

Automatic construction and description of nonparametric models

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This analysis was automatically generated

The raw data and full model posterior with extrapolations are shown in figure 1.

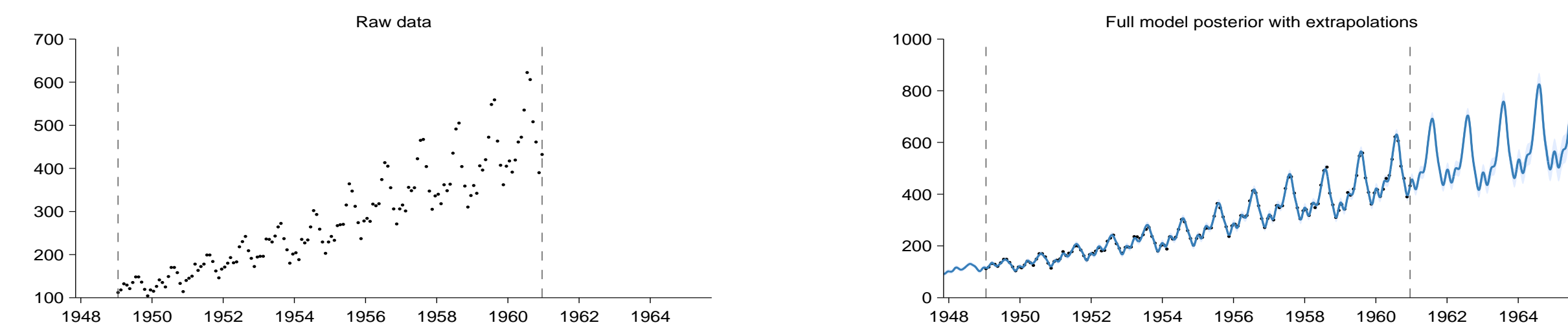


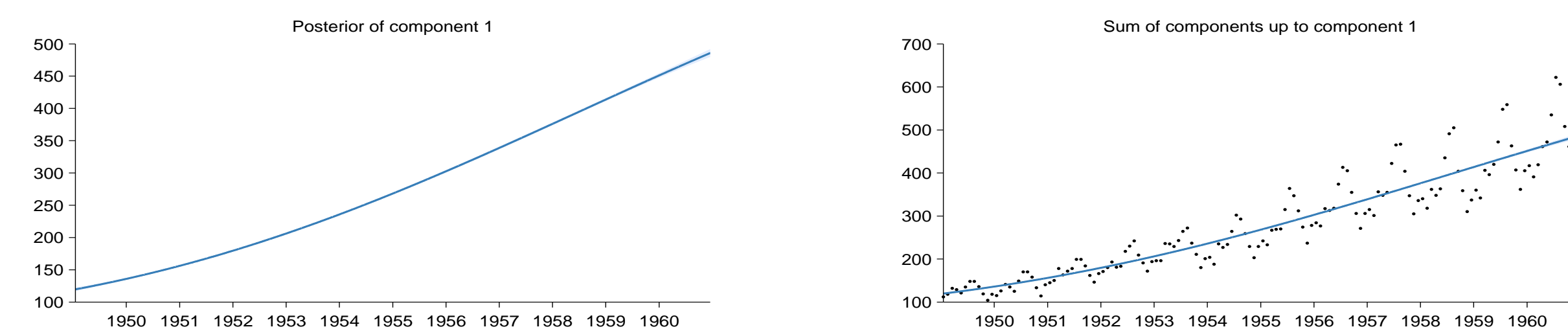
Figure 1: Raw data (left) and model posterior with extrapolation (right)

The structure search algorithm has identified four additive components in the data:

- A very smooth monotonically increasing function.
- An approximately periodic function with a period of 1.0 years and with approximately linearly increasing amplitude.
- An exactly periodic function with a period of 4.3 years but with linearly increasing amplitude.
- Uncorrelated noise with linearly increasing standard deviation.

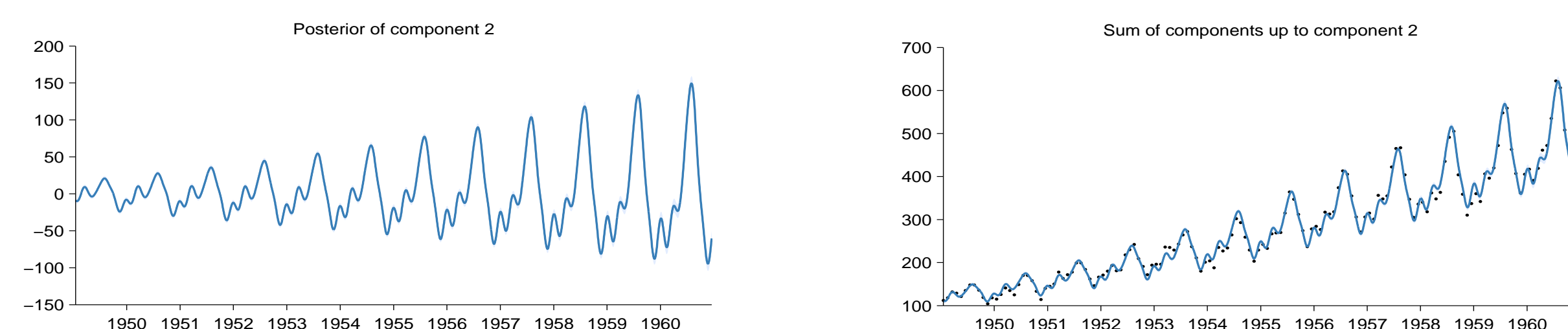
2.1 Component 1

This component is a very smooth and monotonically increasing function.



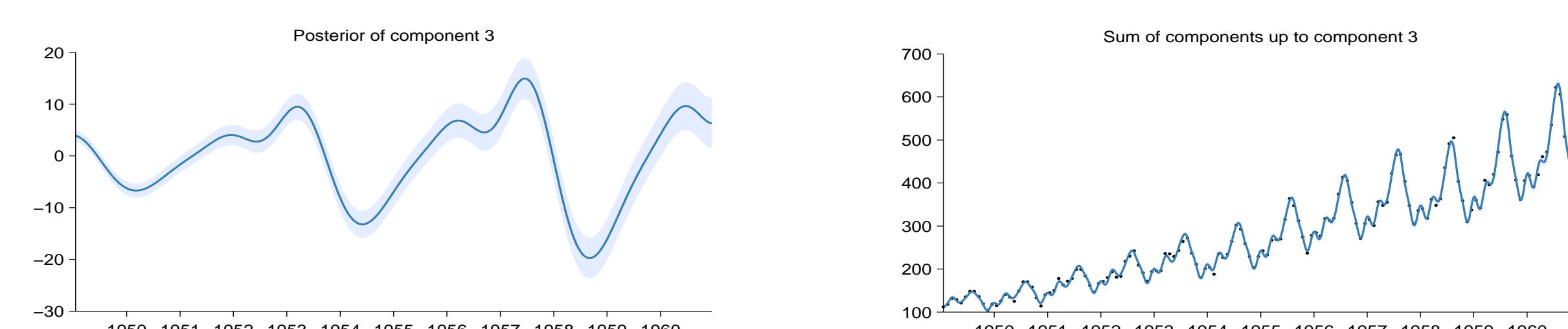
2.2 Component 2

This component is approximately periodic with a period of 1.0 years and varying amplitude. Across periods the shape of this function varies very smoothly. The amplitude of the function increases approximately linearly. The shape of this function within each period has a typical lengthscale of 6.0 weeks.



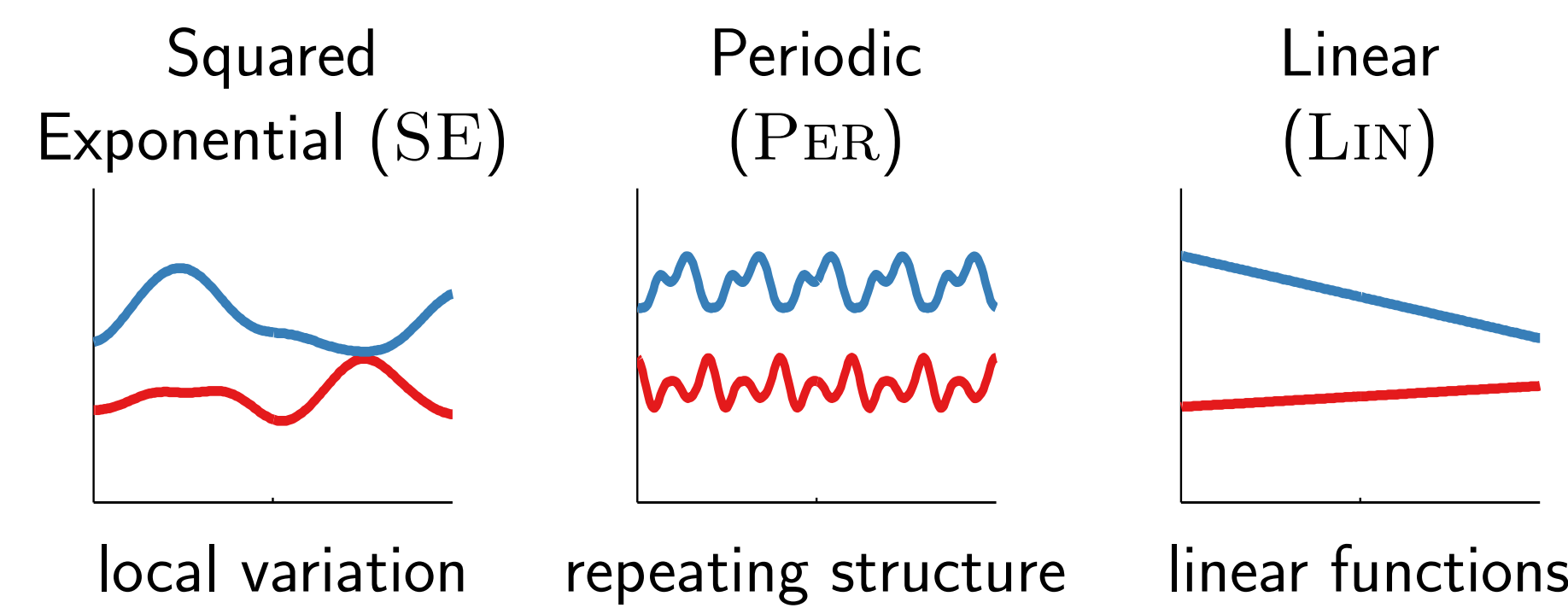
2.3 Component 3

This component is exactly periodic with a period of 4.3 years but with varying amplitude. The amplitude of the function increases linearly. The shape of this function within each period has a typical lengthscale of 7.4 months.

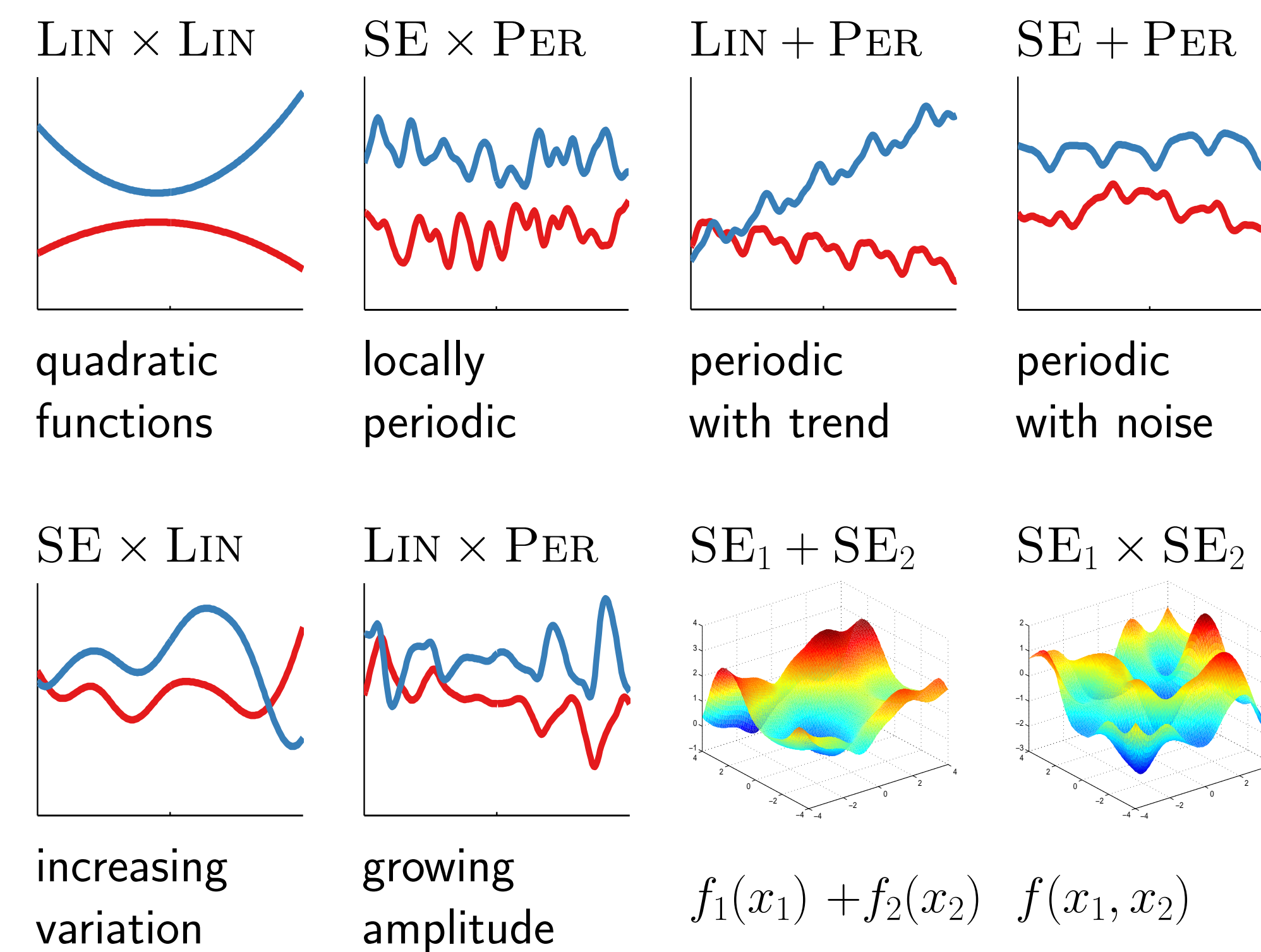


Gaussian processes model structure through kernels

- For Gaussian process models, the prior — and hence, the pattern of generalisation — is determined by a kernel function. Common examples include:

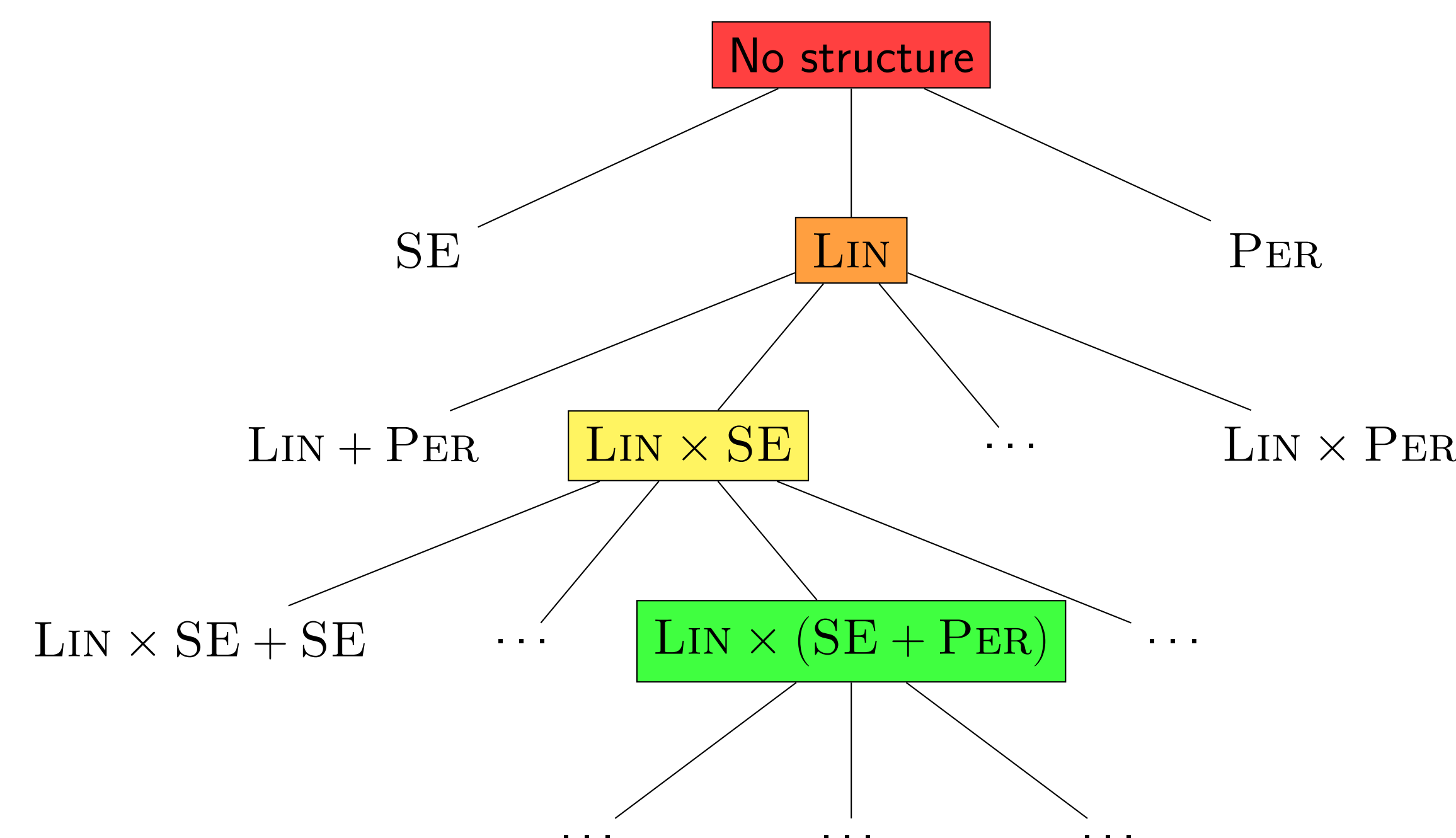


- Composite kernels can express many types of structure



- Building composite kernels has often required much human ingenuity

We build models via a greedy search



Automatically describing model properties

How to automatically describe arbitrarily complex kernels

1. Break each kernel into a sum of products.
2. For each product, look up the properties of each kernel in that product.
3. Combine the properties into one sentence.
4. Plot contribution of this component to the model.

Kernels can be distributed into a sum of products

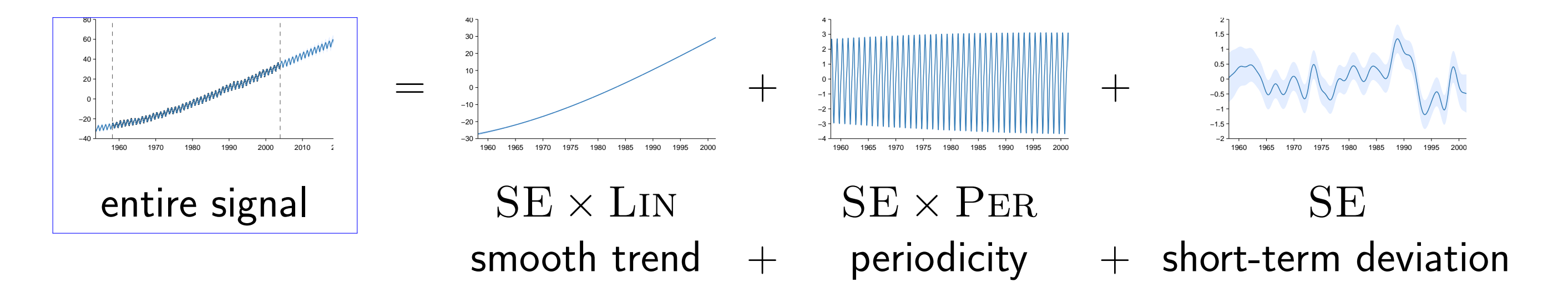
For example:

$$SE \times (LIN + PER + SE)$$

becomes

$$(SE \times LIN) + (SE \times PER) + (SE).$$

Sums of kernels correspond to sums of functions



If $f_1(x) \sim GP(0, k_1)$ and $f_2(x) \sim GP(0, k_2)$ then $f_1(x) + f_2(x) \sim GP(0, k_1 + k_2)$. Therefore, a sum of kernels can be described as a sum of independent functions.

Each kernel in a product roughly corresponds to an adjective

Kernel	How it modifies the prior
SE	functions change smoothly
PER	functions repeat
LIN	amplitude increases linearly

On its own, each kernel simply modifies the constant function $f(x) = c$.

Example short descriptions

Product of Kernels	Description
PER	An exactly periodic function
PER x SE	An approximately periodic function
PER x SE x LIN	An approximately periodic function with linearly varying amplitude
LIN	A linear function
LIN x LIN	A quadratic function
PER x LIN x LIN	An exactly periodic function with quadratically varying amplitude

Code available at github.com/jamesrobertlloyd/gpss-research