

# Higher-Order Template Metaprogramming

# Higher-Order Template Metaprogramming (in C++23)

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Don't do this... yet.

	Logic		
0th order	$P$		
1st order	$P(x)$		
2nd order	$\exists P P(b)$		

	Logic	FP	
0th order	$P$	$x$	
1st order	$P(x)$	$\lambda x. x + 1$	
2nd order	$\exists P P(b)$	$\lambda f x. f(f x)$	

	Logic	FP	TMP
0th order	$P$	$x$	<code>&lt;int I&gt;</code>
1st order	$P(x)$	$\lambda x. x + 1$	<code>&lt;class C&gt;</code>
2nd order	$\exists P P(b)$	$\lambda f x. f(f\ x)$	<code>?</code>

	Logic	FP	TMP
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```
enum class E { a, b, c, };  
std::is_enum_v auto e = E::a;  
auto f(std::is_enum_v auto e) {}  
std::is_enum_v auto f() { return E::a; }  
template<class T>  
concept A = requires(T t, T const tc) {  
    { t.code() } -> std::is_enum_v;  
};
```

*“Naming things is hard.”*

```
enum class E { a, b, c, };  
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static\_assert

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    { t.code() } -> std::is_enum_v;  
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```

static\_assert  
~~BANNED~~

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concept A = requires(T t, T const tc) {  
    { t.code() } -> std::is_enum_v;  
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static\_assert  
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template

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enum class E { a, b, c, };  
std::is_enum_v auto e = E::a;  
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template<class T>  
concept A = requires(T t, T const tc) {  
    { t.code() } -> std::is_enum_v;  
};
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static\_assert

template



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enum class E { a, b, c, };  
std::is_enum_v auto e = E::a;  
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template<class T>  
concept A = requires(T t, T const tc) {  
    { t.code() } -> std::is_enum_v;  
};
```

static\_assert  
~~BANNED~~

template  
~~BANNED~~

decltype

```
enum class E { a, b, c, };  
std::is_enum_v auto e = E::a;  
auto f(std::is_enum_v auto e) {}  
std::is_enum_v auto f() { return E::a; }  
template<class T>  
concept A = requires(T t, T const tc) {  
    { t.code() } -> std::is_enum_v;  
};
```

static\_assert

template

decltype

```
enum class E { a, b, c, };
```

```
// ...
```

```
template<class T>
```

```
concept A = requires(T t, T const tc) {
```

```
    { t.code() } -> std::is_enum;
```

```
};
```

```
template<class T, template<class> class TT>  
concept Trait = TT<T>::value;
```

```
template<class T>  
concept A = requires(T t, T const tc) {  
    { t.code() } -> Trait<std::is_enum>;  
};
```

```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
};
```

```
struct S {
    E code();
};
A auto s = S();
```

```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> ???;
};
```

```
struct S {
    E code();
    void run();
};
A auto s = S();
```

```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
};
```

```
struct S {
    E code();
    void run();
};
A auto s = S();
```

```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> std::same_as<void>;
};
```

```
struct S {
    E code();
    void run();
};
A auto s = S();
```



```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
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struct S {
    E code();
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struct S {
    E code();
    void const run();
};
A auto s = S();
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```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> ???;
};
```

```
struct S {
    E code();
    void const run();
    std::span<int> ids();
};
A auto s = S();
```

```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> RangeOf<int>;
};
```

```
struct S {
    E code();
    void const run();
    std::span<int> ids();
};
A auto s = S();
```

```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> RangeOf<int>;
};

template<class T, class U>
concept RangeOf = std::ranges::range<T> and
    std::same_as<std::ranges::range_value_t<T>, U>;
```

```
struct S {
    E code();
    void const run();
    std::span<int> ids();
};

A auto s = S();
```

```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> RangeOf<int>;
    { t.ids() } -> RangeOver<std::integral>;
};
```

```
struct S {
    E code();
    void const run();
    std::span<int> ids();
};

A auto s = S();
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```
template<class T>
concept A = requires(T t, T const tc) {
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concept A = requires(T t, T const tc) {
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    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> RangeOf<int>;
    { t.ids() } -> RangeOver<[]<std::integral>{}>;
};
```



```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
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concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> RangeOf<int>;
    { t.ids() } -> RangeOver<[]<std::integral>{}>;
};
```

```
template<class T, auto C>
concept RangeOver = std::ranges::range<T> and requires {
    C.template operator()<std::ranges::range_value_t<T>>();
};
```

```
struct S {
    E code();
    void const run();
    std::span<int> ids();
};

A auto s = S();
```

```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> RangeOf<int>;
    { t.ids() } -> RangeOver<[]<std::integral>{}>;
};
```

```
template<class T, auto C>
concept Satisfies = requires {
    C.template operator()<T>();
};
```

```
template<class T, auto C>
concept RangeOver = std::ranges::range<T> and
    Satisfies<std::ranges::range_value_t<T>, C>;
```

```
struct S {
    E code();
    void const run();
    std::span<int> ids();
};

A auto s = S();
```

```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> RangeOf<int>;
    { t.ids() } -> RangeOver<[]<std::integral>{}>;
    { tc.d() } -> ???;
};
```

```
struct B {};
struct D : B {};
struct S {
    E code();
    void const run();
    std::span<int> ids();
    D d() const;
};
A auto s = S();
```

```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> RangeOf<int>;
    { t.ids() } -> RangeOver<[]<std::integral>{}>;
    { tc.d() } -> std::derived_from<B>;
};
```

```
struct B {};
```

```
struct D : B {};
```

```
struct S {
    E code();
    void const run();
    std::span<int> ids();
    D d() const;
};
```

```
A auto s = S();
```

```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> RangeOf<int>;
    { t.ids() } -> RangeOver<[]<std::integral>{}>;
    { tc.d() } -> std::derived_from<B>;
};
```

```
struct B {};
```

```
struct D : B {};
```

```
struct S {
    E code();
    void const run();
    std::span<int> ids();
    D const& d() const;
};
```

```
A auto s = S();
```

```

template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> RangeOf<int>;
    { t.ids() } -> RangeOver<[]<std::integral>{}>;
    { tc.d() } -> SatisfiesAfter<std::remove_cvref,
        []<std::derived_from<B>>{}>;
};

```

```

template<class T, template<class> class TT, auto C>
concept SatisfiesAfter =
    Satisfies<typename TT<T>::type, C>;

```

```

struct S {
    E code();
    void const run();
    std::span<int> ids();
    D const& d() const;
};
A auto s = S();

```

```
template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> RangeOf<int>;
    { t.ids() } -> RangeOver<[]<std::integral>{}>;
    { tc.d() } -> SatisfiesAfter<std::remove_cvref,
        []<std::derived_from<B>>{}>;
    { tc.d() } -> Satisfies<[]<class U> requires
        std::derived_from<std::remove_cvref_t<U>, B> {}>;
};
```

```
struct S {
    E code();
    void const run();
    std::span<int> ids();
    D const& d() const;
};
A auto s = S();
```



```

template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> RangeOf<int>;
    { t.ids() } -> RangeOver<[]<std::integral>{}>;
    { tc.d() } -> SatisfiesAfter<std::remove_cvref,
        []<std::derived_from<B>>{}>;
    { tc.d() } -> Satisfies<[]<class U> requires
        std::derived_from<std::remove_cvref_t<U>, B> {}>;
    { t.elapsed() } -> ???;
};

```

```

struct S {
    E code();
    void const run();
    std::span<int> ids();
    D const& d() const;
    std::chrono::picoseconds
        elapsed();
};
A auto s = S();

```

```

template<class T>
concept A = requires(T t, T const tc) {
    { t.code() } -> Trait<std::is_enum>;
    { t.run() } -> Trait<std::is_void>;
    { t.ids() } -> RangeOf<int>;
    { t.ids() } -> RangeOver<[]<std::integral>{}>;
    { tc.d() } -> SatisfiesAfter<std::remove_cvref,
        []<std::derived_from<B>>{}>;
    { tc.d() } -> Satisfies<[]<class U> requires
        std::derived_from<std::remove_cvref_t<U>, B> {}>;
    { t.elapsed() } -> Satisfies<[]<class U> requires
        requires(U u) { []<std::integral R, auto D>(
            std::chrono::duration<R, std::ratio<1, D>>){}(
                u);
        } {}>;
};

```

```

struct S {
    E code();
    void const run();
    std::span<int> ids();
    D const& d() const;
    std::chrono::picoseconds
        elapsed();
};
A auto s = S();

```

<div>&lt;source&gt;:33:30: internal compiler error: Segmentation fault</div> <div>33   { t.ids() } -&gt; RangeOver&lt;[]&lt;std::integral&gt;{}&gt;;</div> <div>  ^~~~~~</div> <div>0x255cc4e internal_error(char const*, ...)</div> <div>???:0</div> <div>0xceb951 template_parms_to_args(tree_node*)</div> <div>???:0</div> <div>0xd29d62 tsubst_lambda_expr(tree_node*, tree_node*, int, tree_node*)</div> <div>???:0</div> <div>0xd0e051 tsubst_template_arg(tree_node*, tree_node*, int, tree_node*)</div> <div>???:0</div> <div>0xb71b22 constraints_satisfied_p(tree_node*, tree_node*)</div> <div>???:0</div> <div>0xcf8c9b do_auto_deduction(tree_node*, tree_node*, tree_node*, int, auto_deduction_context, tree_node*, int, tree_node*)</div> <div>???:0</div> <div>0xb701d6 tsubst_requires_expr(tree_node*, tree_node*, int, tree_node*)</div> <div>???:0</div> <div>0xb71b22 constraints_satisfied_p(tree_node*, tree_node*)</div> <div>???:0</div> <div>0xcf8c9b do_auto_deduction(tree_node*, tree_node*, tree_node*, int, auto_deduction_context, tree_node*, int, tree_node*)</div> <div>???:0</div> <div>0xbd4e9d cp_finish_decl(tree_node*, tree_node*, bool, tree_node*, int, cp_decomp*)</div> <div>???:0</div> <div>0xcdc754 c_parse_file()</div> <div>???:0</div> <div>0xe1eca9 c_common_parse_file()</div> <div>???:0</div> <div>Please submit a full bug report, with preprocessed source (by using -freport-bug).</div> <div>Please include the complete backtrace with any bug report.</div> <div>See &lt;https://gcc.gnu.org/bugs/&gt; for instructions.</div> <div>Compiler returned: 1</div>		
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<pre>&lt;source&gt;:33:30: internal compiler error: Segmentation fault  33        { t.ids() } -&gt; RangeOver&lt;[]&lt;std::integral&gt;{}&gt;;                                     ^~~~~~ 0x255cc4e internal_error(char const*, ...)     ???:0 0xceb951 template_parms_to_args(tree_node*)     ???:0 0xd29d62 tsubst_lambda_expr(tree_node*, tree_node*, int, tree_node*)     ???:0 0xd0e051 tsubst_template_arg(tree_node*, tree_node*, int, tree_node*)     ???:0 0xb71b22 constraints_satisfied_p(tree_node*, tree_node*)     ???:0 0xcf8c9b do_auto_deduction(tree_node*, tree_node*, tree_node*, int, auto_deduction_context, tree_node*, int, tree_node*)     ???:0 0xb701d6 tsubst_requires_expr(tree_node*, tree_node*, int, tree_node*)     ???:0 0xb71b22 constraints_satisfied_p(tree_node*, tree_node*)     ???:0 0xcf8c9b do_auto_deduction(tree_node*, tree_node*, tree_node*, int, auto_deduction_context, tree_node*, int, tree_node*)     ???:0 0xbd4e9d cp_finish_decl(tree_node*, tree_node*, bool, tree_node*, int, cp_decomp*)     ???:0 0xcdc754 c_parse_file()     ???:0 0xe1eca9 c_common_parse_file()     ???:0 Please submit a full bug report, with preprocessed source (by using -freport-bug). Please include the complete backtrace with any bug report. See &lt;https://gcc.gnu.org/bugs/&gt; for instructions. Compiler returned: 1</pre>	<pre>clang++: /root/llvm-project/clang/lib/AST/ExprConstant.cpp:15495: bool clang::Expr::EvaluateAsConstantExpr(clang::Expr::EvalResul t&amp;, const clang::ASTContext&amp;, clang::Expr::ConstantExprKind) const: Assertion `!isValueDependent() &amp;&amp; "Expression evaluator can't be called on a dependent expression.'" failed. PLEASE submit a bug report to https://github.com/llvm/llvm-project/issues/ and include the crash backtrace, preprocessed source, and associated run script. Stack dump: 0. Program arguments: /opt/compiler-explorer/clang-assertions-trunk/bin/clang++ -gdwarf-4 -g -o /app/output.s -mllvm --x86-asm-syntax=intel -S --gcc-toolchain=/opt/compiler-explorer/gcc-snapshot -fcolor-diagnostics -fno-crash-diagnostics -std=c++2b -O -stdlib=libc++ &lt;source&gt; 1. &lt;source&gt;:47:15: current parser token ';' #0 0x0000000003722508 llvm::sys::PrintStackTrace(llvm::raw_ostream&amp;, int) (/opt/compiler-explorer/clang-assertions-trunk/bin/clang++ +0x3722508) #1 0x00000000037201cc llvm::sys::CleanupOnSignal(unsigned long) (/opt/compiler-explorer/clang-assertions-trunk/bin/clang++ +0x37201cc) #2 0x0000000003668e38 CrashRecoverySignalHandler(int) CrashRecoveryContext.cpp:0:0 #3 0x00007fd43e6ce420 __restore_rt (/lib/x86_64-linux-gnu/libpthread.so.0+0x14420) #4 0x00007fd43e19100b raise (/lib/x86_64-linux-gnu/libc.so.6+0x4300b) #5 0x00007fd43e170859 abort (/lib/x86_64-linux-gnu/libc.so.6+0x22859) #6 0x00007fd43e170729 (/lib/x86_64-linux-gnu/libc.so.6+0x22729) #7 0x00007fd43e181fd6 (/lib/x86_64-linux-gnu/libc.so.6+0x33fd6)</pre>	
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<pre>&lt;source&gt;:33:30: internal compiler error: Segmentation fault   33        { t.ids() } -&gt; RangeOver&lt;[]&lt;std::integral&gt;{}&gt;;                                       ^~~~~~ 0x255cc4e internal_error(char const*, ...)       ???:0 0xceb951 template_parms_to_args(tree_node*)       ???:0 0xd29d62 tsubst_lambda_expr(tree_node*, tree_node*, int, tree_node*)       ???:0 0xd0e051 tsubst_template_arg(tree_node*, tree_node*, int, tree_node*)       ???:0 0xb71b22 constraints_satisfied_p(tree_node*, tree_node*)       ???:0 0xcf8c9b do_auto_deduction(tree_node*, tree_node*, tree_node*, int, auto_deduction_context, tree_node*, int, tree_node*)       ???:0 0xb701d6 tsubst_requires_expr(tree_node*, tree_node*, int, tree_node*)       ???:0 0xb71b22 constraints_satisfied_p(tree_node*, tree_node*)       ???:0 0xcf8c9b do_auto_deduction(tree_node*, tree_node*, tree_node*, int, auto_deduction_context, tree_node*, int, tree_node*)       ???:0 0xbd4e9d cp_finish_decl(tree_node*, tree_node*, bool, tree_node*, int, cp_decomp*)       ???:0 0xcdc754 c_parse_file()       ???:0 0xe1eca9 c_common_parse_file()       ???:0 Please submit a full bug report, with preprocessed source (by using -freport-bug). Please include the complete backtrace with any bug report. See &lt;https://gcc.gnu.org/bugs/&gt; for instructions. Compiler returned: 1</pre>	<pre>clang++: /root/llvm-project/clang/lib/AST/ExprConstant.cpp:15495: bool clang::Expr::EvaluateAsConstantExpr(clang::Expr::EvalResul t&amp;, const clang::ASTContext&amp;, clang::Expr::ConstantExprKind) const: Assertion `!isValueDependent() &amp;&amp; "Expression evaluator can't be called on a dependent expression.'" failed. PLEASE submit a bug report to https://github.com/llvm/llvm-project/issues/ and include the crash backtrace, preprocessed source, and associated run script. Stack dump: 0. Program arguments: /opt/compiler-explorer/clang-assertions-trunk/bin/clang++ -gdwarf-4 -g -o /app/output.s -mllvm --x86-asm-syntax=intel -S --gcc-toolchain=/opt/compiler-explorer/gcc-snapshot -fcolor-diagnostics -fno-crash-diagnostics -std=c++2b -O -stdlib=libc++ &lt;source&gt; 1. &lt;source&gt;:47:15: current parser token ';' #0 0x0000000003722508 llvm::sys::PrintStackTrace(llvm::raw_ostream&amp;, int) (/opt/compiler-explorer/clang-assertions-trunk/bin/clang++ +0x3722508) #1 0x00000000037201cc llvm::sys::CleanupOnSignal(unsigned long) (/opt/compiler-explorer/clang-assertions-trunk/bin/clang++ +0x37201cc) #2 0x0000000003668e38 CrashRecoverySignalHandler(int) CrashRecoveryContext.cpp:0:0 #3 0x00007fd43e6ce420 __restore_rt (/lib/x86_64-linux-gnu/libpthread.so.0+0x14420) #4 0x00007fd43e19100b raise (/lib/x86_64-linux-gnu/libc.so.6+0x4300b) #5 0x00007fd43e170859 abort (/lib/x86_64-linux-gnu/libc.so.6+0x22859) #6 0x00007fd43e170729 (/lib/x86_64-linux-gnu/libc.so.6+0x22729) #7 0x00007fd43e181fd6 (/lib/x86_64-linux-gnu/libc.so.6+0x33fd6)</pre>	<pre>example.cpp Compiler returned: 0</pre>
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