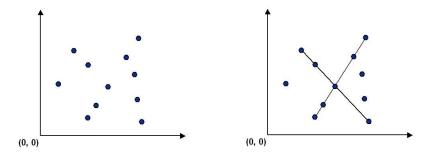
## **Programming Assignment 3: Pattern Recognition**

Write a program to recognize line patterns in a given set of points.

Computer vision involves analyzing patterns in visual images and reconstructing the real-world objects that produced them. The process is often broken up into two phases: *feature detection* and *pattern recognition*. Feature detection involves selecting important features of the image; pattern recognition involves discovering patterns in the features. We will investigate a particularly clean pattern recognition problem involving points and line segments. This kind of pattern recognition arises in many other applications such as statistical data analysis.

The problem. Given a set of n distinct points in the plane, find every (maximal) line segment that connects a subset of 4 or more of the points.



Point data type. Create an immutable data type Point that represents a point in the plane by implementing the following API:

```
public class Point implements Comparable<Point> {
   public Point(int x, int y)
                                                       // constructs the point (x, y)
   public
            void draw()
                                                       // draws this point
           void drawTo(Point that)
                                                       // draws the line segment from this point to that point
   public
  public String toString()
                                                      // string representation
                        int compareTo(Point that)
                                                      // compare two points by y-coordinates, breaking ties by x-coordinates
  public
  public
                     double slopeTo(Point that)
                                                       // the slope between this point and that point
  public Comparator<Point> slopeOrder()
                                                      // compare two points by slopes they make with this point
```

To get started, use the data type <u>Point.java</u>, which implements the constructor and the draw(), drawTo(), and toString() methods. Your job is to add the following components.

- The compareTo() method should compare points by their y-coordinates, breaking ties by their x-coordinates. Formally, the invoking point  $(x_0, y_0)$  is less than the argument point  $(x_1, y_1)$  if and only if either  $y_0 < y_1$  or if  $y_0 = y_1$  and  $x_0 < x_1$ .
- The slopeTo() method should return the slope between the invoking point  $(x_0, y_0)$  and the argument point  $(x_1, y_1)$ , which is given by the formula  $(y_1 y_0) / (x_1 x_0)$ . Treat the slope of a horizontal line segment as positive zero; treat the slope of a vertical line segment as positive infinity; treat the slope of a degenerate line segment (between a point and itself) as negative infinity.
- The slopeOrder() method should return a comparator that compares its two argument points by the slopes they make with the invoking point  $(x_0, y_0)$ . Formally, the point  $(x_1, y_1)$  is *less than* the point  $(x_2, y_2)$  if and only if the slope  $(y_1 y_0) / (x_1 x_0)$  is less than the slope  $(y_2 y_0) / (x_2 x_0)$ . Treat horizontal, vertical, and degenerate line segments as in the slopeTo() method.
- Do *not* override the equals() or hashCode() methods.

Corner cases. To avoid potential complications with integer overflow or floating-point precision, you may assume that the constructor arguments x and y are each between 0 and 32,767.

Line segment data type. To represent line segments in the plane, use the data type LineSegment.java, which has the following API:

**Brute force.** Write a program BruteCollinearPoints.java that examines 4 points at a time and checks whether they all lie on the same line segment, returning all such line segments. To check whether the 4 points p, q, r, and s are collinear, check whether the three slopes between p and q, between p and q, and between p and q are all equal.

The method segments() should include each line segment containing 4 points exactly once. If 4 points appear on a line segment in the order  $p \rightarrow q \rightarrow r \rightarrow s$ , then you should include either the line segment  $p \rightarrow s$  or  $s \rightarrow p$  (but not both) and you should not include *subsegments* such as  $p \rightarrow r$  or  $q \rightarrow r$ . For simplicity, we will not supply any input to BruteCollinearPoints that has 5 or more collinear points.

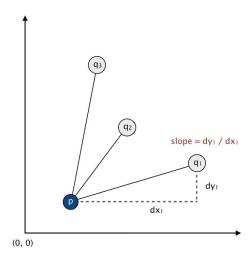
Corner cases. Throw a java.lang.NullPointerException either the argument to the constructor is null or if any point in the array is null. Throw a java.lang.IllegalArgumentException if the argument to the constructor contains a repeated point.

Performance requirement. The order of growth of the running time of your program should be  $n^4$  in the worst case and it should use space proportional to n plus the number of line segments returned.

A faster, sorting-based solution. Remarkably, it is possible to solve the problem much faster than the brute-force solution described above. Given a point p, the following method determines whether p participates in a set of 4 or more collinear points.

- Think of *p* as the origin.
- For each other point q, determine the slope it makes with p.
- Sort the points according to the slopes they makes with p.
- Check if any 3 (or more) adjacent points in the sorted order have equal slopes with respect to p. If so, these points, together with p, are collinear.

Applying this method for each of the n points in turn yields an efficient algorithm to the problem. The algorithm solves the problem because points that have equal slopes with respect to p are collinear, and sorting brings such points together. The algorithm is fast because the bottleneck operation is sorting.



Write a program FastCollinearPoints. java that implements this algorithm.

```
public class FastCollinearPoints {
   public FastCollinearPoints(Point[] points)
   public    int numberOfSegments()
   public LineSegment[] segments()
}

// finds all line segments containing 4 or more points
// the number of line segments
// the line segments
}
```

The method segments() should include each *maximal* line segment containing 4 (or more) points exactly once. For example, if 5 points appear on a line segment in the order  $p \rightarrow q \rightarrow r \rightarrow s \rightarrow t$ , then do not include the subsegments  $p \rightarrow s$  or  $q \rightarrow t$ .

Corner cases. Throw a java.lang.NullPointerException either the argument to the constructor is null or if any point in the array is null. Throw a java.lang.IllegalArgumentException if the argument to the constructor contains a repeated point.

Performance requirement. The order of growth of the running time of your program should be  $n^2 \log n$  in the worst case and it should use space proportional to n plus the number of line segments returned. FastCollinearPoints should work properly even if the input has 5 or more collinear points.

**Sample client.** This client program takes the name of an input file as a command-line argument; read the input file (in the format specified below); prints to standard output the line segments that your program discovers, one per line; and draws to standard draw the line segments.

```
public static void main(String[] args) {
    // read the n points from a file
```

}

```
In in = new In(args[0]);
int n = in.readInt();
Point[] points = new Point[n];
for (int i = 0; i < n; i++) {
    int x = in.readInt();
    int y = in.readInt();
    points[i] = new Point(x, y);
}
// draw the points
StdDraw.enableDoubleBuffering();
StdDraw.setXscale(0, 32768);
StdDraw.setYscale(0, 32768);
for (Point p : points) {
    p.draw();
StdDraw.show();
// print and draw the line segments
BruteCollinearPoints collinear = new BruteCollinearPoints(points);
for (LineSegment segment : collinear.segments()) {
    StdOut.println(segment);
    segment.draw();
StdDraw.show();
```

**Input format.** We supply several sample input files (suitable for use with the test client above) in the following format: An integer n, followed by n pairs of integers (x, y), each between 0 and 32,767. Below are two examples.

```
% more input6.txt
                          % more input8.txt
19000
       10000
                           10000
                                       a
18000
       10000
                               0
                                   10000
                            3000
32000
       10000
                                   7000
21000
       10000
                            7000
                                    3000
1234
        5678
                           20000
                                   21000
                                   4000
14000
       10000
                            3000
                           14000
                                   15000
                            6000
                                   7000
% java BruteCollinearPoints input8.txt
(10000, 0) -> (0, 10000)
(3000, 4000) -> (20000, 21000)
% java FastCollinearPoints input8.txt
(3000, 4000) -> (20000, 21000)
(0, 10000) -> (10000, 0)
% java FastCollinearPoints input6.txt
(14000, 10000) -> (32000, 10000)
```

**Deliverables.** Submit only the files BruteCollinearPoints.java, FastCollinearPoints.java, and Point.java. We will supply LineSegment.java and algs4.jar. You may not call any library functions other those in java.lang, java.util, and algs4.jar. In particular, you may call Arrays.sort().

This assignment was developed by Kevin Wayne. Copyright © 2005.