

## Automatic construction and description of nonparametric models

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### This analysis was automatically generated

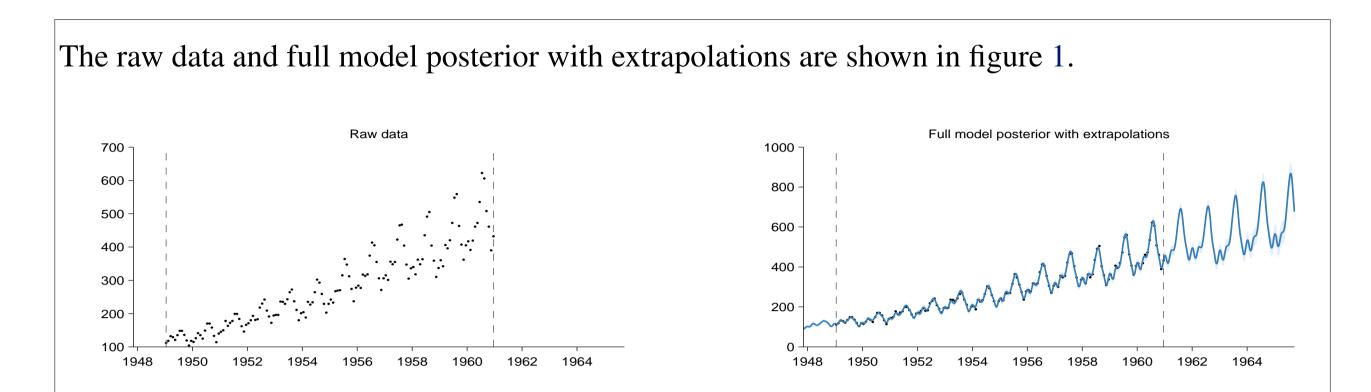


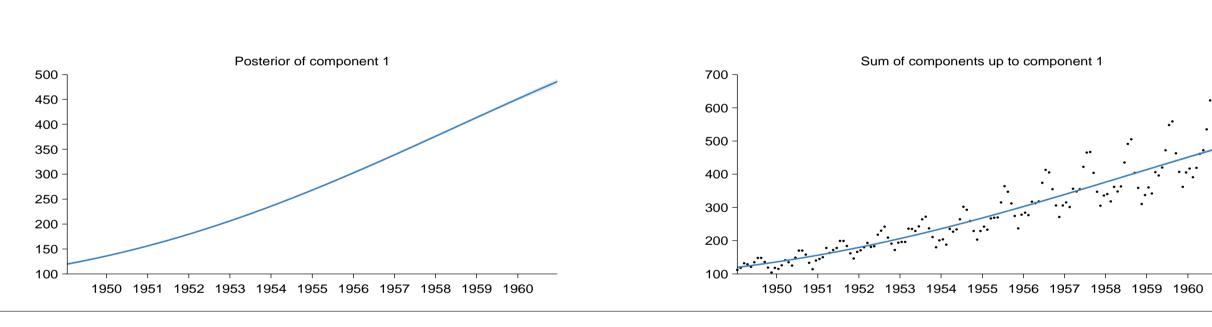
Figure 1: Raw data (left) and model posterior with extrapolation (right)

The structure search algorithm has identified four additive components in the data:

- A very smooth monotonically increasing function.
- An approximately periodic function with a period of 1.0 years and with approximately linearly increasing amplitude.
- An exactly periodic function with a period of 4.3 years but with linearly increasing amplitude.
- Uncorrelated noise with linearly increasing standard deviation.

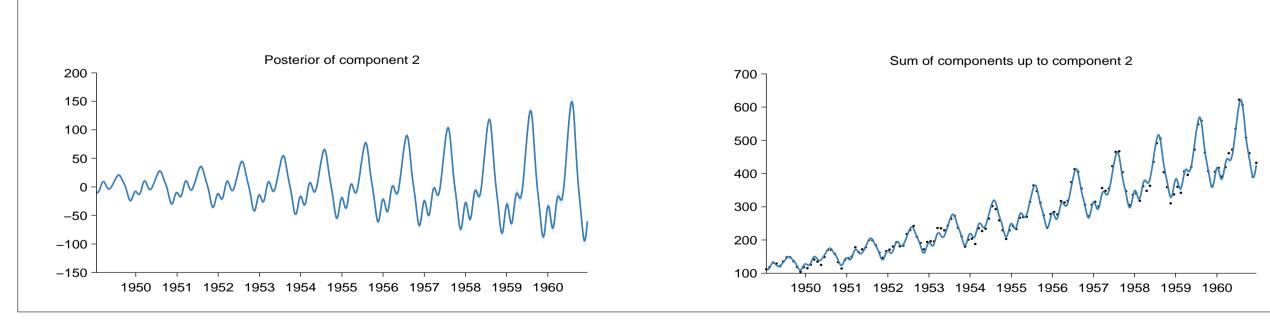
#### 2.1 Component 1

This component is a very smooth and monotonically increasing function.



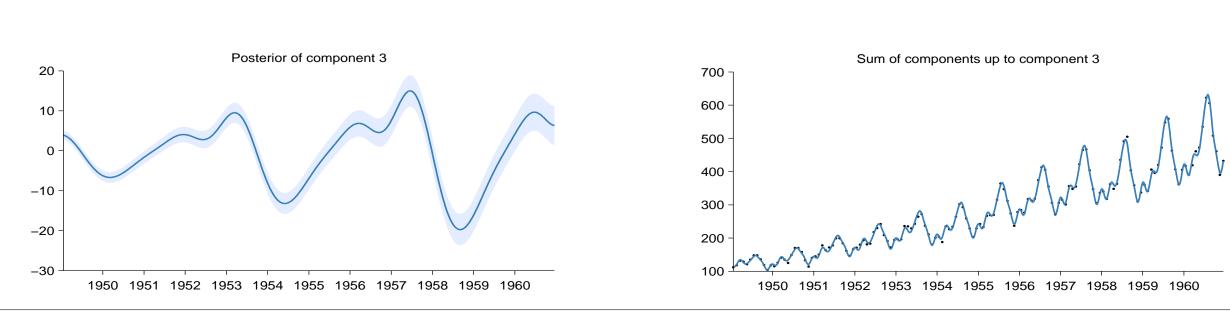
#### 2.2 Component 2

This component is approximately periodic with a period of 1.0 years and varying amplitude. Across periods the shape of this function varies very smoothly. The amplitude of the function increases approximately linearly. The shape of this function within each period has a typical lengthscale of 6.0 weeks.



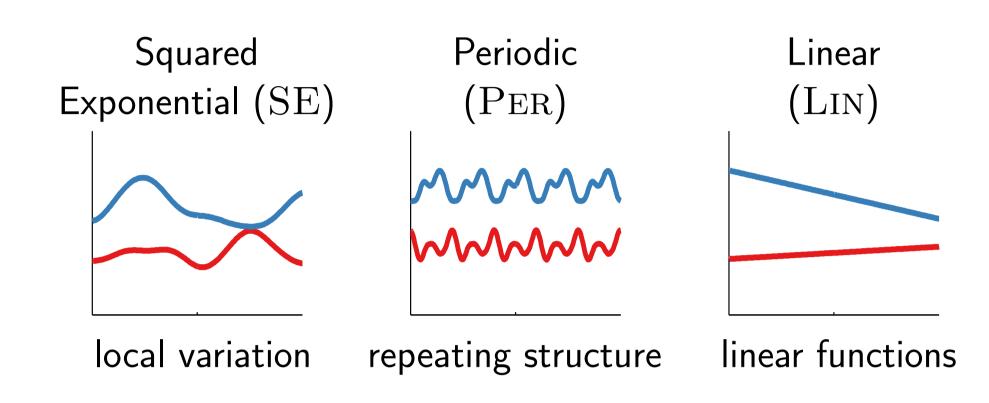
#### 2.3 Component 3

This component is exactly periodic with a period of 4.3 years but with varying amplitude. The amplitude of the function increases linearly. The shape of this function within each period has a typical lengthscale of 7.4 months.

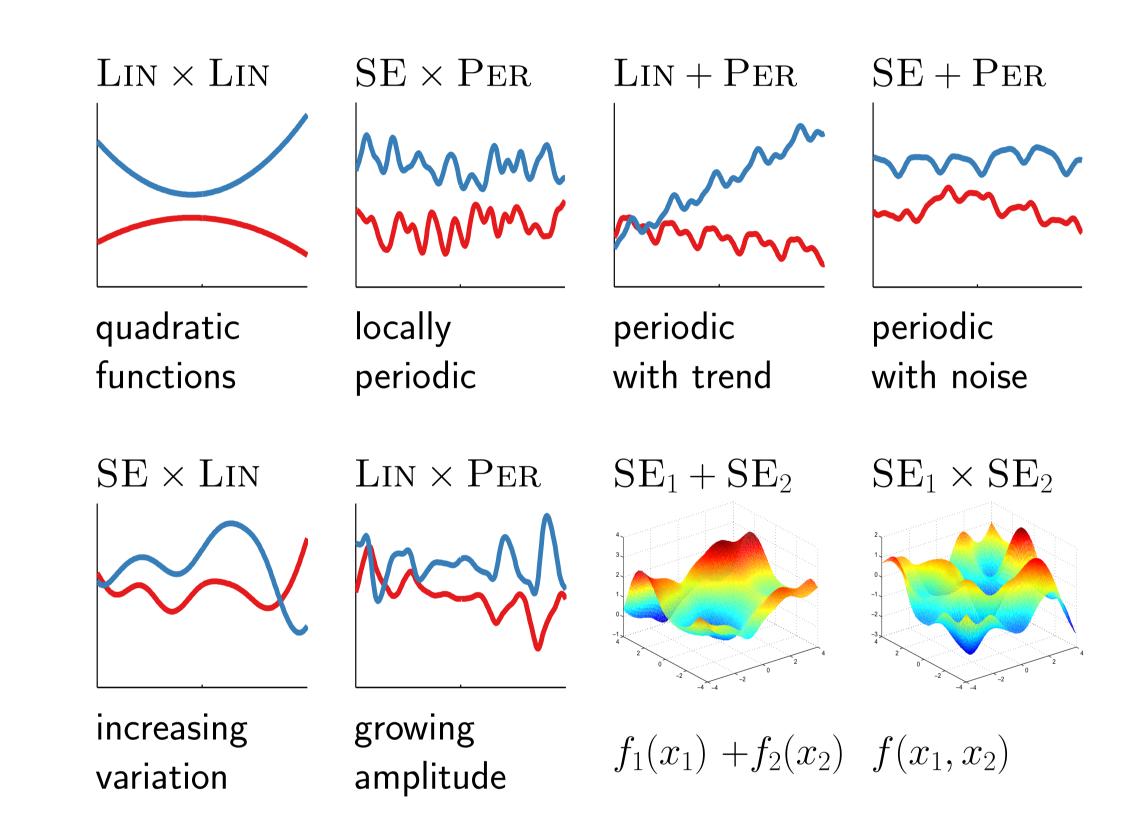


# Gaussian processes model structure through kernels

• For Gaussian process models, the prior — and hence, the pattern of generalisation — is determined by a kernel function. Common examples include:

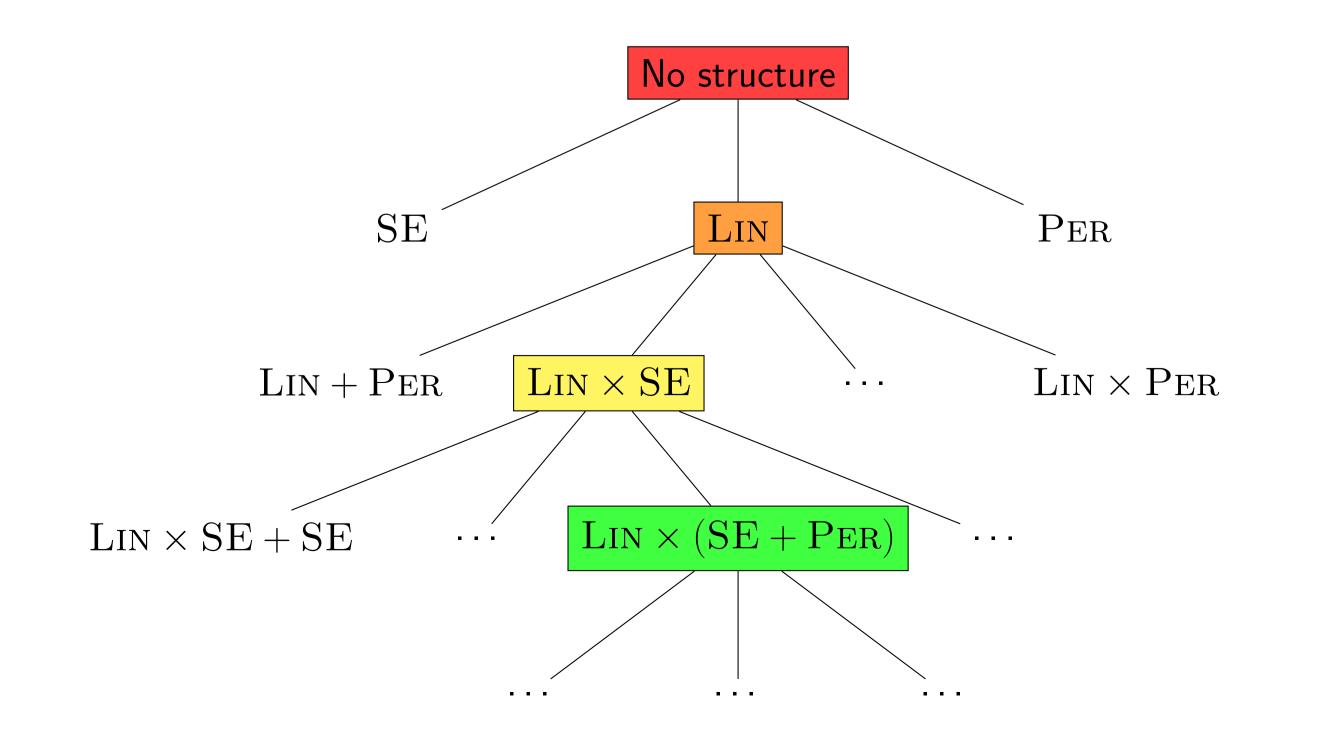


• Composite kernels can express many types of structure



Building composite kernels has often required much human ingenuity

### We build models via a greedy search



### Automatically describing model properties

- How to automatically describe complex kernels?
- 1. Break each kernel into a sum of products.
- 2. For each product, look up the properties of each kernel in that product.
- 3. Combine the properties into one sentence.
- 4. Plot contribution of this compoenent to the model.

### Kernels can be distributed into a sum of products

For example:

$$SE \times (LIN + LIN \times (PER + SE))$$

becomes

$$(SE \times LIN) + (SE \times LIN \times PER) + (SE \times LIN).$$

[Insert a figure here showing an additive decomposition]

### Sums of kernels correspond to sums of functions

If  $f_1(x) \sim \text{GP}(0, k_1)$  and  $f_2(x) \sim \text{GP}(0, k_2)$  then  $f_1(x) + f_2(x) \sim \text{GP}(0, k_1 + k_2)$ . Therefore, a sum of kernels can be described as a sum of independent functions.

### Each kernel in a product corresponds to an adjective

### Kernel How it modifies the prior

SE functions change smoothly

PER functions repeat

LIN amplitude increases linearly

On its own, each kernel simply modifyies the constant function f(x) = c.

### **Example short descriptions**

### Product of Kernels Description

$\operatorname{PER}$	An exactly periodic function
$Per \times SE$	An approximately periodic function
$PER \times SE \times LIN$	An approximately periodic function with linearly varying amplitude
Lin	A linear function
$Lin \times Lin$	A quadratic function

 ${
m Per} imes {
m Lin} imes {
m Lin}$  An exactly periodic function with quadratically varying amplitude

Code available at github.com/jamesrobertlloyd/gpss-research