VR3Dense: Voxel Representation Learning for 3D Object Detection and Monocular Dense Depth Reconstruction

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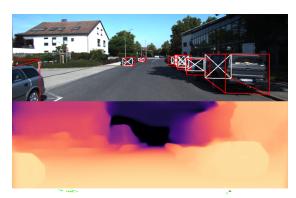
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Abstract

3D object detection and dense depth estimation are one of the most vital tasks in autonomous driving. Multiple sensor modalities can jointly attribute towards better robot perception, and to that end, we introduce a method for jointly training 3D object detection and monocular dense depth reconstruction neural networks. It takes as inputs, a LiDAR point-cloud, and a single RGB image during inference and produces object pose predictions as well as a densely reconstructed depth map. LiDAR point-cloud is converted into a set of voxels, and its features are extracted using 3D convolution layers, from which we regress object pose parameters. Corresponding RGB image features are extracted using another 2D convolutional neural network. We further use these combined features to predict a dense depth map. While our object detection is trained in a supervised manner, the depth prediction network is trained with both self-supervised and supervised loss functions. We also introduce a loss function, edge-preserving smooth loss, and show that this results in better depth estimation compared to the edge-aware smooth loss function, frequently used in depth prediction works.

1 Introduction

3D Object Detection is one of the most significant part in autonomous vehicle perception. An autonomous vehicle needs to be aware of its surrounding objects and should be capable of predicting their future trajectory. Most autonomous vehicles in their development phase today are occupied with LiDARs, Cameras, and RADARs which allow them to perceive the environment. While 2D object detection methods using cameras [Redmon *et al.*, 2016; Tan *et al.*, 2020] have matured quite a bit, it does not really capture the accurate geometry of the scene and hence does not help an autonomous vehicle plan its actions. Few recent papers have also proposed the use of monocular camera to detect object 6-DoF poses



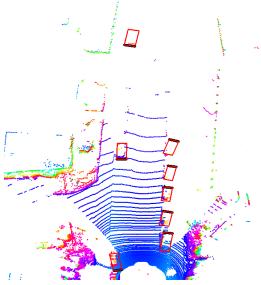


Figure 1: Joint prediction of object poses and dense depth map from a LiDAR point-cloud and an RGB image.

[Shrivastava and Chakravarty, 2021; Brazil and Liu, 2019; Qin *et al.*, 2019], however, these have proven to be inferior to LiDAR based object detection methods. LiDARs have been one of the most crucial sensors for obtaining accurate 3D scene representation, however, its high-cost and sparsity in the point-cloud data have discouraged a small set of automotive companies from utilizing it for perception tasks. Although expensive, it is irrefutable that LiDAR point-cloud provides means of obtaining the most accurate 3D geometry

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¹Code implementation available here: https://github.com/towardsautonomy/VR3Dense

of the scene.

Monocular depth estimation is another field of computer vision research that has been getting a lot of attention recently in 3D scene understanding. Obtaining pixel-wise depth map provides us with a plethora of information about the scene and helps machine understand a dense representation of the environment. A major deterrent in obtaining dense depth though is the scarcity of available public datasets and the hardships involved in generating ground-truth labels. Most available dense depth estimation datasets like NYU Depth Dataset V2 [Nathan Silberman and Fergus, 2012] uses RGB-D cameras for indoor settings, and classical computer vision techniques such as stereo matching, LiDAR points super-resolution [Uhrig et al., 2017], or LiDAR points projected onto the image plane [Guizilini et al., 2020] for the outdoor environment. This has encouraged the research community to innovate several self-supervised and semi-supervised methods for RGB image to depth map estimation [Godard et al., 2017; Guizilini et al., 2020; Amiri et al., 2019].

We combine the two streams of perception tasks and introduce a method of jointly training LiDAR point-cloud based 3D object detection and monocular image to dense depth estimation neural networks. We represent the input point-cloud as a set of non-cubic voxels, each encoding the density of points contained within, and then use a set of 3D convolution layers for extracting spatial features which are concatenated with the latent vector of RGB image to depth estimation network. We pose 3D object detection as a regression problem and regress object pose parameters along with their confidence and class probabilities from the extracted spatial features using a set of fully-connected layers. The dense depth estimation network on the other hand is an hourglass architecture with skip connections, built using 2D convolution layers. We call our method - VR3Dense, which requires point-cloud, left and right stereo images, and object pose labels for training. During inference, we only require a LiDAR point-cloud and corresponding left camera image as inputs and predict object poses along with pixel-wise dense depth map as outputs. We work with KITTI 3D object detection dataset [Geiger et al., 2012] for training and testing our method.

2 Related Work

Several LiDAR-based 3D object detection methods have proven to perform extremely well and achieve state-of-the-art results on existing dataset benchmarks. Researchers utilize various representations of point-clouds such as bird-eye view (BEV), voxels, and stixels - each with its own advantages and disadvantages. While methods such as [Li et al., 2016], and PIXOR [Yang et al., 2019] projects LiDAR point-cloud on a 2D plane and then use 2D CNN for object detection, other methods such as Vote3deep [Engelcke et al., 2017] and Voxelnet [Zhou and Tuzel, 2017] represents point-cloud as a set of 3D voxels and then use 3D convolution to extract features. These methods often employ separate heads for objectness probability prediction and pose prediction. Another stream of research such as VoxNet [Maturana and Scherer, 2015], converts a point-cloud segment into a 3D volumetric grid and then perform detection. Recently, PointNet [Qi et al., 2017a] introduced a different approach to point-representation which eliminates the need to manually structure the points in a predefined manner and was further improved by PointNet++ [Qi et al., 2017b].

Due to scantiness of paired image and depth training datasets, several self-supervised and semi-supervised techniques have been proposed. All these methods use more than one views and poses between them during training to reproject pixels across frames and compute reprojection losses which provides supervision to the network. SfMLearner [Zhou et al., 2017] requires only monocular video sequences during training. It predict poses between multi-view frames using a *Pose CNN* and predicts a depth map for the target view using Depth CNN. Other views are then warped to the target view and the reprojection loss thus computed helps both the network to be trained in an end-to-end fashion. PackNet-SfM [Guizilini et al., 2020] follows a similar path but leverages the camera's velocity when available to solve for the scale ambiguity with monocular vision. They also use 3D packing and unpacking blocks in their encoder and decoder to preserve high resolution depth decoding. Similarly, Monodepth [Godard et al., 2017] uses left and right stereo images with known baseline and exploits epipolar geometry to warp each image to the other in order to compute left-right reprojection losses along with disparity consistency loss which feeds supervisory signal to the network during training. Few other works such as [Kuznietsov et al., 2017] take a semi-supervised approach, where they also use LiDAR points projected on to the image plane to add supervision to the pixels for which a 3D point projection is available.

We take inspiration from all these work to build a 3D object detection network and a semi-supervised monocular depth estimation network. Our object detection network uses 3D convolution layers whereas our depth estimation network uses 2D convolutions; their representations are merged downstream from which our depth estimation decoder benefits and provides a better quality depth reconstruction.

3 Technical Approach

Learning representations from more than one sensor modality furnishes a richer set of information and helps solve perception tasks more accurately. Figure 2 summarizes our technical approach for joint 3D object detection and monocular depth estimation. For learning spatial representation from LiDAR point-clouds, we first encode points into a collection of noncubic voxels, P_{vr} , with each voxel encoding density of points within the occupied volume. This voxelized point-cloud is then passed to a 3D convolutional neural network for feature extraction. At the same time, corresponding left stereo camera image, I_l is passed through a U-Net [Ronneberger et al., 2015] like encoder-decoder architecture with residual blocks to produce a dense depth map, D_l . Encoder of this network encodes the RGB image into a latent vector, to which the encoded voxelized point-cloud features are concatenated before being fed to the decoder. We qualitatively and quantitatively show that this results in better depth estimation. We further use fully-connected layers to extract object pose parameter along with class probabilities from encoded voxel representations.

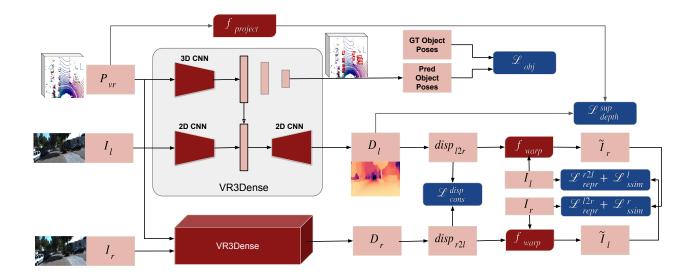


Figure 2: VR3Dense jointly learns 3D object detection from LiDAR point-cloud and dense depth estimation from corresponding monocular camera frame. 3D object detection is trained with supervision from ground-truth labels while monocular depth estimation is trained in a semi-supervised way; self-supervision from stereo image reconstruction and supervision from sparse LiDAR points projected onto the image plane. Learned feature vector from voxel representation is concatenated with the latent vector of depth estimation network which allows depth decoder to take advantage of spatial features extracted from LiDAR points.

3.1 LiDAR point-cloud based 3D Object Detection

For 3D object detection, we divide the voxelized region-ofinterest into a set of volumes, each tasked with predicting an objectness score and the corresponding object pose. Since, a prior knowledge of the environment is known (e.g. cars mostly drive on the road - same plane as ego vehicle), we assume the roll and pitch to be zero. Additionally, class probabilities are also predicted as a one-hot vector for object classification - $(p_{class1}, p_{class2}, ..., p_{classN})$. This results in the predicted output pose vector to be of size $M \times (9 + N)$ for a maximum of M objects with prediction for each object corresponding to (confidence, x_{center} , y_{center} , z_{center} , length, width, height, $cos(\theta)$, $sin(\theta)$, p_{class1} , p_{class2} , ..., p_{classN}), where θ is yaw angle of the object relative to ego-vehicle. We minimize L2 loss for computing $x_{center}, y_{center}, z_{center}$, $length, width, height, cos(\theta), and sin(\theta)$ errors as shown in equation 1 and optimize for their minimization using Adam optimizer.

$$\mathcal{L}_{pose} = \mathbb{1}_{obj} \frac{\sum ||y_{pose} - \hat{y}_{pose}||_2}{n_{true_obj} + \epsilon}$$
 (1)

Where, $pose \in [x_{center}, y_{center}, z_{center}, length, width, height, <math>cos(\theta), sin(\theta)]$.

For confidence loss computation, we again use L2-norm, but weigh them based on number of positive and negative objects in ground-truth labels as given in equation 2.

$$\mathcal{L}_{conf} = \mathbb{1}_{obj} \frac{\sum ||y_{conf} - \hat{y}_{conf}||_2}{n_{true_obj} + \epsilon} + (1 - \mathbb{1}_{obj}) \frac{\sum ||y_{conf} - \hat{y}_{conf}||_2}{n_{false_obj} + \epsilon}$$
(2)

We use cross-entropy loss for the optimization of object class prediction (\mathcal{L}_{class}). Additionally, we attempt to maximize generalized-intersection-over-union (GIoU) [Rezatofighi *et al.*, 2019] directly during the optimization process by minimizing the GIoU loss given in equation 3.

$$\mathcal{L}_{giou} = ||GIoU(y, \hat{y}) - \mathbb{1}_{obj}||_2 \tag{3}$$

In equations 1, 2, and 3, $\mathbb{1}_{obj}$ is 1 if an object exist in the ground-truth label vector, and 0 otherwise. Our complete object detection loss function is a weighted sum of these individual loss terms and is given in equation 4, where λ_n are loss weights.

$$\mathcal{L}_{obj} = \lambda_1 \mathcal{L}_{conf} + \lambda_2 \mathcal{L}_{pose} + \lambda_3 \mathcal{L}_{class} + \lambda_4 \mathcal{L}_{qiou}$$
 (4)

3.2 Semi-Supervised Monocular Depth Estimation

[Kuznietsov et al., 2017] and [Amiri et al., 2019] showed that semi-supervised monocular depth estimation outperforms both supervised and unsupervised methods. Following these papers, we train our depth estimation network with supervision from LiDAR points projected onto the image plane in addition to self-supervision from stereo image reconstruction losses. Unlike other papers however, we attempt to directly predict a higher resolution depth map rather than coarse-to-fine disparity or inverse depth. We notice that the loss functions used in most methods alone are not sufficient for producing high-resolution images with sharp edges around object silhouettes. State-of-the-art monocular depth estimation methods use edge-aware smooth loss as given in equation 5, which penalizes gradients in depth map if a corresponding gradient does not exist in the RGB image. It however, does not penalize the network if predicted depth map is too smooth, even across object boundaries - which is precisely the reason for the predicted depth map not being sharp at full resolution when a coarse-to-fine approach is not taken. To this end, we propose a loss function called *edge persever*ance loss, which promotes edges in depth map proportional to the edges in RGB image and is given in equation 6. Since the magnitude of depth gradients and image gradients might not be of the same scale, we attempt to learn this proportionality parameter (α_0 and α_1 in equation 6). We use a combination thereof which we call - edge-preserving smooth loss, during our monocular depth estimation training and is given in equation 7.

$$\mathcal{L}_{smooth} = \frac{1}{N} \sum_{n \in N} |\partial_x \hat{D}| e^{-|\partial_x I|} + |\partial_y \hat{D}| e^{-|\partial_y I|}$$
 (5)

Where, \hat{D} is the predicted depth map, I is the input image, and N is total number of pixels.

$$\mathcal{L}_{ep} = \frac{1}{N} \sum_{x \in N} \frac{e^{|\partial_x \hat{D} - \alpha_0 \partial_x I|} + e^{|\partial_y \hat{D} - \alpha_1 \partial_y I|}}{2} - 1 \qquad (6)$$

$$\mathcal{L}_{eps} = \beta_{edge} \mathcal{L}_{ep} + (1 - \beta_{edge}) \mathcal{L}_{smooth}$$
 (7)

 $\mathcal{L}_{eps} = \beta_{edge} \mathcal{L}_{ep} + (1 - \beta_{edge}) \mathcal{L}_{smooth} \tag{7}$ In equation 6, $\alpha_0 = tanh(W_0 \partial_x I + b_0)$ and $\alpha_1 = tanh(W_1 \partial_x I + b_1)$, where W_n and b_n are learnable parameters for $n \in [0,1]$. β_{edge} shown in equation 7 is a hyperparameter and we set it to 0.5 during our experiments.

For self-supervision, we use stereo image reconstruction to compute reprojection losses by warping left stereo image (I_l) to right (I_r) and right image (I_r) to left (I_l) . We do this by first converting predicted depth from the left image (D_l) into disparity $(disp_{l2r})$ and then use PyTorch's [Paszke *et al.*, 2019] differentiable bilinear sampling (f_{warp}) to warp the left stereo image to right as shown in equation 8.

$$disp_{l2r} = \frac{fb}{D_l}$$

$$\tilde{I}_r = f_{warp}(I_l, disp_{l2r})$$
(8)

Similarly, we predict the depth map (D_r) for right stereo image and then warp it to the left using right-to-left disparity, which can be computed as $disp_{r2l} = -fb/D_r$. Stereo image reprojection losses are then computed using equation 9, where \mathcal{M}_{l2r} and \mathcal{M}_{r2l} represents a mask of all *ones* warped from left-to-right using $disp_{l2r}$, and right-to-left using $disp_{r2l}$ respectively; and \odot represents an element-wise multiplication. One could also incorporate an additional reprojection loss which measures the consistency between left image and right-to-left warped image using the negative of $disp_{l2r}$, and vice versa.

$$\mathcal{L}_{repr}^{l2r} = \frac{1}{N} \sum_{n \in N} \mathcal{M}_{l2r} \odot Huber(I_r, \tilde{I}_r)$$

$$\mathcal{L}_{repr}^{r2l} = \frac{1}{N} \sum_{n \in N} \mathcal{M}_{r2l} \odot Huber(I_l, \tilde{I}_l)$$

$$\mathcal{L}_{repr} = \frac{\mathcal{L}_{repr}^{l2r} + \mathcal{L}_{repr}^{r2l}}{2}$$
(9)

We also enforce consistency between the disparity computed from left and right images and is given by $\mathcal{L}_{cons}^{disp}$ in equation 10. We also compute structure similarity index between one image and its reconstructed version from the other image as shown in equation 11 which gets incorporated into the appearance matching loss, \mathcal{L}_{app} . Furthermore, we use Huber-norm instead of commonly used L1-norm for computing reprojection and consistency errors - we find it to converge faster in our experiments.

$$\mathcal{L}_{cons}^{disp} = \frac{1}{N} \sum_{r \in N} Huber(disp_{l2r}, -disp_{r2l})$$
 (10)

$$\mathcal{L}_{ssim} = \frac{1}{N} \sum_{n \in N} \frac{1}{4} \left(2 - \left[SSIM(I_l, \tilde{I}_l) + SSIM(I_r, \tilde{I}_r) \right] \right)$$

$$\mathcal{L}_{app} = \alpha_{ssim} \mathcal{L}_{ssim} + (1 - \alpha_{ssim}) \mathcal{L}_{repr}$$
(11)

Loss functions given in equations 7, 9, 10, and 11 together devise our unsupervised loss function $\mathcal{L}_{denth}^{unsup}$.

$$\mathcal{L}_{depth}^{unsup} = \lambda_5 \mathcal{L}_{eps} + \lambda_6 \mathcal{L}_{repr} + \lambda_7 \mathcal{L}_{cons}^{disp} + \lambda_8 \mathcal{L}_{app} \quad (12)$$

Semi-supervision in our depth estimation network comes from the 2D projection of LiDAR points. We use an L2 loss between our depth prediction and the projected LiDAR points as given in equation 13, where P represents LiDAR points, $f_{project}()$ is a 2D projection function which projects LiDAR point-cloud onto the left camera image plane, K is the number points projected within the image boundary, and \mathcal{M}_{proj} is a mask which is 1 at pixel locations for which we have a corresponding projected LiDAR point available and 0 other-

$$\mathcal{L}_{depth}^{sup} = \lambda_9 \frac{1}{K} \sum_{k \in K} \mathcal{M}_{proj} \odot || f_{project}(P) - D_l ||_2 \quad (13)$$

We also find that the supervised loss, $\mathcal{L}^{sup}_{depth}$, is helpful during initial parts of the training for faster convergence but does not help much later in the training process. Hence, we use a decay rate of 0.01 for this loss during training.

Experimental Section

For encoding the LiDAR point-cloud into a set of voxels, we take the points within a region-of-interest (0.0 to 70.0 meters in x-dimension, -25.0 to 25.0 meters in y-dimension, and -2.5 to 1.0 meters in z-direction) and convert them into $256 \times 256 \times 16$ non-cubic voxels, where each voxel also encode the number of points within its volume. In our coordinate convention, x points ahead, y points to the left of the ego-vehicle, and z points up. For the purpose of predicting object presence, their poses, and the classification one-hot vector, we further divide our voxelized space into xy grids of size 16x16, and allow each grid to predict up to 1 object. Images are resized to a resolution of 512×256 before passing them through the network. Our predicted depth resolution is also of the same resolution, and we up-sample it to full resolution using nearest neighbor interpolation before computing losses for depth estimation.

4.1 KITTI Dataset

We use KITTI 3D object training dataset [Geiger et al., 2012] to train both 3D object detection and dense depth reconstruction. This dataset contains 7481 training samples and 7518 testing samples (test split). Following [Shi et al., 2019], we divide the training samples into train split (3712 samples) and val split (3769 samples) for evaluation of our object detection results. For our depth estimation training, we use training dataset of 7518 samples, and the entire object testing dataset with 7518 samples for evaluation.

4.2 3D Object Detection

As summarized in table 1, our evaluation uses *mean average precision* with 40-recall points. For an IOU of 0.7, our method does not perform as well as state-of-the-art methods. For lower IOU however, (0.3, and 0.7), our method achieves high mAP. This illustrates that VR3Dense predictions are accurate in terms of predicting object location, however it lacks the ability of predicting a very tight object boundary and orientation. We hypothesize that, since we use a sparse encoding of point-cloud, the network is not able to find accurate object corners. This issue can be alleviated to some extent by encoding some scene prior into the network such as anchor boxes - and will be the subject of our future work.

Table 1: Performance on the KITTI val split set with mAP calculated by 40 recall positions for car class. mAP_x identify the Mean Average Precision (mAP) for a 3D IOU threshold of x. Higher is better.

Method	mAP.3	mAP.5	mAP.7
[Zhou and Tuzel, 2017] [Shi <i>et al.</i> , 2019]	-	-	70.1
[Shi et al., 2019]	-	-	74.8
[Shi et al., 2020]	-	-	85.5
Ours	96.1	85.3	36.2

4.3 Semi-Supervised Monocular Depth Estimation

For our depth estimation evaluation, we use $Abs\ Rel,\ Sq\ Rel,\ RMSE,\ RMSE\ log,\ \delta<1.25,\ \delta<1.25^2,\ and\ \delta<1.25^3$ to compute performance metrics considering the LiDAR points projected onto image plane as ground-truth. For depth estimation, we split the KITTI 3D object detection *training* dataset into $90\%\ train$ and $10\%\ val$ split. Quantitative results of our semi-supervised monocular depth estimation is summarized in table 2.

4.4 Joint training of 3D object detection and monocular depth estimation

We train our model with batch size of 8, learning rate of $1.0e^{-4}$, and Adam optimizer for training loss minimization, on a PC with i9 10850K processor and a single NVIDIA RTX 3090 GPU which takes about 0.92 seconds per step. With the KITTI object *training* dataset split into 90% *train* and 10% *validation* samples, one epoch during training takes about 13 minutes. Our complete network contains about 363.57M trainable parameters and we train them for 100 epochs with

early stop, which takes about 22 hours to train. During inference, VR3Dense runs at about 141.1fps on the same hardware. Figure 3 shows few qualitative samples of VR3Dense prediction when tested on KITTI raw dataset [Geiger et al., 2013].

4.5 Ablation Study

We study the effect of (a) adding supervision from LiDAR points, (b) replacing the commonly used edge-aware smooth loss with our edge-preserving smooth loss, \mathcal{L}_{eps} , and (c) concatenating the feature vector learnt from voxel representation with the latent vector of monocular depth estimation network; and we find that each of those contribute towards a better performance. We summarize these evaluations in table 3. For this evaluation, we only consider a subset of KITTI object training dataset, where we randomly select a total of 1100 frames and then divide them into 900 train, 100 validation, and 100 test samples. We then train our network with each of these configuration listed in table 3 for 100 epochs and notice a clear upward trend. Baseline model in the evaluations refer to our model with only *unsupervised* loss, and as is evident from table 3, our model with an added supervision from Li-DAR points along with the edge-preserving smooth loss, and voxel feature concatenation with RGB-to-depth *latent vector*, provides the best results.

5 Conclusion

VR3Dense allows joint training of LiDAR point-cloud based 3D object detection and monocular depth estimation. We use 3D convolution layers for extracting spatial features from voxel representation of point-cloud and 2D convolution layers for extracting image features. Additionally, we concatenate the flattened spatial features with the latent vector of our RGB-to-depth encoder-decoder architecture and we show that it achieves a better performance compared to our baseline. While our object detection network is trained in a supervised way, we take a semi-supervised approach for depth estimation and further show that adding supervision from the 2D projection of LiDAR points helps the network converge faster. Lastly, we introduce a loss function, edge-preserving smooth loss, which helps the network produce a sharper depth map with higher level of details, even when a pyramidal structure is not present in the depth decoder for coarse-to-fine reconstruction of dense depth maps.

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Table 2: Monocular Depth Estimation results on KITTI object *test* dataset. Evaluations are done on the pixels for which we have projected points from LiDAR available.

Method	Range	Abs Rel	Sq Rel	RMSE	RMSE log	$\delta < 1.25$	$\delta < 1.25^2$	$\delta < 1.25^3$
	Lower is better			Higher is better				
[Zhou et al., 2017]	0-50m	0.201	1.391	5.181	0.264	0.696	0.900	0.966
[Garg et al., 2016]	0-50m	0.169	1.080	5.104	0.273	0.740	0.904	0.962
[Godard et al., 2017]	0-50m	0.140	0.976	4.471	0.232	0.818	0.931	0.969
[Kuznietsov et al., 2017]	1-50m	_	_	3.518	0.179	0.875	0.964	0.988
[Amiri et al., 2019]	0-80m	0.096	0.552	3.995	0.152	0.892	0.972	0.992
Ours	0-30m	0.214432	3.724554	5.561154	0.287028	0.788234	0.901136	0.950242
Ours	0-50m	0.217422	3.775980	6.507308	0.296695	0.769214	0.893053	0.946789
Ours	0-70m	0.219240	3.859928	7.164907	0.302273	0.760768	0.888690	0.944800

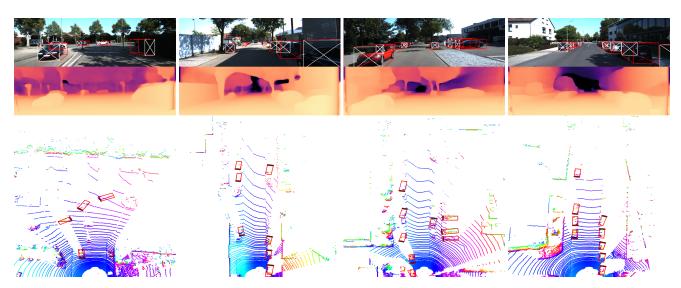


Figure 3: Qualitative results for joint LiDAR point-cloud based object detection and monocular depth prediction. Top row: Predicted 3D oriented bounding-boxes projected on left camera image plane, Middle row: Predicted dense depth map, Bottom row: Bird-eye-view of the predicted 3D oriented bounding-boxes overlayed on orthographic projection of LiDAR point-clouds (point-cloud is color-coded based on the height of each point).

Table 3: Ablation Study for Monocular Depth Estimation on a subset of KITTI object dataset. A subset of 1100 data samples were obtained randomly from the *training* dataset and divided into 900 *training*, 100 *validation*, and 100 *testing* samples. valuations are done on the pixels for which we have projected points from LiDAR available. L2: L2 loss between prediction and projected LiDAR points, S: Edge-Aware Smooth Loss, EPS: Edge-Preserving Smooth Loss, LC: Latent Concatenation (concatenation of object detection flattened features to the latent space).

Method	Abs Rel	Sq Rel	RMSE	RMSE log	$\delta < 1.25$	$\delta < 1.25^2$	$\delta < 1.25^3$
	Lower is better				Higher is better		
Our Baseline	0.414584	13.83466	12.28848	0.434995	0.680209	0.831007	0.904796
Our Baseline + L2	0.307075	6.505432	9.005099	0.368027	0.712899	0.861294	0.927120
Our Baseline $+ L2 + S$	0.335025	6.186975	8.666602	0.383830	0.618205	0.855169	0.926737
Our Baseline + L2 + EPS Our Baseline + L2 + EPS + LC	0.258648 0.248992	3.151716 2.996437	6.814891 6.667879	0.327973 0.317969	0.716325 0.724858	0.865479 0.872039	0.931353 0.935102

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