

Introductions

Saturday, August 22, 2015

7:08 PM

Connect Math cost?

Examples

1) $-8y + 6 = 22 \rightarrow y = -2$

2) $11 = 7 - 2(50 - 2) \rightarrow y = 0$

3) $\frac{1}{3} - \frac{4}{3t} = \frac{7}{t} \rightarrow t = 25$

4) $\frac{\frac{7}{d-7} - \frac{7}{8}}{\frac{4}{d-7}} = \frac{d}{d-7} \rightarrow d \neq 7$

5) $\frac{\frac{4}{x^2 - 2x - 8} - \frac{1}{x^2 - 16}}{\frac{2}{x^2 + 6x + 8}} = \frac{2}{x^2 + 6x + 8} \rightarrow x = -22$

Functions are a new notation & a new concept based upon things like

$$y = 3x - 7$$

before we wrote the following

$$\text{when } x = -1, y = 3(-1) - 7 \\ = -3 - 7 = -10$$

$$\text{when } x = 3, y = 3(3) - 7 \\ = 9 - 7 = 2$$

the difference in y -values from $x = -1$ to $x = 3$ is

$$\underset{\substack{x=3 \\ y=2}}{2} - \underset{\substack{x=-1 \\ y=-10}}{(-10)} = 12$$

this is clumsy, wordy, inefficient notation how about this

$$y(-1) = y\text{-value when } x = -1$$

$$\text{so } y(-1) = -10$$

$$y(3) = y\text{-value when } x = 3$$

$$\text{so } y(3) = 2$$

$$y(3) - y(-1) = 2 - (-10) = 12$$

difference in y-values

Notation

$y(\#)$ means the y-value
when $x = \#$

$y(x)$ represents the y-value
at an arbitrary/unknown
x-value

$y(x) = 3x - 7$
means that we're defining
 $y(x)$ to be $3x - 7$
you don't need to solve for
anything we I use $:=$

Ex Evaluating functions

Let $f(x) := x^2 - 3x - 10$

Compute the following

$$\begin{aligned} \circ f(-4) &= (-4)^2 - 3(-4) - 10 \\ &= 16 + 12 - 10 \\ &= 18 \end{aligned}$$

$$\circ f(1) = (1)^2 - 3(1) - 10$$

$$= 1 - 3 - 10$$

$$= -12$$

$$\circ f(a) = (a)^2 - 3(a) - 10$$

$$= a^2 - 3a - 10$$

$$\circ f(x+h) = (x+h)^2 - 3(x+h) - 10$$

$$= x^2 + xh + hx + h^2 - 3x - 3h - 10$$

$$= x^2 + 2xh + h^2 - 3x - 3h - 10$$

What are functions

$f(\quad) \rightarrow$

x-values go in here (pointing to the parentheses)

y-values come out here (pointing to the arrow)

Functions are like machines on conveyor belts, taking inputs (x-values) and on the other side produces outputs (y-values)

More formally functions associate/map inputs (x-values) to outputs (y-values) in such a way that each input can only be associated with/mapped to exactly one output

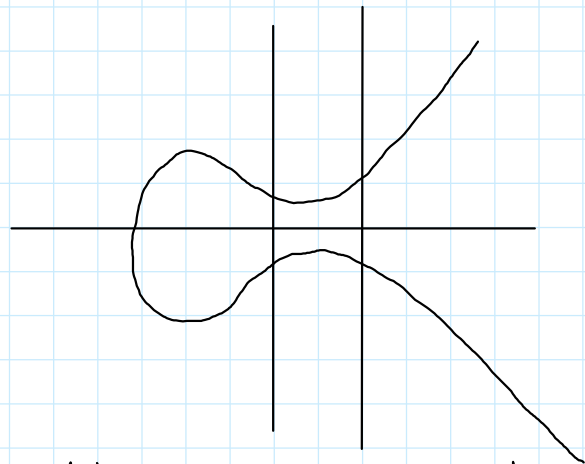
This constraint, that every input be mapped to one and only one output, has a graphical interpretation. It is the vertical line test.

a graph is the graph of a function if every vertical line you could draw crosses the graph no more than one

Ex Vertical Line Test



all vertical lines cross at most once
so this is a function



there is a vertical line (many actually) but one is enough) which crosses more than once
so this is not a function

Domain of a function

is the list of "good" inputs (x-values)
for the function

By good, I mean inputs (x-values)
that avoid any $\div 0$ or any $\sqrt{-\#}$

Ex Domain of function

$$\circ f(x) = \frac{x}{x+3}$$

Domain of $f(x)$ is what?

* we could have to $\div 0$ bc we have
a denom

* no way to have $\sqrt{-\#}$, no $\sqrt{\quad}$ in $f(x)$

to find when denom is 0

set denom = 0 & solve

$$x + 3 = 0$$

$$x = -3$$

this is a bad x-value

this input cause denom of $f(x)$ to be 0

so good inputs are everything else

$$x \neq -3$$

all x -values other than -3

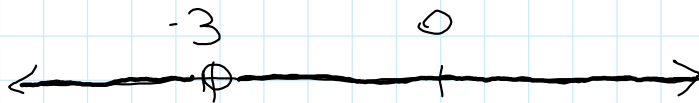
Domain of $f(x) = \frac{x}{x+3}$ is

$x \neq -3$ all x -values other than -3

Interval Notation

The textbook likes its sets & intervals

$x \neq -3$ on number line looks like



in interval notation this is

$$(-\infty, -3) \cup (-3, +\infty)$$

all values ^{join} together
between $-\infty$ and
 -3 not including
either endpoint

all values between
 -3 and $+\infty$ not
including either
endpoint

So book wants us to say

Domain of $f(x) = \frac{x}{x+3}$ is

$$(-\infty, -3) \cup (-3, +\infty)$$

More Ex of Domain of a Function

• $g(t) = \sqrt{2-t}$

Domain of $g(t)$

no denoms in $g(t)$ so no $\neq 0$ here

is a $\sqrt{\quad}$, so inside of $\sqrt{\quad}$
could be negative

if $2-t$ is negative, then

$$2-t < 0$$

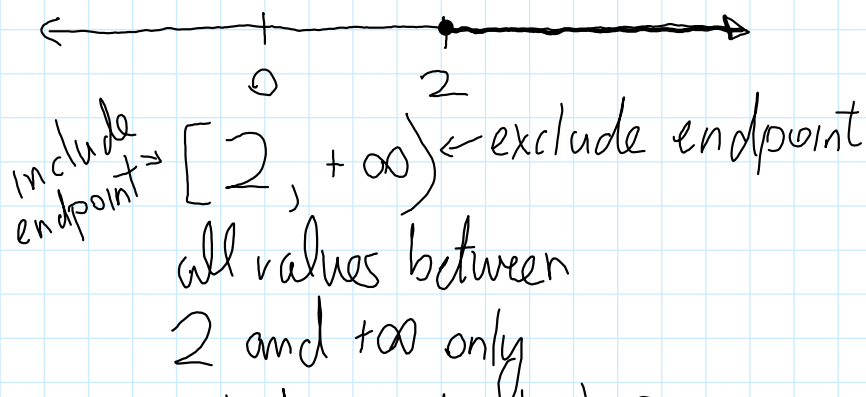
$$2 < t$$

$$t > 2$$

these inputs are bad b/c they
force a $\sqrt{-\#}$

good inputs are everything else
 $t \geq 2$

interval notation



including endpoint at 2

Domain of $g(t)$ is $t \geq 2$

$[2, +\infty)$

interval notation

same notation

$$\circ h(x) = \frac{x}{x^2 + 4}$$

Domain of $h(x)$

could have zero in denom of $h(x)$

no $\sqrt{\quad}$ s in $h(x)$

(don't think ahead just look at the function)

so only bad inputs are the following

denom = 0 \rightarrow cannot happen

$x^2 + 4 = 0$ \rightarrow cannot happen

$x^2 = -4$ \rightarrow cannot happen

$x = \pm\sqrt{-4} \rightarrow$ can't happen

cannot take $\sqrt{-\#}$

it cannot happen that denom = 0

it's always true that denom $\neq 0$

so there cannot be any bad x -values
every x -value is good

Domain of $h(x)$ is all x -values
 $(-\infty, +\infty)$

all values b/w
 $-\infty$ & $+\infty$

excluding both endpoints

Interval notation summary

This is a list of equivalences
between interval notation & number line
graphs

<u>Int Notat</u>	<u>#line</u>	<u>meaning</u>	<u>used with</u>
$(\)$	\circ (open dot)	exclude endpoint	$x < \#$ $x > \#$ $x \neq \#$
$[\]$	\bullet (closed dot)	include endpoint	$x \leq \#$ $x \geq \#$
\cup	$—$	join together intervals	$—$

Domain & Range Graphically

Domain is list of good inputs/x-values

Range is list of outputs/y-values

To read domain from graph of function
smash graph onto x-axis
the part of the x-axis covered by
graph is the domain of function

To read range from graph of function
smash graph onto y-axis
the part of the y-axis covered by

graph is the range of the function^U

[≥ 2 examples]