Since Yi ~ Binomial (40, 0)

We know $E[Yi] = n \cdot \theta$ and $var[Yi] = n\theta(1-\theta)$ Therefore, $\theta = \frac{Y}{40}$ is an unbiased estimator for θ say $\hat{\theta} = E[\theta|TiYi]$, where $T(Y) = \frac{Z}{1-\theta}Yi$, Yi represents θ been attions of each you.

So let's prove Tiy) is complete statistics. If this holds, we can then say $\hat{\theta} = E[\hat{\theta}|Tey)]$ is minimum variance unbiased estimator.

And for T(Y), since $Y \in Binomial(40,0)$, $i \in [0,7]$. $T(Y) = \stackrel{?}{\leq} Y : is also a binomial(320,0)$

From the textbook, we can know T(Y) should be a complete statistic.

Proof: Let g be a function such that $E_{\theta}g(T)=0$ $\stackrel{2^{\infty}}{\underset{t=0}{\stackrel{2^{\infty}}{=}}} g(t) \begin{pmatrix} 3^{2^{\infty}} \\ t \end{pmatrix} \theta^{t} (1-\theta)^{3^{2^{\infty}-t}} = 0$ $\stackrel{t=0}{\underset{t=0}{\stackrel{2^{\infty}}{=}}} since \begin{pmatrix} 3^{2^{\infty}} \\ t \end{pmatrix} > 0, \quad \theta^{t} > 0, \quad (1-\theta)^{3^{2^{\infty}-t}} > 0.$

then gits=0 must hold for tte[0,320] and tez

which implies PO(geT=0)=1 for all O.

so T is a complete statistic.

Variance unbiased estimator.

so at this time MSE is minimized.