

# 006 - Intro to time series and forecasting

## Notation

Autocovariance function      ACVF       $\gamma(h) = \text{Cov}(X_{t+h}, X_t)$

Autocorrelation function      ACF       $\rho(h) = \frac{\gamma(h)}{\gamma(0)}$

Weak stationarity

- $\mu_X(t)$  independent of  $t$
- $\gamma_X(t+h, t)$  independent of  $t$  for each  $h$ .

Models with trends

$$X_t = \underbrace{mt}_{\text{slowly changing function}} + Y_t \quad \text{zero-mean}$$

= trend component  $\rightarrow$  Estimated via LS

Models with seasonality  
(Harmonic Regression)

$$X_t = \underbrace{d_t}_{\downarrow} + Y_t$$

$$d_t = a_0 + \sum_{j=1}^K (g_j \cos(d_j t) + b_j \sin(d_j t))$$

estimate parameters  
via LS

## GENERAL APPROACH TO TIME SERIES MODELING

pg 27.

Plot and check for existence of

(a) Trend

(b) Seasonal component

(c) Apparent sharp changes in behavior

(d) Outlying observations

$\rightarrow$  Remove to get stationary residuals

$\downarrow$

Section 1.5

$\rightarrow$  la figura spiega come si fa