The dimnum package

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Note: Prandtl number is redefined from the amsmath package.

1 Introduction

This package simplifies the calling of Dimensionless Numbers in math or text mode.

In Table 1 you can find all available Dimensionless Numbers.

2 Usage

A Dimensionless number is composed of four items:

- the command,
- the symbol,
- the name,
- its identifier.

You can call a Dimensionless Number in three distinct ways:

- by its symbol using the command (i.e. Ar Ar).
- by its name (short version) appending [s] to the command (i.e. \Bi[s] Biot).
- by its name and identifier (long version) appending [l] to the command (i.e. $\Kn[1]$ Knudsen number).

Symbol, short and long versions, all work in math or text mode without the need of further commands.

Besides the comprehensive list of included Dimensionless Numbers, this package also introduces a command to create new Dimensionless Numbers. Creating a Dimensionless Number is achieved by using

\newdimnum{\command}{symbol}{name}{identifier}

for example, to add the Morton number we write

\newdimnum{\Mo}{Mo}{Morton}{number}

The identifier can be left empty, such as in the case of Drag Coefficient

\newdimnum{Cd}{\ensuremath{C_d}}{Drag Coefficient}{}

in this example we also introduce an important command. When the Dimensionless Number symbol is always expressed in math mode – either by definition or the use of subscripts or superscripts – we add \ensuremath{} to encompass the symbol, ensuring a proper representation of the Dimensionless Number.

You can add your own Dimensionless Numbers to your projects. Requests and suggestions to increment Table 1 are accepted and encouraged.

Table 1: List of Dimensionless Numbers Available

Long Name	Symbol	Command
Abbe number	V	\Ab
Activity coefficient	γ	\AC
Albedo	α	\Al

Table 1 – continued from the previous page

Long Name	Symbol	Command
Archimedes number	Ar	\Ar
Arrhenius number	α	\Arr
Atomic weight	M	\AW
Atwood number	A	\At
Bagnold number	Ba	\Ba
Basic reproduction number	R_0	\Rz
Bejan number	Ве	\Be
Bingham number	$_{ m Bm}$	\Bm
Biot number	Bi	\Bi
Blake number	Bl	\B1
Blondeau number	B_k	\Blo
Bodenstein number	Bs	\Bs
Bond number	Во	\ Bo

Table 1 – continued from the previous page

Long Name	\mathbf{Symbol}	Command
Brinkman number	Br	\Br
Brownell-Katz number	N_{BK}	\BK
Capillary number	Ca	\Ca
Cauchy number	C	\Cau
Chandrasekhar number	Q	\Ch
Chilton-Colburn Heat J-factor	J_H	\Jh
Chilton-Colburn Mass J-factor	J_D	\Jd
Chilton-Colburn Momentum J-factor	J_{M}	\Jm
Coefficient of Determination	R^2	\CoD
Coefficient of Frication	C_f	\CoF
Coefficient of Kinetic Friction	μ_k	\CoK
Coefficient of Static Friction	μ_s	\CoS
Coefficient of Variation	$rac{\sigma}{\mu}$	\CoV

Table 1 – continued from the previous page

Long Name	Symbol	Command
Cohesion number	Coh	\Coh
Condensation number	Со	\Co
Courant-Friedrich-Levy number	C	\CFL
Dahmköhler number	Da	\Dah
Damping ratio	ζ	\Dr
Darcy friction factor	f_D	\fD
Darcy number	Da	\Dar
Dean number	De	\De
Deborah number	De	\Deb
Drag Coefficient	C_d	\Cd
Dukhin number	Du	\Du
Eckert number	Ec	\Ec
Ekman number	Ek	\Ek

Table 1 – continued from the previous page

Long Name	\mathbf{Symbol}	Command
Elasticity number	El	\Ela
Elenbass number	El	\E1
Eötvös number	Eo	\Eo
Ericksen number	Er	\Er
Euler number	Eu	\Eu
Excess Temperature coefficient	Θ_r	\ExT
Fanning friction factor	f	\fF
Fine-structure constant	α	\Fs
Föppl-von Kármán number	γ	\FvK
Fourier number	Fo	\Fo
Fresnel number	\mathbf{F}	\Fre
Froude number	Fr	\Fr
Görtier number	G	\Go

Table 1 – continued from the previous page

Long Name	Symbol	Command
Galilei number	Ga	\Ga
Graetz number	$_{ m Gz}$	\Gz
Grashof number	Gr	\Gr
Hagen number	$_{ m Hg}$	\Hg
Hatta number	На	\Ha
Havnes parameter	P_H	\Hav
Helmholtz number	Не	\He
Hodgson number	Н	\Но
Iribarren number	${\rm Ir}$	\Ir
Jakob number	$_{ m Ja}$	\Ja
Karlovitz number	Ka	\Ka
Keulegan-Carpenter number	K_C	\KC
Knudsen number	Kn	\Kn

Table 1 – continued from the previous page

Long Name	\mathbf{Symbol}	Command
Kutateladze number	Ku	\Ku
Laplace number	La	\La
Lewis number	Le	\Le
Lift Coefficient	C_L	\C1
Lockhart-Martinelli parameter	χ	\LM
Lundquist number	S	\Lu
Mach number	${ m Ma}$	\Ma
Marangoni number	${ m Mg}$	\Mg
Markstein number	\mathcal{M}	\Mar
Morton number	Mo	\Mo
Nusselt number	Nu	\Nus
Ohnesorge number	Oh	\0h
Péclet number	Pe	\Pe

Table 1 – continued from the previous page

Long Name	Symbol	Command
Peel number	N_P	\Peel
pH	рН	\рН
Pierce parameter	C	\Pie
Poisson's ratio	u	\Poi
Power factor	pf	\Pf
Power number	N_p	\Pn
Prandtl number	\Pr	\Pr
Pressure Coefficient	C_P	\Cp
Rayleigh number	Ra	\Ra
Refractive index	n	\Rfi
Reynolds number	Re	\Rey
Richardson number	Ri	\Ri
Rolling resistance coefficient	C_{rr}	\Crr

Table 1 – continued from the previous page

Long Name	Symbol	Command
Roshko number	Ro	\Ro
Rossby number	Ro	\Ros
Rouse number	P	\Rou
Schmidt number	Sc	\Sc
Sherwood number	Sh	\Sh
Shield's parameter	$ au_*$	\Shi
Sommerfield number	S	\So
Stanton number	St	\St
Stefan number	Ste	\Ste
Stokes number	Stk	\Stk
Strouhal number	Sr	\Sr
Stuart number	N	\Stu
Svelteness	Sv	\Sv

Table 1 – continued from the previous page

Long Name	Symbol	Command
Taylor number	Та	\Ta
Ursell number	U	\Ur
Vadasz number	Va	\Va
Van 't Hoff factor	i	\vtH
Wagner number	Wa	\Wa
Wallis parameter	<i>j</i> *	\Wal
Weaver flame speed number	Wea	\Wea
Weber number	We	\We
Weissenberg number	Wi	\Wei
Womersley number	α	\Wo
Zel'dovich number	eta	\Zd

3 Implementation

^{1 \}NeedsTeXFormat{LaTeX2e}

 $^{{\}small 2 \ \ \ \ \ } \\ 2 \ \ \ \ \ \ \\ ProvidesPackage{dimnum}}$

³ [2021/04/05 v1.0.1 Provides commands for Dimensionless numbers]

```
4 \RequirePackage{amsmath}
                                           5 \RequirePackage{xifthen}
                                          6 \let\Pr\relax
                                          7 \newif\ifstartedinmathmode
\newdimnum
                                          8 \newcommand{\newdimnum} [4] {%
                                          9 \expandafter\newcommand\csname #1\endcsname[1][]{%
                                        10 \ifthenelse{\equal{##1}{}}{%
                                       11 \relax\ifmmode\startedinmathmodetrue\else\startedinmathmodefalse\fi%
                                       12 \ifstartedinmathmode\operatorname{#2}\else#2\fi}{%
                                       13 \ifthenelse{\equal{##1}{s}}{\text{#3}}{%
                                       14 \ifthenelse{\equal{##1}{1}}{%
                                       15 \ifthenelse{\equal{#4}{}}{\text{#3}}{\text{#3 #4}}}{%
                                       16 \ifthenelse{\equal{#4}{}}{\text{#3}}{\text{#3}}}%
                                                                                        }%
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                                       18
                                                                          }%
                                                            }%
                                       19
                                       20 }
                                       21 \newdimnum{Ar}{Ar}{Archimedes}{number}
                                       22 \newdimnum{At}{A}{Atwood}{number}
                                       23 \newdimnum{Ba}{Ba}{Bagnold}{number}
                                       24 \newdimnum{Be}{Be}{Bejan}{number}
                                       25 \newdimnum{Bm}{Bm}{Bingham}{number}
                                       26 \newdimnum{Bi}{Bi}{Biot}{number}
                                       27 \newdimnum{Bl}{Bl}{Blake}{number}
                                       28 \newdimnum{Bs}{Bs}{Bodenstein}{number}
                                       29 \newdimnum{Bo}{Bo}{Bond}{number}
                                       30 \newdimnum{Br}{Br}{Brinkman}{number}
                                       31 \mbox{\newdimnum{BK}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\newdimnum{BK}}{\new
                                       32 \newdimnum{Ca}{Ca}{Capillary}{number}
                                       33 \newdimnum{Cau}{C}{Cauchy}{number}
                                       34 \mbox{ } \mbox{ 
                                       {\tt 35 \ \ lemmath \{C_f\} \} \{Coefficient \ of \ Frication\} \{\} }
                                       36 \newdimnum{Co}{Co}{Condensation}{number}
                                       37 \newdimnum{Dah}{Da}{Dahmköhler}{number}
                                       38 \newdimnum{Dar}{Da}{Darcy}{number}
                                       39 \newdimnum{De}{De}{Dean}{number}
                                       40 \newdimnum{Deb}{De}{Deborah}{number}
                                       41 \newdimnum{Cd}{\ensuremath{C_d}}{Drag Coefficient}{}
                                       42 \mbox{newdimnum{Du}{Du}{Dukhin}{number}}
                                       43 \newdimnum{Ec}{Ec}{Eckert}{number}
                                       44 \mbox{ } \mbox{Ek}{Ek}{Ekman}{number}
                                       45 \newdimnum{Ela}{El}{Elasticity}{number}
                                       46 \mbox{ } \mbox{El}{El}{Elenbass}{number}
                                       47 \newdimnum{Eo}{Eo}{Eötvös}{number}
                                       48 \newdimnum{Er}{Er}{Ericksen}{number}
                                       49 \newdimnum{Eu}{Eu}{Euler}{number}
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50 \newdimnum{Fo}{Fo}{Fourier}{number}

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51 \newdimnum{Fr}{Fr}{Froude}{number}
52 \newdimnum{Ga}{Ga}{Galilei}{number}
53 \newdimnum{Go}{G}{Görtier}{number}
54 \newdimnum{Gz}{Gz}{Graetz}{number}
55 \newdimnum{Gr}{Gr}{Grashof}{number}
56 \newdimnum{Ha}{Ha}{Hatta}{number}
57 \newdimnum{Hg}{Hg}{Hagen}{number}
58 \newdimnum{Ho}{H}{Hodgson}{number}
59 \mbox{ $$\normalfootnote{1}{Ir}{Ir}{Iribarren}{number}$}
60 \newdimnum{Ja}{Ja}{Jakob}{number}
61 \newdimnum{Ka}{Ka}{Karlovitz}{number}
62 \newdimnum{KC}{\ensuremath{K_C}}{Keulegan-Carpenter}{number}
63 \newdimnum{Kn}{Kn}{Knudsen}{number}
64 \mbox{ }\mbox{Ku}{Ku}{Kutateladze}{number}
65 \newdimnum{La}{La}{Laplace}{number}
66 \newdimnum{Le}{Le}{Lewis}{number}
67 \newdimnum{Ma}{Ma}{Mach}{number}
68 \newdimnum{Mg}{Mg}{Marangoni}{number}
69 \newdimnum{Mo}{Mo}{Morton}{number}
70 \newdimnum{Nus}{Nu}{Nusselt}{number}
71 \newdimnum{Oh}{Oh}{Ohnesorge}{number}
72 \newdimnum{Pe}{Pe}{Péclet}{number}
74 \newdimnum{Po}{Po}{Poiseuille}{constant}
75 \newdimnum{Pr}{Pr}{Prandtl}{number}
76 \newdimnum{Ra}{Ra}{Rayleigh}{number}
77 \newdimnum{Rey}{Re}{Reynolds}{number}
78 \newdimnum{Ri}{Ri}{Richardson}{number}
79 \newdimnum{Ro}{Ro}{Roshko}{number}
80 \newdimnum{Ros}{Ro}{Rossby}{number}
81 \newdimnum{Rou}{P}{Rouse}{number}
82 \newdimnum{Sc}{Sc}{Schmidt}{number}
83 \newdimnum{Sh}{Sh}{Sherwood}{number}
84 \newdimnum{So}{S}{Sommerfield}{number}
85 \newdimnum{St}{St}{Stanton}{number}
86 \newdimnum{Ste}{Ste}{Stefan}{number}
87 \newdimnum{Stk}{Stk}{Stokes}{number}
88 \newdimnum{Sr}{Sr}{Strouhal}{number}
89 \newdimnum{Stu}{N}{Stuart}{number}
90 \newdimnum{Sv}{Sv}{Svelteness}{}
91 \newdimnum{Ta}{Ta}{Taylor}{number}
92 \newdimnum{Ur}{U}{Ursell}{number}
93 \newdimnum{Va}{Va}{Vadasz}{number}
94 \newdimnum{Wa}{Wa}{Wagner}{number}
95 \newdimnum{Wea}{Wea}{Weaver flame speed}{number}
96 \newdimnum{We}{We}{Weber}{number}
97 \newdimnum{Wei}{Wi}{Weissenberg}{number}
98 \newdimnum{Ab}{\ensuremath{V}}{Abbe}{number}
99 \newdimnum{AC}{\ensuremath{\gamma}}{Activity}{coefficient}
100 \newdimnum{Al}{\ensuremath{\alpha}}{Albedo}{}
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101 \newdimnum{Arr}{\ensuremath{\alpha}}{Arrhenius}{number}
102 \newdimnum{AW}{\ensuremath{M}}}{Atomic}{weight}
103 \mbox{\newdimnum}\{Rz\}{\newdimnum}\{Rz\}\{\newdimnum}\{Rz\}\}
104 \newdimnum{Blo}{\ensuremath{B_k}}{Blondeau}{number}
105 \newdimnum{Jm}{\ensuremath{J_M}}{Chilton-Colburn Momentum J-factor}{}
106 \mbox{ $\newdimnum{Jh}{\ensuremath{J_H}}{Chilton-Colburn Heat J-factor}{}} \label{eq:chilton-colburn}
108 \mbox{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coop}{\coo
109 \newdimnum{CoK}{\ensuremath{\mu_k}}{Coefficient of Kinetic Friction}{}
110 \newdimnum{CoS}{\ensuremath{\mu_s}}{Coefficient of Static Friction}{}
111 \newdimnum{CoV}{\ensuremath{\frac{\sigma}{\mu}}}{Coefficient of Variation}{}
112 \newdimnum{Coh}{\ensuremath{{Coh}}}{Cohesion}{number}
113 \newdimnum{CFL}{\ensuremath{C}}{Courant-Friedrich-Levy}{number}
114 \newdimnum{Dr}{\ensuremath{\zeta}}{Damping}{ratio}
115 \newdimnum{fD}{\ensuremath{f_D}}{Darcy friction}{factor}
116 \newdimnum{ExT}{\ensuremath{\Theta_r}}{Excess Temperature}{coefficient}
117 \newdimnum{fF}{\ensuremath{f}}{Fanning friction}{factor}
118 \newdimnum{Fs}{\ensuremath{\alpha}}{Fine-structure constant}{}
119 \mbox{newdimnum{FvK}{\number}}
120 \newdimnum{Fre}{F}{Fresnel}{number}
121 \newdimnum{Hav}{\ensuremath{P_H}}{Havnes}{parameter}
122 \newdimnum{He}{He}{Helmholtz}{number}
123 \newdimnum{Cl}{\ensuremath{C_L}}{Lift Coefficient}{}
124 \newdimnum{LM}{\ensuremath{\chi}}{Lockhart-Martinelli}{parameter}
125 \newdimnum{Lu}{S}{Lundquist}{number}
126 \newdimnum{Mar}{\ensuremath{\mathcal{M}}}{Markstein}{number}
127 \newdimnum{Peel}{\ensuremath{N_P}}{Peel}{number}
128 \newdimnum{Pie}{\ensuremath{C}}{Pierce}{parameter}
129 \newdimnum{Poi}{\ensuremath{\nu}}{Poisson's}{ratio}
130 \newdimnum{Pf}{\ensuremath{{pf}}}}{Power}{factor}
131 \mbox{\newdimnum{Pn}{\nsuremath{N_p}}{\nower}{\number}}
132 \newdimnum{Cp}{\ensuremath{C_P}}{Pressure Coefficient}{}
133 \newdimnum{Rfi}{\ensuremath{n}}{Refractive index}{}
134 \newdimnum{Crr}{\ensuremath{C_{rr}}}{Rolling resistance}{coefficient}
135 \newdimnum{Shi}{\ensuremath{\tau_*}}{Shield's}{parameter}
136 \newdimnum{vtH}{\ensuremath{i}}{Van 't Hoff}{factor}
137 \newdimnum{Wal}{\ensuremath{j^*}}{Wallis}{parameter}
138 \newdimnum{Wo}{\ensuremath{\alpha}}{Womersley}{number}
139 \mbox{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\colored}{\col
140 \endinput
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