

Automatic construction and description of nonparametric models

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This analysis was automatically generated

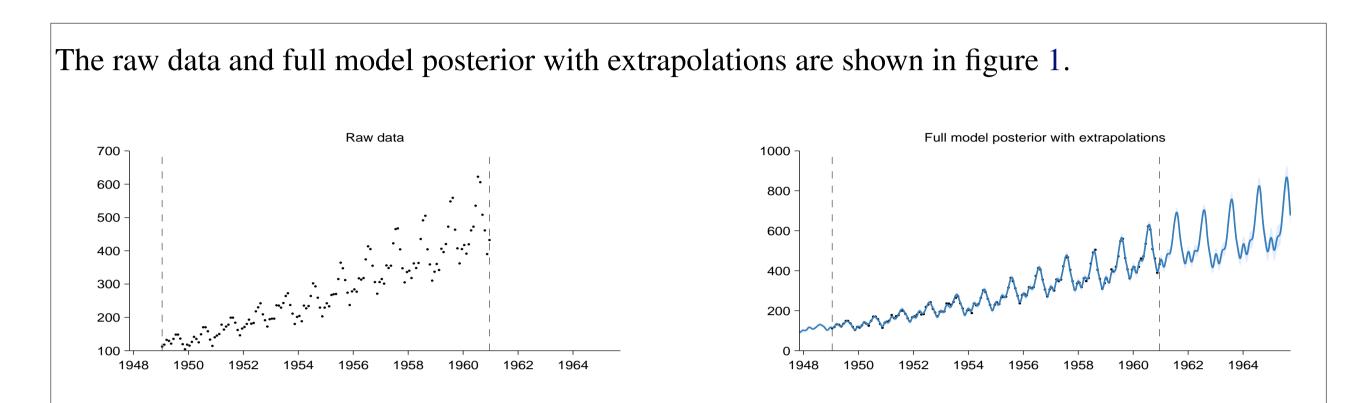


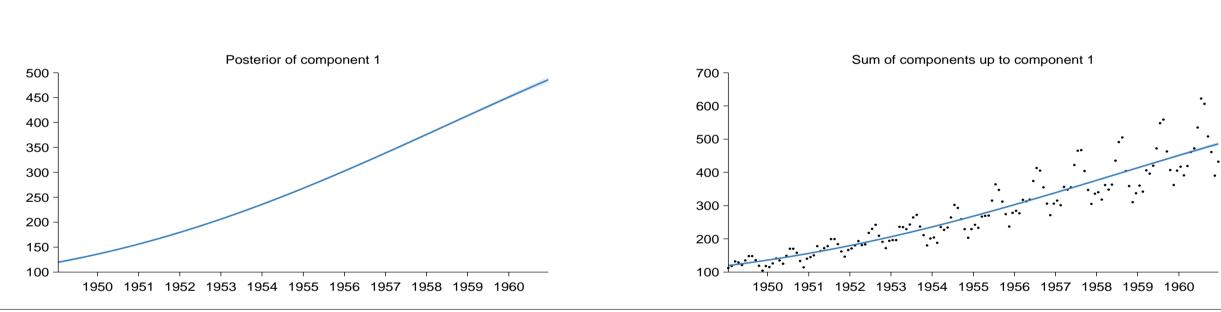
Figure 1: Raw data (left) and model posterior with extrapolation (right)

The structure search algorithm has identified four additive components in the data:

- A very smooth monotonically increasing function.
- An approximately periodic function with a period of 1.0 years and with approximately linearly increasing amplitude.
- An exactly periodic function with a period of 4.3 years but with linearly increasing amplitude.
- Uncorrelated noise with linearly increasing standard deviation.

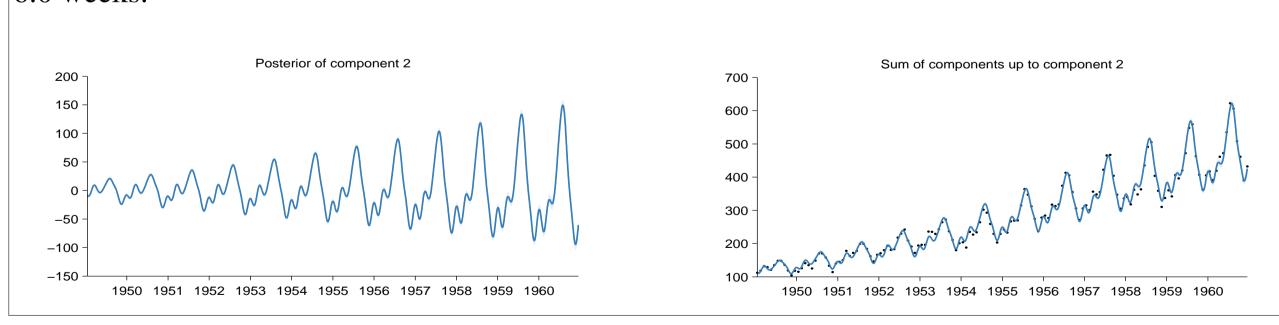
2.1 Component 1

This component is a very smooth and monotonically increasing function.



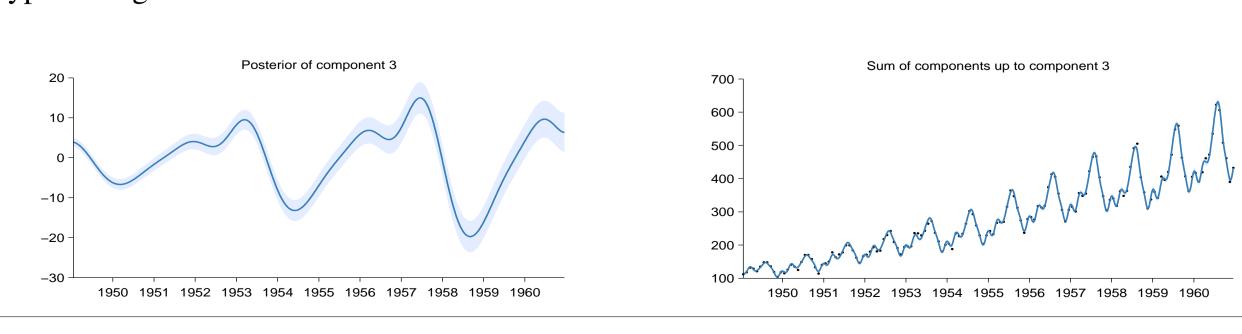
2.2 Component 2

This component is approximately periodic with a period of 1.0 years and varying amplitude. Across periods the shape of this function varies very smoothly. The amplitude of the function increases approximately linearly. The shape of this function within each period has a typical lengthscale of 6.0 weeks.



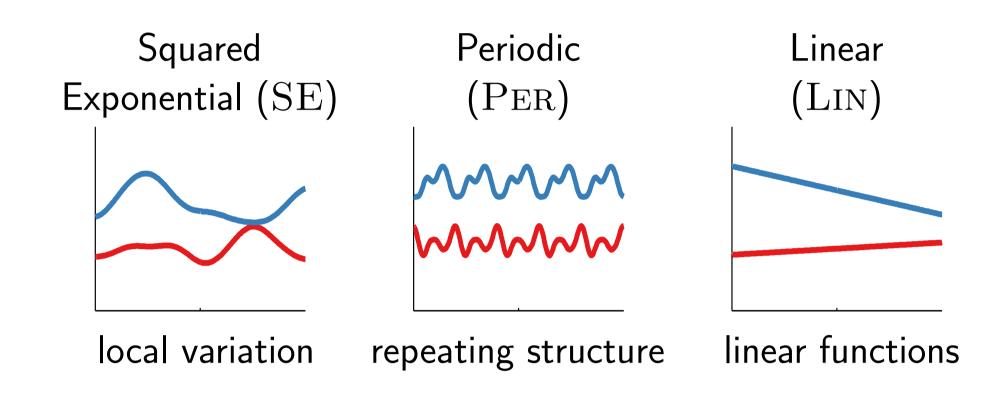
2.3 Component 3

This component is exactly periodic with a period of 4.3 years but with varying amplitude. The amplitude of the function increases linearly. The shape of this function within each period has a typical lengthscale of 7.4 months.

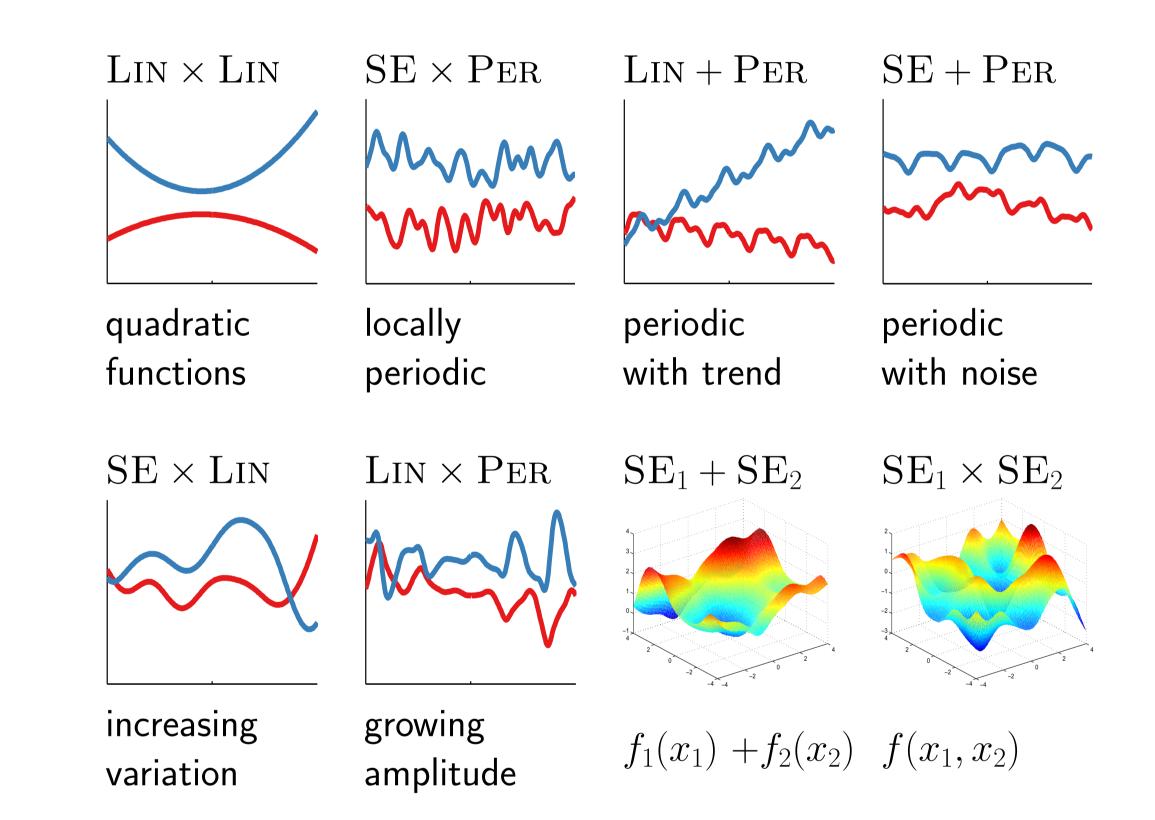


Gaussian processes model structure through kernels

For Gaussian process models, the prior — and hence, the pattern of generalisation
 — is determined by a kernel function. Common examples include:

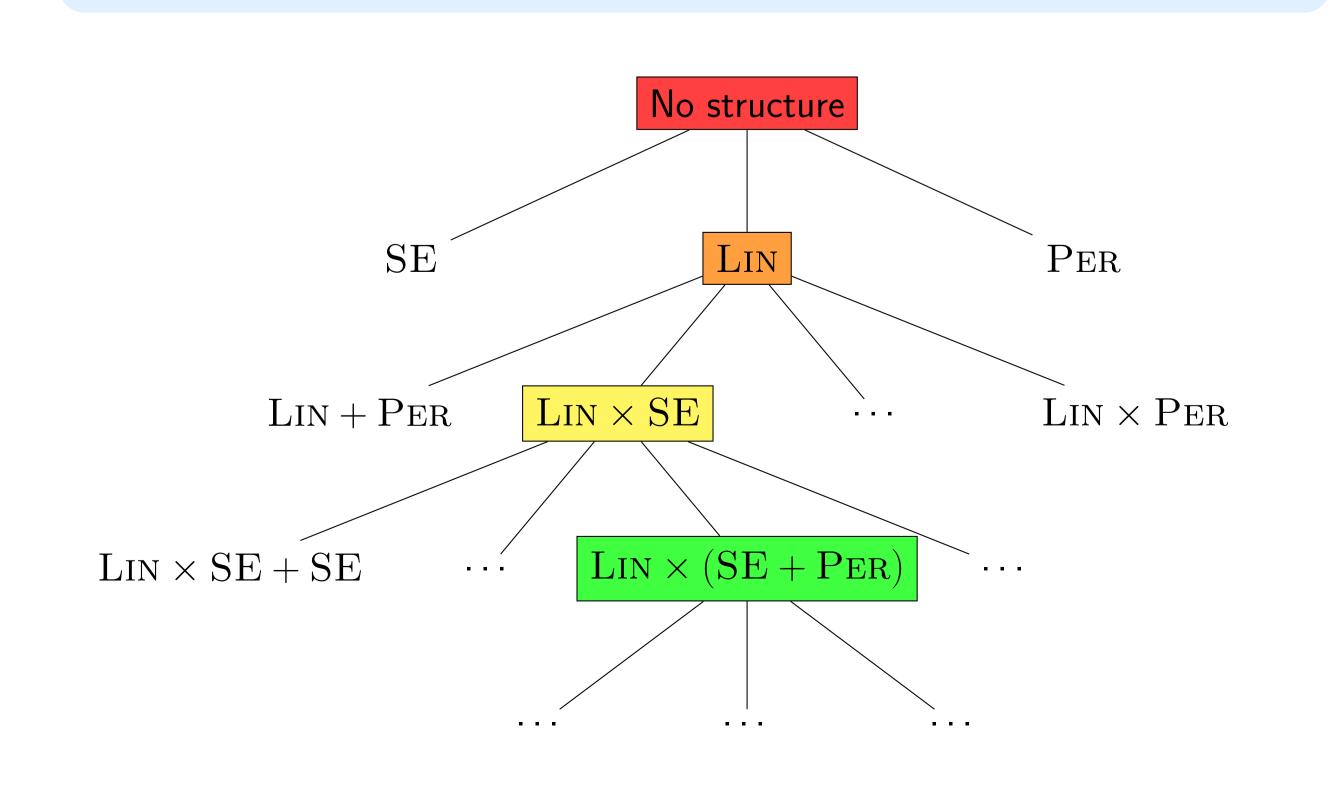


Composite kernels can express many types of structure



• Building composite kernels has often required much human ingenuity

We build models via a greedy search



Automatically describing model properties

It is hard to write a lookup table to handle every kernel that the open-ended search might produce. How to automate this?

Kernels can be distributed into a sum of products

For example:

 $SE \times (LIN + LIN \times (PER + SE))$

becomes

 $(SE \times LIN) + (SE \times LIN \times PER) + (SE \times LIN).$

Sums of kernels correspond to sums of functions

If
$$f_1(x) \sim \text{GP}(0, k_1)$$
 and $f_2(x) \sim \text{GP}(0, k_2)$ then $f_1(x) + f_2(x) \sim \text{GP}(0, k_1 + k_2)$.

Each kernel in a product corresponds to an adjective

Kernel How it modifies the prior

SE functions change smoothly

PER | functions repeat

LIN amplitude increases linearly

Product of Kernels Description

 ${
m Per}$ An exactly periodic function ${
m Per} imes {
m SE}$ An approximately periodic function

 $ext{Per} imes ext{SE} imes ext{Lin}$ An approximately periodic function with linearly varying amplitude

 L_{IN} A linear function $L_{IN} \times L_{IN}$ A quadratic function

 ${
m Per} imes {
m Lin} imes {
m Lin}$ An exactly periodic function with quadratically varying amplitude

Code available at github.com/jamesrobertlloyd/gpss-research