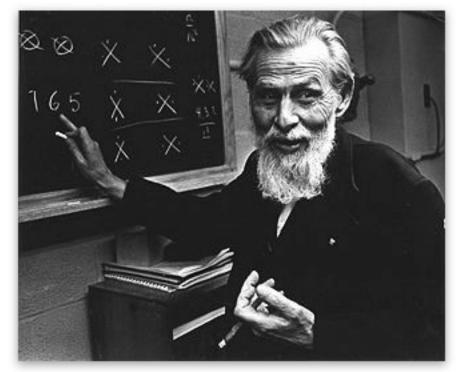
# Perceptron — Intro to Artificial Neural Networks

Diagrams and content from A. Géron Hands on Machine Learning

https://www.amazon.fr/Hands-Machine-Learning-Scikit-Learn-TensorFlow/dp/1491962291

- Artificial Neural networds have been arounf for a while...
- First introduced in 1943 by the neurophysiologist Warren McCulloch and the mathematician Walter Pitts.



https://alchetron.com/Warren-Sturgis-McCulloch

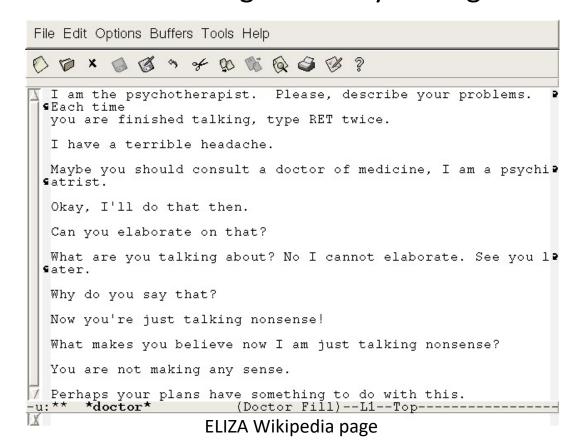
Interest in ANNs came in waves :

1960s: people thought we would soon be conversing with truly intelligent

machines.

• ELIZA, Weisenbaum 1964 :

• When this was'nt the case, funding went elsewhere...



- 1980s : revival of interest, new architectures invented, better training techniques, but progress was slow...
- by the 90s, other machine learning techniques were invented (SVMs) => seemed to offer better results and stronger theoretical foundations.

- Present day: another wave of interest, but this one seems to be different:
  - Now a huge quantity of data available to train neural networks, and ANNs frequently outperform other ML techniques on very large and complex problems.
  - Tremendous increase in computing power since the 1990s now makes it possible to train large neural networks in a reasonable amount of time.
  - Training algorithms have been improved.
  - ANNs seem to have entered a virtuous circle of funding and progress.

### Biological Neurons

- Biological neurons receive short electrical impulses called signals from other neurons via synapses.
- When a neuron receives a sufficient number of signals from other neurons, it fires its own signals.

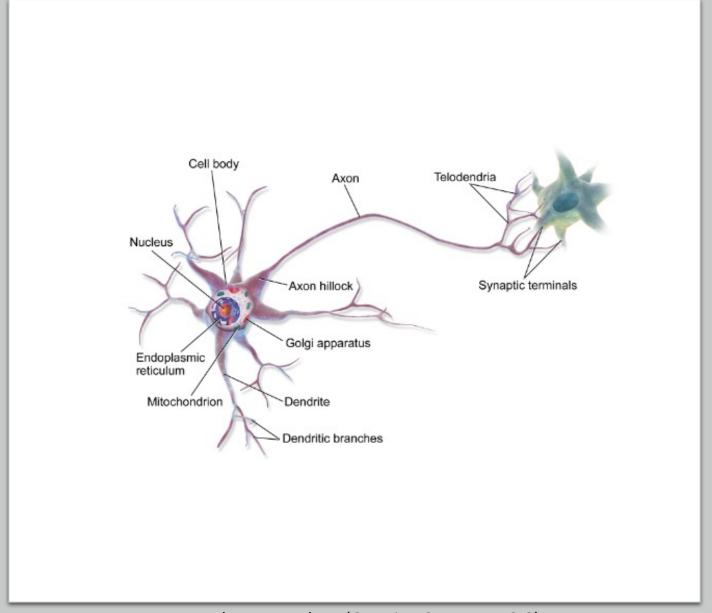


Image by Bruce Blaus (Creative Commons 3.0).
Reproduced from https://en.wikipedia.org/wiki/Neuron

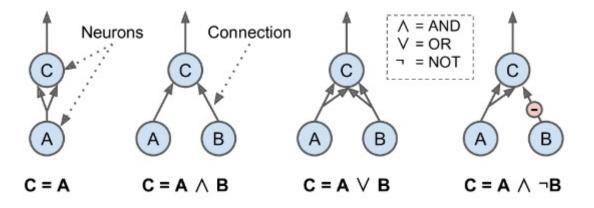
### Biological Neurons

- Organized in a vast network of billions of neurons, each neuron typically connected to thousands of other neurons.
- Research suggests that neurons are often organized in consecutive layers



#### Logical Computations with Neurons

- Warren McCulloch and Walter Pitts proposed a very simple model of the biological neuron
- It has one or more binary (on/off) inputs and one binary output.

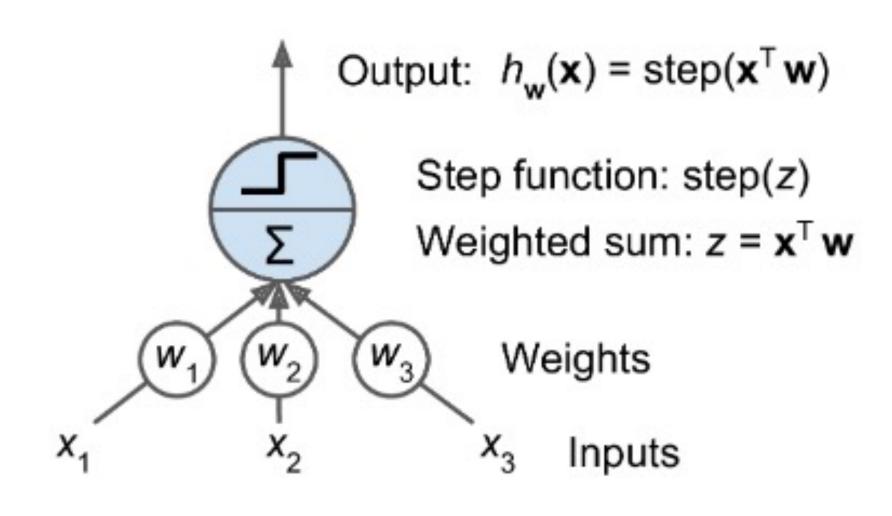


#### The Perceptron

 One of the simplest ANN architectures, invented in 1957 by Frank Rosenblatt

• These artificial neurons are slightly different and are called *Threshold Logic Units*. We will see why.

#### Threshold Logic Unit (TLU)



#### The Step Function

• Most commonly used is the *Heaviside Step Function*:

heaviside 
$$(z) = \begin{cases} 0 & \text{if } z < 0 \\ 1 & \text{if } z \ge 0 \end{cases}$$

• How does this single unit compare to logistic regression?

#### Binary Classification

• A single TLU can be used for simple linear binary classification.

• It computes a linear combination of the inputs and if the result exceeds a threshold, it outputs the positive class or else outputs the negative class.

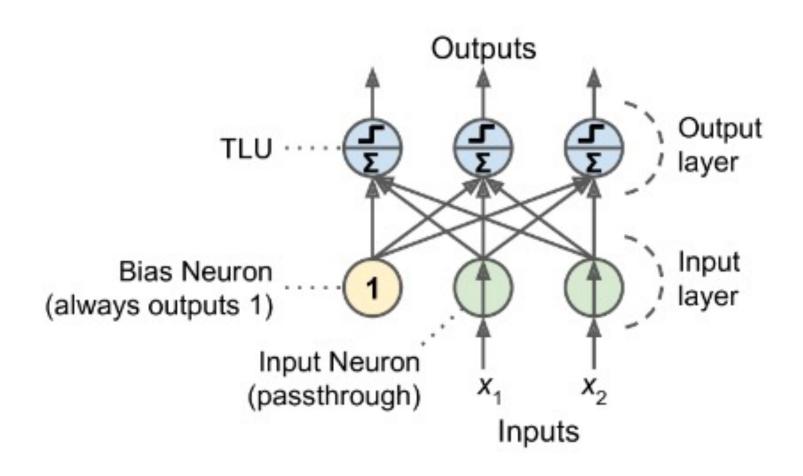
• Training a TLU in this case means finding the right values for w0, w1, and w2 (we will see the training algo in a few slides.)

#### Perceptron

• The Perceptron can refer to this single TLU, but also can refer to a single *layer* of TLUs.

• When all the neurons in a layer are connected to every neuron in the previous layer, it is called a *fully connected layer* or a *dense layer*.

## Perceptron Diagram



#### Perceptron

• Common to draw special passthrough neurons called input neurons

Also, an extra bias feature is usually added.

 This Perceptron can classify instances simultaneously into three different binary classes, which makes it a multi-output classifier

## Computing the outputs of a fully connected layer

$$h_{\boldsymbol{W},\boldsymbol{b}}(\boldsymbol{X}) = activation(\boldsymbol{X}\boldsymbol{W} + \boldsymbol{b})$$

- X represents the matrix of input features. It has one row per instance, one column per feature.
- The weight matrix **W** contains all the connection weights except for the ones from the bias neuron. It has one row per input neuron and one column per artificial neuron in the layer.
- The bias vector **b** contains all the connection weights between the bias neuron and the artificial neurons. It has one bias term per artificial neuron. (this bias can be subsumed into **W** however, as we saw for logistic regression)
- The activation function: when the artificial neurons are TLUs, it is a step function (but we will discuss other activation functions, the sigmoid function being one of them).

#### How is the Perceptron trained?

- In his book *The Organization of Behavior*, published in 1949, Donald Hebb suggested that *when a biological neuron often triggers another neuron*, the *connection* between these two neurons *grows stronger*.
- "Cells that fire together, wire together." (Siegrid Löwel)
- Perceptrons are trained using a variant of this rule that takes into account the error made by the network
- For every output neuron that produced a wrong prediction, it reinforces the connection weights from the inputs that would have contributed to the correct prediction.

#### Perceptron Learning Rule

$$w_{i,j}^{\text{(next step)}} = w_{i,j} + \eta (y_j - \hat{y}_j) x_i$$

- $w_{i,j}$  is the connection weight between the i-th input neuron and the j-th output neuron.
- $x_i$  is the i-th input value of the current training instance.
- $\hat{y}_i$  is the output of the j-th output neuron for the current training instance.
- $y_j$  is the target output of the j-th output neuron for the current training instance.
- $\eta$  is the learning rate.

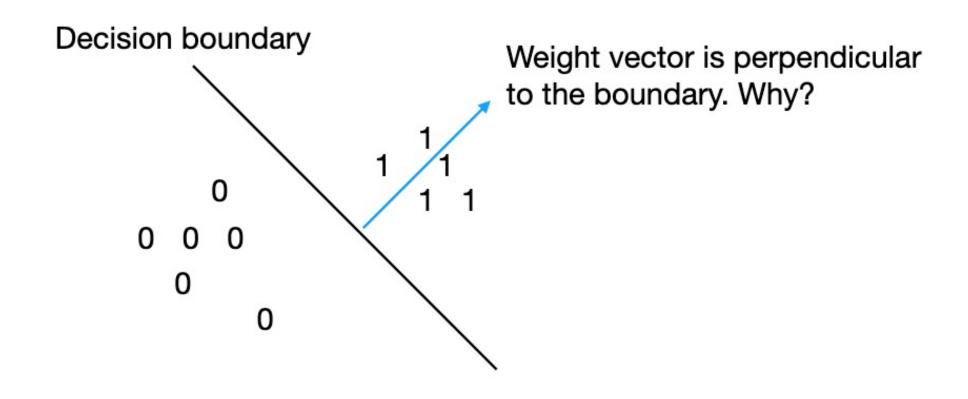
#### What can the Perceptron Learn?

Cannot learn complex patterns in the data

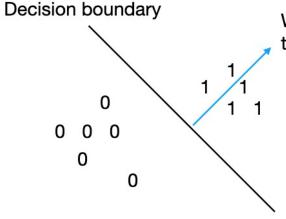
• However, if the training instances are linearly separable, Rosenblatt demonstrated that this algorithm would converge to a solution.

#### Geometric Intuition of the Learning Rule

(Sebastian Raschka: https://www.youtube.com/watch?v=Fj7BgxI73TA)



## Geometric Intuition of the Learning Rule



Weight vector is perpendicular to the boundary. Why?

Remember,

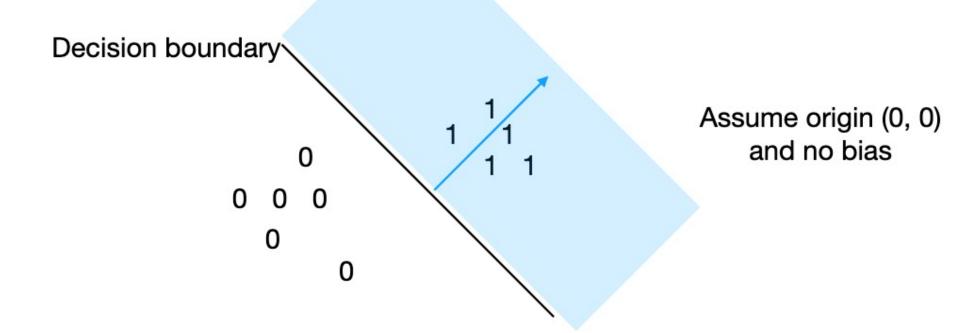
$$\hat{y} = \begin{cases} 0, \ \mathbf{w}^T \mathbf{x} \le 0 \\ 1, \ \mathbf{w}^T \mathbf{x} > 0 \end{cases}$$

$$\mathbf{w}^T \mathbf{x} = ||\mathbf{w}|| \cdot ||\mathbf{x}|| \cdot \cos(\theta)$$

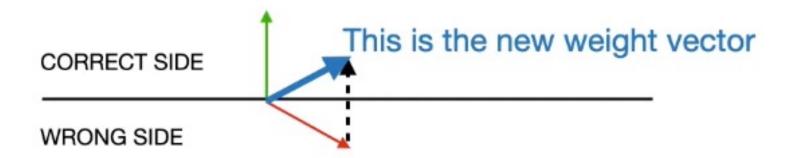
So this needs to be 0 at the boundary, and it is zero at  $90^{\circ}$ 

#### What else does this mean?

Every input vector on this side will have an angle with the weight vector that is  $<90^{\circ}$ 



#### input vector for an example with label 1



For this weight vector, we make a wrong prediction; hence, we update

#### Sklearn Perceptron

 Scikit-Learn provides a Perceptron class that implements a single TLU network (iris dataset example):

```
import numpy as np
from sklearn.datasets import load_iris
from sklearn.linear_model import Perceptron

iris = load_iris()
X = iris.data[:, (2, 3)] # petal length, petal width
y = (iris.target == 0).astype(np.int) # Iris Setosa?

per_clf = Perceptron()
per_clf.fit(X, y)

y_pred = per_clf.predict([[2, 0.5]])
```