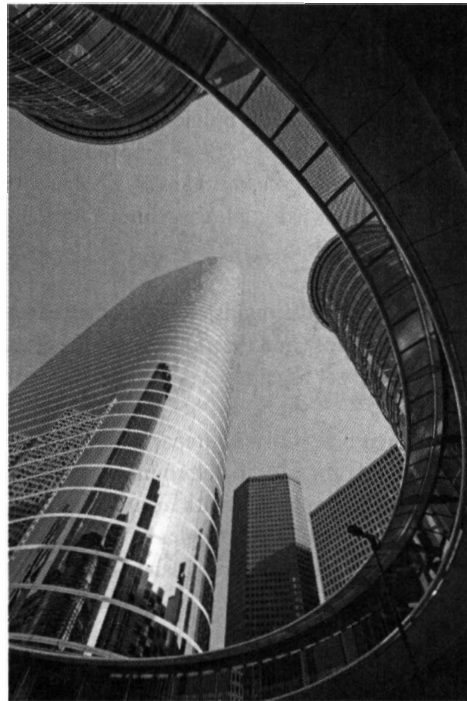


# Data Abstraction & Problem Solving with C++

**Walls And Mirrors**

**Seventh Edition**



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