Zhuo Chen, Yidan Pan Equally contributed

Homework 4

Problem 3

Table 1: General parameters of Training BP Network to Fit f(x) = 1/x

Network parameters				
Topology	$(1+1_{Bias})$ — Varies, refer to the table in each part of the answer — 1			
Transfer function	tanh with slope of 1			
Learning parameters				
Initial weights	drawn from $U[-0.1, 0.1]$			
Learning rate (α)	Varies, refer to the table in each part of the answer			
Momentum	Varies, refer to the table in each part of the answer			
Epoch size $(Epoch)$	200			
Stopping criteria	error $(Err_{RMSD}) < 0.01$ or learn steps =1,000,000			
Monitoring frequency of error measure	Every 10000 learn steps			
Error measure (Err_{RMSD})	Square root of the sum of $(D-y)^2$ that averaged over all training or testing samples (see formula (1) in problem 2)			
Input / output data, representation, scaling				
# training samples (N_{tr})	200 (x values drawn randomly from U[0.1,1])			
# test samples (N_{tst})	100 (x values drawn randomly from $U[0.1,1]$)			
Scaling of inputs	no scaling			
Scaling of outputs	map [global min, global max] to [-1,1]			

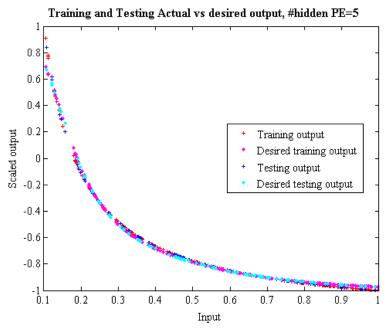
a Different hidden PE number

A small optimization of choosing learning rate and momentum was done. Momentum was picked from the range [0.1,1) first with learning rate = 0.005, with 600,000 learning steps; and learning rate was picked from the range (0.001,0.009), with the optimized momentum that resulted in the lowest error, 0.68. Though a more detailed optimization can be done and repeat for several times for a better result, we found that "luck" is an important condition while doing this simple optimization. The result of using different momentum and/or learning rate will be shown in the next section.

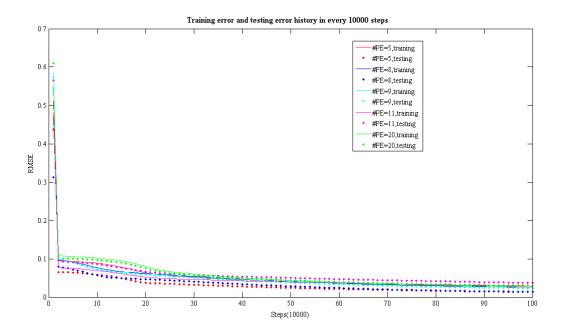
Table 2: Parameters of Training BP Network to Fit f(x) = 1/x with different hidden PE number

Network parameters	
Topology	$(1+1_{Bias})$ — $5, 8, 9, 11, 20+1_{Bias}$ — 1
Learning parameters	
Learning rate (α) Momentum	0.006 0.68

The Testing/Training output versus desired output using 5 hidden PEs is shown as figure below. In general, the output figure are similar during changing PE numbers from 5 to 20, so we only present one of them as the representative.



We then compared the difference of error over time with different PEs. The comparison of error history over time is shown as figure below. The error curves have no peaks as shown in problem2, which indicates that the momentum helps converging. From this figure we can notice that the one with best fitting rate are hidden PE number being equal to 8 and equal to 5. However, the best hidden PE number is not the same all the time (data not shown), revealing the fluctuation of learning.



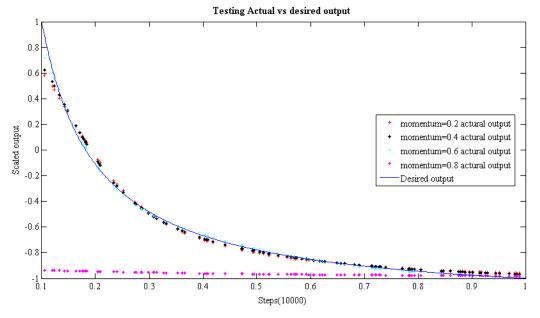
b Different momentum

We hoped to further understand the function of momentum and we tested several of them. Since the testing result showed that the recalling and generalizing were successful (the outputs are similar, while there can be some difference in error rate), we here then only show the testing data.

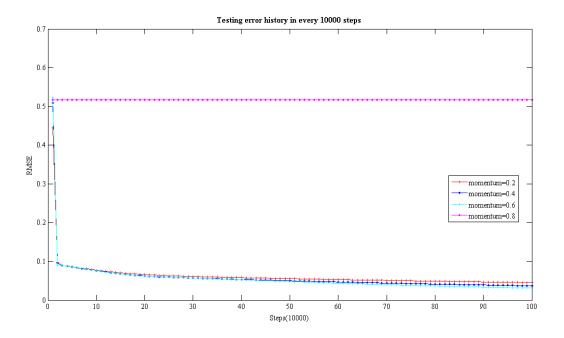
Table 3: Parameters of Training BP Network to Fit f(x) = 1/x with different momentum

Network parameters	
Topology	$(1+1_{Bias})$ — $8+1_{Bias}$ — 1
Learning parameters	
Learning rate (α) Momentum	0.006 0.2, 0.4, 0.6, 0.8

The figure below reveals the output using different momentum. we can see that when momentum get to 0.8, it is too large to make the result converge to a desired error rate.



Also, the error rate history of testing set using different momentum are shown in the figure below. When momentum is around 0.6, the final error rate becomes the lowest.



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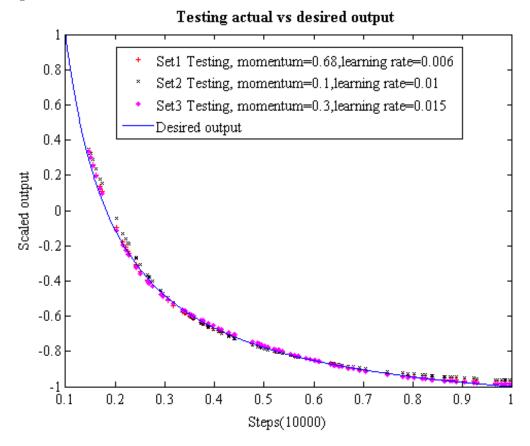
c The best results

From all the figures above we can find that, though finally the reducing of error was getting to a plateau stage, we can still have lower error rate with more steps. Here we limit the maximum learning step as 1,000,000, which is the same as shown before.

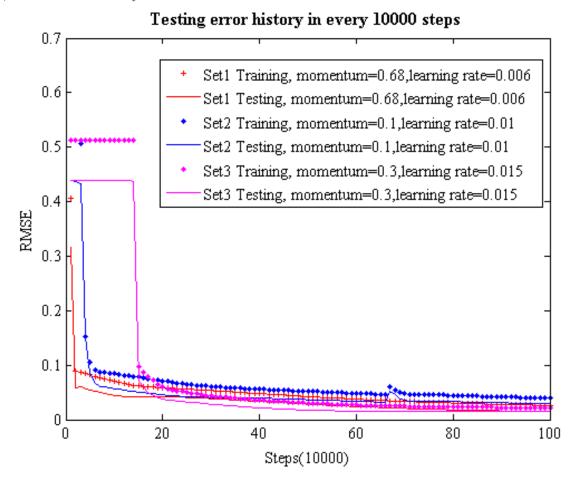
Table 4: Parameters of Training BP Network to Fit f(x) = 1/x that gives the best results

Network parameters						
Topology	$(1+1_{Bias})$ —	$8 + 1_{Bias}$	—1			
Learning parameters						
	Learning rate (α)	Momentum	Testing error	Training error		
Set 1	0.006	0.68	0.0151	0.0261		
Set 2	0.01	0.1	0.0289	0.0392		
Set 3	0.015	0.3	0.0145	0.0219		

The three best outputs are shown in the figure below. Here we only showed the testing output since the training outputs are similar to them in this graph. We can also notice that when input get to a larger value, the learning and the regression is better.



Also, we showed the history of error rate reduction over time.

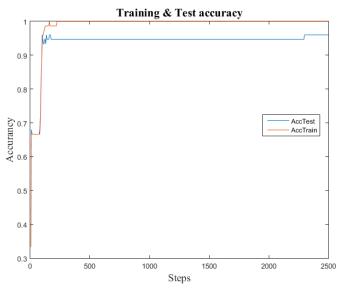


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Table 5: Parameters of Training BP Network to Fit Iris data

Network parameters				
Topology Transfer function	$(4+1_{Bias})$ — $(2+1_{Bias})$ — 3 tanh with slope of 1			
Learning parameters				
Initial weights Learning rate (α) Momentum Epoch size $(Epoch)$ Stopping criteria Error measure	drawn from U[$\frac{-1}{\sqrt{NPE}}$, $\frac{1}{\sqrt{NPE}}$] 0.01 0.7 75 RMSE< 0.2 or learn count (t) > 500 × 75 1 - $\frac{Number\ of\ CorrectlyClassified\ Inputs}{Number\ of\ All\ Inputs}$ (1-Accurancy) and RMSE			
Input / output data, representation, scaling				
# training samples (N_{tr}) # test samples (N_{tst}) Scaling of inputs Scaling of outputs	75 75 already scaled set the maximum element of each column to 1, others to 0			

^{*} As stated, we calculate the error using scaled output, so "Correctly Classified" means exactly same output as desired.



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Table 6: Desired output vs Actual output(Test set)

Actual Desired	Class 1	Class 2	Class 3
Class 1	25	0	0
Class 2	0	24	2
Class 3	0	1	23
Accurancy	1	0.96	0.92

Total Accurancy:0.96

*Class 1 is Setosa, Class 2 is Versacolor, Class 3 is Virginica

In this problem, we tried different topology and training parameters. We find it needs at least 2 hidden PEs to get good result, and more hidden PEs cannot improve the performance. We also tried different momentums and learning rates. As expected, we find that large momentums or learning rate will make the training doesn't converge. Furthermore, smaller learning rate/momentum or more training iterations cannot increase the accurancy. So we pick the largest learning rate and momentum (among we tested) to achieve fastest convergence.

As stated in the parameter table, this time we use RMSE rather than classification error as the stopping criteria. When we plot the change of Accurancy and RMSE along triaining iterations, we can see that even the Accurancy of trianing set hit 100%, the RMSE of both test and training set is still decreasing, and the Accurancy of test set increases after 2,000 learning steps. So if we use the accurancy as the stopping criteria, it will limit the performance of the network.

We think for small datasets as this time, use RMSE as stopping criteria could give better result. Maybe if the dataset is large, restrict the classification accurancy could prevent overfitting issues.

We gives the "Desired output versus Actual output" plot as a classification matrix (Table 3). It's straightforward and contains all the informations we concerned: the performance of each class and the location of error (Since no one concerns the order of samples). Since the training set is perfectly classificated, we didn't show the results

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for training set.

From the Table 3 we can see only class 1 is perfectly classified. Maybe its because class 1 is linearly separatable from the other 2 classes.