

Title

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1 Objectives

For LCDM, interacting models, and CPL, calculate

- ξ range for varying EoS while fixing Ωm_0
- ξ range for varying Ωm_0 or r , while fixing ω
- Does $\xi > 0$ means energy transfer to dark energy in this method?

2 Background

Deceleration parameter reads

$$q(z) = -1 + \frac{1+z}{H} \frac{dH}{dz} \quad (1)$$

For interaction models, the Friedmann equations,

$$\dot{\rho}_c + 3H\rho_c = Q_c \quad (2a)$$

$$\dot{\rho}_d + 3H(1+w)\rho_d = -Q_c \quad (2b)$$

$Q_c = \xi H \rho_c$ Background equations,

$$\Omega m = \Omega m_0 (1+z)^{3-\xi} \quad (3a)$$

$$\Omega d = (\Omega d_0 + \frac{\xi}{3w+\xi} \Omega m_0) (1+z)^{3(1+w)} + \frac{-\xi}{\xi+3w} \Omega m = \Omega \bar{d}_0 (1+z)^3 + \frac{-\xi}{\xi+3w} \Omega m \quad (3b)$$

$Q_c = \xi H \rho_d$

$$\Omega m = (\Omega m_0 + \frac{\xi}{\xi+3w} \Omega d_0) (1+z)^3 + \frac{-\xi}{\xi+3w} \Omega d = \omega \bar{m}_0 (1+z)^3 + \frac{-\xi}{\xi+3w} \Omega d \quad (4a)$$

$$\Omega d = \Omega d_0 (1+z)^{3(1+w)+\xi} \quad (4b)$$

Eqn ?? and eqn ?? shows that the coupling constant has two effects,

1. Change the amplitude of the evolution of matter or dark energy energy density.
2. Transfer energy between DE and DM.

2.1 Some definitions

1. For short

$$r = \frac{\Omega_{m0}}{\Omega_{d0}}$$

CPL EoS is

$$w = w_0 + w_1 \frac{z}{1+z}$$

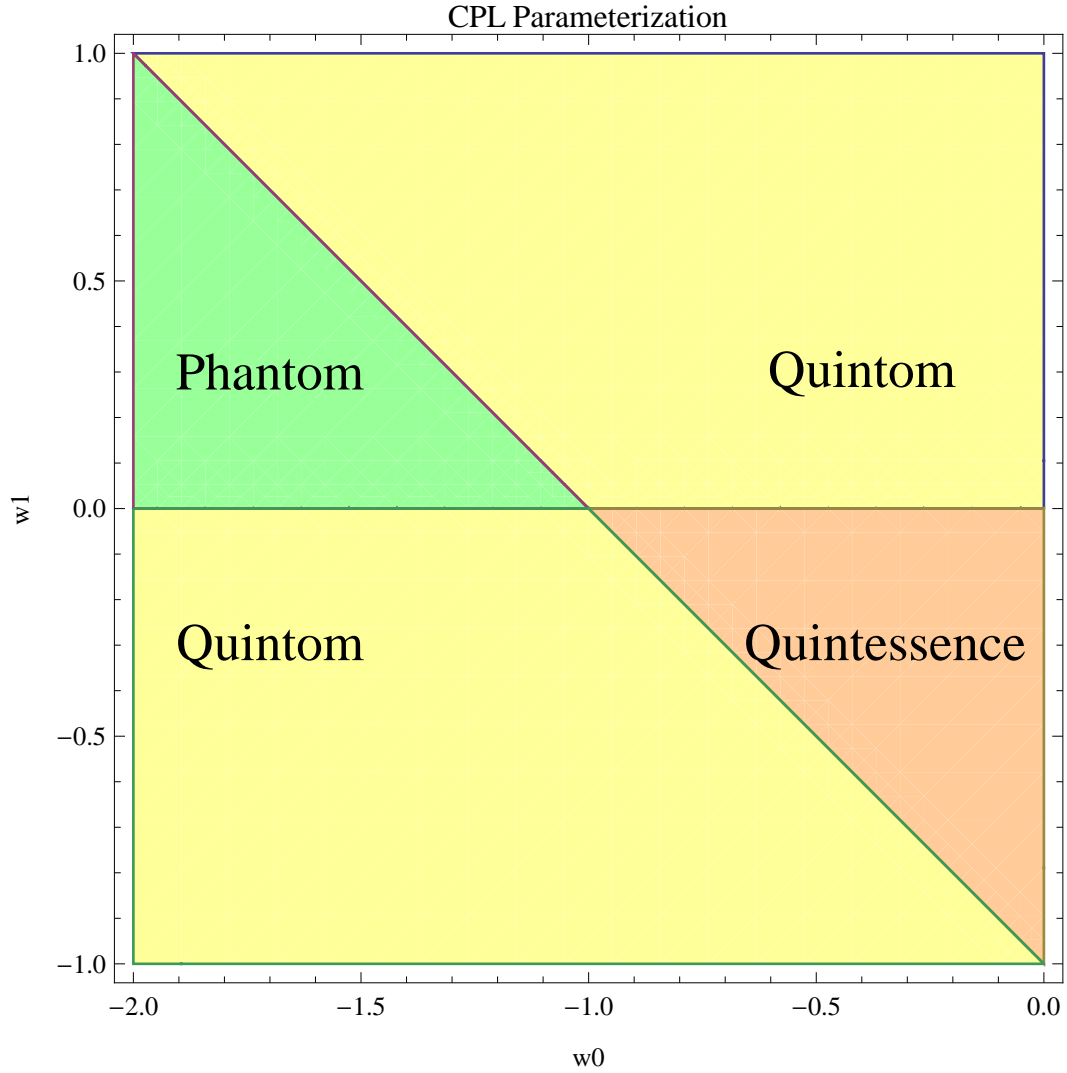


Figure 1: CPL classification

Classification Figure ?? shows how to category the dark energy models in CPL parametrization.

3 Data & Method

3.1 Data

ΛCDM Parameters From WMAP, $\Omega_m0 = 0.265$

Constraints $\Omega_m0 = 0.247(+0.013, -0.013)$; Transition redshift $0.426(+0.082, -0.050)$.(arXiv:1205.4688, arXiv:astro-ph/0611572).

In $(\Omega_m0, \text{Transition redshift})$ plane, allowed region is a rectangle centred at $(0.274, 0.426)$ with two diagonal points $(0.261, 0.376)$ and $(0.287, 0.508)$.

CPL $\Omega_m0 = 0.269(+0.017, -0.008)$, $w0 = -0.97(+0.12, -0.07)$, $w1 = 0.03(+0.26, -0.75)$

4 Results

Check the files in files folder.

4.1 $Q_c = \xi H \rho_c$

Results table

$Q_c = \xi H \rho_c$, constant ξ , constant $w = -1$: Results for ξ			
$\Omega_m0/\Omega_{d0} \backslash \text{Transition}$	$z_t = 0.376$	$z_t = 0.426$	$z_t = 0.508$
$r = 0.358$	-1.25282	-0.965436	-0.617444
$r = 0.378$	-1.15011	-0.875189	-0.542347
$r = 0.398$	-1.05453	-0.791252	-0.472561

Figure 2: ICC Result table

Figure ?? shows that

ρ_c -Dec-1 The universe decelerates faster at the early stage for smaller interaction constant ξ even they have the same matter fraction.

ρ_c -Dec-2 For the same ξ , the deceleration converge ($q = (1 - \xi)/2$ with $3w + \xi < 0$) at early time.

Figure ?? shows

ρ_c -Trans-1 Transition happens earlier when matter fraction is smaller. Matter is against DE's pressure.

ρ_c -Trans-2 Transition is later when ξ is smaller. Energy transfers to DE when ξ is negative, then why later transition? ¹

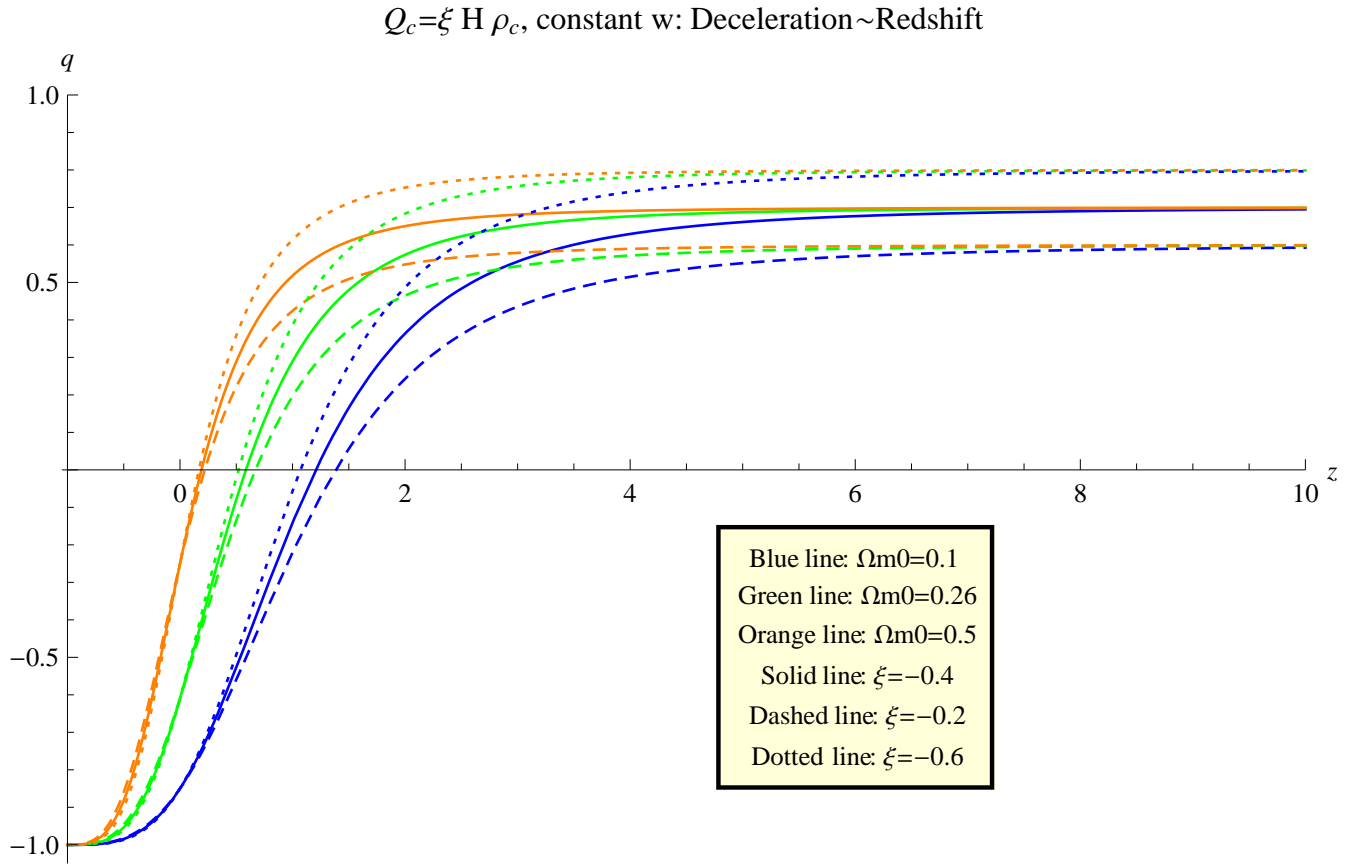


Figure 3: Deceleration parameter

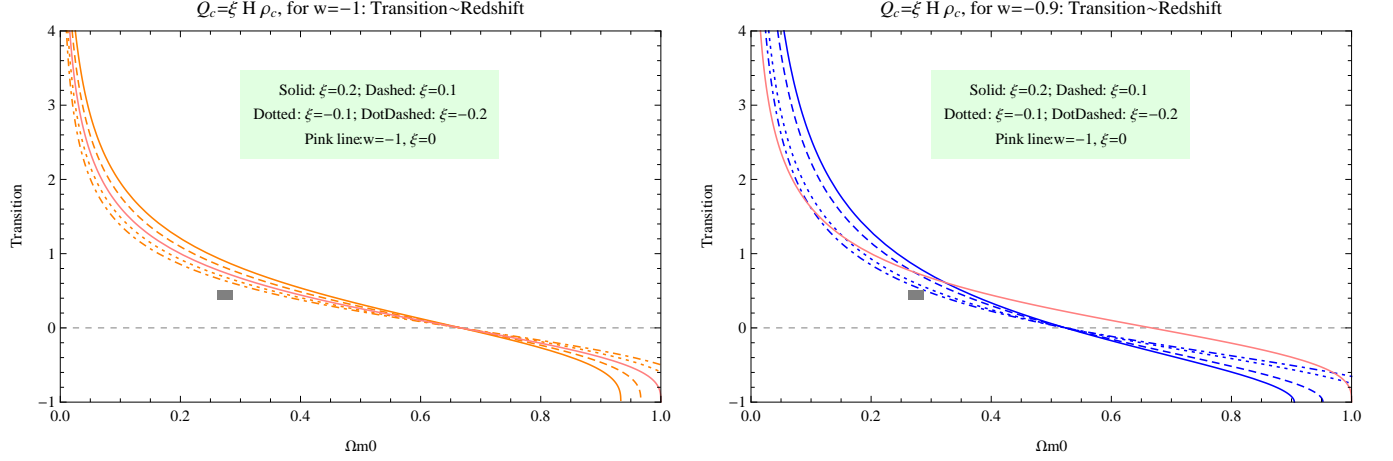


Figure 4: Transition redshift.

Figure ?? and figure ?? (vertical lines are $w = -1 \pm 0.05$) show the value of ξ for different EoS. Results from this figure:

(EoS is -1 within $5w=-1$ (-1.279,-0.457) center:-0.878 ; $w=-1.05$ (-1.293,-0.461) center:-0.887 ; $w=-0.95$ (-1.255,-0.447) center:-0.860 ;

ρ_c -xiVS w -1 NOT monotonic. The result of ξ is greatly affected by $\Omega m0$. In correspondence with another

ρ_c -xiVS w -2 For different $\Omega m0$, ξ values deviate greatly from each other at small w .

Figures ?? show how do we constrain ξ and how do EoS change our constrain results with the transition fixed.

ρ_c -xiVS $\Omega m0$ -1 The smaller, the more difference among ξ values of different EoS. Reason for this is less matter has less effect on the evolution thus the property of dark energy determines more about the transition.

ρ_c -xiVS $\Omega m0$ -2 Second figure shows

- + System with smaller w needs smaller coupling to achieve the same transition time, as expected.
- + So we give the result that $w \in (-0.58406, -0.3334)$ if we constrain $\Omega m0 = 0.2603$ and transition redshift 0.426.

¹Reasons below. All solutions of equation ?? have the same value at $z = 0$, i.e. now. Equation ??a tells us a positive ξ leads to smaller energy density of dark matter at early time of the universe, thus dark energy takes over quickly if the transition happens before today. (For more details, calculation are shown in supplement_08-10.pdf file.)

ξ results for $Q_c = \xi H \rho_c$ (Fitting data: Data From, 2)			
w	Center	Lower	Upper
-1.183	-0.881565	-1.29687	-0.443589
-1.087	-0.88948	-1.29859	-0.459135
-0.991	-0.875238	-1.27522	-0.456176

$Q_c = \xi H \rho_c$, constant w: Coupling Constant \sim EoS

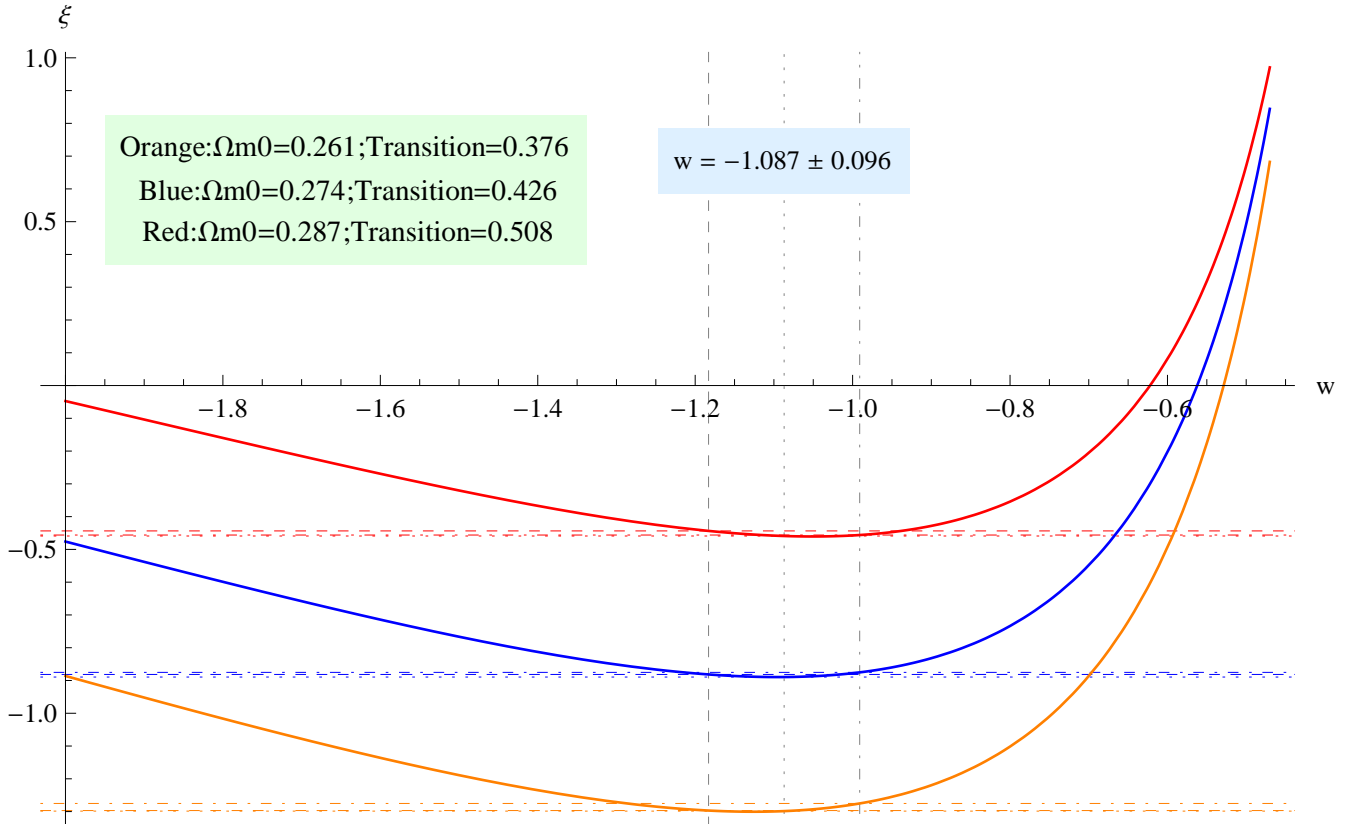


Figure 5: Interacting coefficient for $Q_c = \xi H \rho_c$

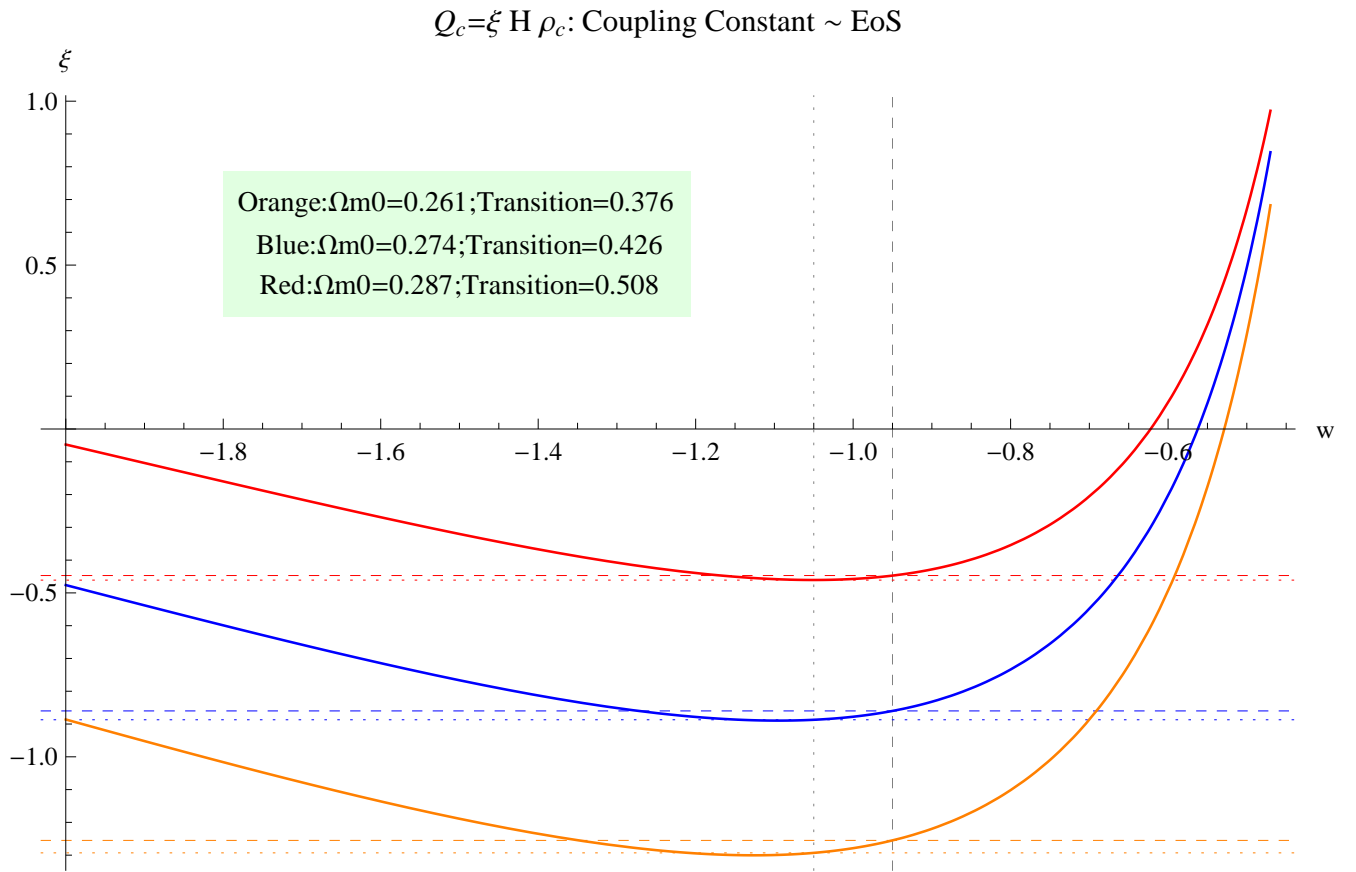
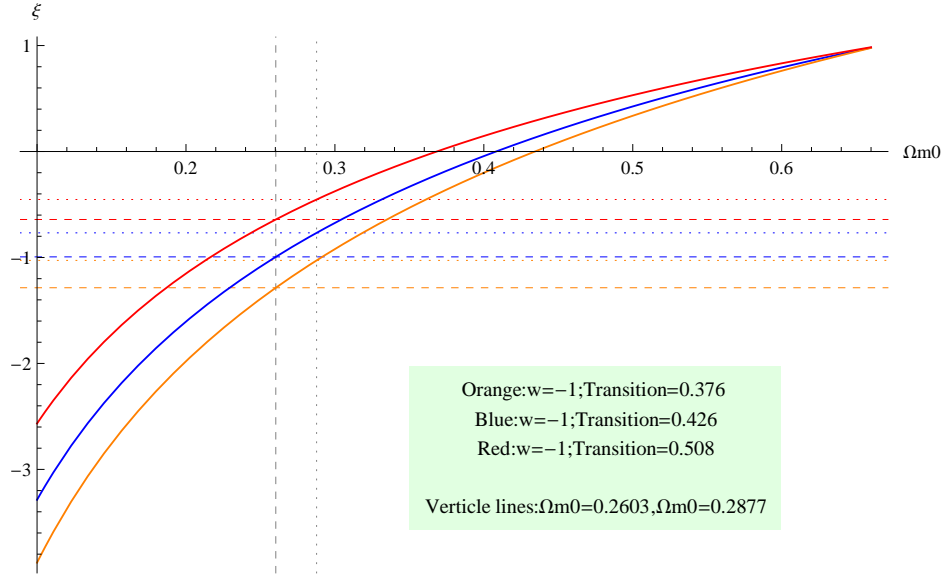


Figure 6: Interacting coefficient for $Q_c = \xi H \rho_c$

For $\Omega_{m0} \in 0.274 (1 \pm 0.05)$			
Table of ξ for different Ω_{m0} -Transition combination			
Ω_{m0} -Transition	0.426	0.376	0.508
0.2603	-0.994339	-1.28571	-0.641508
0.274	-0.877755	-1.15303	-0.544482
0.2877	-0.767582	-1.02756	-0.452892

$Q_c = \xi H \rho_c$, constant w : Coupling Constant $\sim \Omega_{m0}$



$Q_c = \xi H \rho_c$, constant w : Coupling Constant $\sim \Omega_{m0}$

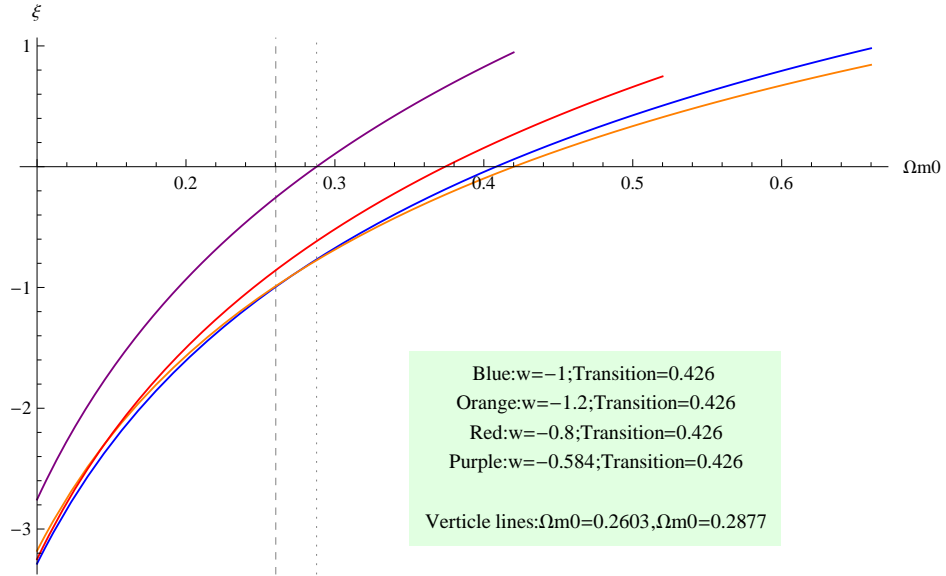


Figure 7: Interacting coefficient changing with Ω_{m0} for $Q_c = \xi H \rho_c$

4.2 $Q_c = \xi H \rho_c$, CPL

For a flat universe, choose the parameters $w_0=-1.02, w_1=0.6$, the region for interaction constant ξ should be $(-1.04, -0.21)$ with a center at -0.64 , derived from the (transition redshift, Ω_{m0}) plane, while a result of $(-1.01, -0.23)$ with a center at -0.63 , derived from (transition redshift, $\Omega_{m0}/$

First let's have a look at the deceleration parameter.

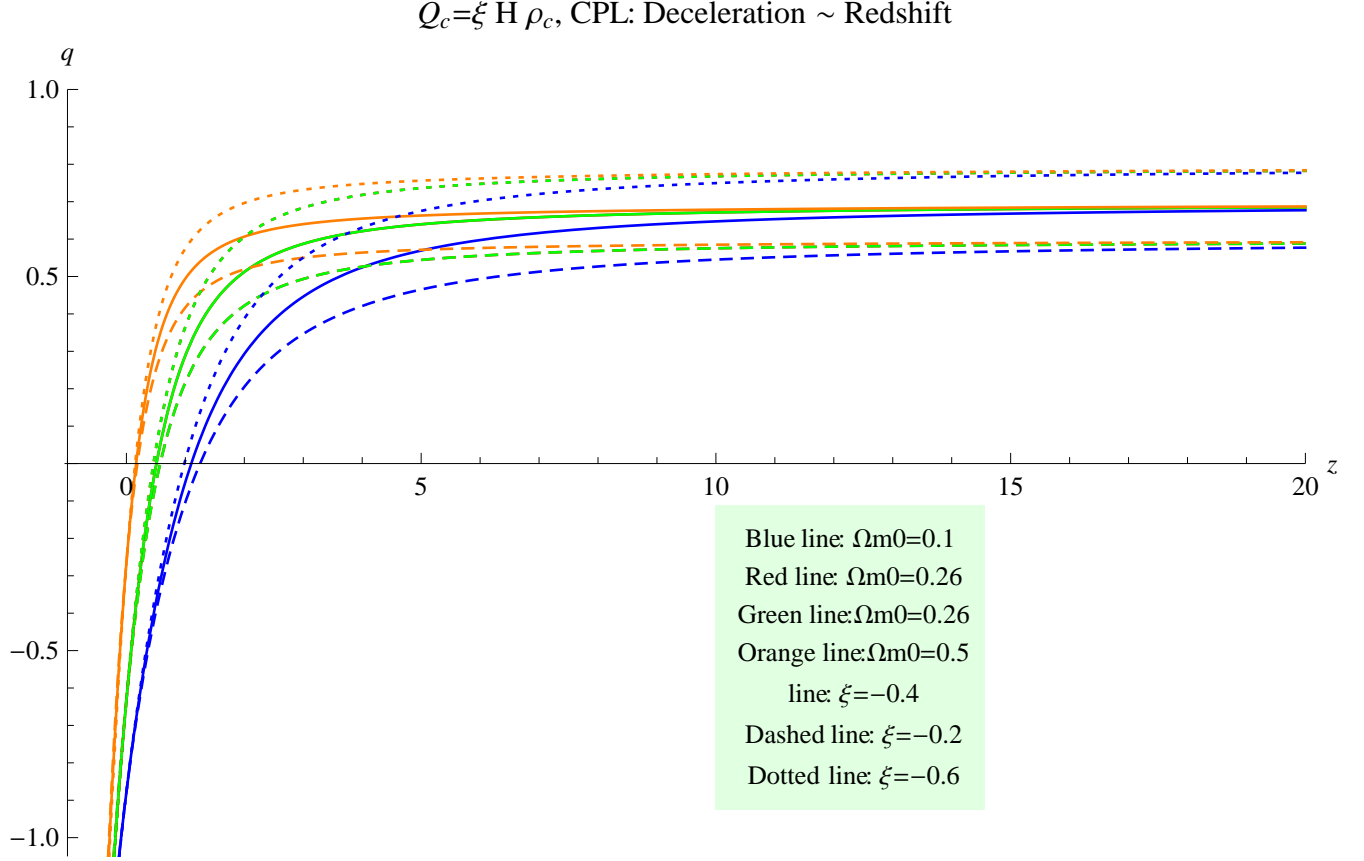


Figure 8: Deceleration parameters for ICCPL ($Q_c = \xi H \rho_c$ with CPL parametrized EoS)

Figure ?? is right similar to constant EoS situation.

Figures ?? show

$\rho_{c\text{-ICCPL-TV}\Omega_{m0}=1}$ Coupling acts on these model similar to constant EoS model.

$\rho_{c\text{-ICCPL-TV}\Omega_{m0}=2}$ The change in w_1 has a similar effect with the change of ξ . Larger w_1 corresponds to smaller ξ . The reason for this is both negative ξ and larger w_1 enhances the energy density of dark energy (check using the CPL EoS).

The dots in figure ?? are the data set of $\xi = 0$. If we need $\xi < 0$, i.e., energy transfers from dark matter to dark energy, the allowed parameter space is the striped area.

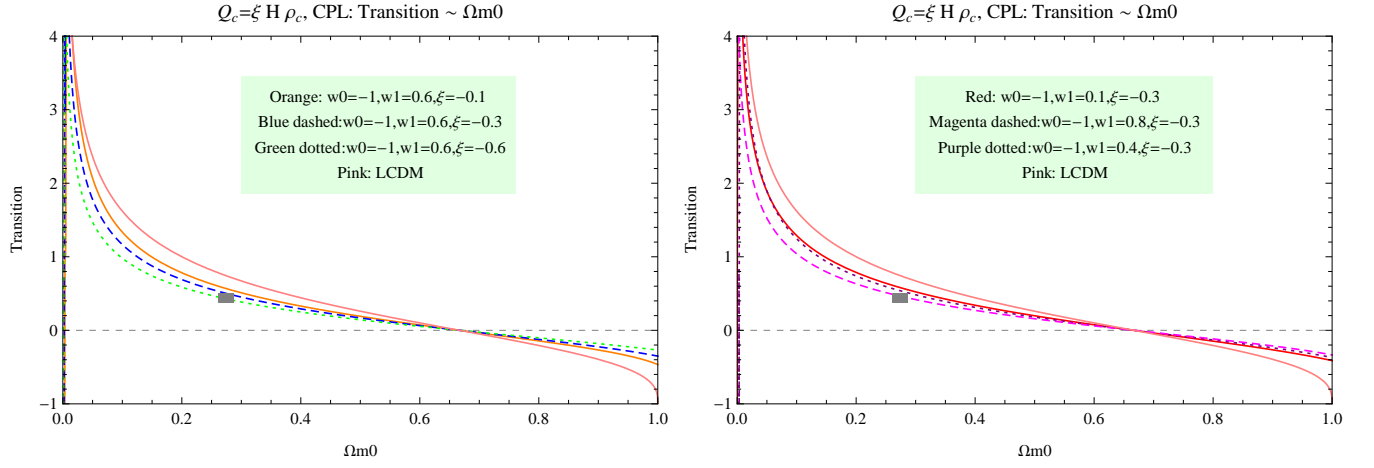


Figure 9: The effect of EoS parameters on Transition and Ωm_0

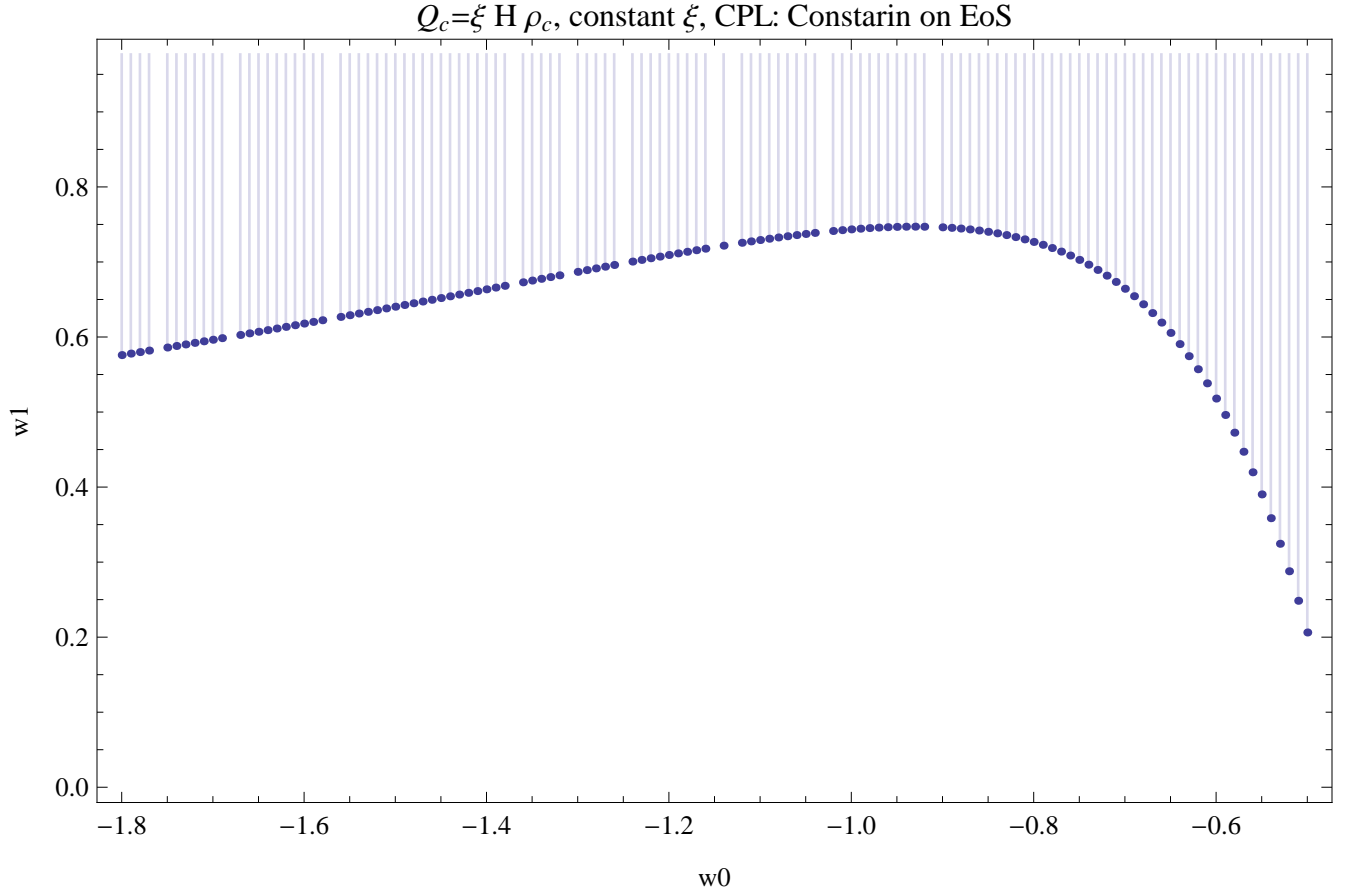


Figure 10: Lower bound in the w_1 w_0 parameter space

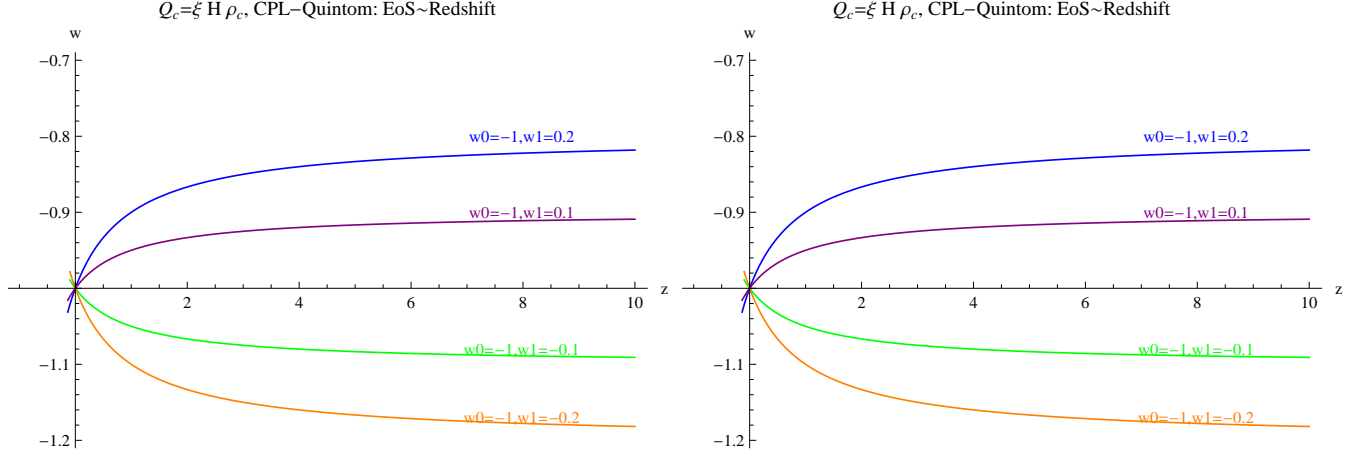


Figure 11: The EoS

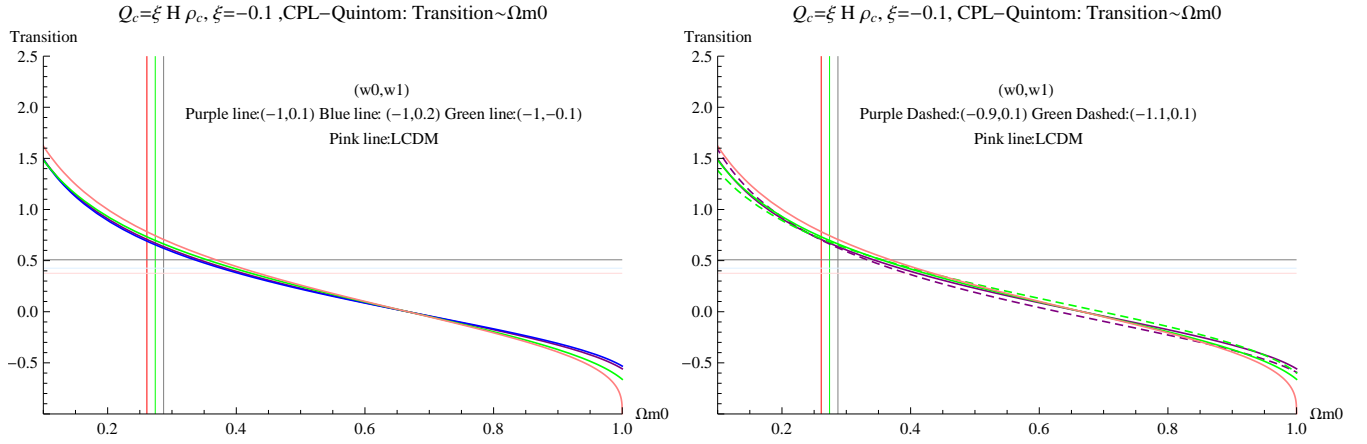


Figure 12: Transition vs Ω_{m0}

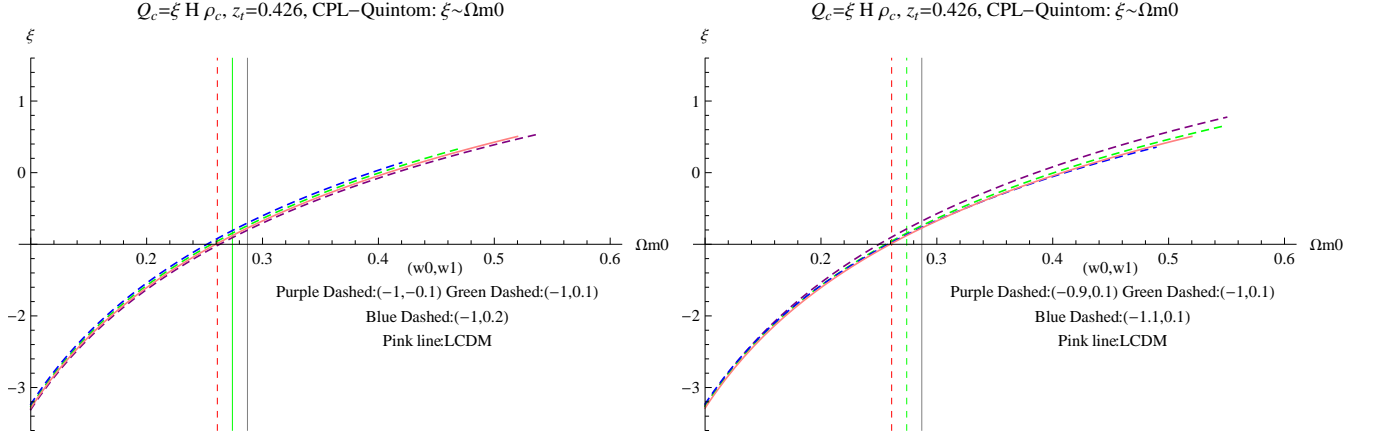


Figure 13: ξ vs $\Omega m0$

4.2.1 Quintom

(Figures ??, ??, ??)

The left figure in ?? indicates a possible stationary point.²

(Other results are shown on the complete results files.)

4.2.2 Quintessence

(Figures ??, ?? and ??.)

4.2.3 Phantom

(Figures ??, ??, ??, ??)

4.3 $Q_c = \xi H \rho_d$

(Figures ??, ??, ??, ??)

4.4 I2CCPL

(Figures ??, ??)

Figure ?? shows the all the deceleration are the same at very early time.

4.4.1 Quintom

(Figures ??, ??)

4.4.2 Quintessence

(Figures ??, ??)

²Only possible because I can only partially prove there is a nearly stationary. This is on my *Cosmologia Notebook*.

$Q_c = \xi H \rho_c$, CPL, Quintessence: EoS ~ Redshift

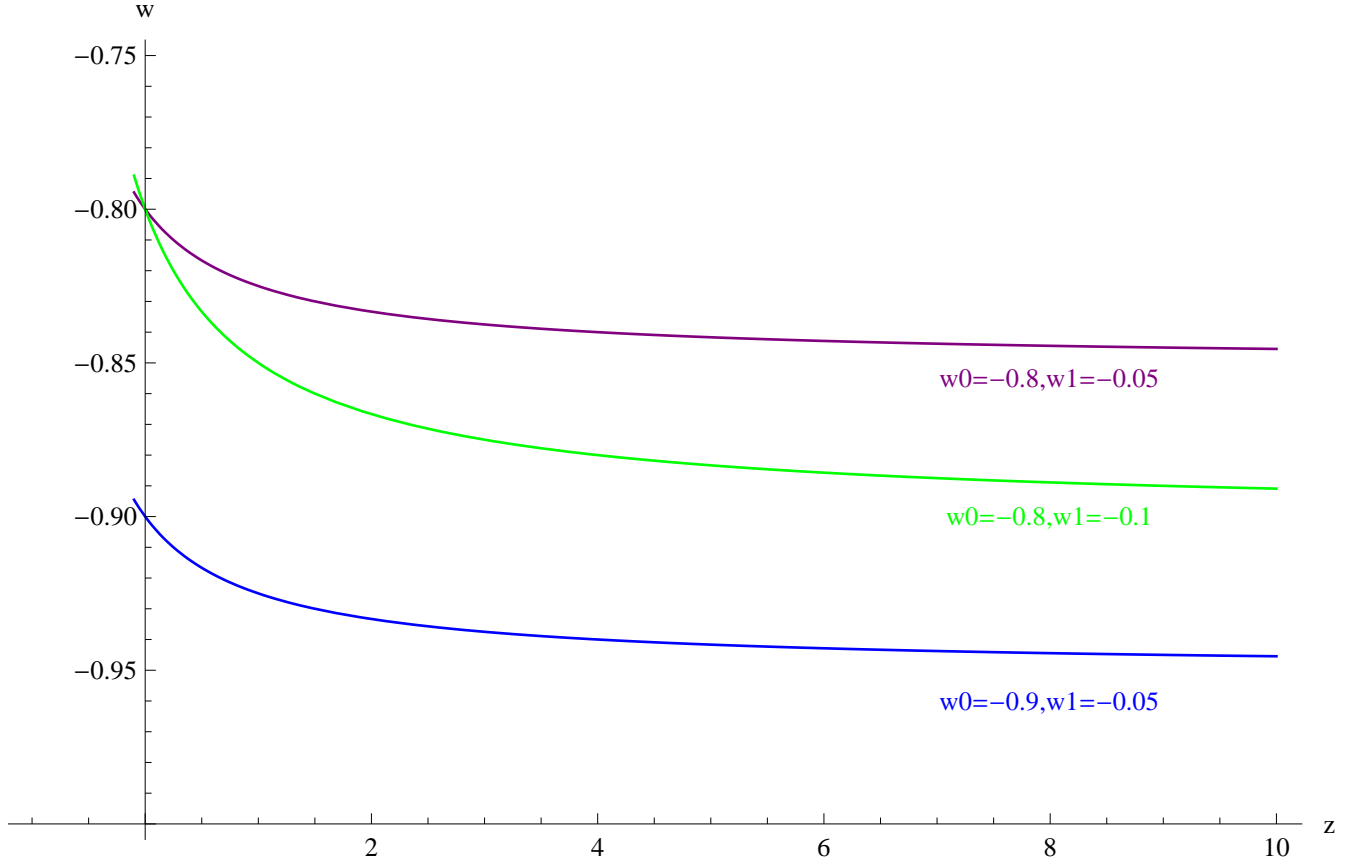
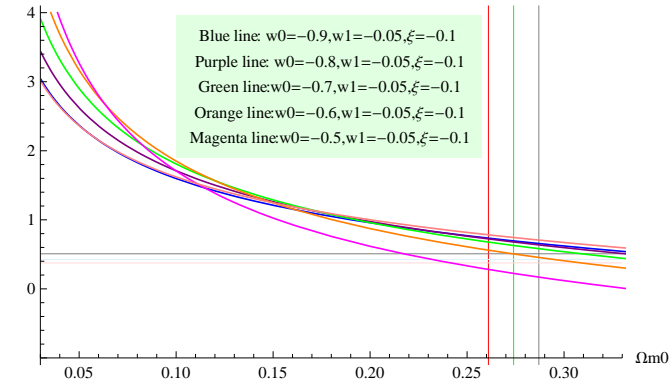


Figure 14: The EoS

$Q_c = \xi H \rho_c$, $\xi = -0.1$, CPL, Quintessence: Transition Redshift ~ Ωm_0



$Q_c = \xi H \rho_c$, $\xi = -0.1$, CPL, CPL, Quintessence: Transition Redshift ~ Ωm_0

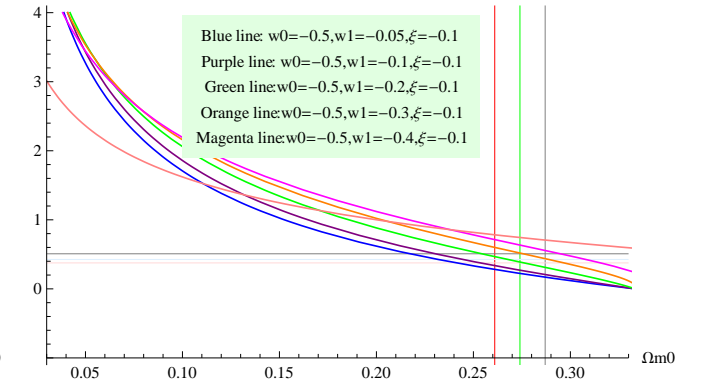


Figure 15: Transition vs Ωm_0

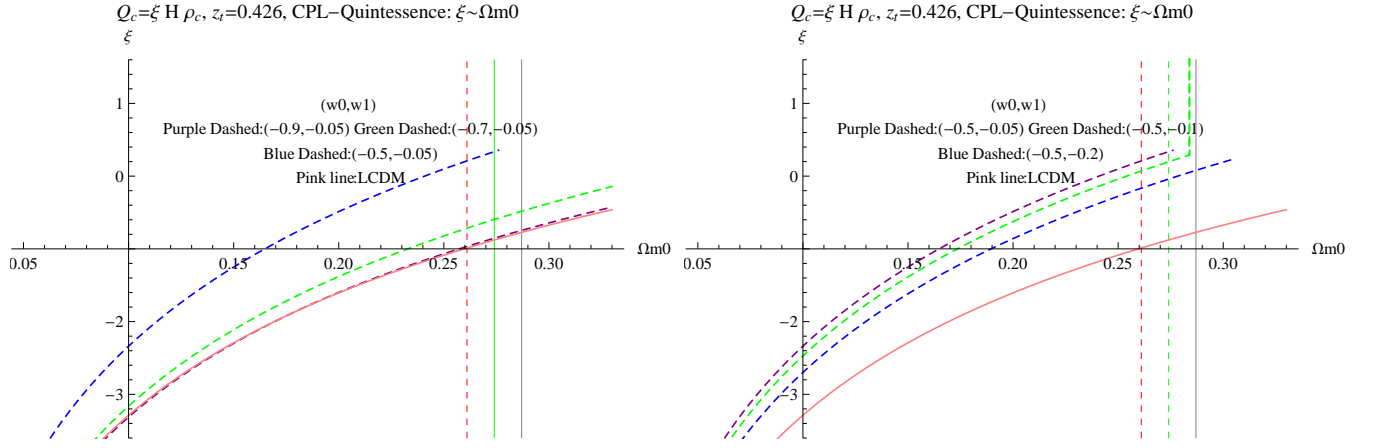


Figure 16: ξ vs Ω_{m0}

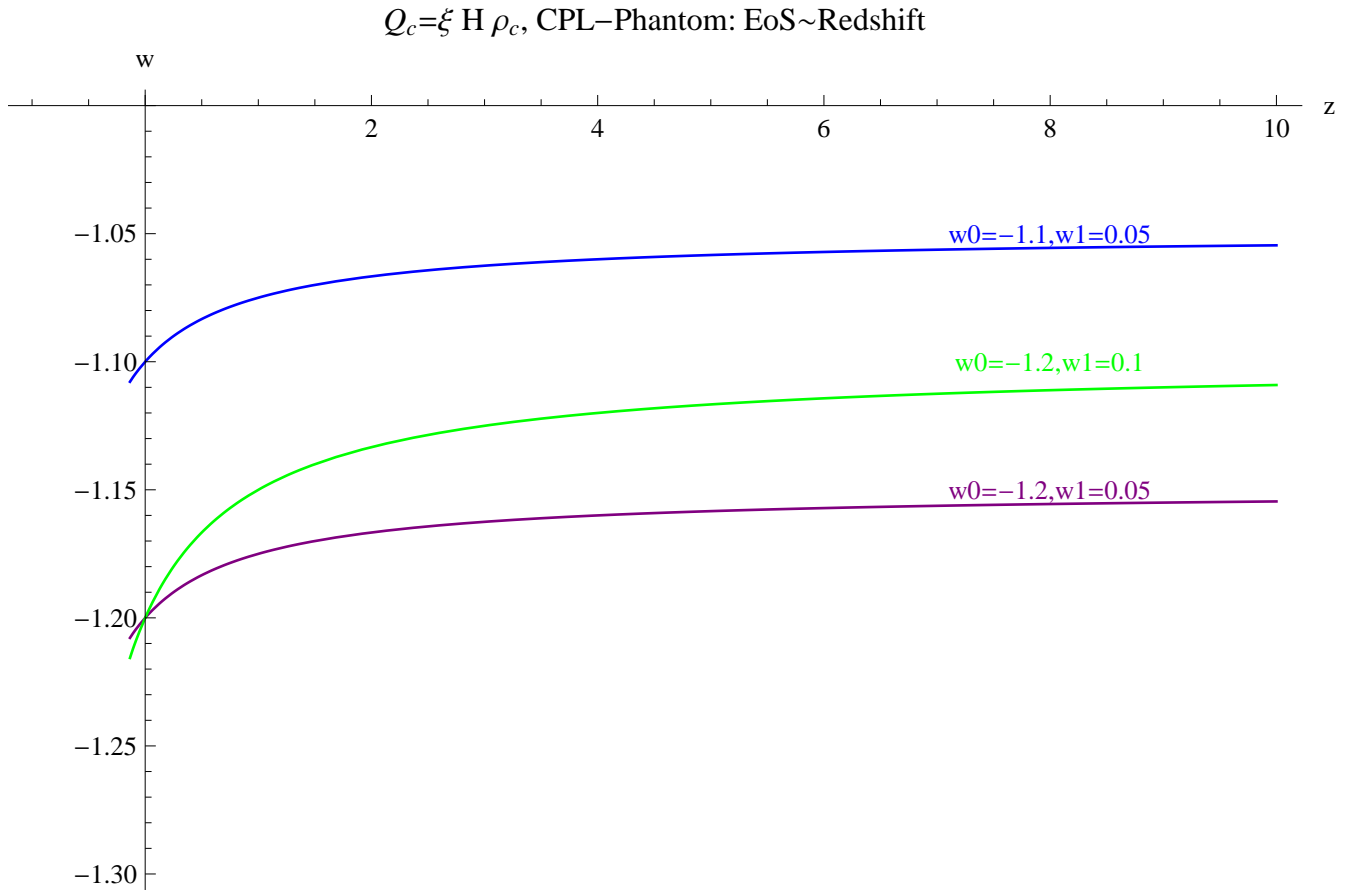


Figure 17: The EoS

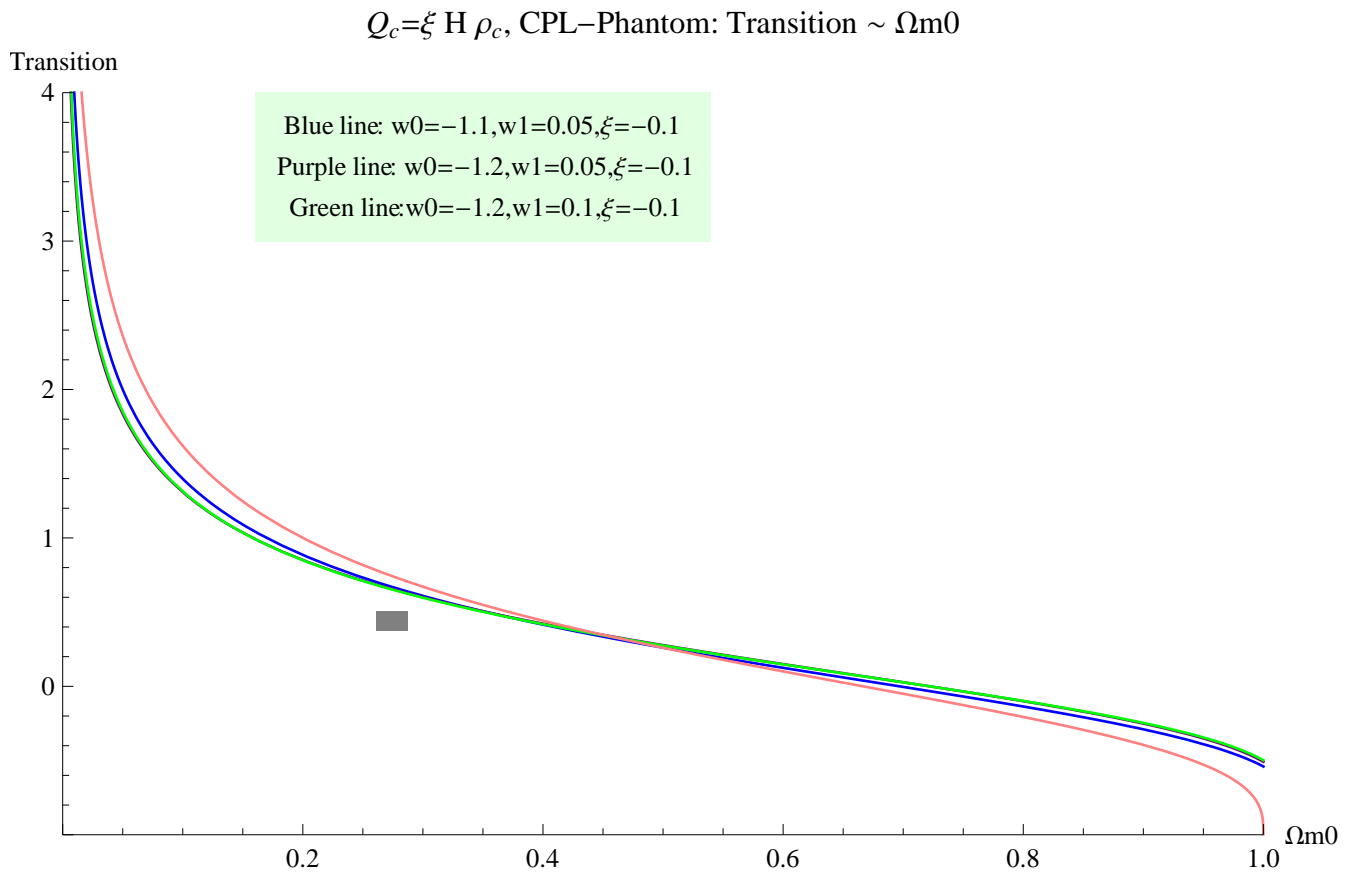


Figure 18: Transition vs Ω_{m0}

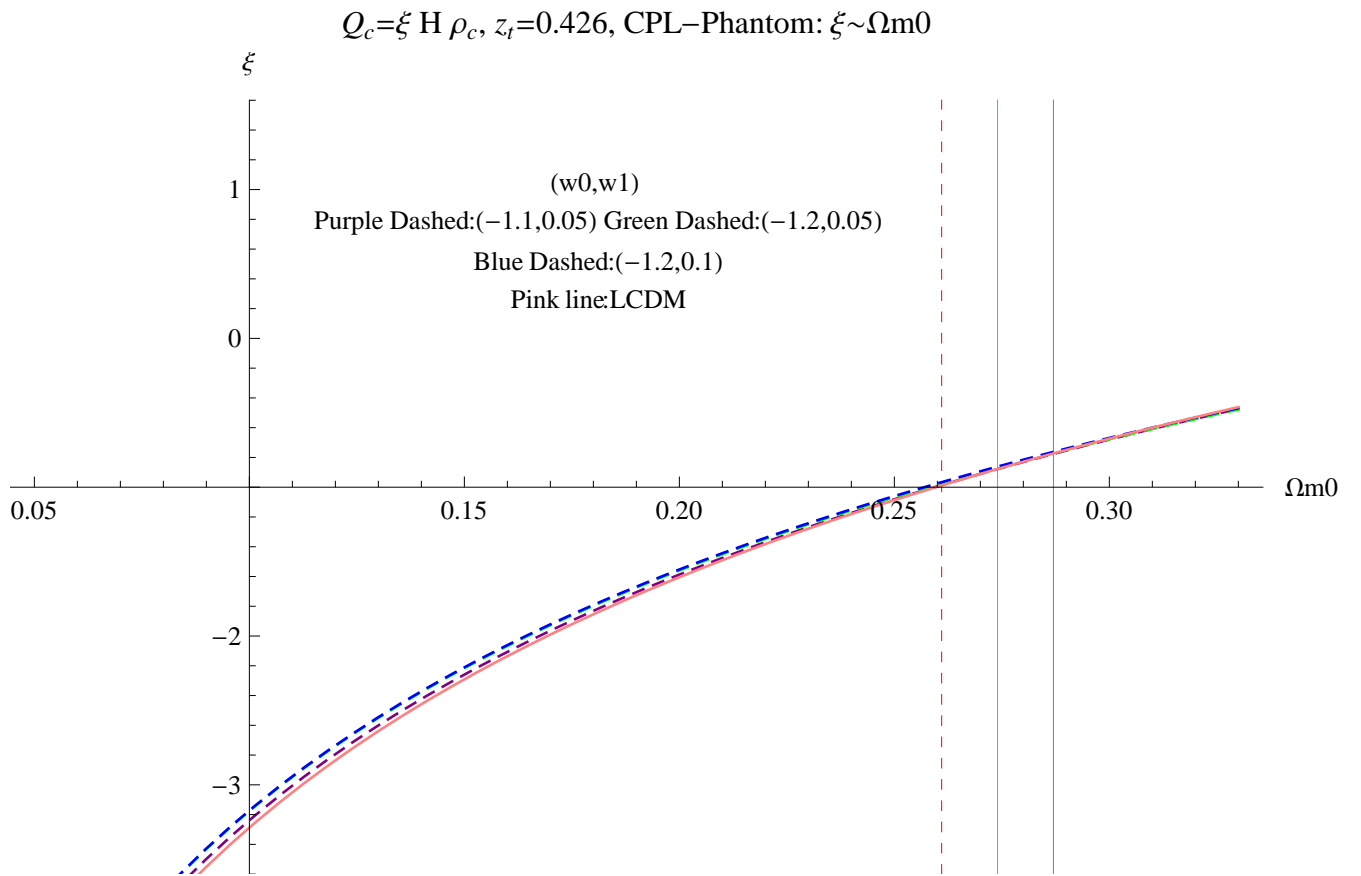
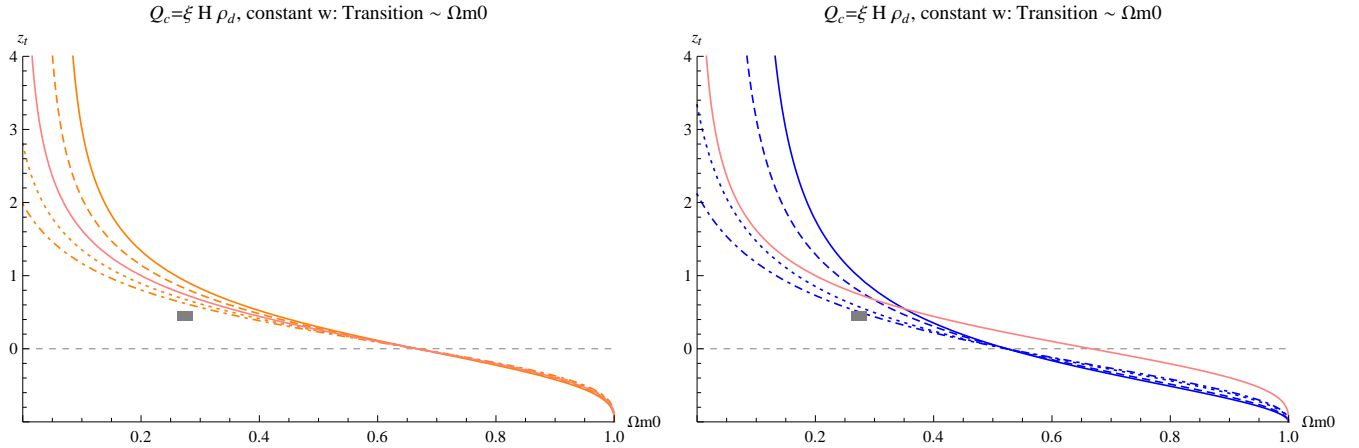
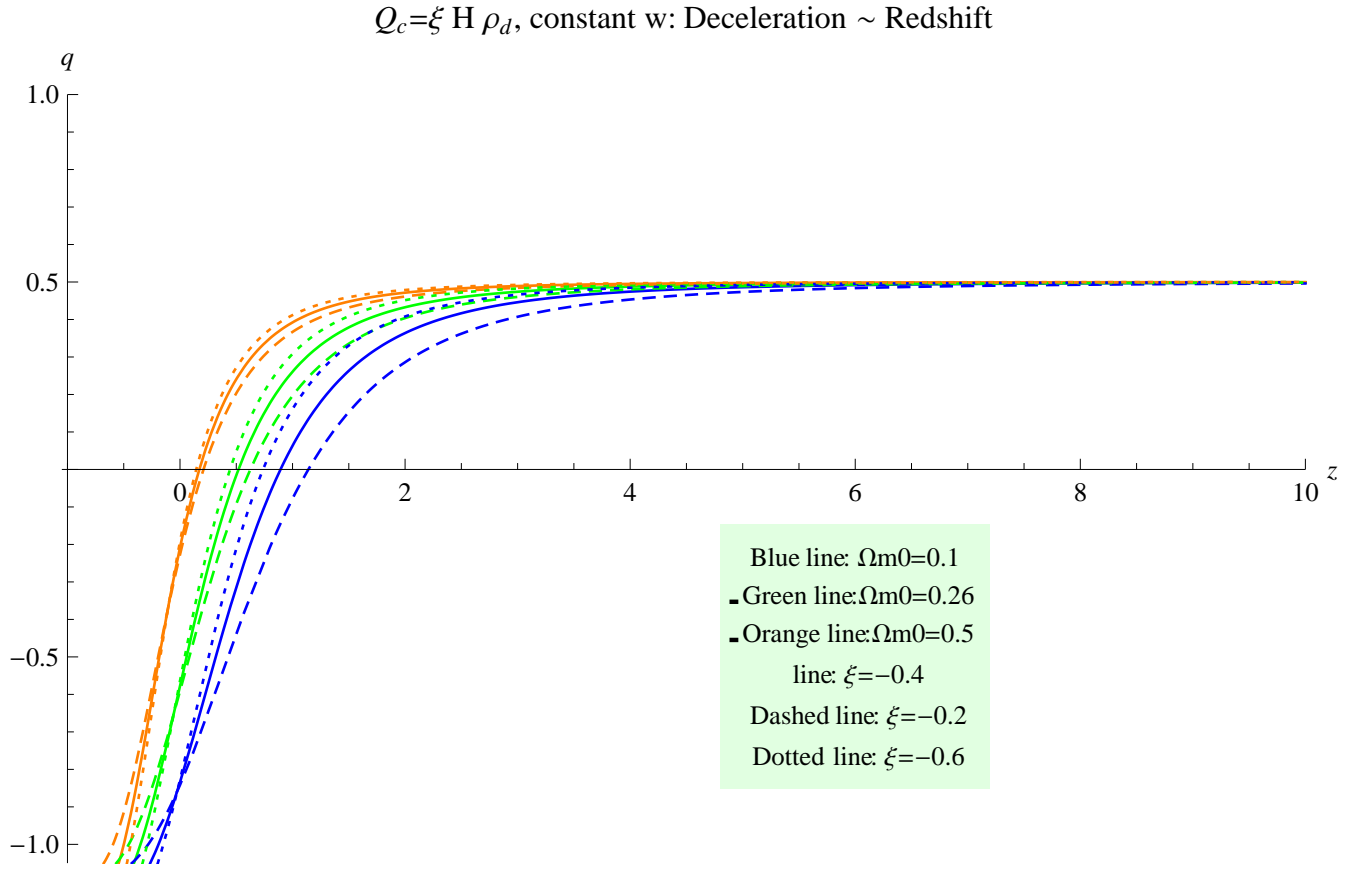


Figure 19: ξ vs Ωm_0



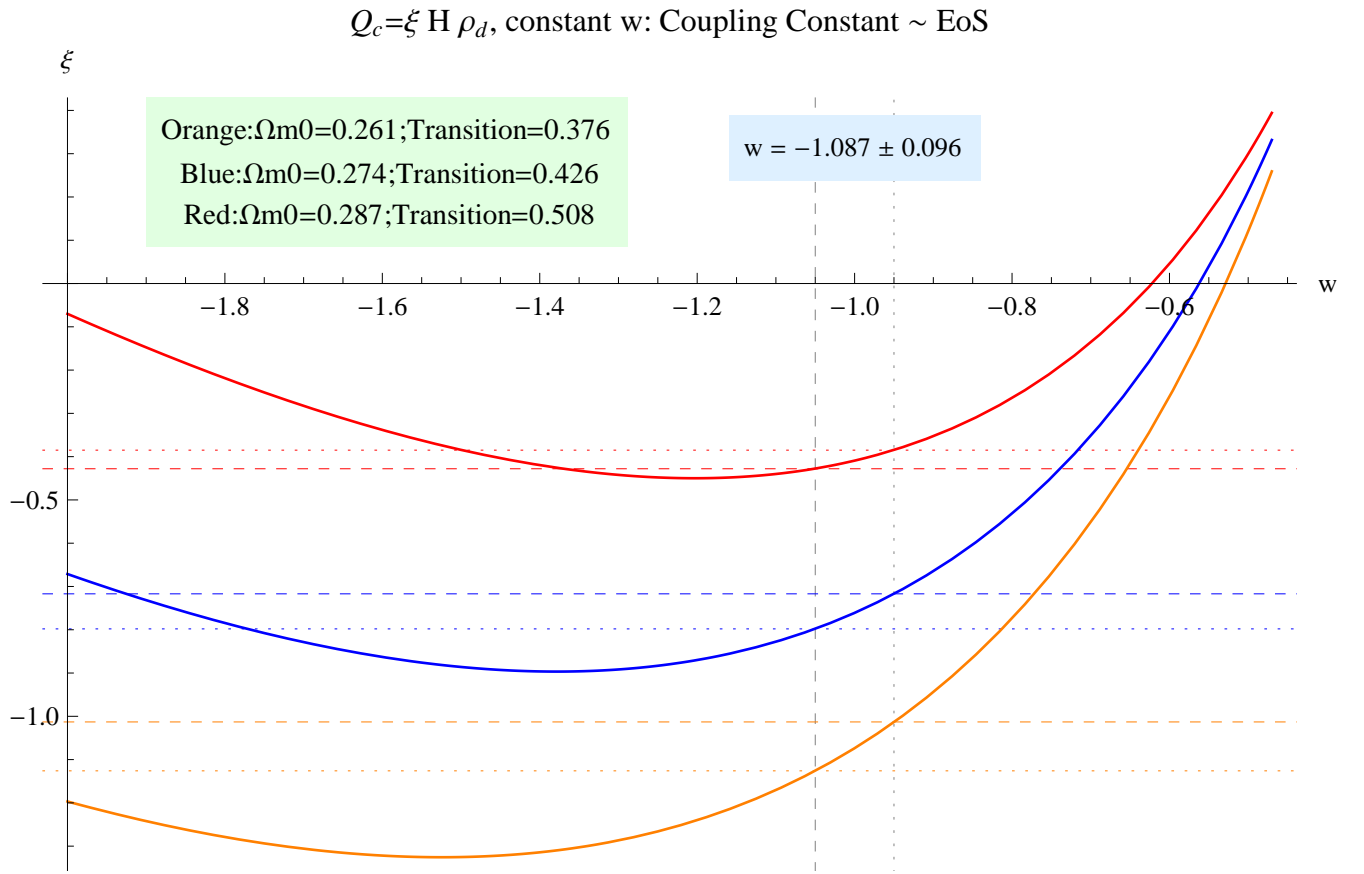


Figure 22: ξ VS w

$Q_c = \xi H \rho_d, \text{Constant } w. \text{ (Data used: Data From, 2)}$			
w	Center	Lower	Upper
-1.183	-0.864289	-1.22984	-0.449552
-1.087	-0.820486	-1.15946	-0.437339
-0.991	-0.753634	-1.06346	-0.405262

$Q_c = \xi H \rho_d, \text{constant } w: \text{Coupling Constant} \sim \text{EoS}$

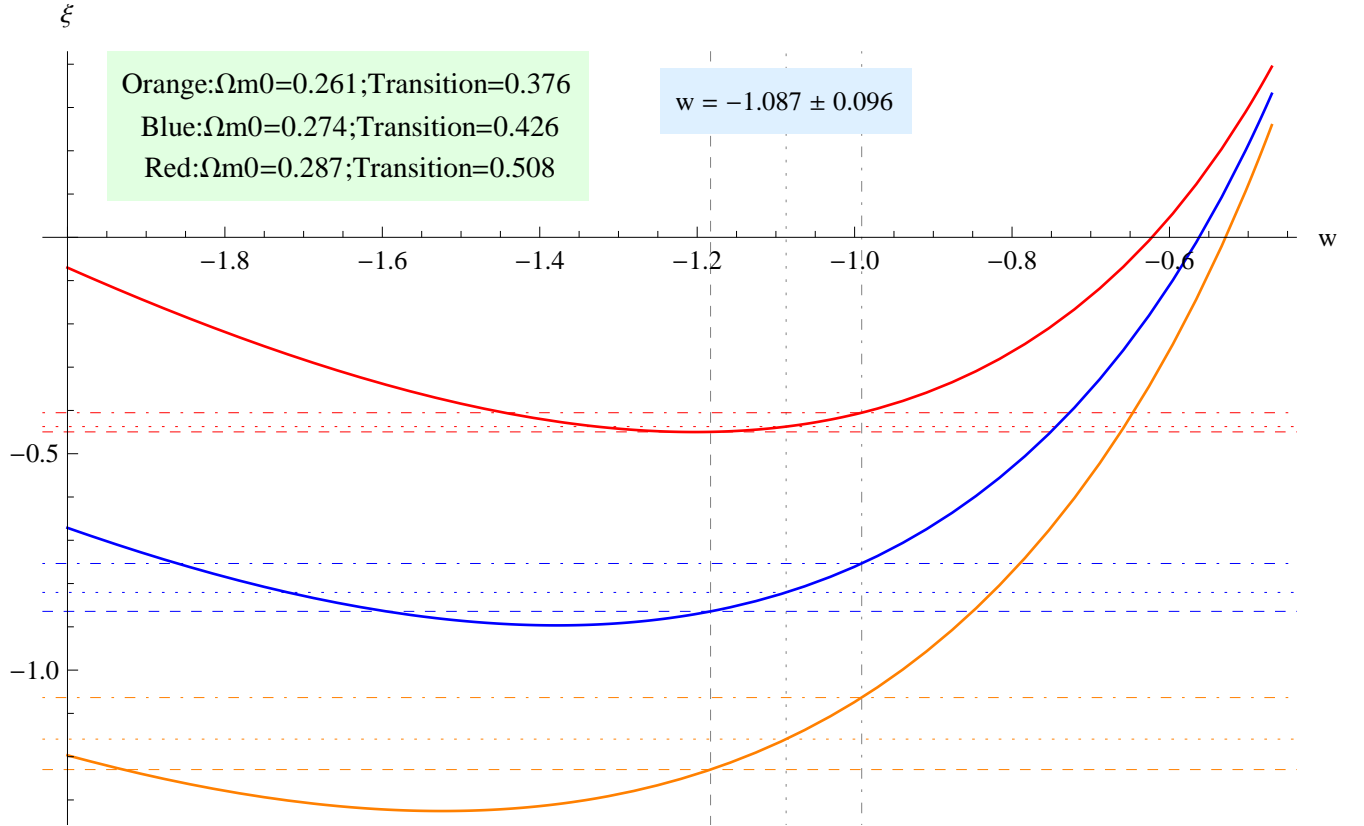


Figure 23: ξ VS w

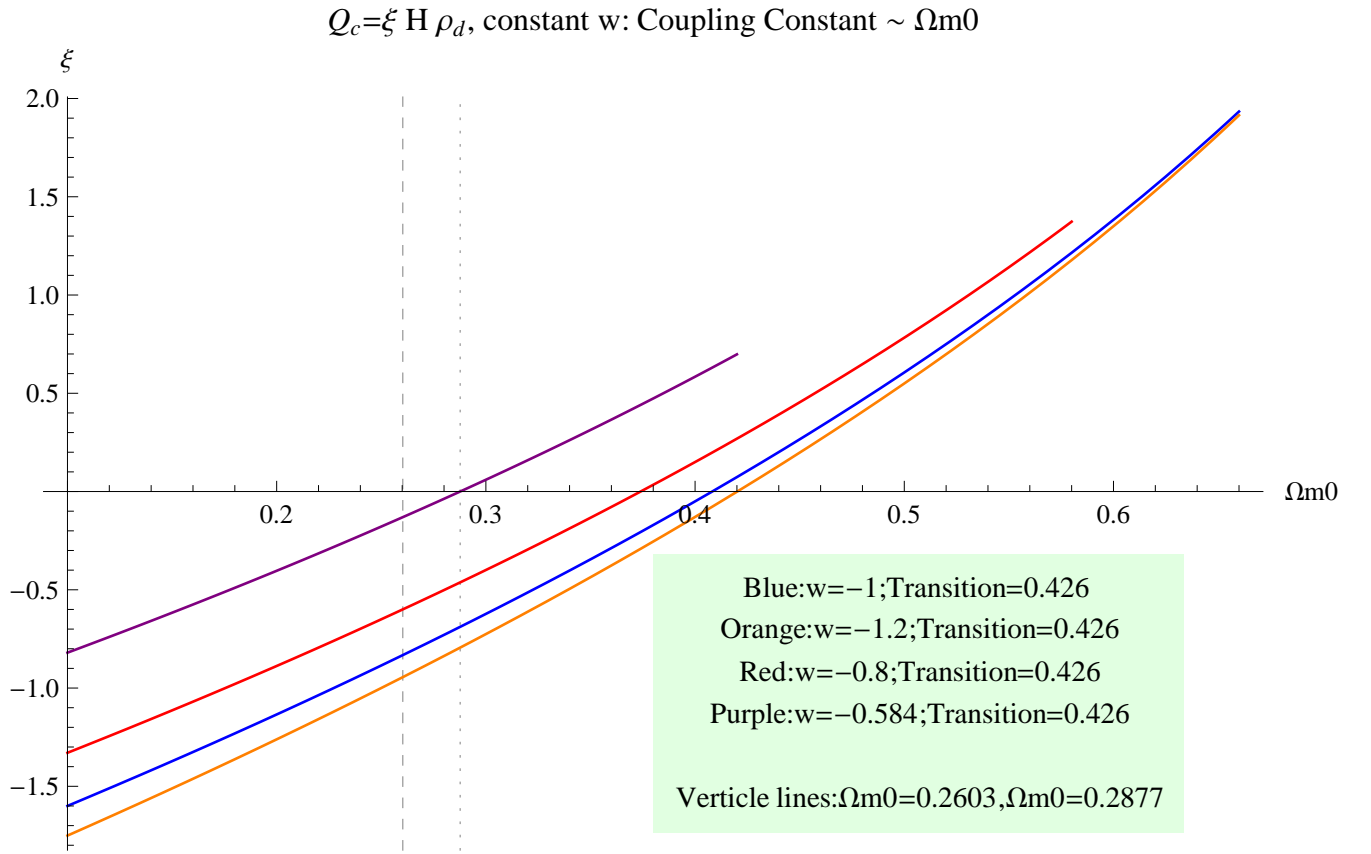


Figure 24: ξ VS Ω_{m0}

$Q_c = \xi H \rho_d$, CPL: Deceleration \sim Redshift

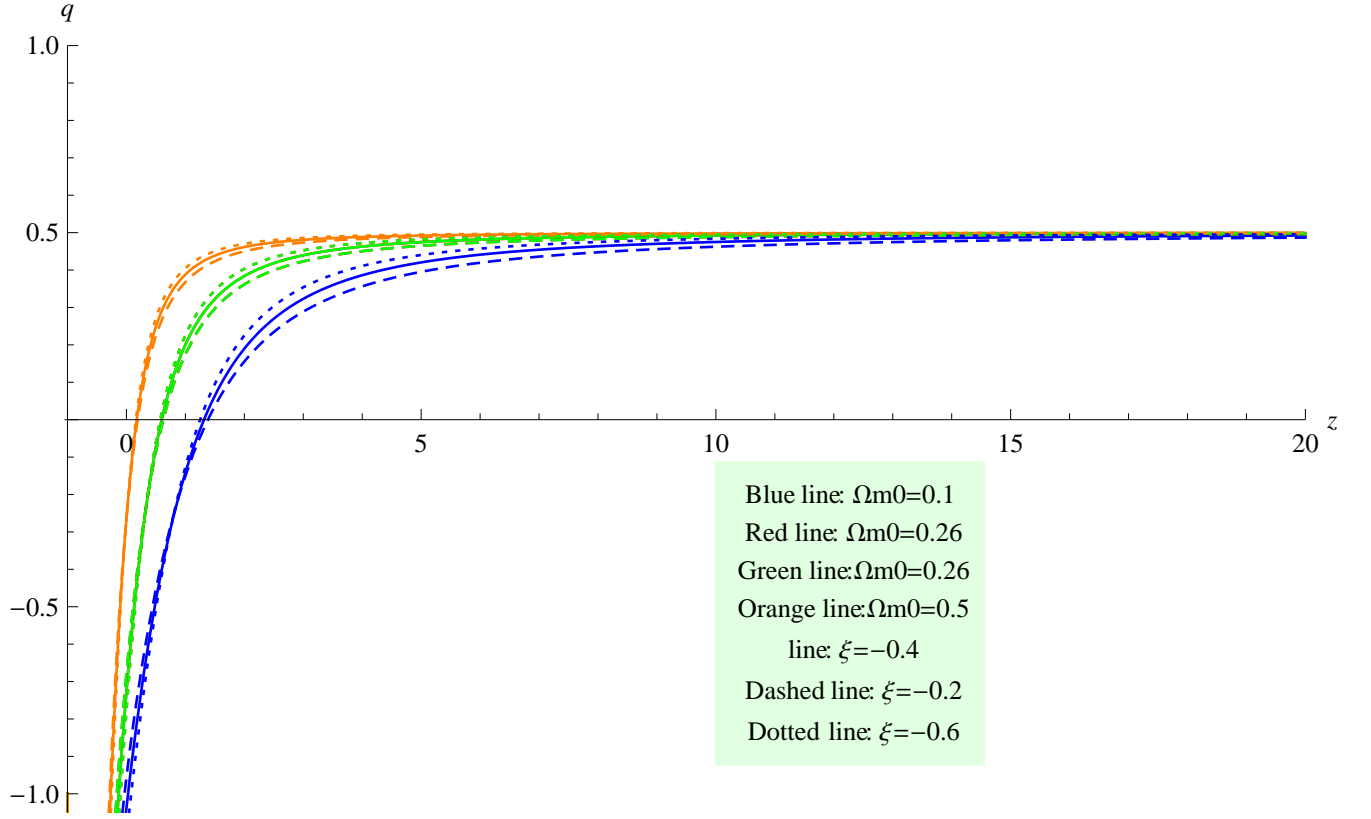


Figure 25: Deceleration parameter

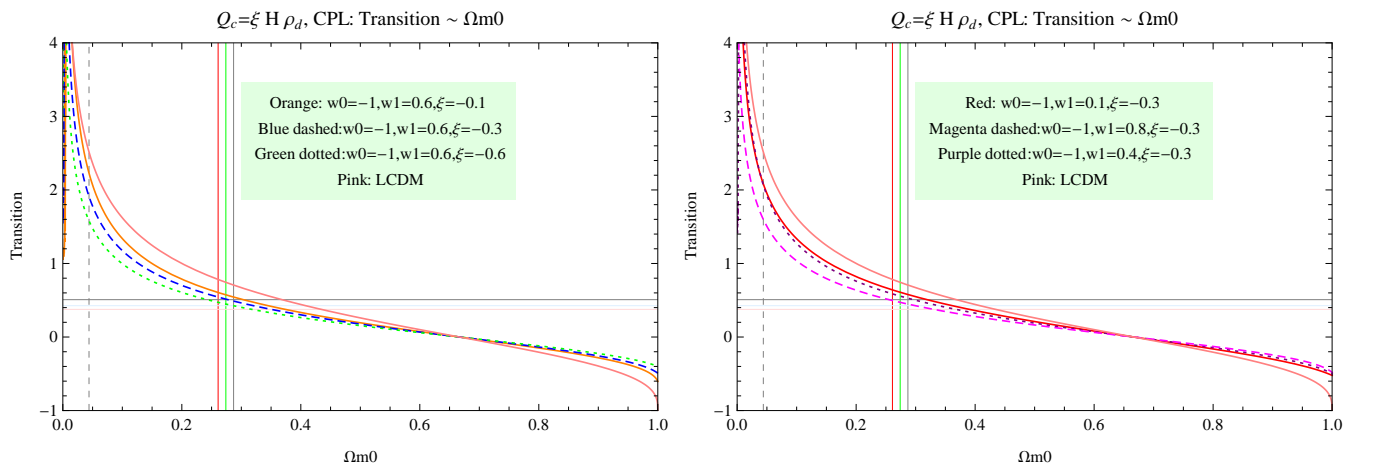


Figure 26: Transition VS Ω_{m0}

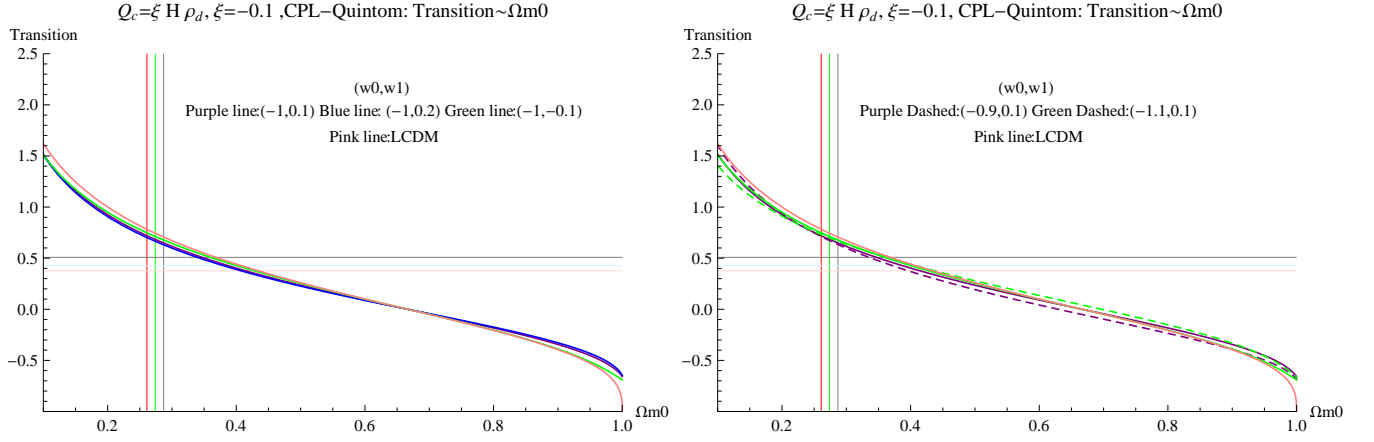


Figure 27: Transition VS Ω_{m0}

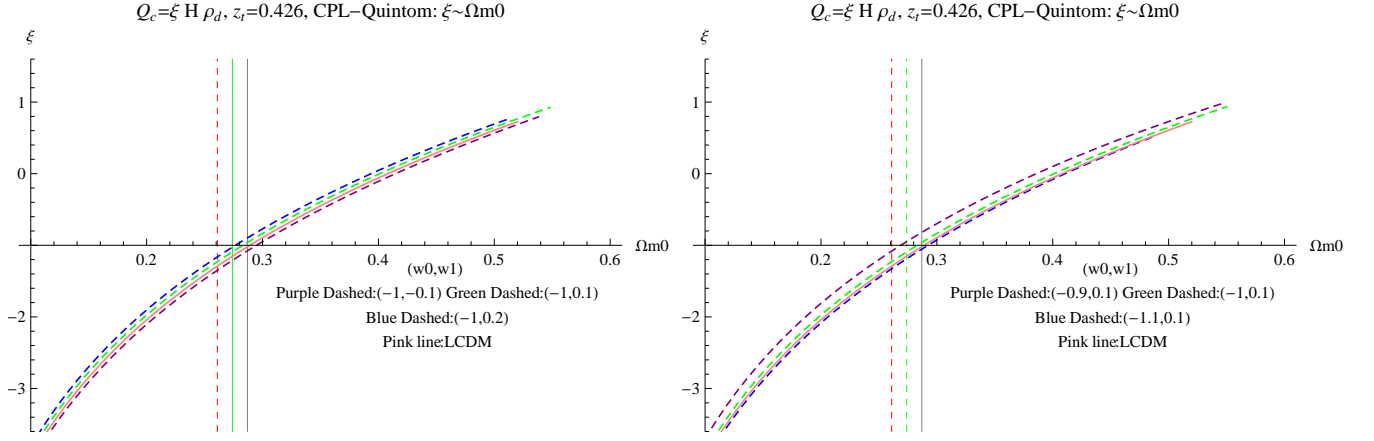


Figure 28: ξ VS Ω_{m0}

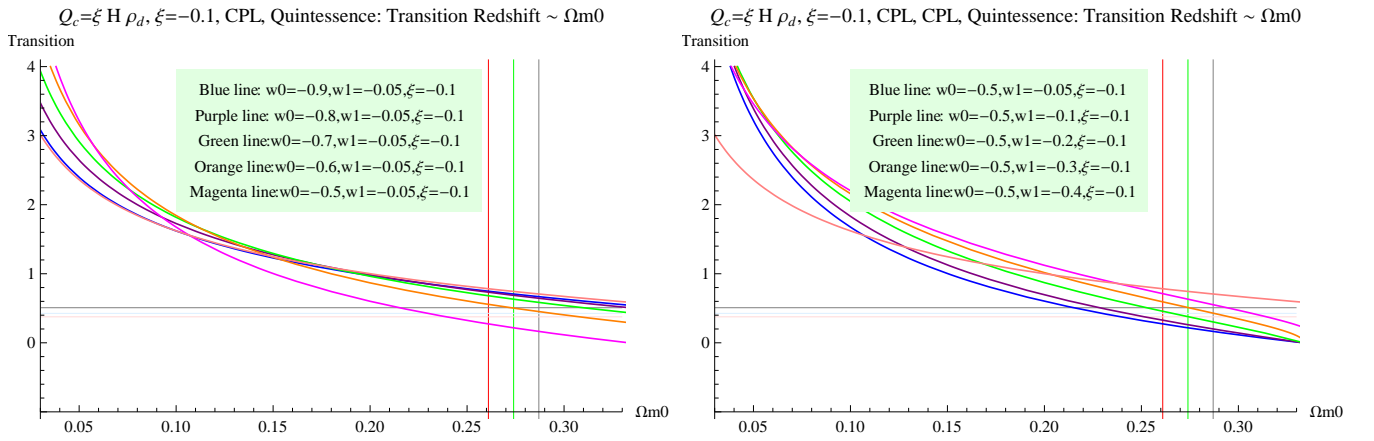


Figure 29: Transition VS Ω_{m0}

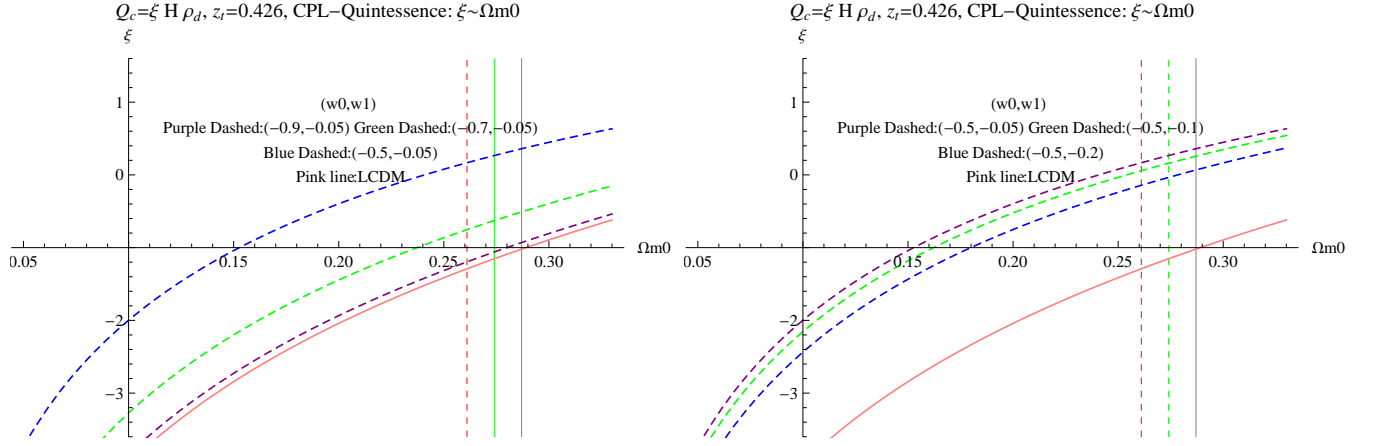


Figure 30: ξ VS Ω_{m0}

4.4.3 Phantom

(Figures ??, ??)

There is always a almost-stationary point.

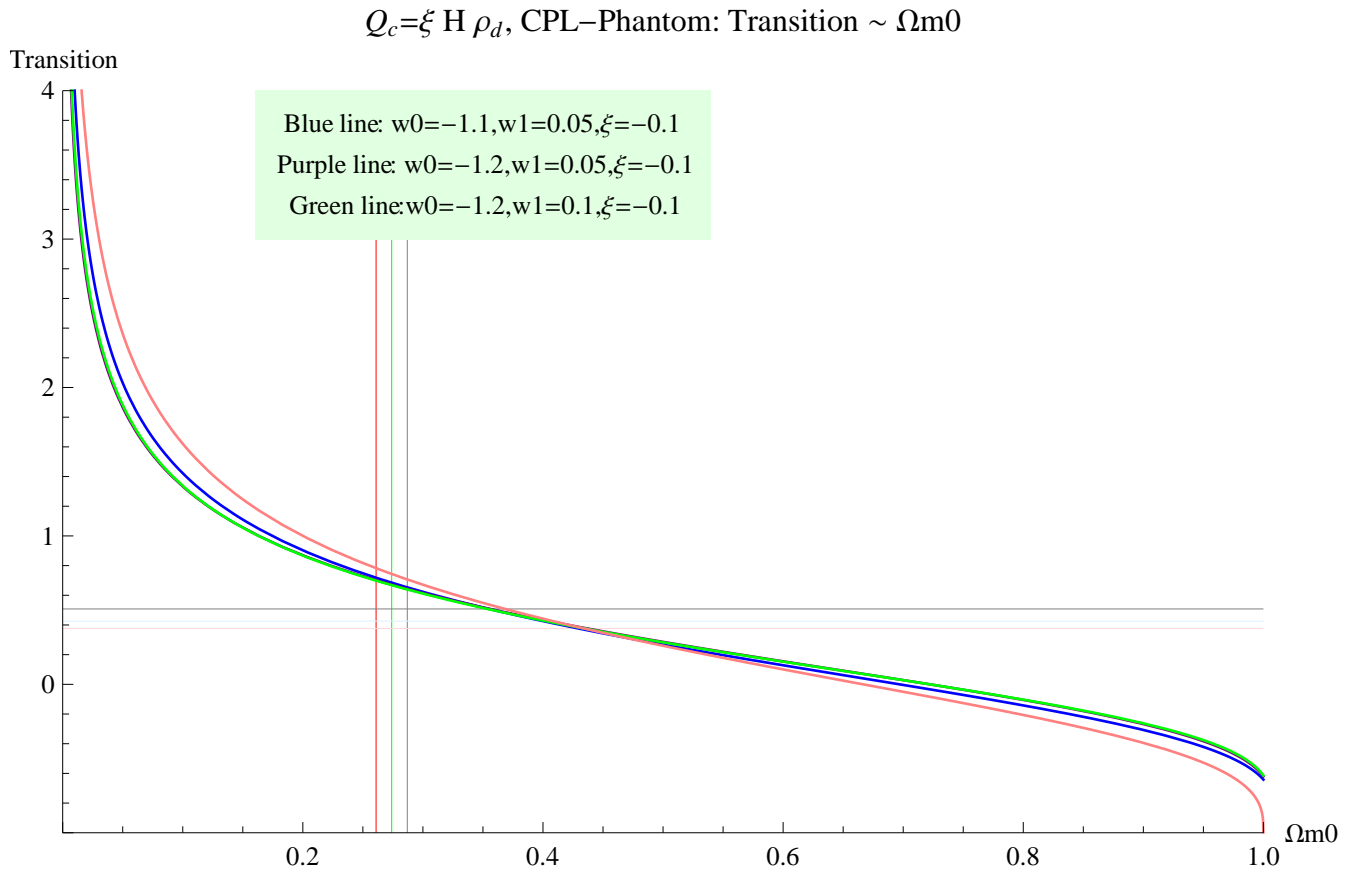


Figure 31: Transition VS Ω_{m0}

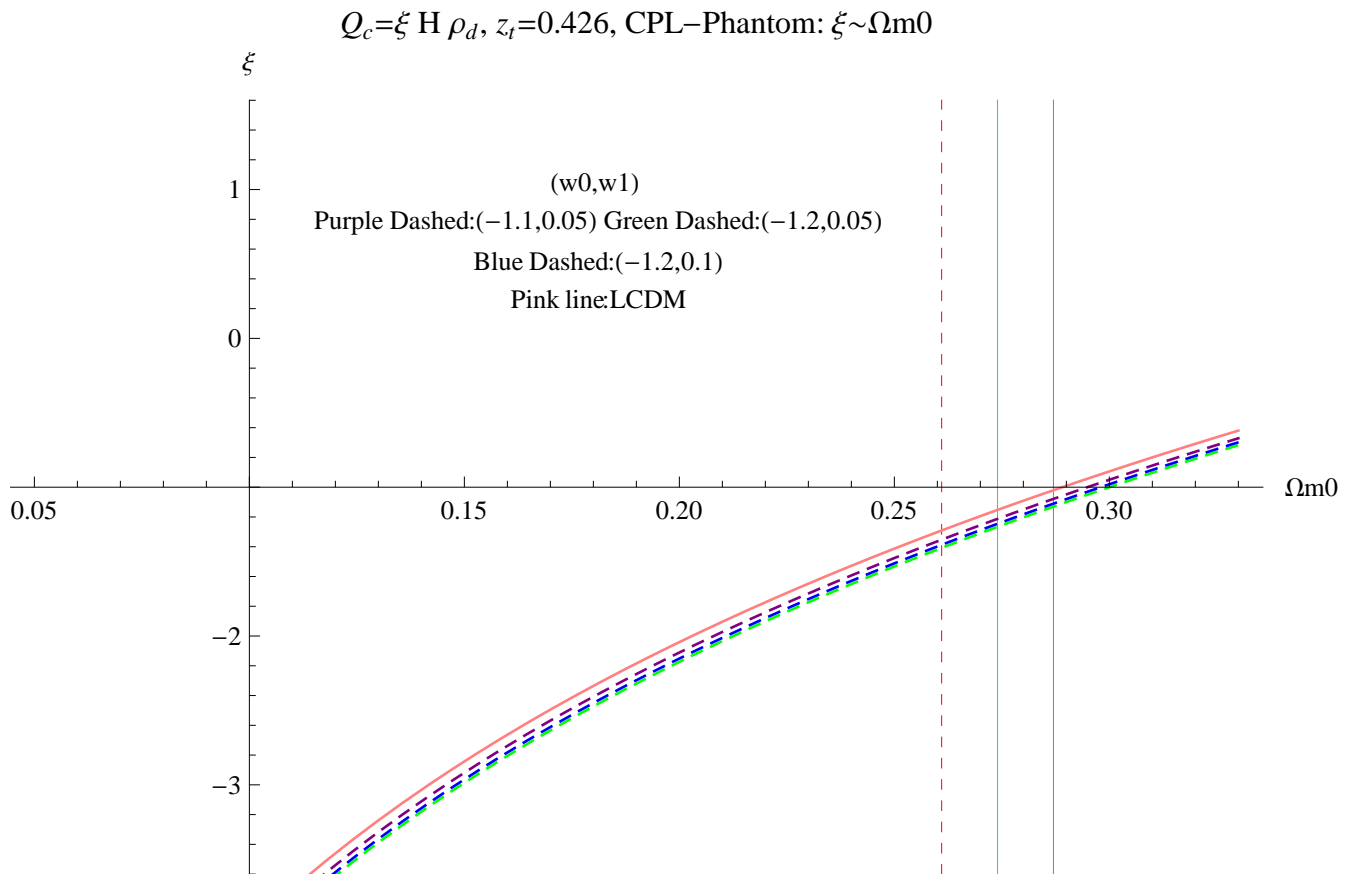


Figure 32: Transition VS Ω_{m0}