# Argumentation among Agents: Review and Commentary

Grigore Costin-Teodor Radu Ștefan-Octavian Vasiliu Florin Vintilă Eduard

Florin

• Reference: Iyad Rahwan's Argumentation among Agents, Chapter 5 in Multiagent Systems, by G. Weiss.

•00000000000

Florin

- Reference: Iyad Rahwan's *Argumentation among Agents*, Chapter 5 in *Multiagent Systems*, by G. Weiss.
- Our contribution: several new examples, and proofs for some merely stated claims.

- Reference: Iyad Rahwan's *Argumentation among Agents*, Chapter 5 in *Multiagent Systems*, by G. Weiss.
- Our contribution: several new examples, and proofs for some merely stated claims.
- What is the author attempting to formalize?

- Reference: Iyad Rahwan's *Argumentation among Agents*, Chapter 5 in *Multiagent Systems*, by G. Weiss.
- Our contribution: several new examples, and proofs for some merely stated claims.
- What is the author attempting to formalize?
- The philosopher's view of argumentation: the giving of claims in favor or against a statement that is open for debate.

Florin

# Prakken's framework, briefly

• Idea: generalize common logics by admitting two kinds of inference rules – *strict* and *defeasible*.

Florin

- Idea: generalize common logics by admitting two kinds of inference rules - strict and defeasible.
- An argumentation system is a tuple  $(\mathcal{L}, cont, S, D)$ .

- Idea: generalize common logics by admitting two kinds of inference rules – strict and defeasible.
- An argumentation system is a tuple  $(\mathcal{L}, cont, \mathcal{S}, \mathcal{D})$ .
- $\mathcal{L}$  is some "logical language" (must contain  $\neg$ ).

Stefan

# Prakken's framework, briefly

- Idea: generalize common logics by admitting two kinds of inference rules – strict and defeasible.
- An argumentation system is a tuple  $(\mathcal{L}, cont, S, D)$ .
- $\mathcal{L}$  is some "logical language" (must contain  $\neg$ ).
- The function

$$cont: \mathcal{L} o \mathcal{P}(\mathcal{L})$$

generalizes negation.

- Idea: generalize common logics by admitting two kinds of inference rules – strict and defeasible.
- An argumentation system is a tuple  $(\mathcal{L}, cont, S, D)$ .
- $\mathcal{L}$  is some "logical language" (must contain  $\neg$ ).
- The function

$$cont: \mathcal{L} o \mathcal{P}(\mathcal{L})$$

generalizes negation.

• *S*, *D* are respectively the sets of strict/defeasible inference rules.

• How does the *cont* function generalize negation?

- How does the *cont* function generalize negation?
- If  $\varphi \in cont(\psi)$ , then
  - if  $\psi \notin cont(\varphi)$ , then  $\varphi$  is a contrary of  $\psi$ ;
  - if  $\psi \in cont(\varphi)$ , then  $\varphi$  and  $\psi$  are contradictory.

- How does the cont function generalize negation?
- If  $\varphi \in cont(\psi)$ , then
  - if  $\psi \notin cont(\varphi)$ , then  $\varphi$  is a contrary of  $\psi$ ;
  - if  $\psi \in cont(\varphi)$ , then  $\varphi$  and  $\psi$  are contradictory.
- It is mandatory that

$$\neg \varphi \in cont(\varphi)$$
 and  $\varphi \in cont(\neg \varphi)$ 

for any formula  $\varphi$ .

• An argument from a knowledge base  $\mathcal K$  is defined similarly to a deduction in propositional logic. (The members of  $\mathcal K$  play the role of the hypotheses.)

- An argument from a knowledge base  $\mathcal K$  is defined similarly to a deduction in propositional logic. (The members of  $\mathcal K$  play the role of the hypotheses.)
- Major difference: incorporation of the used inference rules.

- An argument from a knowledge base  $\mathcal K$  is defined similarly to a deduction in propositional logic. (The members of  $\mathcal K$  play the role of the hypotheses.)
- Major difference: incorporation of the used inference rules.
- The complete framework contains a partial order on defeasible rules. Using it, arguments may be compared.

• Henceforth, an argumentation framework will mean a finite directed graph  $(A, \rightharpoonup)$ , whose nodes are called "arguments". The adjacency relation is pronounced "defeats".

- Henceforth, an argumentation framework will mean a finite directed graph  $(A, \rightharpoonup)$ , whose nodes are called "arguments". The adjacency relation is pronounced "defeats".
- Hence, for arguments  $p, q, p \rightarrow q$  means "p defeats q".

- Henceforth, an argumentation framework will mean a finite directed graph  $(A, \rightharpoonup)$ , whose nodes are called "arguments". The adjacency relation is pronounced "defeats".
- Hence, for arguments p, q, " $p \rightarrow q$ " means "p defeats q".
- Note how the structure of arguments is not taken into account anymore.

Stefan

- Henceforth, an argumentation framework will mean a finite directed graph (A, →), whose nodes are called "arguments".
   The adjacency relation is pronounced "defeats".
- Hence, for arguments  $p, q, p \rightarrow q$  means "p defeats q".
- Note how the structure of arguments is not taken into account anymore.
- Objective: define an "acceptable" argument.

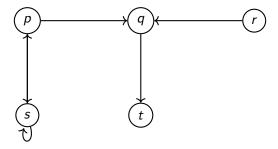


Figure: Our argumentation framework.

•  $S^+ =$  the set of arguments defeated by some member of S.

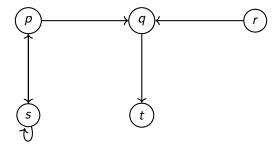


Figure: Our argumentation framework.

- $S^+ =$  the set of arguments defeated by some member of S.
- In the figure,  $\{p, q\}^+ = \{q, s, t\}$ .

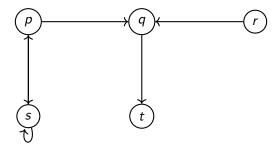


Figure: Our argumentation framework.

•  $a^- =$  the set of arguments which defeat a.

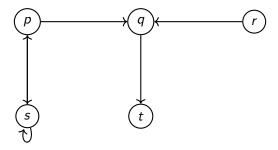


Figure: Our argumentation framework.

- $a^- =$  the set of arguments which defeat a.
- In the figure,  $s^- = \{p, s\}$ .

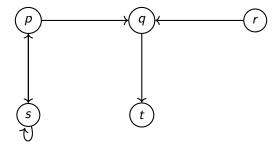


Figure: Our argumentation framework.

• A set S of arguments is *conflict-free* if no argument in S defeats another also in S.

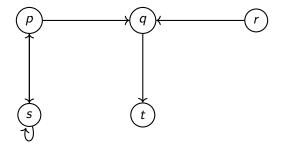


Figure: Our argumentation framework.

- A set S of arguments is *conflict-free* if no argument in S defeats another also in S.
- In the figure,  $\{p, t\}$  and  $\{r, t\}$  are conflict-free.

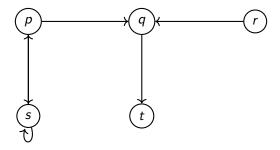


Figure: Our argumentation framework.

• A set S of arguments defends argument a if every argument which defeats a is defeated by S (i.e., is in  $S^+$ ).

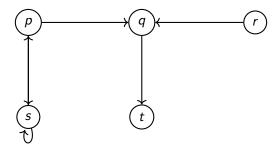


Figure: Our argumentation framework.

- A set S of arguments defends argument a if every argument which defeats a is defeated by S (i.e., is in  $S^+$ ).
- In the figure,  $\{p, t\}$  defends p.



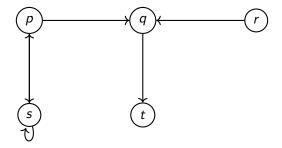


Figure: Our argumentation framework.

• The characteristic function  $\mathcal{F}$  is defined thus:  $\mathcal{F}(S)=$  the set of arguments defended by S.

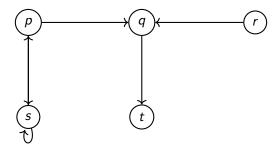


Figure: Our argumentation framework.

- The characteristic function  $\mathcal{F}$  is defined thus:  $\mathcal{F}(S)=$  the set of arguments defended by S.
- In the figure,  $\mathcal{F}(\{p,q,r\}) = \{p,r,t\}$  and  $\mathcal{F}(\{r,t\}) = \{r,t\}$ .

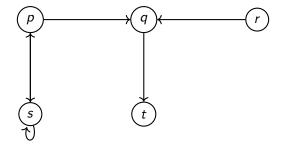


Figure: Our argumentation framework.

• A complete extension is a set S of arguments which is conflict-free and such that  $\mathcal{F}(S) = S$  (i.e., it defends its own members and nothing else).

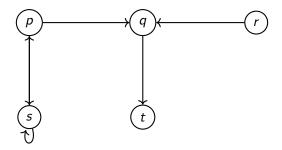


Figure: Our argumentation framework.

- A complete extension is a set S of arguments which is conflict-free and such that  $\mathcal{F}(S) = S$  (i.e., it defends its own members and nothing else).
- By the remarks on previous slides,  $\{r, t\}$  is a complete extension.



• The author exhibits an equivalent characterization of complete extensions via labellings.

- The author exhibits an equivalent characterization of complete extensions via *labellings*.
- An argument *p* is:
  - skeptically accepted iff p belongs to every extension;
  - credulously accepted iff p belongs to some extension;
  - rejected iff p doesn't belong to any extension.

#### The Argument Interchange Format

 Stems from a need for standardized representations of arguments.

#### The Argument Interchange Format

- Stems from a need for standardized representations of arguments.
- Previous attempts unsuitable:

- Stems from a need for standardized representations of arguments.
- Previous attempts unsuitable:
  - designed to be used with specific tools

- Stems from a need for standardized representations of arguments.
- Previous attempts unsuitable:
  - designed to be used with specific tools
  - strong link between language and tool

- Stems from a need for standardized representations of arguments.
- Previous attempts unsuitable:
  - designed to be used with specific tools
  - strong link between language and tool
  - neglected formal logic due to user experience focus

• Objectives:

- Objectives:
  - standardize communication between reasoning-based multi-agent systems

- Objectives:
  - standardize communication between reasoning-based multi-agent systems
  - facilitate the creation of such systems

- Objectives:
  - standardize communication between reasoning-based multi-agent systems
  - facilitate the creation of such systems
  - design an efficient and abstract format for exchanging data

#### Objectives:

- standardize communication between reasoning-based multi-agent systems
- facilitate the creation of such systems
- design an efficient and abstract format for exchanging data
- facilitate argument manipulation and visual representation

• Arguments are composed of networks of interlinked nodes.

- Arguments are composed of networks of interlinked nodes.
- Two types of nodes:

- Arguments are composed of networks of interlinked nodes.
- Two types of nodes:
  - $-\mathcal{N}_I \subset \mathcal{N}$ , information nodes (I-nodes)

- Arguments are composed of networks of interlinked nodes.
- Two types of nodes:
  - $-\mathcal{N}_I \subset \mathcal{N}$ , information nodes (I-nodes)
  - $-\mathcal{N}_{\mathcal{S}}\subset\mathcal{N}$ , scheme nodes (S-nodes)
- Schemes are classes of reasoning patterns.

- Arguments are composed of networks of interlinked nodes.
- Two types of nodes:
  - $-\mathcal{N}_I \subset \mathcal{N}$ , information nodes (I-nodes)
  - $N_S$   $\subset$  N, scheme nodes (S-nodes)
- Schemes are classes of reasoning patterns.
- Schemes are divided into:

- Arguments are composed of networks of interlinked nodes.
- Two types of nodes:
  - $-\mathcal{N}_I \subset \mathcal{N}$ , information nodes (I-nodes)
  - $N_S$   $\subset$  N, scheme nodes (S-nodes)
- Schemes are classes of reasoning patterns.
- Schemes are divided into:
  - $-\mathcal{S}^R \subset \mathcal{S}$ , rule of inference schemes

- Arguments are composed of networks of interlinked nodes.
- Two types of nodes:
  - $-\mathcal{N}_I \subset \mathcal{N}$ , information nodes (I-nodes)
  - $-\mathcal{N}_{\mathcal{S}}\subset\mathcal{N}$ , scheme nodes (S-nodes)
- Schemes are classes of reasoning patterns.
- Schemes are divided into:
  - $-\mathcal{S}^R \subset \mathcal{S}$ , rule of inference schemes
  - $-\mathcal{S}^{\mathcal{C}}\subset\mathcal{S}$ , conflict schemes

- Arguments are composed of networks of interlinked nodes.
- Two types of nodes:
  - $-\mathcal{N}_I \subset \mathcal{N}$ , information nodes (I-nodes)
  - $-\mathcal{N}_{\mathcal{S}}\subset\mathcal{N}$ , scheme nodes (S-nodes)
- Schemes are classes of reasoning patterns.
- Schemes are divided into:
  - $-\mathcal{S}^R \subset \mathcal{S}$ , rule of inference schemes
  - $-\mathcal{S}^{\mathcal{C}}\subset\mathcal{S}$ , conflict schemes
  - $-\mathcal{S}^P \subset \mathcal{S}$ , preference schemes

• S-nodes are actual applications of a scheme.



- S-nodes are actual applications of a scheme.
- S-nodes are of three types, for each scheme class:

- S-nodes are actual applications of a scheme.
- S-nodes are of three types, for each scheme class:
  - $-\mathcal{N}_{S}^{RA}\subset\mathcal{N}_{S}$ , rule of inference application nodes (RA-nodes)

- S-nodes are actual applications of a scheme.
- S-nodes are of three types, for each scheme class:
  - $-\mathcal{N}_{S}^{RA} \subset \mathcal{N}_{S}$ , rule of inference application nodes (RA-nodes)
  - $-\mathcal{N}_{S}^{\mathit{CA}}\subset\mathcal{N}_{S}$ , conflict application nodes (CA-nodes)

- S-nodes are actual applications of a scheme.
- S-nodes are of three types, for each scheme class:
  - $-\mathcal{N}_{S}^{RA} \subset \mathcal{N}_{S}$ , rule of inference application nodes (RA-nodes)
  - $\mathcal{N}_{S}^{\textit{CA}} \subset \mathcal{N}_{S}$ , conflict application nodes (CA-nodes)
  - $\mathcal{N}_{S}^{PA}\subset\mathcal{N}_{S}$ , preference application nodes (PA-nodes)

- S-nodes are actual applications of a scheme.
- S-nodes are of three types, for each scheme class:
  - $-\mathcal{N}_{S}^{RA} \subset \mathcal{N}_{S}$ , rule of inference application nodes (RA-nodes)
  - $-\mathcal{N}_{S}^{CA}\subset\mathcal{N}_{S}$ , conflict application nodes (CA-nodes)
  - $-\mathcal{N}_{S}^{PA}\subset\mathcal{N}_{S}$ , preference application nodes (PA-nodes)
- Example:  $MP_1 \in \mathcal{N}_S^{RA}$ , an RA-node implementing the modus ponens *rule of inference scheme* from propositional logic.

## Argument network

• An argument network  $\Phi$  is a graph, consisting of:

#### Argument network

- An argument network  $\Phi$  is a graph, consisting of:
  - a set  $\mathcal{N} = \mathcal{N}_I \cup \mathcal{N}_S$  of vertices

#### Argument network

- An argument network  $\Phi$  is a graph, consisting of:
  - a set  $\mathcal{N} = \mathcal{N}_{\textit{I}} \cup \mathcal{N}_{\textit{S}}$  of vertices
  - a binary relation  $\xrightarrow{edge}$ :  $\mathcal{N} \times \mathcal{N}$ , representing edges, with the restriction that  $\forall i \in \mathcal{N}_I, \forall j \in \mathcal{N}_I, \not\exists (i,j) \in \xrightarrow{edge}$

• A simple argument, in a network  $\Phi$  and schemes  $\mathcal S$  is a tuple  $\langle P, \tau, c \rangle$ , where:

- A simple argument, in a network  $\Phi$  and schemes  $\mathcal{S}$  is a tuple  $\langle P, \tau, c \rangle$ , where:
  - $-P\subseteq \mathcal{N}_I$  is a set of I-nodes, constituting the premises

- A simple argument, in a network  $\Phi$  and schemes  $\mathcal{S}$  is a tuple  $\langle P, \tau, c \rangle$ , where:
  - $-P\subseteq \mathcal{N}_I$  is a set of I-nodes, constituting the premises
  - $au\in\mathcal{N}_{\mathcal{S}}^{RA}$  is an RA-node

- A simple argument, in a network  $\Phi$  and schemes  $\mathcal S$  is a tuple  $\langle P, \tau, c \rangle$ , where:
  - $-P\subseteq \mathcal{N}_I$  is a set of I-nodes, constituting the premises
  - $\tau \in \mathcal{N}_{\mathcal{S}}^{RA}$  is an RA-node
  - $-c \in \mathcal{N}_I$  is an I-node representing the conclusion, with the condition that  $\tau \xrightarrow{edge} c$ , uses $(\tau, s)$ ,  $s \in \mathcal{S}$  and  $\forall p \in P$  there is  $p \xrightarrow{edge} \tau$

• The argument:

- The argument:
  - $(P_1)$  The sun's UV helps produce Vitamin D in your body

Costin

- The argument:
  - $(P_1)$  The sun's UV helps produce Vitamin D in your body
  - $(P_2)$  Vitamin D is good for your health

- The argument:
  - $(P_1)$  The sun's UV helps produce Vitamin D in your body
  - $(P_2)$  Vitamin D is good for your health
  - $(C_1)$  Therefore, the sun's UV is good for your health

- The argument:
  - $(P_1)$  The sun's UV helps produce Vitamin D in your body
  - $(P_2)$  Vitamin D is good for your health
  - $(C_1)$  Therefore, the sun's UV is good for your health
- We construct the tuple  $A_1 = \langle \{P_1, P_2\}, HS_1, C_1 \rangle$ , a simple argument in natural language, where  $P_1, P_2 \in \mathcal{N}_I$  are premises and  $C_1 \in \mathcal{N}_I$  is the conclusion.  $HS_1 \in \mathcal{N}_S^{RA}$  is an RA-node, that uses the hypothetical syllogism scheme from propositional logic.

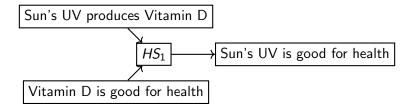


Figure: Argument network using natural language

• Coming up with a rebuttal:

- Coming up with a rebuttal:
  - $(P_3)$  The sun's UV causes skin cancer

- Coming up with a rebuttal:
  - $(P_3)$  The sun's UV causes skin cancer
  - $(P_4)$  Skin cancer is bad for your health

- Coming up with a rebuttal:
  - $(P_3)$  The sun's UV causes skin cancer
  - $(P_4)$  Skin cancer is bad for your health
  - $(C_2)$  Therefore, the sun's UV is bad for your health

- Coming up with a rebuttal:
  - $(P_3)$  The sun's UV causes skin cancer
  - $(P_4)$  Skin cancer is bad for your health
  - $(C_2)$  Therefore, the sun's UV is bad for your health
- We use the previous simple argument  $A_1 = \langle \{P_1, P_2\}, HS_1, C_1 \rangle$  and similarly define another simple argument  $A_2 = \langle \{P_3, P_4\}, HS_2, C_2 \rangle$ , where  $P_3, P_4 \in \mathcal{N}_I$  are premises and  $C_2 \in \mathcal{N}_I$  is the conclusion.  $HS_2 \in \mathcal{N}_S^{RA}$  is an RA-node, that uses the hypothetical syllogism scheme from propositional logic. Conflict is displayed with CA-nodes NEG<sub>1</sub> and NEG<sub>2</sub>, instantiations of a conflict scheme based on propositional contraries.

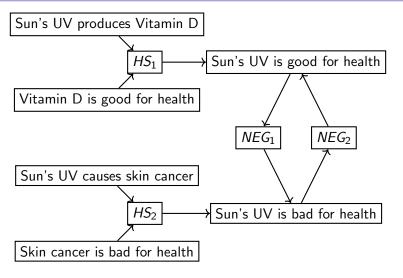


Figure: Argument network containing a rebuttal in natural language