED; // {6}
        this.parent = null; // {7}
    }

    isRed() {
        return this.color === Colors.RED;
    }
}
```

The overwritten `insertNode` method is also presented as follows:

```
insertNode(node, key) {  
    if (this.compareFn(key, node.key) === Compare.LESS_THAN) {  
        if (node.left == null) {  
            node.left = new RedBlackNode(key);  
            node.left.parent = node; // {8}  
            return node.left; // {9}  
        }  
        else {  
            return this.insertNode(node.left, key);  
        }  
    }  
    else if (node.right == null) {  
        node.right = new RedBlackNode(key);  
        node.right.parent = node; // {10}  
        return node.right; // {11}  
    }  
    else {  
        return this.insertNode(node.right, key);  
    }  
}
```

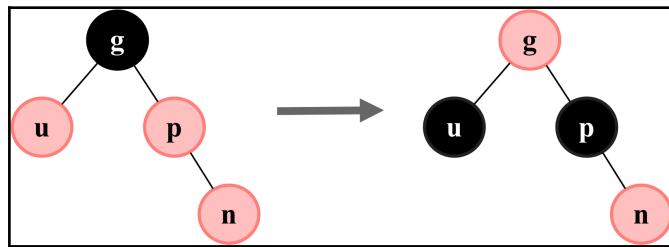
As we can see, the logic is the same as what is used in a regular BST. The difference here is that we are keeping a reference to the inserted node's parent ({8} and {10}) and also returning the node reference ({9} and {11}) so that we can verify the tree properties next.

Verifying the Red-Black tree properties after insertion

To verify whether the Red-Black tree is still balanced and still follows all of its requirements, we will use two concepts: recoloring and rotation.

After inserting a new node into the tree, this new node will be red. This does not affect the rule of the count of black nodes (rule 6), but it can affect rule 5: two adjacent red nodes cannot coexist. If the parent of the inserted node is black, then there is no problem. However, if the parent of the inserted node is red, then we have a violation of rule 5. To solve this violation, we simply need to change the color of the node's **parent**, the node's **grandparent**, and the node's **uncle** (because we are changing the parent color as well).

The following diagram exemplifies this action:



The following is the initial code for `fixTreeProperties`:

```
fixTreeProperties(node) {
    while (node && node.parent && node.parent.color.isRed() // {1}
        && node.color !== Colors.BLACK) { // {2}
        let parent = node.parent; // {3}
        const grandParent = parent.parent; // {4}
        // case A: parent is left child
        if (grandParent && grandParent.left === parent) { // {5}
            const uncle = grandParent.right; // {6}

            // case 1A: uncle of node is also red - only recoloring
            if (uncle && uncle.color === Colors.RED) { // {7}
                grandParent.color = Colors.RED;
                parent.color = Colors.BLACK;
                uncle.color = Colors.BLACK;
                node = grandParent; // {8}
            }
            else {
                // case 2A: node is right child - left rotate

                // case 3A: node is left child - right rotate
            }
        }
        else { // case B: parent is right child
            const uncle = grandParent.left; // {9}

            // case 1B: uncle is read - only recoloring
            if (uncle && uncle.color === Colors.RED) { // {10}
                grandParent.color = Colors.RED;
                parent.color = Colors.BLACK;
                uncle.color = Colors.BLACK;
                node = grandParent;
            }
            else {
                // case 2B: node is left child - right rotate
            }
        }
    }
}
```

```

        // case 3B: node is right child - left rotate
    }
}
this.root.color = Colors.BLACK; // {11}
}

```

Starting from the inserted node, we will verify whether its parent is red ({1}) and whether the node is also not black ({2}). To make our code easier to read, we will keep a reference to the node's parent ({3}) and grandparent ({4}).

Next, we will verify whether the node's parent is a left ({5} - case A) or right child (case B). For case 1A, where we only need to recolor the nodes, it does not make any difference if the parent is a left or right child, but this will make a difference for the following cases which we will learn about.

Since we need to change the uncle's color as well, we need a reference to it ({6} and {9}). So if the uncle's color is red ({7} and {10}), we change the color of the grandparent, parent, and uncle, and we also change the reference of the current node to the grandparent ({8}) and keep checking the tree for more violations.

To make sure the root color is always black (rule 2), we will assign the color to the root at the end of the code ({11}).

In case the node's uncle is black, this means recoloring alone will not be enough since the tree is not balanced, so we need to perform the rotations, which are as follows:

- **Left-Left (LL)**: The parent is the left child of the grandparent, and the node is the left child of the parent (case 3A)
- **Left-Right (LR)**: The parent is the left child of the grandparent, and the node is the right child of the parent (case 2A)
- **Right-Right (RR)**: The parent is the right child of the grandparent, and the node is the right child of the parent (case 3B)
- **Right-Left (RL)**: The parent is the right child of the grandparent, and the node is the left child of the parent (case 2B)

Let's take a look at cases 2A and 3A:

```

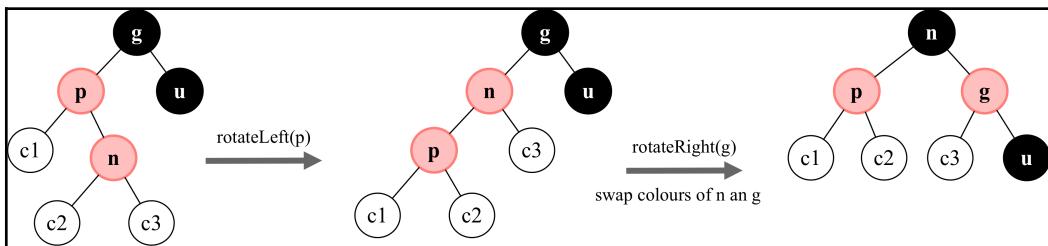
// case 2A: node is right child - left rotate
if (node === parent.right) {
    this.rotationRR(parent); // {12}
    node = parent; // {13}
    parent = node.parent; // {14}
}

```

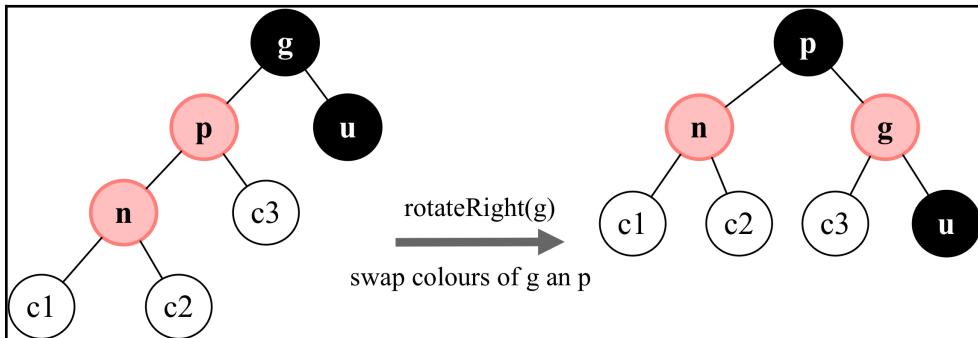
```
// case 3A: node is left child - right rotate
this.rotationLL(grandParent); // {15}
parent.color = Colors.BLACK; // {16}
grandParent.color = Colors.RED; // {17}
node = parent; // {18}
```

If the parent is a left child and the node is a right child, we will do a double rotation, first a right-right rotation ({12}), and also update the references for the node ({13}) and parent ({10}). After the first rotation, we will rotate it again using the grandparent as the source node ({15}) and update the colors of the parent ({16}) and grandparent ({17}) during the rotation. Finally, we update the reference to the current node ({18}) so that we keep checking the tree for more violations.

Case 2A can be exemplified in the following diagram:



In case the node is a left child, then we go directly to line {15} to perform the left-left rotation. Case 3A can be exemplified in the diagram as follows:

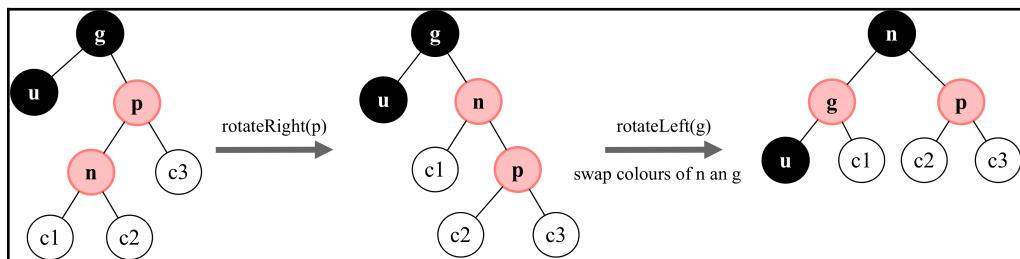


Now, let's take a look at cases 2B and 3B:

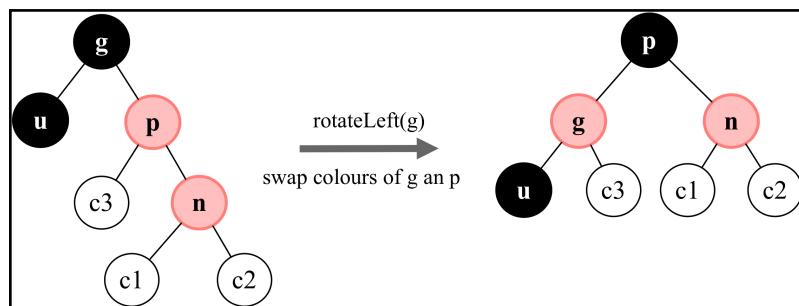
```
// case 2B: node is left child - left rotate
if (node === parent.left) {
    this.rotationLL(parent); // {19}
    node = parent;
    parent = node.parent;
}

// case 3B: node is right child - left rotate
this.rotationRR(grandParent); // {20}
parent.color = Colors.BLACK;
grandParent.color = Colors.RED;
node = parent;
```

The logic is the same, but the differences are that the rotations that will be performed as follows: first the left-left rotation ({18}) and then the right-right rotation ({20}). Case 2B can be exemplified as follows:



And finally, case 3B can be exemplified as follows:



Red-Black tree rotations

In the insertion algorithm, we only used the right-right and left-left rotations. The logic is the same as the AVL tree, however, since we are keeping a reference to the node's parent, we also need to update the `node.parent` reference to the new parent after the node is rotated.

The code for the left-left rotation (right rotation) is presented as follows (update of parent highlighted):

```
rotationLL(node) {
    const tmp = node.left;
    node.left = tmp.right;
    if (tmp.right && tmp.right.key) {
        tmp.right.parent = node;
    }
    tmp.parent = node.parent;
    if (!node.parent) {
        this.root = tmp;
    }
    else {
        if (node === node.parent.left) {
            node.parent.left = tmp;
        }
        else {
            node.parent.right = tmp;
        }
    }
    tmp.right = node;
    node.parent = tmp;
}
```

The code for the right-right rotation (left rotation) is presented as follows (update of parent highlighted):

```
rotationRR(node) {
    const tmp = node.right;
    node.right = tmp.left;
    if (tmp.left && tmp.left.key) {
        tmp.left.parent = node;
    }
    tmp.parent = node.parent;
    if (!node.parent) {
        this.root = tmp;
    }
    else {
        if (node === node.parent.left) {
```

```
        node.parent.left = tmp;
    }
    else {
        node.parent.right = tmp;
    }
}
tmp.left = node;
node.parent = tmp;
}
```

Summary

In this chapter, we covered the algorithms to add, search, and remove keys from a binary search tree, which is the basic tree data structure largely used in computer science. We covered three traversal approaches to visit all the nodes of a tree. We also learned how to create self-balanced trees using the AVL tree and insert and remove keys to/from it, and we also covered the Red-Black tree.

In the next chapter, we will learn about a special data structure called heap (or priority queue).

11

Binary Heap and Heap Sort

In the previous chapter, we learned about the **tree** data structure. In this chapter, we will learn about a special type of binary tree, which is the **heap** data structure, also known as the **binary heap**. The binary heap is a very famous data structure in computer science, commonly applied in **priority queues** due to its efficiency of quickly extracting the maximum or minimum values. It is also used by the famous **heap sort** algorithm.

In this chapter, we will cover:

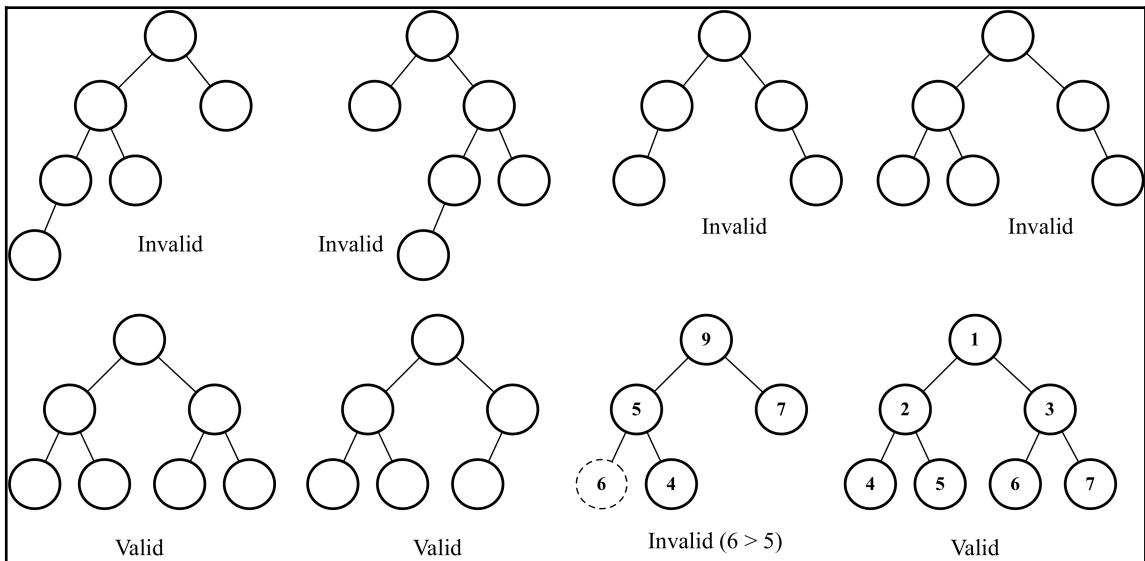
- The binary heap data structure
- Max and min heap
- The heap sort algorithm

The binary heap data structure

The binary heap is a special binary tree with the following two properties:

- It is a complete binary tree, meaning all levels of the tree have both left and right children (with the exception of the last-level leaves), and the last level has all children as left as possible. This is called as **shape property**.
- A binary heap is either a min heap or a max heap. The min heap allows you to quickly extract the minimum value of the tree, and the max heap allows you to quickly extract the maximum value of the tree. All nodes are either greater than or equal to (max heap), or less than or equal to (min heap), each of its child nodes. This is called **heap property**.

The following diagram contains some examples of invalid and valid heaps:



Although the binary heap is a binary tree, it is not necessarily a **binary search tree (BST)**. In the binary heap, every child node needs to be greater than or equal to its parent node (min heap) or less than or equal to its parent node (max heap). In the BST, however, the left child is always smaller than its parent and the right child always has a greater key as well.

Creating the MinHeap class

Let's start by creating the basic structure of the `MinHeap` class as follows:

```
import { defaultCompare } from '../util';

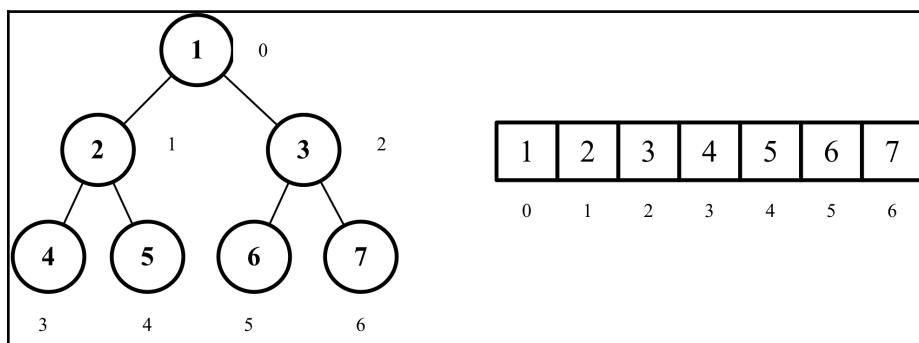
export class MinHeap {
  constructor(compareFn = defaultCompare) {
    this.compareFn = compareFn; // {1}
    this.heap = []; // {2}
  }
}
```

To compare the values that will be stored in this data structure, we will use `compareFn ({1})`, which is going to perform a basic comparison in case no custom function is passed to the class constructor as was done in previous chapters.

To store the values, we will use an array representation ({2}).

Binary tree array representation

There are two ways of representing a binary tree. The first is using a dynamic representation using pointers (node representation) as we did in the previous chapter. The second is using an array accessing the correct indexes to retrieve the values of the parent, left, and right children. The following diagram demonstrates the binary tree's different representations:



To access the *nodes* of a binary tree using a regular array, we can manipulate the index with the following behavior:

For any given node at position `index`:

- Its left child is located at `2 * index + 1` (if available)
- Its right child is located at `2 * index + 2` (if available)
- Its parent node is located at `index / 2` (if available)

To access a specific node following the preceding rules, we can add the following methods to the `MinHeap` class:

```
getLeftIndex(index) {
    return 2 * index + 1;
}
getRightIndex(index) {
```

```

        return 2 * index + 2;
    }
    getParentIndex(index) {
        if (index === 0) {
            return undefined;
        }
        return Math.floor((index - 1) / 2);
    }
}

```

We can perform three main operations in a heap data structure:

- `insert (value)`: This method inserts a new `value` into the heap. It returns `true` if the `value` was successfully inserted and `false` otherwise.
- `extract ()`: This method removes the minimum `value` (min heap) or the maximum `value` (max heap) and returns it.
- `findMinimum() ()`: This method returns the minimum `value` (min heap) or maximum `value` (max heap) without removing it.

Let's learn about each one in the following topics.

Inserting a value into the heap

Inserting a value into the heap is performed by adding the `value` at the bottom leaf of the heap (the last position of the array—`{1}`) and then performing the `siftUp` method (`{2}`), meaning we will swap the `value` with its parent until its parent is smaller than the `value` being inserted. The `sift up` operation is also called **up head, percolate up, bubble up, heapify up, or cascade up**.

The code to insert a new `value` into the heap is presented as follows:

```

insert(value) {
    if (value != null) {
        this.heap.push(value); // {1}
        this.siftUp(this.heap.length - 1); // {2}
        return true;
    }
    return false;
}

```

The sift up operation

The code for the sift up operation is presented as follows:

```
siftUp(index) {  
    let parent = this.getParentIndex(index); // {1}  
    while (  
        index > 0 &&  
        this.compareFn(this.heap[parent], this.heap[index]) >  
        Compare.BIGGER_THAN  
    ) { // {2}  
        swap(this.heap, parent, index); // {3}  
        index = parent;  
        parent = this.getParentIndex(index); // {4}  
    }  
}
```

The `siftUp` method receives the `index` of the inserted value. We also need to retrieve the index of its parent ({1}).

If the inserted value is smaller than its parent ({2}) — in case of min heap or greater than its parent in case of the max heap), we swap the element with its parent ({3}). We will repeat this process until the root of the heap is also processed by updating the `index` and the parent indexes ({4}) after every swap.

The `swap` function is presented as follows:

```
function swap(array, a, b) {  
    const temp = array[a]; // {5}  
    array[a] = array[b]; // {6}  
    array[b] = temp; // {7}  
}
```

To swap two values within an array, we need a helper variable that will make a copy of the first element we want to swap ({5}). Next, we will assign the second element to the first element's position ({6}). Finally, we overwrite the second element's value with the first element's value ({7}) by assigning the copy made in line {5}.



The `swap` function will be used often in Chapter 13, *Sorting and Searching Algorithms*.

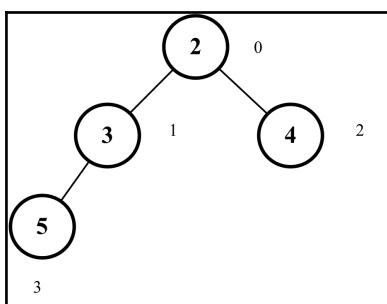
We can also rewrite the `swap` function using ECMAScript 2015 (ES6) syntax:

```
const swap = (array, a, b) => [array[a], array[b]] = [array[b], array[a]];
```

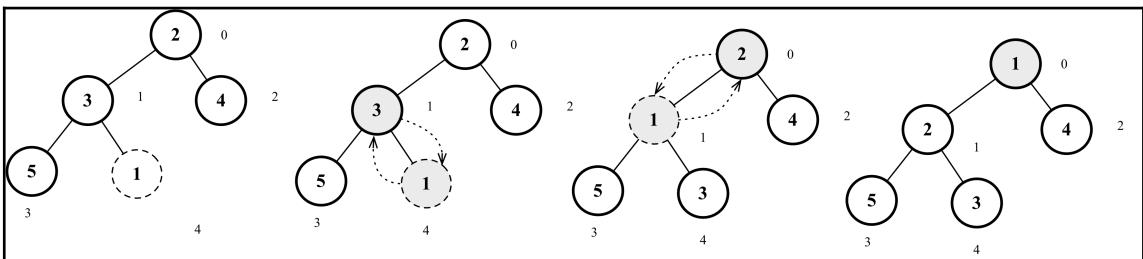


ES2015 introduced the object and array destructuring functionality `[a, b] = [b, a]`, as we learned in *Chapter 2, ECMAScript and TypeScript Overview*. However, there is an open issue at the time of writing this book regarding the performance of the destructuring operation being slower than the normal assignment. For more information about the issue, please visit https://bugzilla.mozilla.org/show_bug.cgi?id=1177319.

Let's see the `insert` method in action. Consider the following heap data structure:



Suppose we want to insert the value 1 into the heap. The algorithm will perform a few sift up operations, as demonstrated in the following diagram:



The following code exemplifies the creation of the heap and the actions demonstrated in the diagram:

```
const heap = new MinHeap();

heap.insert(2);
heap.insert(3);
heap.insert(4);
```

```
heap.insert(5);  
heap.insert(1);
```

Finding the minimum or maximum value from the heap

In the min heap, the minimum value is always located at the first index of the array (the root of the heap). The code is presented as follows:

```
size() {  
    return this.heap.length;  
}  
isEmpty() {  
    return this.size() === 0;  
}  
findMinimum() {  
    return this.isEmpty() ? undefined : this.heap[0]; // {1}  
}
```

So if the heap is not empty, we return the first index of the array ({1}). We can also create the `size` and `empty` methods for the `MinHeap` data structure.

The following code can be used to test these three methods:

```
console.log('Heap size: ', heap.size()); // 5  
console.log('Heap is empty: ', heap.isEmpty()); // false  
console.log('Heap min value: ', heap.findMinimum()); // 1
```



In the max heap, the first index of the array will store the maximum value, so we can use this same code.

Extracting the minimum or maximum value from the heap

Removing the minimum value (min heap) or the maximum value (max heap) consists of removing the element located at the first index of the array (the root of the heap). After the removal, we move the last element of the heap to the root and then we perform the function called `siftDown`, meaning we will swap elements until the heap is organized again. The **sift down** operation is also called **sink down**, **percolate down**, **bubble down**, **heapify down**, or **cascade down**.

The code is presented as follows:

```
extract() {
    if (this.isEmpty()) {
        return undefined; // {1}
    }
    if (this.size() === 1) {
        return this.heap.shift(); // {2}
    }
    const removedValue = this.heap.shift(); // {3}
    this.siftDown(0); // {4}
    return removedValue; // {5}
}
```

If the heap is empty, there is no value to extract, so we can return `undefined` ({1}). If there is only one value in the heap, we can simply remove and return it ({2}). However, if the heap has more than one value, we will remove the value from the first index ({3}) and store it in a temporary variable so we can return it ({5}) after performing the sift down operation ({4}).

The sift down operation (heapify)

The code for the sift down operation is presented as follows:

```
siftDown(index) {
    let element = index;
    const left = this.getLeftIndex(index); // {1}
    const right = this.getRightIndex(index); // {2}
    const size = this.size();
    if (
        left < size &&
        this.compareFn(this.heap[element], this.heap[left]) >
        Compare.BIGGER_THAN
    ) { // {3}
        element = left; // {4}
    }
    if (
        right < size &&
        this.compareFn(this.heap[element], this.heap[right]) >
        Compare.BIGGER_THAN
    ) { // {5}
        element = right; // {6}
    }
    if (index !== element) { // {7}
        swap(this.heap, index, element); // {8}
        this.siftDown(element); // {9}
    }
}
```

```

    }
}

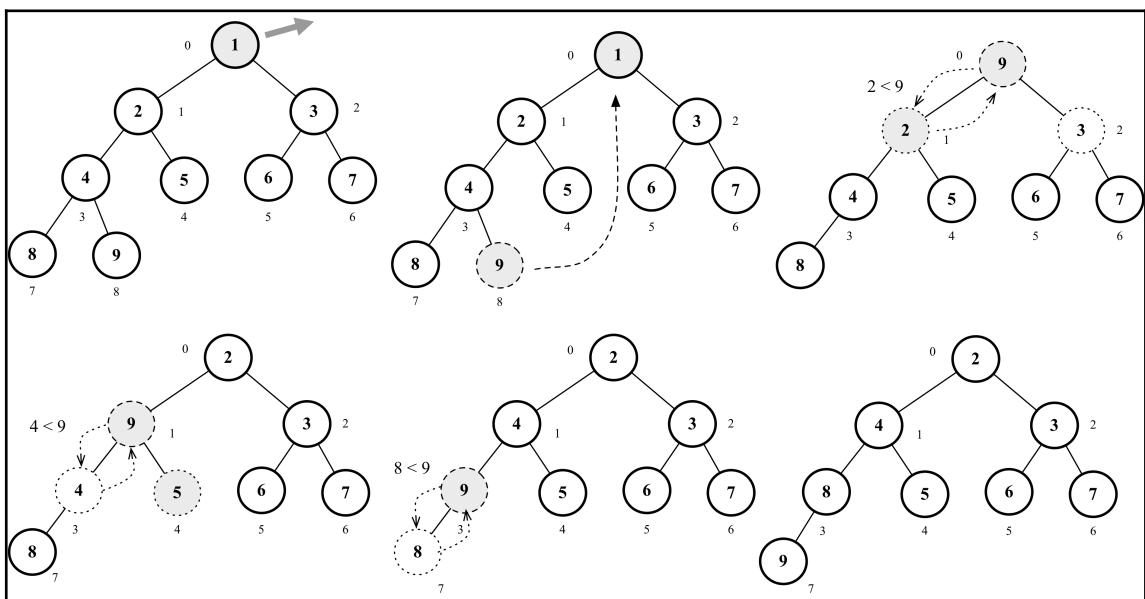
```

The `siftDown` method receives the `index` of the removed value. We will make a copy of the received `index` in the `element` variable. We will also retrieve the indexes of the `left` ({1}) and `right` ({2}) children.

The `sift down` operation consists of swapping the `element` with its smallest child (min heap) or greatest child (max heap). If the `element` is smaller than its left child ({3})—and the `index` is also valid), we will swap the `element` with its `left child` ({4}). If the `element` is smaller than its `right child` ({5})—and the `index` is also valid), we will swap the `element` with its `right child` ({6}).

After finding the smallest child `index`, we will verify whether its value is the same as the `index` of the `element` (passed to the `siftDown` method— {7})—no point in swapping the value with itself! If not, then we swap it with its smallest `element` ({8}) and we repeat the same process starting with the smallest `element` ({9}) until the `element` is placed in its correct position.

Suppose we want to do an extraction from the heap. The algorithm will perform a few `sift down` operations, as demonstrated in the following diagram:



The following code can be used to test the actions demonstrated in the diagram:

```
heap = new MinHeap();
for (let i = 1; i < 10; i++) {
    heap.insert(i);
}

console.log('Extract minimum: ', heap.extract()); // 1
```

Creating the MaxHeap class

The algorithm for the MaxHeap class will be exactly the same as the MinHeap class. The difference is that whenever we perform a $>$ (more than) comparison, we will change it to use the $<$ (less than) comparison.

The code for the MaxHeap class is presented as follows:

```
export class MaxHeap extends MinHeap {
    constructor(compareFn = defaultCompare) {
        super(compareFn);
        this.compareFn = reverseCompare(compareFn); // {1}
    }
}
```

But instead of copying the code and duplicating it, we can extend the `MinHeap` class to inherit all the code we created in this chapter and do a reverse comparison whenever needed. To reverse the comparison, instead of comparing `a` with `b`, we can compare `b` with `a` ({1}) instead, as demonstrated in the following code:

```
function reverseCompare(compareFn) {
    return (a, b) => compareFn(b, a);
}
```

We can use the same code that we used for the `MinHeap` to test the `MaxHeap`. The difference is that the biggest value will be the root of the heap instead of the lowest value:

```
const maxHeap = new MaxHeap();

maxHeap.insert(2);
maxHeap.insert(3);
maxHeap.insert(4);
maxHeap.insert(5);

maxHeap.insert(1);
```

```
console.log('Heap size: ', maxHeap.size()); // 5
console.log('Heap min value: ', maxHeap.findMinimum()); // 5
```

The heap sort algorithm

We can use the binary heap data structure to help us create a very famous sorting algorithm: the heap sort. The heap sort algorithm consists of three steps:

1. Create a max heap using the array to be sorted as the source.
2. After creating the max heap, the largest value will be stored in the first index of the heap. We will replace the first value with the last value of the heap, decreasing the size of the heap by 1.
3. Finally, we **heapify** (sift down) the root of the heap and repeat step 2 until the size of the heap is equal to 1.

We use the max heap results in an array sorted in ascending order (from smallest to biggest). If we want the array to be sorted in descending order, we can use the min heap instead.

The following is the code for the heap sort algorithm:

```
function heapSort(array, compareFn = defaultCompare) {
    let heapSize = array.length;
    buildMaxHeap(array, compareFn); // step 1
    while (heapSize > 1) {
        swap(array, 0, --heapSize); // step 2
        heapify(array, 0, heapSize, compareFn); // step 3
    }
    return array;
}
```

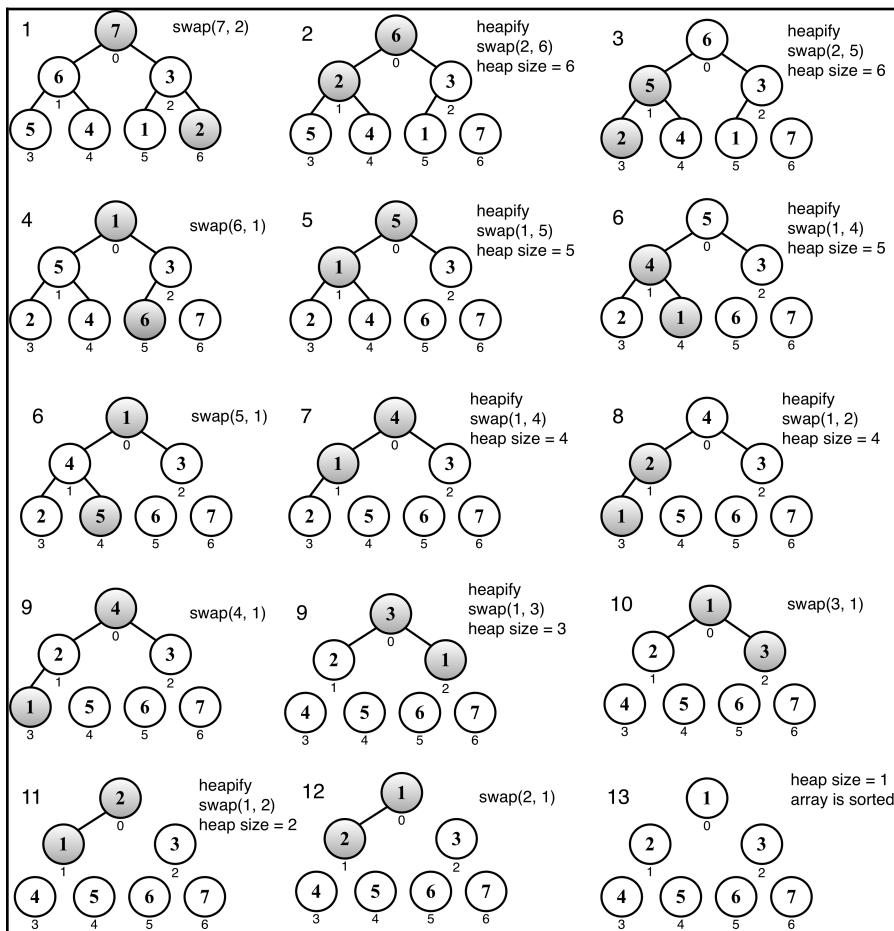
To build the max heap, we can use the following function:

```
function buildMaxHeap(array, compareFn) {
    for (let i = Math.floor(array.length / 2); i >= 0; i -= 1) {
        heapify(array, i, array.length, compareFn);
    }
    return array;
}
```

The max heap function will reorganize the array. Due to all the comparisons that will be made, we only need to run the `heapify` function (sift down) for the last half of the positions of the array (the first half will be organized automatically, so we do not need to run the function for the positions we know will be already sorted).

The `heapify` function has the same code as the `siftDown` method we created earlier in this chapter. The difference is that we also pass the heap itself, the size of the heap, and the comparison function we want to use as parameters. This is because we are not using the heap data structure directly, but we are using its logic to develop the `heapSort` algorithm.

The following diagram exemplifies the heap sort algorithm:



The following code can be used to test the `heapSort` function:

```
const array = [7, 6, 3, 5, 4, 1, 2];  
  
console.log('Before sorting: ', array);  
console.log('After sorting: ', heapSort(array));
```



The heap sort algorithm is not a stable sorting algorithm, meaning if the array is already sorted, it is possible that the values could end up in a different order. We will explore better sorting algorithms in Chapter 13, *Sorting and Searching Algorithms*.

Summary

In this chapter, we learned about the binary heap data structure and its two variants: the min heap and max heap. We learned how to insert values, how to peek or find the minimum or maximum values, and also how to extract a value from the heap. We also covered the sift up and sift down operations that help to maintain the organized heap.

We also learned how to use the heap data structure to create the heap sort algorithm.

In the next chapter, we will study the basic concepts of graphs, which are non-linear data structures.

12 Graphs

In this chapter, you will learn about another nonlinear data structure, called graphs. This will be the last data structure we will cover before diving into sorting and searching algorithms.

This chapter will cover a considerable part of the wonderful applications of graphs. Since this is a vast topic, we could write a book like this just to dive into the amazing world of graphs.

In this chapter, we will cover:

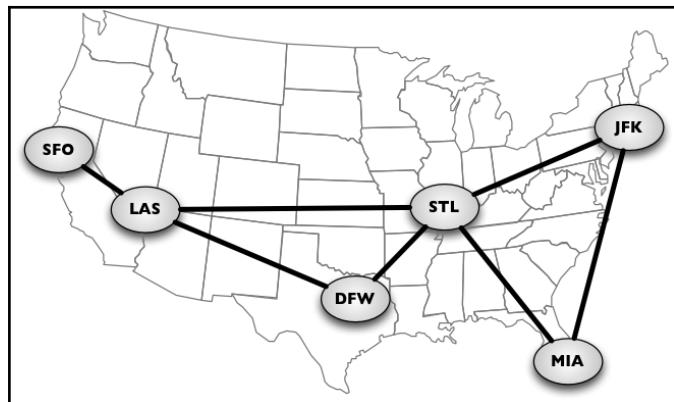
- Graph terminology
- Representing a graph in three different ways
- The graph data structure
- Graph search algorithms
- Shortest path algorithms
- Minimum spanning tree algorithms

Graph terminology

A **graph** is an abstract model of a network structure. A graph is a set of **nodes** (or **vertices**) connected by **edges**. Learning about graphs is important because any binary relationship can be represented by a graph.

Any social network, such as Facebook, Twitter, and Google+, can be represented by a graph.

We can also use graphs to represent roads, flights, and communications, as shown in the following image:

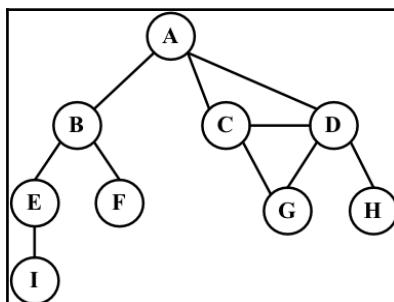


Let's learn more about the mathematical and technical concepts of graphs.

A graph $G = (V, E)$ is composed of:

- V : A set of vertices
- E : A set of edges connecting the vertices in V

The following diagram represents a graph:



Let's cover some graph terminology before we start implementing any algorithms.

Vertices connected by an edge are called **adjacent vertices**. For example, **A** and **B** are adjacent, **A** and **D** are adjacent, **A** and **C** are adjacent, and **A** and **E** are *not* adjacent.

A **degree** of a vertex consists of the number of adjacent vertices. For example, **A** is connected to three vertices. Therefore, **A** has degree 3. **E** is connected to two vertices. Therefore, **E** has degree 2.

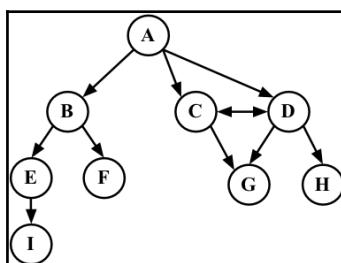
A **path** is a sequence of consecutive vertices, such as v_1, v_2, \dots, v_k , where v_i and v_{i+1} are adjacent. Using the graph from the previous diagram as an example, we have the paths **A B E I** and **A C D G**, among others.

A simple path does not contain repeated vertices. As an example, we have the path **A D G**. A **cycle** is a simple path, except for the last vertex, which is the same as the first vertex: **A D C A** (back to **A**).

A graph is **acyclic** if it does not have cycles. A graph is **connected** if there is a path between every pair of vertices.

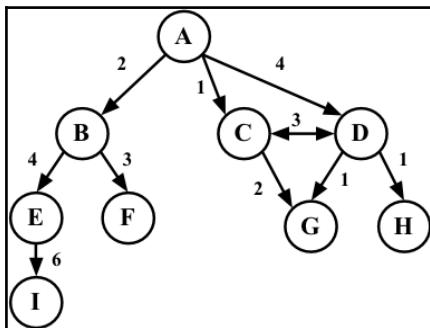
Directed and undirected graphs

Graphs can be **undirected** (where edges do not have a direction) or **directed (digraph)**, where edges have a direction, as demonstrated in the following diagram:



A graph is **strongly connected** if there is a path in both directions between every pair of vertices. For example, **C** and **D** are strongly connected, while **A** and **B** are not strongly connected.

Graphs can also be **unweighted** (as we have noted so far) or **weighted** (in which the edges have weights—or values), as shown in the following diagram:



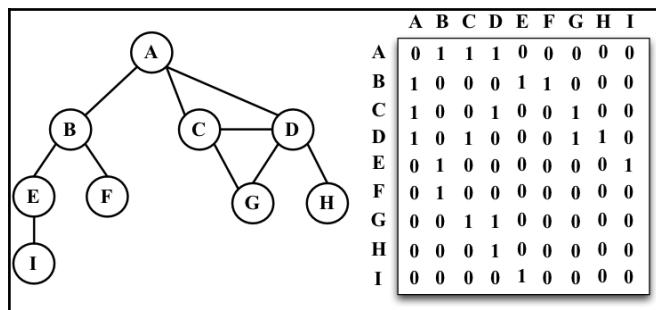
We can solve many problems in the computer science world using graphs, such as searching a graph for a specific vertex or searching for a specific edge, finding a path in the graph (from one vertex to another), finding the shortest path between two vertices, and cycle detection.

Representing a graph

There are a few ways in which we can represent graphs when it comes to data structures. There is no correct way of representing a graph among the existing possibilities. It depends on the type of problem you need to resolve, and the type of graph as well.

The adjacency matrix

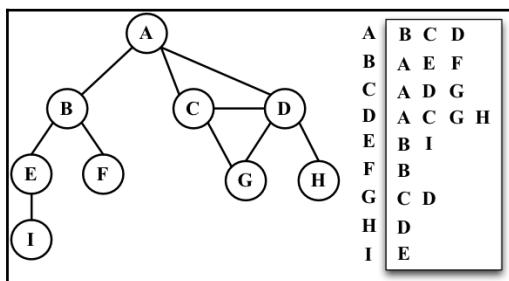
The most common implementation is the **adjacency matrix**. Each node is associated with an integer, which is the array index. We will represent the connectivity between vertices using a two-dimensional array, as `array[i][j] == 1` if there is an edge from the node with index `i` to the node with index `j` or as `array[i][j] == 0` otherwise, as demonstrated by the following diagram:



Graphs that are not strongly connected (**sparse graphs**) will be represented by a matrix with many zero entries in the adjacency matrix. This means we would waste space in the computer memory to represent edges that do not exist. For example, if we need to find the adjacent vertices of a given vertex, we will have to iterate through the whole row even if this vertex has only one adjacent vertex. Another reason this might not be a good representation is that the number of vertices in the graph may change, and a two-dimensional array is not flexible.

The adjacency list

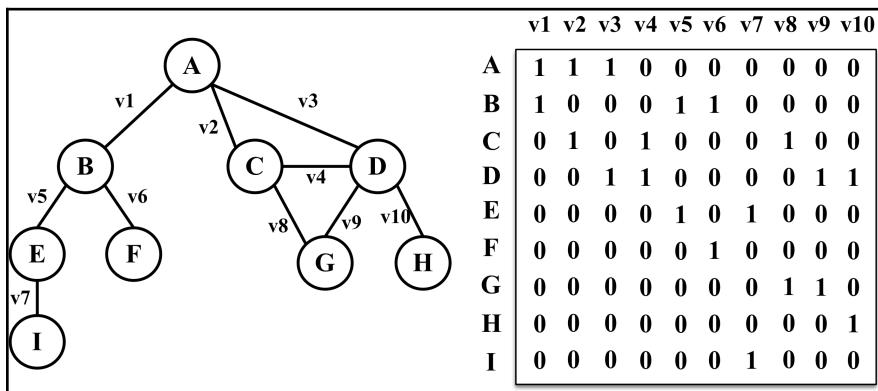
We can use a dynamic data structure to represent graphs as well, called an **adjacency list**. This consists of a list of adjacent vertices for every vertex of the graph. There are a few different ways we can represent this data structure. To represent the list of adjacent vertices, we can use a list (array), a linked list, or even a hash map or dictionary. The following diagram exemplifies the adjacency list data structure:



Both representations are very useful and have different properties (for example, finding out whether the vertices v and w are adjacent is faster using an adjacency matrix), although adjacency lists are probably better for most problems. We will use the adjacency list representation for the examples in this book.

The incidence matrix

We can also represent a graph using an **incidence matrix**. In an incidence matrix, each row of the matrix represents a vertex, and each column represents an edge. We will represent the connectivity between two objects using a two-dimensional array, as `array[v][e] == 1` if the vertex v is an incident upon edge e or as `array[v][e] == 0` otherwise, as demonstrated in the following diagram:



An incidence matrix is usually used to save space and memory when we have more edges than vertices.

Creating the Graph class

As usual, we will declare the basic structure of our class:

```
class Graph {
    constructor(isDirected = false) {
        this.isDirected = isDirected; // {1}
        this.vertices = []; // {2}
        this.adjList = new Dictionary(); // {3}
    }
}
```

The Graph constructor can receive a parameter to indicate if the graph is directed or not ({1}), and by default, the graph will not be directed. We will use an array to store the names of all the vertices of the graph ({2}), and we will use a dictionary (implemented in Chapter 8, *Dictionaries and Hashes*) to store the adjacent list ({3}). The dictionary will use the name of the vertex as a key and the list of adjacent vertices as a value.

Next, we will implement two methods: one to add a new vertex to the graph (because when we instantiate the graph, it will create an empty graph with no vertices), and another method to add edges between the vertices. Let's implement the `addVertex` method first, as follows:

```
addVertex(v) {  
    if (!this.vertices.includes(v)) { // {5}  
        this.vertices.push(v); // {6}  
        this.adjList.set(v, []); // {7}  
    }  
}
```

This method receives a vertex `v` as a parameter. We will add this vertex to the list of vertices (`{6}`) only if the vertex does not exist in the graph yet (`{5}`), and we will also initialize the adjacent list with an empty array by setting the dictionary value of the vertex `v` key with an empty array (`{7}`).

Now, let's implement the `addEdge` method via the following code:

```
addEdge(v, w) {  
    if (!this.adjList.get(v)) {  
        this.addVertex(v); // {8}  
    }  
    if (!this.adjList.get(w)) {  
        this.addVertex(w); // {9}  
    }  
    this.adjList.get(v).push(w); // {10}  
    if (!this.isDirected) {  
        this.adjList.get(w).push(v); // {11}  
    }  
}
```

This method receives two vertices as parameters, which are the vertices we want to link in the graph. Before we link the vertices, we will verify if the vertices exist in the graph. If vertices `v` or `w` do not exist in the graph, we will add them to the list of vertices (`{8}` and `{9}`).

Then, we will add an edge from vertex `v` to vertex `w` (`{10}`) by adding `w` to the adjacent list of `v`. If you want to implement a directed graph, line `{10}` is enough. As we are working with undirected graphs in most examples in this chapter, we also need to add an edge from `w` to `v` (`{11}`).



Note that we are only adding new elements to the array, as we have already initialized it in line {7}.

And to complete the creation of our `Graph` class, we will also declare two getter methods: one to return the list of vertices, and another one to return the adjacent list:

```
getVertices() {
    return this.vertices;
}
getAdjList() {
    return this.adjList;
}
```

Let's test this code, as follows:

```
const graph = new Graph();

const myVertices = ['A', 'B', 'C', 'D', 'E', 'F', 'G', 'H', 'I']; // {12}

for (let i = 0; i < myVertices.length; i++) { // {13}
    graph.addVertex(myVertices[i]);
}
graph.addEdge('A', 'B'); // {14}
graph.addEdge('A', 'C');
graph.addEdge('A', 'D');
graph.addEdge('C', 'D');
graph.addEdge('C', 'G');
graph.addEdge('D', 'G');
graph.addEdge('D', 'H');
graph.addEdge('B', 'E');
graph.addEdge('B', 'F');
graph.addEdge('E', 'I');
```

To make our lives easier, let's create an array with all the vertices we want to add to our graph ({12}). Then, we only need to iterate through the `myVertices` array and add the values one by one to our graph ({13}). Finally, we will add the desired edges ({14}). This code will create the graph we used in the diagrams presented so far in this chapter.

To make our lives even easier, let's also implement the `toString` method for the `Graph` class so that we can output the graph on the console:

```
toString() {
    let s = '';
    for (let i = 0; i < this.vertices.length; i++) { // {15}
        s += `${this.vertices[i]} -> `;
        const neighbors = this.adjList.get(this.vertices[i]); // {16}
        for (let j = 0; j < neighbors.length; j++) { // {17}
            s += `${neighbors[j]} `;
        }
        s += '\n'; // {18}
    }
    return s;
}
```

We will build a string with the adjacent list representation. First, we will iterate the list of `vertices` arrays ({15}) and add the name of the vertex to our string `s`. Then, we will get the adjacent list for this vertex ({16}), and we will also iterate it ({17}) to get the name of the adjacent vertex and add it to our string. After we iterate the adjacent list, we will add a new line to our string ({18}) so that we can see a pretty output on the console. Let's try this code:

```
console.log(graph.toString());
```

This will be the output:

```
A -> B C D
B -> A E F
C -> A D G
D -> A C G H
E -> B I
F -> B
G -> C D
H -> D
I -> E
```

A pretty adjacent list! From this output, we know that vertex `A` has the following adjacent vertices: `B`, `C`, and `D`.

Graph traversals

Similar to the tree data structure, we can also visit all the nodes of a graph. There are two algorithms that can be used to traverse a graph, called **breadth-first search (BFS)** and **depth-first search (DFS)**. Traversing a graph can be used to find a specific vertex or a path between two vertices, to check whether the graph is connected, to check whether it contains cycles, and so on.

Before we implement the algorithms, let's try to better understand the idea of traversing a graph.

The idea of **graph traversal algorithms** is that we must track each vertex when we first visit it and keep track of which vertices have not yet been completely explored. For both traversal graph algorithms, we need to specify which will be the first vertex to be visited.

To completely explore a vertex, we need to look at each edge of this vertex. For each edge connected to a vertex that has not been visited yet, we will mark it as discovered and add it to the list of vertices to be visited.

In order to have efficient algorithms, we must visit each vertex twice at the most when each of its endpoints is explored. Every edge and vertex in the connected graph will be visited.

The BFS and DFS algorithms are very similar, but with one important difference, which is the data structure used to store the list of vertices to be visited. Take a look at the following table:

Algorithm	Data structure	Description
DFS	Stack	By storing the vertices in a stack (learned in Chapter 4, <i>Stacks</i>), the vertices are explored along a path, visiting a new adjacent vertex if there is one available
BFS	Queue	By storing the vertices in a queue (learned in Chapter 5, <i>Queues and Deques</i>), the oldest unexplored vertices are explored first

When marking the vertices that we have already visited, we will use three colors to reflect their status:

- **White:** This represents that the vertex has not been visited
- **Grey:** This represents that the vertex has been visited but not explored
- **Black:** This represents that the vertex has been completely explored

This is why we must visit each vertex twice at the most, as mentioned earlier.

To help us mark the vertices in the BFS and DFS algorithms, we will use the `Colors` variable (that will work as an enumerator), declared as follows:

```
const Colors = {
    WHITE: 0,
    GREY: 1,
    BLACK: 2
};
```

Both algorithms will also need a helper object to help to store if the vertex has been visited or not. In the beginning of each algorithm, all the vertices will be marked as not visited (white color). We will use the following function to initialize the color for the vertices:

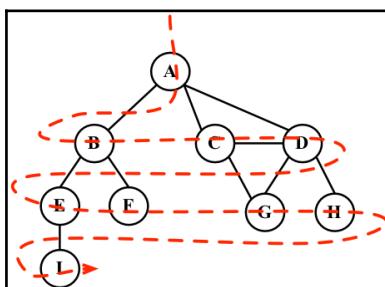
```
const initializeColor = vertices => {
    const color = {};
    for (let i = 0; i < vertices.length; i++) {
        color[vertices[i]] = Colors.WHITE;
    }
    return color;
};
```



Note we are using the ES2015 syntax to declare a function using a `const` and arrow functions that we learned in [Chapter 2, ECMAScript and TypeScript Overview](#). We could also declare the `initializeColor` function using the function syntax as `function initializeColor(vertices) {}`.

Breadth-first search (BFS)

The BFS algorithm starts traversing the graph from the first specified vertex and visits all its neighbors (adjacent vertices) first, one layer of the graph at a time. In other words, it visits the vertices first widely and then deeply, as demonstrated by the following diagram:



These are the steps followed by the BFS algorithm, starting at vertex v :

1. Create a queue Q
2. Mark v as discovered (grey) and enqueue v into Q
3. While Q is not empty, perform the following steps:
 1. dequeue u from Q
 2. Mark u as discovered (grey)
 3. enqueue all the unvisited (white) neighbors w of u
 4. Mark u as explored (black)

The BFS algorithm is declared as follows:

```
export const breadthFirstSearch = (graph, startVertex, callback) => {  
    const vertices = graph.getVertices();  
    const adjList = graph.getAdjList();  
    const color = initializeColor(vertices); // {1}  
    const queue = new Queue(); // {2}  
  
    queue.enqueue(startVertex); // {3}  
  
    while (!queue.isEmpty()) { // {4}  
        const u = queue.dequeue(); // {5}  
        const neighbors = adjList.get(u); // {6}  
        color[u] = Colors.GREY; // {7}  
        for (let i = 0; i < neighbors.length; i++) { // {8}  
            const w = neighbors[i]; // {9}  
            if (color[w] === Colors.WHITE) { // {10}  
                color[w] = Colors.GREY; // {11}  
                queue.enqueue(w); // {12}  
            }  
        }  
        color[u] = Colors.BLACK; // {13}  
        if (callback) { // {14}  
            callback(u);  
        }  
    }  
};
```

Let's dive into the BFS method implementation. The first thing we will do is use the `initializeColor` function to initialize the `color` array with the white color ({1}). We also need to declare and create a `Queue` instance ({2}) that will store the vertices that need to be visited and explored.

Following the steps we explained at the beginning of this chapter, the `breadthFirstSearch` function receives the `graph` instance and the vertex that will be used as the point of origin for our algorithm. As we need a starting point, we will enqueue this vertex into the queue ({3}).

If the queue is not empty ({4}), we will remove a vertex from the queue by using `dequeue` ({5}), and we will get its adjacency list that contains all its neighbors ({6}). We will also mark this vertex as `grey` ({7}), meaning we have discovered it (but have not finished exploring it yet).

For each neighbor of `u` ({8}), we will obtain its value (the name of the vertex, {9}), and if it has not been visited yet (the color of the vertex is `white`, {10}), we will mark that we have discovered it (the color is set to `grey`, {11}) and will add this vertex to the queue (line {12}) so that it can be finished exploring when we `dequeue` it from the queue.

When we finish exploring the vertex and its adjacent vertices, we will mark it as explored (the color is set to `black`, {13}).

The `breadthFirstSearch` function we are implementing also receives a `callback` (we used a similar approach in Chapter 10, *Trees*, for tree traversals). This parameter is optional, and if we pass any `callback` function ({14}), we will evoke it.

Let's test this algorithm by executing the following code:

```
const printVertex = (value) => console.log('Visited vertex: ' + value); // {15}

breadthFirstSearch(graph, myVertices[0], printVertex);
```

First, we declared a `callback` function ({15}) that will simply output on the browser's console the name of the vertex that was completely explored by the algorithm. Then, we called the `breadthFirstSearch` function, passing the `graph` (the same graph we used as the example to test the `Graph` class previously in this chapter), the first vertex (vertex `A` from the `myVertices` array that we also declared at the beginning of this chapter) and the `callback` function (`printVertex`). When we execute this code, the algorithm will output the following result in the browser's console:

```
Visited vertex: A
Visited vertex: B
Visited vertex: C
Visited vertex: D
Visited vertex: E
Visited vertex: F
Visited vertex: G
```

```
Visited vertex: H  
Visited vertex: I
```

The order of the vertices visited is the same as shown in the diagram at the beginning of this section.

Finding the shortest paths using BFS

So far, we have only demonstrated how the BFS algorithm works. We can use it for more things than just outputting the order of vertices visited. For example, how would we solve the following problem?

Given a graph G and the source vertex v , find the distance (number of edges) from v to each vertex $u \in G$ along the shortest path between v and u .

Given a vertex v , the BFS algorithm visits all the vertices with distance 1, then distance 2, and so on. So, we can use the BFS algorithm to solve this problem. We can modify the `breadthFirstSearch` function to return some information for us:

- The `distances[u]` from v to u
- The `predecessors[u]`, which are used to derive the shortest path from v to every other vertex u

Let's take a look at the implementation of an improved `BFS` function:

```
const BFS = (graph, startVertex) => {  
    const vertices = graph.getVertices();  
    const adjList = graph.getAdjList();  
    const color = initializeColor(vertices);  
    const queue = new Queue();  
    const distances = {} // {1}  
    const predecessors = {} // {2}  
    queue.enqueue(startVertex);  
  
    for (let i = 0; i < vertices.length; i++) { // {3}  
        distances[vertices[i]] = 0; // {4}  
        predecessors[vertices[i]] = null; // {5}  
    }  
  
    while (!queue.isEmpty()) {  
        const u = queue.dequeue();  
        const neighbors = adjList.get(u);  
        color[u] = Colors.GREY;  
        for (let i = 0; i < neighbors.length; i++) {
```

```

        const w = neighbors[i];
        if (color[w] === Colors.WHITE) {
            color[w] = Colors.GREY;
            distances[w] = distances[u] + 1; // {6}
            predecessors[w] = u; // {7}
            queue.enqueue(w);
        }
    }
    color[u] = Colors.BLACK;
}
return { // {8}
    distances,
    predecessors
};
};

```

What has changed in this version of the BFS method?

We also need to declare the `distances` array ({1}), and the `predecessors` array ({2}). The next step would be initializing the `distances` array with 0 ({4}) and the `predecessors` array with `null` ({5}) for every vertex of the graph ({3}).

When we discover the neighbor `w` of a vertex `u`, we will set the predecessor value of `w` as `u` ({7}) and also increment the distance ({6}) between `v` and `w` by adding 1 and the distance of `u` (as `u` is a predecessor of `w`, we have the value of `distances[u]` already).

At the end of the method, we can return an object with `distances` and `predecessors` ({8}).

Now, we can execute the `BFS` method again and store its return value in a variable, as follows:

```
const shortestPathA = BFS(graph, myVertices[0]);
console.log(shortestPathA);
```

As we executed the `BFS` method for the vertex `A`, this will be the output on the console:

```
distances: [A: 0, B: 1, C: 1, D: 1, E: 2, F: 2, G: 2, H: 2, I: 3],
predecessors: [A: null, B: "A", C: "A", D: "A", E: "B", F: "B", G: "C", H: "D", I: "E"]
```

This means that vertex A has a distance of 1 edge from vertices B, C, and D; a distance of 2 edges from vertices E, F, G, and H; and a distance of 3 edges from vertex I.

With the predecessor's array, we can build the path from vertex A to the other vertices using the following code:

```
const fromVertex = myVertices[0]; // {9}

for (i = 1; i < myVertices.length; i++) { // {10}
    const toVertex = myVertices[i]; // {11}
    const path = new Stack(); // {12}
    for (let v = toVertex;
        v !== fromVertex;
        v = shortestPathA.predecessors[v]) { // {13}
        path.push(v); // {14}
    }
    path.push(fromVertex); // {15}
    let s = path.pop(); // {16}
    while (!path.isEmpty()) { // {17}
        s += ' - ' + path.pop(); // {18}
    }
    console.log(s); // {19}
}
```

We will use the vertex A as the source vertex ({9}). For every other vertex (except vertex A, {10}), we will calculate the path from vertex A to it. To do so, we will get the value (name) of the vertex from the myVertices array ({11}), and we will create a stack to store the path values ({12}).

Next, we will follow the path from toVertex to fromVertex ({13}). The v variable will receive the value of its predecessor, and we will be able to take the same path backward. We will add the v variable to the stack ({14}). Finally, we will add the origin vertex to the stack as well ({15}) to have the complete path.

After this, we will create an s string, and we will assign the origin vertex to it (this will be the last vertex added to the stack, so it is the first item to be popped out—{16}). Until the path is empty ({17}), we will remove an item from the stack and concatenate it to the existing value of the s string ({18}). Finally, we simply output the path on the browser's console ({19}).

After executing the previous code, we will get the following output:

A - B
A - C
A - D

A – B – E
A – B – F
A – C – G
A – D – H
A – B – E – I

Here, we have the shortest path (number of edges) from A to the other vertices of the graph.

Further study on the shortest paths algorithms

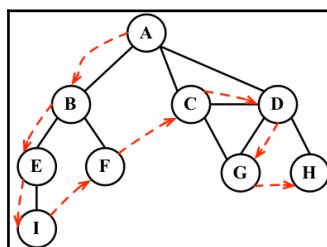
The graph we used in this example is not a weighted graph. If we want to calculate the shortest path in weighted graphs (for example, what the shortest path is between city A and city B, an algorithm used in GPS and Google Maps), BFS is not the appropriate algorithm.

There is **Dijkstra's algorithm**, which solves the single-source shortest path problem, for example. The **Bellman-Ford algorithm** solves the single-source problem if edge weights are negative. The **A* search algorithm** provides the shortest path for a single pair of vertices using heuristics to try to speed up the search. The **Floyd-Warshall algorithm** provides the shortest path for all pairs of vertices.

We will explore Dijkstra's algorithm and the Floyd-Warshall algorithm later in this chapter.

Depth-first search (DFS)

The DFS algorithm will start traversing the graph from the first specified vertex and will follow a path until the last vertex of this path is visited. Next, it is going to backtrack the path and then follow the next path. In other words, it visits the vertices first deep and then wide, as demonstrated in the following diagram:



The DFS algorithm does not need a source vertex. In the DFS algorithm, for each unvisited vertex v in graph G , visit the vertex v .

To visit vertex v , perform the following steps:

1. Mark v as discovered (grey).
2. For all unvisited (white) neighbors w of v , visit vertex w .
3. Mark v as explored (black).

As you can note, the DFS steps are recursive, meaning the DFS algorithm uses a stack to store the calls (a stack created by the recursive calls).

Let's implement the DFS algorithm, as follows:

```
const depthFirstSearch = (graph, callback) => { // {1}
    const vertices = graph.getVertices();
    const adjList = graph.getAdjList();
    const color = initializeColor(vertices);

    for (let i = 0; i < vertices.length; i++) { // {2}
        if (color[vertices[i]] === Colors.WHITE) { // {3}
            depthFirstSearchVisit(vertices[i], color, adjList, callback); // {4}
        }
    }
};

const depthFirstSearchVisit = (u, color, adjList, callback) => {
    color[u] = Colors.GREY; // {5}
    if (callback) { // {6}
        callback(u);
    }
    const neighbors = adjList.get(u); // {7}
    for (let i = 0; i < neighbors.length; i++) { // {8}
        const w = neighbors[i]; // {9}
        if (color[w] === Colors.WHITE) { // {10}
            depthFirstSearchVisit(w, color, adjList, callback); // {11}
        }
    }
    color[u] = Colors.BLACK; // {12}
};
```

The `depthFirstSearch` function received an instance of the `Graph` class and the `callback` function ({1}). After initializing the colors of each vertex, for each unvisited vertex {2} and {3}) of the `Graph` instance, we will call the recursive (private) function `depthFirstSearchVisit`, passing the vertex that is being visited `u`, the `color` array, and the `callback` function ({4}).

Whenever we visit the `u` vertex, we will mark it as discovered (grey, {5}). If there is a `callback` function ({6}), we will evoke it. Then, the next step is getting the list of neighbors of the vertex `u` ({7}). For each unvisited (color white, {10} and {8}) neighbor `w` ({9}) of `u`, we will call the `depthFirstSearchVisit` function, passing `w` as the vertex to be visited ({11}, adding `w` to the stack so it can be visited next). At the end, after the vertex and its adjacent vertices are visited deeply, we will backtrack, meaning the vertex is completely explored and is marked with color black ({12}).

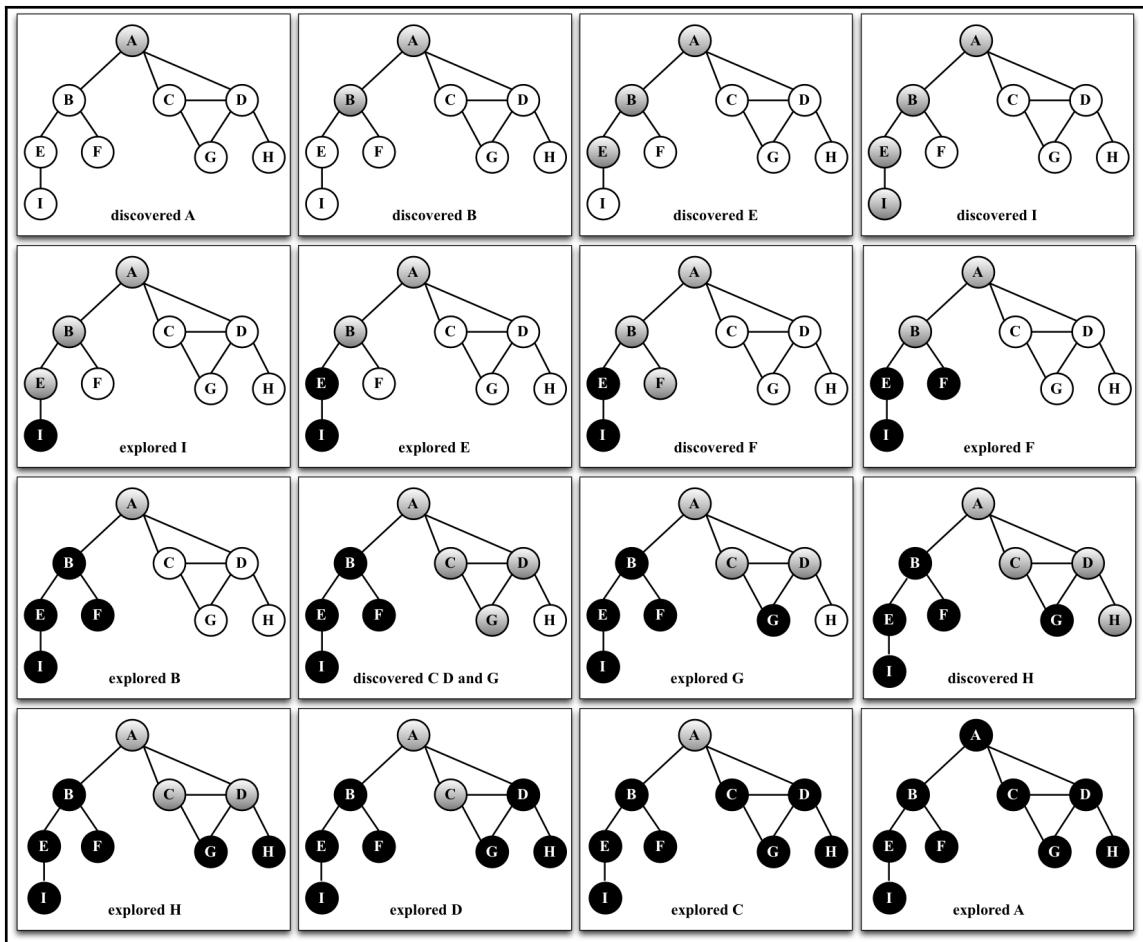
Let's test the `depthFirstSearch` method by executing the following code:

```
depthFirstSearch(graph, printVertex);
```

This will be its output:

```
Visited vertex: A
Visited vertex: B
Visited vertex: E
Visited vertex: I
Visited vertex: F
Visited vertex: C
Visited vertex: D
Visited vertex: G
Visited vertex: H
```

The order is the same as demonstrated by the diagram at the beginning of this section. The following diagram demonstrates the step-by-step process of the algorithm:



In this graph that we used as an example, line { 4 } will be executed only once, because all the other vertices have a path to the first one that is called the `depthFirstSearchVisit` function (vertex A). If vertex B is the first one to call the function, then line { 4 } would be executed again for another vertex (for example, vertex A).



The algorithm used by **Angular** (v2+) in its change detection logic (verify if the HTML template needs to be updated) is very similar to the DFS algorithm. To learn more about it, please visit <https://goo.gl/9kQj4i>. Data structures and algorithms are also important to understand how popular frontend frameworks work and take your knowledge to the next level!

Exploring the DFS algorithm

So far, we have only demonstrated how the DFS algorithm works. We can use it for other functionalities than just outputting the order of vertices visited.

Given a graph G , the DFS algorithm traverses all the vertices of G and constructs a forest (a collection of **rooted trees**) together with a set of source vertices (roots) and outputs two arrays: the discovery time and finish explorer time. We can modify the `depthFirstSearch` function to return some information for us, such as the following:

- The discovery time $d[u]$ of u
- The finish time $f[u]$ when u is marked black
- The predecessors $p[u]$ of u

Let's take a look at the implementation of the `BFS` method:

```
export const DFS = graph => {
    const vertices = graph.getVertices();
    const adjList = graph.getAdjList();
    const color = initializeColor(vertices);
    const d = {};
    const f = {};
    const p = {};
    const time = { count : 0}; // {1}
    for (let i = 0; i < vertices.length; i++) { // {2}
        f[vertices[i]] = 0;
        d[vertices[i]] = 0;
        p[vertices[i]] = null;
    }
    for (let i = 0; i < vertices.length; i++) {
        if (color[vertices[i]] === Colors.WHITE) {
            DFSVisit(vertices[i], color, d, f, p, time, adjList);
        }
    }
    return { // {3}
        discovery: d,
        finished: f,
```

```
    predecessors: p
  };
};

const DFSVisit = (u, color, d, f, p, time, adjList) => {
  color[u] = Colors.GREY;
  d[u] = ++time.count; // {4}
  const neighbors = adjList.get(u);
  for (let i = 0; i < neighbors.length; i++) {
    const w = neighbors[i];
    if (color[w] === Colors.WHITE) {
      p[w] = u; // {5}
      DFSVisit(w, color, d, f, p, time, adjList);
    }
  }
  color[u] = Colors.BLACK;
  f[u] = ++time.count; // {6}
};
```

As we want to track the time of discovery and the time when we finished exploring, we need to declare a variable to do this ({1}).



We are declaring the `time` as an object with `count` property due to the parameters by value and by reference method in JavaScript. In some languages, there is a difference when passing the parameters as values or references. The primitive values are passed by value, meaning the scope of the value will be only during the execution of the function. If we modify its value, the new value will have a scope only inside the function. When parameters are passed as references (objects), and if we modify any property from the object, we will be modifying the value. Objects are passed as references because only the reference to the memory is passed to the function or method. In this particular case, we want the time count updates to be used *globally* during the execution of this algorithm; hence we need to pass the object as a parameter, and not only its primitive value.

Next, we will declare the `d`, `f`, and `p` arrays, and we also need to initialize these arrays for each vertex of the graph ({2}). At the end of the method, we will return these values ({3}) so that we can work with them later.

When a vertex is first discovered, we will track its discovery time ({4}). When it is discovered as an edge from u , we also keep track of its predecessor ({5}). At the end, when the vertex is completely explored, we will track its finish time ({6}).

What is the idea behind the DFS algorithm? The edges are explored out of the most recently discovered vertex u . Only the edges to unvisited vertices are explored. When all the edges of u are explored, the algorithm backtracks to explore other edges where the vertex u was discovered. The process continues until we discover all the vertices that are reachable from the original source vertex. If any undiscovered vertices remain, we will repeat the process for a new source vertex. We will repeat the algorithm until all the vertices from the graph are explored.

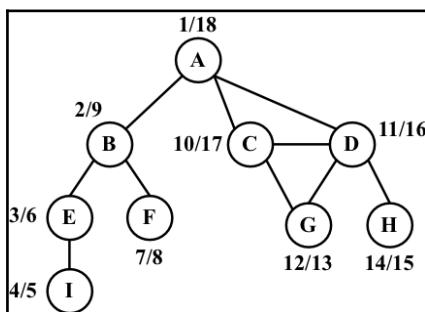
There are two things that we need to check in the DFS algorithm:

- The t ime variable can only have values from one to two times the number of vertices of the graph ($2|V|$)
- For all the vertices u , $d[u] < f[u]$ (meaning the discovered time needs to have a lower value than the finish time)

With these two assumptions, we have the following rule:

$$1 \leq d[u] < f[u] \leq 2|V|$$

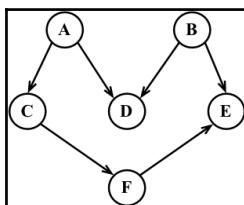
If we run the new DFS method for the same graph again, we will get the following discovery/finish time for each vertex of the graph:



However, what can we do with this information? Let's find out in the following section.

Topological sorting using DFS

Given the following graph, suppose each vertex is a task that you need to execute:



This is a directed graph, meaning there is an order that the tasks need to be executed in. For example, task **F** cannot be executed before task **A**. Note that the previous graph also does not have a cycle, meaning it is an acyclic graph. So, we can say that the previous graph is a **directed acyclic graph (DAG)**.

When we need to specify the order that some tasks or steps need to be executed in, it is called **topological sorting** (or **topsort** or even **toposort**). This problem is present in different scenarios of our lives. For example, when we start a computer science course, there is an order of disciplines that we can take before taking any other discipline (you cannot take Algorithms II before taking Algorithms I). When we are working in a project, there are some steps that need to be executed in order; for example, first we need to get the requirements from the client, then develop what is asked for by the client, and then deliver the project. You cannot deliver the project and then gather the requirements.

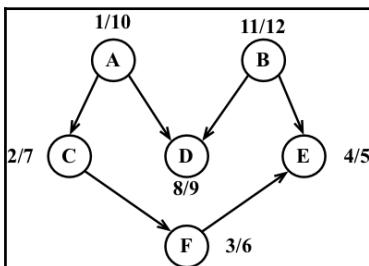
Topological sorting can only be applied to DAGs. So, how can we use topological sorting using DFS? Let's execute the DFS algorithm for the diagram presented at the beginning of this topic:

```
graph = new Graph(true); // directed graph

myVertices = ['A', 'B', 'C', 'D', 'E', 'F'];
for (i = 0; i < myVertices.length; i++) {
    graph.addVertex(myVertices[i]);
}
graph.addEdge('A', 'C');
graph.addEdge('A', 'D');
graph.addEdge('B', 'D');
graph.addEdge('B', 'E');
graph.addEdge('C', 'F');
graph.addEdge('F', 'E');

const result = DFS(graph);
```

This code will create the graph and its edges, execute the improved DFS algorithm, and store the results inside the `result` variable. The following diagram demonstrates the discovery and finish time of the graph after DFS is executed:



Now, all we have to do is sort the finishing time array and the decreasing order of finishing time, and we will have the topological sorting for the graph, as follows:

```
const fTimes = result.finished;
s = '';
for (let count = 0; count < myVertices.length; count++) {
    let max = 0;
    let maxName = null;
    for (i = 0; i < myVertices.length; i++) {
        if (fTimes[myVertices[i]] > max) {
            max = fTimes[myVertices[i]];
            maxName = myVertices[i];
        }
    }
    s += ' - ' + maxName;
    delete fTimes[maxName];
}
console.log(s);
```

After executing the preceding code, we will get the following output:

B - A - D - C - F - E

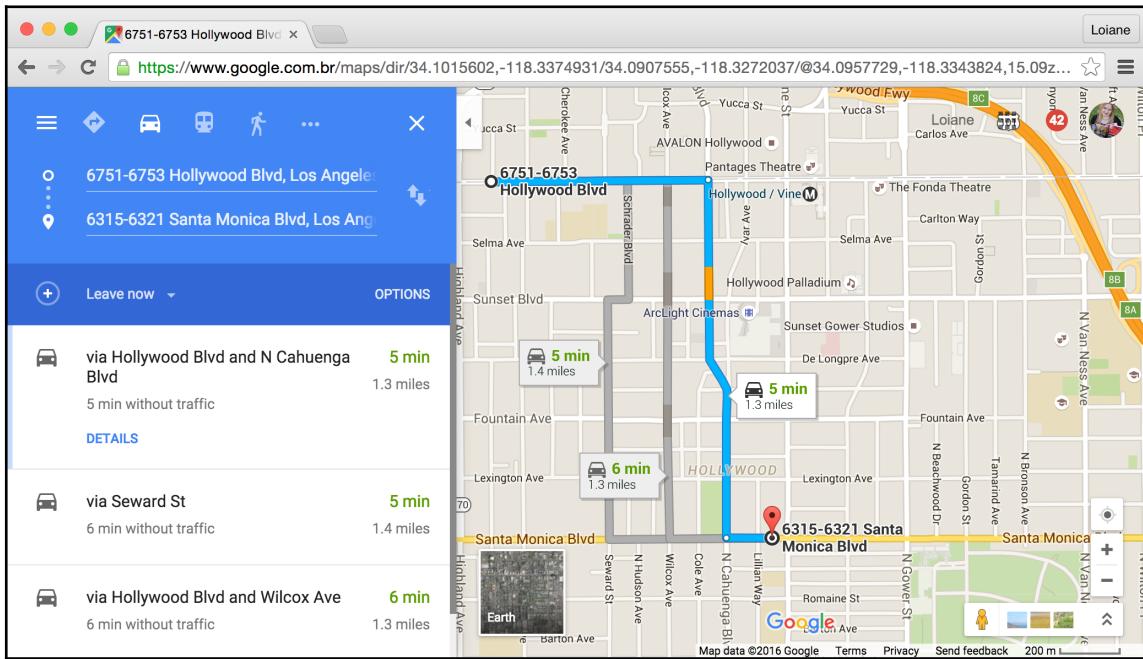
Note that the previous toposort result is only one of the possibilities. There might be different results if we modify the algorithm a little bit. For example, the following result is one of many other possibilities:

A - B - C - D - F - E

This could also be an acceptable result.

Shortest path algorithms

Given a map of streets, consider you want to get from point A to point B using the shortest path possible. We can use, as an example for this problem, directions from **Santa Monica Blvd** to **Hollywood Blvd** in Los Angeles, as demonstrated by the following screenshot:



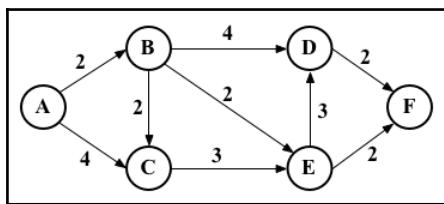
This is a very common problem in our lives, and we will use apps such as *Apple*, or *Google Maps*, or *Waze* to try to solve it, especially if you live in a big city. Of course, we also have other constraints involved, such as time or car traffic, but the original problem remains: how do we get from A to B using the shortest path?

We can use graphs to solve this problem for us, and the algorithm is called the shortest path. There are two algorithms that are very famous, which are Dijkstra's algorithm and the Floyd-Warshall algorithm, which we will cover in the next sections.

Dijkstra's algorithm

Dijkstra's algorithm is a **greedy algorithm** (you will learn more about greedy algorithms in Chapter 14, *Algorithm Design and Techniques*) to calculate the shortest path between a single source and all the other sources, meaning we can use it to calculate the shortest path from a graph vertex to all the other vertices.

Consider the following graph:



Let's take a look at how we can find the shortest path between the vertex A and all the other vertices. But first, we need to declare the adjacent matrix that represents the preceding graph, as follows:

```

var graph = [[0, 2, 4, 0, 0, 0],
             [0, 0, 1, 4, 2, 0],
             [0, 0, 0, 0, 3, 0],
             [0, 0, 0, 0, 0, 2],
             [0, 0, 0, 3, 0, 2],
             [0, 0, 0, 0, 0, 0]];
  
```

Dijkstra's algorithm is given as follows:

```

const INF = Number.MAX_SAFE_INTEGER;

const dijkstra = (graph, src) => {
  const dist = [];
  const visited = [];
  const { length } = graph;
  for (let i = 0; i < length; i++) { // {1}
    dist[i] = INF;
    visited[i] = false;
  }
  dist[src] = 0; // {2}
  for (let i = 0; i < length - 1; i++) { // {3}
    const u = minDistance(dist, visited); // {4}
    visited[u] = true; // {5}
    for (let v = 0; v < length; v++) {
      if (!visited[v] &&
        graph[u][v] < INF) {
        dist[v] = Math.min(dist[v], dist[u] + graph[u][v]);
      }
    }
  }
}

function minDistance(dist, visited) {
  let min = INF;
  let index = -1;
  for (let i = 0; i < dist.length; i++) {
    if (!visited[i] && dist[i] < min) {
      min = dist[i];
      index = i;
    }
  }
  return index;
}
  
```

```

        graph[u][v] !== 0 &&
        dist[u] !== INF &&
        dist[u] + graph[u][v] < dist[v]) { // {6}
        dist[v] = dist[u] + graph[u][v]; // {7}
    }
}
}
return dist; // {8}
};

```

The following is a description of how the algorithm works:

1. {1}: First, we need to initialize all distances (`dist`) as infinite (JavaScript max number `INF = Number.MAX_SAFE_INTEGER`) and `visited[]` as false
2. {2}: Second, we will set the distance of the source vertex from itself as 0
3. {3}: Then, we will find the shortest path for all vertices
4. {4}: To do so, we need to select the minimum distance vertex from the set of vertices that have not been processed yet
5. {5}: We need to mark the selected vertex as `visited` so that we do not calculate it twice
6. {6}: In case the shortest path is found, we will set the new value for the shortest path ({7})
7. {8}: After all the vertices are processed, we will return the result containing the shortest path value from the vertex source (`src`) to all the other vertices of the graph

To calculate the `minDistance`, we will search for the minimum value in the `dist` array, as follows, and return the array index that contains the minimum value:

```

const minDistance = (dist, visited) => {
    let min = INF;
    let minIndex = -1;
    for (let v = 0; v < dist.length; v++) {
        if (visited[v] === false && dist[v] <= min) {
            min = dist[v];
            minIndex = v;
        }
    }
    return minIndex;
};

```

If we execute the preceding algorithm for the graph we presented at the beginning of the section, we will have the following output:

0	0
1	2
2	4
3	6
4	4
5	6



It is also possible to modify the algorithm to return the value of the shortest path and also the path itself.

The Floyd-Warshall algorithm

The Floyd-Warshall algorithm is a **dynamic programming algorithm** (you will learn more about dynamic programming in [Chapter 14, Algorithm Design and Techniques](#)) to calculate all the shortest paths on a graph. With this algorithm, we can find the shortest path from all the sources to all the vertices.

The Floyd-Warshall algorithm is given as follows:

```
const floydWarshall = graph => {
  const dist = [];
  const { length } = graph;
  for (let i = 0; i < length; i++) { // {1}
    dist[i] = [];
    for (let j = 0; j < length; j++) {
      if (i === j) {
        dist[i][j] = 0; // {2}
      } else if (!isFinite(graph[i][j])) {
        dist[i][j] = Infinity; // {3}
      } else {
        dist[i][j] = graph[i][j]; // {4}
      }
    }
  }
  for (let k = 0; k < length; k++) { // {5}
    for (let i = 0; i < length; i++) {
      for (let j = 0; j < length; j++) {
        if (dist[i][k] + dist[k][j] < dist[i][j]) { // {6}
          dist[i][j] = dist[i][k] + dist[k][j]; // {7}
        }
      }
    }
  }
}
```

```

        }
    }
}
return dist;
};

```

The following is the description of how the algorithm works.

First, we will initiate the distance array with the value of the weight between each vertex (`{1}`) as the minimum possible distance between `i` and `j` is the weight of these vertices (`{4}`). The distance of the vertex to itself is zero (`{2}`). In case there is no edge between two vertices, we will represent it as `Infinity` (`{3}`). Using vertices `0...k` as intermediate points (`{5}`), the shortest path between `i` and `j` is given through `k`. The formula used to calculate the shortest path between `i` and `j` through vertex `k` is given in line `{6}`. If a new value for the shortest path is found, we will use it and store it (`{7}`).

The formula in line `{6}` is the heart of the Floyd-Warshall algorithm. If we execute the preceding algorithm with the graph we exemplified at the beginning of the section, we will have the following output:

```

0  2  4  6  4  6
INF 0  2  4  2  4
INF INF 0  6  3  5
INF INF INF 0  INF 2
INF INF INF 3  0  2
INF INF INF INF INF 0

```

Here, `INF` means that there is no shortest path between vertex `i` and `j`.

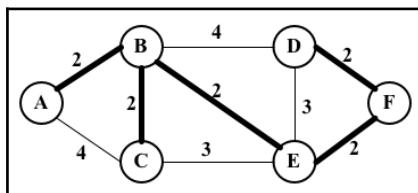
Another way of obtaining the same result would be to run Dijkstra's algorithm for each vertex of the graph.

Minimum spanning tree (MST)

The minimum spanning tree (MST) problem is very common in network designing. Imagine you have a business with several offices and want to connect the office's phone lines with each other with a minimum total cost to save money. Which is the best way of doing this?

This can also be applied to the island bridge problem. Consider you have an n number of islands and want to build bridges to connect each of them with a minimum cost.

Both the preceding problems can be solved with an MST algorithm, in which each office or island can be represented as a vertex of a graph, and the edges represent the cost. Here, we have an example of a graph where the thicker edges are a solution to the MST:



There are two main algorithms to find the minimal spanning trees: **Prim's algorithm** and **Kruskal's algorithm**, which you will learn in the following sections.

Prim's algorithm

Prim's algorithm is a greedy algorithm that finds an MST problem for a connected weighted undirected graph. It finds a subset of the edges that forms a tree that includes every vertex, where the total weight of all the edges in the tree is minimized.

Prim's algorithm is given as follows:

```
const INF = Number.MAX_SAFE_INTEGER;

const prim = graph => {
    const parent = [];
    const key = [];
    const visited = [];
    const { length } = graph;
    for (let i = 0; i < length; i++) { // {1}
        key[i] = INF;
        visited[i] = false;
    }
    key[0] = 0; // {2}
    parent[0] = -1;
    for (let i = 0; i < length - 1; i++) { // {3}
        const u = minKey(graph, key, visited); // {4}
        visited[u] = true; // {5}
        for (let v = 0; v < length; v++) {
            if (graph[u][v] && !visited[v] && graph[u][v] < key[v]) { // {6}
                parent[v] = u; // {7}
                key[v] = graph[u][v]; // {8}
            }
        }
    }
}
```

```

    }
    return parent; // {9}
};


```

The following is a description of how the algorithm works:

- 1}: First, we need to initialize all the `key` vertices as infinite (JavaScript max number `INF = Number.MAX_SAFE_INTEGER`) and `visited[]` as `false`
- 2}: Second, we will set the first `key` as 0 so that this vertex is picked as the first vertex and `parent[0] = -1` because the first node is always the root of the MST
- 3}: Then, we will find the MST for all vertices
- 4}: To do so, we need to select the minimum `key` vertex from the set of vertices that have not been processed yet (the same function as we used in Dijkstra's algorithm (`minDistance`) but with a different name)
- 5}: We need to mark the selected vertex as `visited` so that we do not calculate it twice
- 6}: In case a minimum weight is found, we will store the MST path value (`parent`, line {7}) and set the new cost for the MST value (line {8})
- 7}: After all the vertices are processed, we will return the result containing the MST



If we compare Prim's algorithm with Dijkstra's algorithm, we will see that they are very similar, with the exception of lines {7} and {8}. Line {7} keeps the `parent` array, which is the array that stores the MST. Line {8} stores the minimum edge value, while in Dijkstra's algorithm, the distance array is used instead of the `key` array to store the distance. We can modify Dijkstra's algorithm to add to the `parent` array, and this way, we can track the path along with its distance value.

Let's now execute the preceding algorithm for the following graph:

```

var graph = [[0, 2, 4, 0, 0, 0],
             [2, 0, 2, 4, 2, 0],
             [4, 2, 0, 0, 3, 0],
             [0, 4, 0, 0, 3, 2],
             [0, 2, 3, 3, 0, 2],
             [0, 0, 0, 2, 2, 0]];

```

We will have the following output:

Edge	Weight
0 – 1	2
1 – 2	2
5 – 3	2
1 – 4	2
4 – 5	2

Kruskal's algorithm

Similarly to Prim's algorithm, Kruskal's algorithm is also a greedy algorithm that finds the MST for a connected weighted undirected graph.

Kruskal's algorithm is given as follows:

```
const kruskal = graph => {
  const { length } = graph;
  const parent = [];
  let ne = 0;
  let a; let b; let u; let v;
  const cost = initializeCost(graph); // {1}
  while (ne < length - 1) { // {2}
    for (let i = 0, min = INF; i < length; i++) { // {3}
      for (let j = 0; j < length; j++) {
        if (cost[i][j] < min) {
          min = cost[i][j];
          a = u = i;
          b = v = j;
        }
      }
    }
    u = find(u, parent); // {4}
    v = find(v, parent); // {5}
    if (union(u, v, parent)) { // {6}
      ne++;
    }
    cost[a][b] = cost[b][a] = INF; // {7}
  }
  return parent;
};
```

The following is a description of how the algorithm works:

1. {1}: First, we will copy the adjacent matrix values to the cost array so that we can modify it without losing the original values ({7})
2. {2}: While the MST has fewer edges than total edges by -1
3. {3}: Find the edge with the minimum cost
4. **Lines {4} and {5}**: To avoid cycles, verify that the edge is already in the MST
5. {6}: If edges u and v are not the same, then add it to the MST
6. {7}: Remove the edges from the list so that we do not calculate it twice
7. {8}: Return the MST

The `find` function is given as follows. It prevents cycles in the MST:

```
const find = (i, parent) => {
    while (parent[i]) {
        i = parent[i];
    }
    return i;
};
```

The `union` function is also given here:

```
const union = (i, j, parent) => {
    if (i !== j) {
        parent[j] = i;
        return true;
    }
    return false;
};
```

There are a few variations of this algorithm that can be developed. It will depend on the data structure used to sort the weight of the edge's values (such as the priority queue) and also how the graph is represented.

Summary

In this chapter, we covered the basic concepts of graphs. We learned the different ways we can represent this data structure, and we created a class to represent a graph using an adjacency list. We also learned how to traverse a graph using BFS and DFS approaches. This chapter also covered two applications of BFS and DFS, which find the shortest path using BFS and topological sorting using DFS.

This chapter also covered some famous algorithms, such as Dijkstra's algorithm and the Floyd-Warshall algorithm, to calculate the shortest path. We also covered Prim's algorithm and Kruskal's algorithm to calculate the minimum spanning tree of a graph.

In the next chapter, you will learn about the most common sorting algorithms used in computer science.

13

Sorting and Searching Algorithms

Suppose we have a telephone directory (or a notebook) that does not have any sorting order. When you need to add a contact with telephone numbers, you simply write it down in the next available slot. Suppose you also have a high number of contacts in your contact list. On any ordinary day, you need to find a particular contact and his/her telephone number. However, as the contact list is not organized in any order, you have to check it contact by contact until you find the desired one. This approach is horrible, don't you agree? Imagine that you have to search for a contact in *Yellow Pages* and it is not organized! It could take forever!

For this reason, among others, we need to organize sets of information, such as the information we have stored in data structures. Sorting and searching algorithms are widely used in the daily problems we have to solve.

In this chapter, you will learn about the most commonly used sorting and searching algorithms, such as bubble sort, selection sort, insertion sort, shell sort, merge sort, quick sort, counting sort, bucket sort, and radix sort, as well as the sequential, interpolation, and binary search algorithms.

Sorting algorithms

In this section, we will cover some of the most well-known sorting algorithms in computer science. We will start with the slowest one, and then we will cover some better algorithms. We will understand that we first need to learn how to sort and then search for any given information.



You can see an animated version of how the most famous algorithms covered in this chapter work in the following links at <https://visualgo.net/en/sorting> and <https://www.toptal.com/developers/sorting-algorithms>.

Let's get started!

The bubble sort

When developers start learning sorting algorithms, they usually learn the bubble sort algorithm first, because it is the simplest of all the sorting algorithms. However, it is one of the worst-case sorting algorithms with respect to runtime, and you will see why.

The **bubble sort** algorithm compares every two adjacent values and swaps them if the first one is bigger than the second one. It has this name because the values tend to move up into the correct order, like bubbles rising to the surface.

Let's implement the bubble sort algorithm, as follows:

```
function bubbleSort(array, compareFn = defaultCompare) {  
    const { length } = array; // {1}  
    for (let i = 0; i < length; i++) { // {2}  
        for (let j = 0; j < length - 1; j++) { // {3}  
            if (compareFn(array[j], array[j + 1]) === Compare.BIGGER_THAN) { //  
{4}  
                swap(array, j, j + 1); // {5}  
            }  
        }  
    }  
    return array;  
}
```

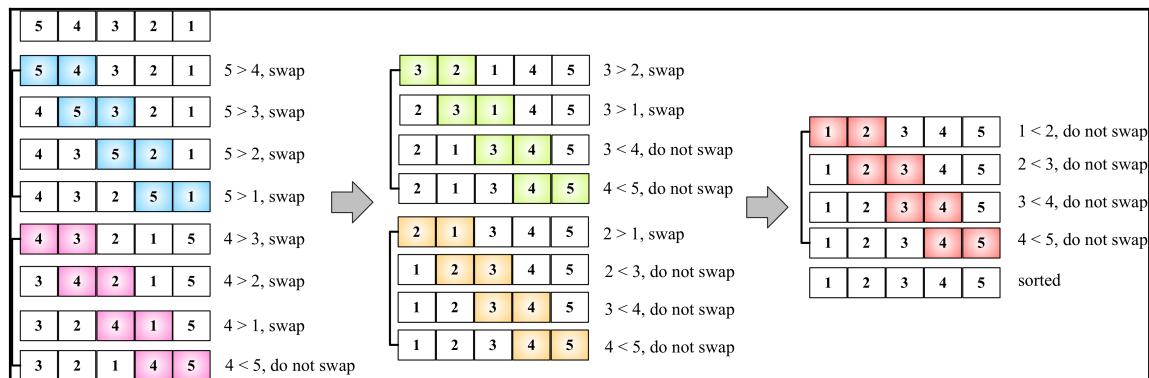
Each **non-distribution** sort algorithm we will create in this chapter will receive the array to be sorted as a parameter and a comparison function. To make testing easier to understand, we will work with arrays of numbers in our examples. But in case we need to sort an array of complex objects (array of people objects sorted by age property), our algorithm will be ready as well. The `compareFn` function to be used as default is the `defaultCompare` function we have used in previous chapters (`return a < b ? Compare.LESS_THAN : Compare.BIGGER_THAN`).

First, let's declare a variable called `length`, which will store the size of the array (`{1}`). This step will help us to get the size of the array on lines `{2}` and `{3}`, and this step is optional. Next, we will have an outer loop (`{2}`) that will iterate the array from its first position to the last one, controlling how many passes are done in the array (which should be one pass per item of the array as the number of passes is equal to the size of the array). Then, we have an inner loop (`{3}`) that will iterate the array, starting from its first position to the penultimate value that will actually do the comparison between the current value and the next one (`{4}`). If the values are out of order (that is, the current value is bigger than the next one), then we will swap them (`{5}`), meaning that the value of the `j+1` position will be transferred to the `j` position and vice versa.

We have created the `swap` function in chapter 11, *Binary Heap and Heap Sort*. Just to remind ourselves, the code for the `swap` function is presented as follows:

```
function swap(array, a, b) {
    /* const temp = array[a];
    array[a] = array[b];
    array[b] = temp; */ // classic way
    [array[a], array[b]] = [array[b], array[a]]; // ES2015 way
}
```

The following diagram illustrates the bubble sort in action:



Each different section in the preceding diagram represents a pass made by the outer loop (`{2}`), and each comparison between two adjacent values is made by the inner loop (`{3}`).

To test the bubble sort algorithm and get the same results shown in the diagram, we will use the following code:

```
function createNonSortedArray(size) { // 6
    const array = [];
    for (let i = size; i > 0; i--) {
        array.push(i);
    }
    return array;
}

let array = createNonSortedArray(5); // {7}
console.log(array.join()); // {8}
array = bubbleSort(array); // {9}
console.log(array.join()); // {10}
```

To help us test the sorting algorithms that you will learn in this chapter, we will create a function that will automatically create a non-sorted array with the size that is passed by the parameter ({6}). If we pass 5 as the parameter, the function will create the following array for us: [5, 4, 3, 2, 1]. Then, all we have to do is call this function and store its return value in a variable that contains the instance of the array initialized with some numbers ({7}). Just to make sure we have an unsorted array, we will output the array's content on the console ({8}), call the bubble sort function ({9}), and output the sorted array's content on the console again so that we can verify that the array was sorted ({10}).



You can find more examples and test cases on the source code that you downloaded from the support page (or from the GitHub repository at <https://github.com/loiane/javascript-datastructures-algorithms>).

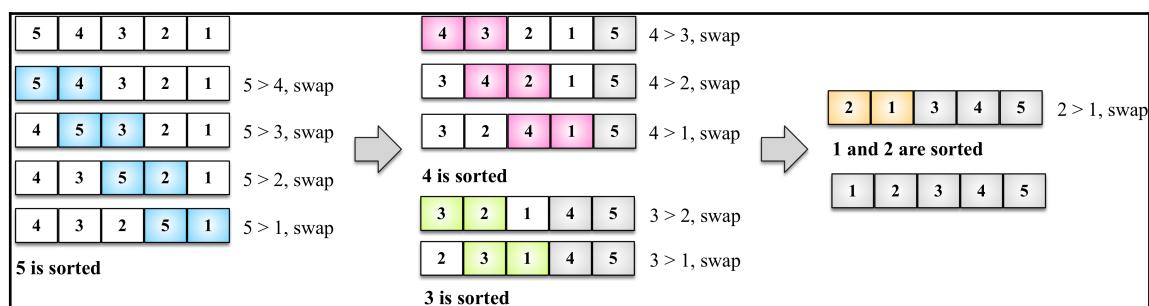
Note that when the algorithm executes the second pass of the outer loop (the second section of the previous diagram), the numbers 4 and 5 are already sorted. Nevertheless, on subsequent comparisons, we will keep comparing them even if the comparison is not needed. For this reason, we will make a small improvement on the bubble sort algorithm.

The improved bubble sort

If we subtract the number of passes from the inner loop, we will avoid all the unnecessary comparisons made by the inner loop ({1}):

```
function modifiedBubbleSort(array, compareFn = defaultCompare) {
  const { length } = array;
  for (let i = 0; i < length; i++) {
    for (let j = 0; j < length - 1 - i; j++) { // {1}
      if (compareFn(array[j], array[j + 1]) === Compare.BIGGER_THAN) {
        swap(array, j, j + 1);
      }
    }
  }
  return array;
}
```

The following diagram exemplifies how the improved bubble sort works:



Note that we did not compare the numbers that are already in place. Even though we made this small change to improve the bubble sort algorithm a little bit, it is not a recommended algorithm. It has a complexity of $O(n^2)$.

We will talk more about the **big O notation** in Chapter 15, *Algorithm Complexity*, to learn more about algorithms.

The selection sort

The **selection sort** algorithm is an in-place comparison sort algorithm. The general idea of the selection sort is to find the minimum value in the data structure, place it in the first position, then find the second minimum value, place it in the second position, and so on.

The following is the source code for the selection sort algorithm:

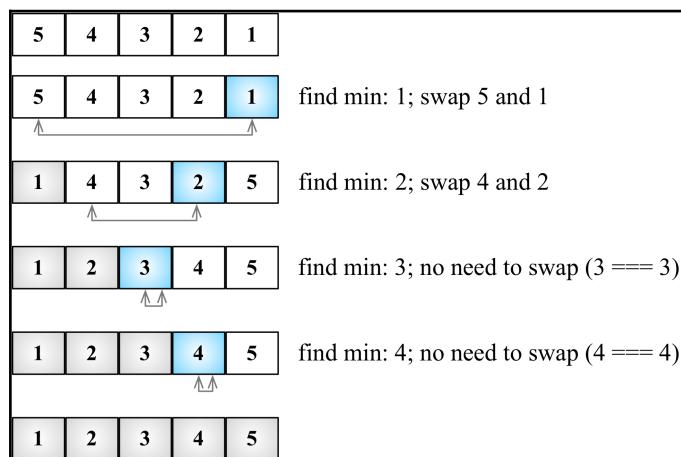
```
function selectionSort(array, compareFn = defaultCompare) {  
    const { length } = array; // {1}  
    let indexMin;  
    for (let i = 0; i < length - 1; i++) { // {2}  
        indexMin = i; // {3}  
        for (let j = i; j < length; j++) { // {4}  
            if (compareFn(array[indexMin], array[j]) === Compare.BIGGER_THAN) {  
                // {5}  
                indexMin = j; // {6}  
            }  
        }  
        if (i !== indexMin) { // {7}  
            swap(array, i, indexMin);  
        }  
    }  
    return array;  
};
```

First, we will declare some of the variables that we will use in the algorithm ({1}). Then, we have an outer loop ({2}) that will iterate the array and control the passes (that is, which n th value of the array we need to find next or the next minimum value). We will assume that the first value of the current pass is the minimum value of the array ({3}). Then, starting from the current i value to the end of the array ({4}), we will compare whether the value in the j position is lesser than the current minimum value ({5}); if this is true, we will change the value of the minimum to the new minimum value ({6}). When we get out of the inner loop ({4}), we will have the n th minimum value of the array. Then, if the minimum value is different from the original minimum value ({7}), we will swap them.

To test the selection sort algorithm, we can use the following code:

```
let array = createNonSortedArray(5);  
console.log(array.join());  
array = selectionSort(array);  
console.log(array.join());
```

The following diagram exemplifies the selection sort algorithm in action based on our array, which was created in the preceding code [5, 4, 3, 2, 1]:



The arrows at the bottom of the array indicate the positions currently in consideration to find the minimum value (inner loop: line {4}), and each step of the preceding diagram represents the outer loop (line {2}).

The selection sort is also an algorithm of complexity $O(n^2)$. Similar to the bubble sort, it contains two nested loops that are responsible for the quadratic complexity. However, the selection sort performs worse than the insertion sort algorithm, which we will learn next.

The insertion sort

The **insertion sort** algorithm builds the final sorted array one value at a time. It assumes that the first element is already sorted. Then, a comparison with the second value is performed—should the second value stay in its place or be inserted before the first value? The first two values will get sorted, then the comparison will take place with the third value (that is, should it be inserted in the first, second, or third position?), and so on.

The following code represents the insertion sort algorithm:

```
function insertionSort(array, compareFn = defaultCompare) {
  const { length } = array; // {1}
  let temp;
  for (let i = 1; i < length; i++) { // {2}
    let j = i; // {3}
    temp = array[i]; // {4}
```

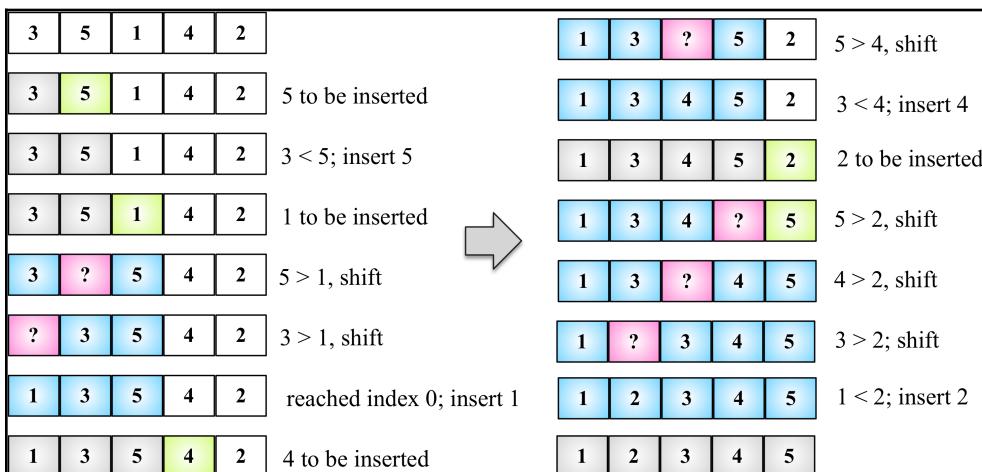
```

        while (j > 0 && compareFn(array[j - 1], temp) === Compare.BIGGER_THAN)
    { // {5}
        array[j] = array[j - 1]; // {6}
        j--;
    }
    array[j] = temp; // {7}
}
return array;
};

```

As usual, the first line of the algorithm is used to declare the variables we will use in the source code ({1}). Then, we will iterate the array to find the correct place for the value of *i* ({2}). Note that we started from the second position (index 1), instead of position 0 (as we considered the first value already sorted). Then, we assign the value of *i* to an auxiliary variable ({3}), and we also stored the value of the *i* position of the array in a temporary variable ({4}) so that we can insert it in the correct position later. The next step is finding the correct place to insert the value. As long as the *j* variable is bigger than 0 (because the first index of the array is 0 and there is no negative index) and the previous value in the array is bigger than the value we are comparing ({5}), we will shift the previous value to the current position ({6}) and decrease the value of *j*. At the end, we will insert the value in its correct position.

The following diagram exemplifies the insertion sort in action:



For example, suppose the array we are trying to sort is [3, 5, 1, 4, 2]. These values will be carried out in the steps performed by the insertion sort algorithm, as described in the following steps:

1. The value 3 is already sorted, so we will start sorting the second value of the array, which is the value 5. The value 3 is less than the value 5, so 5 stays in the same place (meaning the second position of the array). The values 3 and 5 are already sorted.
2. The next value to be sorted and inserted in the correct place is 1 (which is currently in the third position of the array). The value 5 is greater than 1, so 5 is shifted to the third position. We need to analyze whether 1 should be inserted in the second position—is 1 greater than 3? It's not, so the value 3 gets shifted to the second position. Next, we need to verify that 1 is inserted in the first position of the array. As 0 is the first position and there isn't a negative position, 1 needs to be inserted in the first position. The values 1, 3, and 5 are sorted.
3. We move to the next value: 4. Should the value 4 stay in the current position (index 3), or does it need to be moved to a lower position? The value 4 is less than 5, so 5 will get shifted to index 3. Should we insert 4 in index 2? The value 4 is greater than 3, so 4 is inserted in position 3 of the array.
4. The next value to be inserted is 2 (position 4 of the array). The value 5 is greater than 2, so 5 gets shifted to index 4. The value 4 is greater than 2, so 4 will also get shifted (position 3). The value 3 is also greater than 2, and 3 also gets shifted. The value 1 is less than 2, so 2 is inserted at the second position of the array. Thus, the array is sorted.

This algorithm has a better performance than the selection and bubble sort algorithms when sorting small arrays.

The merge sort

The **merge sort** algorithm is the first sorting algorithm that can be used in a real-world scenario. The three first sorting algorithms that we learned about in this book do not have a good performance, but the merge sort has good performance with a complexity of $O(n \log n)$.



The JavaScript `Array` class defines a `sort` function (`Array.prototype.sort`) that can be used to sort arrays using JavaScript (with no need to implement the algorithm ourselves). ECMAScript does not define which sorting algorithm needs to be used, so each browser can implement its own algorithm. For example, Mozilla Firefox uses the merge sort as the `Array.prototype.sort` implementation, while Chrome (V8 engine) uses a variation of the quick sort (which we will learn about next).

The merge sort is a divide-and-conquer algorithm. The idea behind it is to divide the original array into smaller arrays until each small array has only one position, and then merge these smaller arrays into bigger ones until we have a single big array at the end that is sorted.

Because of the divide-and-conquer approach, the merge sort algorithm is also recursive. We will divide the algorithm into two functions: the first one will be responsible for dividing the array into smaller ones and evoking the helper function that will perform the sort. Let's take a look at the main function declared here:

```
function mergeSort(array, compareFn = defaultCompare) {  
    if (array.length > 1) { // {1}  
        const { length } = array;  
        const middle = Math.floor(length / 2); // {2}  
        const left = mergeSort(array.slice(0, middle), compareFn); // {3}  
        const right = mergeSort(array.slice(middle, length), compareFn); // {4}  
        array = merge(left, right, compareFn); // {5}  
    }  
    return array;  
}
```

The merge sort will transform a bigger array into smaller arrays until they have only one value in them. As the algorithm is recursive, we need a stop condition—that is, if the array has a size less than 1 ({1}). If positive, we will return the array with size 1 or empty because it is already sorted.

If the array size is bigger than 1, then we will split it into smaller arrays. To do so, first we need to find the middle of the array ({2}), and once we find the middle, we will split the array into two smaller arrays, which we will call `left` ({3}) and `right` ({4}). The `left` array is composed of elements from index 0 to the middle index, and the `right` array consists of elements from the middle index to the end of the original array. Lines {3} and {4} will also evoke the `mergeSort` function itself until the `left` and `right` arrays have a size less than or equal to 1.

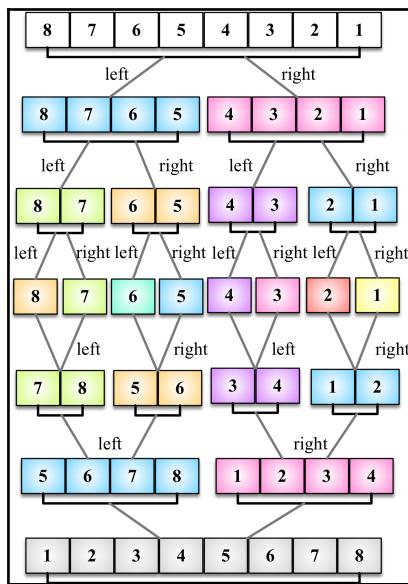
The next steps will be to call the `merge` function ({5}), which will be responsible for merging and sorting the smaller arrays into bigger ones until we have the original array sorted and back together. The `merge` function is presented here:

```
function merge(left, right, compareFn) {  
    let i = 0; // {6}  
    let j = 0;  
    const result = [];  
    while (i < left.length && j < right.length) { // {7}  
        result.push(  
            compareFn(left[i], right[j]) === Compare.LESS_THAN ? left[i++] :  
            right[j++]  
        ); // {8}  
    }  
    return result.concat(i < left.length ? left.slice(i) : right.slice(j));  
// {9}  
}
```

The `merge` function receives two arrays and merges them into a bigger array. During the `merge` is when the sorting happens. First, we need to declare a new array that will be created for the merge and also declare two variables ({6}) that will be used to iterate the two arrays (the `left` and `right` arrays). While we can iterate through the two arrays ({7}), we will compare whether the value from the `left` array is less than the value from the `right` array. If positive, we will add the value from the `left` array to the merged `result` array and also increment the variable that is used to iterate the array ({8}); otherwise, we will add the value from the `right` array and increment the variable that is used to iterate the array.

Next, we will add every remaining value from the `left` array ({9}) to the merged result array and will do the same for the remaining values from the `right` array. At the end, we will return a merged array.

If we execute the `mergeSort` function, this is how it will be executed:



Note that first the algorithm splits the original array until it has smaller arrays with a single element, and then it starts merging. While merging, it does the sorting as well until we have the original array completely back together and sorted.

The quick sort

The **quick sort** is probably the most used sorting algorithm. It has a complexity of $O(n \log n)$, and it usually performs better than other $O(n \log n)$ sorting algorithms. Similarly to the merge sort, it also uses the divide-and-conquer approach, dividing the original array into smaller ones (but without splitting them as the merge sort does) to do the sorting.

The quick sort algorithm is a little bit more complex than the other ones you have learned so far. Let's learn it step by step, as follows:

1. First, we need to select a value from the array called **pivot**, which will be the value at the middle of the array.

2. We will create two pointers (references)—the left-hand side one will point to the first value of the array, and the right-hand side one will point to the last value of the array. We will move the left pointer until we find a value that is bigger than the pivot, and we will also move the right pointer until we find a value that is less than the pivot and swap them. We will repeat this process until the left-hand side pointer passes the right-hand side pointer. This process helps to have values lower than the pivot reference before the pivot and values greater than the pivot after the pivot reference. This is called the **partition** operation.
3. Next, the algorithm repeats the previous two steps for smaller arrays (subarrays with smaller values and then subarrays with greater values) until the arrays are completely sorted.

Let's start the implementation of the quick sort algorithm using the following code:

```
function quickSort(array, compareFn = defaultCompare) {  
    return quick(array, 0, array.length - 1, compareFn);  
};
```

Similarly to the merge sort, we will start declaring the main method that will call the recursive function, passing the array that we want to sort along with index 0 and its last position (because we want to have the whole array sorted, not only a subset of it).

Next, we will declare the quick function, as follows:

```
function quick(array, left, right, compareFn) {  
    let index; // {1}  
    if (array.length > 1) { // {2}  
        index = partition(array, left, right, compareFn); // {3}  
        if (left < index - 1) { // {4}  
            quick(array, left, index - 1, compareFn); // {5}  
        }  
        if (index < right) { // {6}  
            quick(array, index, right, compareFn); // {7}  
        }  
    }  
    return array;  
};
```

First, we will declare the `index` variable ({1}), which will help us separate the subarray with smaller and greater values so that we can recursively call the `quick` function again. We will obtain the `index` value as the return value of the `partition` function ({3}).

If the size of the array is larger than 1 (because an array with a single element is already sorted—{2}), we will execute the `partition` operation on the given subarray (the first call will pass the complete array) to obtain the `index` ({3}). If a subarray with smaller elements exists ({4}), we will repeat the process for the subarray ({5}). We will do the same thing for the subarray with greater values. If there is any subarray with a greater value ({6}), we will repeat the quick sort process ({7}) as well.

Let's take a look how the partition process works in the next section.

The partition process

The first thing we need to do is choose the pivot element. There are a few ways in which we can do this. The simplest one is selecting the first value of the array (the leftmost value). However, studies show that this is not a good selection if the array is almost sorted, causing the worst behavior of the algorithm. Another approach is selecting a random value of the array or the middle value.

Now, let's take a look at the `partition` method:

```
function partition(array, left, right, compareFn) {  
    const pivot = array[Math.floor((right + left) / 2)]; // {8}  
    let i = left; // {9}  
    let j = right; // {10}  
  
    while (i <= j) { // {11}  
        while (compareFn(array[i], pivot) === Compare.LESS_THAN) { // {12}  
            i++;  
        }  
        while (compareFn(array[j], pivot) === Compare.BIGGER_THAN) { // {13}  
            j--;  
        }  
        if (i <= j) { // {14}  
            swap(array, i, j); // {15}  
            i++;  
            j--;  
        }  
    }  
    return i; // {16}  
}
```

For this implementation, we will select the middle value as the `pivot` ({8}). We will also initiate the two pointers: `left` (low at line {9}) with the first element of the array and `right` (high at line {10}) with the last element of the array.

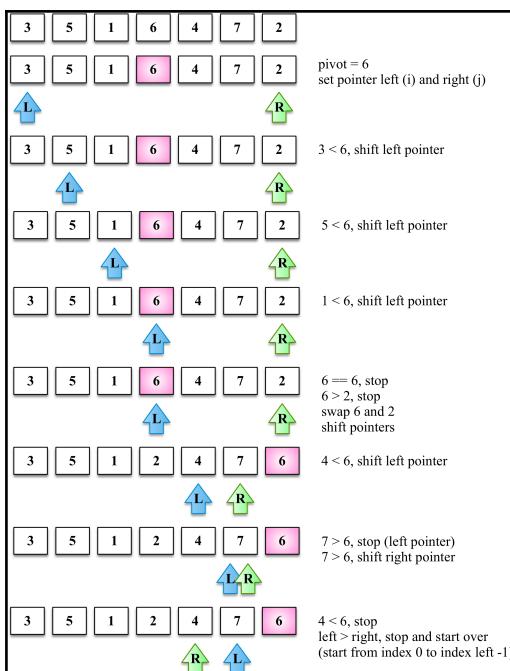
While the `left` and `right` pointers do not cross each other ({}11{}), we will execute the partition operation. First, until we find an element that is greater than the `pivot` ({}12{}), and we will shift the `left` pointer. We will do the same with the `right` pointer until we find an element that is less than the `pivot`, and we will shift the `right` pointer as well ({}13{}).

When the `left` pointer is greater than the `pivot` and the `right` pointer is lower than the `pivot`, we will compare whether the `left` pointer index is bigger than the `right` pointer index ({}14{}), meaning whether the left value is greater than the right value (in value). We will swap these values ({}15{}), shift both the pointers, and repeat the process (starting again at line {}11{}).

At the end of the partition operation, we will return the index of the `left` pointer that will be used to create the subarrays in line {}3{}.

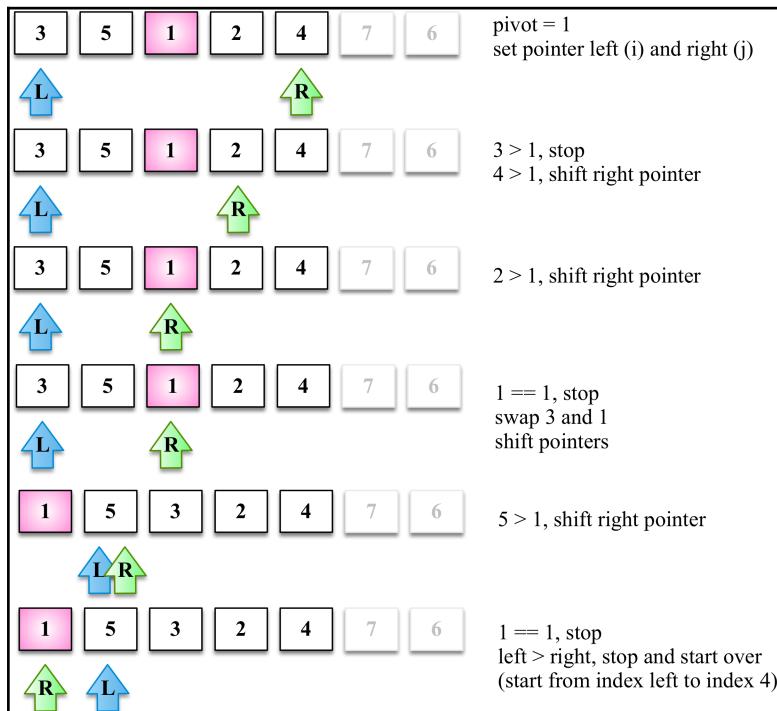
The quick sort in action

Let's take a look at the quick sort algorithm in action step by step:

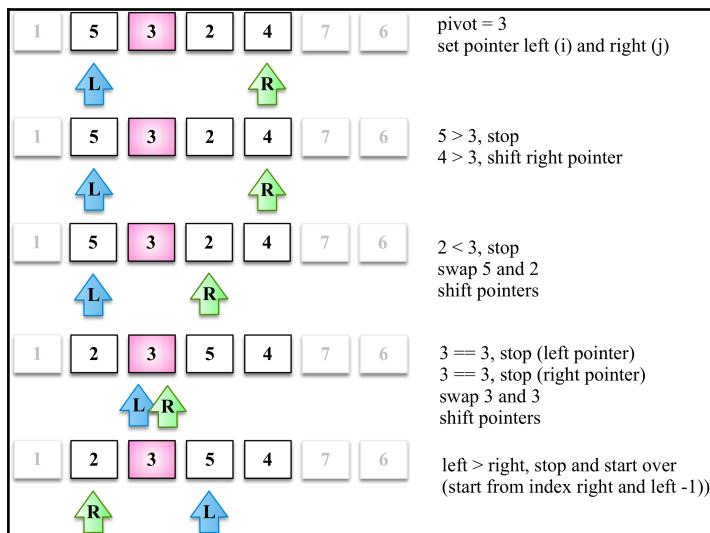


Given the `[3, 5, 1, 6, 4, 7, 2]` array, the preceding diagram represents the first execution of the partition operation.

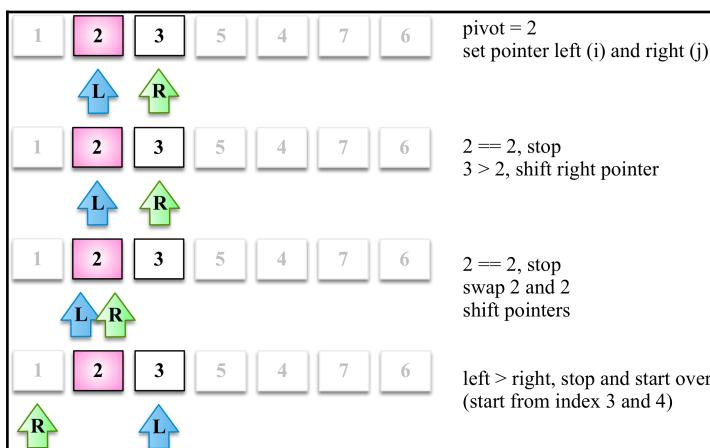
The following diagram exemplifies the execution of the partition operation for the first subarray of lower values (note that 7 and 6 are not part of the subarray):



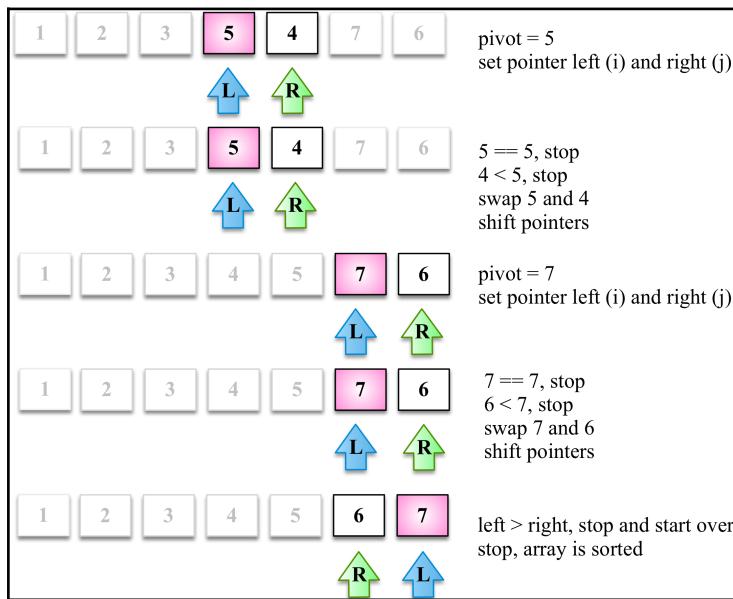
Next, we will continue creating subarrays, as seen in the following diagram, but now with greater values than the subarray of the preceding diagram (the lower subarray with value `1` does not need to be partitioned because it only contains one value):



The lower subarray [2, 3] from the ([2, 3, 5, 4]) subarray continues to be partitioned (line {5} from the algorithm):



Then, the greater subarray [5, 4] from the [2, 3, 5, 4] subarray also continues to be partitioned (line {7} from the algorithm), as shown in the following diagram:



At the end, the greater subarray [6, 7] will also get affected by the partition operation, completing the execution of the quick sort algorithm.

The counting sort

The **counting sort** is the first distribution sort we will learn about in this book. Distribution sort algorithms use auxiliary data structures (known as buckets) that are organized and then merged, resulting in the sorted array. The counting sort uses a temporary array that will store how many times each element appears in the original array. After all the elements are counted, the temporary array is sorted and it can be iterated to construct the resultant sorted array.

It is a good algorithm to sort integers (it is an **integer sorting algorithm**) with complexity $O(n + k)$, where k is the size of the temporary counting array; however, it does require more memory for the temporary array.

The following code represents the counting sort algorithm:

```
function countingSort(array) {
    if (array.length < 2) { // {1}
        return array;
    }
    const maxValue = findMaxValue(array); // {2}

    const counts = new Array(maxValue + 1); // {3}
    array.forEach(element => {
        if (!counts[element]) { // {4}
            counts[element] = 0;
        }
        counts[element]++;
    });
}

let sortedIndex = 0;
counts.forEach((count, i) => {
    while (count > 0) { // {6}
        array[sortedIndex++] = i; // {7}
        count--;
    }
});
return array;
}
```

If the array to be sorted has none or a single element ({1}), there is no need to run the sorting algorithm.

For the counting sort algorithm, we need to create the counts array, starting from index 0 (zero) until the maximum *value* + 1 index ({3}). For this reason, we also need to find what is the maximum value stored in the array ({2}). To find the maximum value of the array, we will simply need to iterate it and find what value is the higher one, as follows:

```
function findMaxValue(array) {
    let max = array[0];
    for (let i = 1; i < array.length; i++) {
        if (array[i] > max) {
            max = array[i];
        }
    }
    return max;
}
```

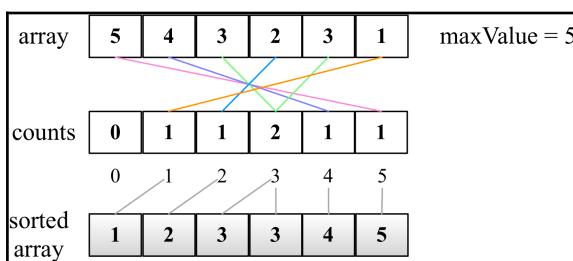
Next, we will iterate each position of the array and will increment the counting of the element in the `counts` array (`{5}`). Just to make sure the increment will work, if the `counts` array has not been initialized with 0 (zero) the first time we are counting the element, we assign the value zero to it as well (`{4}`).



In this algorithm, we are not using the `for` loop to iterate the arrays from index 0 to its length. This is to demonstrate that although the classic way of iterating arrays is using the `for` loop, we also have other possibilities, such as using the `forEach` method, as we learned about in Chapter 3, *Arrays*.

Now that all elements have been counted, we will iterate the `counts` array and construct the resultant sorted array. As there might be more than one element with the same value, we will add the element as many times as it appears in the original array. To do so, we will decrement the `count` (`{8}`) until its value is zero (`{6}`), adding the value (`i`) in the resultant array. For this reason, we also need an auxiliary index (`sortedIndex`) to help us in assigning the values to their correct index in the resultant sorted array.

Let's see the counting sort algorithm in action to help us understand the preceding code:



The bucket sort

The **bucket sort** algorithm (also known as bin sort) is also a distributed sorting algorithm that separates the elements into different *buckets* (smaller arrays), and then uses a simpler sorting algorithm, such as the insertion sort (a good algorithm for small arrays), to sort each bucket. It then merges all the buckets into the resultant sorted array.

The following code represents the bucket sort algorithm:

```
function bucketSort(array, bucketSize = 5) { // {1}
    if (array.length < 2) {
        return array;
```

```

    }
    const buckets = createBuckets(array, bucketSize); // {2}
    return sortBuckets(buckets); // {3}
}

```

For the bucket sort algorithm, we need to specify how many buckets will be used to sort the elements ({1}). By default, we will use 5 buckets. The bucket sort algorithm executes its best scenario when the elements can be distributed into the buckets evenly. If the elements are largely sparse, then using more buckets is better. If the elements are densely allocated, then using fewer buckets is better. And for this reason, we allow the `bucketSize` to be passed as a parameter.

We will divide the algorithm into two parts: the first part is creating the buckets and distributing the elements into the different buckets ({2}). The second part of the algorithm consists of running the insertion sort algorithm for each bucket and adding all bucket elements into the resultant sorted array ({3}).

Let's take a look at the code that is responsible for creating the buckets:

```

function createBuckets(array, bucketSize) {
    let minValue = array[0];
    let maxValue = array[0];
    for (let i = 1; i < array.length; i++) { // {4}
        if (array[i] < minValue) {
            minValue = array[i];
        } else if (array[i] > maxValue) {
            maxValue = array[i];
        }
    }
    const bucketCount = Math.floor((maxValue - minValue) / bucketSize) + 1;
    // {5}
    const buckets = [];
    for (let i = 0; i < bucketCount; i++) { // {6}
        buckets[i] = [];
    }
    for (let i = 0; i < array.length; i++) { // {7}
        const bucketIndex = Math.floor((array[i] - minValue) / bucketSize); // {8}
        buckets[bucketIndex].push(array[i]);
    }
    return buckets;
}

```

The first important step in the bucket sort is calculating how many elements will be distributed in each bucket ({}5). To calculate this number, we will use a formula that consists of calculating the difference between the higher and lower values of the array, divided by the bucket size. In this case, we also need to iterate the original array and find the maximum and minimum values ({}4). We could use the `findMaxValue` function that we created for the counting sort algorithm and also create a `findMinValue` function, but it would mean iterating through the same array twice. So, to optimize this search, we can find both values iterating the array only once.

After calculating the `bucketCount`, we need to initialize each bucket ({}6). The `buckets` data structure is a matrix (multidimensional array). Each position of the `buckets` variable will hold another array.

And the last step is to distribute the elements into the buckets. We need to iterate each element of the array ({}7), calculate what bucket we will put the element in ({}8), and insert the element into the correct bucket. This step concludes the first part of the algorithm.

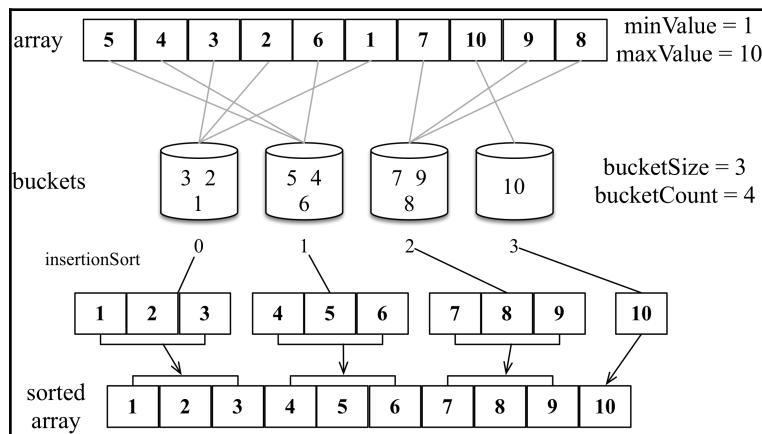
Let's take a look at the next part of the bucket sort algorithm, which is sorting each bucket:

```
function sortBuckets(buckets) {  
    const sortedArray = []; // {}9  
    for (let i = 0; i < buckets.length; i++) { // {}10  
        if (buckets[i] != null) {  
            insertionSort(buckets[i]); // {}11  
            sortedArray.push(...buckets[i]); // {}12  
        }  
    }  
    return sortedArray;  
}
```

We will create a new array which is going to our resultant sorted array ({}9)—this means the original array is not modified since we return a new one. Next, we will iterate through each valid bucket and will apply the insertion sort ({}11)—depending on the scenario, we could also apply other sorting algorithms, such as quick sort. And finally, we add all the elements from the sorted bucket into the sorted array ({}12).

Note that in one line {}12, we are using the destructing operator introduced in ES2015 that we learned about in [Chapter 2, ECMAScript and TypeScript Overview](#). A classic approach would be iterating each element of `buckets[i]` (`buckets[i][j]`) and adding each element separately into the sorted array.

The following diagram demonstrates how the bucket sort algorithm works in action:



The radix sort

The **radix sort** algorithm is also a distribution sort algorithm that distributes the integers into buckets based on a number's *significant digit* or value (the radix, hence the name radix sort). The radix is based on the number system of the values of the arrays.

For example, for numbers of the decimal system, radix 10 is used; therefore, the algorithm is going to use 10 buckets to distribute the elements and will first sort the numbers based on the 1s, then 10s, then 100s, and so on.

The following code represents the radix sort algorithm:

```
function radixSort(array, radixBase = 10) {
  if (array.length < 2) {
    return array;
  }
  const minValue = findMinValue(array);
  const maxValue = findMaxValue(array);

  let significantDigit = 1; // {1}
  while ((maxValue - minValue) / significantDigit >= 1) { // {2}
    array = countingSortForRadix(array, radixBase, significantDigit,
minValue); // {3}
    significantDigit *= radixBase; // {4}
  }
  return array;
}
```

Since the radix sort is also used to sort integers, we will start sorting all numbers by their last digit ({1}). It is also possible to modify this algorithm to make it work with alpha characters. We will sort the number based on their last digit only, and in the next iteration, we will sort the number based on their second significant digit (the 10s), then the third significant digit (the 100s), and on ({4}). We will do this until there are no significant digits to sort ({2}), and that is why we need to know the minimum and maximum values present in the array.

If the array to be sorted contains only values between 1 and 9, the loop in line {2} will run only once. If there are values less than 99, then the loop will run a second time, and so on.

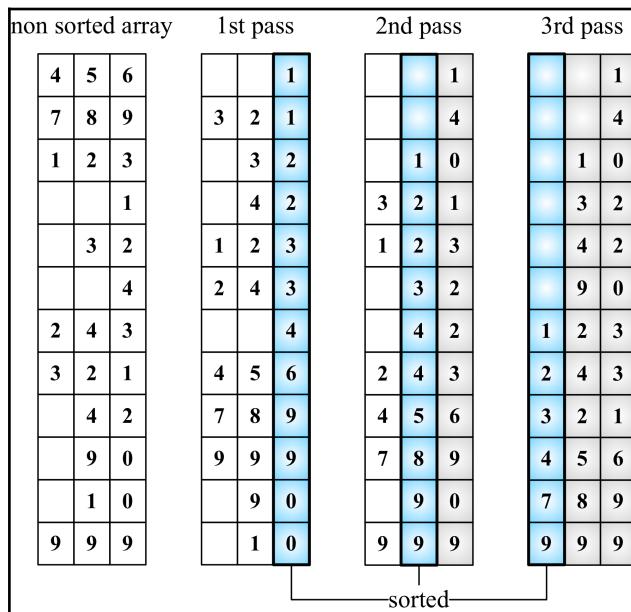
Let's take a look at the code that is responsible for sorting based on the significant digit (the radix):

```
function countingSortForRadix(array, radixBase, significantDigit, minValue)
{
    let bucketsIndex;
    const buckets = [];
    const aux = [];
    for (let i = 0; i < radixBase; i++) { // {5}
        buckets[i] = 0;
    }
    for (let i = 0; i < array.length; i++) { // {6}
        bucketsIndex = Math.floor(((array[i] - minValue) / significantDigit) %
radixBase); // {7}
        buckets[bucketsIndex]++;
    }
    for (let i = 1; i < radixBase; i++) { // {9}
        buckets[i] += buckets[i - 1];
    }
    for (let i = array.length - 1; i >= 0; i--) { // {10}
        bucketsIndex = Math.floor(((array[i] - minValue) / significantDigit) %
radixBase); // {11}
        aux[--buckets[bucketsIndex]] = array[i]; // {12}
    }
    for (let i = 0; i < array.length; i++) { // {13}
        array[i] = aux[i];
    }
    return array;
}
```

First, we initialize the buckets ({5}) based on the radix base. As we are working with base 10 numbers, we will work with 10 buckets. Next, we will do a counting sort ({8}) based on the significant digit of the numbers ({7}) that are in the array ({6}). Because we are doing a counting sort, we also need to compute the cumulates so we have a correct count ({9}).

After counting the values, we will start moving the values back to the original array. We will use a temporary array (`aux`) to help us with this task. For each value of the original array (`{10}`), we will retrieve its significant digit again (`{11}`) and will move its value to the `aux` array (subtracting the count from the `buckets` array—`{12}`). The last step is optional (`{13}`), as we transfer all the values from the `aux` array to the original array. As we are returning the array, we could return the `aux` array directly instead of copying its values.

Let's see how the radix sort algorithm works in action:



Searching algorithms

Now, let's talk about searching algorithms. If we take a look at the algorithms we implemented in previous chapters, such as the `search` method of the `BinarySearchTree` class (Chapter 10, *Trees*) or the `indexOf` method of the `LinkedList` class (Chapter 6, *Linked Lists*), these are all search algorithms, and of course, each one was implemented according to the behavior of its data structure. So we are already familiar with two search algorithms; we just do not know their "official" names yet!

The sequential search

The **sequential search** or **linear search** is the most basic search algorithm. It consists of comparing each element of the data structure with the one we are looking for. It is also the most inefficient one.

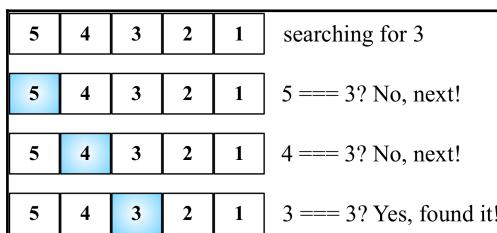
Let's take a look at its implementation:

```
const DOES_NOT_EXIST = -1;

function sequentialSearch(array, value, equalsFn = defaultEquals) {
    for (let i = 0; i < array.length; i++) { // {1}
        if (equalsFn(value, array[i])) { // {2}
            return i; // {3}
        }
    }
    return DOES_NOT_EXIST; // {4}
}
```

The sequential search iterates through the array ({1}) and compares each `value` with the value we are searching for ({2}). If we find it, we can return something to indicate that we found it. We can return the `value` itself, the `true`, or its `index` ({3}). In the preceding implementation, we returned the `index` of the `value`. If we don't find the `value`, we can return `-1` ({4}), indicating that the `index` does not exist; the values `false` and `null` are among the other options.

Suppose we have the `[5, 4, 3, 2, 1]` array and we are looking for the value `3`, then the following diagram shows the steps of the sequential search:



The binary search

The **binary search** algorithm works similar to the number guessing game, in which someone says "*I'm thinking of a number between 1 and 100*". We will begin by responding with a number, and the person will say "*higher*", "*lower*", or that we got it right.

To make the algorithm work, the data structure needs to be sorted first. These are the steps that the algorithm follows:

1. A value is selected in the middle of the array.
2. If the value is the one we are looking for, we are done (the value was found).
3. If the value we are looking for is less than the selected one, then we will go back to step 1 using the left subarray (lower).
4. If the value we are looking for is bigger than the selected one, then we will go back to step 1 using the right subarray (higher).

Let's take a look at its implementation:

```
function binarySearch(array, value, compareFn = defaultCompare) {  
    const sortedArray = quickSort(array); // {1}  
    let low = 0; // {2}  
    let high = sortedArray.length - 1; // {3}  
    while (lesserOrEquals(low, high, compareFn)) { // {4}  
        const mid = Math.floor((low + high) / 2); // {5}  
        const element = sortedArray[mid]; // {6}  
        if (compareFn(element, value) === Compare.LESS_THAN) { // {7}  
            low = mid + 1; // {8}  
        } else if (compareFn(element, value) === Compare.BIGGER_THAN) { // {9}  
            high = mid - 1; // {10}  
        } else {  
            return mid; // {11}  
        }  
    }  
    return DOES_NOT_EXIST; // {12}  
}
```

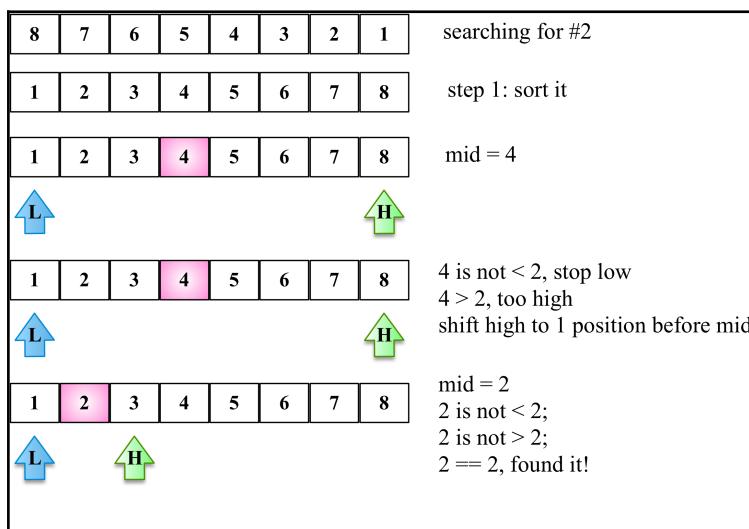
To get started, the first thing we need to do is sort the array. We can use any algorithm we implemented in the *Sorting algorithms* section. The quick sort was chosen for this implementation ({1}). After the array is sorted, we will set the `low` ({2}) and `high` ({3}) pointers (which will work as boundaries).

While `low` is lower than `high` ({4}), in this case, `low` is greater than `high`, which means that the value does not exist. So, we will return `-1` ({12}), find the middle index ({5}), and hence have the value of the middle `value` ({6}). Then, we will start comparing whether the selected `value` is less than the `value` we are looking for ({7}), and we need to go lower ({8}) and start over. If the selected `value` is greater than the `value` we are looking for ({9}), we need to go higher ({10}) and start over. Otherwise, it means that the `value` is equal to the `value` we are looking for; therefore, we will return its index ({11}).

The `lesserOrEquals` function used in the preceding code is declared here:

```
function lesserOrEquals(a, b, compareFn) {
    const comp = compareFn(a, b);
    return comp === Compare.LESS_THAN || comp === Compare.EQUALS;
}
```

Given the array in the following diagram, let's try to search for the value 2. These are the steps that the algorithm will perform:



The `BinarySearchTree` class we implemented in [Chapter 10, Trees](#), has the search method, which is exactly the same as the binary search but applied to tree data structures.



The interpolation search

The **interpolation search** algorithm is an improved variation of the binary search. While the binary search always checks the value in the `mid` position, the interpolation search might check different places of the array depending on the value that is being searched.

To make the algorithm work, the data structure needs to be sorted first. These are the steps that the algorithm follows:

1. A value is selected using the position formula
2. If the value is the one we are looking for, we are done (the value was found)
3. If the value we are looking for is lesser than the selected one, then we will go back to step 1 using the left subarray (lower)
4. If the value we are looking for is bigger than the selected one, then we will go back to step 1 using the right subarray (higher)

Let's take a look at its implementation:

```
function interpolationSearch(array, value,
    compareFn = defaultCompare,
    equalsFn = defaultEquals,
    diffFn = defaultDiff
) {
    const { length } = array;
    let low = 0;
    let high = length - 1;
    let position = -1;
    let delta = -1;
    while (
        low <= high &&
        biggerOrEquals(value, array[low], compareFn) &&
        lesserOrEquals(value, array[high], compareFn)
    ) {
        delta = diffFn(value, array[low]) / diffFn(array[high], array[low]); // {1}
        position = low + Math.floor((high - low) * delta); // {2}
        if (equalsFn(array[position], value)) { // {3}
            return position;
        }
        if (compareFn(array[position], value) === Compare.LESS_THAN) { // {4}
            low = position + 1;
        } else {
            high = position - 1;
        }
    }
}
```

```

        return DOES_NOT_EXIST;
    }
}

```

The first thing we need to do is calculate the position ({2}) to compare the value with. The idea of the formula is to find the higher value near the position if the searched value is closer to `array[high]` and the lowest value near the position if the searched value is closer to `array[low]`. This algorithm works better if the value instances are uniformly distributed in the array (delta will be very low if value instances are uniformly distributed) ({1}).

If the value is found, then we return its index ({3}). Otherwise, if the searched value is less than the value in the current position, we repeat the logic using the left subarray or the right subarray({4}).

The `lesserEquals` and `biggerEquals` functions are presented here:

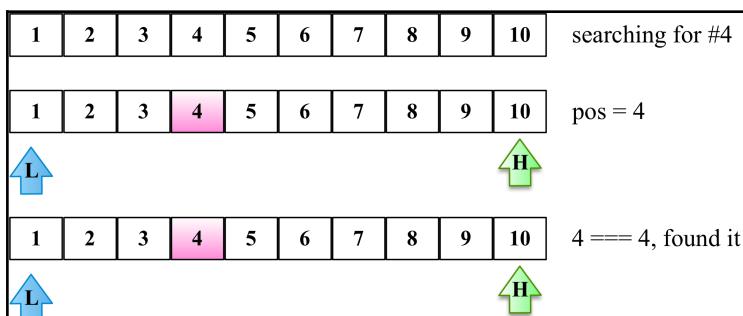
```

function lesserEquals(a, b, compareFn) {
    const comp = compareFn(a, b);
    return comp === Compare.LESS_THAN || comp === Compare.EQUALS;
}

function biggerEquals(a, b, compareFn) {
    const comp = compareFn(a, b);
    return comp === Compare.BIGGER_THAN || comp === Compare.EQUALS;
}

```

The following diagram demonstrates the algorithm in action—the array uniformly distributes (delta/difference between numbers is very low):



Shuffle algorithms

In this chapter, we learned how to sort an array to organize all its elements and also how to search elements after the array is sorted. But there are also scenarios where we need to shuffle the values of an array. A common scenario in real life is shuffling a deck of cards.

In the next section, we will learn about the most famous algorithm used to shuffle arrays.

The Fisher-Yates shuffle

This algorithm was created by **Fisher and Yates** and popularized by *Donald E. Knuth* in *The Art of Computer Programming* book series.

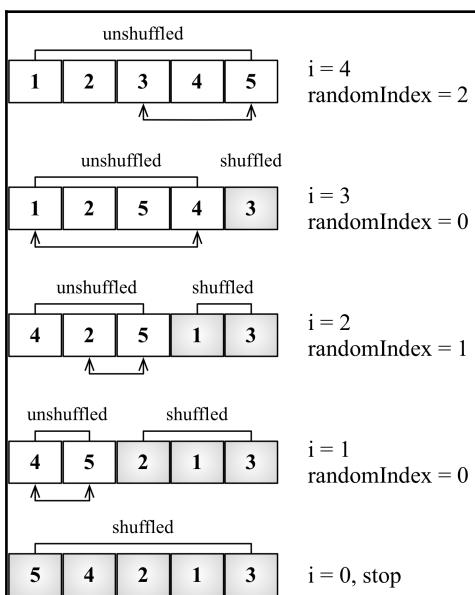
It consists of iterating each position of the array, starting with its last position and swapping the current position with a random position. The random position is lesser than the current position; this way, the algorithm makes sure the positions already shuffled will not be shuffled again (the more we shuffle a deck of cards, the worse is the shuffle).

The following code presents the Fisher-Yates shuffle algorithm:

```
function shuffle(array) {
  for (let i = array.length - 1; i > 0; i--) {
    const randomIndex = Math.floor(Math.random() * (i + 1));
    swap(array, i, randomIndex);
  }

  return array;
}
```

In the following diagram, we can see the algorithm in action:



Summary

In this chapter, we learned about sorting, searching, and shuffling algorithms.

We learned about the bubble, selection, insertion, merge, quick, counting, bucket, and radix sort algorithms, which are used to sort data structures. We also learned about the sequential search, interpolation search, and binary search (which require the data structure to be sorted already). We also covered how to shuffle values of an array.

In the next chapter, we will learn about some advanced techniques used in algorithms.

14

Algorithm Designs and Techniques

So far, we have had fun discussing how to implement several different data structures and the most commonly used sorting and searching algorithms. An algorithm in the programming world is very interesting. The most beautiful thing about algorithms (and programming logic) is that there is more than one approach to resolving a problem. As we learned in previous chapters, we can design a solution using the iterative approach or make the code easier to read using recursion. There are also other techniques we can use to solve problems with algorithms. In this chapter, we will learn about different techniques, and we will also discuss the next steps in case you are interested in diving deeper into this world.

In this chapter, we will cover:

- Divide and conquer algorithms
- Dynamic programming
- Greedy algorithms
- Backtracking algorithms
- Famous algorithm problems

Divide and conquer

In Chapter 13, *Sorting and Searching Algorithms*, we learned how to develop the merge and quick sort algorithms. What both sorting solutions have in common is that they are divide and conquer algorithms. Divide and conquer is one of the approaches to algorithm design. It breaks the problem into small subproblems that are similar to the original problem, it solves the subproblems recursively, and combines the solutions of the subproblems to solve the original problem.

The divide and conquer algorithm can be split into three parts:

1. **Divide** the original problem into smaller subproblems (smaller instances of the original problem).
2. **Conquer** the smaller subproblems by solving them with recursive algorithms that return the solution for the subproblems. The base case of the recursive algorithm solves and returns the solution for the smallest subproblem.
3. **Combine** the solutions of the subproblems into the solution for the original problem.

As we have already covered the two most famous divide and conquer algorithms in Chapter 13, *Sorting and Searching Algorithms*, we will learn how to implement the **binary search** using the divide and conquer approach.

Binary search

In Chapter 13, *Sorting and Searching Algorithms*, we learned how to implement the binary search using an iterative approach. If we go back and take a look at the algorithm, we can use the divide and conquer approach to implement the binary search as well. The logic is the following:

- **Divide**: Calculate `mid` and search lower or upper half of the array
- **Conquer**: Search value in the lower or upper half of the array
- **Combine**: Not applicable as we are returning the index directly

The divide and conquer binary search algorithm is the following:

```
function binarySearchRecursive(
  array, value, low, high, compareFn = defaultCompare
) {
  if (low <= high) {
    const mid = Math.floor((low + high) / 2);
    const element = array[mid];

    if (compareFn(element, value) === Compare.LESS_THAN) { // {1}
      return binarySearchRecursive(array, value, mid + 1, high, compareFn);
    } else if (compareFn(element, value) === Compare.BIGGER_THAN) { // {2}
      return binarySearchRecursive(array, value, low, mid - 1, compareFn);
    } else {
      return mid; // {3}
    }
  }
  return DOES_NOT_EXIST; // {4}
}
```

```

}

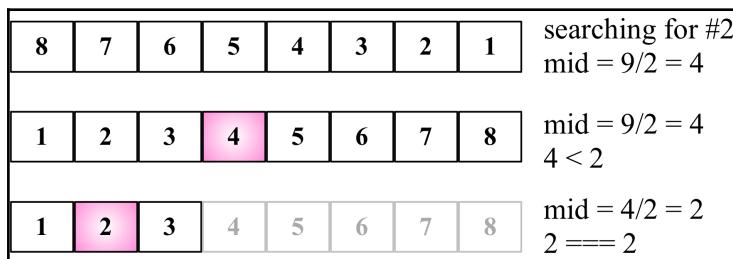
export function binarySearch(array, value, compareFn = defaultCompare) {
  const sortedArray = quickSort(array);
  const low = 0;
  const high = sortedArray.length - 1;

  return binarySearchRecursive(array, value, low, high, compareFn);
}

```

In the preceding algorithm, we have two functions: `binarySearch` and `binarySearchRecursive`. The `binarySearch` function is the one exposed to the developer to perform the search. The `binarySearchRecursive` is the divide and conquer algorithm. We start passing the `low` parameter as 0 and the `high` parameter as `sortedArray.length - 1` to perform the search in the complete sorted array. After calculating what is the index of the `mid` element, we ascertain whether the value we are looking for is smaller or bigger than `mid`. If it is lesser ({1}) or bigger ({2}), we evoke the `binarySearchRecursive` function again, but this time, we only perform the search in the subarray, adapting the `low` or `high` parameters (instead of moving the pointer as in the classic algorithm we learned about in Chapter 13, *Sorting and Searching Algorithms*). If not lesser or bigger, it means we have found the value ({3}) and this is one of the base cases. In a situation where `low` is bigger than `high`, this is also another base case, and it means the algorithm did not find the value ({4}).

The following diagram exemplifies the algorithm in action:



Dynamic programming

Dynamic programming (DP) is an optimization technique used to solve complex problems by breaking them into smaller subproblems.



Note that the dynamic programming approach is different from the divide and conquer approach. While the divide and conquer approach breaks the problem into independent subproblems and then combines the solutions, dynamic programming breaks the problem into dependent subproblems.

An example of a dynamic programming algorithm is the Fibonacci problem we solved in Chapter 9, *Recursion*. We broke the Fibonacci problem into smaller problems.

There are three important steps we need to follow when solving problems with DP:

1. Define the subproblems.
2. Implement the recurrence that solves the subproblems (in this step, we need to follow the steps for recursion that we discussed in the previous section).
3. Recognize and solve the base cases.

There are some famous problems that can be solved with dynamic programming:

- **The knapsack problem:** In this problem, given a set of items, each one with a value and volume, the goal is to determine the best collection of items out of the set in a way to maximize the total value. The constraint of the problem is that the total volume needs to be the volume supported by the *knapsack* or less.
- **The longest common subsequence:** This consists of finding the longest subsequence (a sequence that can be derived from another sequence by deleting some elements without changing the order of the remaining elements) common to all sequences in a set of sequences.
- **Matrix chain multiplication:** In this problem, given a sequence of matrices, the goal is to find the most efficient way to multiply these matrices (with as few operations as possible). The multiplication is not performed; the solution is finding the sequences in each of the matrices that need to be multiplied.
- **Coin change:** This consists of finding how many different ways we can make change in a particular amount of cents using a given amount of set denominations ($d_1 \dots d_n$).
- **All-pairs shortest paths in a graph:** This consists of finding the shortest path from vertex u to vertex v for all pairs of vertices (u, v) . You learned about this problem in Chapter 12, *Graphs*, using the **Floyd-Warshall** algorithm.

We will cover these problems in the following sections.



These problems and their solutions are very common in programming the interviews of big companies such as Google, Amazon, Microsoft, and Oracle.

The minimum coin change problem

The **minimum coin change problem** is a variation of the **coin change problem**. The coin change problem consists of finding out in how many ways we can make change for a particular amount of cents using a given amount of set denominations ($d_1 \dots d_n$). The minimum coin change problem consists of finding the minimum number of coins needed to make a particular amount of cents using a given amount of set denominations ($d_1 \dots d_n$).

For example, the United States has the following denominations (coins): $d_1 = 1$; $d_2 = 5$; $d_3 = 10$; and $d_4 = 25$.

If we need to make change for 36 cents, we can use 1 quarter (25), 1 dime (10), and 1 penny (1).

How do we transform this solution into an algorithm?

The min-coin change solution consists of finding the minimum number of coins for n . But to do this, first we need to find the solution for every $x < n$. Then, we can build up the solution out of the solutions for smaller values.

Let's take a look at the algorithm:

```
function minCoinChange(coins, amount) {  
    const cache = [];  
    const makeChange = (value) => { // {2}  
        if (!value) { // {3}  
            return [];  
        }  
        if (cache[value]) { // {4}  
            return cache[value];  
        }  
        let min = [];  
        let newMin;  
        let newAmount;  
        for (let i = 0; i < coins.length; i++) { // {5}  
            const coin = coins[i];  
            newAmount = value - coin; // {6}
```

```

        if (newAmount >= 0) {
            newMin = makeChange(newAmount); // {7}
        }
        if (
            newAmount >= 0 && // {8}
            (newMin.length < min.length - 1 || !min.length) && // {9}
            (newMin.length || !newAmount) // {10}
        ) {
            min = [coin].concat(newMin); // {11}
            console.log('new Min ' + min + ' for ' + amount);
        }
    }
    return (cache[value] = min); // {12}
};

return makeChange(amount); // {13}
}

```

The `minCoinChange` function receives the `coins` parameter, which represents the denominations of our problem. For the US coin system, it would be `[1, 5, 10, 25]`. We can pass any denominations that we like. Also, to be more efficient and not recalculate values, we will keep a `cache` ({1})—this technique is called **memoization**).

Then, we have the `makeChange` function inside the `minCoinChange` function ({2}), which is also recursive and is the function that will solve the problem for us. The `makeChange` function is being evoked at line {13} with the `amount` passed as a parameter to the `minCoinChange` function. And because `makeChange` is an inner function, it also has access to the `cache` variable.

Now let's get to the main logic of the algorithm. First, if `amount` is not positive (`< 0`), then we will return an empty array ({3}); at the end of the execution of this method, we will return an array with the amount of each coin that can be used to make change (the minimum amount of coins). Next, we will check `cache`. If the result is already cached ({4}), then we will simply return its `value`; otherwise, we execute the algorithm.

To help us further, we will solve the problem based on the `coins` parameter (denominations). So, for each `coin` ({5}), we will calculate `newAmount` ({6}), which will decrease the `value` until we reach the minimum amount of change we can give (remember that this algorithm will calculate all `makeChange` results for `x < amount`). If `newAmount` is a valid value (positive value), then we will calculate the result for it as well ({7}).

At the end, we will verify whether `newAmount` is valid, whether `minValue` (the minimum amount of coins) is the best result, and whether `minValue` and `newAmount` are valid values ({}10{}). If all the verifications are positive, it means we have a better result than previously ({}11{})—for example, for 5 cents, we can give 5 pennies or 1 nickel, 1 nickel being the best solution). At the end, we will return the final result ({}12{}).

Let's test this algorithm using the following code:

```
console.log(minCoinChange([1, 5, 10, 25], 36));
```

Note that if we inspect the `cache` variable, it will hold all the results for 1 to 36 cents. The result for the preceding code will be [1, 10, 25].

In the source code of this book, you will find some extra lines of code that will output the steps of this algorithm. For example, if we use the denominations 1, 3, and 4, and execute the algorithm for the amount 6, we will produce the following output:

```
new Min 1 for 1
new Min 1,1 for 2
new Min 1,1,1 for 3
new Min 3 for 3
new Min 1,3 for 4
new Min 4 for 4
new Min 1,4 for 5
new Min 1,1,4 for 6
new Min 3,3 for 6
[3, 3]
```

So, for the amount 6, the best solution is giving two coins of value 3.

The knapsack problem

The knapsack problem is a combinatorial optimization problem. It can be described as follows: given a fixed-size knapsack with a capacity to carry W amount of weight and a set of items that have a value and weight, find the best solution in a way to fill the knapsack with the most valuable items so that the total weight is less than or equal to W .

Here, we have an example:

Item #	Weight	Value
1	2	3
2	3	4
3	4	5

Consider that the knapsack can only carry a weight of 5. For this example, we can say that the best solution would be filling the knapsack with items 1 and 2, which together have a weight of 5 and a total value of 7.



There are two versions of this problem: the **0-1** version, in which we can only fill the knapsack with the whole item, and the **fractional knapsack problem**, in which we can take fractions of the items. For this example, we will work with the 0-1 version of the problem. The fractional version cannot be solved with dynamic programming, but it can be solved with a greedy algorithm, which you will learn about later on in this chapter.

Let's take a look at the knapsack algorithm, as follows:

```
function knapSack(capacity, weights, values, n) {
    const kS = [];
    for (let i = 0; i <= n; i++) { // {1}
        kS[i] = [];
    }

    for (let i = 0; i <= n; i++) {
        for (let w = 0; w <= capacity; w++) {
            if (i === 0 || w === 0) { // {2}
                kS[i][w] = 0;
            } else if (weights[i - 1] <= w) { // {3}
                const a = values[i - 1] + kS[i - 1][w - weights[i - 1]];
                const b = kS[i - 1][w];
                kS[i][w] = a > b ? a : b; // {4} max(a,b)
            } else {
                kS[i][w] = kS[i - 1][w]; // {5}
            }
        }
    }

    findValues(n, capacity, kS, weights, values); // {6} additional code
    return kS[n][capacity]; // {7}
}
```

Let's take a look at how this algorithm works.

First, we will initialize the matrix that will be used to find the solution (`{1}`). This matrix is `ks[n+1][capacity+1]`. Next, we will ignore the first column and row of the matrix so that we can work only with indexes different from `0` (`{2}`) and we will iterate each item available in the array. Item `i` can only be part of the solution if its weight is less than the constraint (`capacity - {3}`); otherwise, the total weight will be bigger than the `capacity`, and this cannot happen. When this happens, we will simply ignore its value and use the previous one (`{5}`). When we find that an item can be part of a solution, we will choose the one with the maximum value (`{4}`). The solution can be found in the last cell of the two-dimensional table, which is found in the lower right-hand corner of the table (`{7}`).

We can test the following algorithm using our initial example:

```
const values = [3, 4, 5],
weights = [2, 3, 4],
capacity = 5,
n = values.length;
console.log(knapSack(capacity, weights, values, n)); //outputs 7
```

The following diagram exemplifies the construction of the `ks` matrix for our example:

1	i/w	0	1	2	3	4	5	
0	0	0	0	0	0	0	0	Items: 1: (2,3) 2: (3,4) 3: (4,5)
1	0							
2	0							
3	0							

2	i/w	0	1	2	3	4	5	
0	0	0	0	0	0	0	0	Items: 1: (2,3) 2: (3,4) 3: (4,5)
1	0	0	3	3	3	3	3	
2	0	0	3	4	4	4	7	
3	0							

3	i/w	0	1	2	3	4	5	
0	0	0	0	0	0	0	0	Items: 1: (2,3) 2: (3,4) 3: (4,5)
1	0	0	3	3	3	3	3	
2	0	0	3	4	4	4	7	
3	0							

4	i/w	0	1	2	3	4	5	
0	0	0	0	0	0	0	0	Items: 1: (2,3) 2: (3,4) 3: (4,5)
1	0	0	3	3	3	3	3	
2	0	0	3	4	4	4	7	
3	0	0	3	4	5	5	7	

Note that this algorithm only outputs the maximum value that can be carried by the knapsack but not the actual items. We can add the following additional function to find the items that are part of the solution:

```
function findValues(n, capacity, kS, weights, values) {
    let i = n;
    let k = capacity;
    console.log('Items that are part of the solution:');
    while (i > 0 && k > 0) {
        if (kS[i][k] !== kS[i - 1][k]) {
            console.log(`item ${i} can be part of solution w,v: ${weights[i - 1]} ${values[i - 1]}`);
            i--;
            k -= kS[i][k];
        } else {
            i--;
        }
    }
}
```

We can call this function right before line {7} of the `knapSack` function (declared at line {6}). If we execute the complete algorithm, we will have the following output:

```
Items that are part of the solution:
item 2 can be part of solution w,v: 3,4
item 1 can be part of solution w,v: 2,3
Total value that can be carried: 7
```



The knapsack problem can also be written recursively. You can find the recursive version within the source code bundle of this book.

The longest common subsequence

Another DP problem that is very often used in programming challenge problems is the **longest common subsequence (LCS)**. This problem consists of finding the length of the longest subsequence in two string sequences. The longest subsequence is a sequence that appears in the same relative order but is not necessarily contiguous (not a substring) in both strings.

Consider the following example:

string 1	a	c	b	a	e	d
string 2	a	b	c	a	d	f
LCS: "acad" with length 4						

Now, let's take a look at the following algorithm:

```
function lcs(wordX, wordY) {
    const m = wordX.length;
    const n = wordY.length;
    const l = [];

    for (let i = 0; i <= m; i++) {
        l[i] = []; // {1}
        for (let j = 0; j <= n; j++) {
            l[i][j] = 0; // {2}
        }
    }

    for (let i = 0; i <= m; i++) {
        for (let j = 0; j <= n; j++) {
            if (i === 0 || j === 0) {
                l[i][j] = 0;
            } else if (wordX[i - 1] === wordY[j - 1]) {
                l[i][j] = l[i - 1][j - 1] + 1; // {3}
            } else {
                const a = l[i - 1][j];
                const b = l[i][j - 1];
                l[i][j] = a > b ? a : b; // {4} max(a,b)
            }
        }
    }
    return l[m][n]; // {5}
}
```

If we compare the knapsack problem with the LCS algorithm, we will notice that both are very similar. This technique is called memoization, which consists of building the solution in a top-down manner, and the solution is given in the lower right-hand corner of the table/matrix.

As with the knapsack problem algorithm, this approach only outputs the length of the LCS, but not the actual LCS. To be able to extract this information, we need to modify our algorithm a little bit by declaring a new matrix called `solution`. Note that in our code, there are some comments, and we need to replace the comments with the following code:

- Line {1}: `solution[i] = [];`
- Line {2}: `solution[i][j] = '0';`
- Line {3}: `solution[i][j] = 'diagonal';`
- Line {4}: `solution[i][j]=(l[i][j] == l[i-1][j]) ? 'top' : 'left';`
- Line {5}: `printSolution(solution, wordX, m, n);`

The `printSolution` function is given as follows:

```
function printSolution(solution, wordX, m, n) {
    let a = m;
    let b = n;
    let x = solution[a][b];
    let answer = '';
    while (x !== '0') {
        if (solution[a][b] === 'diagonal') {
            answer = wordX[a - 1] + answer;
            a--;
            b--;
        } else if (solution[a][b] === 'left') {
            b--;
        } else if (solution[a][b] === 'top') {
            a--;
        }
        x = solution[a][b];
    }
    console.log('lcs: ' + answer);
}
```

We can add the `char` to the `answer` whenever the direction of the `solution` matrix is diagonal.

If we execute the preceding algorithm using the 'acbaed' and 'abcadf' strings, we will get the output 4. The matrix `l` that was used to build the result will look similar to the following. We can use the additional algorithm to backtrack the LCS value, as well (this is highlighted in the following diagram):

	a	b	c	a	d	f
a	0	0	0	0	0	0
c	0	1	1	2	2	2
b	0	1	2	2	2	2
a	0	1	2	2	3	3
e	0	1	2	2	3	3
d	0	1	2	2	3	4

From the preceding matrix, we know that the LCS algorithm is **acad** with a length of **4**.



The LCS problem can also be written recursively. You can find the recursive version within the source code bundle of this book.

Matrix chain multiplication

Matrix chain multiplication is another famous problem that can be solved with dynamic programming. The problem consists of finding the best way (order) of multiplying a set of matrices.

Let's try to understand the problem a little better. To multiply two matrices, *A* being a matrix *m* by *n*, and *B* a matrix *m* by *p*. The result is matrix *C*, *n* by *p*.

Now, consider that we want to multiply *A*B*C*D*. As multiplication is associative, we can multiply these matrices in any order. So, let's consider the following:

- *A* is a 10 by 100 matrix
- *B* is a 100 by 5 matrix
- *C* is a 5 by 50 matrix
- *D* is a 50 by 1 matrix
- The result is an *A*B*C*D* 10 by 1 matrix

Within this example, there are five ways of doing this multiplication:

- **(A(B(CD)))**: The total of the multiplications is 1,750
- **((AB)(CD))**: The total of the multiplications is 5,300
- **((AB)C)D**: The total of the multiplications is 8,000
- **((A(BC))D)**: The total of the multiplications is 75,500
- **(A((BC)D))**: The total of the multiplications is 31,000

The order of the multiplication can make a difference to the total number of multiplications performed. So, how can we create an algorithm to find the minimum number of operations? The matrix chain multiplication algorithm is given as follows:

```
function matrixChainOrder(p) {
    const n = p.length;
    const m = [];
    const s = [];
    for (let i = 1; i <= n; i++) {
        m[i] = [];
        m[i][i] = 0;
    }

    for (let l = 2; l < n; l++) {
        for (let i = 1; i <= (n - l) + 1; i++) {
            const j = (i + l) - 1;
            m[i][j] = Number.MAX_SAFE_INTEGER;
            for (let k = i; k <= j - 1; k++) {
                const q = m[i][k] + m[k + 1][j] + ((p[i - 1] * p[k]) * p[j]); // {1}
                if (q < m[i][j]) {
                    m[i][j] = q; // {2}
                }
            }
        }
    }
    return m[1][n - 1]; // {3}
}
```

The most important line of this code is line {1} because this is the one doing all the magic, meaning it calculates the number of multiplications of a given parenthesis order and stores the value in the auxiliary matrix m.

If we execute the preceding algorithm to our initial example, we will have the output 1750, this being the minimum number of operations as we mentioned before. Take a look at this:

```
const p = [10, 100, 5, 50, 1];
console.log(matrixChainOrder(p));
```

However, this algorithm does not provide us with the order of the parenthesis of the optimal solution either. We can make some changes to our code to be able to get this information.

First, we need to declare and initialize an auxiliary matrix `s` via the following code:

```
const s = [];
for (let i = 0; i <= n; i++) {
  s[i] = [];
  for (let j=0; j <= n; j++) {
    s[i][j] = 0;
  }
}
```

Then, in line {2} of the `matrixChainOrder` function, we will add the following code:

```
s[i][j] = k;
```

In line {3}, we will call the function that will print the parenthesis for us, as follows:

```
printOptimalParenthesis(s, 1, n-1);
```

Finally, we will have the `printOptimalParenthesis` function, which would be as follows:

```
function printOptimalParenthesis(s, i, j) {
  if(i === j) {
    console.log("A[" + i + "]");
  } else {
    console.log("(");
    printOptimalParenthesis(s, i, s[i][j]);
    printOptimalParenthesis(s, s[i][j] + 1, j);
    console.log(")");
  }
}
```

If we execute the modified algorithm, we will also get the optimal order of the parenthesis, $(A[1] (A[2] (A[3] A[4])))$, which can be translated to $(A (B (C D)))$.

Greedy algorithms

A **greedy algorithm** follows the problem-solving heuristic of making the locally optimal choice (the best solution at the time) at each stage with the hope of finding a global optimum (global best solution). It does not evaluate the bigger picture like a dynamic programming algorithm does.

Let's take a look at how we can solve the min-coin change and knapsack problems we covered in the dynamic programming topic using the greedy approach.



We covered some other greedy algorithms in this book in Chapter 12, *Graphs*, such as **Dijkstra's algorithm**, **Prim's algorithm**, and **Kruskal's algorithm**.

The min-coin change problem

The min-coin change problem can also be resolved with a greedy algorithm. Most of the time, the result is also optimal, but for some denominations, the result will not be optimal.

Let's take a look at the algorithm:

```
function minCoinChange(coins, amount) {  
    const change = [];  
    let total = 0;  
    for (let i = coins.length; i >= 0; i--) { // {1}  
        const coin = coins[i];  
        while (total + coin <= amount) { // {2}  
            change.push(coin); // {3}  
            total += coin; // {4}  
        }  
    }  
    return change;  
}
```

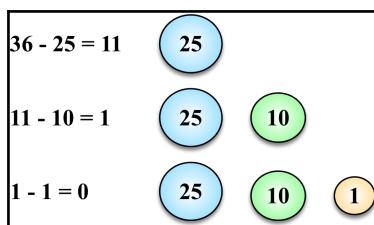
Note that the greedy version of `minCoinChange` is much simpler than the DP one. For each coin ({1}), starting from the biggest one to the smallest one), we will add the `coin` value to `total`, and `total` needs to be less than `amount` ({2}). We will add `coin` to the result ({3}) and also to `total` ({4}).

The solution is simple and greedy. We will start with the coin with the greatest value and give the change that is possible with this coin. When we cannot give more coins for the current coin value, we will start giving change with the coin that has the second greatest value and so on.

To test the code, we will use the same code we used in the DP approach, as follows:

```
console.log(minCoinChange([1, 5, 10, 25], 36));
```

The result will also be [25, 10, 1], the same result that we got using DP. The following diagram exemplifies how the algorithm is executed:



However, if we use the [1, 3, 4] denomination and execute the preceding greedy algorithm, we will get [4, 1, 1] as the result. If we use the dynamic programming solution, we will get [3, 3] as the result, which is the optimal result.

Greedy algorithms are simpler and also faster than dynamic programming algorithms. However, as we can note, it does not give the optimal answer all the time. However, on average, it would output an acceptable solution for the time it takes to execute.

The fractional knapsack problem

The algorithm to solve the fractional knapsack problem is a little different from the dynamic programming version. While, in the 0-1 knapsack problem, we can only use the whole item to fill the knapsack, in the fractional knapsack problem, we can use fractions of the items. Let's use the same example we used before to compare the differences, as follows:

Item #	Weight	Value
1	2	3
2	3	4
3	4	5

In the dynamic programming example, we considered that the knapsack could only carry a weight of 5. For this example, we can say that the best solution would be filling the knapsack with items 1 and 2, which together have a weight of 5 and a total value of 7.

If we consider the same capacity for the fractional knapsack problem, we will have the same output. So, let's consider the capacity as 6 instead of 5.

In this case, the solution would be to use items 1 and 2 and only 25% of item 3. This would give a maximum value of 8.25 with a total weight of 6.

Let's take a look at the following algorithm:

```
function knapSack(capacity, weights, values) {  
    const n = values.length;  
    let load = 0;  
    let val = 0;  
    for (let i = 0; i < n && load < capacity; i++) { // {1}  
        if (weights[i] <= capacity - load) { // {2}  
            val += values[i];  
            load += weights[i];  
        } else {  
            const r = (capacity - load) / weights[i]; // {3}  
            val += r * values[i];  
            load += weights[i];  
        }  
    }  
    return val;  
}
```

While the total `load` is less than the `capacity` (we cannot carry more than the `capacity`), we will iterate the items ({1}). If we can use the total weight of the item ({2})—it is less than or equal to the `capacity`)—then we will add it to the total value (`val`) and update the current `load` of the knapsack. If we cannot use the total weight of the item, we will calculate what is the ratio (`r`) that we can use ({3})—the fraction that we can carry).

If we apply capacity 6 to the 0-1 knapsack problem, we will see that items 1 and 3 will be selected as part of the solution. In this case, we have two different outputs for the same problem, but are using different approaches to solve the problem.

Backtracking algorithms

Backtracking is a strategy used to find and build a solution incrementally. We start with a possible move and we try to solve the problem with the selected move. If it does not work, we backtrack and then we select another move and so on until we have the problem solved. Due to this behavior, backtracking algorithms will try all possible moves (or a few moves if a solution is found sooner) to solve a problem.

There are some famous problems that can be solved with backtracking:

- The Knight's tour problem
- N Queen problem
- Rat in a maze
- Sudoku Solver



In this book, we will learn the **Rat in a Maze** and **Sudoku Solver** problems as they are easier to understand. However, you can find the source code for other backtracking problems along with the source code bundle of this book.

Rat in a Maze

Suppose we have a matrix with size $N \times N$, and each position of the matrix is a block. The position (or block) can be free (value 1) or it can be blocked (value 0), as shown in the following diagram, where **S** is source and **D** is destination:

S					1	0	0	0	1	0	0	0
					1	1	1	1	1	1	1	1
					0	0	1	0	0	0	1	0
				D	0	1	1	1	0	1	1	1

The matrix is the maze and the goal is for the "rat" to start at position [0][0] and go to position [n-1][n-1] (destination). The rat can move in two directions: vertically or horizontally in any position that is not blocked.

Let's start declaring the basic structure of our algorithm, as follows:

```
export function ratInAMaze(maze) {
    const solution = [];
```

```

for (let i = 0; i < maze.length; i++) { // {1}
    solution[i] = [];
    for (let j = 0; j < maze[i].length; j++) {
        solution[i][j] = 0;
    }
}
if (findPath(maze, 0, 0, solution) === true) { // {2}
    return solution;
}
return 'NO PATH FOUND'; // {3}
}

```

We will first start creating the matrix that contains the solution. We will initialize every position with zero ({1}). For every move the rat makes, we will mark the path with value 1. If the algorithm is able to find a solution ({2}), it will return the `solution` matrix, or an error message, otherwise ({3}).

Next, we have the `findPath` method that will try to find the solution for a given `maze` matrix, starting at positions `x` and `y`. As with the other techniques presented in this chapter, the backtracking technique also uses recursion, and that is what allows the algorithm to backtrack, as shown here:

```

function findPath(maze, x, y, solution) {
    const n = maze.length;

    if (x === n - 1 && y === n - 1) { // {4}
        solution[x][y] = 1;
        return true;
    }

    if (isSafe(maze, x, y) === true) { // {5}
        solution[x][y] = 1; // {6}
        if (findPath(maze, x + 1, y, solution)) { // {7}
            return true;
        }

        if (findPath(maze, x, y + 1, solution)) { // {8}
            return true;
        }
    }

    solution[x][y] = 0; // {9}
    return false;
}
return false; // {10}
}

```

The first step of the algorithm is to verify whether the rat reached its destination ({4}). If so, we mark the last position as part of the path and return `true`, meaning the move was done successfully. If it is not the last position, we will verify whether it is safe for the rat to move into position ({5} meaning the position is free, as declared in the `isSafe` method declared next). If it is safe, then we add the move into the path ({6}) and we try to move in the `maze` matrix horizontally (to the right) to the next position ({7}). If moving horizontally is not possible, then we try to move vertically to the next position, moving towards the bottom of the matrix ({8}). If it is not possible to move horizontally or vertically, then we remove the move from the path and we backtrack ({9}), meaning the algorithm will try another possible solution. After the algorithm tries all possible moves and it does not find a solution, then it will return `false` ({10}), meaning there is no solution to the puzzle.

```
function isSafe(maze, x, y) {  
    const n = maze.length;  
    if (x >= 0 && y >= 0 && x < n && y < n && maze[x][y] !== 0) {  
        return true; // {11}  
    }  
    return false;  
}
```

We can test this algorithm by using the following code:

```
const maze = [  
    [1, 0, 0, 0],  
    [1, 1, 1, 1],  
    [0, 0, 1, 0],  
    [0, 1, 1, 1]  
];  
console.log(ratInAMaze(maze));
```

And the output will be:

```
[[1, 0, 0, 0],  
 [1, 1, 1, 0],  
 [0, 0, 1, 0],  
 [0, 0, 1, 1]]
```

Sudoku Solver

Sudoku is a very fun puzzle game and one of the most popular games of all time. The objective is to fill a 9x9 matrix with the digits 1 to 9 in order that each row and each column is composed with all the nine digits. The matrix also contains smaller boxes (3x3 matrix) that also need to contain all the nine digits. The puzzle provides an initial matrix partially filled, as displayed in the following diagram:

5	3			7				
6			1	9	5			
	9	8					6	
8				6				3
4			8		3			1
7				2				6
	6					2	8	
			4	1	9			5
				8			7	9

The backtracking algorithm for Sudoku Solver will try to place each number in each row and each column in order to solve the puzzle. As with the Rat in a Maze problem, we will start with the main method of the algorithm:

```
function sudokuSolver(matrix) {  
    if (solveSudoku(matrix) === true) {  
        return matrix;  
    }  
    return 'NO SOLUTION EXISTS!';  
}
```

The algorithm will return the matrix filled with the missing digits if a solution is found or it will return an error message. Now, let's dive into the main logic of the algorithm:

```
const UNASSIGNED = 0;

function solveSudoku(matrix) {
    let row = 0;
    let col = 0;
    let checkBlankSpaces = false;
    for (row = 0; row < matrix.length; row++) { // {1}
        for (col = 0; col < matrix[row].length; col++) {
            if (matrix[row][col] === UNASSIGNED) {
                checkBlankSpaces = true; // {2}
                break;
            }
        }
        if (checkBlankSpaces === true) { // {3}
            break;
        }
    }
    if (checkBlankSpaces === false) {
        return true; // {4}
    }
    for (let num = 1; num <= 9; num++) { // {5}
        if (isSafe(matrix, row, col, num)) { // {6}
            matrix[row][col] = num; // {7}
            if (solveSudoku(matrix)) { // {8}
                return true;
            }
            matrix[row][col] = UNASSIGNED; // {9}
        }
    }
    return false; // {10}
}
```

The first step is verifying whether the puzzle has been resolved ({1}). If there are no blank spaces (positions with value 0), it means the puzzle is complete ({4}). But if there are blank spaces ({2}), we will break out of the two loops ({3}) and the `row` and `col` variables will have the position of the blank space that needs to be filled with a 1-9 digit. Next, the algorithm will try to fill out the blank spaces with the 1-9 digits, one at a time ({5}). We will check whether it is safe to add the digit ({6}), meaning the digit is not present in the row, column, or in the box (matrix 3x3). If it is safe, then we add the digit to the puzzle ({7}) and we run the `solveSudoku` function again to try the next available space ({8}). In case a digit is placed in an incorrect position, we mark the position as blank again ({9}) and the algorithm will backtrack ({10}) and try a different digit.

The `isSafe` function is declared with the verifications required to input a digit into the matrix as follows:

```
function isSafe(matrix, row, col, num) {
    return (
        !usedInRow(matrix, row, num) &&
        !usedInCol(matrix, col, num) &&
        !usedInBox(matrix, row - (row % 3), col - (col % 3), num)
    );
}
```

And the specific verifications are declared as follows:

```
function usedInRow(matrix, row, num) {
    for (let col = 0; col < matrix.length; col++) { // {11}
        if (matrix[row][col] === num) {
            return true;
        }
    }
    return false;
}

function usedInCol(matrix, col, num) {
    for (let row = 0; row < matrix.length; row++) { // {12}
        if (matrix[row][col] === num) {
            return true;
        }
    }
    return false;
}

function usedInBox(matrix, boxStartRow, boxStartCol, num) {
    for (let row = 0; row < 3; row++) {
        for (let col = 0; col < 3; col++) {
            if (matrix[row + boxStartRow][col + boxStartCol] === num) { // {13}
                return true;
            }
        }
    }
    return false;
}
```

First, we will verify whether the digit already exists in the `row` by iterating every position of the matrix in the given `row` ({11}). Next, we will iterate all columns to verify whether the digit exists in the given column ({12}). And the final verification is to check whether the digit exists in the box ({13}), by iterating all positions of the 3x3 box matrix.

We can test the algorithm using the following example:

```
const sudokuGrid = [
  [5, 3, 0, 0, 7, 0, 0, 0, 0],
  [6, 0, 0, 1, 9, 5, 0, 0, 0],
  [0, 9, 8, 0, 0, 0, 0, 6, 0],
  [8, 0, 0, 0, 6, 0, 0, 0, 3],
  [4, 0, 0, 8, 0, 3, 0, 0, 1],
  [7, 0, 0, 0, 2, 0, 0, 0, 6],
  [0, 6, 0, 0, 0, 0, 2, 8, 0],
  [0, 0, 0, 4, 1, 9, 0, 0, 5],
  [0, 0, 0, 0, 8, 0, 0, 7, 9]
];
console.log(sudokuSolver(sudokuGrid));
```

And the output will be:

```
[ [5, 3, 4, 6, 7, 8, 9, 1, 2],
  [6, 7, 2, 1, 9, 5, 3, 4, 8],
  [1, 9, 8, 3, 4, 2, 5, 6, 7],
  [8, 5, 9, 7, 6, 1, 4, 2, 3],
  [4, 2, 6, 8, 5, 3, 7, 9, 1],
  [7, 1, 3, 9, 2, 4, 8, 5, 6],
  [9, 6, 1, 5, 3, 7, 2, 8, 4],
  [2, 8, 7, 4, 1, 9, 6, 3, 5],
  [3, 4, 5, 2, 8, 6, 1, 7, 9]]
```

Introduction to functional programming

So far in this book, we have used a paradigm called **imperative programming**. In imperative programming, we code each step of the program, describing in detail what needs to be done and in which order it needs to be done.

In this section, we will introduce a new paradigm called **functional programming (FP)**. We have already used some FP code snippets in some algorithms in this book. Functional programming is a paradigm used especially by academics, and thanks to modern languages such as Python and Ruby, it has started to become popular among industry developers as well. And thankfully, we can use JavaScript to program functionally, leveraging its ES2015 capabilities as well.

Functional versus imperative programming

Developing in the **functional paradigm** is not difficult; it is just a matter of getting used to how the paradigm works. Let's code an example to note the differences.

Consider that we need to print all the elements of an array. We can use imperative programming and declare the following function:

```
const printArray = function(array) {
    for (var i = 0; i < array.length; i++) {
        console.log(array[i]);
    }
};

printArray([1, 2, 3, 4, 5]);
```

In the preceding code, we iterated the `array` and logged each of the items.

Now, let's try converting the example to functional programming. In functional programming, the functions are the rock stars. We need to focus on what needs to be described, not how. Let's go back to the phrase, "we iterated the array and logged each of the items". So, the first thing we will focus on is iterating the data, and then we will take action on it, which is logging the items. The following function will be responsible for iterating the array:

```
const forEach = function(array, action) {
    for (var i = 0; i < array.length; i++) {
        action(array[i]);
    }
};
```

Then, we will create another function that will be responsible for logging the array elements to the console (we can consider it a **callback function**), as follows:

```
const logItem = function(item) {
    console.log(item);
};
```

Finally, we can use the functions we declared, as follows:

```
forEach([1, 2, 3, 4, 5], logItem);
```

Looking closely at the preceding code, we can describe that we will log each item of the array to the console. And we have our first functional programming example!

A few things to keep in mind:

- The main goal is to describe the data and the transformation we need to apply to the data.
- The order of the execution of the program has low importance, while the steps and their sequence are very important in imperative programming.
- Functions and data collections are the rock stars in functional programming.
- We can use and abuse functions and recursion in functional programming, while the loops, assignments, conditionals, and also functions are used in imperative programming.
- With functional programming we need to avoid side effects and mutable data, meaning we do not modify the data that is being passed to the function. If we need to return a solution based on the input, we can make a copy and return the modified copy of the data.

ES2015+ and functional programming

With the ES2015+ functionalities, developing functional programs in JavaScript is even easier. Let's consider an example.

Consider we want to find the minimum value of an array. In imperative programming, to perform this task, we simply need to iterate throughout the array and verify that the current minimum value is bigger than the value of the array; if so, we will assign the new minimum value, as follows:

```
var findMinArray = function(array) {
    var minValue = array[0];
    for (var i=1; i<array.length; i++) {
        if (minValue > array[i]){
            minValue = array[i];
        }
    }
    return minValue;
};
console.log(findMinArray([8, 6, 4, 5, 9])); // outputs 4
```

To perform the same task in functional programming, we can use the `Math.min` function, passing all the elements of the array to be compared. To transform the array into single elements, we can use the ES2015 spread operator (...), as in the following example:

```
const min_ = function(array) {
    return Math.min(...array)
};

console.log(min_([8, 6, 4, 5, 9])); //outputs 4
```

Using ES2015 **arrow functions**, we can simplify the preceding code a little bit more:

```
const min = arr => Math.min(...arr);
console.log(min([8, 6, 4, 5, 9]));
```

We can also rewrite the first example using the ES2015 syntax:

```
const forEach = (array, action) => array.forEach(item => action(item));
const logItem = (item) => console.log(item);
```

The JavaScript functional toolbox – map, filter, and reduce

The `map`, `filter`, and `reduce` functions (which you learned about in Chapter 3, *Arrays*) are the base of functional programming in JavaScript.

Using the `map` function, we can transform or map a collection of data into another collection of data. Let's take a look at an example using imperative programming:

```
const daysOfWeek = [
    {name: 'Monday', value: 1},
    {name: 'Tuesday', value: 2},
    {name: 'Wednesday', value: 7}
];

let daysOfWeekValues_ = [];
for (let i = 0; i < daysOfWeek.length; i++) {
    daysOfWeekValues_.push(daysOfWeek[i].value);
}
```

Now let's consider the same example using functional programming with ES2015+ syntax, as follows:

```
const daysOfWeekValues = daysOfWeek.map(day => day.value);
console.log(daysOfWeekValues);
```

Using the `filter` function, we can filter values out of a collection. Let's consider an example:

```
const positiveNumbers_ = function(array) {
    let positive = [];
    for (let i = 0; i < array.length; i++) {
        if (array[i] >= 0) {
            positive.push(array[i]);
        }
    }
    return positive;
}
console.log(positiveNumbers_([-1, 1, 2, -2]));
```

We can write the same code using the functional paradigm, as follows:

```
const positiveNumbers = (array) => array.filter(num => (num >= 0));
console.log(positiveNumbers([-1, 1, 2, -2]));
```

Also, using the `reduce` function, we can reduce a collection to a specific value. For example, let's take a look at how to sum the values of an array:

```
const sumValues = function(array) {
    let total = array[0];
    for (let i = 1; i < array.length; i++) {
        total += array[i];
    }
    return total;
};
console.log(sumValues([1, 2, 3, 4, 5]));
```

We can also write the preceding code as follows:

```
const sum_ = function(array) {
    return array.reduce(function(a, b) {
        return a + b;
    })
};
console.log(sum_([1, 2, 3, 4, 5]));
```

We can also mix these functions with the ES2015 functionalities, such as the destructuring assignment operator and arrow functions, as shown in the following code:

```
const sum = arr => arr.reduce((a, b) => a + b);
console.log(sum([1, 2, 3, 4, 5]));
```

Let's take a look at another example. Consider that we need to write a function to concatenate several arrays. To do so, we can create another array that will contain all the elements from the other arrays. We can execute the following code using the imperative paradigm:

```
const mergeArrays_ = function(arrays) {
    const count = arrays.length;
    let newArray = [];
    let k = 0;
    for (let i = 0; i < count; i++) {
        for (var j = 0; j < arrays[i].length; j++) {
            newArray[k++] = arrays[i][j];
        }
    }
    return newArray;
};
console.log(mergeArrays_([[1, 2, 3], [4, 5], [6]]));
```

Note that in this example, we are declaring variables and using loops. Now, let's execute the code written before using functional JavaScript programming, as follows:

```
const mergeArraysConcat = function(arrays) {
    return arrays.reduce(function(p, n) {
        return p.concat(n);
    });
};
console.log(mergeArraysConcat([[1, 2, 3], [4, 5], [6]]));
```

The preceding code does exactly the same task, but it is function-oriented. We can also simplify the code even more with ES2015, as shown in the following code:

```
const mergeArrays = (...arrays) => [...].concat(...arrays);
console.log(mergeArrays([1, 2, 3], [4, 5], [6]));
```

From 11 lines of code to only one (although readability is lower)!



If you want to practice JavaScript functional programming a little bit more, you can try the exercises (which are very fun to do!) at <http://reactivex.io/learnrx/>.

JavaScript functional libraries and data structures

There are some great JavaScript libraries that support the functional paradigm with utility functions and also functional data structures. In the following list, you can find some of the most famous functional JavaScript libraries:

- **Underscore.js**: <http://underscorejs.org/>
- **Bilby.js**: <http://bilby.brianmckenna.org/>
- **Lazy.js**: <http://danieltao.com/lazy.js/>
- **Bacon.js**: <https://baconjs.github.io/>
- **Fn.js**: <http://elipermel.com/fn.js/>
- **Functional.js**: <http://functionaljs.com/>
- **Rambda.js**: <http://ramdajs.com/0.20.1/index.html>
- **Mori**: <http://swannodette.github.io/mori/>



If you are interested in learning more about JavaScript functional programming, take a look at this book, also by Packt at <https://www.packtpub.com/web-development/functional-programming-javascript>.

Summary

In this chapter, we covered the most famous dynamic programming problems, such as a variation of the min-coin change problem, the knapsack problem, the longest common subsequence, and matrix chain multiplication. We learned about divide and conquer algorithms and how they are different from dynamic programming.

We learned about greedy algorithms and how to develop a greedy solution for the min-coin change problem and the fractional knapsack problem. We also covered the concept of backtracking and some famous problems, such as Rat in a Maze and Sudoku Solver.

We also learned about functional programming, and we covered some examples of how to use JavaScript functionalities in this paradigm.

In the next chapter, we will cover the *big-O* notation and discuss how we can calculate the complexity of an algorithm. We will also learn more concepts that exist in the algorithm world.

15

Algorithm Complexity

In this chapter, we will cover the famous **big O notation** and the **NP-completeness** theory, and also take a look at how we can have some fun with algorithms and boost our knowledge to improve our programming and problem-solving skills.

Big O notation

In Chapter 13, *Sorting and Searching Algorithms*, we introduced the concept of big O notation. What does it mean, exactly? It is used to describe the performance or complexity of an algorithm. Big O notation is used to classify algorithms according to how much time it will take for the algorithm to run, depending on space/memory requirements as the input size grows.

When analyzing algorithms, the following classes of function are most commonly encountered:

Notation	Name
$O(1)$	Constant
$O(\log(n))$	Logarithmic
$O((\log(n))c)$	Poly-logarithmic
$O(n)$	Linear
$O(n^2)$	Quadratic
$O(n^c)$	Polynomial
$O(c^n)$	Exponential

Understanding big O notation

How do we measure the efficiency of an algorithm? We usually use resources such as CPU (time) usage, memory usage, disk usage, and network usage. When talking about big O notation, we usually consider CPU (time) usage.

Let's try to understand how big O notation works using some examples.

O(1)

Consider the following function:

```
function increment(num) {  
    return ++num;  
}
```

If we try to execute the `increment(1)` function, we will have an execution time equal to x . If we try to execute the `increment` function again with a different parameter (let's say `num` is 2), the execution time will also be x . The parameter does not matter; the performance of the function `increment` will be the same. For this reason, we can say the preceding function has a complexity of $O(1)$ (which is constant).

O(n)

Now, let's use the sequential search algorithm we implemented in Chapter 13, *Sorting and Searching Algorithms*, as an example:

```
function sequentialSearch(array, value, equalsFn = defaultEquals) {  
    for (let i = 0; i < array.length; i++) {  
        if (equalsFn(value, array[i])) { // {1}  
            return i;  
        }  
    }  
    return -1;  
}
```

If we pass an array with 10 elements (`[1, ..., 10]`) to this function and search for element 1, in the first attempt, we will find the element we are looking for. Let's suppose the cost is 1 for each time we execute line {1}.

Let's try another example. Suppose we are searching for element 11. Line `{1}` will be executed 10 times (it will iterate through all of the values of the array and it will not find the value we are looking for; therefore, it will return `-1`). If line `{1}` has a cost of 1, executing it 10 times has a cost of 10, which is 10 times more than the first example.

Now, suppose the array has 1,000 elements (`[1, ..., 1,000]`). Searching for element 1,001 will result in line `{1}` being executed 1,000 times (and it will then return `-1`).

Note that the total cost of executing the `sequentialSearch` function depends on the number of elements of the array (size) and also on the value we are looking for. If the item we are looking for exists in the array, then how many times will line `{1}` be executed? If the item we are looking for does not exist, then line `{1}` will be executed size-of-the-array times, which we call the worst-case scenario.

Considering the worst-case scenario of the `sequentialSearch` function, if we have an array of size 10, the cost will be 10. If we have an array of size 1,000, the cost will be 1,000. We can conclude that the `sequentialSearch` function has a complexity of $O(n)$ — n being the size of the array (input).

To see the preceding explanation in practice, let's modify the algorithm to calculate the cost (the worst-case scenario), as follows:

```
function sequentialSearch(array, value, equalsFn = defaultEquals) {  
    let cost = 0;  
    for (let i = 0; i < array.length; i++) {  
        cost++;  
        if (equalsFn(value, array[i])) {  
            return i;  
        }  
    }  
    console.log(`cost for sequentialSearch with input size ${array.length} is  
${cost}`);  
    return -1;  
}
```

Try executing the preceding algorithm using different input sizes so that you can see the different outputs.

$O(n^2)$

For the $O(n^2)$ example, let's use the *bubble sort* algorithm:

```
function bubbleSort(array, compareFn = defaultCompare) {
    const { length } = array;
    for (let i = 0; i < length; i++) { // {1}
        for (let j = 0; j < length - 1; j++) { // {2}
            if (compareFn(array[j], array[j + 1]) === Compare.BIGGER_THAN) {
                swap(array, j, j + 1);
            }
        }
    }
    return array;
}
```

Consider that lines {1} and {2} have a cost of 1 each. Let's modify the algorithm to calculate the cost as follows:

```
function bubbleSort(array, compareFn = defaultCompare) {
    const { length } = array;
    let cost = 0;
    for (let i = 0; i < length; i++) { // {1}
        cost++;
        for (let j = 0; j < length - 1; j++) { // {2}
            cost++;
            if (compareFn(array[j], array[j + 1]) === Compare.BIGGER_THAN) {
                swap(array, j, j + 1);
            }
        }
    }
    console.log(`cost for bubbleSort with input size ${length} is ${cost}`);
    return array;
}
```

If we execute `bubbleSort` for an array with size 10, the `cost` will be 100 (10^2). If we execute `bubbleSort` for an array with size 100, the `cost` will be 10,000 (100^2). Note that the execution will take even longer every time we increase the input size.



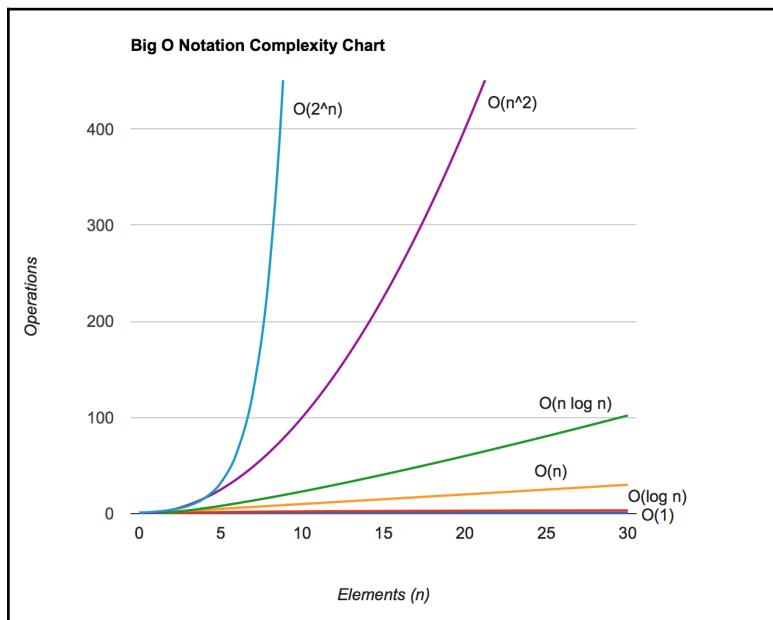
Note that the code from the $O(n)$ complexity has only one for loop, whereas $O(n^2)$ has two nested for loops. If the algorithm has three for loops iterating through the array, it will probably be $O(n^3)$.

Comparing complexities

We can create a table with some values to exemplify the cost of the algorithm given its input size as follows:

Input Size (n)	O(1)	O(log (n))	O(n)	O(n log(n))	O(n ²)	O(2 ⁿ)
10	1	1	10	10	100	1,024
20	1	1.30	20	26.02	400	1,048,576
50	1	1.69	50	84.94	2,500	Very big number
100	1	2	100	200	10,000	Very big number
500	1	2.69	500	1,349.48	250,000	Very big number
1,000	1	3	1,000	3,000	1,000,000	Very big number
10,000	1	4	10,000	40,000	10,000,000	Very big number

We can draw a chart based on the information presented in the preceding table to display the cost of different big O notation complexities as follows:





The preceding chart was also plotted using JavaScript. You can find its source code in the `examples/chapter15` directory of the source code bundle.

In the following section, you will find a cheat-sheet that shows the complexities of the algorithms we implemented in this book.



If you would like to have a printed version of the big O cheat sheet, the following link contains a nice version: <http://www.bigocheatsheet.com> (please note that, for some data structures such as stacks and queues, this book implemented an improved version of the data structure, therefore having a smaller big O complexity than the one displayed in the referenced link).

Data structures

The following table shows the complexities of data structures:

Data Structure	Average Cases			Worst Cases		
	Insert	Delete	Search	Insert	Delete	Search
Array/Stack/Queue	$O(1)$	$O(1)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
Linked list	$O(1)$	$O(1)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
Doubly linked list	$O(1)$	$O(1)$	$O(n)$	$O(1)$	$O(1)$	$O(n)$
Hash table	$O(1)$	$O(1)$	$O(1)$	$O(n)$	$O(n)$	$O(n)$
Binary Search Tree	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(n)$	$O(n)$	$O(n)$
AVL tree	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$
Red Black Tree	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$	$O(\log(n))$
Binary heap	$O(\log(n))$	$O(\log(n))$	$O(1)$: find max/min	$O(\log(n))$	$O(\log(n))$	$O(1)$

Graphs

The following table shows the complexities of graphs:

Node/ Edge Management	Storage Size	Add Vertex	Add Edge	Remove Vertex	Remove Edge	Query
Adjacency list	$O(V + E)$	$O(1)$	$O(1)$	$O(V + E)$	$O(E)$	$O(V)$
Adjacency matrix	$O(V ^2)$	$O(V ^2)$	$O(1)$	$O(V ^2)$	$O(1)$	$O(1)$

Sorting Algorithms

The following table shows the complexities for sorting algorithms:

Algorithm (applied to Array)	Time Complexity		
	Best Cases	Average Cases	Worst Cases
Bubble sort	$O(n)$	$O(n^2)$	$O(n^2)$
Selection sort	$O(n^2)$	$O(n^2)$	$O(n^2)$
Insertion sort	$O(n)$	$O(n^2)$	$O(n^2)$
Shell sort	$O(n \log(n))$	$O(n \log^2(n))$	$O(n \log^2(n))$
Merge sort	$O(n \log(n))$	$O(n \log(n))$	$O(n \log(n))$
Quick sort	$O(n \log(n))$	$O(n \log(n))$	$O(n^2)$
Heap sort	$O(n \log(n))$	$O(n \log(n))$	$O(n \log(n))$
Counting sort	$O(n+k)$	$O(n+k)$	$O(n+k)$
Bucket sort	$O(n+k)$	$O(n+k)$	$O(n^2)$
Radix sort	$O(nk)$	$O(nk)$	$O(nk)$

Searching Algorithms

The following table shows the complexities for searching algorithms:

Algorithm	Data Structure	Worst Cases
Sequential search	Array	$O(n)$
Binary search	Sorted array	$O(\log(n))$
Interpolation search	Sorted array	$O(n)$
Depth-first search (DFS)	Graph of $ V $ vertices and $ E $ edges	$O(V + E)$
Breadth-first search (BFS)	Graph of $ V $ vertices and $ E $ edges	$O(V + E)$

Introduction to the NP-completeness theory

In general, we say an algorithm is efficient if it is $O(n^k)$ for some constant, k , and this is called a polynomial algorithm.

Given a problem in which there is a polynomial algorithm even for the worst case, the algorithm is denoted by P (polynomial).

There is another set of algorithms called **NP (nondeterministic polynomial)**. An NP problem is a problem for which the solution can be verified in a polynomial time.

If a problem, P , has an algorithm that runs in a polynomial time, we can also verify its solution in polynomial time. Then, we can conclude that P is a subset of, or equal to, NP . However, it is unknown whether $P = NP$.

NP-complete problems are the hardest problems in an NP set. A decision problem L is NP-complete if:

1. L is in NP (that is, any given solution for NP-complete problems can be verified quickly, but there is no known efficient solution).
2. Every problem in NP is reducible to L in polynomial time.

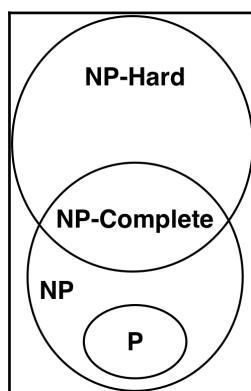
To understand what the reduction of a problem is, consider L and M as two decision problems. Suppose algorithm A solves L . That is, if y is an input for M , then algorithm B will answer Yes or No depending upon whether y belongs to M or not. The idea is to find a transformation from L to M so that the algorithm B can be part of algorithm A to solve A .

We also have another set of problems called **NP-hard**. A problem is NP-hard if it follows property 2 (of NP-complete), and it does not need to follow property 1. Therefore, the NP-complete set is also a subset of the NP-hard set.



Whether $P = NP$ or not is one of the biggest questions in computer science. If someone finds the answer to this question, it will have a major impact in cryptography, algorithm research, artificial intelligence, and many other fields.

The following diagram represents the Euler diagram for the **P**, **NP**, **NP-Complete**, and **NP-Hard** problems, considering that $P < NP$:



As examples of NP-hard problems that are not NP-complete problems, we can mention the **halting problem** and **Boolean Satisfiability Problem (SAT)**.

As examples of NP-complete problems, we can also mention the subset sum problem, traveling salesman problem, and vertex cover problem.



For more information about these problems, refer to <https://en.wikipedia.org/wiki/NP-completeness>.

Impossible problems and heuristic algorithms

Some of these problems we mentioned are impossible to solve. However, there are techniques that can be used to achieve an approximate solution in a satisfactory time. One technique would be using heuristic algorithms. A solution produced by heuristics might not be the best of all solutions, but it is good enough to solve the problem at the time.

Some examples of heuristics are local search, genetic algorithms, heuristics routing, and machine learning. For more information, take a look at [https://en.wikipedia.org/wiki/Heuristic_\(computer_science\)](https://en.wikipedia.org/wiki/Heuristic_(computer_science)).



Heuristics are a great and fun way of trying to solve a problem. You can try to pick a problem and develop a heuristic for your college or master's degree thesis.

Having fun with algorithms

We do not learn algorithms only because we need to study them in college or want to become developers. You can become a better professional by boosting your problem solving skills using the algorithms you learned in this book as a way of solving problems.

The best way of boosting our knowledge in problem solving is practicing, and practicing does not need to be boring. In this section, we will present some websites that you can go to and start having fun with algorithms (and even earn some cash while doing so!).

Here is a list of some useful websites (some of them do not support a solution written in JavaScript, but we can apply the logic we discussed in this book to other programming languages as well):

- **UVa Online Judge** (<http://uva.onlinejudge.org/>): This site contains a set of problems used in several programming contests around the world, including the **ACM International Collegiate Programming Contest (ICPC)**, which is sponsored by IBM. (If you are still in college, try to participate in this contest and, if your team wins, you can travel around the world with all expenses paid!) This site contains hundreds of problems in which we can use the algorithms learned in this book.
- **Sphere Online Judge** (<http://www.spoj.com/>): This site is similar to UVa Online Judge but supports more languages (including JavaScript submissions).
- **Coderbyte** (<http://coderbyte.com/>): This site contains problems (easy, medium, and hard) that can also be solved with JavaScript.
- **Project Euler** (<https://projecteuler.net/>): This site contains a series of mathematical/computer programming problems. All you have to do is input the answer to the problem, but we can use algorithms to find the answer for us.
- **HackerRank** (<https://www.hackerrank.com>): This site contains challenges divided into 16 categories (you can use the algorithms that you learned in this book and much more). It also supports JavaScript, among other languages.

- **CodeChef** (<http://www.codechef.com/>): This site also contains several problems and hosts competitions online.
- **Top Coder** (<http://www.topcoder.com/>): This site organizes programming tournaments, usually sponsored by companies such as NASA, Google, Yahoo, Amazon, and Facebook. Some contests give you the opportunity to work with the sponsoring company, and some contests can give you cash prizes. The website also offers great tutorials for problem solving and algorithms.

Another nice thing about the previous websites is that they usually present a real-world problem, and we need to identify which algorithm we can use to solve this problem. It is a way of knowing that the algorithms we learned in this book are not only educational, but can also be applied to solve real-world problems.

If you are starting a career in technology, it is highly recommended you create an account on **GitHub** (<https://github.com>) for free, and you can commit the source code you write to solve the problems from the previous websites. If you do not have any professional experience, GitHub can help you build a portfolio, and it can also help you get your first job!

Summary

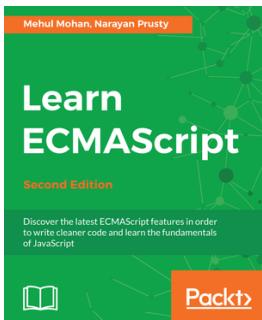
In this chapter, we covered big O notation and also discussed how we can calculate the complexity of an algorithm by applying this concept. We introduced the NP-completeness theory, a concept that you can delve into if you are interested in learning more about solving impossible problems and using heuristics for an approximately satisfactory solution.

We also presented some websites on which you can register for free, apply all the knowledge you acquired while reading this book, and even be offered your first job in IT!

Happy coding!

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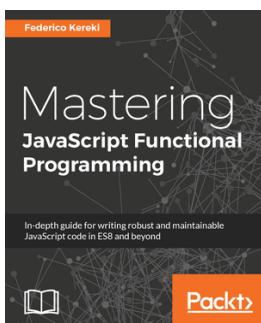
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