

# EE FORMULA SHEET

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- $\frac{1}{\rho} = \sigma = \frac{q^2 n \tau}{m^*}$ ; Fermi distribution:  $f(E) = \frac{1}{e^{\frac{E-E_F}{kT}} + 1}$
- When  $E_F < E_C - 3kT$ ,  $n = N_E e^{-\frac{E_C-E_F}{kT}}$ ;  $N_C = 2 \left( \frac{2\pi m_n^* kT}{h^2} \right)^{\frac{3}{2}}$ .
- When  $E_F > E_V + 3kT$ ,  $p = N_V e^{-\frac{E_F-E_V}{kT}}$ ;  $N_V = 2 \left( \frac{2\pi m_p^* kT}{h^2} \right)^{\frac{3}{2}}$ .  $N_C, N_V$  are effective DOSes in the two bands.
- Drift velocity =  $\mu \vec{E}$ ,  $\mu = \frac{e\tau}{m^*}$ ,  $J = -env = \sigma E$
- Where  $\sigma = e(n\mu_e + p\mu_h)$
- Diffusion:  $\Phi(flux) = -Dd_x\eta$  thus  $J_{p,diff} = -eDd_xp$ , same for  $n$ .
- $J_n = en(x)\mu_n V(x) + ED_n \frac{dn(x)}{dx}$ , same for  $p$  with opposite sign for second term.
- Einstein:  $\frac{D_n}{\mu_n} = \frac{kT}{q}$  at equilibrium for non uniform doping
- $E_F = E_i + kT \ln \frac{n_0}{n_i}$ . Same formula for  $p$ , with a minus sign
- $n_0 + N_A = p_D + N_D$
- Continuity equation:  $\frac{\partial n}{\partial x} = \frac{1}{q} \frac{\partial J}{\partial x} + \frac{\partial n}{\partial x} \big|_{thermal, R-G, light}$ . Same for  $p$  with first term negative
- Built in potential  $V_{bi} = \frac{1}{q}((E_i - E_F)_p - (E_i - E_F)_n)$
- Equilibrium in PN junction:  $\frac{p_{p0}}{p_{n0}} = e^{eV_{bi}/kT}$ ; with potential  $p_n = p_{n0} e^{eV_A/kT}$
- Minority carrier diffusion:  $\frac{\partial \Delta n_p}{\partial t} = D_n \frac{\partial^2 \Delta n_p}{\partial x^2} - \frac{\Delta n_p}{\tau_n} + G_L$ , same for  $p_n$
- Poisson's eqn:  $\nabla^2 \phi = -\frac{\rho}{\epsilon} = \frac{q}{\epsilon}((n_0 - p_0) - (N_A - N_D))$
- Depletion width  $W = \sqrt{\frac{2\epsilon}{q} \frac{N_A + N_D}{N_A N_D} V_{bi}}$
- Concentration gradient of minority holes  $\delta p(x_n) = p_{n0}(e^{eV/kT} - 1)e^{-x_n/L_p}$
- $J_p(x_n) = \frac{eD_p}{L_p} \delta p$
- Shockley:  $J = \left( \frac{qD_p}{L_p} p_{n0} + \frac{qD_n}{L_n} n_{p0} \right) (e^{qV_A/kT} - 1) = J_0(e^{\dots} - 1)$ .  $J_0$  is reverse saturation current.
- $R = \frac{dV}{dJ} = \frac{kt}{qJ}$
- $V_{BR} \propto N_B^{-1}$ , where  $N_B$  is doping of lightly doped side
- Schottky:  $e\Phi_B = e\Phi_m - e\chi_s$  ( $\chi_s$  is EA of semiconductor)
- Current  $J = J_s \left( e^{\frac{qV}{kT}} - 1 \right)$ .  $E_{max} = \sqrt{\frac{2eN_D}{\epsilon} (V_D - V)}$
- $\alpha = I_C/I_E, \beta = I_C/I_B$
- Emitter efficiency  $\gamma \simeq i - \frac{I_{En}}{I_{Ep}}$
- Bl
- MOSFET  $I_{D,sat} = \frac{W}{2L} \mu_n C_{ox} (V_{GS} - V_T)^2$
- Saturation discipline:  $V_0 > Vi - V_T, Vi > V_T, V_0 \geq \sqrt{\frac{i_{DS}}{k}}$