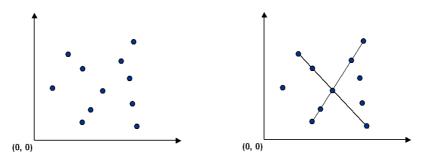
## **Programming Assignment 3: Pattern Recognition**

Write a program to recognize line patterns in a given set of points.

Computer vision involves analyzing patterns in visual images and reconstructing the real-world objects that produced them. The process in often broken up into two phases: *feature detection* and *pattern recognition*. Feature detection involves selecting important features of the image; pattern recognition involves discovering patterns in the features. We will investigate a particularly clean pattern recognition problem involving points and line segments. This kind of pattern recognition arises in many other applications such as statistical data analysis.

**The problem.** Given a set of *N* distinct points in the plane, draw every (maximal) line segment that connects a subset of 4 or more of the points.



Point data type. Create an immutable data type Point that represents a point in the plane by implementing the following API:

```
public class Point implements Comparable<Point> {
   public final Comparator<Point> SLOPE_ORDER;
                                                       // compare points by slope to this point
   public Point(int x, int y)
                                                       // construct the point (x, y)
            void draw()
                                                       // draw this point
   public
   public
            void drawTo(Point that)
                                                       // draw the line segment from this point to that point
   public String toString()
                                                       // string representation
             int compareTo(Point that)
                                                       // is this point lexicographically smaller than that point?
   public
                                                       // the slope between this point and that point
   public double slopeTo(Point that)
```

To get started, use the data type Point.java, which implements the constructor and the draw(), drawTo(), and toString() methods. Your job is to add the following components.

- The compareTo() method should compare points by their y-coordinates, breaking ties by their x-coordinates. Formally, the invoking point  $(x_0, y_0)$  is less than the argument point  $(x_1, y_1)$  if and only if either  $y_0 < y_1$  or if  $y_0 = y_1$  and  $x_0 < x_1$ .
- The slopeTo() method should return the slope between the invoking point  $(x_0, y_0)$  and the argument point  $(x_1, y_1)$ , which is given by the formula  $(y_1 y_0) / (x_1 x_0)$ . Treat the slope of a horizontal line segment as positive zero; treat the slope of a vertical line segment as positive infinity; treat the slope of a degenerate line segment (between a point and itself) as negative infinity.
- The SLOPE\_ORDER comparator should compare points by the slopes they make with the invoking point  $(x_0, y_0)$ . Formally, the point  $(x_1, y_1)$  is *less than* the point  $(x_2, y_2)$  if and only if the slope  $(y_1 y_0) / (x_1 x_0)$  is less than the slope  $(y_2 y_0) / (x_2 x_0)$ . Treat horizontal, vertical, and degenerate line segments as in the slopeTo() method.

**Brute force.** Write a program Brute.java that examines 4 points at a time and checks whether they all lie on the same line segment, printing out any such line segments to standard output and drawing them using standard drawing. To check whether the 4 points p, q, r, and s are collinear, check whether the slopes between p and q, between p and r, and between p and r are all equal.

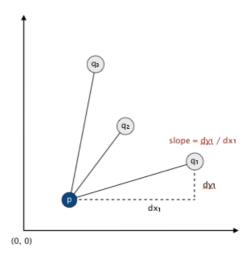
The order of growth of the running time of your program should be  $N^4$  in the worst case and it should use space proportional to N.

A faster, sorting-based solution. Remarkably, it is possible to solve the problem much faster than the brute-force solution described above. Given a point p, the following method determines whether p participates in a set of 4 or more collinear points.

- Think of p as the origin.
- For each other point q, determine the slope it makes with p.
- Sort the points according to the slopes they makes with p.

• Check if any 3 (or more) adjacent points in the sorted order have equal slopes with respect to p. If so, these points, together with p, are collinear

Applying this method for each of the N points in turn yields an efficient algorithm to the problem. The algorithm solves the problem because points that have equal slopes with respect to p are collinear, and sorting brings such points together. The algorithm is fast because the bottleneck operation is sorting.



Write a program Fast.java that implements this algorithm. The order of growth of the running time of your program should be  $N^2 \log N$  in the worst case and it should use space proportional to N.

**APIs.** Each program should take the name of an input file as a command-line argument, read the input file (in the format specified below), print to standard output the line segments discovered (in the format specified below), and draw to standard draw the line segments discovered (in the format specified below). Here are the APIs.

```
public class Brute {
    public static void main(String[] args)
}

public class Fast {
    public static void main(String[] args)
}
```

**Input format.** Read the points from an input file in the following format: An integer N, followed by N pairs of integers (x, y), each between 0 and 32,767. Below are two examples.

% more	input6.txt	% more	input8.txt
6		8	
19000	10000	10000	0
18000	10000	0	10000
32000	10000	3000	7000
21000	10000	7000	3000
1234	5678	20000	21000
14000	10000	3000	4000
		14000	15000
		6000	7000

**Output format.** Print to standard output the line segments that your program discovers, one per line. Print each line segment as an *ordered* sequence of its constituent points, separated by " -> ".

```
% java Brute input6.txt
(14000, 10000) -> (18000, 10000) -> (19000, 10000) -> (21000, 10000)
(14000, 10000) -> (18000, 10000) -> (19000, 10000) -> (32000, 10000)
(14000, 10000) -> (18000, 10000) -> (21000, 10000) -> (32000, 10000)
(14000, 10000) -> (19000, 10000) -> (21000, 10000) -> (32000, 10000)
(14000, 10000) -> (19000, 10000) -> (21000, 10000) -> (32000, 10000)
(18000, 10000) -> (19000, 10000) -> (21000, 10000) -> (32000, 10000)

% java Brute input8.txt
(10000, 0) -> (7000, 3000) -> (3000, 7000) -> (0, 10000)
(3000, 4000) -> (6000, 7000) -> (14000, 15000) -> (21000, 10000)

% java Fast input6.txt
(14000, 10000) -> (18000, 10000) -> (19000, 10000) -> (21000, 10000) -> (32000, 10000)

% java Fast input8.txt
(10000, 0) -> (7000, 3000) -> (3000, 7000) -> (0, 10000)
(3000, 4000) -> (6000, 7000) -> (14000, 15000) -> (0, 10000)
(3000, 4000) -> (6000, 7000) -> (14000, 15000) -> (20000, 21000)
```

Also, draw the points using draw() and draw the line segments using drawTo(). Your programs should call draw() once for each point in the input file and it should call drawTo() once for each line segment discovered. Before drawing, use stdDraw.setXscale(0, 32768) and StdDraw.setYscale(0, 32768) to rescale the coordinate system.

For full credit, do not print *permutations* of points on a line segment (e.g., if you output  $p \rightarrow q \rightarrow r \rightarrow s$ , do not also output either  $s \rightarrow r \rightarrow q \rightarrow p$  or  $p \rightarrow r \rightarrow q \rightarrow s$ ). Also, for full credit in Fast. java, do not print or plot *subsegments* of a line segment containing 5 or more points (e.g., if you output  $p \rightarrow q \rightarrow r \rightarrow s \rightarrow t$ , do not also output either  $p \rightarrow q \rightarrow s \rightarrow t$  or  $q \rightarrow r \rightarrow s \rightarrow t$ ); you should print out such subsegments in Brute. java.

**Deliverables.** Submit only Brute.java, Fast.java, and Point.java. We will supply stdlib.jar and algs4.jar. Your may not call any library functions other than those in java.lang, java.util, stdlib.jar, and algs4.jar.

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