

See Through Walls with Wi-Fi



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Wonseok

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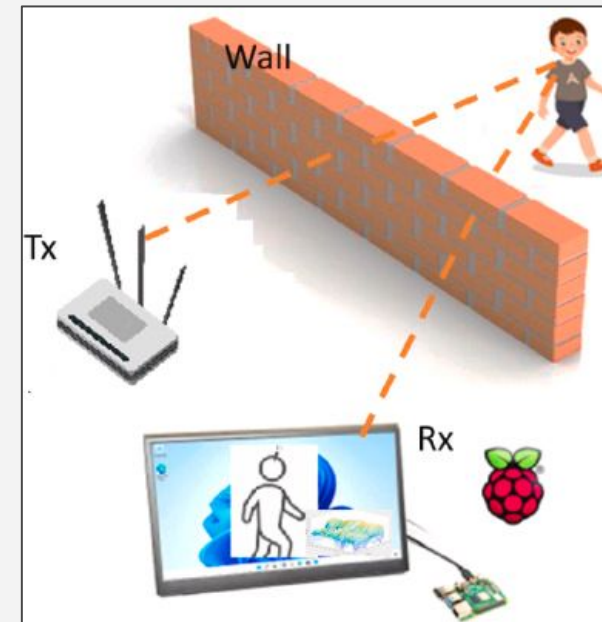
Overview

- Background

- Reflections of signals are imprinted with a signature of what's inside a closed room
- Limitations of existing systems
 - An 2.4 meters long antenna array
 - To achieve smaller **Angular Resolution**
 - At 2 GHz ultra wide bandwidth
 - To eliminate **Flash Effect**

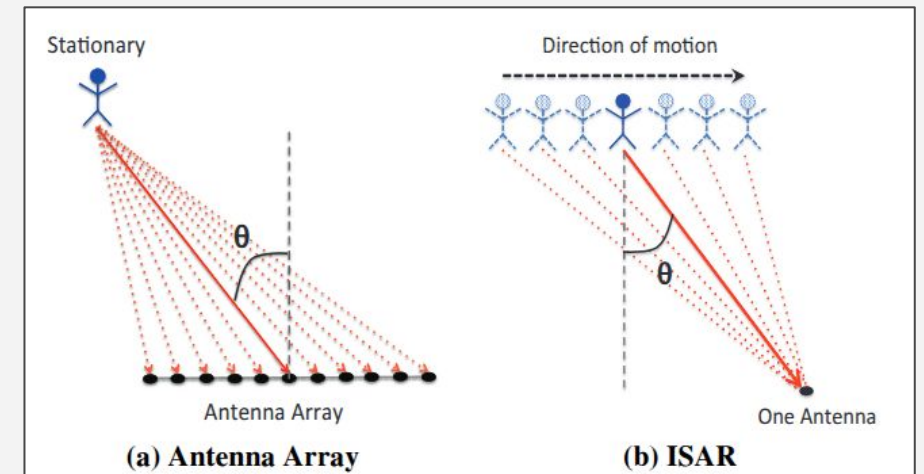
- Terms

- Angular Resolution
 - The smallest angle that can reliably detect two objects
 - The longer antenna array, the smaller angular resolution
- Flash Effect
 - Strong reflections from nearby surfaces
 - The wider the bandwidth, the less flash effect



Core Problems

- Ultra-wide Bandwidth (2GHz)
 - How to eliminate flash effect without using GHz bandwidth?
 - Use MIMO → nulling to eliminate reflections (signals)
 - 1. (Tx ↔ Rx) Measure the CSI matrix
 - 2. (Tx → Rx) Null the signals
 - Reflections off static objects are nulled
 - Received signals are only reflections of moving objects
- Long Antenna Array (2.4m)
 - How to track moving objects without an antenna array?
 - Use ISAR* → virtual antenna array in snapshots
 - 1. Take snapshots of phase shift of a moving target
 - 2. Estimate a steering vector fits with θ
 - A moving target acts as an antenna array

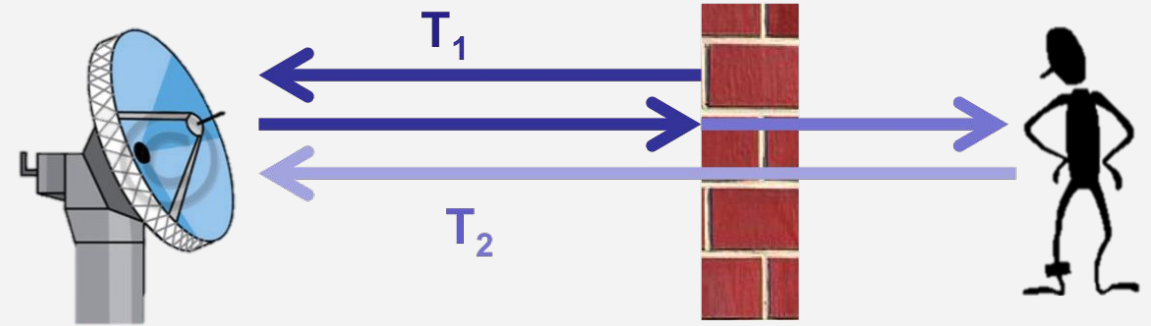


*ISAR: Inverse Synthetic Aperture Radar

Wi-Vi

• Hardware Requirements

- OFDM signals at 2.4GHz
- 3-antenna MIMO (2 Tx + 1 Rx)
- Directional antennas



• Main Components

- 1. MIMO Nulling
 - To eliminate the **flash effect** off the wall
- 2. Inverse SAR
 - To track a moving object and to detect gestures

Building Materials	2.4 GHz
Glass	3 dB
Solid Wood Door 1.75 inches	6 dB
Interior Hollow Wall 6 inches	9 dB
Concrete Wall 18 inches	18 dB
Reinforced Concrete	40 dB

• Challenges

- Severe **RF attenuation** and low reflection coefficient of target object
- **Direct signals** from Tx antennas to Rx antenna

Eliminate Flash Effect

- 1. Initial Nulling

- a. Measure the CSI h_1, h_2 of each antenna

- b. Pre-code only the second antenna as $\rho = -\frac{\hat{h}_1}{\hat{h}_2}$ \longrightarrow

$$h_{receive} = h_1 + h_2\left(-\frac{\hat{h}_1}{\hat{h}_2}\right) \approx 0$$

\rightarrow Ideally, nulling the signals reflected from static objects

- 2. Power Boosting

- Initial nulling also reduces the received signal power

- Making it indistinguishable from noise

\rightarrow Boost the transmit power to increase SNR (roughly by 12 dB)

- 3. Iterative Nulling

- Power boosting also amplifies residual reflections

- Why not first boost the power and measure? \rightarrow ADC saturation

\rightarrow Iteratively re-estimate h'_1, h'_2 with the power boosted

Iterative Nulling

- Problem

- The receiver gets the combined CSI
 - One equation and two unknowns

$$h_{receive} = h_1 + h_2 \left(-\frac{\hat{h}_1}{\hat{h}_2} \right) \approx 0$$

- Solution

- Assume one of \hat{h}_1 and \hat{h}_2 is accurate
 - Errors of \hat{h}_1 and \hat{h}_2 are much smaller than themselves
- Each Tx \rightarrow Rx iteration, alternate \hat{h}_1 and \hat{h}_2 **in turn**

$$\begin{aligned} \hat{h}_1^{(i+1)} &= h_{receive} + \hat{h}_1^{(i)} \\ \hat{h}_2^{(i+1)} &= \left(1 - \frac{h_{receive}}{\hat{h}_1^{(i)}} \right) \hat{h}_2^{(i)} \end{aligned}$$

- Lemma

- \hat{h}_1 and \hat{h}_2 converge exponentially fast

Assume that $\left| \frac{\hat{h}_2 - h_2}{h_2} \right| < 1$, then, after i iterations,

$$|h_{res}^{(i)}| = |h_{res}^{(0)}| \left| \frac{\hat{h}_2 - h_2}{h_2} \right|^i$$

Algorithm

Algorithm 1 Pseudocode for Wi-Vi's Nulling

INITIAL NULLING:

▷ Channel Estimation

Tx ant. 1 sends x ; Rx receives y ; $\hat{h}_1 \leftarrow y/x$ Tx ant. 2 sends x ; Rx receives y ; $\hat{h}_2 \leftarrow y/x$ ▷ Pre-coding: $p \leftarrow -\hat{h}_1/\hat{h}_2$ **POWER BOOSTING:**

Tx antennas boost power

Tx ant. 1 transmits x , Tx ant. 2 transmits px concurrently**ITERATIVE NULLING:** $i \leftarrow 0$ **repeat**Rx receives y ; $h_{res} \leftarrow y/x$ **if** i even **then** $\hat{h}_1 \leftarrow h_{res} + \hat{h}_1$ **else** $\hat{h}_2 \leftarrow \left(1 - \frac{h_{res}}{\hat{h}_1}\right) \hat{h}_2$ $p \leftarrow -\hat{h}_1/\hat{h}_2$

Tx antennas transmit concurrently

 $i \leftarrow i + 1$ **until** Converges

Human Tracking

• Idea

- A moving human can be treated as an antenna array
 - Successive time samples as spatial samples

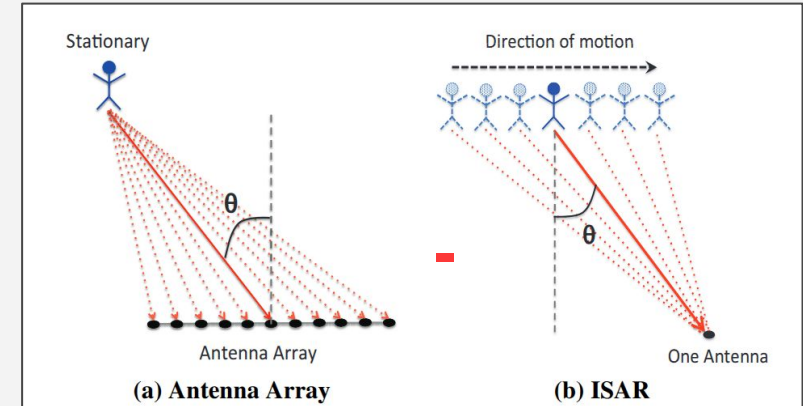
• Phase Shift $\Phi(\theta, n)$

- θ : Spatial angle
 - The angle between human to Wi-Fi and the normal to the motion
- Δ : Spacing between successive antennas
 - $\Delta = vt (v \approx 1m/s)$

• Beamforming

- The virtual antenna array performs 'beamforming'
 - w : Number of time samples
 - $h[n]$: Channel gain

*ISAR: Inverse Synthetic Aperture Radar



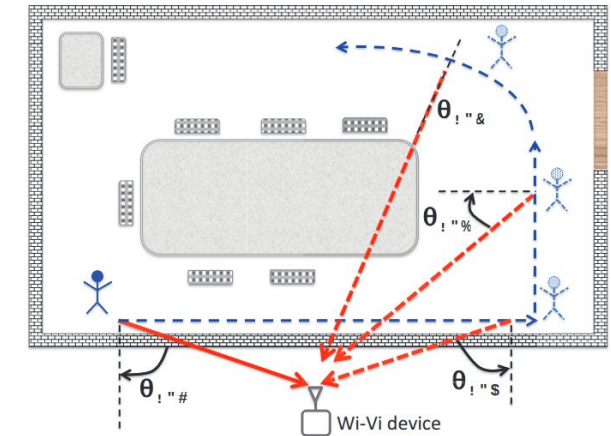
$$\Phi(\theta, n) = \frac{2\pi}{\lambda} n \Delta \sin \theta$$

$$A[\theta, n] = \sum_{i=1}^w h[n + i] e^{j\Phi(\theta, n)}$$

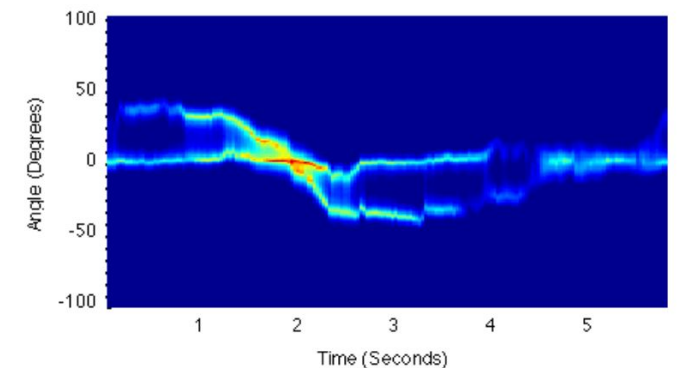
Beamforming

- Motion Direction
 - Estimate θ that maximizes the channel sum
 - Successive time samples as spatial samples
- Experiment Setup
 - **2s**: The person crosses the Wi-Vi device
 - **2s~3s**: The person is moving away from the device
 - **3s**: The person turns inward, but signal gets weaker
- Heatmap Output of $A[\theta, n]$
 - Two lines are present
 - Zero line: Amplified residual reflection on power boosting
 - Curved line: Human motion

$$A[\theta, n] = \sum_{i=1}^w h[n + i] e^{j\Phi(\theta, n)}$$



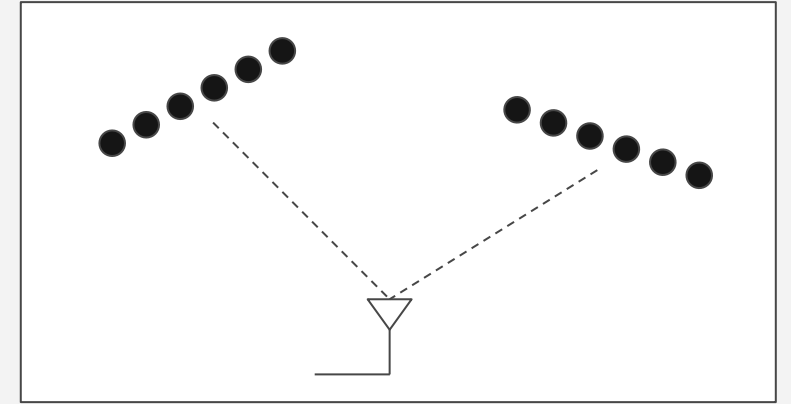
(a) Experimental Setup



Multiple Human Tracking

- MUSIC Algorithm

- Estimate incoming AoAs from entangled channel gain
 - Orthogonality between noise space and steering vectors
- How come?
 - Only a steering vector matters, not distance
 - Antenna spacing Δ are assumed the same ($\Delta = vt(v \approx 1m/s)$)
 - **Limitation** of this paper



- Steps

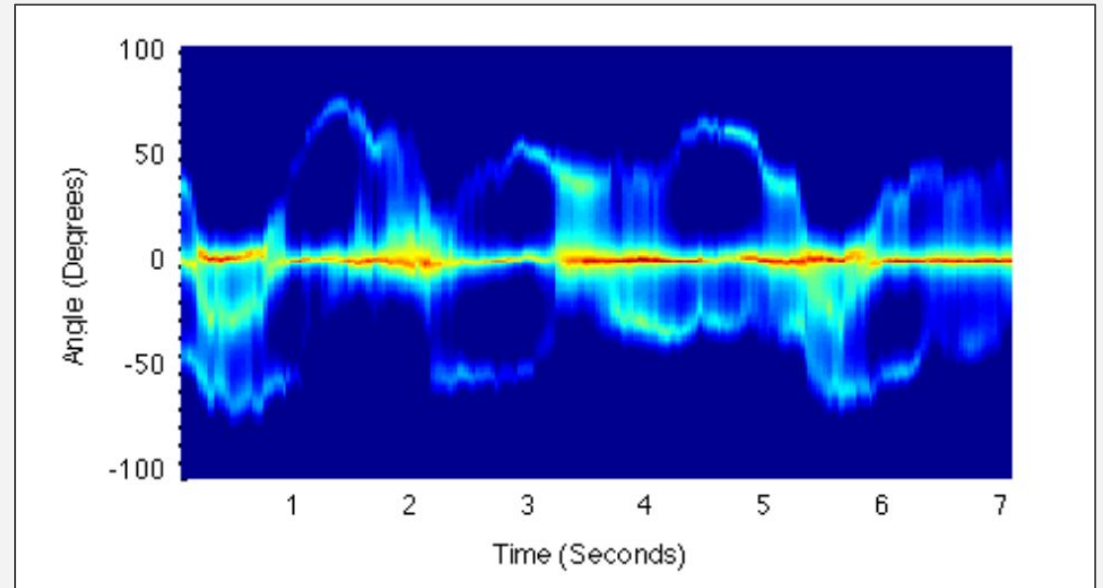
- 1. Create a correlation matrix $R_{w \times w} = E[hh^H]$
- 2. Find noise space from eigen-decomposition
- 3. Project angles onto the noise space
- 4. Find peaks at θ
 - Orthogonality at θ

$$A'[\theta, n] = \frac{1}{\sum_{k=1}^K || \sum_{i=1}^w e^{-j \frac{2\pi}{\lambda} i \Delta \sin \theta} U_N[n](i, k) ||^2}.$$

$$P_{MUSIC}(\theta) = A'[\theta, n] = \frac{1}{||U_n^H \vec{a}_n(\theta)||}$$

Number of Humans

- Number of Humans
 - Heuristically found
 - N people → N lines on the graph
 - Try machine learning
 - Related to $\text{VAR}[\theta]$ in statistical sense
 - Machine Learning (Classification)
 - How many people given $\text{VAR}[\theta]$?
 - **Input:** time-averaged angular variance
- $$x = \frac{1}{T} \sum_{n=1}^T \text{VAR}_n[\theta]$$
- **Output:** 0, 1, 2, or 3 humans



$$E[n] \approx C[n] = \sum_{\theta=-90}^{90} \theta \cdot 20 \log_{10} A'[\theta, n]$$

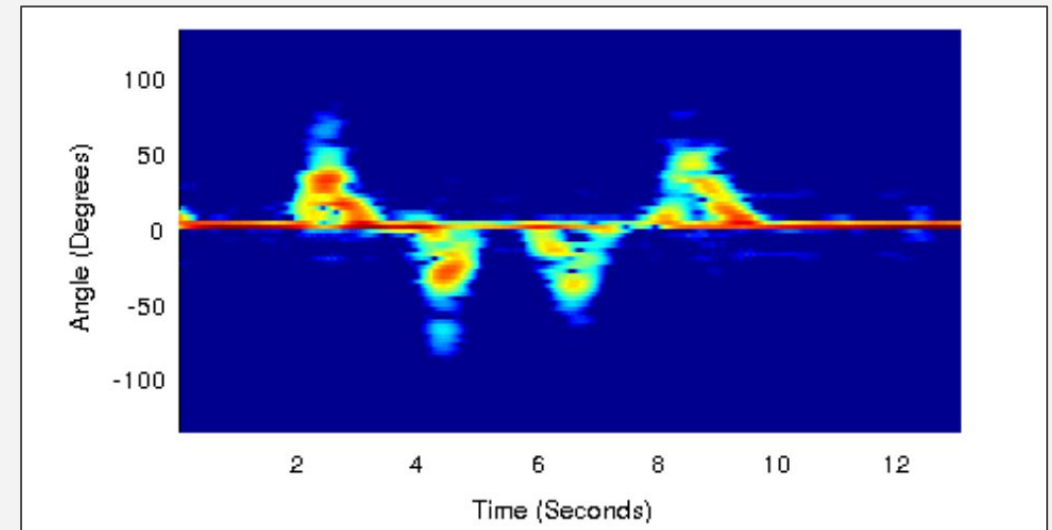
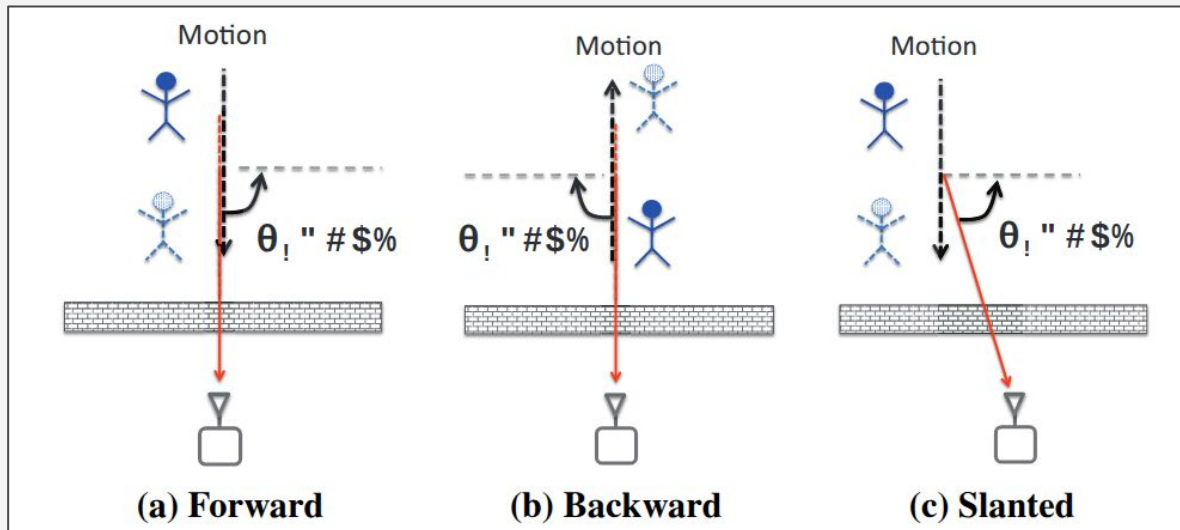


$$\text{VAR}_n[\theta] = E[\theta^2] - E^2[\theta]$$

Gesture Encoding

- Gestures

- '0' : A step forward + a step backward
 - MUSIC peaks at positive θ first
- '1': A step backward + a step forward
 - MUSIC peaks at negative θ first



Gesture Decoding

- Decoding Steps
 - 1. Apply 'matched filter' on the heatmap $A[\theta, n]$
 - Matched filter's template: ▲ ▼

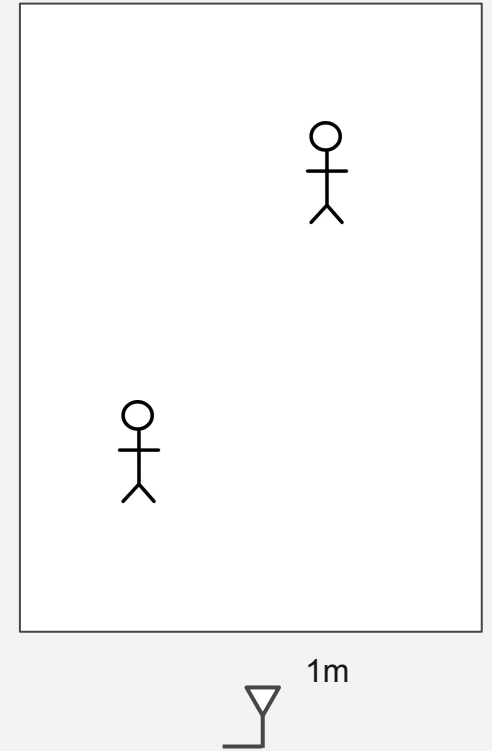
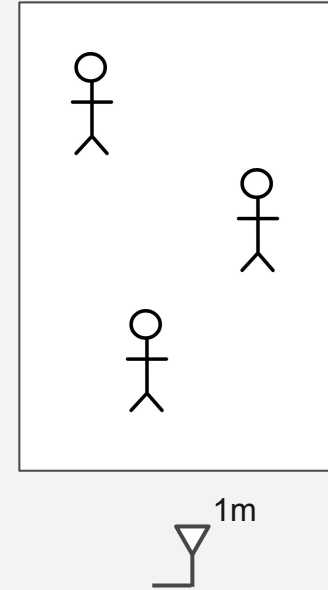
$$Matched\ Output = \sum_{\theta=90}^{90} A[\theta, n] * template[\theta]$$

- 2. Apply peak detector on the output

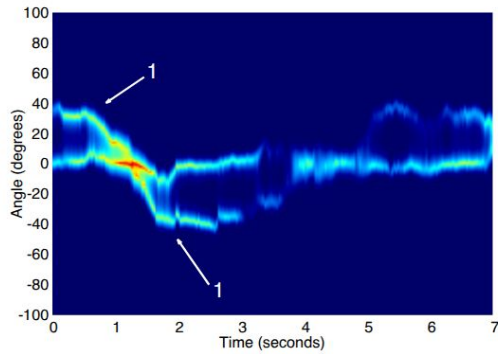
Environment

- Locations

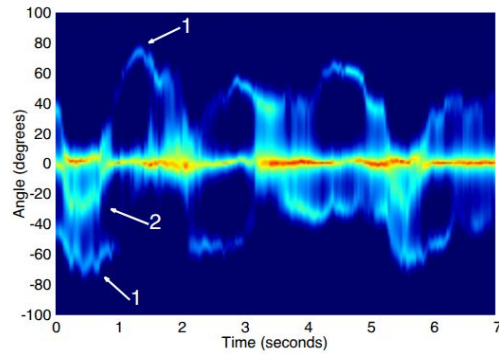
- Two conference rooms with standard furniture (tables, chairs, ...)
 - Room A: 7 X 4 meters
 - Room B: 11 X 7 meters
 - Wall: 6-inch, hollow
- Wi-Vi device 1m away from a wall



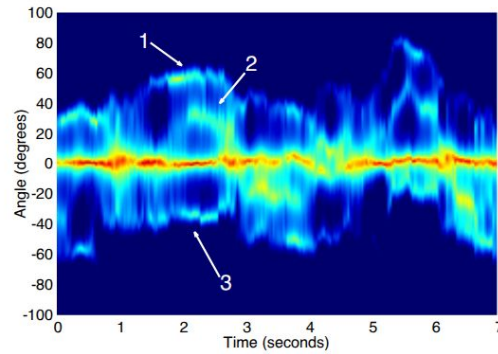
Tracking



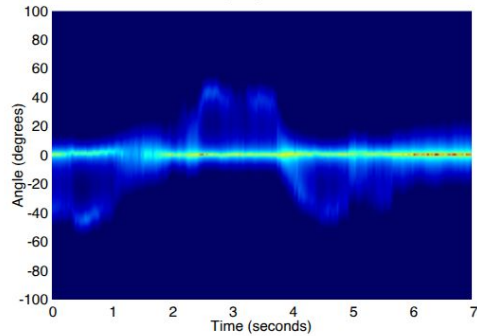
(a1)



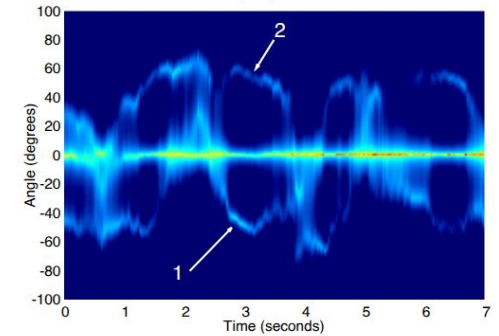
(b1)



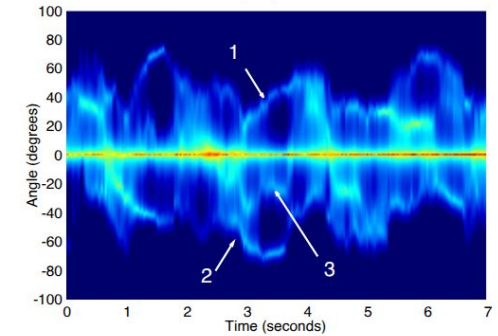
(c1)



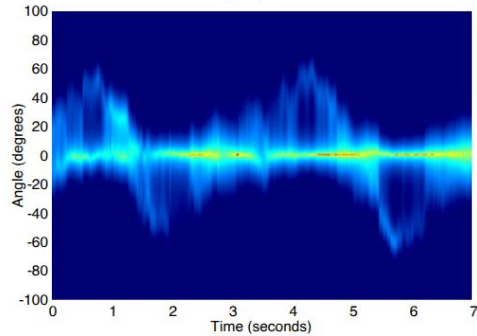
(a2)



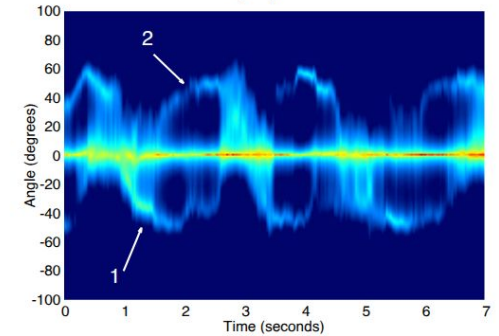
(b2)



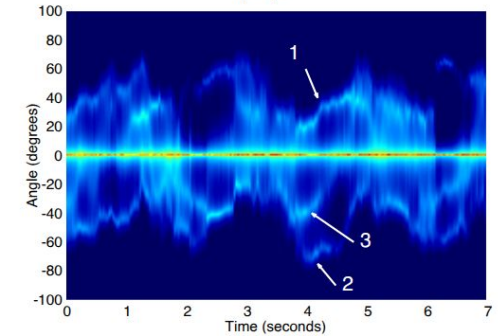
(c2)



(a3)



(b3)



(c3)

(a) One Human

(b) Two Humans

(c) Three Humans

- Brightness
--> Indicates distance

- Fuzziness
--> Worsen by body partsz

$$P_{MUSIC}(\theta) = A'[\theta, n] = \frac{1}{||U_n^H \vec{a}_n(\theta)||}$$

Automatic Detection

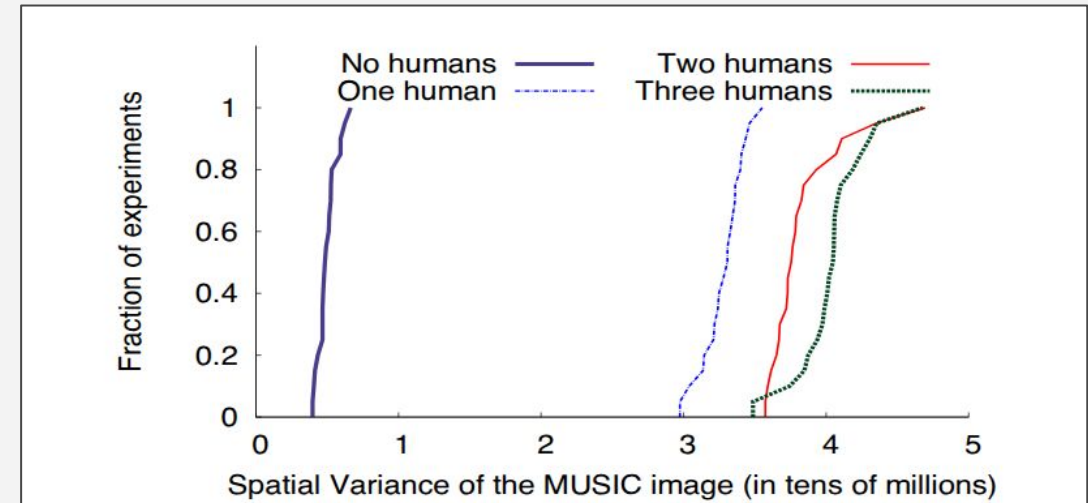
- CDF (20 Trials each)

- **x-axis:** spatial variance $\frac{1}{T} \sum_{n=1}^T VAR_n[\theta]$ \longrightarrow
- **y-axis:** fraction of experiments
- \rightarrow **y** trials had variance \leq **x**

$$VAR[n] = \sum_{\theta=-90}^{90} \theta^2 C[n] - C[n]^2$$

- Observations

- Spatial variance is higher with more moving bodies
- Steep curves \rightarrow consistent variance
- The separation between successive CDFs ▼



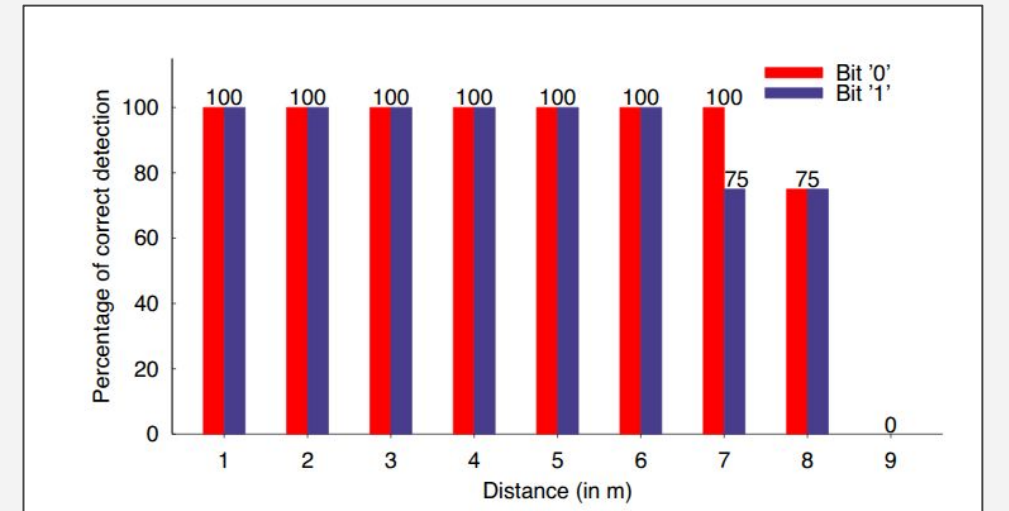
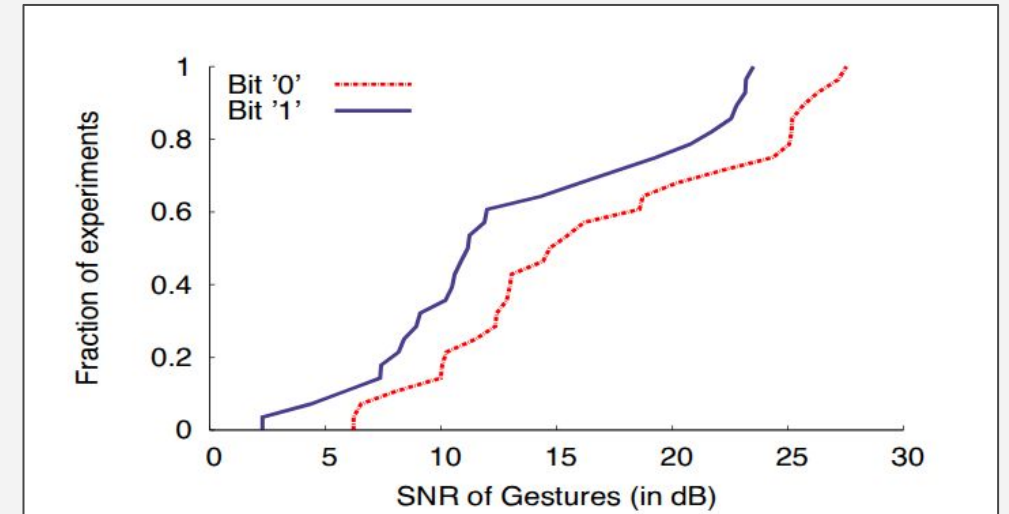
- Accuracy

- Training set on Room A, testing set on Room B

Detected \ Actual		Detected			
		0	1	2	3
Actual	0	100%	0%	0%	0%
	1	0%	100%	0%	0%
	2	0%	0%	85%	15%
	3	0%	0%	10%	90%

Gesture Decoding

- CDF
 - '0' bit's SNR is higher than '1'
 - Taking a step forward first -> average closer
 - Taking a step backward is naturally harder
 - People tend to take smaller steps
- Accuracy
 - 9m: 0% -> not enough energy to detect from the noise
 - 20mW used (USRP)
 - Never mistook '0' or '1' bit



Conclusion

- Impact
 - First low-bandwidth through-wall radar
 - Military purpose and ultra wide-band so far
 - MIMO interference nulling
 - Cancelling “flash effect”
- Limitation
 - Moving objects have constant speed
 - Only detect the direction of motion
 - **Cannot** detect if a person stops
 - **Cannot** estimate distance