C++ is a Metacompiler

Daniel Nikpayuk

2024

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Practical:

Theory:

- Introduction
- Motivation
- Oemonstration
- Performance

Practical:

- Introduction
- Motivation
- Oemonstration
- Performance

Theory:

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1st half:

Practical



Introduction



Who am I?

- I'm a self-taught coder.
- I've been programming in C++ since 2005.
- I don't currently work in the tech industry.
- I have a Bachelor of Arts majoring in mathematics, minoring in economics.
- I am an Inuit person (specifically Inuvialuit) from Canada's western Arctic.
- I am devoted to the continued renewal of my people's language and culture.

Why C++?

- It is a life goal of mine to build a programming language for multimedia production.
- I hope to offer said language as an option for telling and retelling my people's stories, traditional and new.



Figure: inuksuk

 Such a language will generally require systems level performance, and so C++ is a good fit for writing its first compiler.

Motivation

What is a metacompiler?

What is a metacompiler? The short answer for now. . .

What is a metacompiler? The short answer for now. . . is it's a compile time compiler.

What is a metacompiler? The short answer for now. . . is it's a compile time compiler.

My talk is about the working metacompiler that I have built, and this section provides my motivation for doing so. How long have I been working on this project?

How long have I been working on this project? Directly, about 2 years.

How long have I been working on this project? Directly, about 2 years. Indirectly,

How long have I been working on this project? Directly, about 2 years. Indirectly, about 10 years. What would motivate me

What would motivate me to work on this for 10 years?

What would motivate me to work on this for 10 years?

loops.

When I first starting programming,

When I first starting programming, the initial years were about getting to know the language.

After that,

After that,

I spent time writing in the Qt framework,

After that,

I spent time writing in the Qt framework, because graphical programming is fun.

I had some success, I even wrote some (unpublished) smartphone apps, I had some success, I even wrote some (unpublished) smartphone apps,

but after a while I plateaued and decided it was time to improve my skillset.

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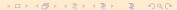
What did I do?



I reproduced the standard library containers, such as vector.

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In doing so, I found myself writing many loops which I felt were both small variations of each other,



I reproduced the standard library containers, such as vector.

In doing so, I found myself writing many loops which I felt were both small variations of each other, and tedious to write.

```
while (in != end)
{
    perform_action(in);
    increment(in);
}
```

```
while (in <= end)
{
    perform_action(in);
    increment(in);
}</pre>
```

```
while (in != end)
   perform_action(in);
   increment(in);
perform_action(in);
```

```
increment(in);
while (in != end)
   perform_action(in);
   increment(in);
perform_action(in);
```

With loops like these,

With loops like these, I was spending more effort thinking about the syntax With loops like these, I was spending more effort thinking about the syntax than the semantics of the loop.

With this style of grammar, scope is hardcoded.

With this style of grammar, scope is hardcoded. This limits our options when it comes to loops.

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Scope is good though:

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Scope is good though: If you've ever written assembly,

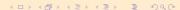
With this style of grammar, scope is hardcoded. This limits our options when it comes to loops.

Scope is good though: If you've ever written assembly, you realize the importance of scope.

With this style of grammar, scope is hardcoded. This limits our options when it comes to loops.

Scope is good though: If you've ever written assembly, you realize the importance of scope.

So I had to find another way.



Ranges are the standard solution to this problem,

Ranges are the standard solution to this problem,

I designed an alternative called: Intervals.



I borrow the interval notation from math.

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The idea of an interval is it encodes an iteration, but with options which communicate how the iteration algorithm acts on its endpoints.

I borrow the interval notation from math.

The idea of an interval is it encodes an iteration, but with options which communicate how the iteration algorithm acts on its endpoints.

The options are defined as follows:

- [] closed
- (] opening
- () open
- [) closing

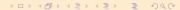
- [] closed: acts on the left and right endpoints.
- (] opening
- () open
- [) closing

- [] closed
- (] opening: skips the left, acts on the right.
- () open
- [) closing

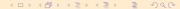
- [] closed
- (] opening
- () open: skips the left, doesn't act on the right.
- [) closing

- [] closed
- (] opening
- () open
- [) closing: acts on the left, not on the right.

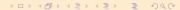
$$sum [1, 3] == 6$$



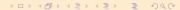
$$sum (1, 3] == 5$$



$$sum (1, 3) == 2$$



$$sum [1, 3) == 3$$



To summarize,

To summarize, I wanted access to a domain specific language (DSL),

To summarize, I wanted access to a domain specific language (DSL), within C++ itself.

Demonstration

What is a metacompiler?

What is a metacompiler?

It's a compile time compiler,

What is a metacompiler?

It's a compile time compiler, which compiles DSLs.

In this section I introduce my chord DSL.

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It's not the point of this talk,

In this section I introduce my chord DSL.

It's not the point of this talk, but it does demonstrate what's possible



In this section I introduce my chord DSL.

It's not the point of this talk, but it does demonstrate what's possible given a working metacompiler.

example: square

```
main x

body:
    . = multiply x x;
    return _ ;
```

example: sum of squares

```
main x y
body:
 x = multiply x x ;
  y = multiply y y ;
  = add
               х у;
  return
```

example:

$$(x+1)^2$$

example: exponents

example: square (argpose)

```
main x
vars:
  declare sq
defs:
  sq # argpose[1]{multiply 0 0}
body:
  . = sq x
  return
```

```
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vars:
  declare sq
defs:
  sq # argpose[1]{multiply 0 0}
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  return
```

```
main x
vars:
  declare sq
defs:
  sq # argpose[1]{multiply 0 0}
body:
  = sq x
  return
```

example: sum of squares (subpose)

```
main x y
vars:
  declare sq sum_of_sq
defs:
            # argpose[1]{multiply 0 0}
  sq
  sum_of_sq # subpose[2]{add sq sq}
body:
  . = sum_of_sq x y
  return
```

```
main x y
vars:
  declare sq sum_of_sq
defs:
            # argpose[1]{multiply 0 0}
  sq
  sum_of_sq # subpose[2]{add sq sq}
body:
  . = sum_of_sq x y
  return
```

```
main x y
vars:
  declare sq sum_of_sq
defs:
            # argpose[1]{multiply 0 0};
  sq
  sum_of_sq # subpose[2]{add sq sq}
body:
  . = sum_of_sq x y
  return
```

```
main x y
vars:
  declare sq sum_of_sq
defs:
            # argpose[1]{multiply 0 0}
  sq
  sum_of_sq # subpose[2]{add sq sq}
body:
  . = sum_of_sq x y
  return
```

```
main x y
vars:
  declare sq sum_of_sq
defs:
            # argpose[1]{multiply 0 0}
  sq
  sum_of_sq # subpose[2]{add sq sq}
body:
  . = sum_of_sq x y
  return
```

```
main x y
vars:
  declare sq sum_of_sq
defs:
            # argpose[1]{multiply 0 0}
  sq
  sum_of_sq # subpose[2]{add sq sq}
body:
  . = sum_of_sq x y
  return
```

example: twice (curry)

```
main x
vars:
  declare twice
defs:
  twice # curry[1]{multiply two}
body:
  . = twice x
  return
```

, binding("two", 2)

```
main x
vars:
  declare twice
defs:
  twice # curry[1]{multiply two}
body:
  . = twice x
  return
, binding("two", 2)
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  twice # curry[1]{multiply two}
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```

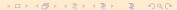
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```
main x
vars:
  declare twice
defs:
  twice # curry[1]{multiply two}
body:
  . = twice x
  return
```

, binding("two", 2)



example: factorial (naive)

```
type T
factorial n -> T ;
body:
 test equal n 0
  branch done
  . = subtract n 1 ;
  . = factorial ;
  . = multiply n _ ;
  return
done:
  return 1:T
```

```
type T ;
factorial n -> T ;
```

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```
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```
type T
factorial n -> T
```

```
body:
 test equal n 0
  branch done
  . = subtract n 1 :
  . = factorial _ ;
  . = multiply n _ ;
  return
```

```
done:
return 1:T
```

```
done:
return 1:T
```

example: factorial (goto)

```
main p n
loop:
  test is_zero n ;
  branch done
  p = multiply p n ;
  n = decrement n ;
  goto loop
done:
  return p
```

Why is this language called chord?

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Chord is a high level assembly language, which provides direct support for the classical functional operators:

Why is this language called chord?

Chord is a high level assembly language, which provides direct support for the classical functional operators:

{repeat, map, fold, find, sift}

In particular,

In particular, I modified these operators to work well with $\mathsf{C}++$ iterators.

In particular, I modified these operators to work well with C++ iterators.

I wanted a distinct terminology to describe these new grammatical patterns,

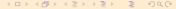
In particular, I modified these operators to work well with $\mathsf{C}++$ iterators.

I wanted a distinct terminology to describe these new grammatical patterns, and so I loosely borrowed from music terminology.

• I first rename an iterator to be a note.

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- Two notes together define an interval: [in, end)

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- Two notes together define an interval: [in, end)
- A sequence of intervals is a chord: [,)[)[]



- I first rename an iterator to be a note.
- Two notes together define an interval: [in, end)
- A sequence of intervals is a chord: [,)[)[]
- A sequence of chords is a progression.

Refering back to my original motivation:

Refering back to my original motivation:

I wanted to write loops with a grammar

Refering back to my original motivation:

I wanted to write loops with a grammar that let me focus on the semantics of the algorithm, not the syntax.

This started with the idea of an interval:

$$sum [1, 3] == 6$$



example: sum (fold)

```
main out in end
vars:
  declare sum
defs:
  sum # fold[1]{add * @|||} <> [,];
body:
  . = sum !out in end
  return
```

fold[N] {combine|act|mutate|break}

fold[N]{combine|act|mutate|break}

```
defs:
  sum # fold[1]{add * @|||} <> [,];
body:
  . = sum !out in end
  return
```

```
defs:
  sum # fold[1]{add * @|||} <> [,];
body:
  . = sum !out in end
  return
```

```
defs:
  sum # fold[1]{add * @|||} <> [,];
body:
  . = sum !out in end
  return
```

```
defs:
  sum # fold[1]{add * @|||} <> [,] ;
body:
  . = sum !out in end
  return
```

```
defs:
  sum # fold[1]{add * @|||} <> [,] ;
body:
  . = sum !out in end
  return
```

```
defs:
  sum # fold[1]{add * 0|||} <> [,];
body:
  . = sum !out in end
  return
```

```
defs:
  sum # fold[1]{add * @|||} <> [,];
body:
  . = sum !out in end
  return
```

example: vector addition (map)

```
main out in end in1
vars:
  declare vec add
defs:
  vec_add # map[2]{add||} [) [,) [);
body:
  . = vec_add !out in end in1
  return
```

```
defs:
    vec_add # map[2]{add||} [) [,) [);
body:
    . = vec_add !out in end in1 ;
    return _ ;
```

example:

change of base (progression)

$$12_{\text{(base 10)}} \quad \rightarrow \quad ?_{\text{(base 2)}}$$

```
main out in
vars:
 declare change_base print_change
defs:
 change_base # map[1]{rem_by_n @||} [) [div_by_n|~,)
 print_change # repeat[1]{|print * @|} (-|+,] <>
body:
  . = change_base !out in 0
  . = print_change _ out format
 return
           // template<auto radix>
           , binding( "div_by_n" , _divide_by_<radix> )
           , binding( "rem_by_n" , _modulo_by_<radix> )
           , binding( "format" , strlit_type{"%d"} )
```

```
defs:
    change_base # map[1]{rem_by_n @||} [) [div_by_n|~,);
    print_change # repeat[1]{|print * @|} (-|+,] <> ;
body:
    . = change_base !out in 0 ;
    . = print_change _ out format ;
    return
```

```
map[1]{rem_by_n @||} [) [div_by_n|~,);
```



```
defs:
    change_base # map[1]{rem_by_n @||} [) [div_by_n|~,);
    print_change # repeat[1]{|print * @|} (-|+,] <> ;
body:
    . = change_base !out in 0 ;
    . = print_change _ out format ;
    return
```

Hustle

What is a metacompiler?

What is a metacompiler?

It's a compile time compiler,



What is a metacompiler?

It's a compile time compiler, which compiles DSLs.

What is a metacompiler?

It's a compile time compiler, which compiles DSLs. The key phrase being DSLs.

Here I also introduce my hustle DSL.

Here I also introduce my hustle DSL.

It is as close to the scheme (lisp) programming language that this paradigm will allow.

example: factorial

```
(type T
  (define (factorial n) -> T
    (if (= n 0)
        1:T
        (* n (factorial (- n 1)))
    )))
```

Performance

This short section is informal.

This short section is informal.

Before we commit to detailed theory (in the following),

This short section is informal.

Before we commit to detailed theory (in the following), I thought I'd offer some basic stats here.

First, a reality check.

In the previous section we introduced the hustle DSL:

```
(type T
  (define (factorial n) -> T
    (if (= n 0)
        1:T
        (* n (factorial (- n 1)))
    )))
```

In
$$C++17$$
,

In order to metacompile it, we actually write it like this:



```
constexpr auto _hustle_factorial_v0()
  return source
      "(type T
                                             11
         (define (factorial n) -> T
                                             11
      11
            (if (= n 0))
                                             ш
      11
              1:T
                                             ш
              (* n (factorial (- n 1)))
      ш
      11
                                             ш
                                             п
      ш
      ")
                                             ш
```

It's a string literal we wrap in a function,

It's a string literal we wrap in a function, so we can pass it as a template parameter:

Our metacompiler is a compile time compiler,

Our metacompiler is a compile time compiler,

That turns C++ string literals into C++ constexpr functions.



Our metacompiler is a compile time compiler,

That turns C++ string literals into C++ constexpr functions. They can be used both at compile time and at run time.

We won't go into detail here,

We won't go into detail here,

but a quick explanation as to how this works



We won't go into detail here,

but a quick explanation as to how this works is that a metacompiler turns this:



```
constexpr auto _chord_factorial_v0()
{
        return source
        (
                "type T
                "factorial n -> T
                "body:
                " test equal n 0
                " branch done
                   . = subtract n 1 ;"
                   . = factorial _ ;"
                   . = multiply n _
                   return _
                "done:
                " return 1:T
                                     ;"
        );
}
```

into this:

```
constexpr size_type value[][8] =
{
    { MN::id
                        . MT::id
                                                                          1 },
                                                   0.
                                                               0,
                                                                    0,
    { MN::hash
                        , MT::port
                                              5,
                                                   0,
                                                                    0.
                                                                          1 },
                                                         0,
                                                               0,
    { MN::pad
                        , MT::select
                                                               0.
                                                                          1 },
                                                         0.
                                                                          1 },
    { MN::pad
                        , MT::id
                                              0,
                                                   0.
                                                         0.
                                                                    0.
    { MN::go_to
                                                                          1 },
                        . MT::id
                                                                    0.
                                             50.
                                                   0.
                                                         0.
                                                               0,
                                                                          1 },
    { MN::id
                        , MT::id
                                                                    0.
                                              0,
                                                   0,
    { MN::eval
                        . MT::back
                                              7,
                                                                    0,
                                                                          4 },
                                                               0,
    { MN::id
                        . MT::id
                                              0.
                                                   0,
                                                         0,
                                                                    0.
                                                                          1 },
                                                               0,
    { MN::lookup
                        , MT::first
                                              0,
                                                   7.
                                                         0.
                                                                    0.
                                                                          1 },
    { MN::halt
                        . MT::first
                                                                          1 },
                                              0.
                                                   0.
                                                                    0.
                                                                          5 },
    { MN::eval
                        , MT::back
                                             11.
                                                   0.
                                                                    0,
                                                                          1 },
    { MN::id
                        . MT::id
                                                   0.
                                                                    0.
                                              0,
                                                         0.
                                                               0,
    { MN::arg
                        . MT::select
                                              1,
                                                   0,
                                                               0,
                                                                    0,
                                                                          1 },
                                                                          1 },
    { MN::arg
                        , MT::drop
                                                         0.
                                                                    0.
                                              0,
                                                   0.
    { MN::halt
                        . MT::first
                                              0,
                                                   0,
                                                               0,
                                                                    0.
                                                                          1 },
    { MN::type
                        . MT::n number
                                                                          1 },
                                              0,
                                                   0,
                                                         0,
                                                               0,
                                                                    0,
    { MN::literal
                        . MT::back
                                             0,
                                                   0.
                                                         0.
                                                                    0.
                                                                          1 },
                                                               0,
```

which we then pass to this:

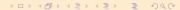


which finally turns into a constexpr function.

which finally turns into a constexpr function.

As for performance. . .

The square root function,



The square root function, implemented using newton's method,

The square root function, implemented using newton's method, written in the hustle DSL:



```
(type T
  (define (sqrt x)
    (define (square y) (* y y))
    (define (abs y) (if (< y 0) (- y) y))
    (define (good-enough? guess) (< (abs (- (square guess) x)) tolerance))</pre>
    (define (average y z) (/ (+ y z) 2))
    (define (improve guess) (average guess (/ x guess)) )
    (define (sqrt-iter guess) -> T
      (if (good-enough? guess) guess (sqrt-iter (improve guess)))
    (sqrt-iter 1:T)))
, binding("tolerance", 0.0001)
```

Before showing performance stats on this algorithm,

Before showing performance stats on this algorithm, let's observe the stats if it were reimplemented in standard C++17:

```
template<typename T>
constexpr auto sqrt_iter(T x, T guess) -> T
   auto tolerance = 0.0001:
   auto square = [](T y){ return y * y; };
   auto abs = [](T y){return (y < 0) ? -y : y; };
   auto good_enough = [&](T g){ return (abs(square(g) - x) < tolerance); };</pre>
   auto average = [](T y, T z){return (y + z) / 2;};
                    = [&](T g){ return average(g, x/g); };
   auto improve
   if (good_enough(guess)) return guess;
   else
                           return sqrt_iter(x, improve(guess));
}
template<typename T>
constexpr auto sqrt(T x) { return sqrt_iter<T>(x, 1.0); }
```

| | gcc | clang |
|--------------------|----------|----------|
| compile time | 0.100 s | 0.114 s |
| run time | 0.001 s | 0.001 s |
| -01 binary size | 16 176 B | 16 104 B |
| -02/03 binary size | 16 128 B | 16 104 B |

```
(type T
  (define (sqrt x)
    (define (square y) (* y y))
    (define (abs y) (if (< y 0) (- y) y))
    (define (good-enough? guess) (< (abs (- (square guess) x)) tolerance))</pre>
    (define (average y z) (/ (+ y z) 2))
    (define (improve guess) (average guess (/ x guess)) )
    (define (sqrt-iter guess) -> T
      (if (good-enough? guess) guess (sqrt-iter (improve guess)))
    (sqrt-iter 1:T)))
, binding("tolerance", 0.0001)
```



| | gcc | clang |
|--------------------|----------|----------|
| compile time | 0.390 s | 0.842 s |
| run time | 0.002 s | 0.001 s |
| -01 binary size | 17 432 B | 16 624 B |
| -02/03 binary size | 16 272 B | 16 632 B |

2nd half:

Theory



This half of the talk is much more academic.

I introduce a lot of my own terminology.

I introduce a lot of my own terminology. Reasoning about a metacompiler involves a lot of context switching,

I introduce a lot of my own terminology. Reasoning about a metacompiler involves a lot of context switching, and so having distinct terms helps keep contextual boundaries clear.

Philosophy

Before we can engineer, we need to design.

Before we can engineer, we need to design. A good start is to question our terms.

Before we can engineer, we need to design. A good start is to question our terms.

This section is about design,

Before we can engineer, we need to design. A good start is to question our terms.

This section is about design, and the philosophy behind the metacompiler paradigm.

• A metacompiler is a compile time compiler.

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- C++ is a metacompiler.

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- C++ is a metacompiler.
- We've seen what a metacompiler does.

- A metacompiler is a compile time compiler.
- C++ is a metacompiler.
- We've seen what a metacompiler does.
- We now ask what a metacompiler is.

Let's take a short tour of related concepts.



• What is a compiler?

- What is a compiler?
- What is an interpreter?

- What is a compiler?
- What is an interpreter?
- What is a transpiler?

 A compiler takes source code and translates it into assembly.

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- An interpreter takes source code, translates, then executes it directly.

- A compiler takes source code and translates it into assembly.
- An *interpreter* takes source code, translates, then executes it directly.
- A *transpiler* takes source code and translates it into the source code of another language.

Do these ideas apply to a metacompiler?

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• Compiler: Yes, a metacompiler takes source code and translates it into an intermediate assembly.

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- Compiler: Yes, a metacompiler takes source code and translates it into an intermediate assembly.
- Interpreter: Maybe, a metacompiled function can be executed at compile time.
- Transpiler: Maybe, a metacompiler takes source code and does translate it into C++, but only C++.

What makes it "meta?"

• The prefix comes from metaprogramming.

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- The prefix comes from metaprogramming.
- In C++ this means compile time programming.
- This includes constexpr time programming, as well as template metaprogramming.

As such, a metacompiler requires we refine our notion of time.

We ask:

We ask:

• What is a timescape?



We ask:

- What is a timescape?
- What is a timescope?

The short answer:

When observing the lifespan of a program, a timescape allows us to decompose it into timescopes.

• Run time is when a program is being executed.

- Run time is when a program is being executed.
- Compile time is when a program is being translated for execution.

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program lifespan [compile time | run time | | metacompile time | metarun time |

What about constexpr time?

What about constexpr time?

• This is C++ specific.

What about constexpr time?

- This is C++ specific.
- This timescope in effect represents either run time or metarun time.

A metacompiler requires we also consider ideas of self similarity.

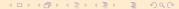
Why?

Why?

Because in theory we could metacompile source code from the same language that is otherwise being compiled.



• What is a metacircular evaluator?



- What is a metacircular evaluator?
- What is a self-hosting compiler?

- What is a metacircular evaluator?
- What is a self-hosting compiler?
- What is an abstract machine?

- What is a metacircular evaluator?
- What is a self-hosting compiler?
- What is an abstract machine?
- What is a virtual machine?

• Starts with interpreted language.

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- Builds a metacircular library.

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A metacircular evaluator:

- Starts with interpreted language.
- Builds a metacircular library.
- Builds a function called an evaluator.
- This evaluator simulates the language's own interpreter.
- This evaluator can execute source code from the same language.

• Is the compiled version of a metacircular evaluator.

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• Is the compiled version of a metacircular evaluator.

What's the difference?

• An interpreter is allowed to interleave source code translation with execution.

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- An interpreter is allowed to interleave source code translation with execution.
- A compiler is restricted to modularizing source code translation from execution. It must translate first, only then can it execute.
- This creates subtle differences in their respective designs.

• Is a state machine.

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- It performs computations by passing data through a chain of states $[0 \rightarrow N]$:

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$$S_{0:\mathsf{begin}} \quad o \quad S_1 \quad o \quad \dots \quad o \quad S_{N:\mathsf{end}}$$

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- Such states are usually expected to have the same shape. In effect, you can consider them to be a data structure.
- These machines are generally given some kind of controller (sometimes source code) to direct their computation.

A virtual machine



Is an abstract machine.

- Is an abstract machine.
- Has states that represent actual hardware.

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- Has states that represent actual hardware.
- Can be used to simulate hardware on top of actual hardware.

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- metacircular evaluator: Sort of, in theory we can interleave translation and execution to interpret.
- self-hosting compiler: Maybe, in theory we could rebuild C++ itself, but done at compile time it might not be performant enough to be worth it.
- abstract machine: Yes, such machines underly the implementation design.
- virtual machine: Somewhat, in theory optimized state transitions can be designed with hardware in mind.

• It is a toolchain of related technologies which translate source code into assembly.

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- In terms of the technologies that make up this chain,

- It is a toolchain of related technologies which translate source code into assembly.
- In terms of the technologies that make up this chain, it is the idea of a DSL engine that is most relevant to this talk.

What is a DSL engine?



What is a DSL engine?

It is an abstract machine which translates domain specific languages into assembly.

We've discussed the idea of a metacompiler more broadly,

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Why is C++ a metacompiler?

- It is a metacompiler because of its specification,
 C++17 and later.
- C++17 has an emergence of grammar and rules to support a DSL engine, one which is also performant.
- It is independent of vendor implementation.

Methodology

• A parser generator.

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- DSLs, each having their own lexers, and parsers.

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- A shared intermediate representation (IR).

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- DSLs, each having their own lexers, and parsers.
- A shared intermediate representation (IR).
- A DSL engine which turns the IR into a constexpr C++ function.

In this section we give a brief history and overview of the theoretical methods needed

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As for the DSL engine, the actual implementation details will be given in the next section.

Why talk about methods?

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A general purpose DSL engine needs to be able to metacompile any language,

Why talk about methods?

A general purpose DSL engine needs to be able to metacompile any language, and so we need its implementation design to be based on expressive theoretical foundations We start with the methods of compiler theory, which is divided into the frontend and backend.

The frontend focuses on the lexing and parsing of source code.

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The backend focuses on multilayered translations from an initial IR assembly, to the final target assembly.

To keep things simple, lexers:

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Read source code.



To keep things simple, lexers:

- Read source code.
- Translate words into tokens.

To keep things simple, lexers:

- Read source code.
- Translate words into tokens.
- Are constructed from regular languages and regular automata.

To keep things simple, parsers:

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- Translate sentences into IR assembly.

- Read tokenized source code.
- Confirm "sentence" structure.
- Translate sentences into IR assembly.
- Are constructed from context free grammars and pushdown automata.

 Assembly languages are generally implemented using methods derived from register machines.

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- Such methods coincide well with implementing imperative DSLs.

- Assembly languages are generally implemented using methods derived from register machines.
- Such methods coincide well with implementing imperative DSLs.
- Such methods are less effective when implementing functional DSLs.

We need methods that can implement both imperative and functional languages.

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To motivate such methods, let's now take a quick tour of computing history.

• Alan Turing, 1936.

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- Equivalent to μ -recursive functions (math).
- Well suited for modeling theoretical properties of computable functions.
- Less well suited for modeling practical or performant computable functions.

• Alonzo Church, 1930s.

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- Equipotent to Turing machines.
- Well suited for modeling theoretical grammar of computable functions.
- Less well suited (on its own) for modeling certain consistency semantics of computable functions.

• John McCarthy, late 1950s.

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- Is now a family of languages, including Common Lisp, Scheme, Clojure, and Racket.

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- Influenced by the lambda calculus.
- Is now a family of languages, including Common Lisp, Scheme, Clojure, and Racket.
- Aligns well with the functional programming paradigm.

To delve further into functional programming,

To delve further into functional programming, we need to equip the lambda calculus (or lisp) with a type theory.

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But first...

^{*}See Russell's Paradox.

• Georg Cantor, late 1800s.

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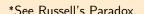
- Georg Cantor, late 1800s.
- A foundational language of mathematics.

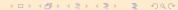
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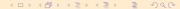
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- Proof that there are "different sizes of infinity."

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- Georg Cantor, late 1800s.
- A foundational language of mathematics.
- Proof that there are "different sizes of infinity."
- If taken as a naive theory, it leads to contradictions.*







 Bertrand Russell and Alfred North Whitehead, early 1900s.

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- Principia Mathematica, intended as an alternative to set theory.
- Mathematicians did not adopt this approach, instead vying for axiomatic set theory.
- Helped advance the subject of symbolic logic.

• Multiple contributors (here unnamed), mid 1900s.

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- Well suited for modeling certain *consistency* semantics of computable functions.

- Multiple contributors (here unnamed), mid 1900s.
- More recently Per Martin-Löf, late 1900s.
- Well suited for modeling certain consistency semantics of computable functions.
- Aligns well with the lambda calculus[†], functional programming, and the family of LISPs.

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Although my current chord and hustle DSLs do not have their own type systems (mostly),

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The important realization here is that if you equip the lambda calculus (or LISP) with a given type theory, you get a modern functional language such as Haskell. Type theory or not, this leads us to...

Type theory or not, this leads us to... abstract machines.

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We previously introduced this idea, but in the context of the lambda calculus and LISP, we can specifically mention SECD, CESK, and Krivine machines.

Type theory or not, this leads us to... abstract machines.

We previously introduced this idea, but in the context of the lambda calculus and LISP, we can specifically mention SECD, CESK, and Krivine machines.

Each uses different grammatical artifacts from the untyped lambda calculus to implement its own version of an abstract machine. Abstract machines

VS

Register machines

Abstract machines:

Abstract machines:

 Consist of some version of a controller, memory lookup, and call stack.

Abstract machines:

- Consist of some version of a controller, memory lookup, and call stack.
- They transition states by updating these components, which is how they perform their computations.

Register machines:

Register machines:

• They are abstract machines.

Register machines:

- They are abstract machines.
- The only difference is their design more closely resembles actual computer architecture.

A final method worth mentioning. . .

A variation on the idea of a function where instead of returning a value,

A variation on the idea of a function where instead of returning a value, it is passed as the input to another continuation passing function.

A variation on the idea of a function where instead of returning a value, it is passed as the input to another continuation passing function.

CPS is theoretically sound, and even has its own form of composition:

$$f(x, c_1(y)) \star g(y, c_2(z))$$

:= $f(x, \lambda y.g(y, c_2(z)))$
= $f^*(x, c_2(z))$

(types are hidden for clarity)

Library

In this section I introduce my cctmp library.

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It is an open source repo on GitHub[‡],

In this section I introduce my cctmp library.

It is an open source repo on GitHub[‡], It is not currently ready for official release.

• It is implemented using C++17.

- It is implemented using C++17.
- It does not use the standard library. (std::)

- It is implemented using C++17.
- It does not use the standard library. (std::)
- It is currently split in two: A proof of concept, as well as a semiself hosting version.

• It is roughly 20 000 lines of code.



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- All DSL code examples I've already shown can be metacompiled in this version.

- It is roughly 20 000 lines of code.
- All DSL code examples I've already shown can be metacompiled in this version.
- The hustle DSL does not yet support all language features of the scheme lang (for which it is based).

For example:

```
(define (main n)
  ((if (= n 0) + *) 2 3)
)
```

What about the semiself hosting version?

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What is semiself hosting?

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What is semiself hosting? One of the long term goals for this metacompiler is to use the chord and hustle DSLs to reimplement parts of the metacompiler itself.

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As this is not proper self hosting (C++) implementing C++, I prefix it with semi- to make the distinction.

As for the semiself hosting version:

As for the semiself hosting version:

• It is a restructuring of the proof of concept version.

As for the semiself hosting version:

- It is a restructuring of the proof of concept version.
- The first 4 000 lines of code represents the bare minimum C++ needed to run meta-assembly programs.

Although the front end comes first in the translation process,

Although the front end comes first in the translation process, it is the backend which shapes the overall design.

Although the front end comes first in the translation process, it is the backend which shapes the overall design. As such, we'll discuss it first.

The backend is designed as an abstract machine,

$$S_0 \rightarrow \ldots \rightarrow S_n$$

$$S_0 \rightarrow \ldots \rightarrow S_n$$

Each state holds some version of a controller, memory lookup, and call stack.

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The thing is,

$$S_0 \rightarrow \ldots \rightarrow S_n$$

Each state holds some version of a controller, memory lookup, and call stack.

The thing is, we don't want to run this abstract machine as an interpreter,

$$S_0 \rightarrow \ldots \rightarrow S_n$$

Each state holds some version of a controller, memory lookup, and call stack.

The thing is, we don't want to run this abstract machine as an interpreter, the trick in fact is that we use continuation passing functions to represent our machine states.

The twist:

The twist:

Instead of continuation passing, we're continuation constructing.

The twist:

Instead of continuation passing, we're continuation constructing. We're using continuation passing composition to construct our function, which is what we want from a compiler.

Continuation constructing machines.

- Continuation constructing machines.
- To date, there are 56 distinct machines, making up roughly 1 500 lines of code.

- Continuation constructing machines.
- To date, there are 56 distinct machines, making up roughly 1500 lines of code.
- Each machine is an indexed function template.

By the way,

By the way, cctmp stands for: continuation constructing template metaprogramming.

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As for how these machines are implemented:

```
template<machine_params(c, i, 1, t, r), typename... Ts>
constexpr static auto result(Ts... vs)
{
```

```
template<auto... filler>
struct T_machine<name::go_to, note::id, filler...>
{
   template<machine_params(c, i, 1, t, r), typename... Ts>
   constexpr static auto result(Ts... vs)
   {
   }
};
```

```
template<auto... filler>
struct T_machine<name::go_to, note::id, filler...>
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};

```
template<machine_params(c, i, 1, t, r), typename... Ts>
constexpr static auto result(Ts... vs)
{
```

```
template<machine_params(c, i, 1, t, r), typename... Ts>
constexpr static auto result(Ts... vs)
{
    constexpr auto ni = dispatch<c>::pos(i);
}
```

```
template<auto... filler>
struct T_machine<name::go_to, note::id, filler...>
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          constexpr auto ni = dispatch<c>::pos(i);
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```

What about the controller, memory lookup, and call stack?

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 controller: It is passed along as a template parameter.



What about the controller, memory lookup, and call stack?

- controller: It is passed along as a template parameter.
- memory lookup: It is passed along the variadic pack.

What about the controller, memory lookup, and call stack?

- controller: It is passed along as a template parameter.
- memory lookup: It is passed along the variadic pack.
- call stack: It is also passed along the variadic pack.



• It is a program composed of meta-assembly.

- It is a program composed of meta-assembly.
- It is implemented as an array of instructions.

- It is a program composed of meta-assembly.
- It is implemented as an array of instructions.
- Each instruction is an array of unsigned integers.

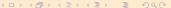
What does this assembly look like?

What does this assembly look like?

We saw it once before:



```
constexpr size_type value[][8] =
{
    { MN::id
                        . MT::id
                                                                          1 },
                                              0,
                                                   0.
                                                               0,
                                                                    0,
    { MN::hash
                        , MT::port
                                              5,
                                                   0,
                                                                    0.
                                                                          1 },
                                                         0,
                                                               0,
    { MN::pad
                        , MT::select
                                              0.
                                                               0.
                                                                          1 },
                                                         0.
                                                                          1 },
    { MN::pad
                        , MT::id
                                              0,
                                                   0.
                                                         0.
                                                               0,
                                                                    0.
    { MN::go_to
                        . MT::id
                                                                    0,
                                                                          1 },
                                             50.
                                                   0.
                                                         0.
                                                               0,
                                                                          1 },
    { MN::id
                        , MT::id
                                                                    0.
                                              0,
                                                   0,
    { MN::eval
                        . MT::back
                                              7,
                                                                    0,
                                                                          4 },
                                                               0,
    { MN::id
                        . MT::id
                                              0.
                                                   0,
                                                         0,
                                                                    0.
                                                                          1 },
                                                               0,
    { MN::lookup
                        , MT::first
                                              0,
                                                   7.
                                                         0.
                                                                    0.
                                                                          1 },
    { MN::halt
                        . MT::first
                                                                          1 },
                                              0.
                                                   0,
                                                                    0.
                                                                          5 },
    { MN::eval
                        , MT::back
                                             11.
                                                   0.
                                                                    0,
                                                                          1 },
    { MN::id
                        . MT::id
                                                   0.
                                                                    0.
                                              0,
                                                         0.
                                                               0,
    { MN::arg
                        . MT::select
                                              1,
                                                   0,
                                                         0,
                                                               0,
                                                                    0,
                                                                          1 },
                                                                          1 },
    { MN::arg
                        , MT::drop
                                                         0,
                                                                    0.
                                              0,
                                                   0.
    { MN::halt
                        . MT::first
                                              0,
                                                   0,
                                                               0,
                                                                    0.
                                                                          1 },
    { MN::type
                        . MT::n number
                                                                          1 },
                                              0,
                                                   0,
                                                         0,
                                                               0,
                                                                    0,
    { MN::literal
                        . MT::back
                                              0,
                                                   0.
                                                         0.
                                                                    0.
                                                                          1 },
                                                               0,
```



Within the context of a variadic pack, and for clarity,

Within the context of a variadic pack, and for clarity, I use the term universe for the memory lookup,

Within the context of a variadic pack, and for clarity, I use the term universe for the memory lookup, and the term stage for the call stack.

As for the universe:



As for the universe:

 It is implemented using the left side of the variadic pack.

As for the universe:

- It is implemented using the left side of the variadic pack.
- New values are inserted at the end of the left side of the pack.



• It is implemented using the right side of the variadic pack.

- It is implemented using the right side of the variadic pack.
- New values are pushed to the back of the pack.

- It is implemented using the right side of the variadic pack.
- New values are pushed to the back of the pack.
- Argument order is preserved when applying functions to their values.

This concludes our discussion of the back end.

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We continue now with the front end.



[§]https://en.wikipedia.org/wiki/Compilers:_Principles,_Techniques,_and_Tools

• The component design and implementation is inspired by the "Dragon Book".§

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- A constexpr LL(1) parser generator is used to construct transition tables for DSL context free grammars.

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- A constexpr LL(1) parser generator is used to construct transition tables for DSL context free grammars.
- The parser generator is designed analogous to the DSLs, where you take a string literal as input.

```
constexpr auto source()
{
    return generator::context_free_grammar
        // start:
            "Start",
        // hustle:
            "Start -> ( Generic )
            "Generic -> type Param Params ( Main ) ;"
                   -> Main
            "Params -> Param Params
                    -> empty
            "Param -> identifier : param_type
            // main:
```

Not yet supported.

Not yet supported.
On my list of things to do.

Not yet supported. On my list of things to do.

Currently each DSL handcodes its own lexer, based on automata theory.

Next, we need to discuss how we map DSL source code variables

[¶]Structure and Interpretation of Computer Programs. (3) (2) (2) (2) (2)

Next, we need to discuss how we map DSL source code variables onto continuation constructing universes

Structure and Interpretation of Computer Programs.

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Structure and Interpretation of Computer Programs.

I borrow a design from the classic SICP¶ textbook, which teaches how to build a metacircular evaluator.

Structure and Interpretation of Computer Programs.

I borrow a design from the classic SICP¶ textbook, which teaches how to build a metacircular evaluator. It uses what's called an environment to keep track of its variables

[¶]Structure and Interpretation of Computer Programs. (3) (2) (2) (2) (2)

• Each environment is a list of frames.

- Each environment is a list of frames.
- Each frame is a list of bindings.

- Each environment is a list of frames.
- Each frame is a list of bindings.
- Each binding is a variable/value pair.

In our case when we parse the source code of a DSL,

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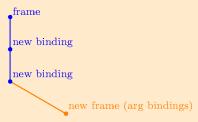
With that in mind, we have the following illustration:

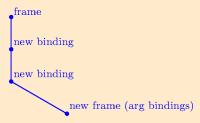
frame



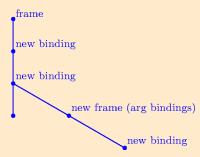


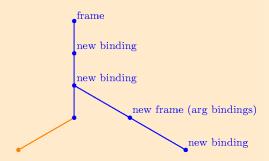


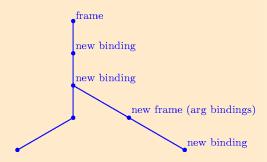


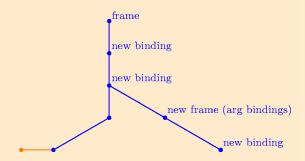


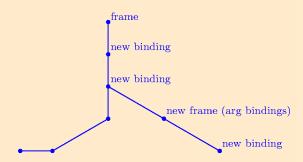


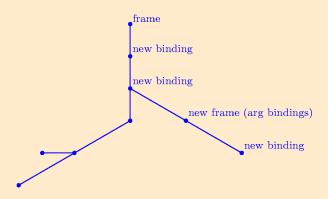


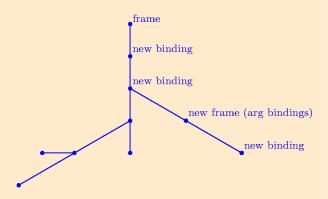


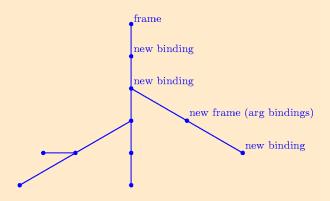


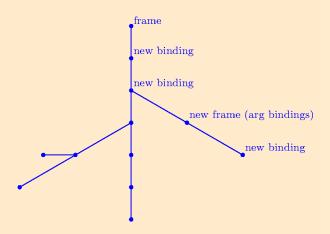












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- Instead of keeping track of values, it holds an index (a promise) of where those values will eventually be in the continuation constructing universe.
- This is why the meta-assembly controller consists of numerical content only.

Before we finish this section,

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Recursion.

Before we finish this section, We have two final technical issues to address, Which are of fundamental importance:

- Recursion.
- Well definedness.

As for recursion?

Anything further right in the universe was defined later in the program.

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Anything further right in the universe was defined later in the program. Mutability can complicate this, but otherwise when we define a function—even a recursive one—we only need the left side of the universe at the time the function was defined.

When we apply a function call, we must provide that leftside universe along with the function arguments.

Even though our functions are continuation passing,

If we call the same function template with the same type input,

If we call the same function template with the same type input, the C++ compiler will recognize it as a recursive call and so complete the function.

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This is why recursion works.



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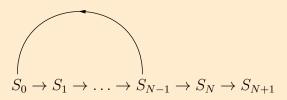
When we move to the next continuation, does it correspond with the next instruction?

The only time this might *not* happen is when the C++ compiler recognizes a recursive call,

The only time this might *not* happen is when the C++ compiler recognizes a recursive call, that the coder didn't intend

The only time this might *not* happen is when the C++ compiler recognizes a recursive call, that the coder didn't intend.

In that case:



We're at step N-1 and we think we're moving to step N, when in fact the compiler creates a recursive call and moves us to step 0.

Because of this $(S_N == S_0)$, but we have no way of knowing if $(S_{N+1} == S_1)$.

If not, no worries, this case doesn't show up in practice:

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If not, no worries, this case doesn't show up in practice: As our metacompiler continuation constructs, it moves forward along the controller, and so calls the next function template with an entirely new controller index. Two C++ functions are considered different if they have different template parameters.

Is it possible to move backward in the controller?

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Yes, but that requires an explicit jump instruction.

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Yes, but that requires an explicit jump instruction. The chord and hustle DSLs require the user explicitly request a jump as a goto, a branch, or a recursive call.

Finally, there is still the possibility that the user asks for a goto or branch,

Finally, there is still the possibility that the user asks for a goto or branch, but the C++ compiler recognizes it as a recursive call.

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In this case the compiler also requires the return type of the function being defined since our continuation machines use auto deduction.

Finally, there is still the possibility that the user asks for a goto or branch, but the C++ compiler recognizes it as a recursive call.

In this case the compiler also requires the return type of the function being defined since our continuation machines use auto deduction. As we did not explicitly provide that information, the C++ compiler will then halt with its own error message.

Entailment

This metacompiler paradigm has now been properly introduced.

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There are several consequences worth discussing,

This metacompiler paradigm has now been properly introduced

There are several consequences worth discussing, but as this talk winds down I will instead leave you with what I hope is a thought provoking idea.

It is safe to say that C++ has problems as of late:



It is safe to say that C++ has problems as of late: ABI.

It is safe to say that C++ has problems as of late: ABI. Safety.

It is safe to say that C++ has problems as of late: ABI. Safety. Successor Languages.

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C++ has also become so successful that it now has an oversaturated grammar space.

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C++ has also become so successful that it now has an oversaturated grammar space. This metacompiler paradigm, with its DSL engine, can help mitigate these problems.

Foundations are all about design,



Foundations are all about design, and after spending time on programming language design,

Foundations are all about design, and after spending time on programming language design, I'm willing to say math has things to learn from software engineering, but that software engineering also has a few things it can learn from pure math. Math,

See Algebraic Topology, Algebraic Geometry, Analytic Combinatorics, etc.

Math, like computing,

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The reason for this is that math has already found ways to mitigate its consistency problems.

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Math, like computing, has many domain specific languages. It's not so concerned with performance, but it doesn't have interoperability concerns between languages either.

The reason for this is that math has already found ways to mitigate its consistency problems. It chooses to seek out foundational languages (such as Set Theory) to implement all other languages.

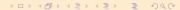
See Algebraic Topology, Algebraic Geometry, Analytic Combinatorics, etc.

The fact that C++ can effectively model all other programming languages means it is a foundational language of computing.

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Any C++ successor language should directly support this metaprogramming paradigm.

Why?



Why?

If it's truly a successor lang, it will eventually have the same grammar oversaturation problem. Why?

If it's truly a successor lang, it will eventually have the same grammar oversaturation problem.

Oversaturation comes from many communities using the language, each with their own overlapping but distinct domains of interest.

Such a lang can certainly still mitigate safety concerns with type checkers and borrow checkers,

Such a lang can certainly still mitigate safety concerns with type checkers and borrow checkers, but it can also mitigate safety with well designed and standardized DSLs,

Such a lang can certainly still mitigate safety concerns with type checkers and borrow checkers, but it can also mitigate safety with well designed and standardized DSLs, especially if it already provides that support.

End

(thank you)

Questions?

example: array square (map)

```
main out in end
vars:
  declare arr_sq
defs:
  arr_sq # map[1]{square||} [) [,)
body:
                                     ,
  . = arr_sq !out in end
  return
, binding( "square" , _square_ )
```

example: dot product (fold)

```
main out in end in1
vars:
  declare dot_prod
defs:
  dot_prod # fold[2]{add * @|multiply||} <> [,)
body:
  . = dot_prod !out in end in1
  return
```

example: convolution (fold)

```
main out in end in1
vars:
  declare conv
defs:
  conv # fold[2]{add * @|multiply||} <> (-|+,]
body:
  . = conv !out end in in1
  return
```

example:

void effects (mutability):



example:

semidynamic typing (deferred type checking):



```
type T
main c n
body:
  test equal c _1_0i
  branch set_c_to_five ;
  c = increment n
  return c
set_c_to_five:
  c # 5:T
  return c
```

```
, binding("_1_0i", complex_number{1, 0})
```