# INTRO TO DATA SCIENCE LECTURE 11: ENSEMBLE TECHNIQUES

## **LAST TIME:**

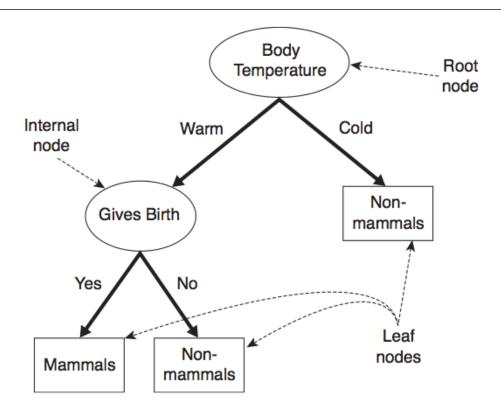
- DECISION TREES
- DECISION TREES IN SCIKIT-LEARN

## **QUESTIONS?**

#### **AGENDA**

- I. ENSEMBLE TECHNIQUES
- II. PROBLEMS IN CLASSIFICATION
- III. BAGGING
- IV. BOOSTING
- V. RANDOM FORESTS

#### **EXAMPLE — DECISION TREE**



#### Figure 4.4. A decision tree for the mammal classification problem.

source: http://www-users.cs.umn.edu/~kumar/dmbook/ch4.pdf

#### NOTE

Internal nodes represent test conditions which partition the records at that node.

# REVIEW: RANDOM FORESTS

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- 3) Predict based on majority vote of N trees

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- A: Methods of improving classification accuracy by aggregating predictions over several base classifiers.

Ensembles are often much more accurate than the base classifiers that compose them.

# There are two general ensemble techniques:

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**Averaging:** build several models independently and then to average their predictions.

**Examples**: Random Forests and Bagging.

There are two general ensemble techniques:

**Boosting**: models are built sequentially to combine several weak models to produce a powerful ensemble.

**Examples**: Ada Boost and Gradient Tree Boosting

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1) the base classifiers must be **accurate**: they must outperform random guessing

2) the base classifiers must be **diverse**: their misclassifications must occur on different training examples

# II. PROBLEMS IN CLASSIFICATION

#### **PROBLEMS IN CLASSIFICATION**

In any supervised learning task, our goal is to make predictions of the true classification function f by learning the classifier h.

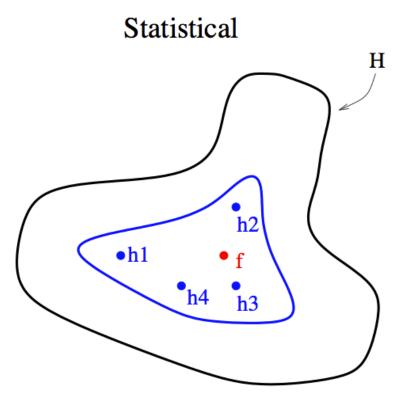
In any supervised learning task, our goal is to make predictions of the true classification function f by learning the classifier h.

There are three main problems that can prevent this:

- statistical problem
- computational problem
- representational problem

If the amount of training data available is small, the base classifier will have difficulty converging to h.

An ensemble classifier can mitigate this problem by "averaging out" base classifier predictions to improve convergence.



#### NOTE

The true function f is best approximated as an average of the base classifiers.

#### THE COMPUTATIONAL PROBLEM

Even with sufficient training data, it may still be computationally difficult to find the best classifier h.

For example, if our base classifier is a decision tree, an exhaustive search of the hypothesis space of all possible classifiers is extremely complex (NP-complete).

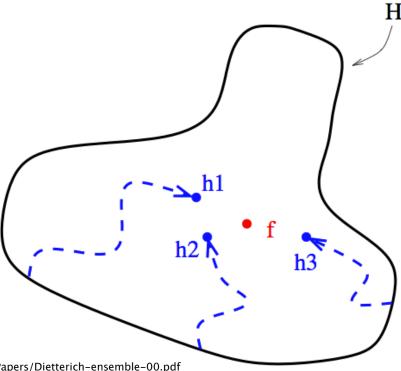
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An ensemble composed of several BC's with different starting points can provide a better approximation to f than any individual BC.

# Computational



#### NOTE

The true function f is often best approximated by using several starting points to explore the hypothesis space.

source: http://www.cs.iastate.edu/~jtian/cs573/Papers/Dietterich-ensemble-00.pdf

#### THE REPRESENTATIONAL PROBLEM

Sometimes f cannot be expressed in terms of our hypothesis at all.

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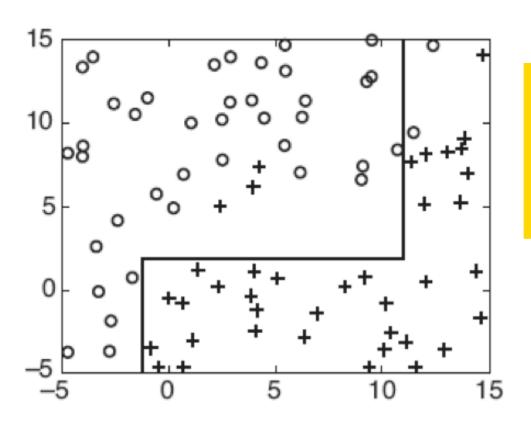
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A decision tree works by forming a rectilinear partition of the feature space.



#### NOTE

What is a rectilinear decision boundary?

One whose segments are orthogonal to the x & y axes.

#### THE REPRESENTATIONAL PROBLEM

But what if f is a diagonal line?

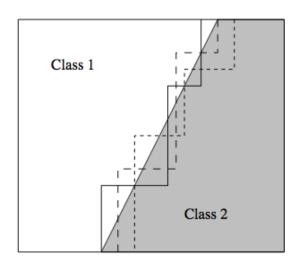
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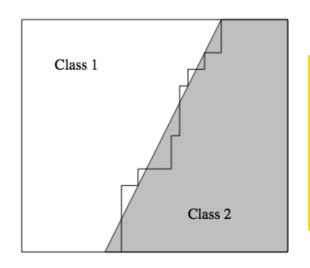
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Then it cannot be represented by finitely many rectilinear segments, and therefore the true decision boundary cannot be obtained by a decision tree classifier.

However, it may be still be possible to approximate f or even to expand the space of representable functions using ensemble methods.



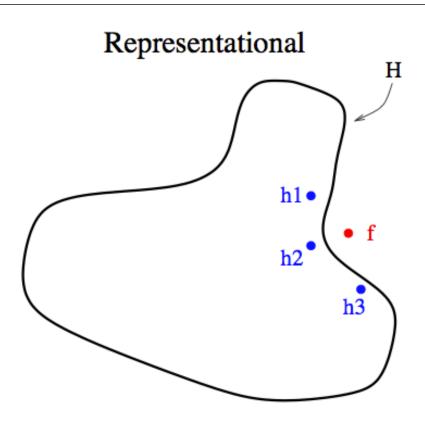


#### NOTE

An ensemble of decision trees can approximate a diagonal decision boundary.

**Fig. 4.** The left figure shows the true diagonal decision boundary and three staircase approximations to it (of the kind that are created by decision tree algorithms). The right figure shows the voted decision boundary, which is a much better approximation to the diagonal boundary.

### THE REPRESENTATIONAL PROBLEM — EXPANDING THE HYPOTHESIS SPACE



#### NOTE

Ensemble classifiers can be effective even if the true decision boundary lies outside the hypothesis space.

# **CREATING AN ENSEMBLE PREDICTION**

Q: How do you create an ensemble classifier using averaging methods?

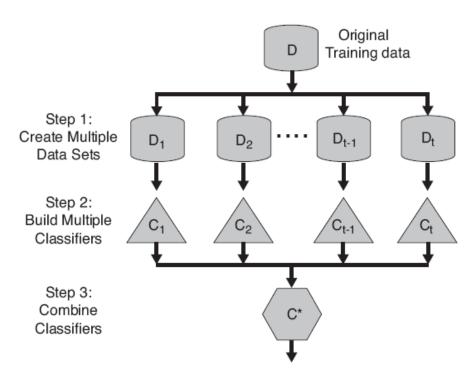


Figure 5.31. A logical view of the ensemble learning method.

## **CREATING AN ENSEMBLE PREDICTION**

Q: How do you generate several base classifiers?

- Q: How do you generate several base classifiers?
- A: There are several ways to do this:

- manipulating the training set
- manipulating the output labels
- manipulating the learning algorithm itself

We will talk about a few examples of each of these.

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# III. BAGGING

# **BAGGING**

**Bagging** (bootstrap aggregating) is a method that involves manipulating the training set by resampling.

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We learn k base classifiers on k different samples of training data.

These samples are independently created by resampling the training data using uniform weights (eg, a uniform sampling distribution).

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Each training sample is the same size as the original training

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#### NOTE

- Resampling means
- that some training
  - records may appear in a sample more than once, or even not at all.

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We learn k base classifiers on k different samples of training data.

These samples are independently created by resampling the training data using uniform weights (eg, a uniform sampling distribution).

The final prediction is made by taking a majority vote across bc's.

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Bagging reduces the variance in our generalization error by aggregating multiple base classifiers together (provided they satisfy our earlier requirements).

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If the base classifier is stable (to minor changes in training data), then the ensemble error is primarily due to bc bias, and bagging may not be effective.

Since each sample of training data is equally likely, bagging is not very susceptible to overfitting with noisy data.

## INTRO TO DATA SCIENCE

# IV. BOOSTING

Boosting is an iterative procedure that adaptively changes the sampling distribution of training records at each iteration.

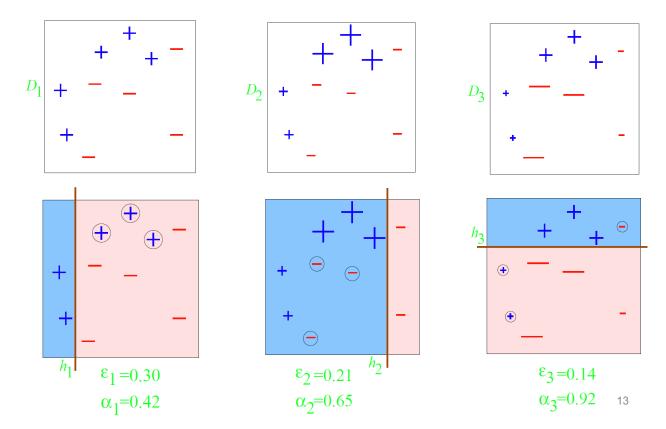
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The final prediction is constructed by a weighted vote (where the weights for a bc depends on its training error).



http://www.cs.cmu.edu/~aarti/Class/10701/slides/Lecture10.pdf

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- 5) *Repeat*

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- 5) Repeat
- 6) Predict based on majority vote (or vote based on accuracy inverse error)

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These omitted records will likely be misclassified, and given greater weight in subsequent iterations once the sampling distribution is updated.

So even if a record is left out at one stage, it will be emphasized later.

# V. RANDOM FORESTS

RANDOM FORESTS 66

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# EX: ENSEMBLE METHODS IN SCIKIT-LEARN