



# Weak-lensing stacking techniques

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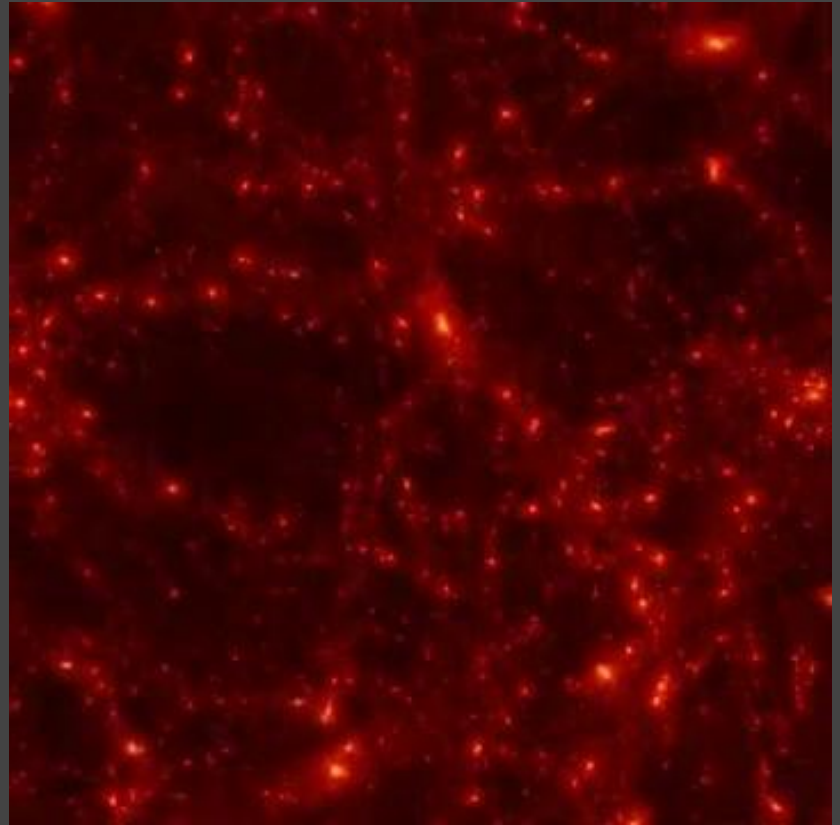
I A T E

# The LSS of the Universe

Navigating in a dark-matter only Universe

Ruiz et al. (2011)

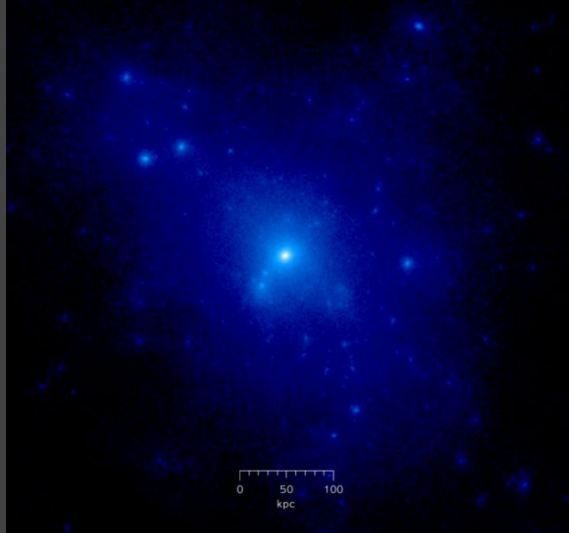
60 Mpc/h,  $8.93 \times 10^8 M_{\text{sun}}/h$



# Galaxy systems

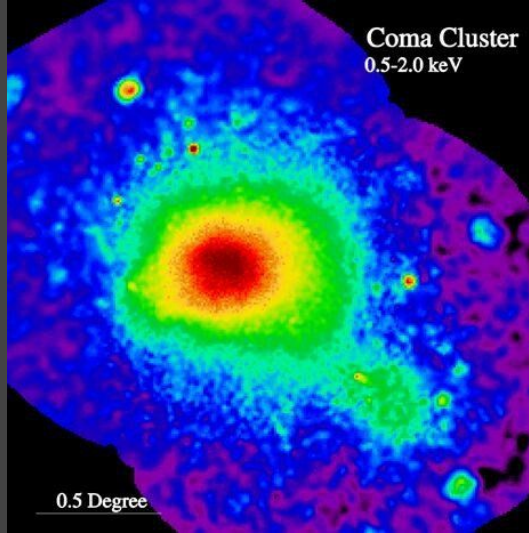
Galaxies tend to group together and form galaxy systems ranging from galaxy pairs to rich clusters.





~80%

Matéria escura



~15%

Gás



~5%

Estrelas

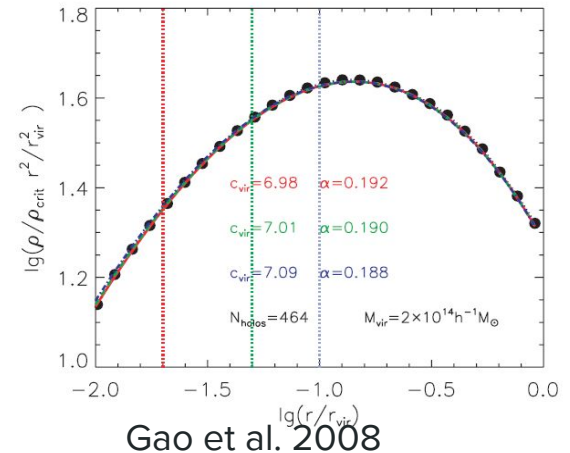
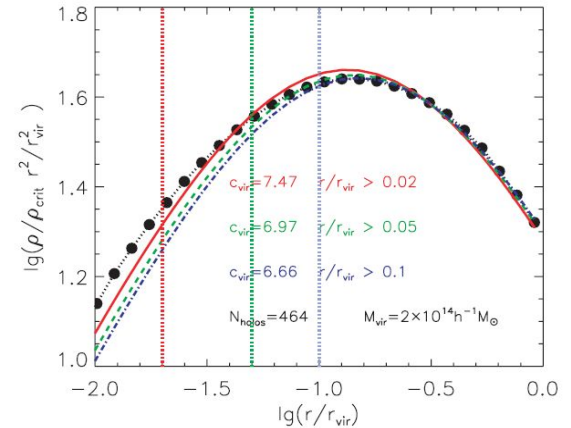
# Dark matter halos

NFW model (Navarro et al. 1997):

$$\rho(r) = \frac{\rho_{\text{crit}} \delta_c}{(r/r_s)(1+r/r_s)^2} \quad \delta_c = \frac{\Delta}{3} \frac{c_\Delta^3}{\ln(1+c_\Delta) - c_\Delta/(1+c_\Delta)}$$

Einasto model (Einasto & Haud 1989;  
Retana-Montenegro et al. 2012):

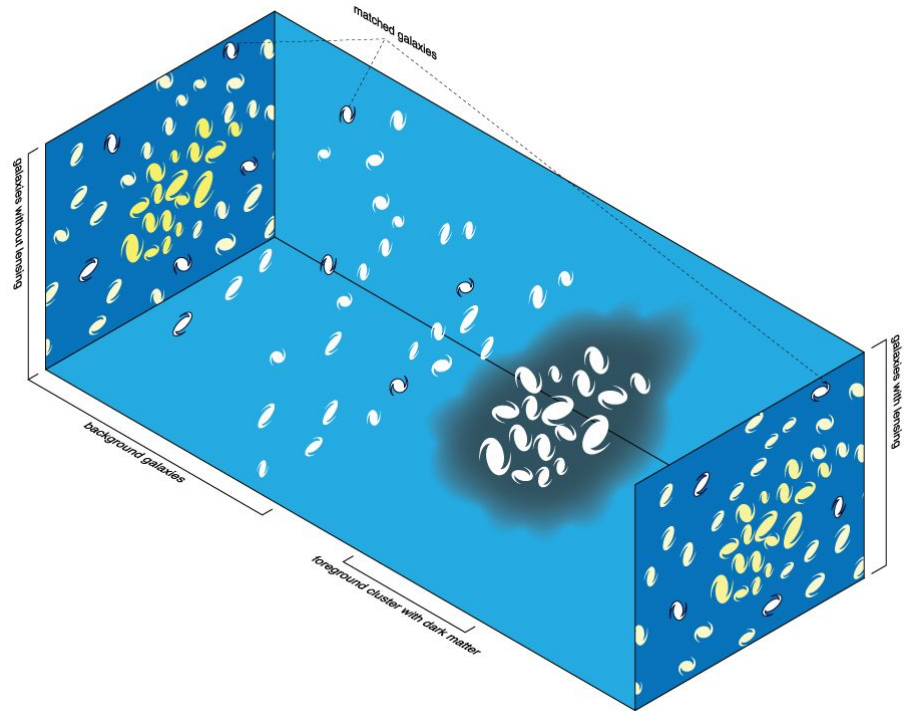
$$\rho(r) = \rho_{-2} \exp \left( -\frac{2}{\alpha} \left[ \left( \frac{r}{r_{-2}} \right)^\alpha - 1 \right] \right)$$



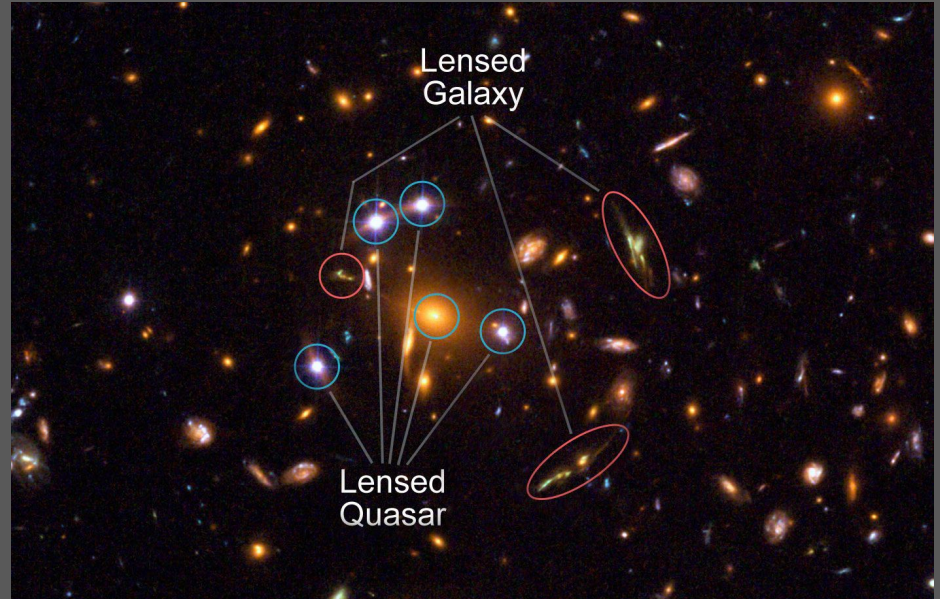


# Lensing effect by galaxy clusters

The gravitational lensing effect introduces a distortion in the luminous sources that are behind a gravitational potential considered as the lens. Galaxy systems in particular are powerful lenses that distort the shape of the galaxies that are behind.



# Strong lensing effect



# Weak lensing effect

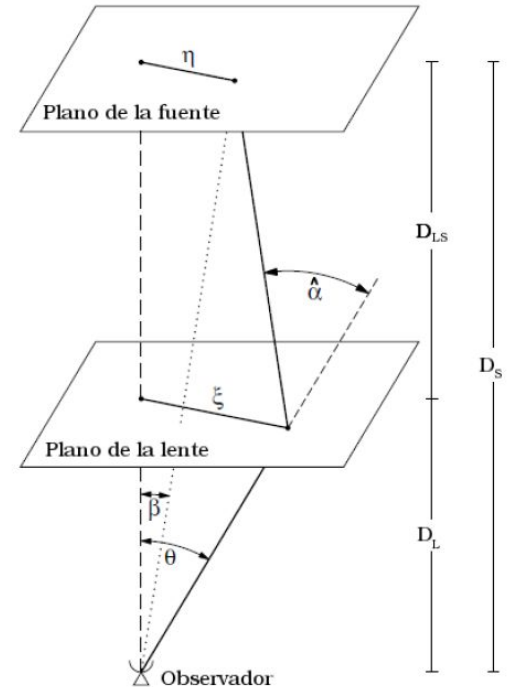
At the weak lensing regime the effect can be quantified through the shear

$$e = \frac{a - b}{a + b} = \frac{|\gamma|}{1 - \kappa} \approx |\gamma|$$

$$\gamma_t(r) \times \Sigma_{\text{crit}} = \bar{\Sigma}(< r) - \bar{\Sigma}(r) \equiv \Delta \Sigma(r)$$

$$\Sigma_{\text{crit}} = \frac{c^2}{4\pi G} \frac{D_{\text{os}}}{D_{\text{OL}} D_{\text{LS}}}$$

"You have a mass distribution about which you don't know anything, and then you observe sources which you don't know either, and then you claim to learn something about the mass distribution?"





# Weak lensing effect

At the weak lensing regime the effect can be quantified through the shear

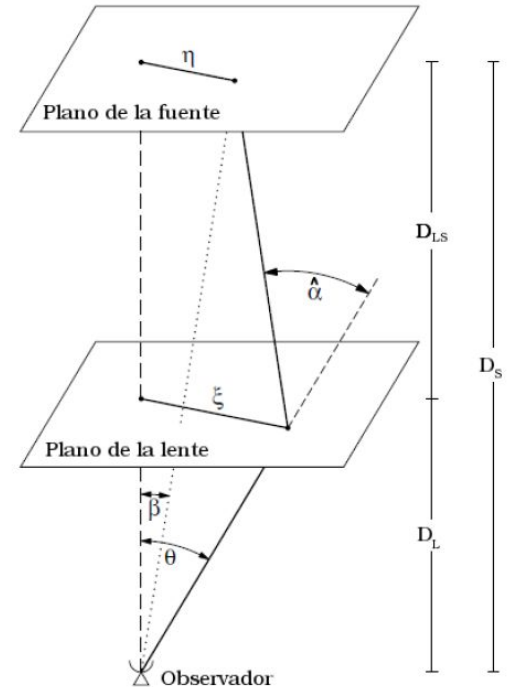
$$e = \frac{a - b}{a + b} = \frac{|\gamma|}{1 - \kappa} \approx |\gamma|$$

*Surface density distribution*

$$\gamma_t(r) \times \Sigma_{\text{crit}} = \bar{\Sigma}(< r) - \bar{\Sigma}(r) \equiv \Delta \Sigma(r)$$

$$\Sigma_{\text{crit}} = \frac{c^2}{4\pi G} \frac{D_{\text{os}}}{D_{\text{OL}} D_{\text{LS}}}$$

"You have a mass distribution about which you don't know anything, and then you observe sources which you don't know either, and then you claim to learn something about the mass distribution?"



# Weak lensing effect

At the weak lensing regime the effect can be quantified through the shear

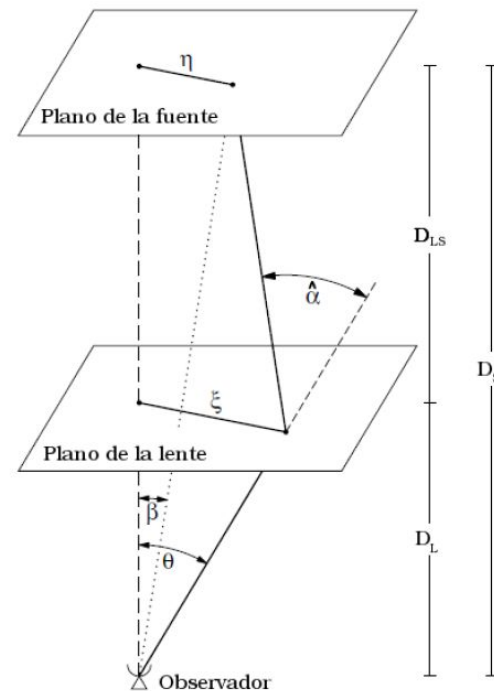
$$e = \frac{a - b}{a + b} = \frac{|\gamma|}{1 - \kappa} \approx |\gamma|$$

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$$\Sigma_{\text{crit}} = \frac{c^2}{4\pi G} \frac{D_{\text{os}}}{D_{\text{OL}} D_{\text{LS}}}$$

*Density contrast*

"You have a mass distribution about which you don't know anything, and then you observe sources which you don't know either, and then you claim to learn something about the mass distribution?"

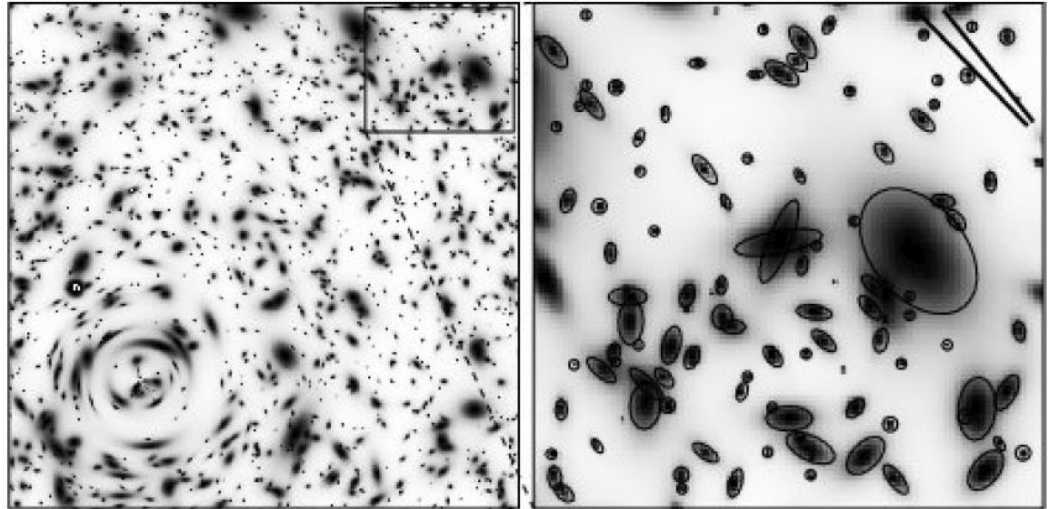


# Weak lensing effect

$$\mathbf{e} = \mathbf{e}_s + \boldsymbol{\gamma}$$

$$\langle \mathbf{e} \rangle = \langle \boldsymbol{\gamma} \rangle$$

$$\sigma_{\gamma} \approx \frac{\sigma_{\epsilon}}{\sqrt{N}}$$



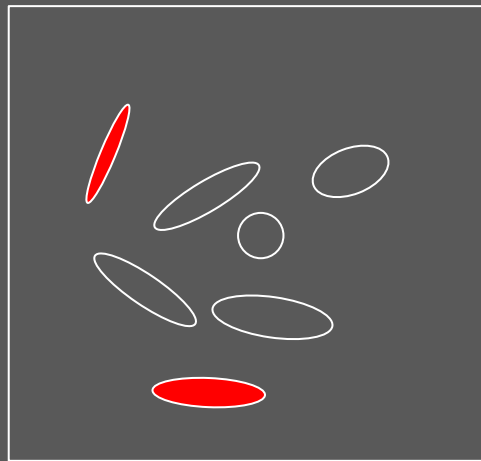
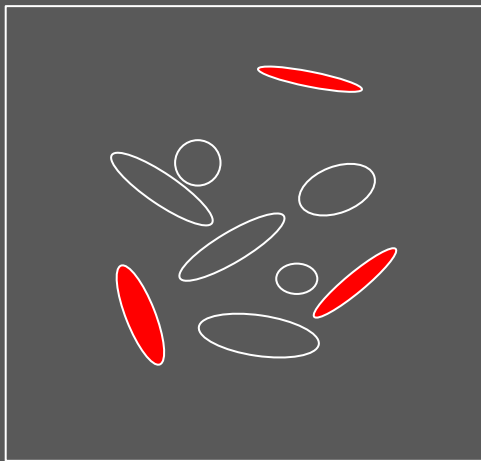
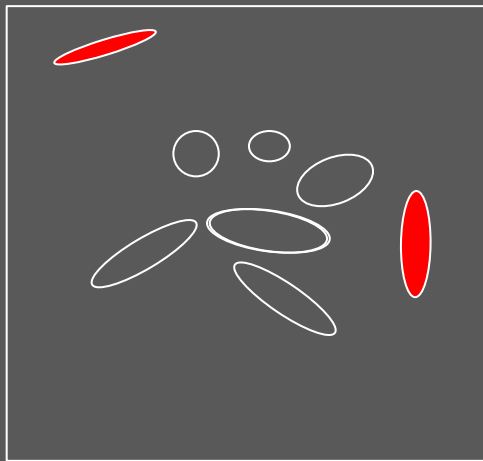
# Stacking techniques

Enables to obtain the mean mass distribution at large radial ranges of a combined sample of clusters, by artificially increasing the lensing signal



# Stacking techniques

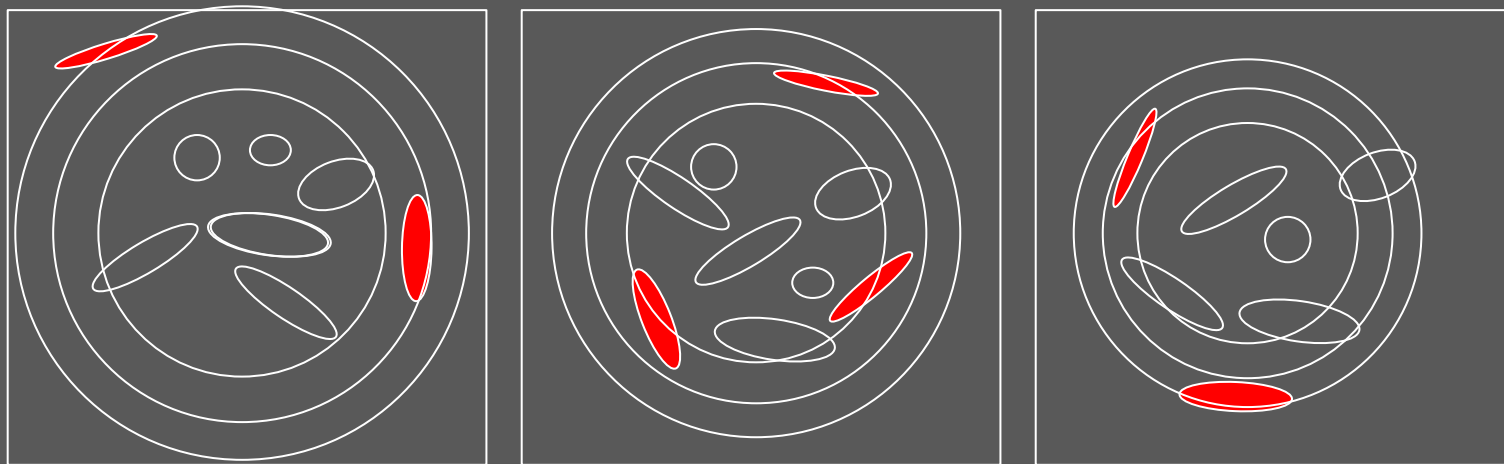
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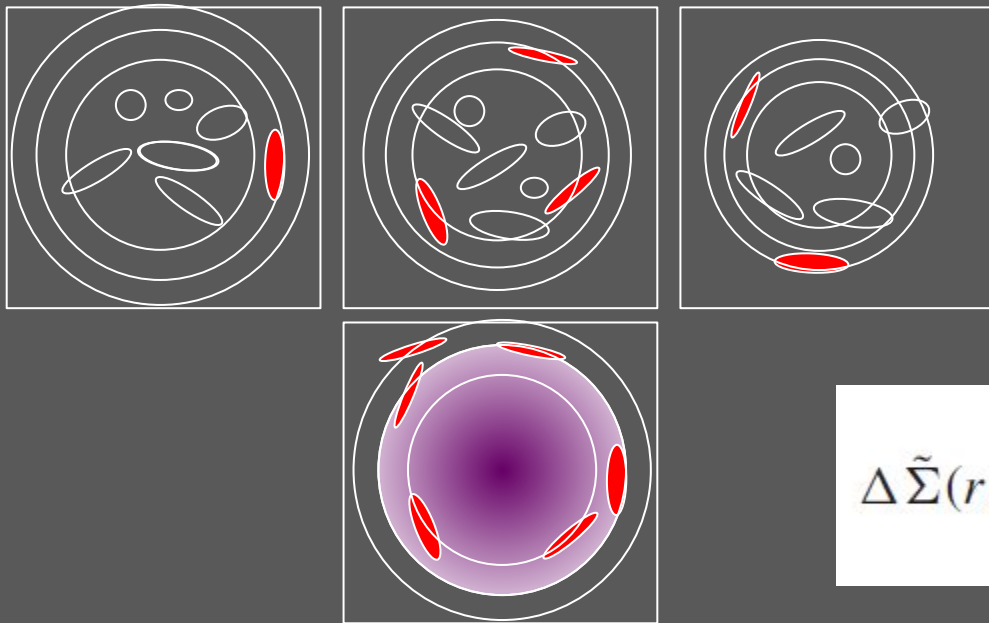


# Stacking techniques

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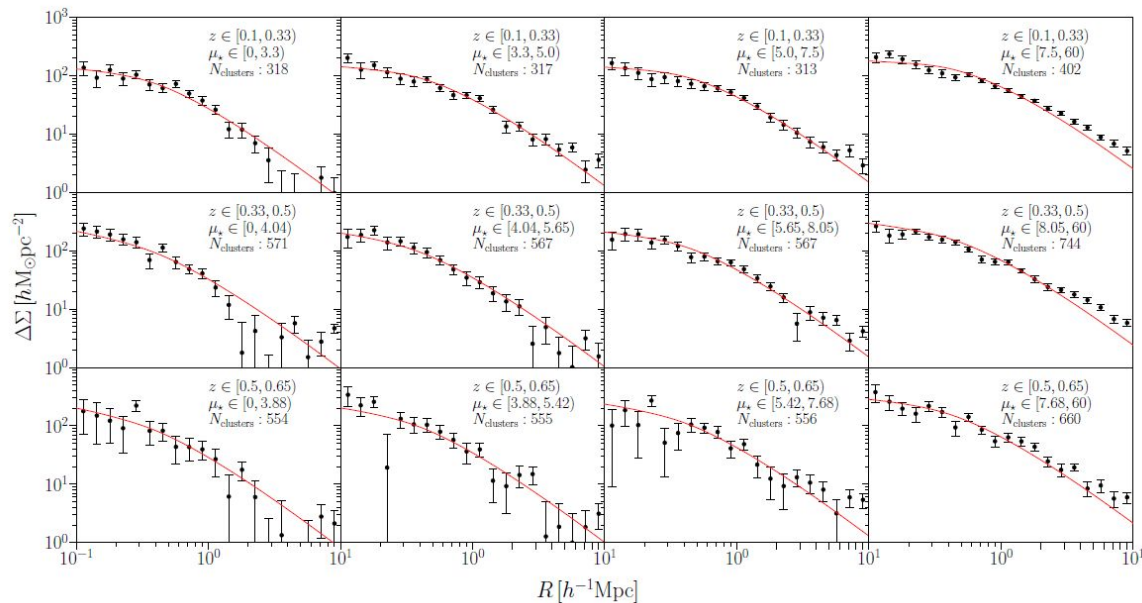


# Stacking techniques

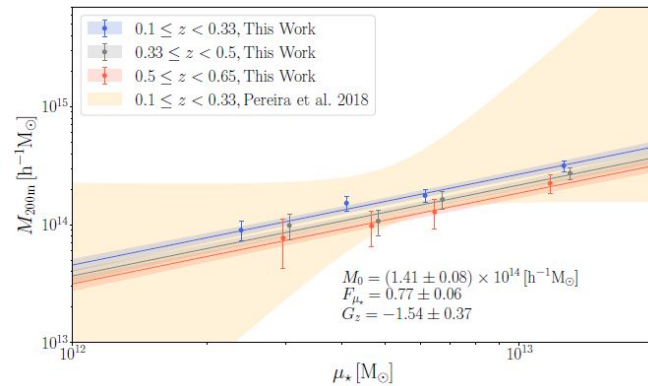


$$\Delta \tilde{\Sigma}(r) = \frac{\sum_{j=1}^{N_L} \sum_{i=1}^{N_{S,j}} \omega_{LS,ij} \Sigma_{\text{crit},ij} e_{t,ij}}{\sum_{j=1}^{N_L} \sum_{i=1}^{N_{S,j}} \omega_{LS,ij}}$$

# Stacking techniques



Pereira et al. (2020)



# Let's lens!

**Lenses** -> **redMaPPer** Galaxy Clusters (v6.3; Rykoff et al. 2016, <http://risa.stanford.edu/redmapper/>)

**Sources** -> **CFHTLens** shear catalogue

You can access to the data through the COSMOSHub platform (<https://cosmohub.pic.es/home>)

Combining the shapes of the sources tangentially to the cluster centres we obtain

$$\Delta \tilde{\Sigma}(r) = \frac{\sum_{j=1}^{N_L} \sum_{i=1}^{N_{S,j}} \omega_{LS,ij} \Sigma_{\text{crit},ij} e_{t,ij}}{\sum_{j=1}^{N_L} \sum_{i=1}^{N_{S,j}} \omega_{LS,ij}}$$

# Let's model!

Go to [https://github.com/elizabethig/example\\_fit](https://github.com/elizabethig/example_fit) and follow the instructions :)

Main halo component (NFW ):

$$\rho(r) = \frac{\rho_{\text{crit}} \delta_c}{(r/r_s)(1+r/r_s)^2} \cdot \delta_c = \frac{\Delta}{3} \frac{c_\Delta^3}{\ln(1+c_\Delta) - c_\Delta/(1+c_\Delta)}$$

Neighbouring mass component:

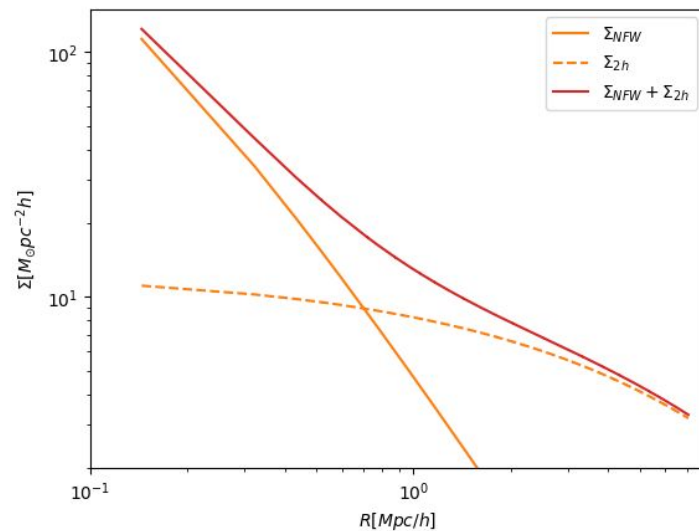
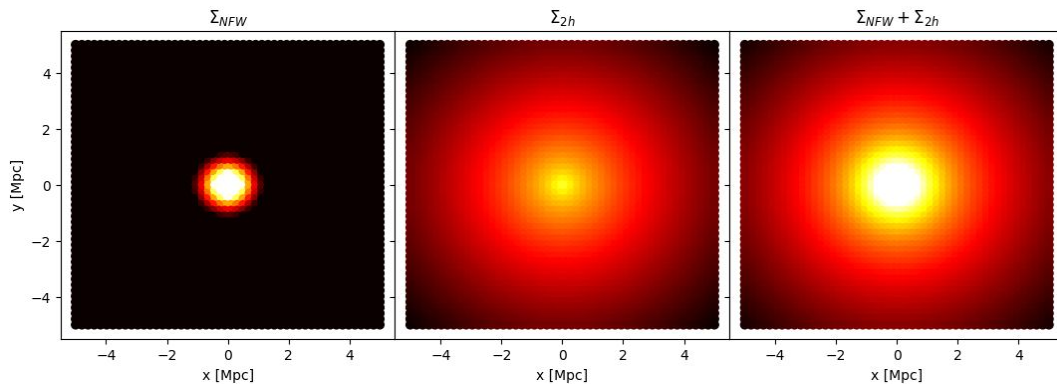
$$\rho_{2h}(r) = \rho_m \xi_{hm} = \rho_{\text{crit}} \Omega_m (1+z)^3 b(M_{200}, \langle z \rangle) \xi_{mm}$$



# Let's model!

$\rho \rightarrow \Sigma$

$$\Sigma(\vec{\xi}) \equiv \int \rho(\xi_1, \xi_2, r_3) dr_3$$



# Let's model!

$\rho \rightarrow \Sigma \rightarrow \Delta\Sigma$

$$\Delta\Sigma(R) = \frac{1}{\pi R^2} \int_0^R 2\pi r \Sigma(r) dr - \Sigma(R)$$

