

prova

February 10, 2023

```
[1]: import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import matplotlib as mplt
import seaborn as sns
import arviz as az
import datetime
```

```
[2]: import fit_arima
```

```
[3]: import open_data
df = open_data.open()
```

```
[4]: ritorno = fit_arima.compute(2, 1, catene=4, samples_per_chain=2500, burnin=1000)
```

```
21:10:52 - cmdstanpy - INFO - CmdStan start processing
chain 1 | 00:00 Status
chain 2 | 00:00 Status
chain 3 | 00:00 Status
chain 4 | 00:00 Status
```

```
21:38:05 - cmdstanpy - INFO - CmdStan done processing.
21:38:05 - cmdstanpy - WARNING - Non-fatal error during sampling:
Exception: normal_lpdf: Scale parameter is -0.111703, but must be positive! (in
'/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan',
line 143, column 4 to column 61)
    Exception: code_model_namespace::log_prob: phi[2][11] is 1, but must be
less than or equal to 1.000000 (in '/home/br1/PythonProjects/PythonStats/ARIMA_1
ast_computation/NoCovariates/code.stan', line 83, column 2 to column 47)
    Exception: code_model_namespace::log_prob: phi[1][1] is -nan, but must
be greater than or equal to -1.000000 (in '/home/br1/PythonProjects/PythonStats/
ARIMA_last_computation/NoCovariates/code.stan', line 83, column 2 to column 47)
    Exception: code_model_namespace::log_prob: phi[1][33] is 1, but must be
less than or equal to 1.000000 (in '/home/br1/PythonProjects/PythonStats/ARIMA_1
ast_computation/NoCovariates/code.stan', line 83, column 2 to column 47)
```

```
Exception: normal_lpdf: Scale parameter is 0, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 157, column 4 to column 34)
    Exception: normal_lpdf: Scale parameter is 0, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 157, column 4 to column 34)
        Exception: normal_lpdf: Scale parameter is 0, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 157, column 4 to column 34)
            Exception: code_model_namespace::log_prob: phi[2][8] is -nan, but must be greater than or equal to -1.000000 (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 83, column 2 to column 47)
                Exception: normal_lpdf: Scale parameter is 0, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 157, column 4 to column 34)
                    Exception: normal_lpdf: Scale parameter is -0.00468339, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 143, column 4 to column 61)
                        Exception: normal_lpdf: Scale parameter is -0.00781159, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 143, column 4 to column 61)
                        Exception: normal_lpdf: Scale parameter is -19.3346, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 143, column 4 to column 61)
                        Exception: normal_lpdf: Scale parameter is -20.4458, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 143, column 4 to column 61)
                        Exception: normal_lpdf: Scale parameter is -1.84055, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 143, column 4 to column 61)
                        Exception: code_model_namespace::log_prob: phi[2][4] is -nan, but must be greater than or equal to -1.000000 (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 83, column 2 to column 47)
                        Exception: normal_lpdf: Scale parameter is -9.85741, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 143, column 4 to column 61)
                        Exception: normal_lpdf: Scale parameter is -0.00793045, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 143, column 4 to column 61)
                        Exception: normal_lpdf: Scale parameter is -1.48033, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 143, column 4 to column 61)
                        Exception: normal_lpdf: Scale parameter is -0.370182, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 143, column 4 to column 61)
                        Exception: normal_lpdf: Scale parameter is -3.13815, but must be positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/code.stan', line 143, column 4 to column 61)
```

```

Exception: normal_lpdf: Scale parameter is -2.7382, but must be
positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCov
ariates/code.stan', line 143, column 4 to column 61)
Exception: normal_lpdf: Scale parameter is -0.274406, but must be
positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCov
ariates/code.stan', line 143, column 4 to column 61)
Exception: code_model_namespace::log_prob: phi[1][10] is -nan, but must
be greater than or equal to -1.000000 (in '/home/br1/PythonProjects/PythonStats/
ARIMA_last_computation/NoCovariates/code.stan', line 83, column 2 to column 47)
Exception: normal_lpdf: Scale parameter is -3.44707, but must be
positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCov
ariates/code.stan', line 143, column 4 to column 61)
Exception: normal_lpdf: Scale parameter is -0.00909615, but must be
positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCov
ariates/code.stan', line 143, column 4 to column 61)
Exception: normal_lpdf: Scale parameter is -0.0018971, but must be
positive! (in '/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCov
ariates/code.stan', line 143, column 4 to column 61)
Consider re-running with show_console=True if the above output is unclear!

```

```

/home/br1/PythonProjects/PythonStats/ARIMA_last_computation/NoCovariates/fit_ari
ma.py:37: FutureWarning: Indexing with a float is deprecated, and will raise an
IndexError in pandas 2.0. You can manually convert to an integer key instead.
y_missing_list.append({'Stazione':df.columns[v[i]],'Data':df.index[u[i]],'Samp
les':inference_data.posterior.w.values[:, :, i].reshape(catene*samples_per_chain)}
)

```

Tempo di computazione: 27:12

```
[5]: res = az.loo(ritorno['inference_data'], var_name="log_lik", pointwise=True, u
        ↴scale='deviance')
res
```

```

/home/br1/PythonProjects/PythonStats/.venv/lib/python3.10/site-
packages/arviz/stats/stats.py:803: UserWarning: Estimated shape parameter of
Pareto distribution is greater than 0.7 for one or more samples. You should
consider using a more robust model, this is because importance sampling is less
likely to work well if the marginal posterior and LOO posterior are very
different. This is more likely to happen with a non-robust model and highly
influential observations.
warnings.warn(

```

```
[5]: Computed from 10000 posterior samples and 17191 observations log-likelihood
matrix.
```

	Estimate	SE
deviance_loo	-14506.23	309.87

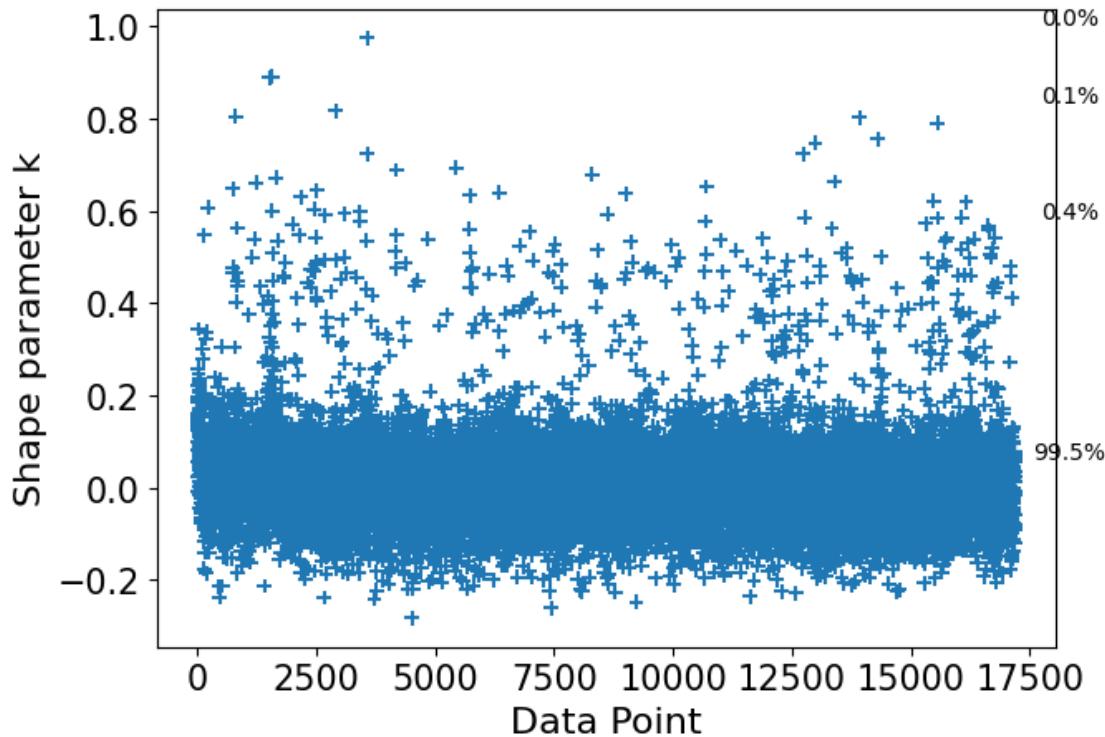
```
p_loo      296.12      -
```

```
There has been a warning during the calculation. Please check the results.
```

```
-----  
Pareto k diagnostic values:
```

		Count	Pct.
(-Inf, 0.5]	(good)	17112	99.5%
(0.5, 0.7]	(ok)	68	0.4%
(0.7, 1]	(bad)	11	0.1%
(1, Inf)	(very bad)	0	0.0%

```
[6]: aux_plt = az.plot_khat(res, show_bins=True, figsize=(7,5))
```



```
[7]: res = az.waic(ritorno['inference_data'], var_name="log_lik", scale='deviance')  
res
```

```
/home/br1/PythonProjects/PythonStats/.venv/lib/python3.10/site-  
packages/arviz/stats/stats.py:1645: UserWarning: For one or more samples the  
posterior variance of the log predictive densities exceeds 0.4. This could be  
indication of WAIC starting to fail.
```

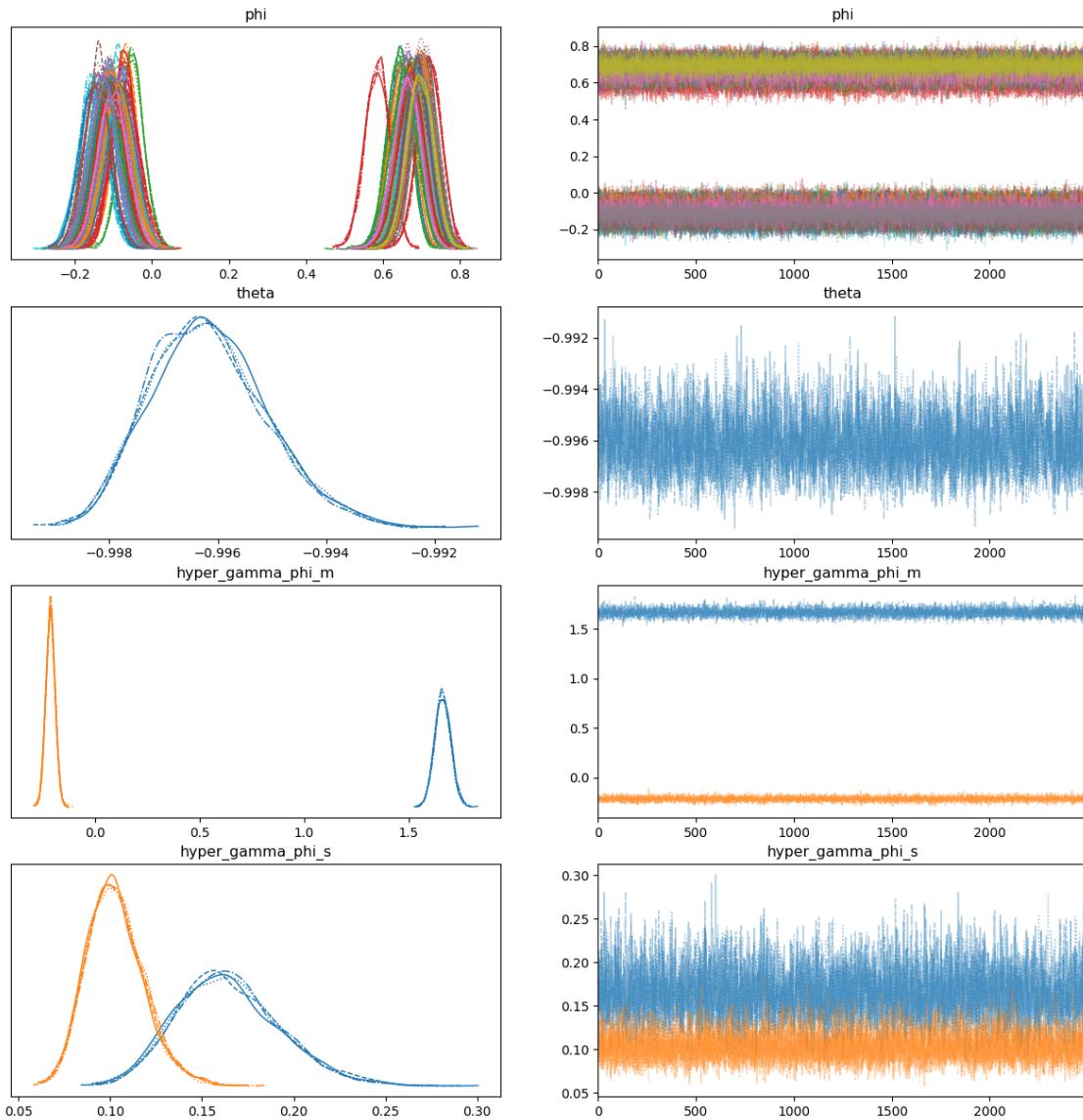
```
See http://arxiv.org/abs/1507.04544 for details  
warnings.warn(
```

[7]: Computed from 10000 posterior samples and 17191 observations log-likelihood matrix.

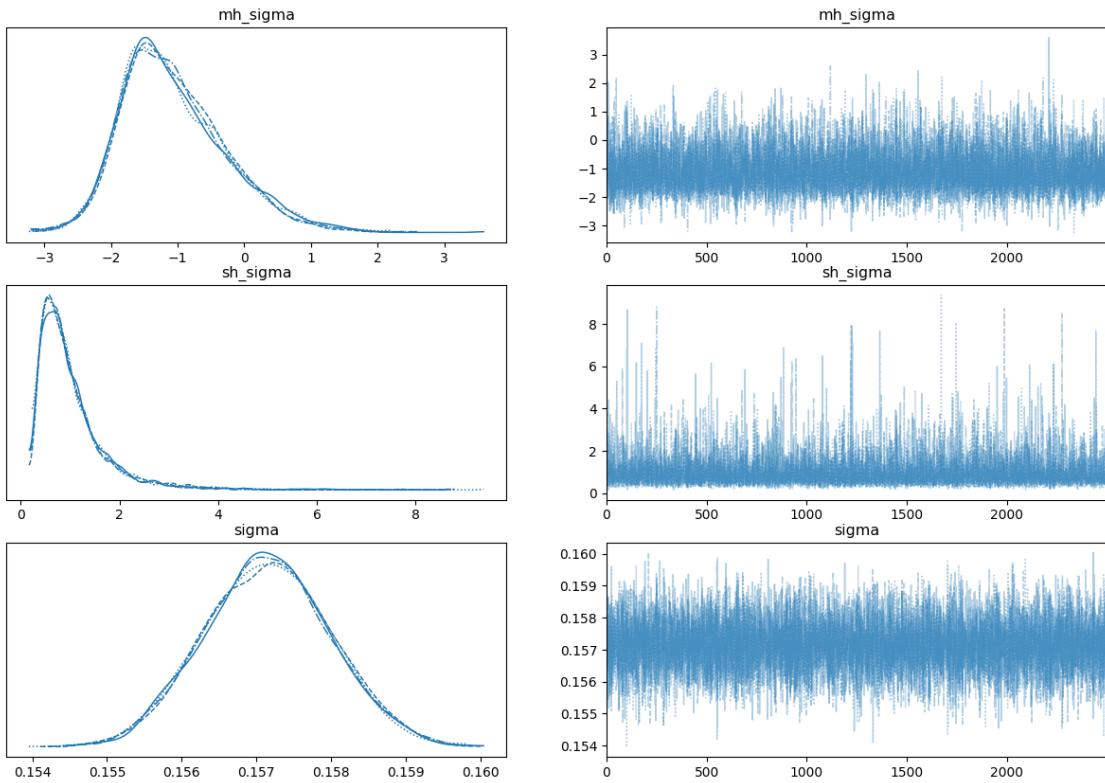
	Estimate	SE
deviance_waic	-14528.97	309.61
p_waic	284.76	-

There has been a warning during the calculation. Please check the results.

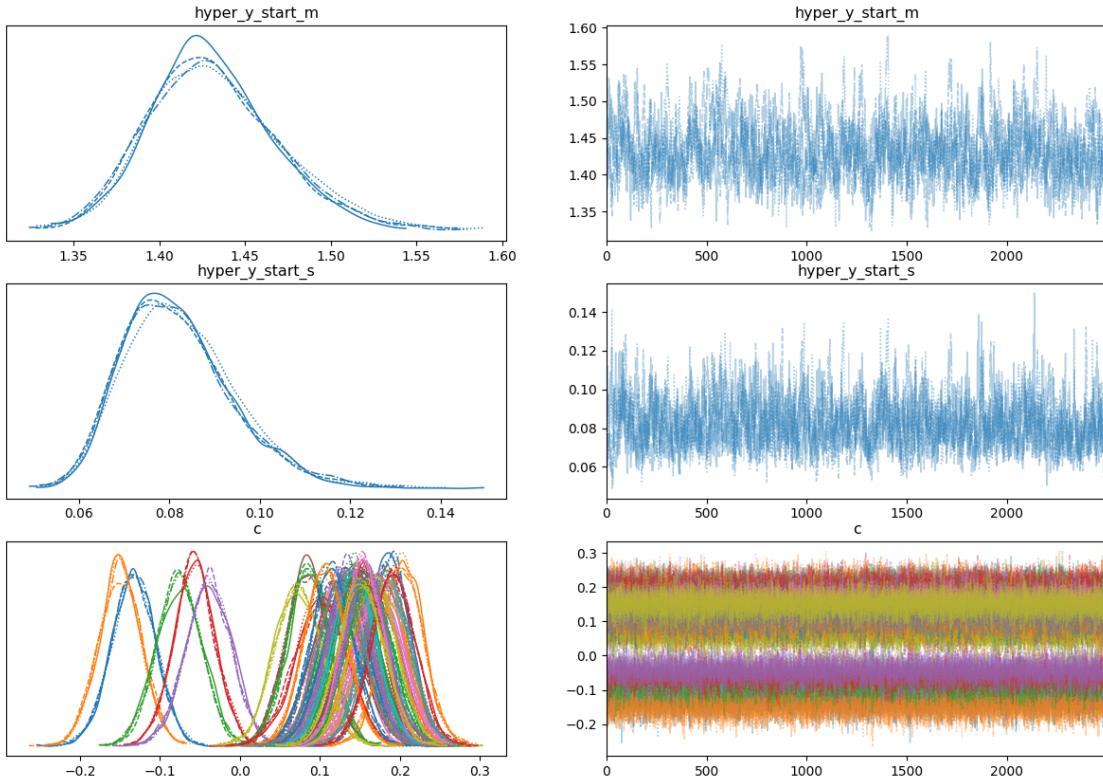
```
[8]: plt_aux = az.plot_trace(ritorno['inference_data'],  
                           var_names=['phi', 'theta', 'hyper_gamma_phi_m', 'hyper_gamma_phi_s'],  
                           divergences=True, figsize=(15,15))
```



```
[9]: plt_aux = az.plot_trace(ritorno['inference_data'],  
    var_names=['mh_sigma','sh_sigma','sigma'], divergences=True, figsize=(15,10))
```



```
[10]: plt_aux = az.plot_trace(ritorno['inference_data'],  
    var_names=['hyper_y_start_m','hyper_y_start_s','c'], divergences=True,  
    figsize=(15,10))
```



```
[11]: az.summary(ritorno['inference_data'], var_names=['y_start'])
```

	mean	sd	hdi_3%	hdi_97%	mcse_mean	mcse_sd	ess_bulk	\
y_start[0, 0]	1.422	0.089	1.251	1.587	0.002	0.001	2935.0	
y_start[0, 1]	1.419	0.091	1.248	1.591	0.002	0.001	3125.0	
y_start[0, 2]	1.422	0.090	1.252	1.593	0.002	0.001	3105.0	
y_start[0, 3]	1.424	0.090	1.253	1.594	0.002	0.001	3232.0	
y_start[0, 4]	1.427	0.092	1.245	1.595	0.002	0.001	2847.0	
...	
y_start[2, 44]	1.445	0.054	1.345	1.548	0.001	0.001	1875.0	
y_start[2, 45]	1.442	0.055	1.340	1.549	0.001	0.001	1967.0	
y_start[2, 46]	1.438	0.054	1.334	1.535	0.001	0.001	2333.0	
y_start[2, 47]	1.452	0.055	1.348	1.556	0.001	0.001	1877.0	
y_start[2, 48]	1.459	0.057	1.360	1.572	0.001	0.001	1908.0	
					ess_tail	r_hat		
y_start[0, 0]	3563.0	1.0						
y_start[0, 1]	3114.0	1.0						
y_start[0, 2]	4272.0	1.0						
y_start[0, 3]	3953.0	1.0						
y_start[0, 4]	3181.0	1.0						
...						

```
y_start[2, 44]    2615.0    1.0
y_start[2, 45]    2244.0    1.0
y_start[2, 46]    3204.0    1.0
y_start[2, 47]    2748.0    1.0
y_start[2, 48]    2766.0    1.0
```

[147 rows x 9 columns]

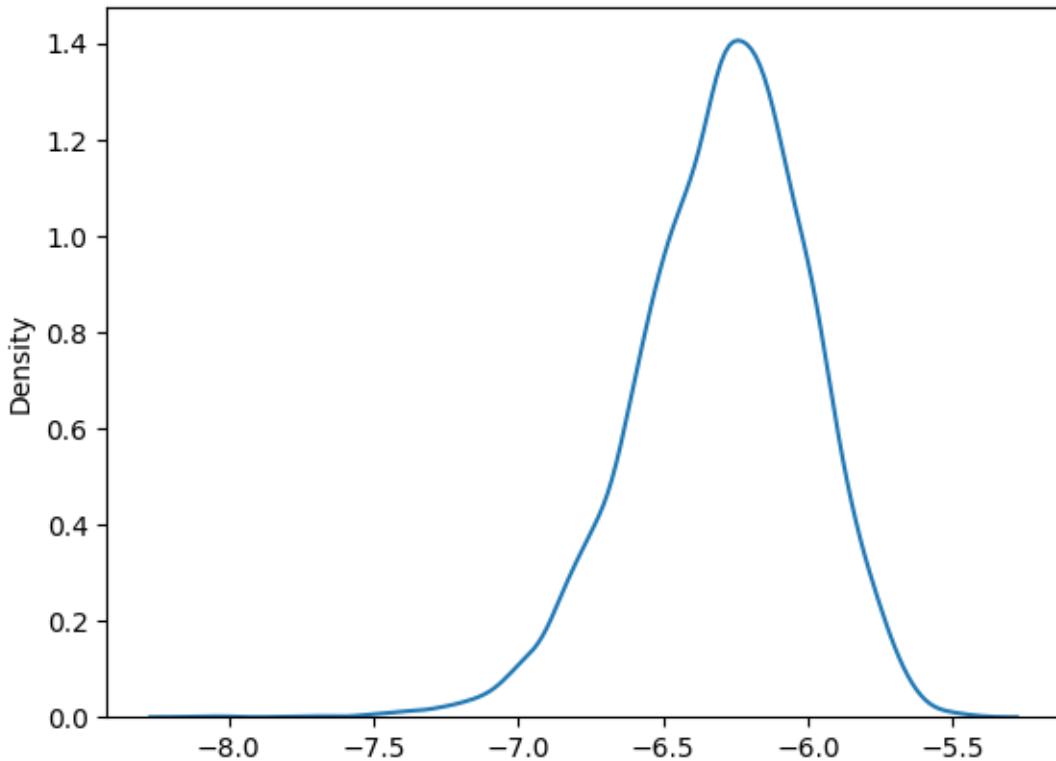
```
[12]: az.summary(ritorno['inference_data'], var_names=['hyper_y_start_m', ↴'hyper_y_start_s'])
```

```
mean      sd   hdi_3%   hdi_97%  mcse_mean  mcse_sd  ess_bulk \
hyper_y_start_m  1.432  0.038   1.364   1.506     0.002    0.001    578.0
hyper_y_start_s  0.082  0.012   0.061   0.106     0.000    0.000    688.0

ess_tail  r_hat
hyper_y_start_m    852.0   1.00
hyper_y_start_s    1692.0   1.01
```

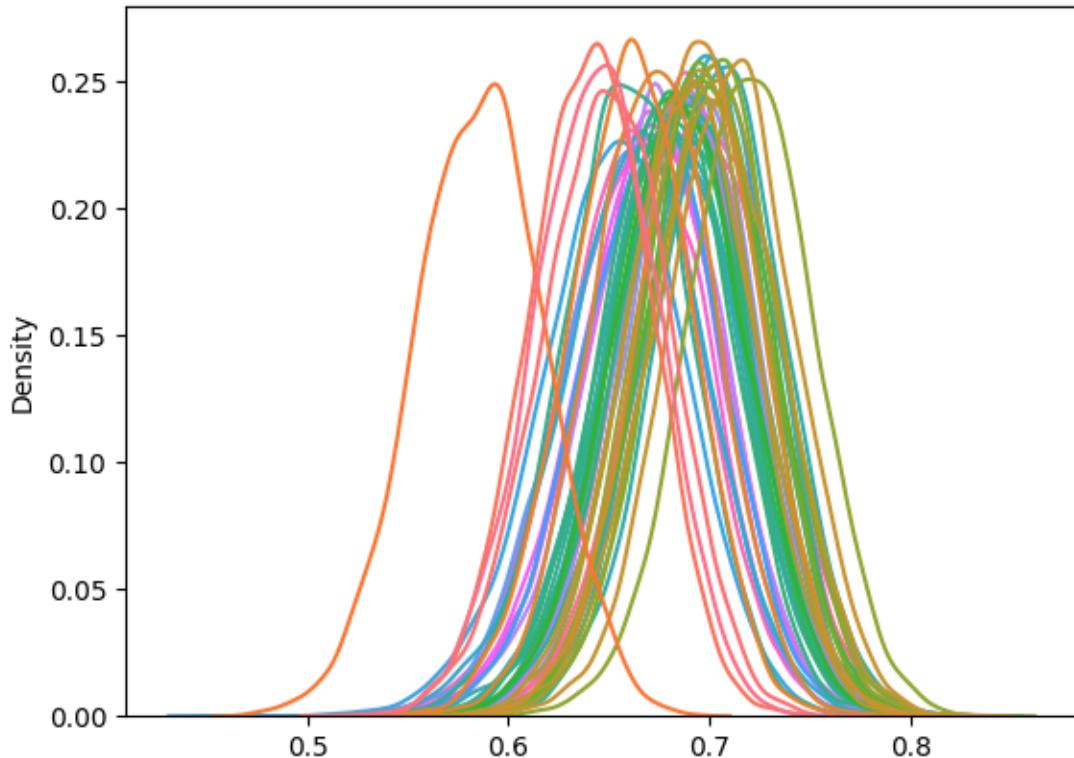
```
[13]: aux_shape = ritorno['inference_data'].posterior.gamma_th.values.shape
sns.kdeplot(ritorno['inference_data'].posterior.gamma_th.values.
             ↴reshape((aux_shape[0]*aux_shape[1])), legend=False)
```

```
[13]: <AxesSubplot: ylabel='Density'>
```



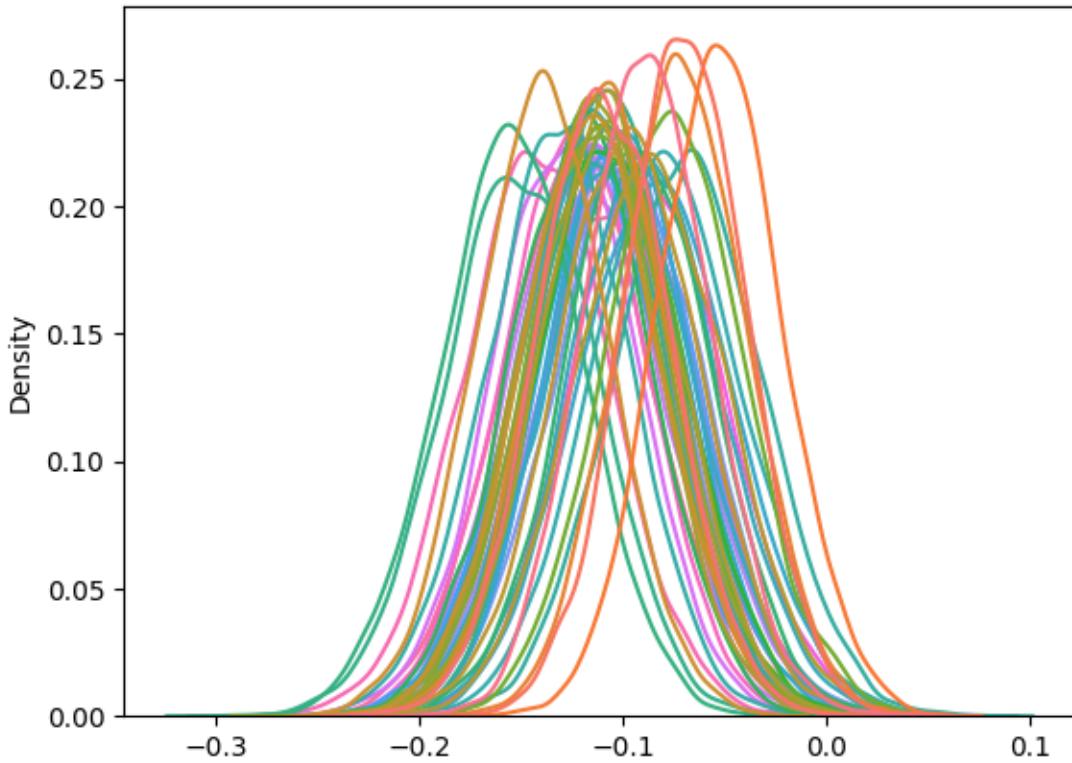
```
[14]: aux_shape = ritorno['inference_data'].posterior.phi.values.shape
sns.kdeplot(ritorno['inference_data'].posterior.phi.values.
             ↪reshape((aux_shape[0]*aux_shape[1],aux_shape[2],aux_shape[3]))[:,0,:,:], ↪
             ↪legend=False)
```

```
[14]: <AxesSubplot: ylabel='Density'>
```



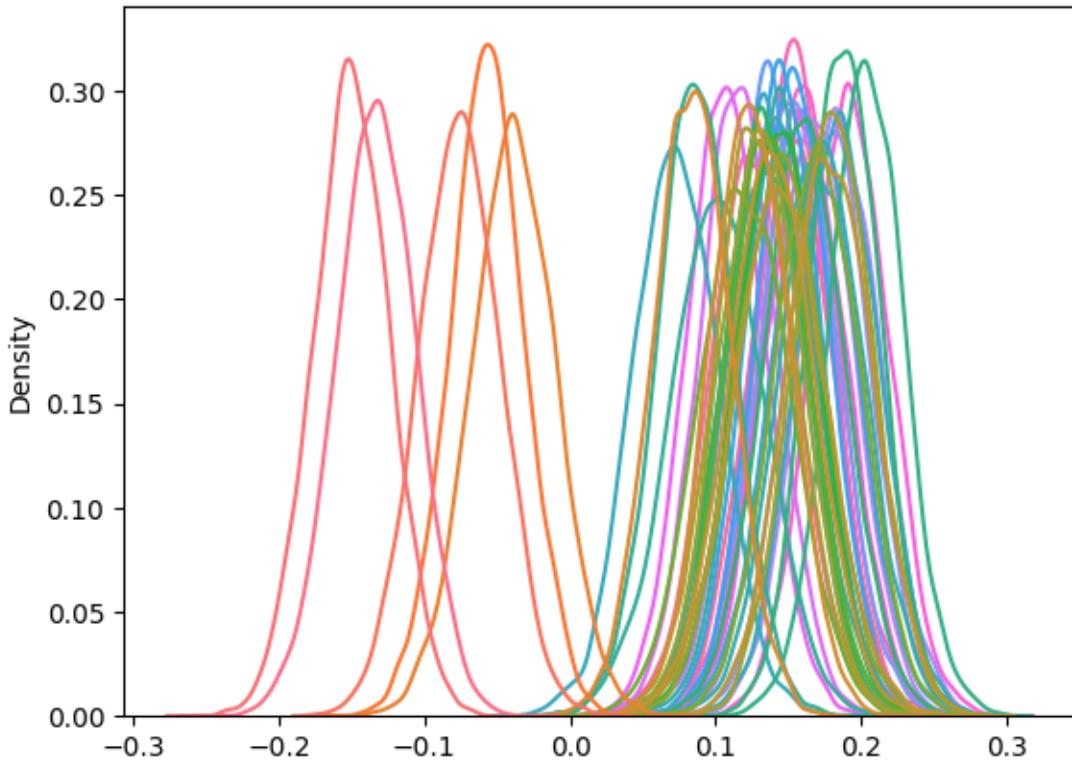
```
[15]: aux_shape = ritorno['inference_data'].posterior.phi.values.shape
sns.kdeplot(ritorno['inference_data'].posterior.phi.values.
             ↪reshape((aux_shape[0]*aux_shape[1],aux_shape[2],aux_shape[3]))[:,1,:,:], ↪
             ↪legend=False)
```

```
[15]: <AxesSubplot: ylabel='Density'>
```



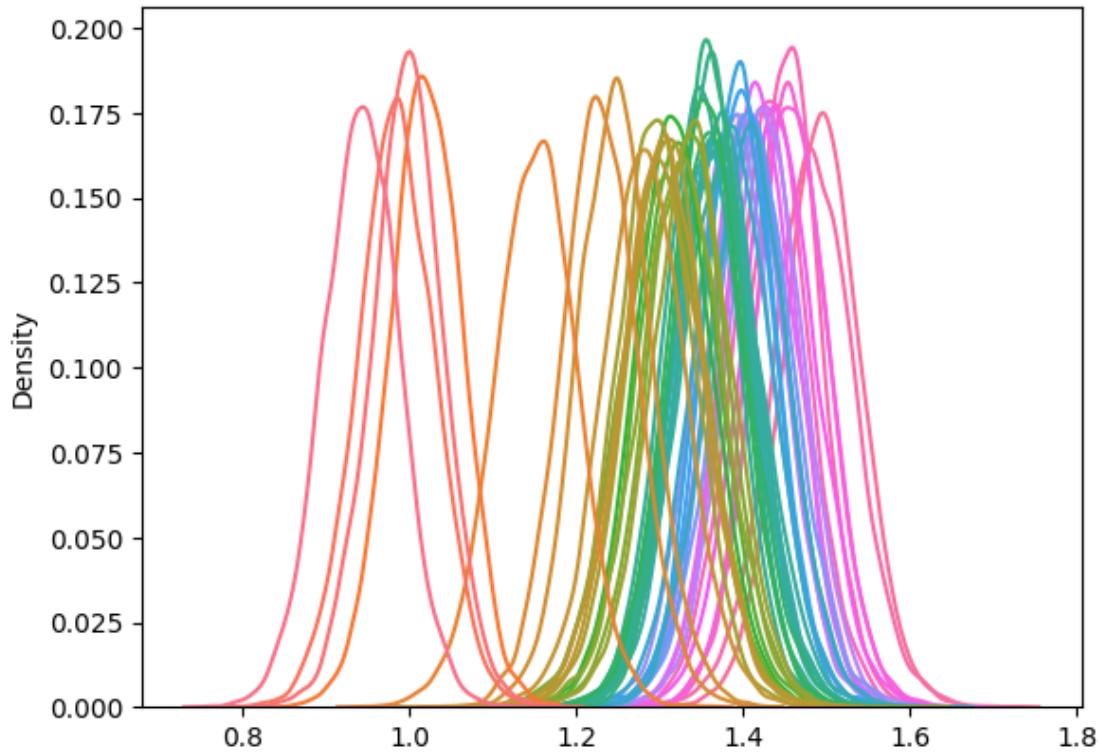
```
[16]: aux_shape = ritorno['inference_data'].posterior.c.values.shape
sns.kdeplot(ritorno['inference_data'].posterior.c.values.
             .reshape((aux_shape[0]*aux_shape[1],aux_shape[2])), legend=False)
```

```
[16]: <AxesSubplot: ylabel='Density'>
```



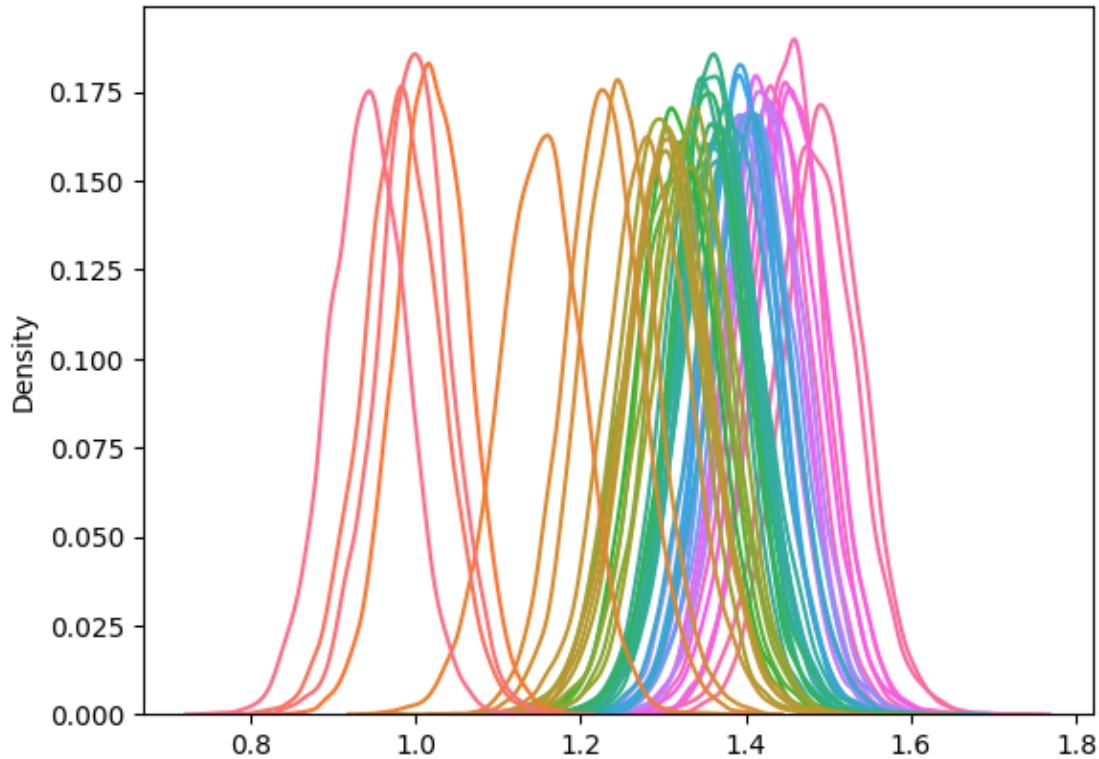
```
[17]: aux_shape = ritorno['inference_data'].posterior.annual_mean.values.shape
sns.kdeplot(ritorno['inference_data'].posterior.annual_mean.values,
             reshape((aux_shape[0]*aux_shape[1],aux_shape[2])), legend=False)
```

```
[17]: <AxesSubplot: ylabel='Density'>
```



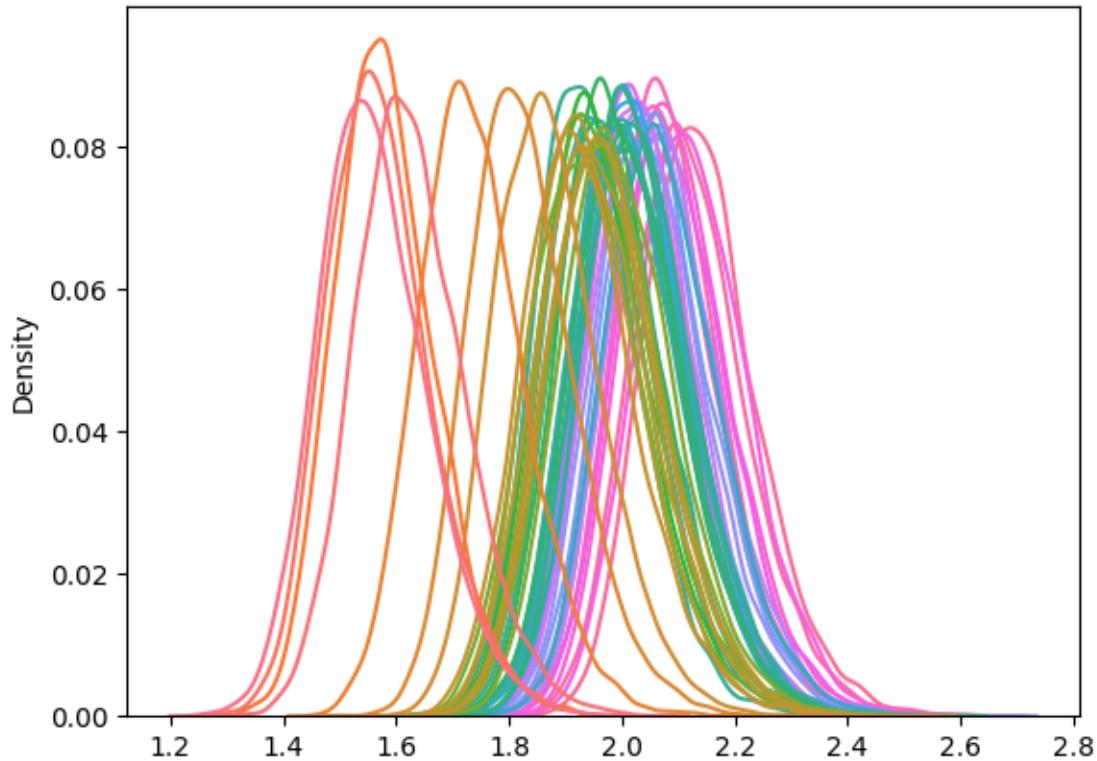
```
[18]: aux_shape = ritorno['inference_data'].posterior.annual_median.values.shape
sns.kdeplot(ritorno['inference_data'].posterior.annual_median.values.
             .reshape((aux_shape[0]*aux_shape[1],aux_shape[2])), legend=False)
```

```
[18]: <AxesSubplot: ylabel='Density'>
```



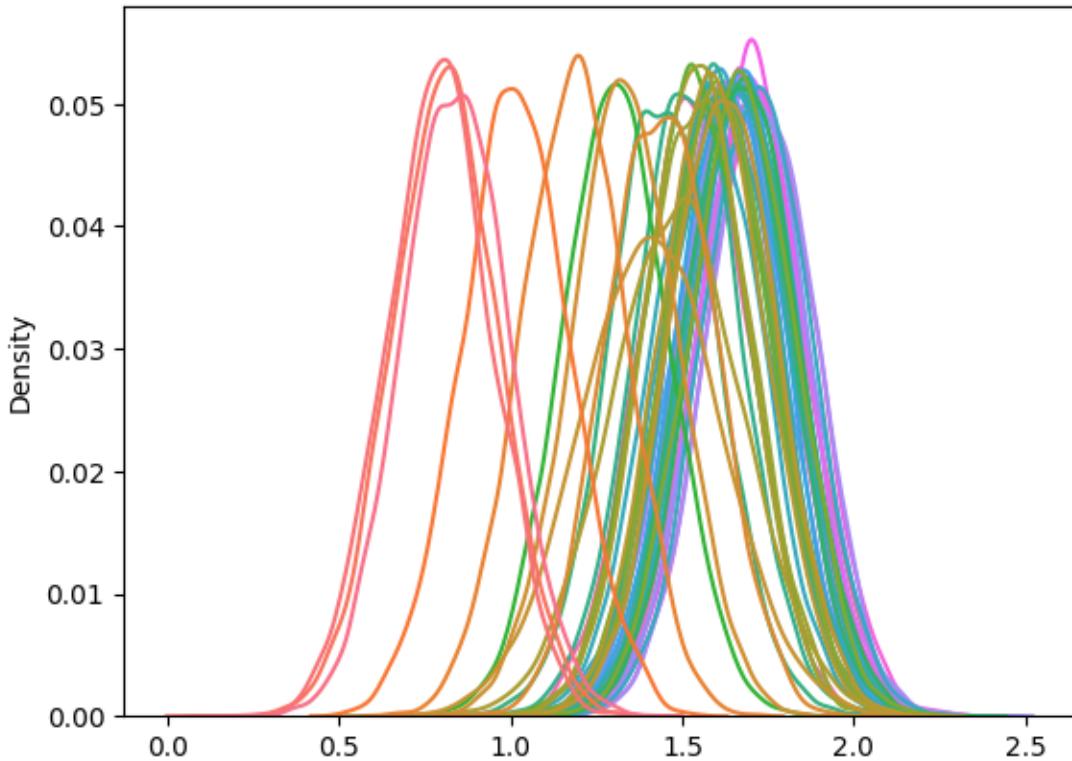
```
[19]: aux_shape = ritorno['inference_data'].posterior.annual_max.values.shape
sns.kdeplot(ritorno['inference_data'].posterior.annual_max.values.
             .reshape((aux_shape[0]*aux_shape[1],aux_shape[2])), legend=False)
```

```
[19]: <AxesSubplot: ylabel='Density'>
```



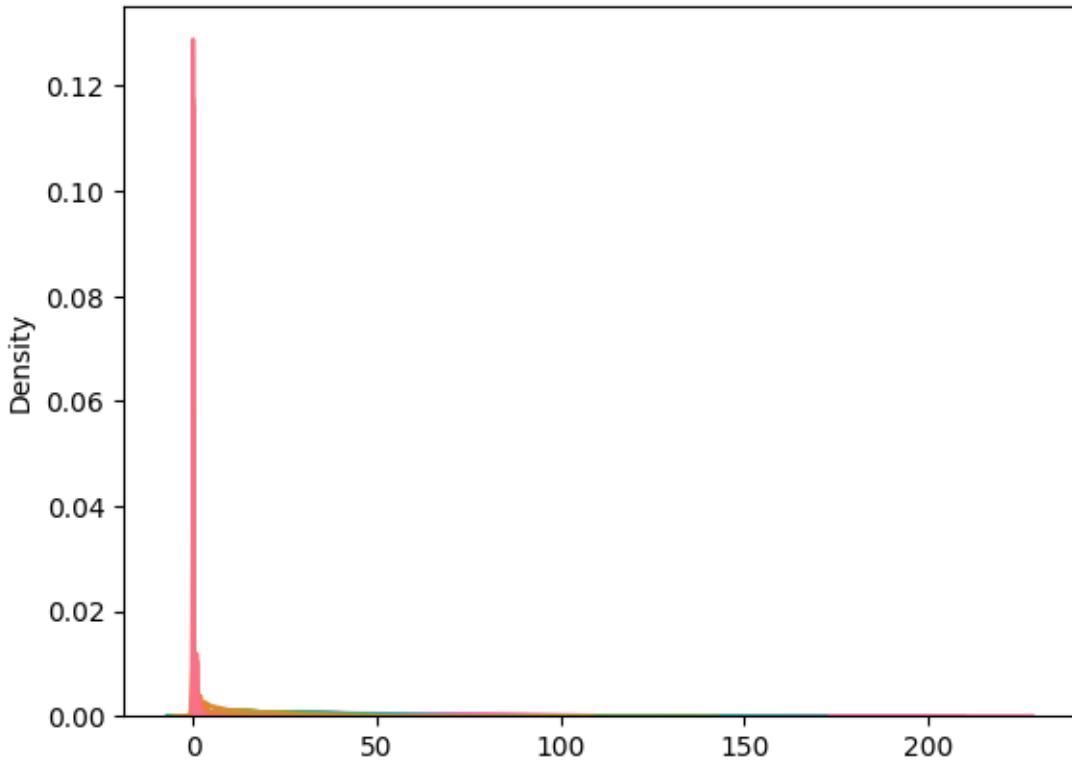
```
[20]: valori_31_dic = []
for dizionario in ritorno['missing']:
    if dizionario['Data'] == '2018-12-31':
        valori_31_dic.append(dizionario['Samples'])

res_plot = sns.kdeplot(valori_31_dic, legend=False)
```



```
[21]: aux_shape = ritorno['inference_data'].posterior.annual_days_over_threshold.  
      ↪values.shape  
sns.kdeplot(ritorno['inference_data'].posterior.annual_days_over_threshold.  
      ↪values.reshape((aux_shape[0]*aux_shape[1],aux_shape[2])), legend=False)
```

```
[21]: <AxesSubplot: ylabel='Density'>
```



```
[22]: pd.set_option('display.max_columns', 500)
aux_results = pd.DataFrame(ritorno['inference_data'].posterior.
    ↪annual_days_over_threshold.values.
    ↪reshape((aux_shape[0]*aux_shape[1],aux_shape[2])), columns=df.columns).
    ↪describe()
aux_results.sort_values('mean', axis=1, ascending=True)
```

	CASTELLUCCIO	CORTE BRUGNATELLA	SAVIGNANO DI RIGO	FEBBIO	\
count	10000.00000	10000.00000	10000.00000	10000.00000	
mean	0.10200	0.11500	0.118500	0.302400	
std	0.36443	0.394703	0.398087	0.680147	
min	0.00000	0.000000	0.000000	0.000000	
25%	0.00000	0.000000	0.000000	0.000000	
50%	0.00000	0.000000	0.000000	0.000000	
75%	0.00000	0.000000	0.000000	0.000000	
max	4.00000	7.000000	6.000000	8.000000	
	SAN LEO	VERUCCHIO	BADIA	GIARDINI MARGHERITA	\
count	10000.000000	10000.000000	10000.000000	10000.000000	
mean	1.567600	4.877900	7.790400	13.415600	
std	1.962961	4.054311	5.462239	8.325383	
min	0.000000	0.000000	0.000000	0.000000	

25%	0.000000	2.000000	4.000000	7.000000
50%	1.000000	4.000000	7.000000	12.000000
75%	2.000000	7.000000	10.000000	18.000000
max	21.000000	38.000000	41.000000	80.000000

	MARECCHIA	SAN PIETRO	CAPOFIUME	PARCO BERTOZZI	DELTA CERVIA	\
count	10000.000000		10000.000000	10000.000000	10000.000000	
mean	15.608700		15.637100	17.239500	17.616200	
std	9.067712		9.744521	10.226974	9.588717	
min	0.000000		0.000000	0.000000	0.000000	
25%	9.000000		9.000000	10.000000	11.000000	
50%	14.000000		14.000000	15.000000	16.000000	
75%	20.250000		21.000000	22.000000	23.000000	
max	84.000000		92.000000	91.000000	83.000000	

	LUGAGNANO	DE AMICIS	SAN LAZZARO	PARCO RESISTENZA	\
count	10000.000000	10000.000000	10000.000000	10000.000000	
mean	17.707000	17.769500	18.701500	19.475400	
std	9.695842	9.423346	10.193998	10.424829	
min	0.000000	0.000000	0.000000	0.000000	
25%	11.000000	11.000000	11.000000	12.000000	
50%	16.000000	16.000000	17.000000	18.000000	
75%	23.000000	23.000000	24.000000	25.000000	
max	86.000000	85.000000	83.000000	104.000000	

	FRANCHINI-ANGELONI	GHERARDI	VIA CHIARINI	GAVELLO	\
count	10000.000000	10000.000000	10000.000000	10000.000000	
mean	21.104400	21.166500	21.361500	23.260100	
std	11.205492	11.605751	11.138134	11.271324	
min	0.000000	0.000000	0.000000	0.000000	
25%	13.000000	13.000000	13.000000	15.000000	
50%	19.000000	19.000000	20.000000	21.000000	
75%	27.000000	27.000000	27.000000	30.000000	
max	102.000000	112.000000	85.000000	101.000000	

	SAVIGNANO	BESENZONE	ROMA	VILLA FULVIA	\
count	10000.000000	10000.000000	10000.000000	10000.000000	
mean	23.932500	23.949300	28.18090	28.534400	
std	11.896567	12.455571	13.45773	13.180083	
min	0.000000	0.000000	1.00000	0.000000	
25%	15.000000	15.000000	19.00000	19.000000	
50%	22.000000	22.000000	26.00000	27.000000	
75%	31.000000	31.000000	35.00000	36.000000	
max	137.000000	105.000000	130.00000	166.000000	

	PORTE SAN FELICE	CAORLE	CASTELLARANO	CENTO	\
count	10000.000000	10000.000000	10000.000000	10000.000000	

mean	28.738900	29.321800	29.62880	30.606900
std	13.040335	14.381499	12.01704	14.105356
min	0.000000	0.000000	2.00000	1.000000
25%	19.000000	19.000000	21.00000	20.000000
50%	27.000000	27.000000	28.00000	29.000000
75%	36.000000	37.000000	37.00000	38.250000
max	101.000000	111.000000	98.00000	121.000000

	ZALAMELLA	PARCO MONTECUCCO	PARCO EDILCARANI	BOGOLESE	\
count	10000.000000	10000.000000	10000.000000	10000.000000	
mean	30.616000	30.740400	31.929900	32.091500	
std	14.220372	14.289571	12.852171	13.487006	
min	1.000000	0.000000	2.000000	1.000000	
25%	20.000000	20.000000	23.000000	22.000000	
50%	28.000000	29.000000	30.000000	31.000000	
75%	39.000000	39.000000	39.000000	40.000000	
max	119.000000	124.000000	100.000000	119.000000	

	SARAGAT	PARADIGNA	MALCANTONE	S. LAZZARO	REMESINA	\
count	10000.000000	10000.000000	10000.000000	10000.000000	10000.000000	
mean	34.509200	35.694200	35.87640	36.64660	36.97600	
std	14.189815	15.221756	15.03205	15.35704	14.94129	
min	1.000000	2.000000	0.00000	2.00000	2.00000	
25%	24.000000	25.000000	25.00000	26.00000	26.00000	
50%	33.000000	34.000000	34.00000	35.00000	35.00000	
75%	43.000000	44.000000	44.25000	45.00000	46.00000	
max	120.000000	130.000000	130.00000	144.00000	126.00000	

	S. ROCCO	CENO	ISONZO	PARCO FERRARI	\
count	10000.000000	10000.000000	10000.000000	10000.000000	
mean	38.350700	41.990600	42.731600	42.800400	
std	15.436954	16.984556	16.497745	16.676348	
min	3.000000	4.000000	1.000000	1.000000	
25%	27.000000	30.000000	31.000000	31.000000	
50%	36.000000	40.000000	41.000000	41.000000	
75%	47.000000	52.000000	52.000000	53.000000	
max	120.000000	153.000000	156.000000	141.000000	

	GIORDANI-FARNESE	CITTADELLA	SAN FRANCESCO	FLAMINIA	\
count	10000.000000	10000.000000	10000.000000	10000.000000	
mean	46.467400	46.507200	50.969500	51.176500	
std	17.410958	17.140721	17.009283	18.785703	
min	4.000000	7.000000	9.000000	8.000000	
25%	34.000000	34.000000	39.000000	38.000000	
50%	45.000000	45.000000	50.000000	49.000000	
75%	57.000000	57.000000	61.000000	62.000000	
max	155.000000	157.000000	139.000000	159.000000	

	MONTEBELLO	GIARDINI	GERBIDO	TIMAVO
count	10000.00000	10000.000000	10000.000000	10000.000000
mean	54.85700	60.543300	63.666400	70.191400
std	18.80313	19.254184	22.584466	21.885408
min	8.00000	10.000000	5.000000	9.000000
25%	41.00000	47.000000	48.000000	55.000000
50%	53.00000	59.000000	61.000000	69.000000
75%	66.00000	72.000000	77.000000	83.000000
max	156.00000	163.000000	199.000000	218.000000

```
[23]: pd.set_option('display.max_columns', 500)
aux_results = pd.DataFrame(ritorno['inference_data'].posterior.
    ↪is_over_daily_limit.values.
    ↪reshape((aux_shape[0]*aux_shape[1],aux_shape[2])), columns=df.columns).
    ↪describe()
aux_results.sort_values('mean', axis=1, ascending=True)
```

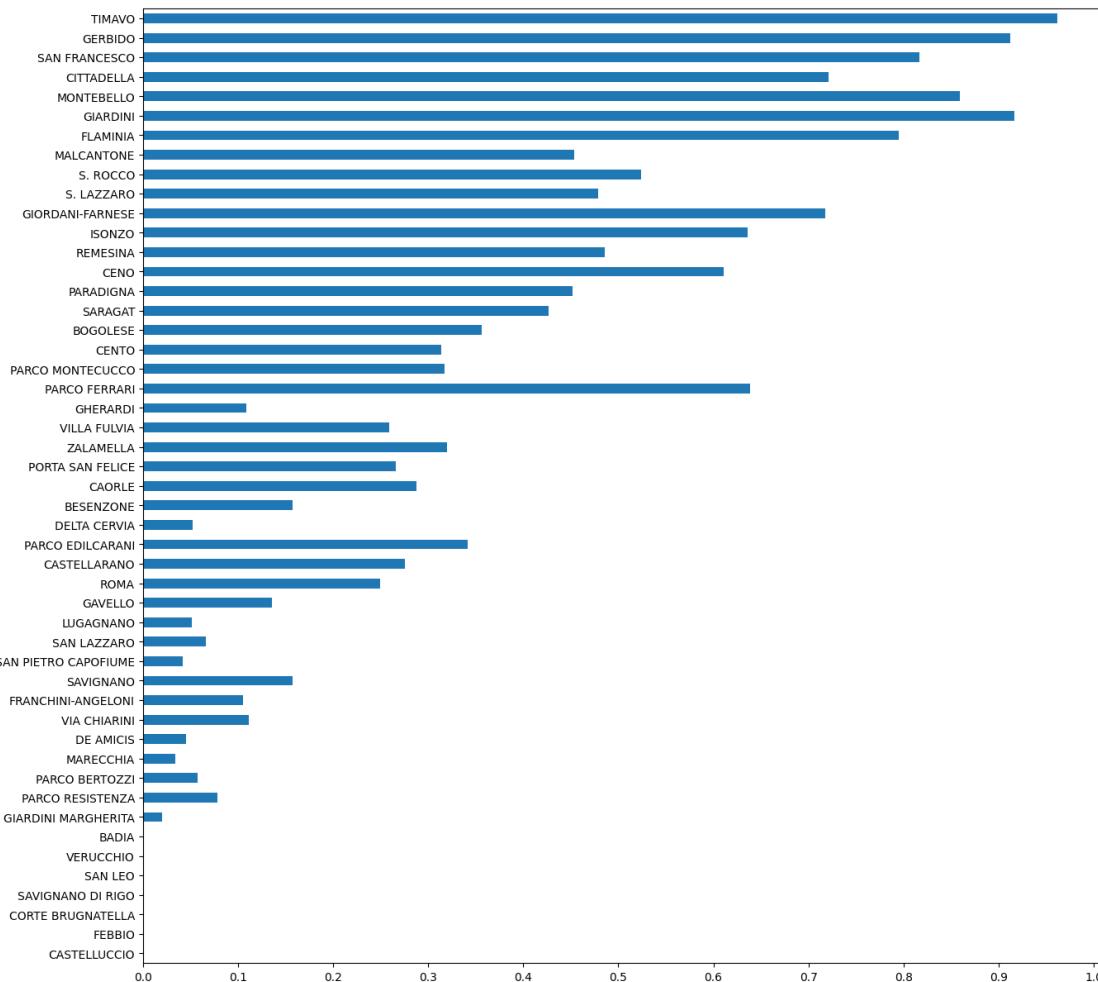
	CASTELLUCCIO	FEBBIO	CORTE BRUGNATELLA	SAVIGNANO DI RIGO	SAN LEO	\
count	10000.0	10000.0	10000.0	10000.0	10000.0	
mean	0.0	0.0	0.0	0.0	0.0	
std	0.0	0.0	0.0	0.0	0.0	
min	0.0	0.0	0.0	0.0	0.0	
25%	0.0	0.0	0.0	0.0	0.0	
50%	0.0	0.0	0.0	0.0	0.0	
75%	0.0	0.0	0.0	0.0	0.0	
max	0.0	0.0	0.0	0.0	0.0	
	VERUCCHIO	BADIA	GIARDINI MARGHERITA	MARECCHIA	\	
count	10000.000000	10000.000000	10000.000000	10000.000000		
mean	0.000200	0.001300	0.019700	0.034300		
std	0.014141	0.036034	0.138974	0.182008		
min	0.000000	0.000000	0.000000	0.000000		
25%	0.000000	0.000000	0.000000	0.000000		
50%	0.000000	0.000000	0.000000	0.000000		
75%	0.000000	0.000000	0.000000	0.000000		
max	1.000000	1.000000	1.000000	1.000000		
	SAN PIETRO CAPOFIUME	DE AMICIS	LUGAGNANO	DELTA CERVIA	\	
count	10000.000000	10000.000000	10000.000000	10000.000000		
mean	0.041900	0.045500	0.051700	0.05210		
std	0.200371	0.208408	0.221432	0.22224		
min	0.000000	0.000000	0.000000	0.00000		
25%	0.000000	0.000000	0.000000	0.00000		
50%	0.000000	0.000000	0.000000	0.00000		
75%	0.000000	0.000000	0.000000	0.00000		
max	1.000000	1.000000	1.000000	1.00000		

	PARCO BERTOZZI	SAN LAZZARO	PARCO RESISTENZA	FRANCHINI-ANGELONI	\
count	10000.000000	10000.000000	10000.000000	10000.000000	
mean	0.057100	0.066200	0.078100	0.105000	
std	0.232045	0.248644	0.268342	0.306569	
min	0.000000	0.000000	0.000000	0.000000	
25%	0.000000	0.000000	0.000000	0.000000	
50%	0.000000	0.000000	0.000000	0.000000	
75%	0.000000	0.000000	0.000000	0.000000	
max	1.000000	1.000000	1.000000	1.000000	
	GHERARDI	VIA CHIARINI	GAVELLO	SAVIGNANO	BESENZONE \
count	10000.000000	10000.000000	10000.000000	10000.000000	10000.000000
mean	0.108900	0.111100	0.135500	0.157300	0.157400
std	0.311529	0.314272	0.342274	0.364102	0.364196
min	0.000000	0.000000	0.000000	0.000000	0.000000
25%	0.000000	0.000000	0.000000	0.000000	0.000000
50%	0.000000	0.000000	0.000000	0.000000	0.000000
75%	0.000000	0.000000	0.000000	0.000000	0.000000
max	1.000000	1.000000	1.000000	1.000000	1.000000
	ROMA	VILLA FULVIA	PORTA SAN FELICE	CASTELLARANO	\
count	10000.000000	10000.000000	10000.000000	10000.000000	
mean	0.249100	0.258900	0.26580	0.275400	
std	0.432513	0.438052	0.44178	0.446738	
min	0.000000	0.000000	0.00000	0.000000	
25%	0.000000	0.000000	0.00000	0.000000	
50%	0.000000	0.000000	0.00000	0.000000	
75%	0.000000	1.000000	1.00000	1.000000	
max	1.000000	1.000000	1.00000	1.000000	
	CAORLE	CENTO	PARCO MONTECUCCO	ZALAMELLA	\
count	10000.000000	10000.000000	10000.000000	10000.000000	
mean	0.287700	0.313500	0.316800	0.319500	
std	0.452713	0.463939	0.465252	0.466306	
min	0.000000	0.000000	0.000000	0.000000	
25%	0.000000	0.000000	0.000000	0.000000	
50%	0.000000	0.000000	0.000000	0.000000	
75%	1.000000	1.000000	1.000000	1.000000	
max	1.000000	1.000000	1.000000	1.000000	
	PARCO EDILCARANI	BOGOLESE	SARAGAT	PARADIGNA	\
count	10000.000000	10000.000000	10000.000000	10000.000000	
mean	0.34190	0.356600	0.426600	0.452100	
std	0.47437	0.479019	0.494608	0.497725	
min	0.00000	0.000000	0.000000	0.000000	
25%	0.00000	0.000000	0.000000	0.000000	

50%	0.00000	0.000000	0.000000	0.000000	
75%	1.00000	1.000000	1.000000	1.000000	
max	1.00000	1.000000	1.000000	1.000000	
	MALCANTONE	S. LAZZARO	REMESINA	S. ROCCO	CENO \
count	10000.00000	10000.00000	10000.000000	10000.000000	10000.000000
mean	0.453500	0.47890	0.485400	0.524300	0.610400
std	0.497858	0.49958	0.499812	0.499434	0.487684
min	0.000000	0.00000	0.000000	0.000000	0.000000
25%	0.000000	0.00000	0.000000	0.000000	0.000000
50%	0.000000	0.00000	0.000000	1.000000	1.000000
75%	1.000000	1.00000	1.000000	1.000000	1.000000
max	1.000000	1.00000	1.000000	1.000000	1.000000
	ISONZO	PARCO FERRARI	GIORDANI-FARNESE	CITTADELLA \	
count	10000.00000	10000.00000	10000.00000	10000.00000	
mean	0.635600	0.638300	0.717900	0.721100	
std	0.481286	0.480517	0.450044	0.448481	
min	0.000000	0.000000	0.000000	0.000000	
25%	0.000000	0.000000	0.000000	0.000000	
50%	1.000000	1.000000	1.000000	1.000000	
75%	1.000000	1.000000	1.000000	1.000000	
max	1.000000	1.000000	1.000000	1.000000	
	FLAMINIA	SAN FRANCESCO	MONTEBELLO	GERBIDO	GIARDINI \
count	10000.00000	10000.00000	10000.00000	10000.00000	10000.00000
mean	0.794600	0.816300	0.858800	0.912300	0.916200
std	0.404014	0.387259	0.348245	0.282872	0.277101
min	0.000000	0.000000	0.000000	0.000000	0.000000
25%	1.000000	1.000000	1.000000	1.000000	1.000000
50%	1.000000	1.000000	1.000000	1.000000	1.000000
75%	1.000000	1.000000	1.000000	1.000000	1.000000
max	1.000000	1.000000	1.000000	1.000000	1.000000
	TIMAVO				
count	10000.00000				
mean	0.961700				
std	0.191929				
min	0.000000				
25%	1.000000				
50%	1.000000				
75%	1.000000				
max	1.000000				

```
[24]: aux_results.loc['mean',:].plot(kind='barh', figsize=(15,15), xticks=np.linspace(0,1,11))
#res = plt.xticks(rotation = 30)
```

[24]: <AxesSubplot: >



```
[25]: pd.set_option('display.max_columns', 500)
aux_results = pd.DataFrame(ritorno['inference_data'].posterior.
    ↪is_over_annual_limit.values.
    ↪reshape((aux_shape[0]*aux_shape[1],aux_shape[2])), columns=df.columns).
    ↪describe()
aux_results.sort_values('mean', axis=1, ascending=True)
```

```
[25]:      CASTELLUCCIO      ROMA  CASTELLARANO  PARCO EDILCARANI  DELTA CERVIA \
count    10000.0    10000.0    10000.0    10000.0    10000.0
mean      0.0        0.0        0.0        0.0        0.0
std       0.0        0.0        0.0        0.0        0.0
min       0.0        0.0        0.0        0.0        0.0
25%       0.0        0.0        0.0        0.0        0.0
50%       0.0        0.0        0.0        0.0        0.0
75%       0.0        0.0        0.0        0.0        0.0
```

max	0.0	0.0	0.0	0.0	0.0	0.0	0.0
count	10000.0		10000.0	10000.0	10000.0		10000.0
mean	0.0		0.0	0.0	0.0		0.0
std	0.0		0.0	0.0	0.0		0.0
min	0.0		0.0	0.0	0.0		0.0
25%	0.0		0.0	0.0	0.0		0.0
50%	0.0		0.0	0.0	0.0		0.0
75%	0.0		0.0	0.0	0.0		0.0
max	0.0		0.0	0.0	0.0		0.0
count	10000.0	10000.0	10000.0	10000.0	10000.0	10000.0	10000.0
mean	0.0	0.0	0.0	0.0	0.0	0.0	0.0
std	0.0	0.0	0.0	0.0	0.0	0.0	0.0
min	0.0	0.0	0.0	0.0	0.0	0.0	0.0
25%	0.0	0.0	0.0	0.0	0.0	0.0	0.0
50%	0.0	0.0	0.0	0.0	0.0	0.0	0.0
75%	0.0	0.0	0.0	0.0	0.0	0.0	0.0
max	0.0	0.0	0.0	0.0	0.0	0.0	0.0
count	10000.0		10000.0	10000.0	10000.0	10000.0	10000.0
mean	0.0		0.0	0.0	0.0	0.0	0.0
std	0.0		0.0	0.0	0.0	0.0	0.0
min	0.0		0.0	0.0	0.0	0.0	0.0
25%	0.0		0.0	0.0	0.0	0.0	0.0
50%	0.0		0.0	0.0	0.0	0.0	0.0
75%	0.0		0.0	0.0	0.0	0.0	0.0
max	0.0		0.0	0.0	0.0	0.0	0.0
count	10000.0		10000.0	10000.0	10000.0	10000.0	10000.0
mean	0.0		0.0	0.0	0.0	0.0	0.0
std	0.0		0.0	0.0	0.0	0.0	0.0
min	0.0		0.0	0.0	0.0	0.0	0.0
25%	0.0		0.0	0.0	0.0	0.0	0.0
50%	0.0		0.0	0.0	0.0	0.0	0.0
75%	0.0		0.0	0.0	0.0	0.0	0.0
max	0.0		0.0	0.0	0.0	0.0	0.0
count	10000.0	10000.0	10000.0		10000.0		10000.0
mean	0.0	0.0	0.0		0.0		0.0
std	0.0	0.0	0.0		0.0		0.0
min	0.0	0.0	0.0		0.0		0.0
25%	0.0	0.0	0.0		0.0		0.0
50%	0.0	0.0	0.0		0.0		0.0
75%	0.0	0.0	0.0		0.0		0.0
max	0.0	0.0	0.0		0.0		0.0
count	10000.0	10000.0	10000.0		10000.0		10000.0
mean	0.0	0.0	0.0		0.0		0.0
std	0.0	0.0	0.0		0.0		0.0
min	0.0	0.0	0.0		0.0		0.0
25%	0.0	0.0	0.0		0.0		0.0
50%	0.0	0.0	0.0		0.0		0.0
75%	0.0	0.0	0.0		0.0		0.0
max	0.0	0.0	0.0		0.0		0.0
count	10000.0	10000.0	10000.0		10000.0		10000.0
mean	0.0	0.0	0.0		0.0		0.0
std	0.0	0.0	0.0		0.0		0.0
min	0.0	0.0	0.0		0.0		0.0
25%	0.0	0.0	0.0		0.0		0.0
50%	0.0	0.0	0.0		0.0		0.0
75%	0.0	0.0	0.0		0.0		0.0
max	0.0	0.0	0.0		0.0		0.0

25%	0.0	0.0	0.0	0.0	0.0
50%	0.0	0.0	0.0	0.0	0.0
75%	0.0	0.0	0.0	0.0	0.0
max	0.0	0.0	0.0	0.0	0.0

	PARCO	RESISTENZA	VILLA FULVIA	MALCANTONE	SAVIGNANO	S. LAZZARO	\
count		10000.0	10000.0000	10000.0000	10000.0000	10000.0000	
mean		0.0	0.0001	0.0001	0.0001	0.0001	
std		0.0	0.0100	0.0100	0.0100	0.0100	
min		0.0	0.0000	0.0000	0.0000	0.0000	
25%		0.0	0.0000	0.0000	0.0000	0.0000	
50%		0.0	0.0000	0.0000	0.0000	0.0000	
75%		0.0	0.0000	0.0000	0.0000	0.0000	
max		0.0	1.0000	1.0000	1.0000	1.0000	

	CENO	ISONZO	PARADIGNA	SAN FRANCESCO	PARCO FERRARI	\
count	10000.0000	10000.000000	10000.000000	10000.000000	10000.000000	
mean	0.0001	0.000200	0.000200	0.000300	0.000400	
std	0.0100	0.014141	0.014141	0.017319	0.019997	
min	0.0000	0.000000	0.000000	0.000000	0.000000	
25%	0.0000	0.000000	0.000000	0.000000	0.000000	
50%	0.0000	0.000000	0.000000	0.000000	0.000000	
75%	0.0000	0.000000	0.000000	0.000000	0.000000	
max	1.0000	1.000000	1.000000	1.000000	1.000000	

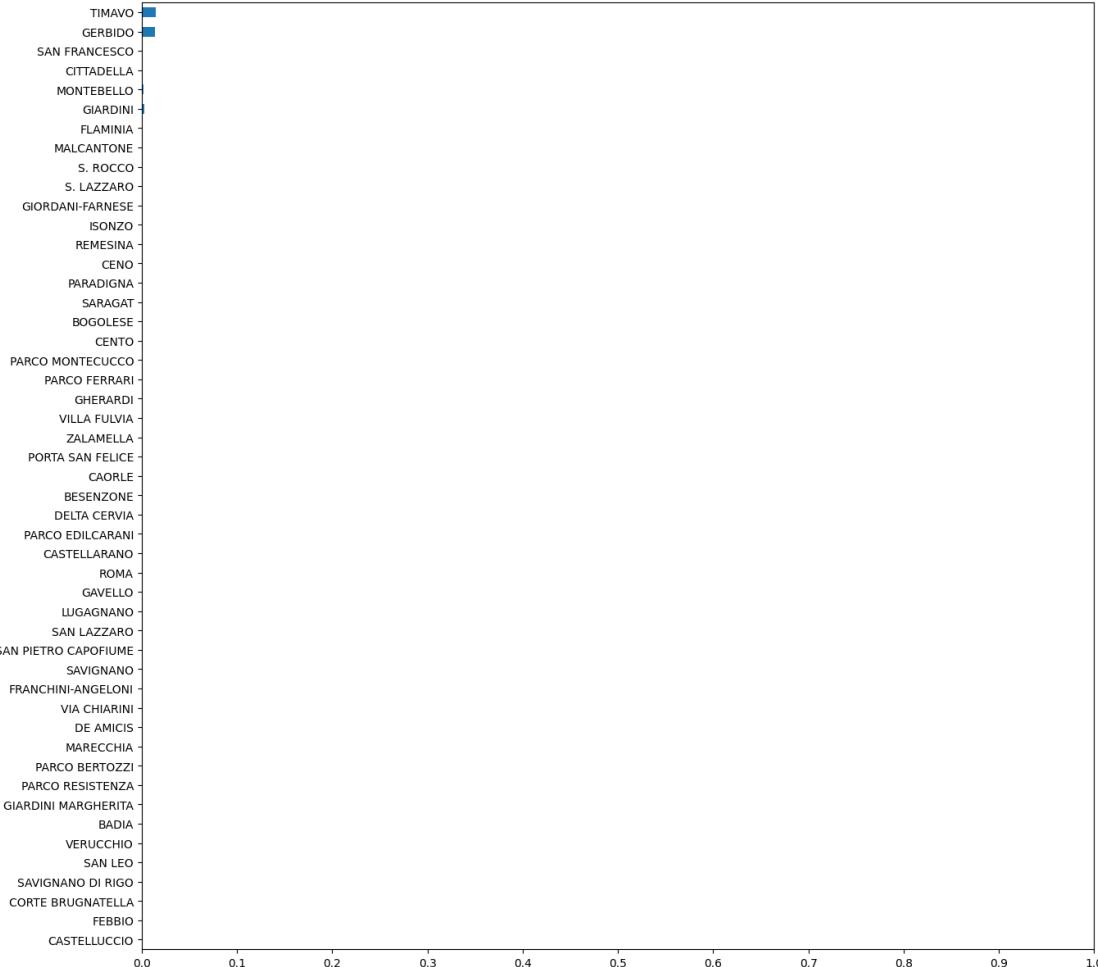
	GIORDANI-FARNESE	CITTADELLA	FLAMINIA	MONTEBELLO	\
count	10000.000000	10000.000000	10000.000000	10000.000000	
mean	0.000400	0.000600	0.001400	0.001700	
std	0.019997	0.024489	0.037392	0.041198	
min	0.000000	0.000000	0.000000	0.000000	
25%	0.000000	0.000000	0.000000	0.000000	
50%	0.000000	0.000000	0.000000	0.000000	
75%	0.000000	0.000000	0.000000	0.000000	
max	1.000000	1.000000	1.000000	1.000000	

	GIARDINI	GERBIDO	TIMAVO
count	10000.000000	10000.000000	10000.000000
mean	0.002400	0.014100	0.014600
std	0.048933	0.117909	0.119951
min	0.000000	0.000000	0.000000
25%	0.000000	0.000000	0.000000
50%	0.000000	0.000000	0.000000
75%	0.000000	0.000000	0.000000
max	1.000000	1.000000	1.000000

```
[26]: aux_results.loc['mean', :].plot(kind='barh', figsize=(15,15), xticks=np.linspace(0,1,11))
```

```
#res = plt.xticks(rotation = 30)
```

[26]: <AxesSubplot: >



```
[27]: y_post_pred = ritorno['inference_data'].posterior.y_post_pred.to_numpy()
y_post_pred = y_post_pred.reshape(y_post_pred.shape[0]*y_post_pred.shape[1],  
                                 ↪y_post_pred.shape[2], y_post_pred.shape[3])
y_post_pred.shape
```

[27]: (10000, 365, 49)

```
[28]: import ipywidgets as widgets
from ipywidgets import HBox, VBox
from IPython.display import display
```

```
[29]: @widgets.interact(stazione = df.columns)
def f(stazione):
    col_map = sns.light_palette((20, 75, 70), input='husl', as_cmap=True)

    plt.figure(figsize=(14,8))
    ax = plt.subplot(1,1,1)

    idx_stazione = df.columns.to_list().index(stazione)

    """
    sns.lineplot(np.transpose(y_post_pred[0:50,:,:idx_stazione]))
    """

    lower_lim = np.zeros(len(df.index))
    upper_lim = np.zeros(len(df.index))
    for i in range(len(df.index)):
        lower_lim[i] = np.percentile(y_post_pred[:,i,idx_stazione],2.5)
        upper_lim[i] = np.percentile(y_post_pred[:,i,idx_stazione],97.5)

    # sns.lineplot(lower_lim)
    # sns.lineplot(upper_lim)

    for i in range(len(df.index)):
        ax.add_patch(mplt.patches.Rectangle((i,lower_lim[i]),1,upper_lim[i]-lower_lim[i], fill=True,color=col_map(180)))

    sns.lineplot(df[stazione])
    sns.lineplot(np.mean(y_post_pred[:, :, idx_stazione], axis=0))

    index = 0
    for line in ax.get_lines():
        if index == 0:
            col_map = sns.dark_palette((230,90,65), input='husl', as_cmap=True)
            line.set_c(col_map(155))
        else:
            col_map = sns.dark_palette((10,90,65), input='husl', as_cmap=True)
            line.set_c(col_map(175))
        index += 1

    plt.ylim(bottom=0,top=2.5)

    primo_giorno = datetime.date(2018,1,1)
    date_da_segnare = []
    date_da_segnare_posizioni = []
```

```

for i in range(12):
    date_da_segnare.append(datetime.date(2018,i+1,1))
    date_da_segnare_posizioni.append((date_da_segnare[2*i] - primo_giorno).
    ↵days)
    date_da_segnare.append(datetime.date(2018,i+1,15))
    date_da_segnare_posizioni.append((date_da_segnare[2*i+1] -
    ↵primo_giorno).days)
    date_da_segnare[2*i] = date_da_segnare[2*i].isoformat()
    date_da_segnare[2*i+1] = date_da_segnare[2*i+1].isoformat()

plt.xticks(date_da_segnare_posizioni,date_da_segnare,rotation=65)
plt.tick_params(
    axis='x',          # changes apply to the x-axis
    which='both',      # both major and minor ticks are affected
    bottom=True,       # ticks along the bottom edge are off
    top=False,         # ticks along the top edge are off
    labelbottom=True)
plt.grid()

"""
ax.get_legend().remove()
col_vals = np.linspace(1,255,num=len(df.columns))
index = 0
for line in ax.get_lines():
    if(index == len(ax.get_lines()) - 1):
        col_map = sns.dark_palette((230,90,65), input='husl', as_cmap=True)
        line.set_c(col_map(175))
        continue
    if(index == len(ax.get_lines()) - 2):
        col_map = sns.dark_palette((120,90,65), input='husl', as_cmap=True)
        line.set_c(col_map(175))
        index += 1
        continue

    #line.set_c(col_map(int(np.round(col_vals[index]))))
    line.set_c(col_map(220))
    line.set_alpha(0.3)
    index += 1
"""

plt.show()

interactive(children=(Dropdown(description='stazione', options=('CASTELLUCCIO', 'FEBBIO', 'CORTE BRUGNATELLA',...

```

```
[30]: def f(stazione):
    col_map = sns.light_palette((20, 75, 70), input='husl', as_cmap=True)

    plt.figure(figsize=(14,8))
    ax = plt.subplot(1,1,1)

    idx_stazione = df.columns.to_list().index(stazione)

    """
    sns.lineplot(np.transpose(y_post_pred[0:50,:,:idx_stazione]))
    """

    lower_lim = np.zeros(len(df.index))
    upper_lim = np.zeros(len(df.index))
    for i in range(len(df.index)):
        lower_lim[i] = np.percentile(y_post_pred[:,i,idx_stazione],2.5)
        upper_lim[i] = np.percentile(y_post_pred[:,i,idx_stazione],97.5)

    # sns.lineplot(lower_lim)
    # sns.lineplot(upper_lim)

    for i in range(len(df.index)):
        ax.add_patch(mplt.patches.Rectangle((i,lower_lim[i]),1,upper_lim[i]-lower_lim[i], fill=True,color=col_map(180)))

    sns.lineplot(df[stazione])
    sns.lineplot(np.mean(y_post_pred[:, :, idx_stazione], axis=0))

    index = 0
    for line in ax.get_lines():
        if index == 0:
            col_map = sns.dark_palette((230,90,65), input='husl', as_cmap=True)
            line.set_c(col_map(155))
        else:
            col_map = sns.dark_palette((10,90,65), input='husl', as_cmap=True)
            line.set_c(col_map(175))
        index += 1

    plt.ylim(bottom=0,top=2.5)

    primo_giorno = datetime.date(2018,1,1)
    date_da_segnare = []
    date_da_segnare_posizioni = []
```

```

for i in range(12):
    date_da_segnare.append(datetime.date(2018,i+1,1))
    date_da_segnare_posizioni.append((date_da_segnare[2*i] - primo_giorno).
days)
    date_da_segnare.append(datetime.date(2018,i+1,15))
    date_da_segnare_posizioni.append((date_da_segnare[2*i+1] - primo_giorno).days)
    date_da_segnare[2*i] = date_da_segnare[2*i].isoformat()
    date_da_segnare[2*i+1] = date_da_segnare[2*i+1].isoformat()

plt.xticks(date_da_segnare_posizioni,date_da_segnare,rotation=65)
plt.tick_params(
    axis='x',          # changes apply to the x-axis
    which='both',      # both major and minor ticks are affected
    bottom=True,       # ticks along the bottom edge are off
    top=False,         # ticks along the top edge are off
    labelbottom=True)
plt.grid()

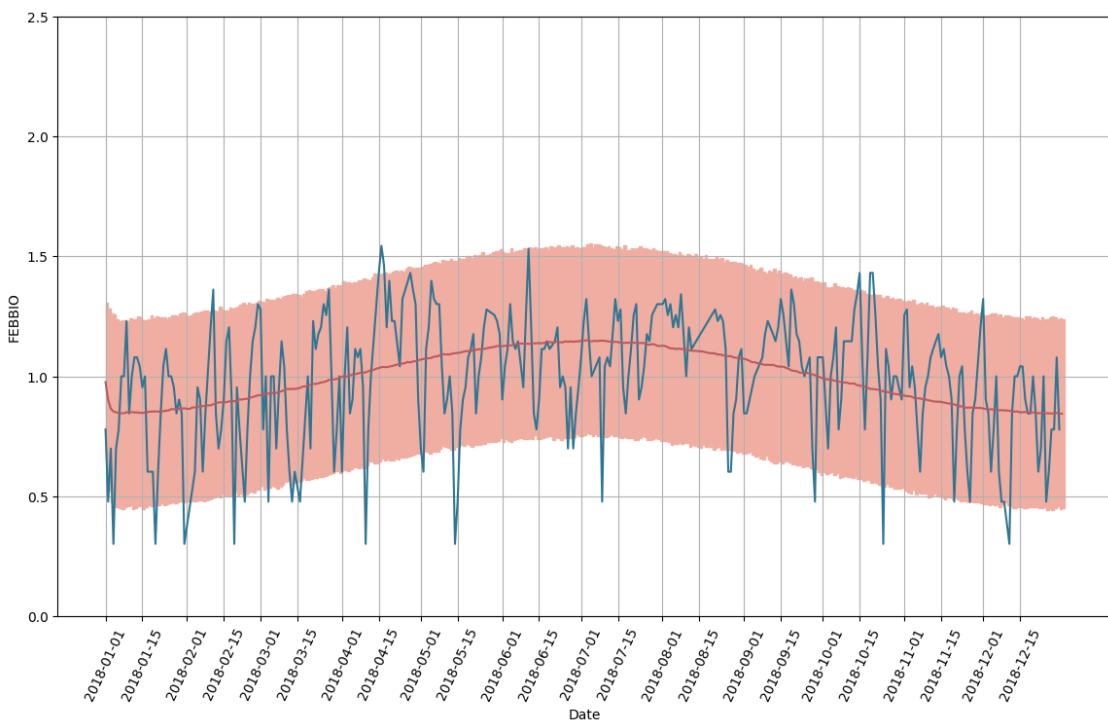
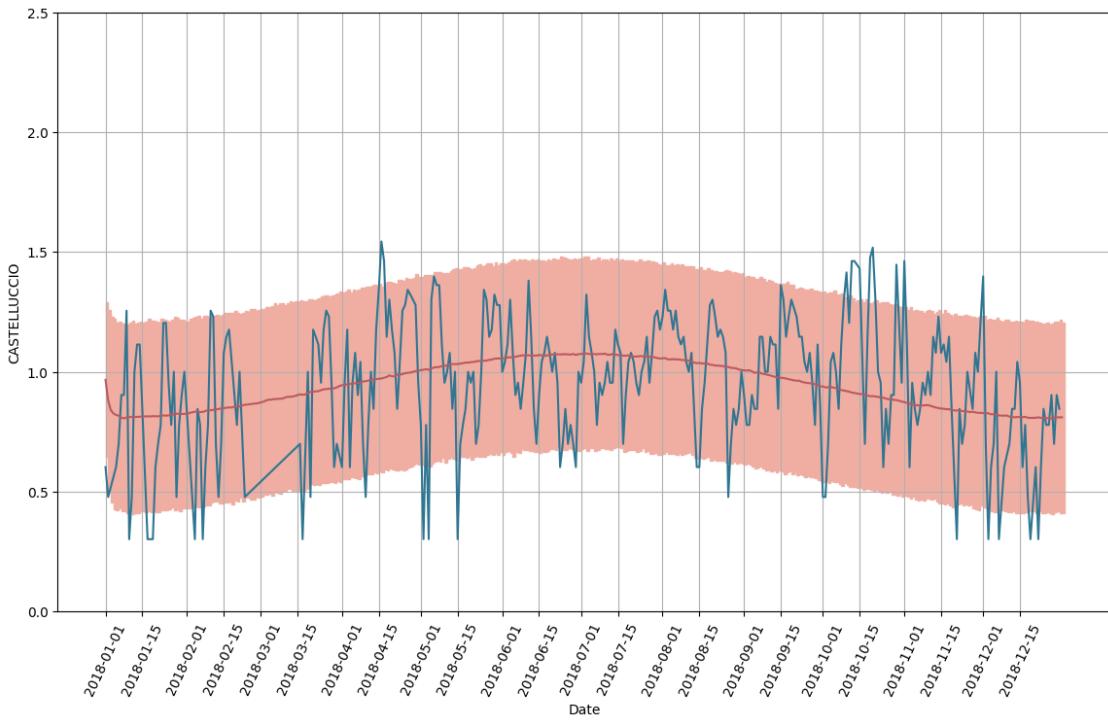
"""
ax.get_legend().remove()
col_vals = np.linspace(1,255,num=len(df.columns))
index = 0
for line in ax.get_lines():
    if(index == len(ax.get_lines()) - 1):
        col_map = sns.dark_palette((230,90,65), input='husl', as_cmap=True)
        line.set_c(col_map(175))
        continue
    if(index == len(ax.get_lines()) - 2):
        col_map = sns.dark_palette((120,90,65), input='husl', as_cmap=True)
        line.set_c(col_map(175))
        index += 1
        continue

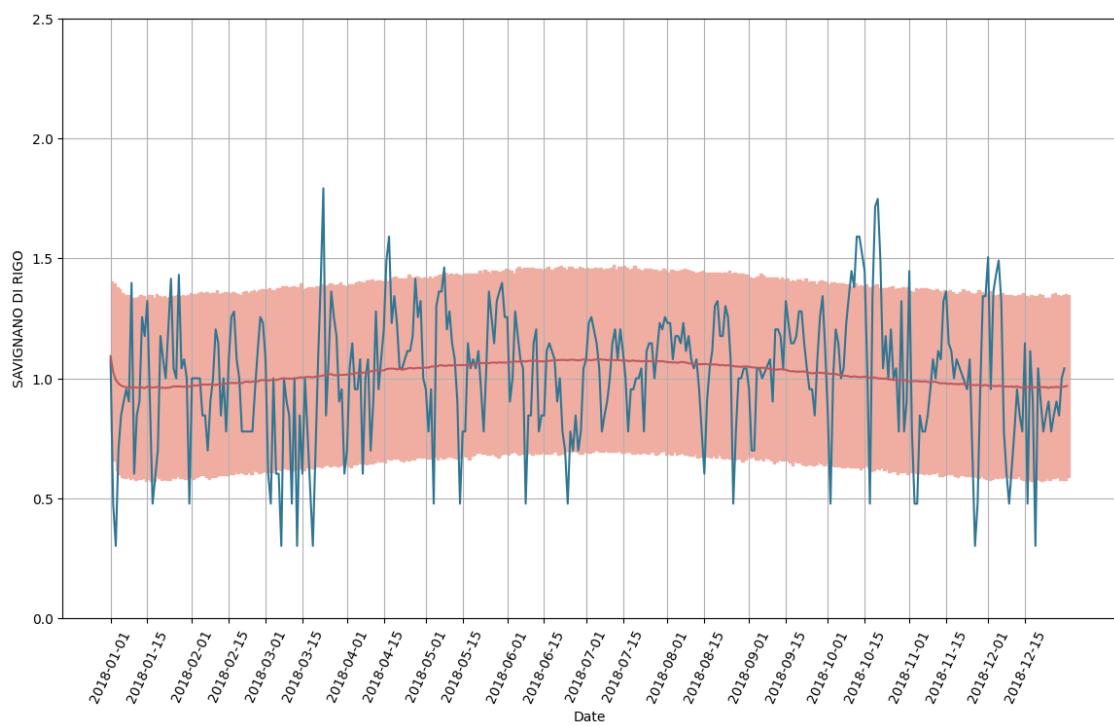
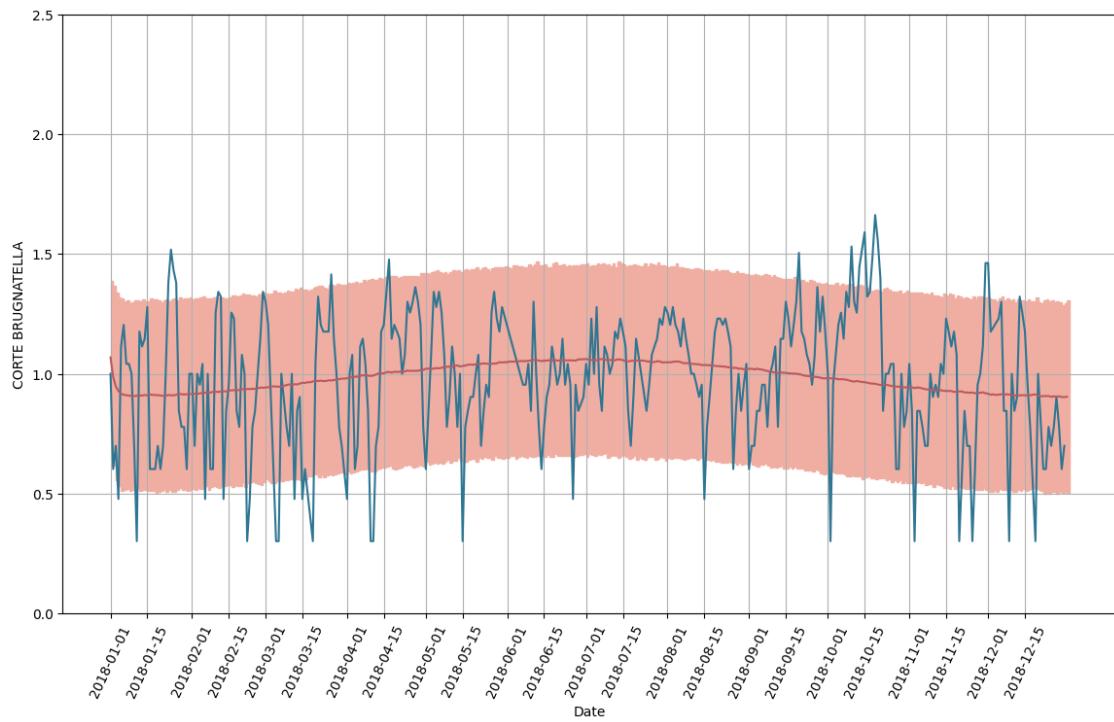
    #line.set_c(col_map(int(np.round(col_vals[index]))))
    line.set_c(col_map(220))
    line.set_alpha(0.3)
    index += 1
"""

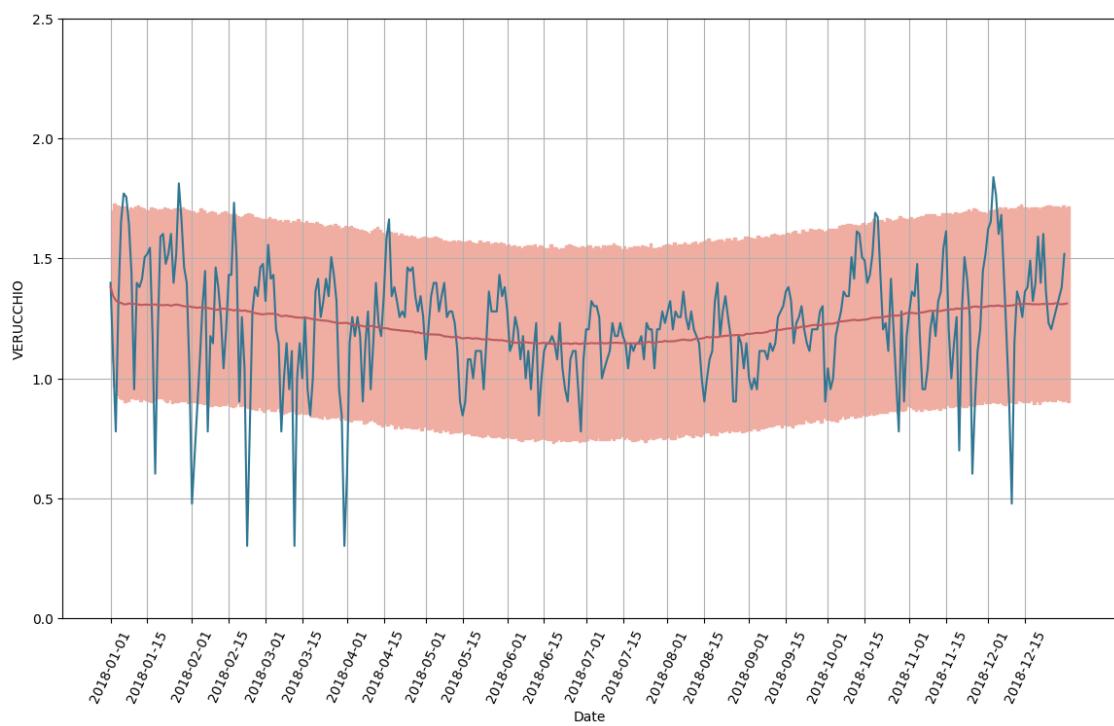
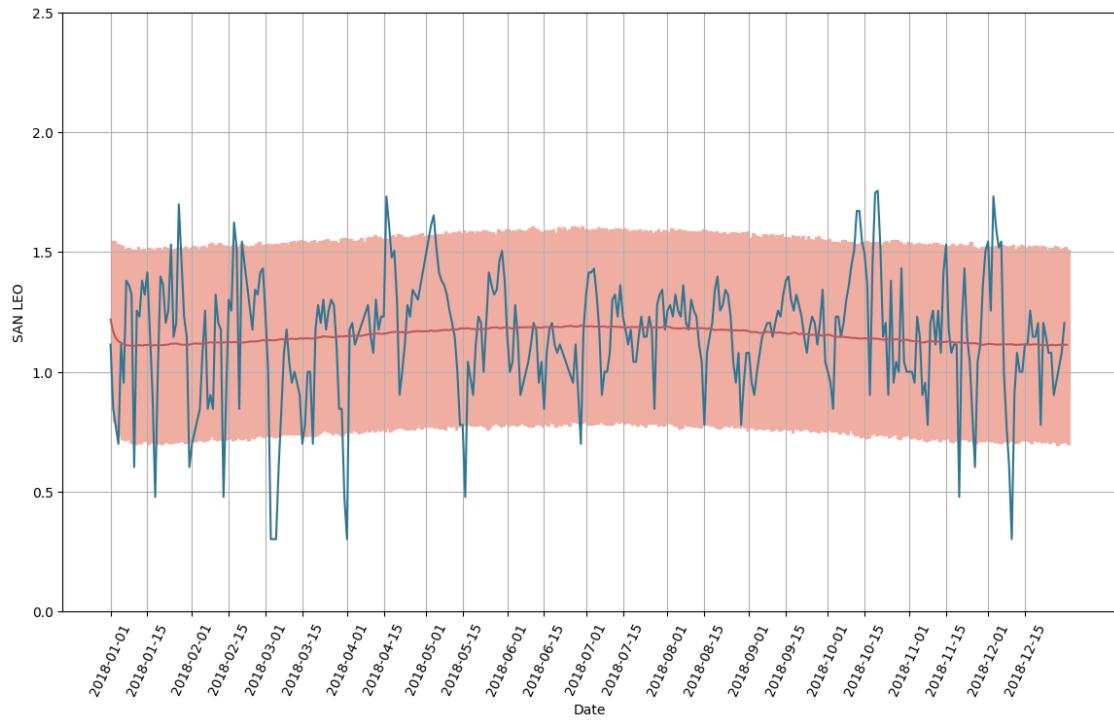
plt.show()

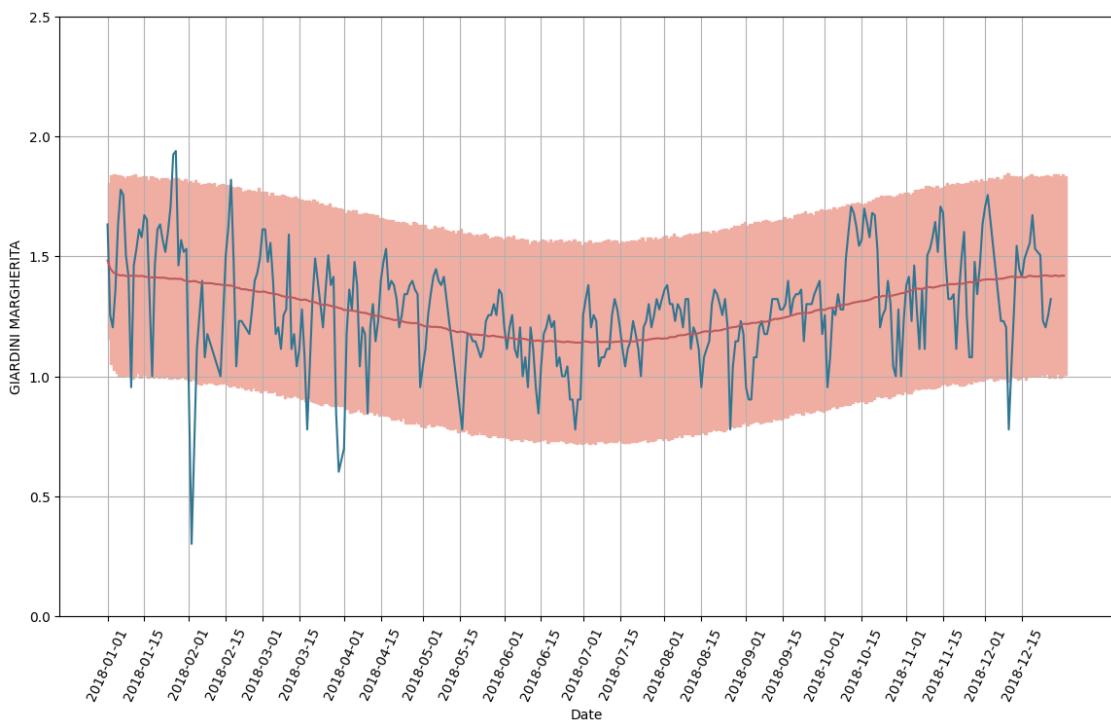
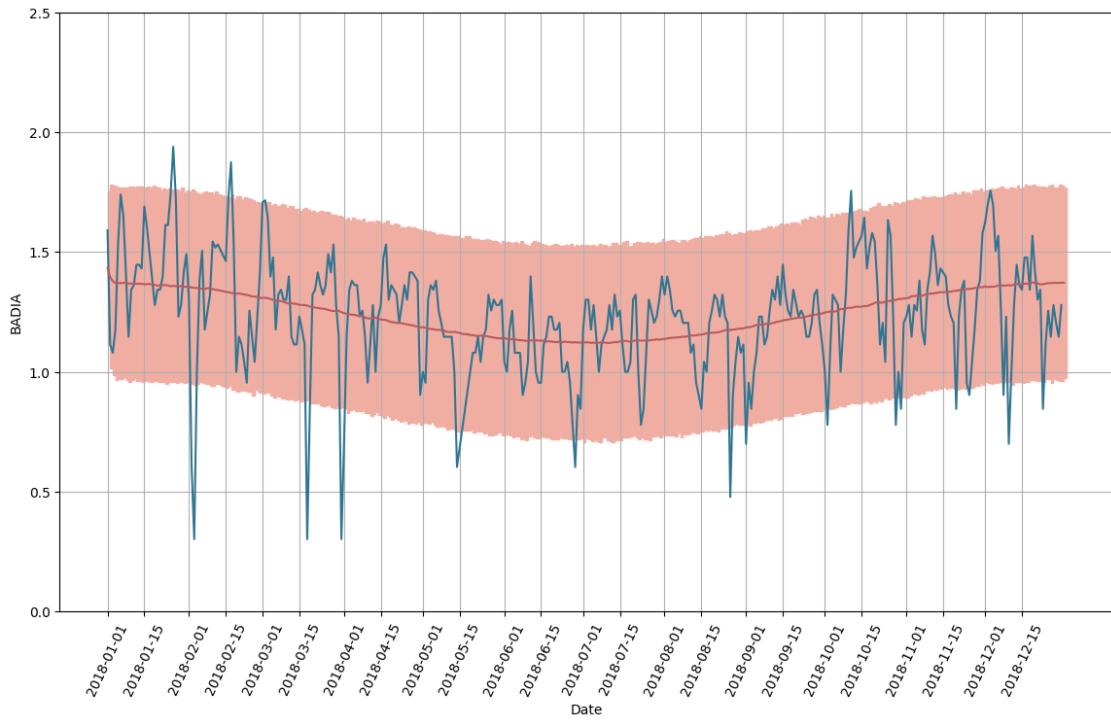
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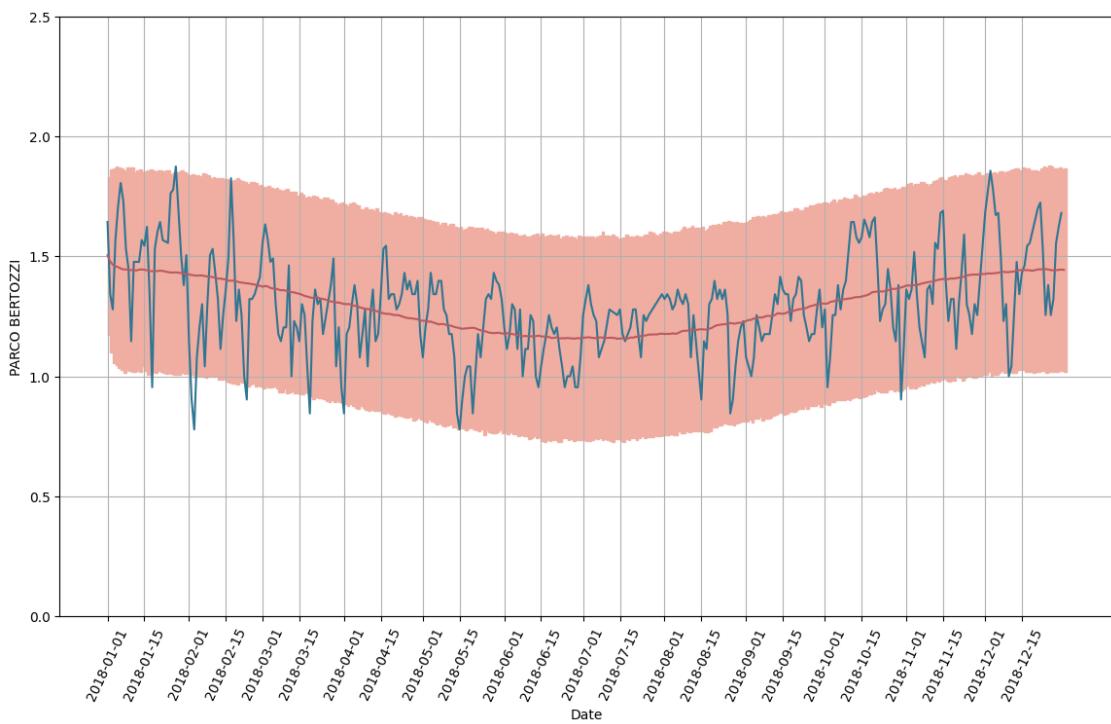
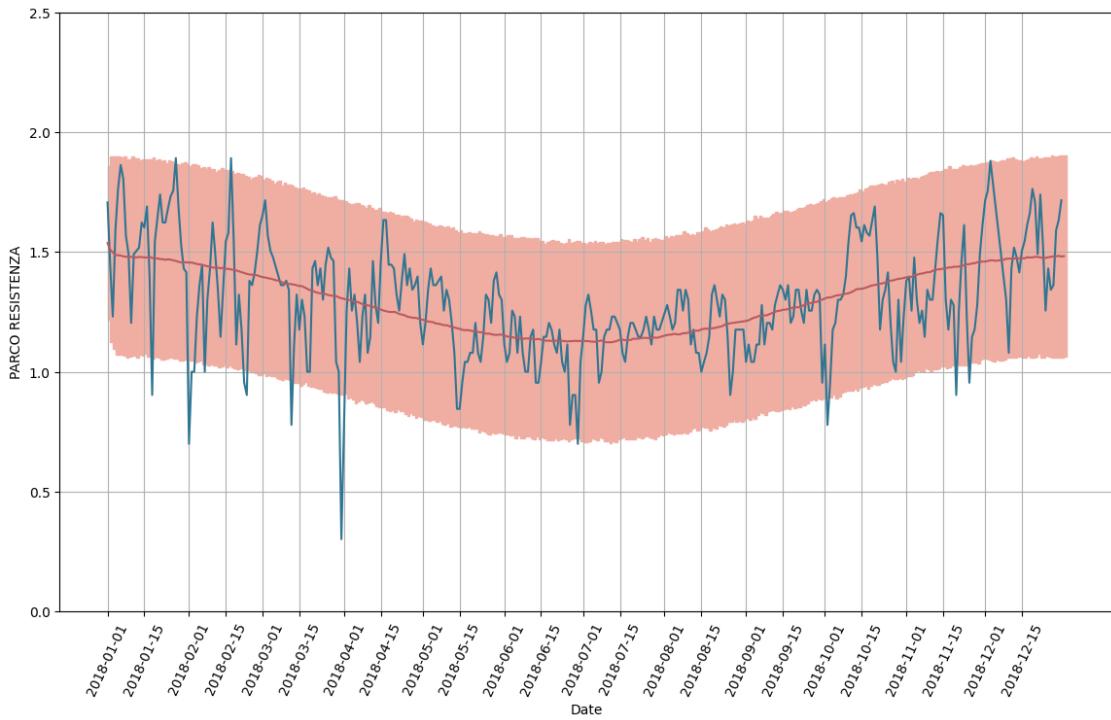
[31]: `for stazione in df.columns:
f(stazione)`

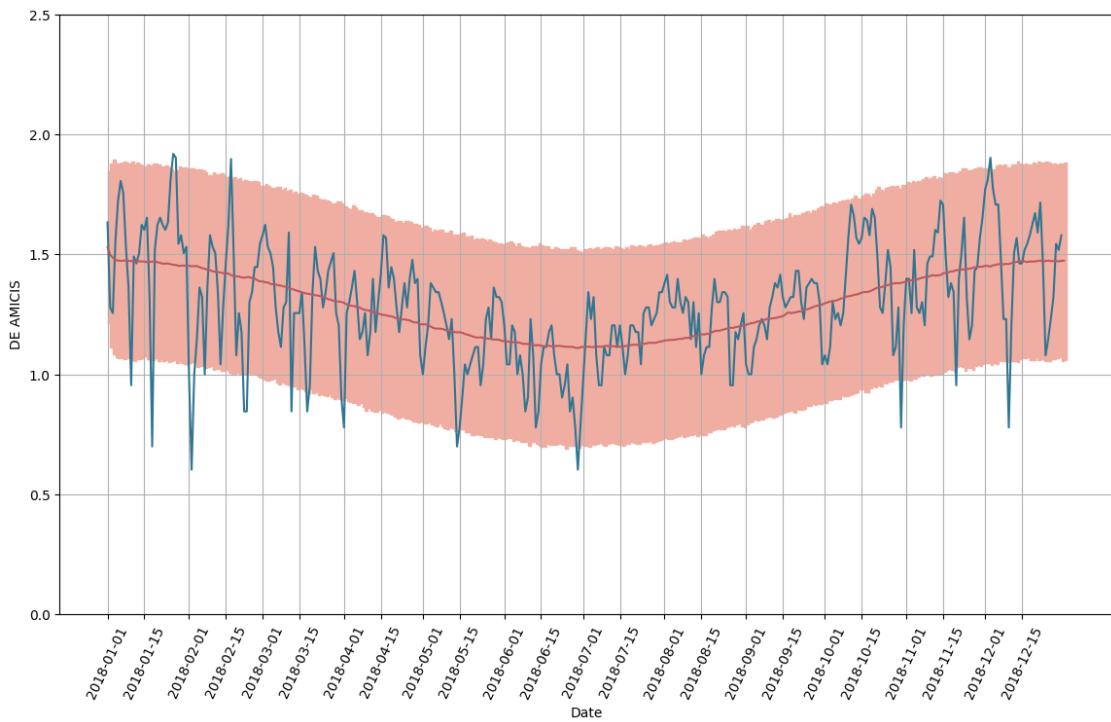
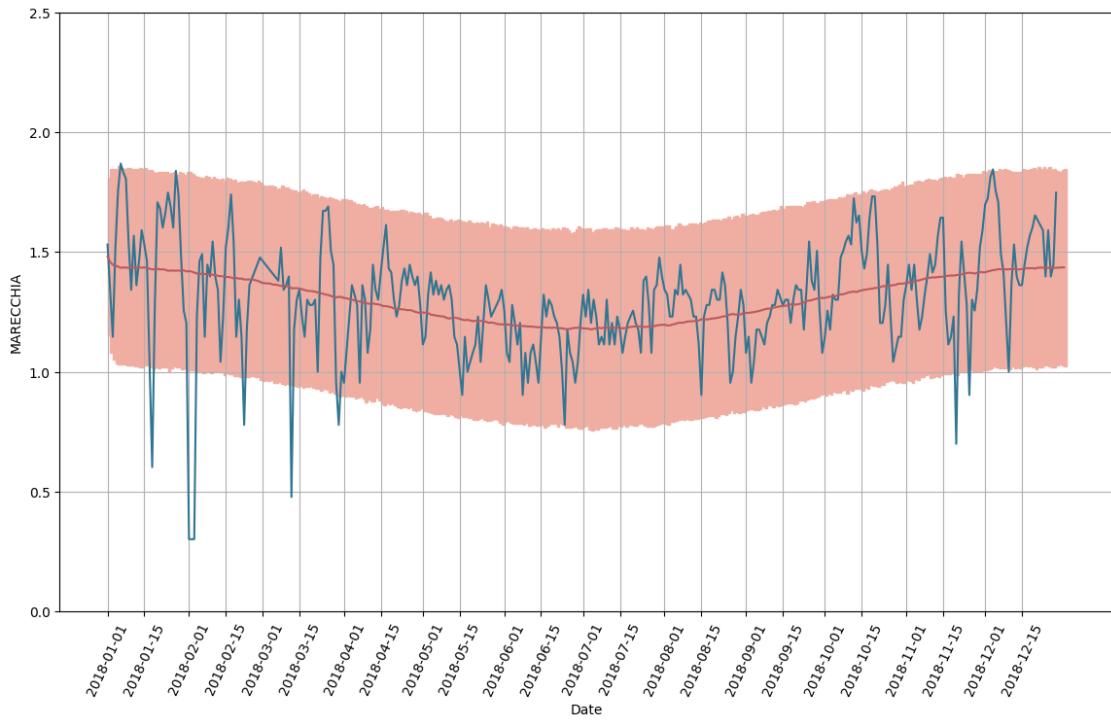


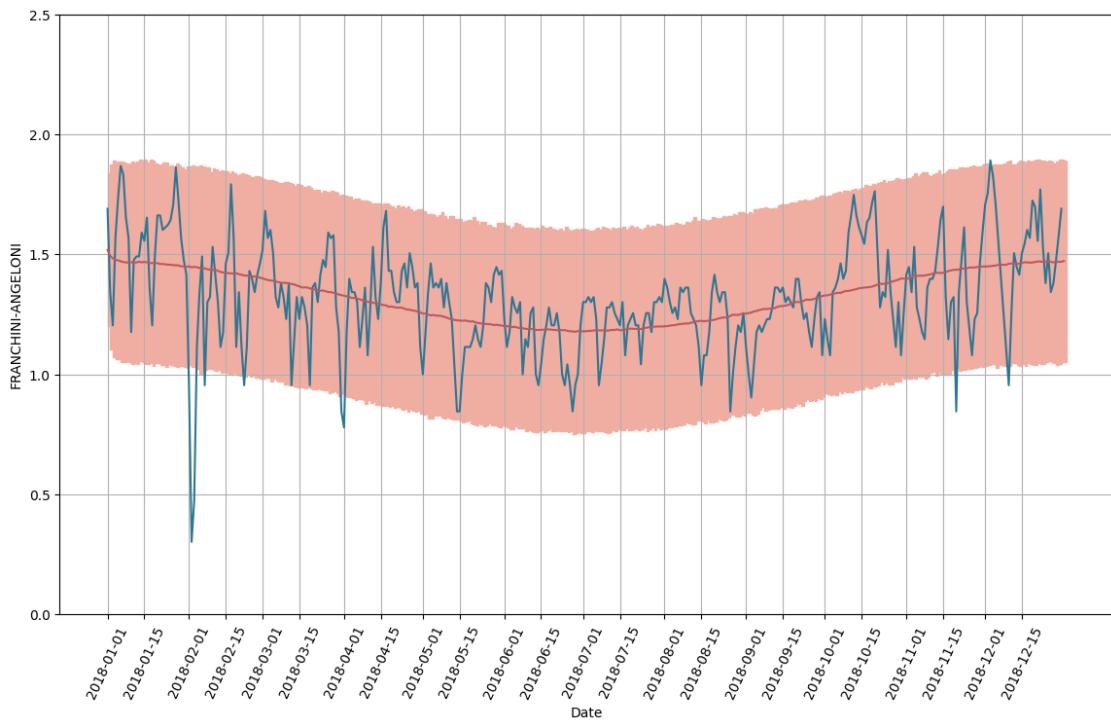
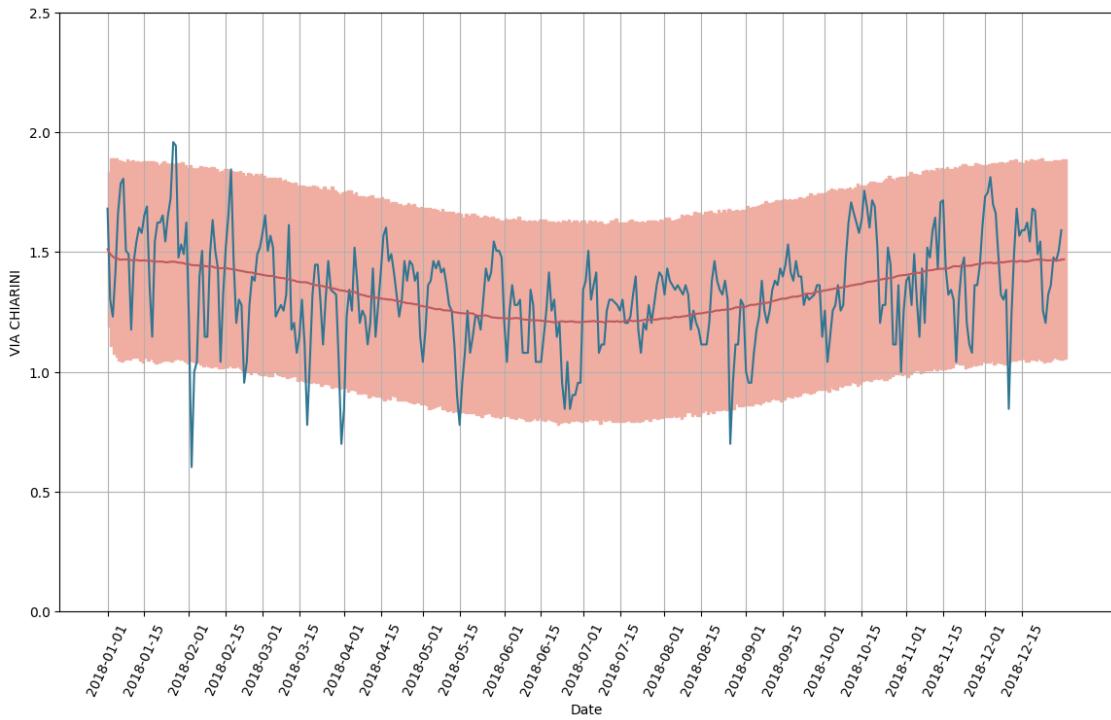


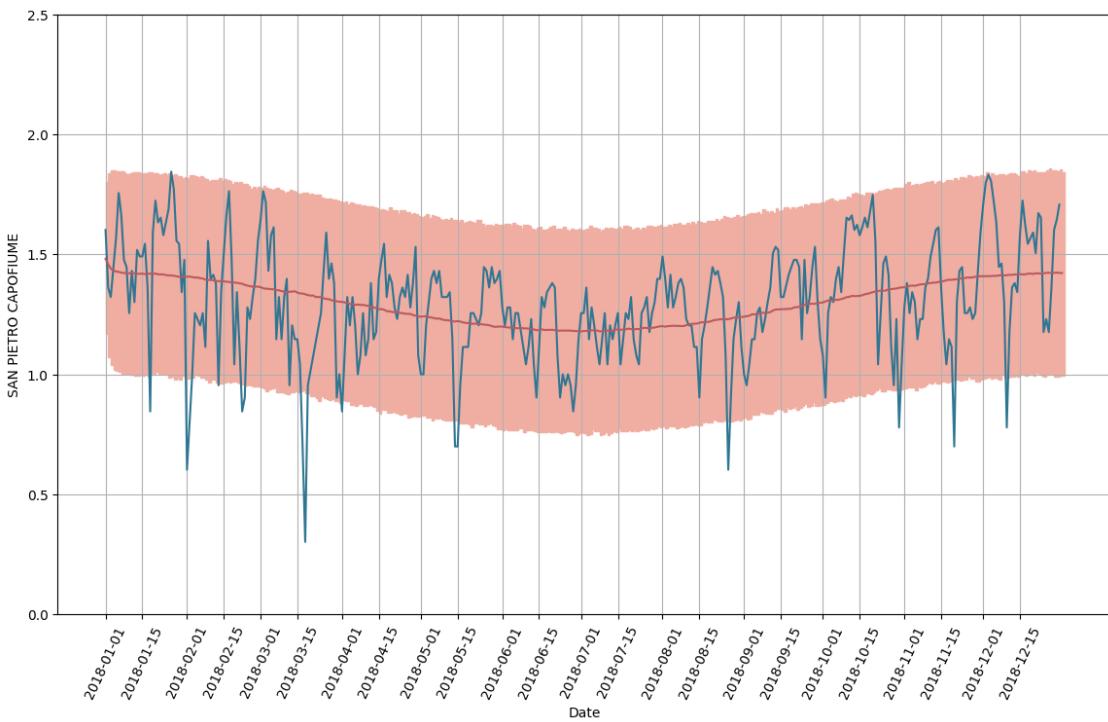
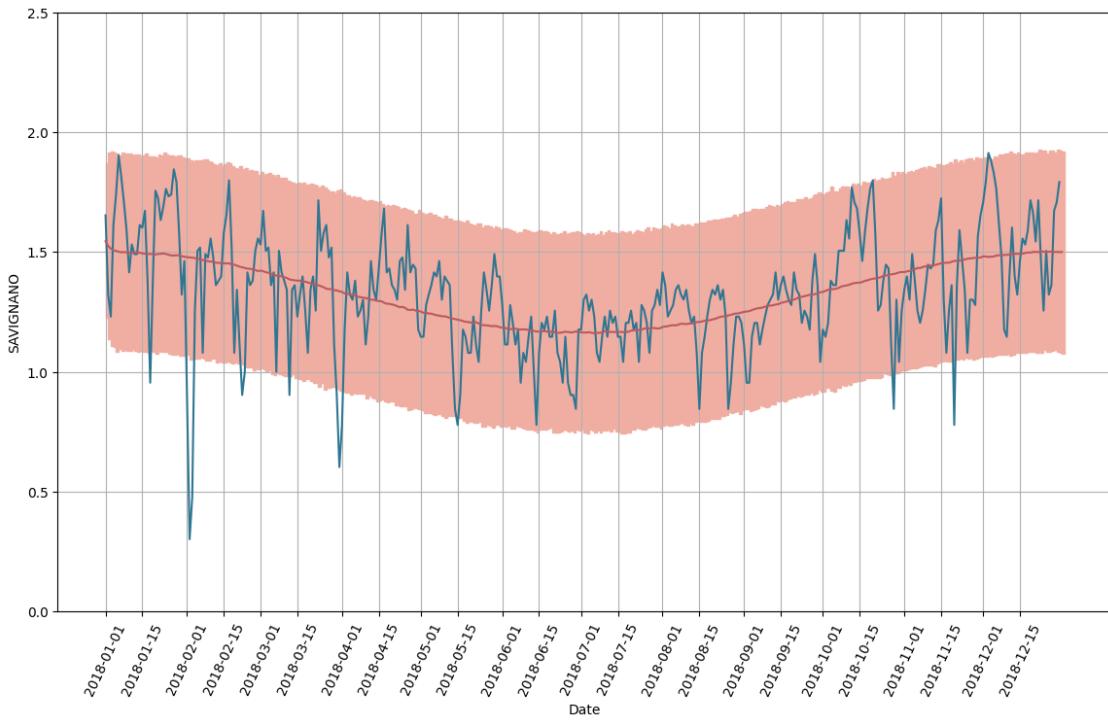


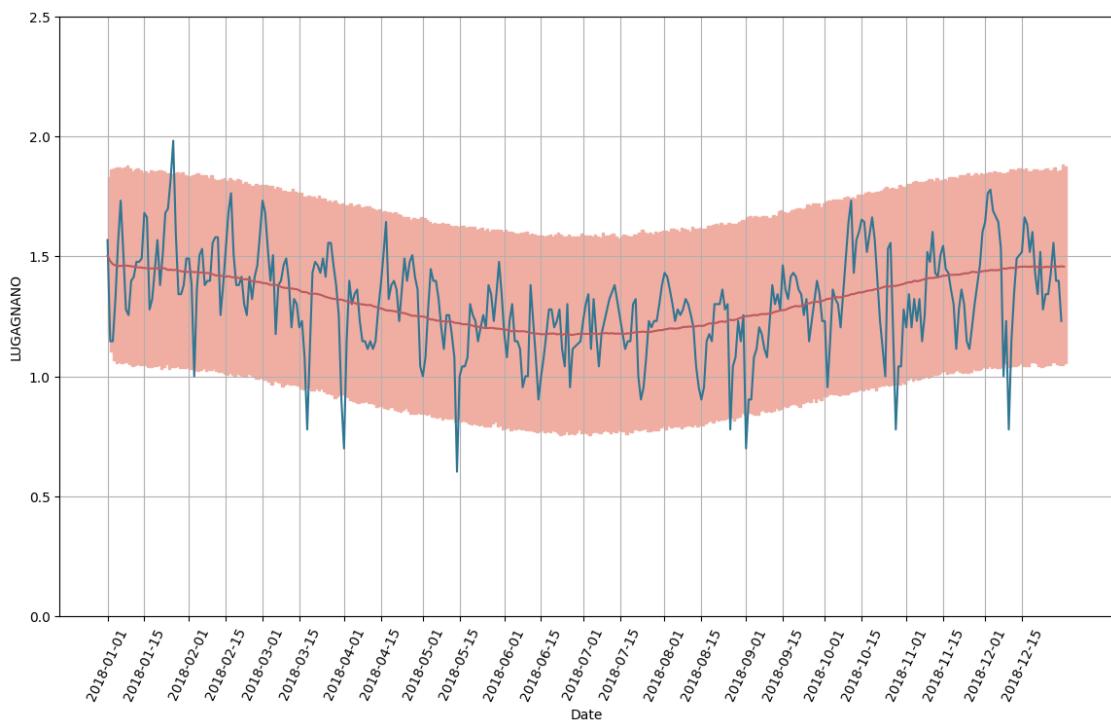
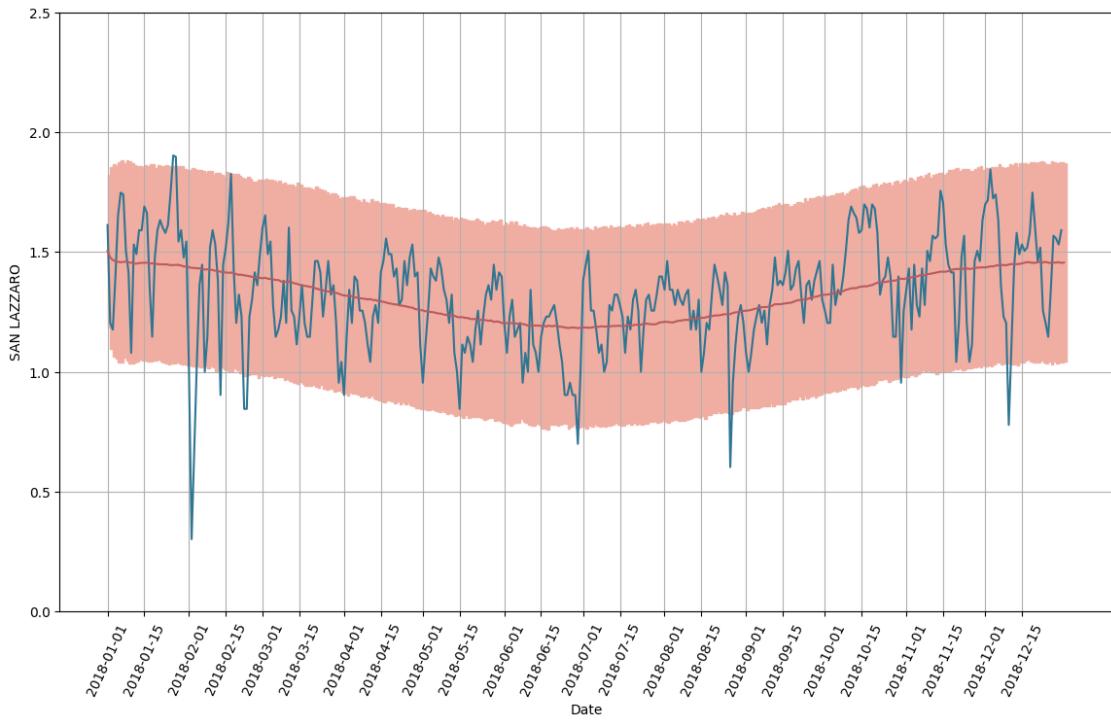


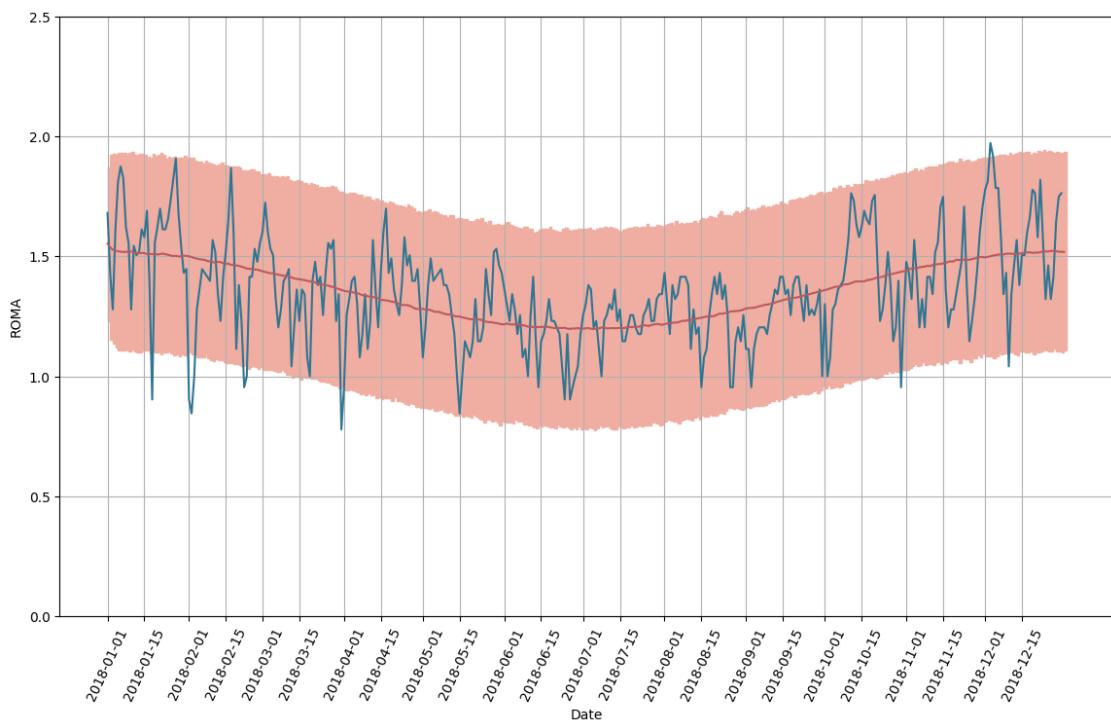
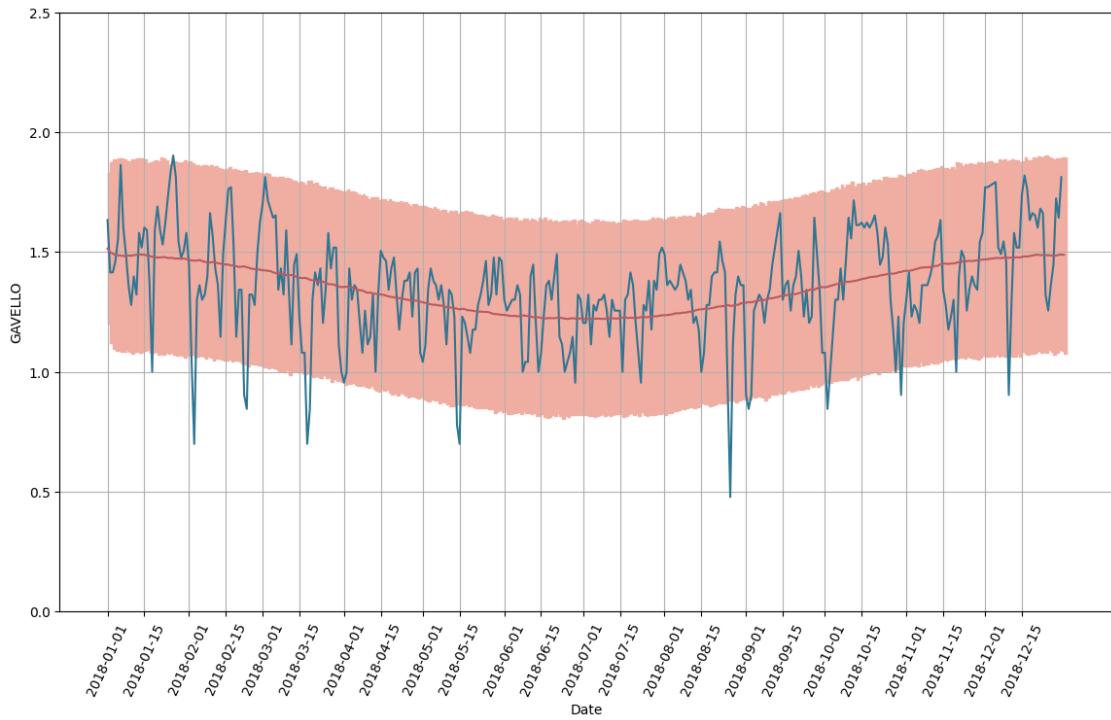


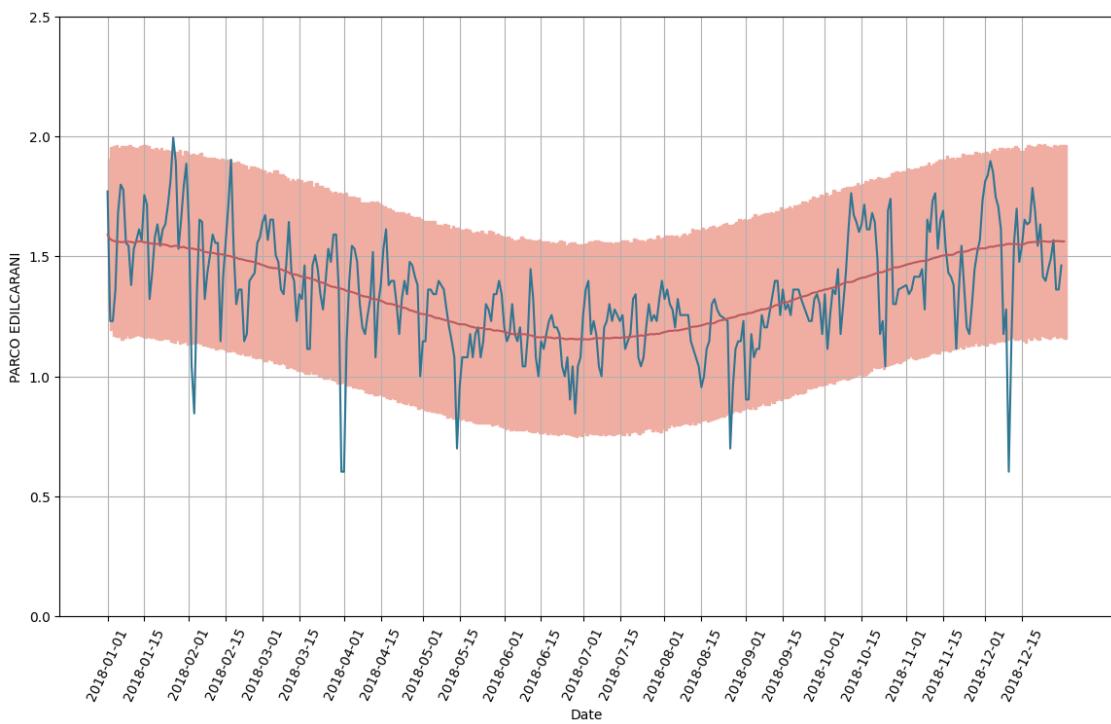
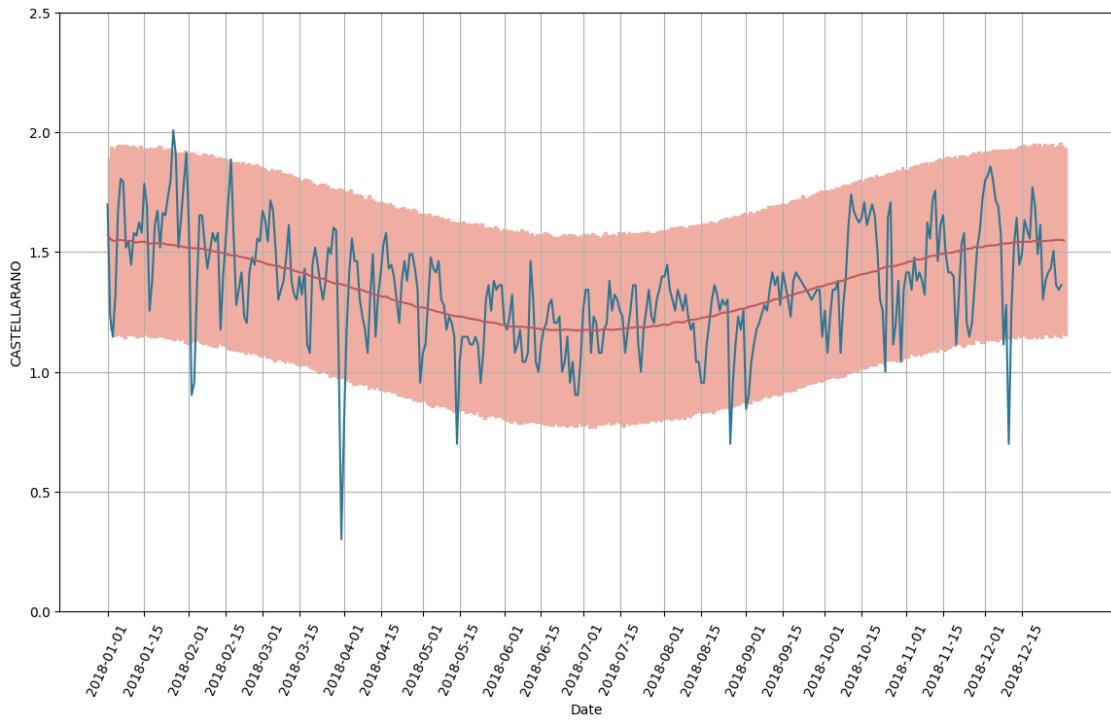


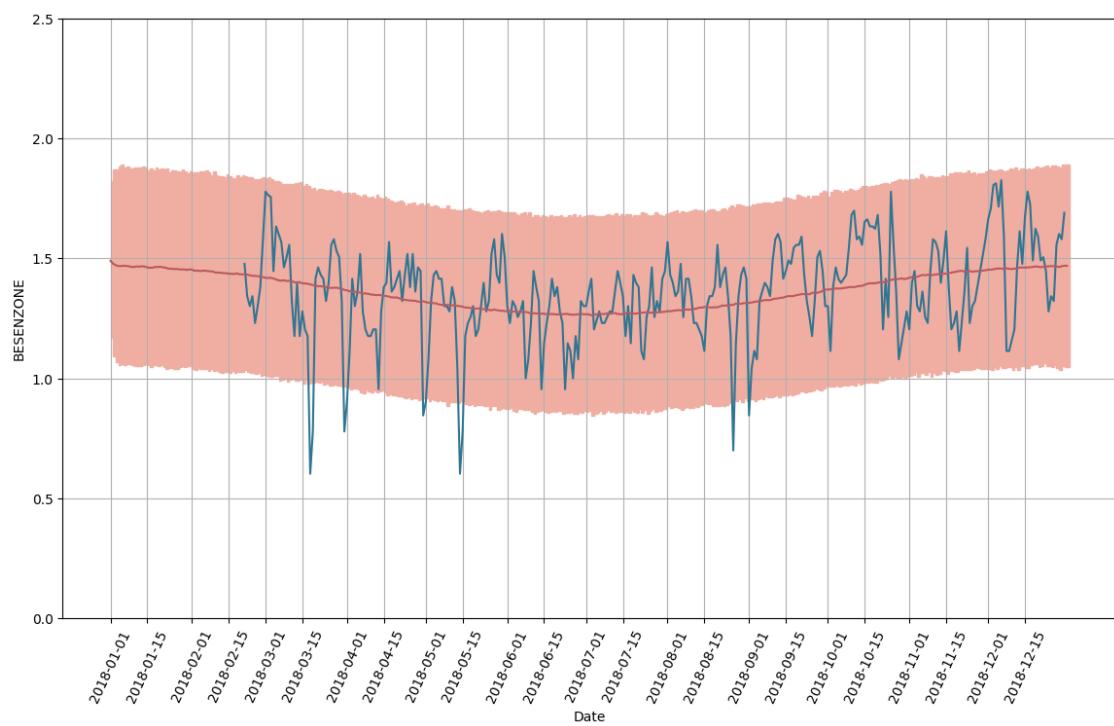
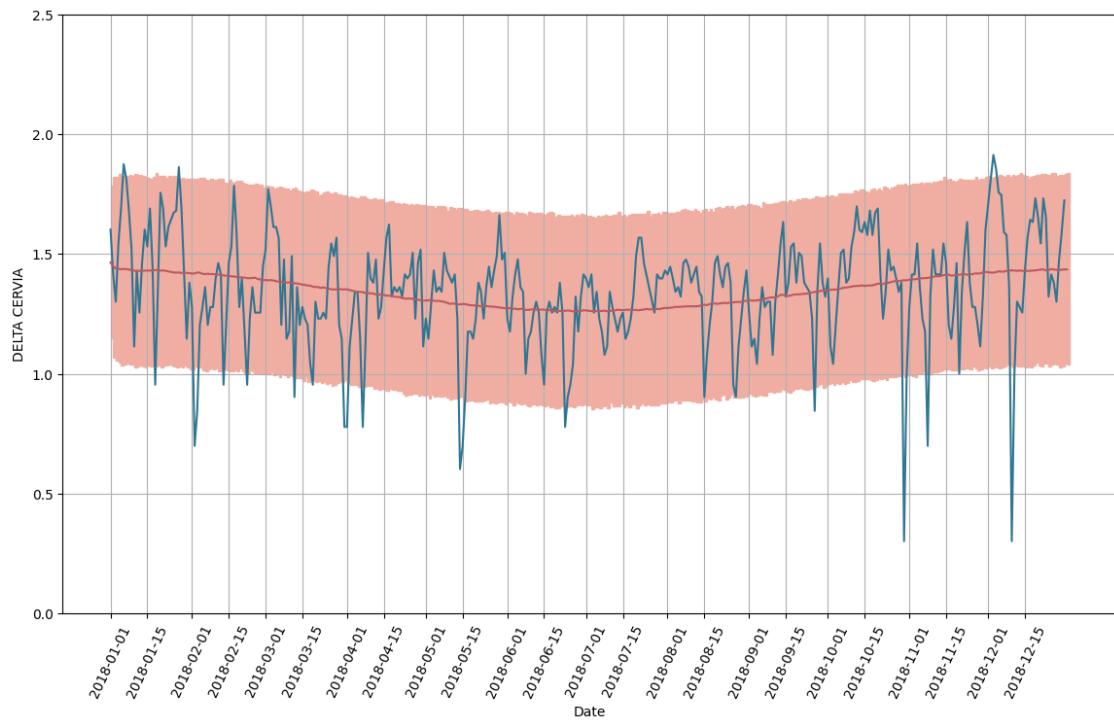


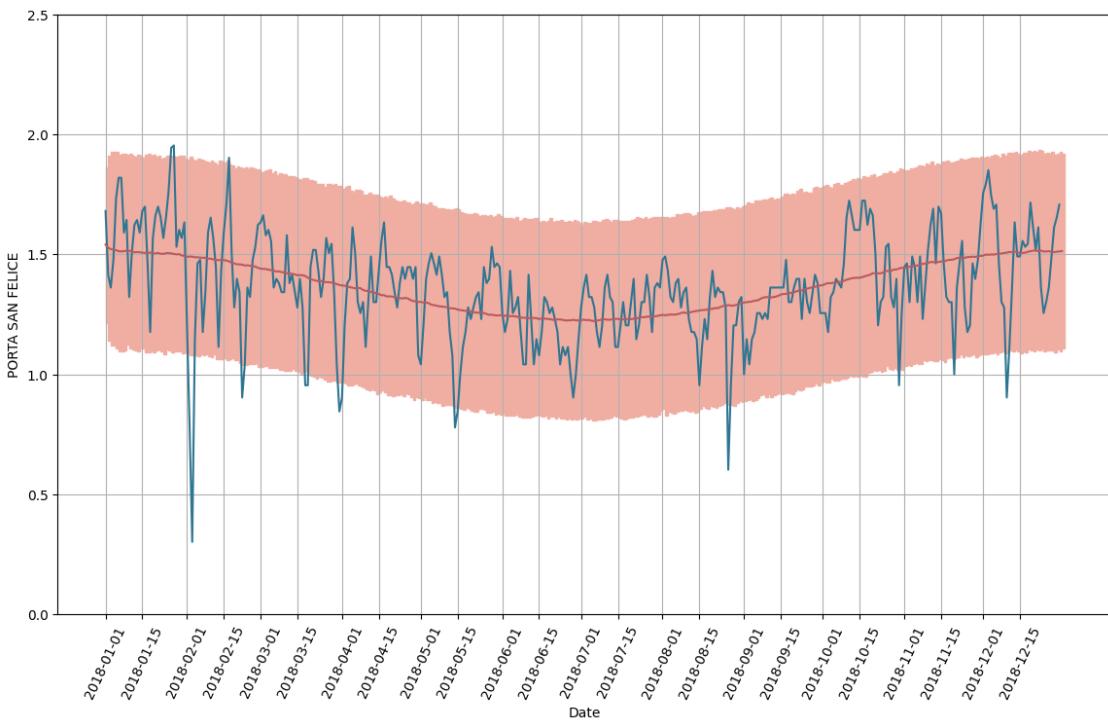
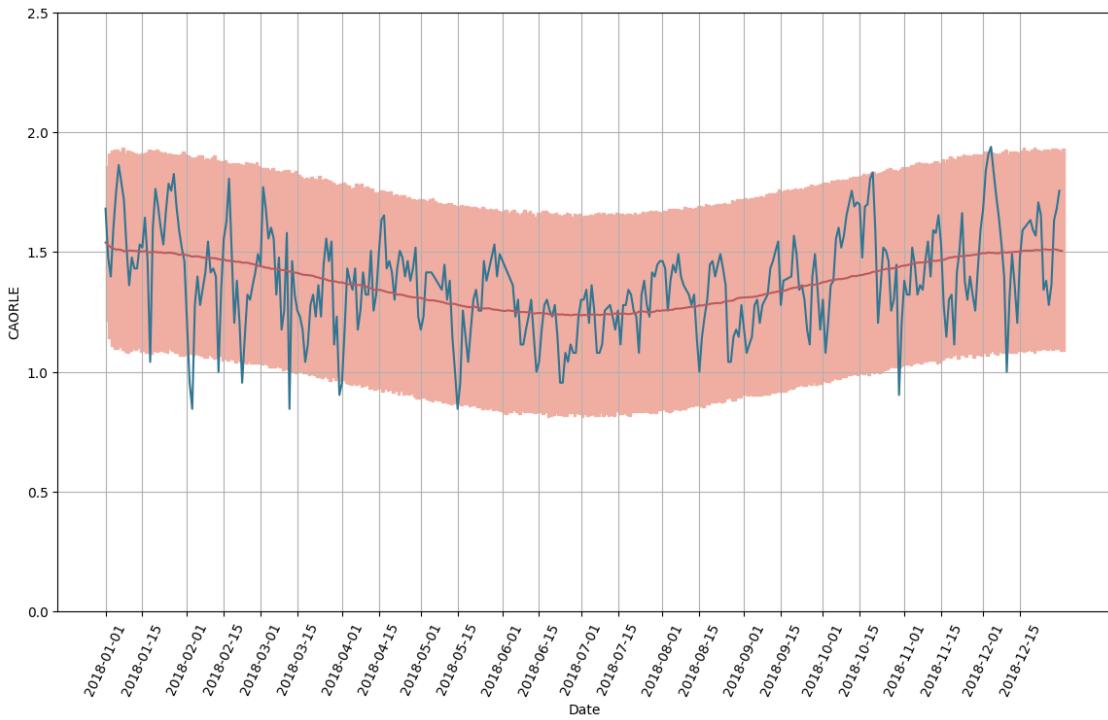


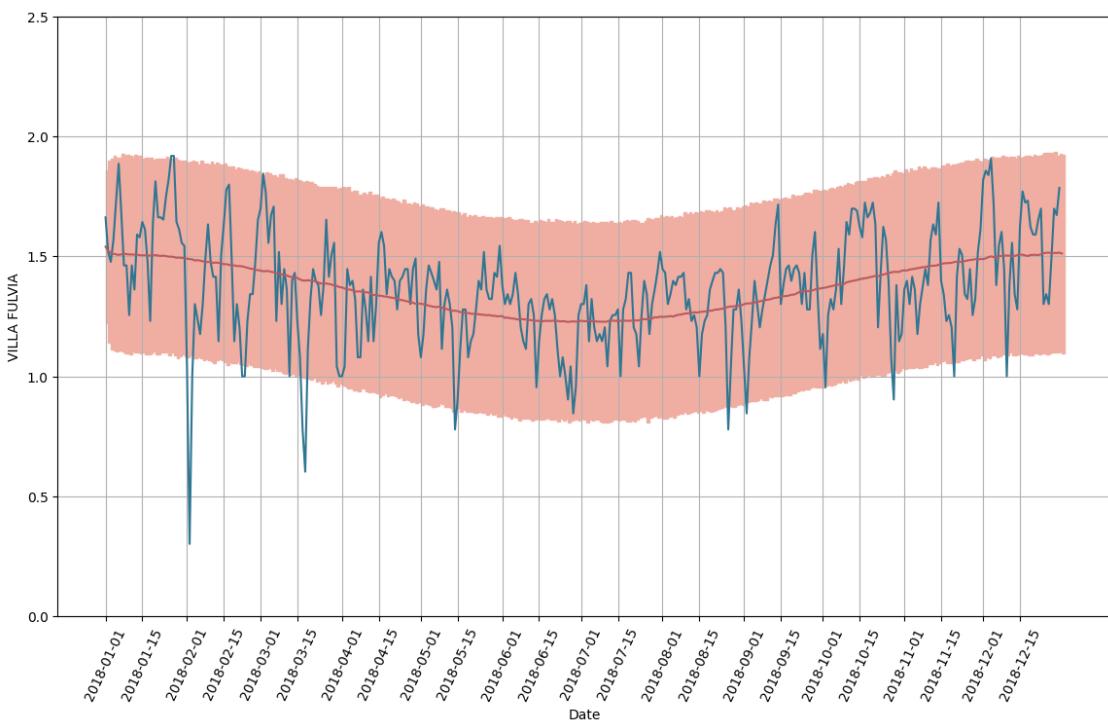
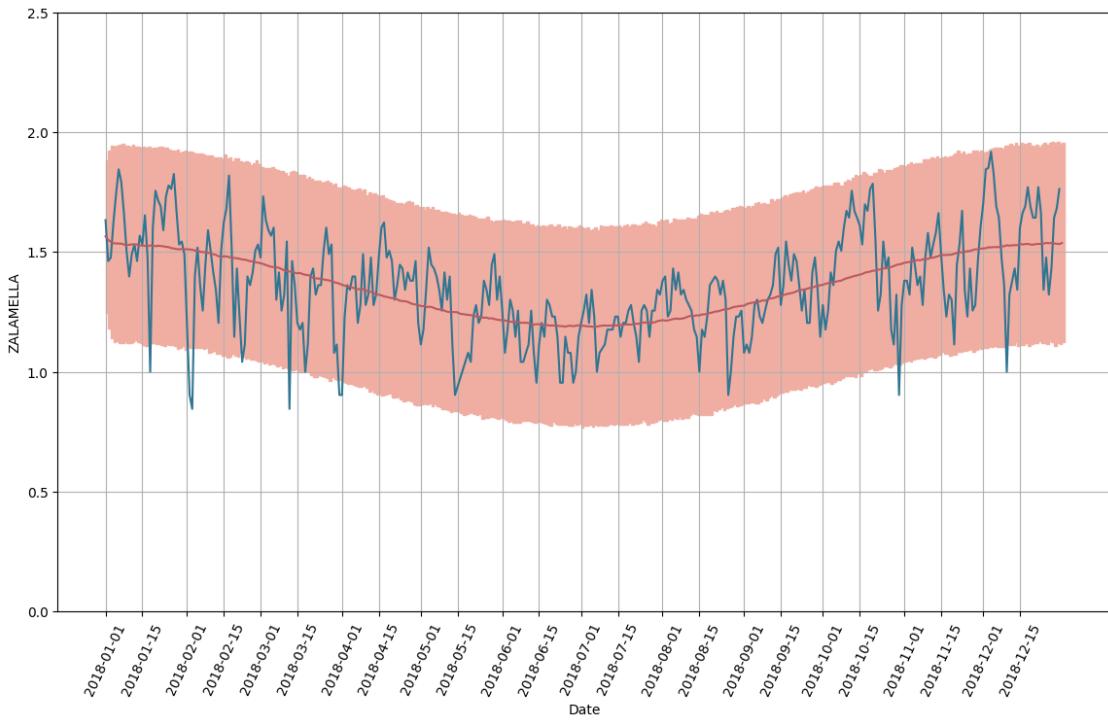


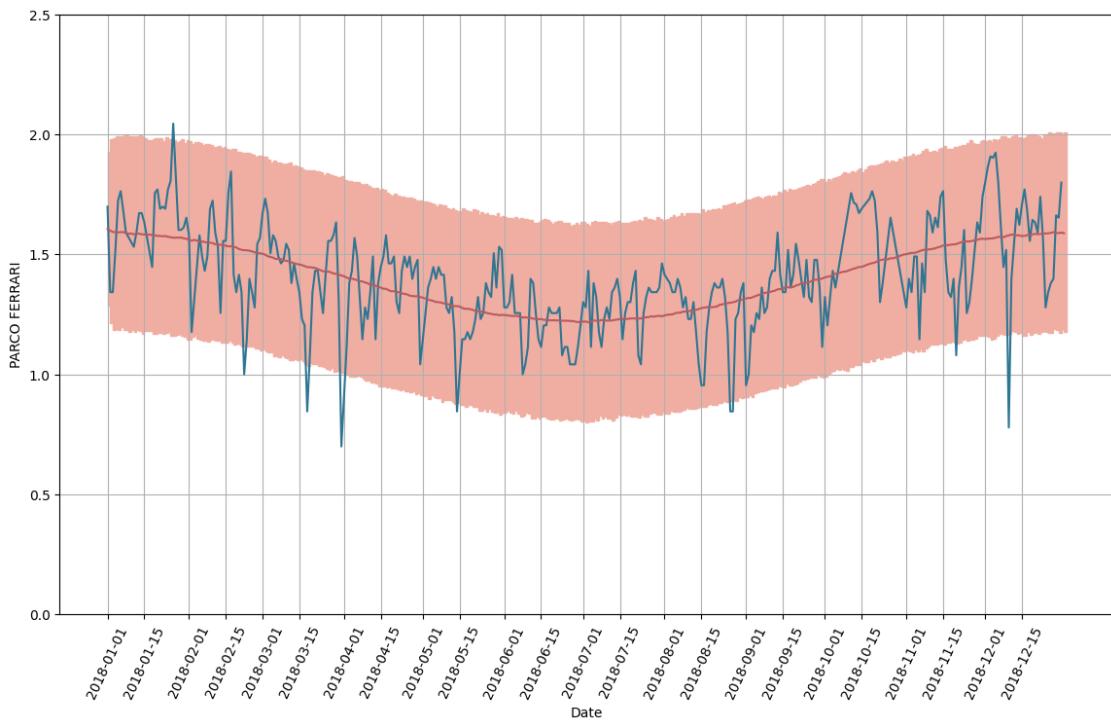
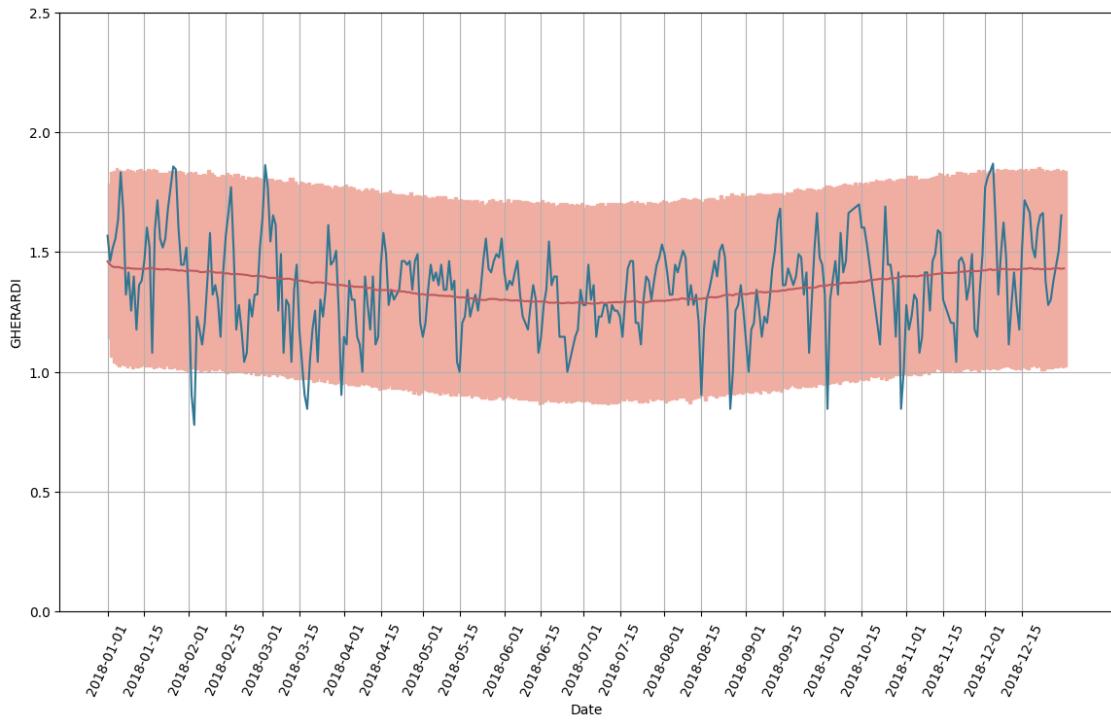


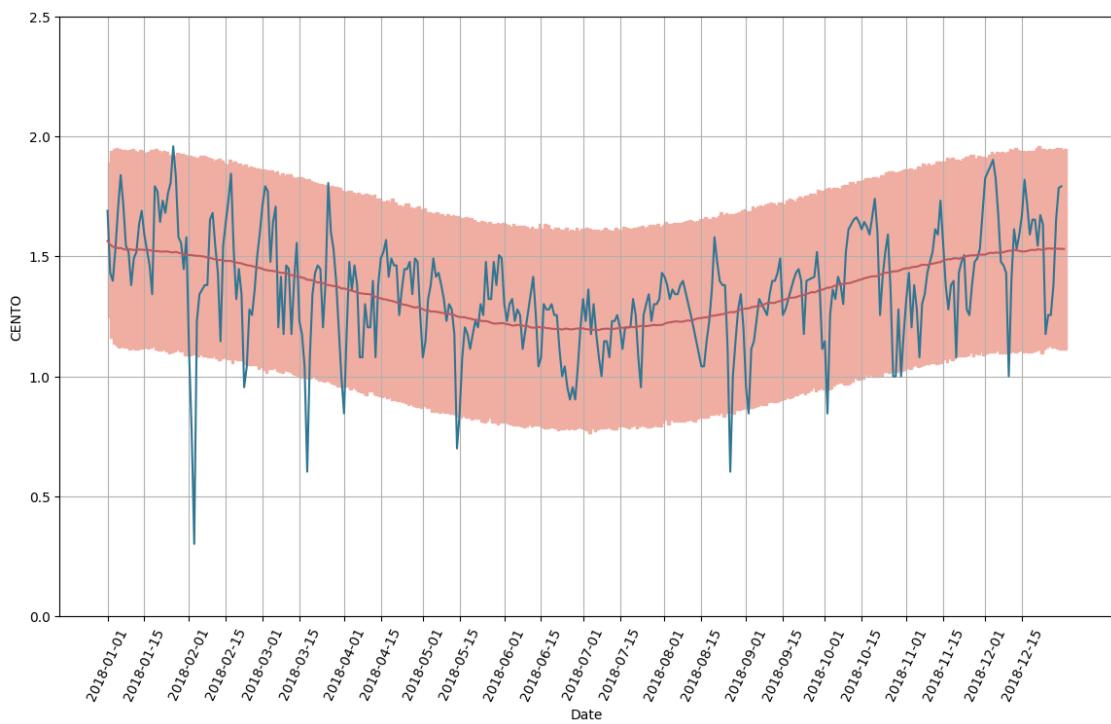
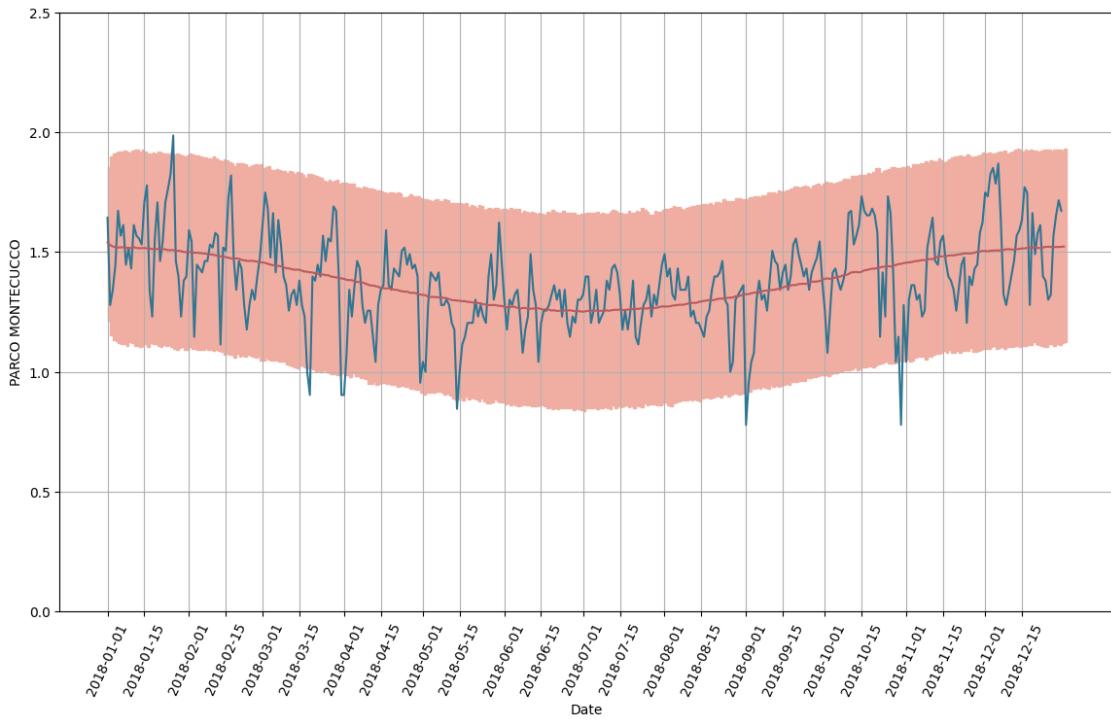


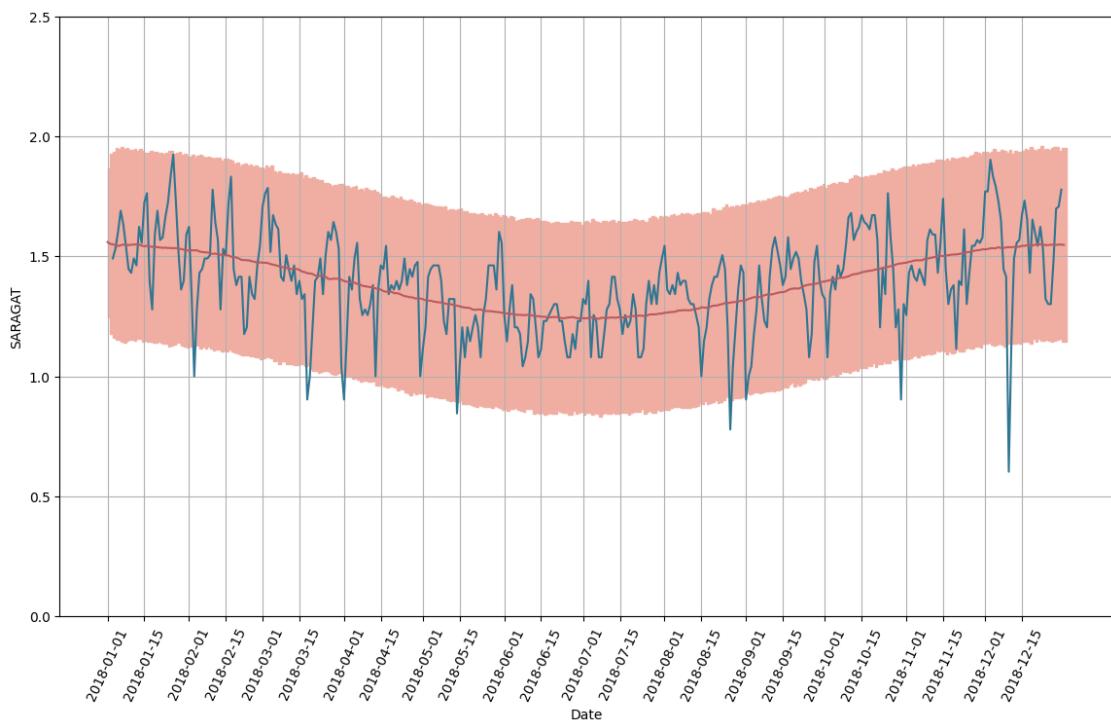
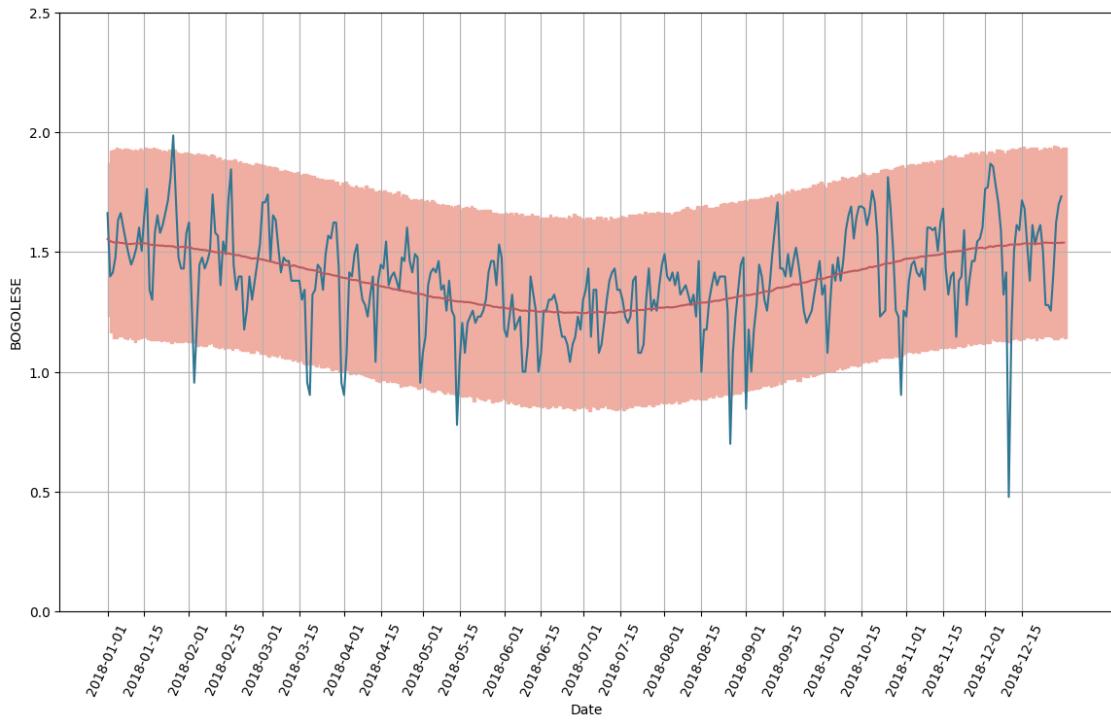


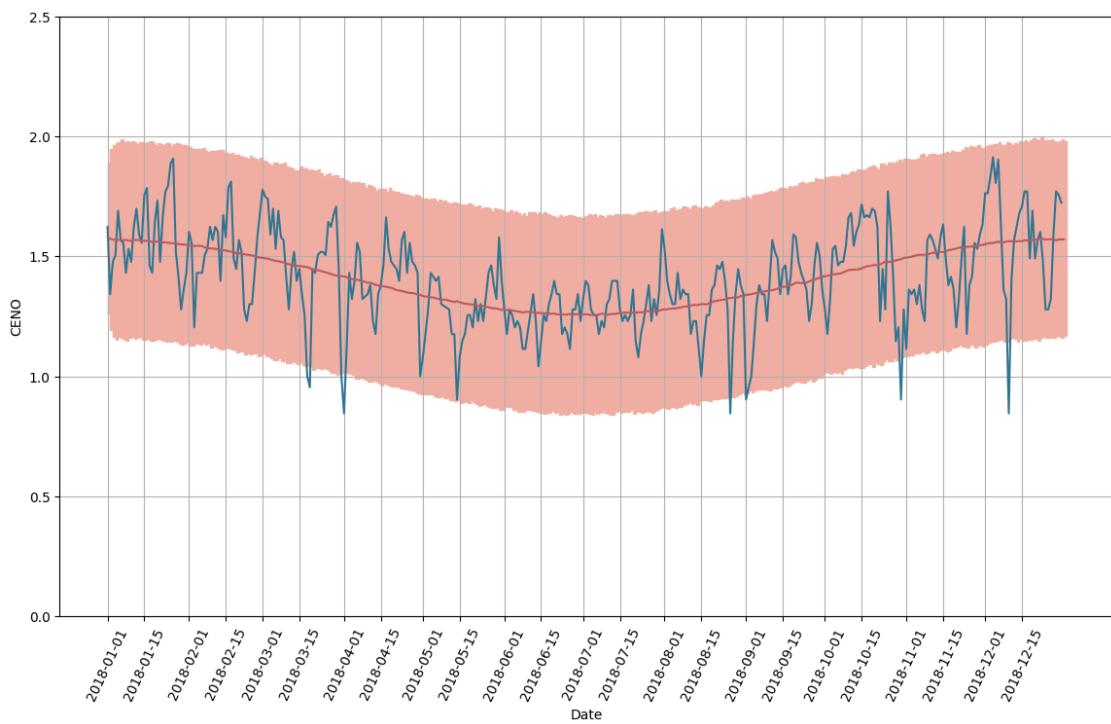
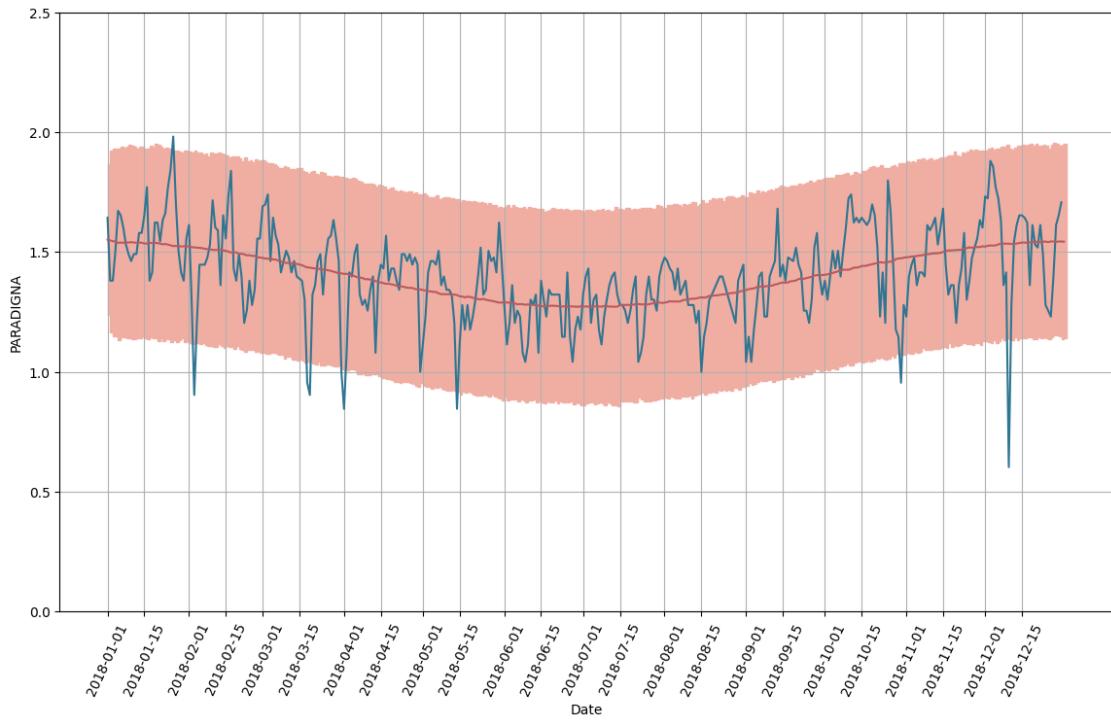


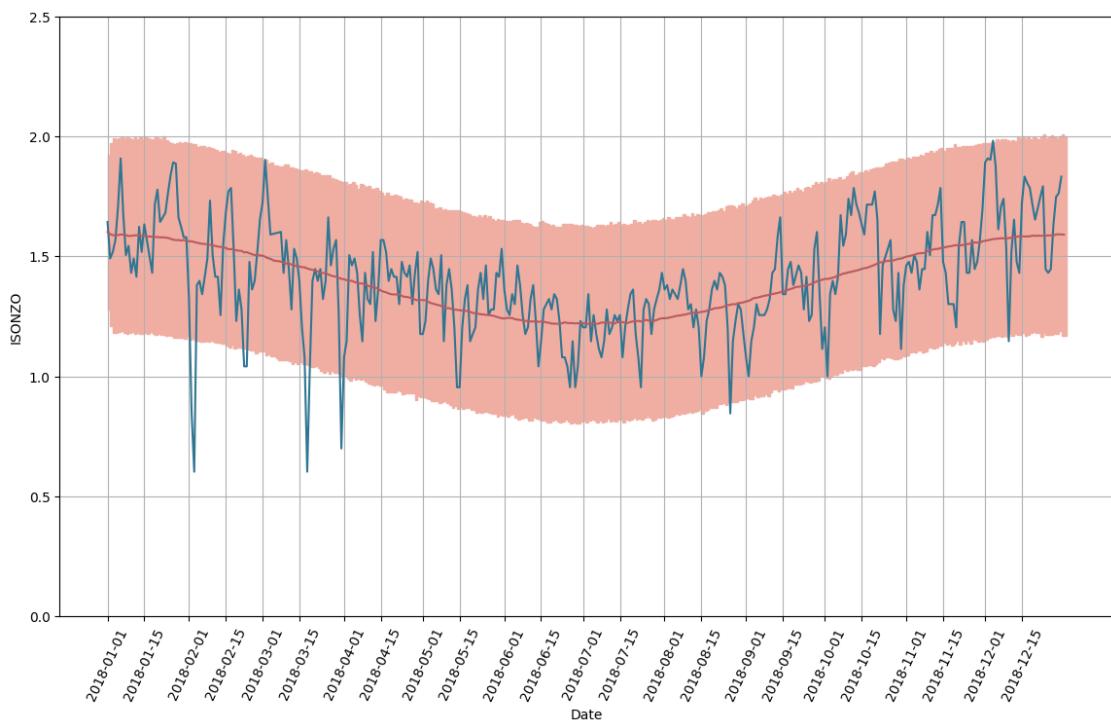
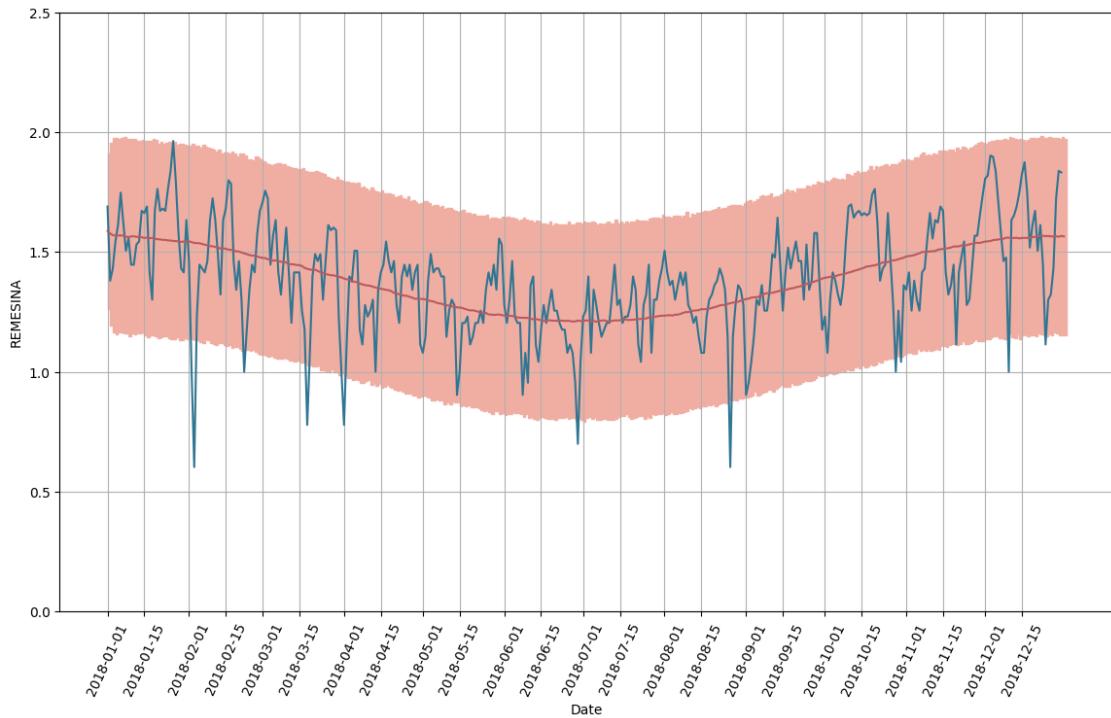


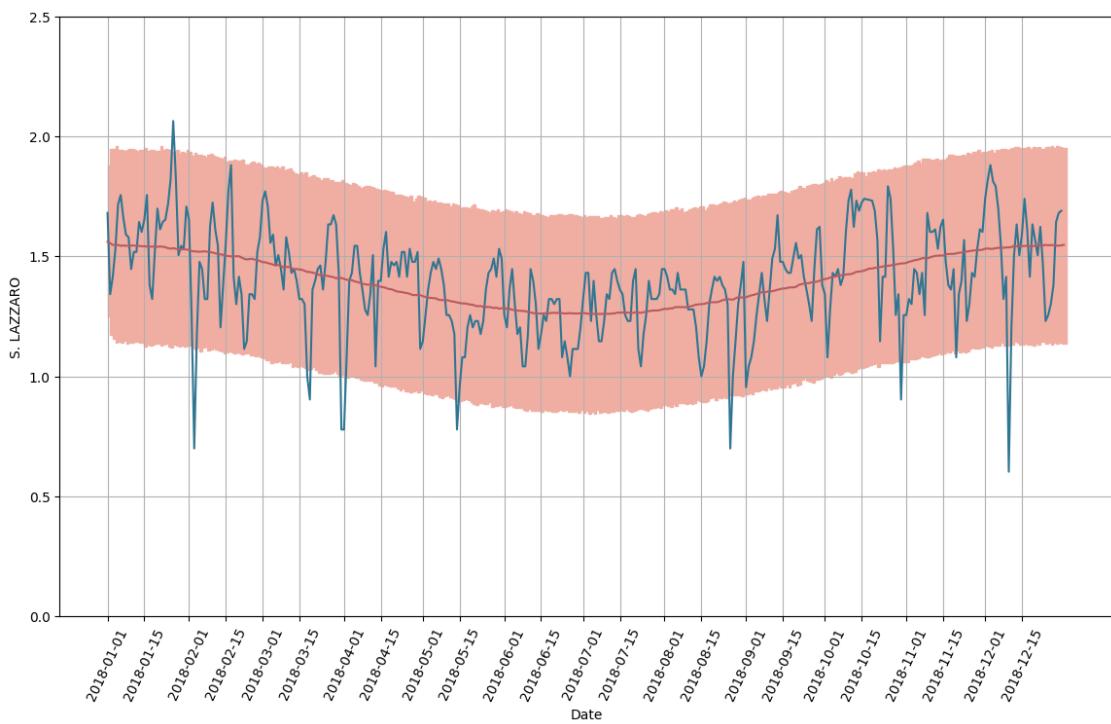
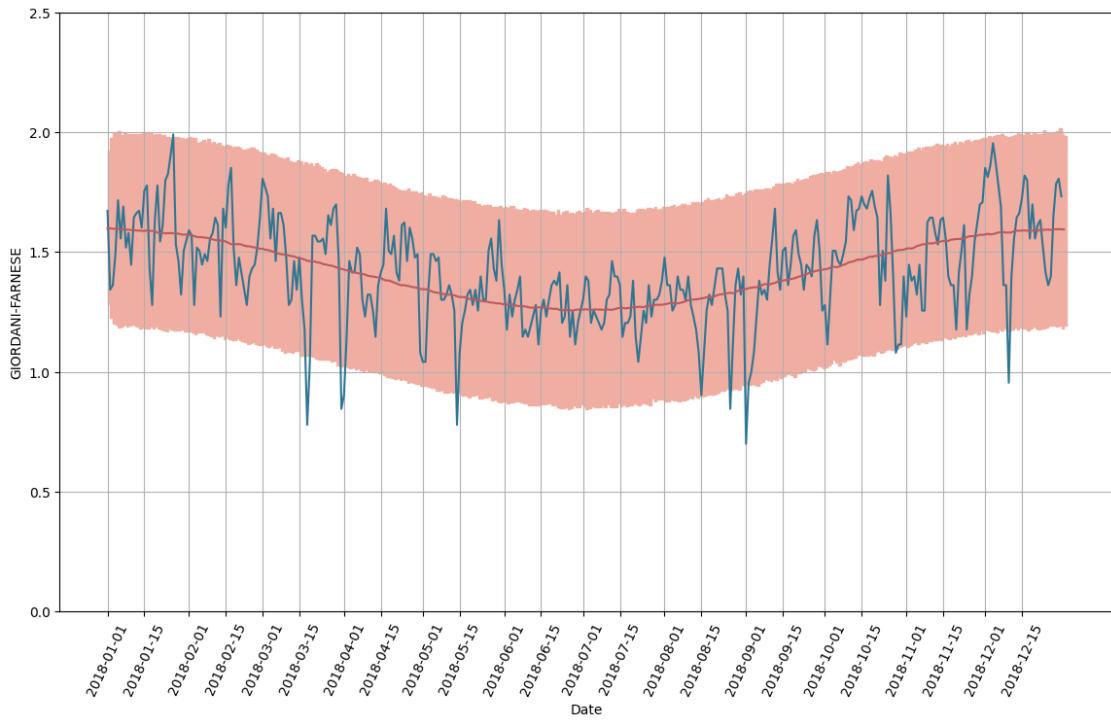


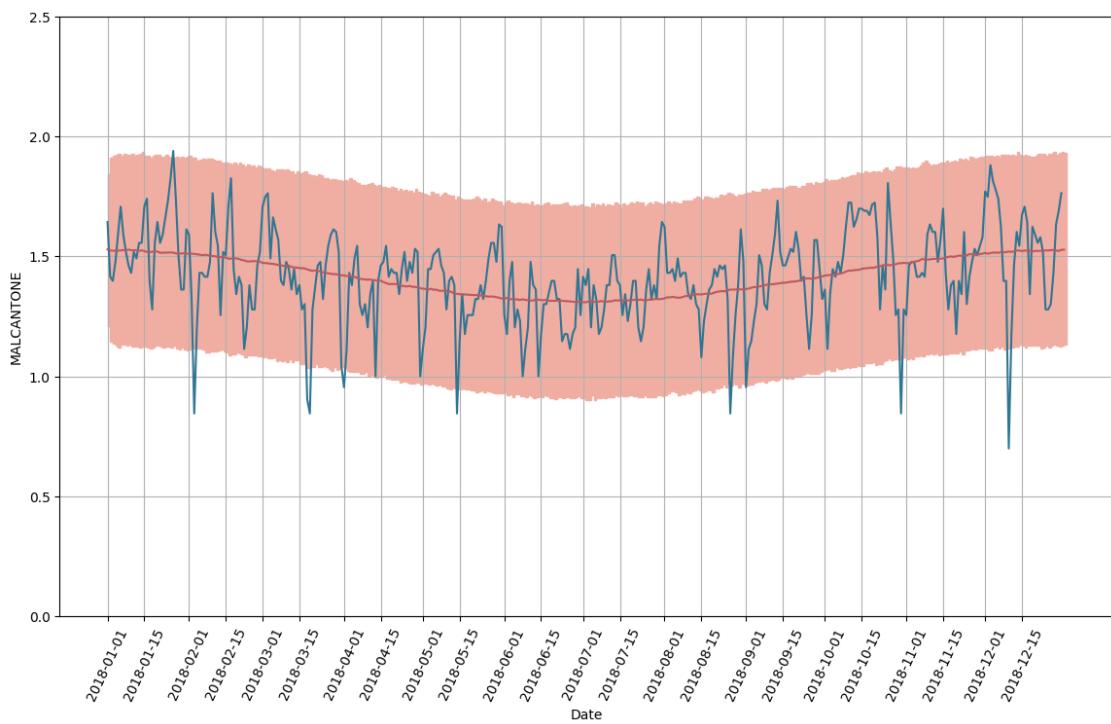
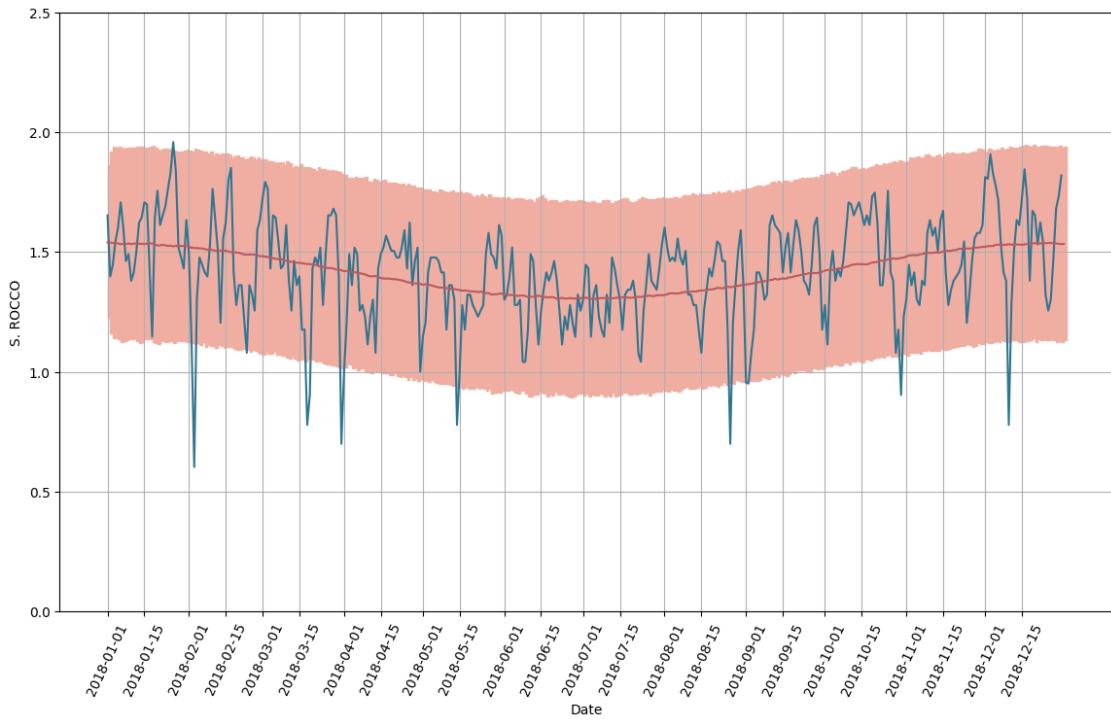


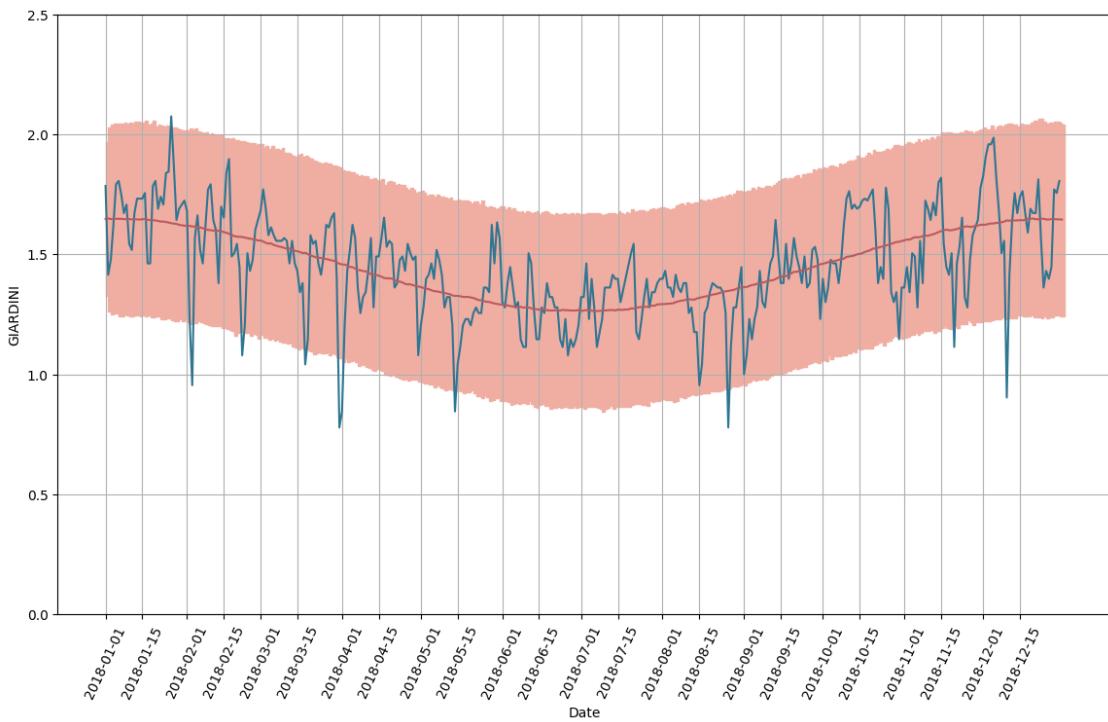
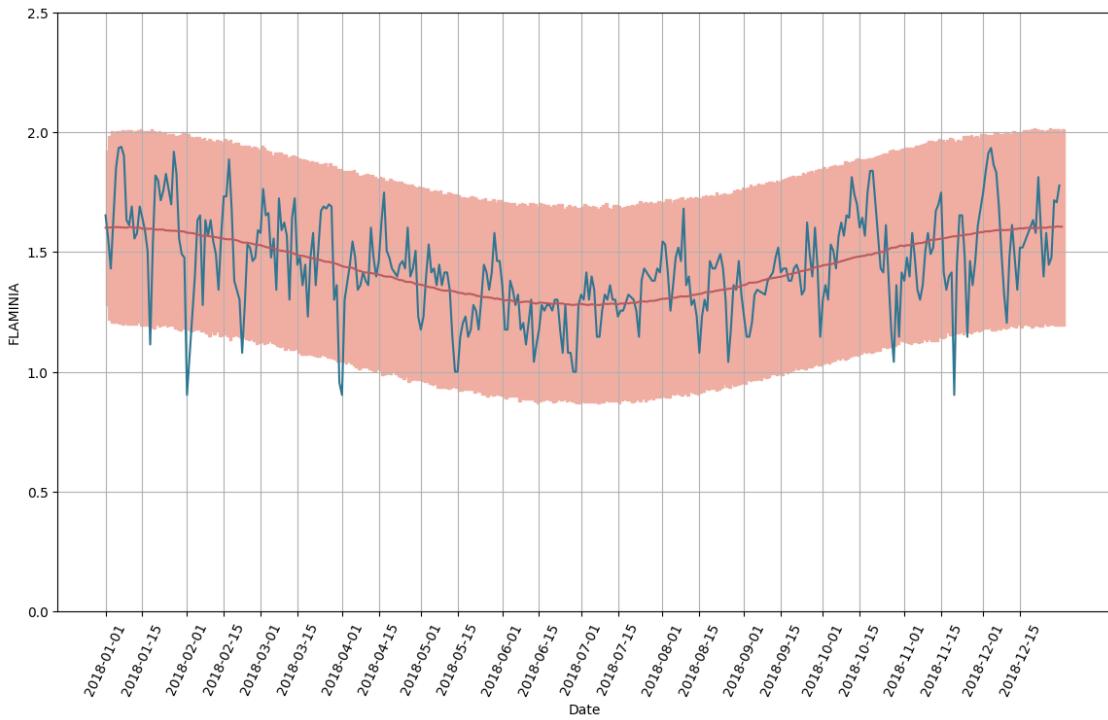


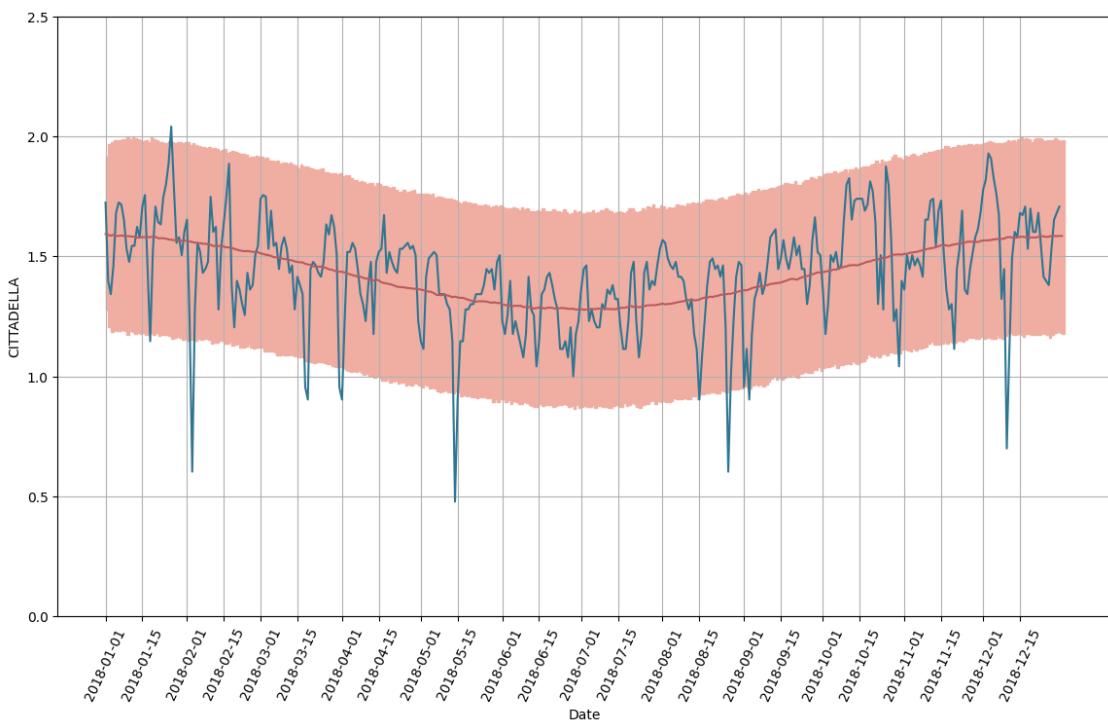
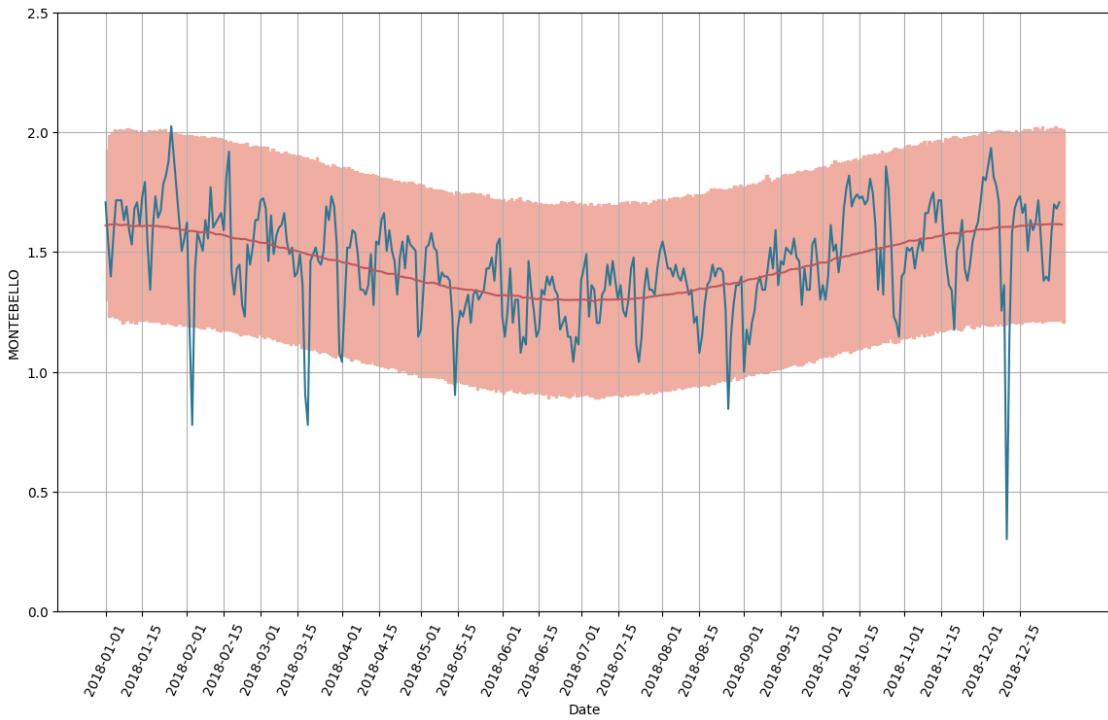


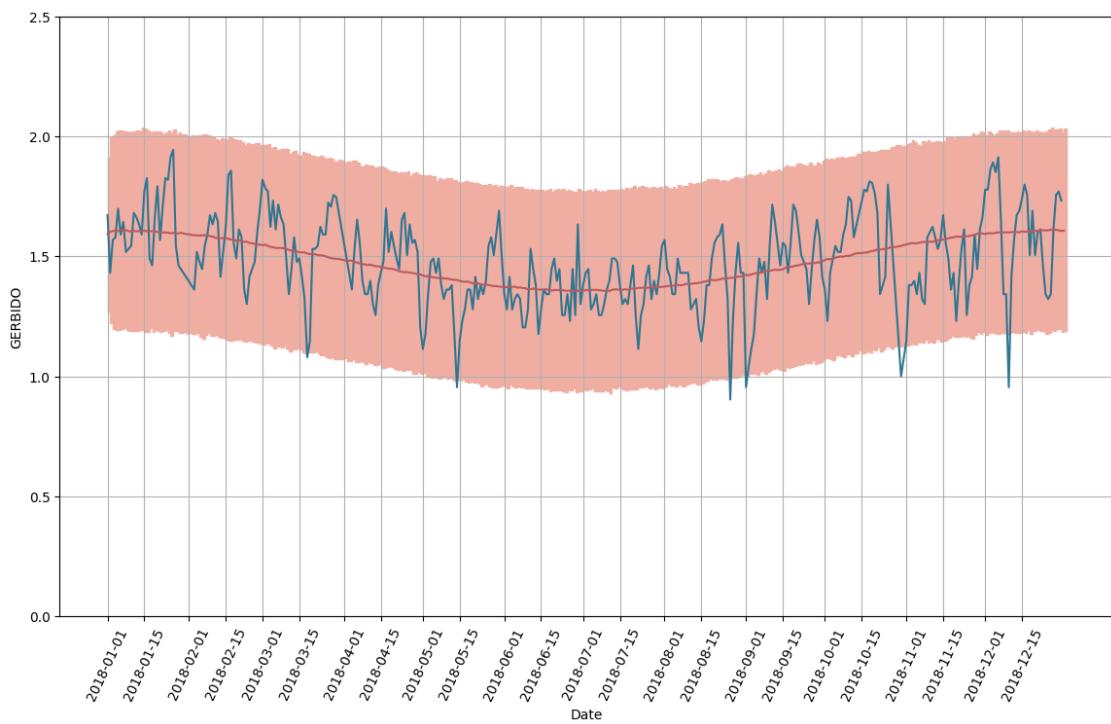
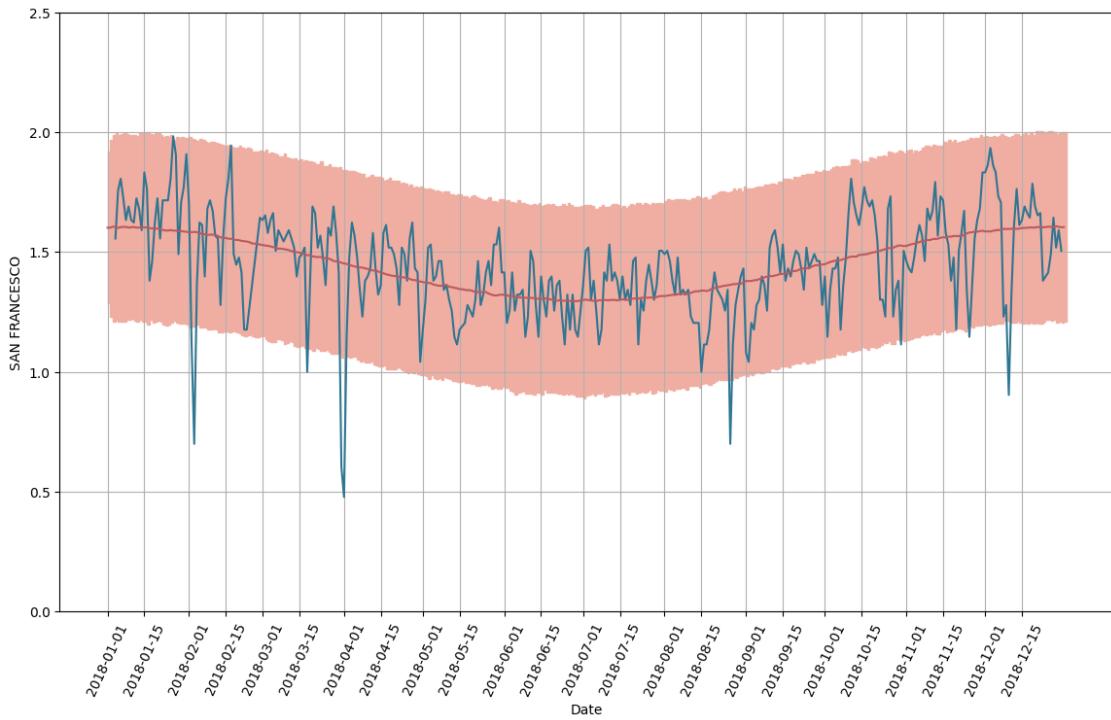


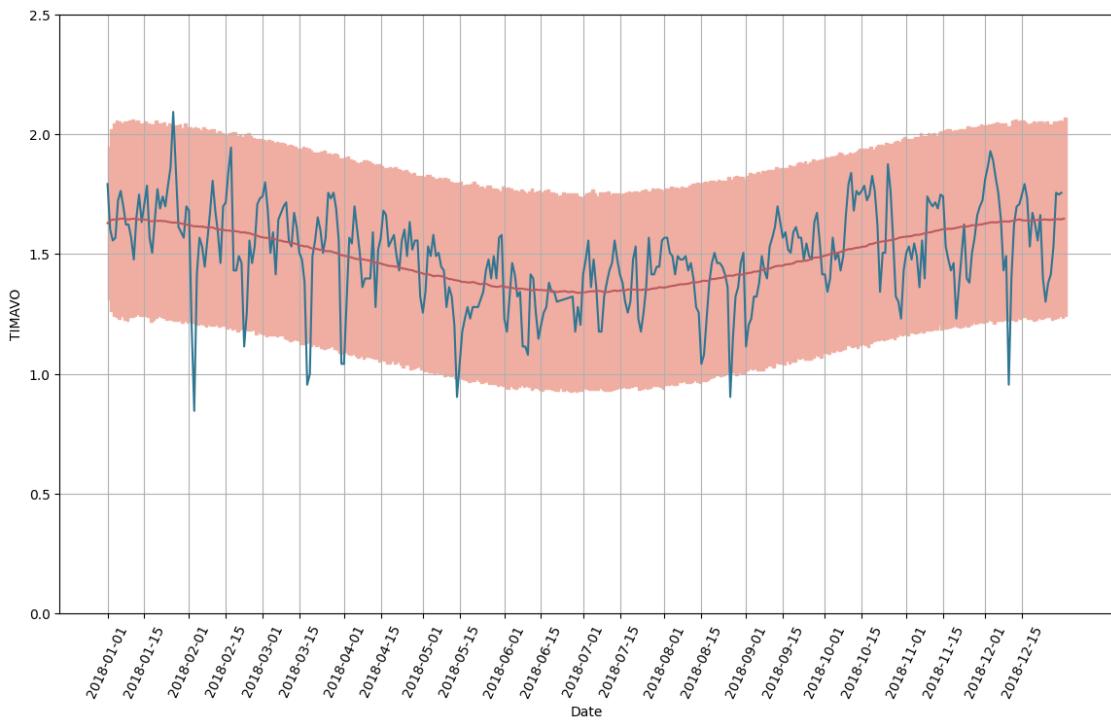












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