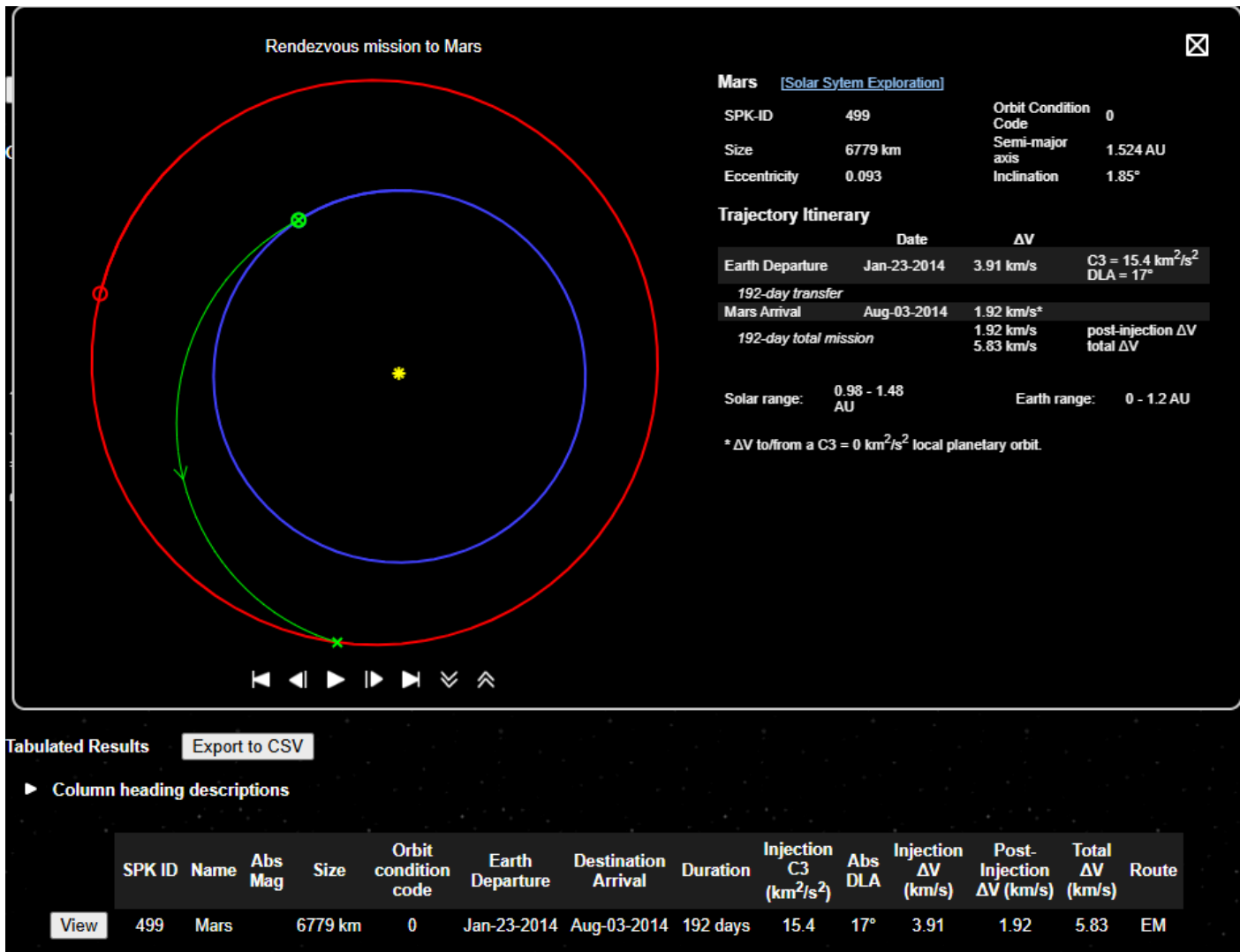


Part 1:



Part 1:

$$C_3 \text{ at departure: } (V_{inf} - 1)^2 \Rightarrow (4.0184)^2 = 16.1476$$

$$C_3 \text{ at arrival: } (V_{inf} - 2)^2 \Rightarrow (4.7639)^2 = 22.69$$

Calculating delta-v at earth:

$$V_{\infty} \text{ departure} = 4.0184 \text{ km/s}$$

$$N_{\text{earth}} = 398,600 \text{ km}^3/\text{s}^2$$

$$r_p = 6779 \text{ km}$$

$$V_p = \sqrt{(V_{\infty} \text{ departure})^2 + \frac{2 \cdot N_{\text{earth}}}{r_p}}$$

$$V_p = 11.5649$$

$$V_c = \sqrt{\frac{N_{\text{earth}}}{r_p}} \quad V_c = 7.66807$$

$$\Delta V_{\text{departure}} = V_p - V_c = 3.8968$$

Calculating delta-v at mars:

$$a = 227.9 \cdot 10^6 \text{ km}$$

$$r_p = 5.771 \cdot 10^5 \text{ km}$$

$$r_{\text{sof of mars:}} \quad 227.9 \cdot 10^6 \left( \frac{6.419 \cdot 10^{25}}{1.989 \cdot 10^{30}} \right)^{2/5} = 5.771 \cdot 10^5 \text{ km}$$

$$N = 42.830 \text{ km}^3/\text{s}^2 \quad V = 4.7639 \text{ km/s}$$

$$e = \frac{V^2}{2} - \frac{N}{r_p} = -\frac{N}{2a}$$

$$-\frac{1}{r} = \left( \frac{-N}{2a} - \frac{V^2}{2} \right) \cdot \frac{1}{N} \quad r = r_p = 3774 \text{ km} \quad \text{at arrival of hyperbola}$$

$$e_{\text{ellipse}} = 1 - \frac{r_p}{a_{\text{ellipse}}} \Rightarrow 1 - \frac{5.771 \cdot 10^5}{227.9 \cdot 10^6} = 0.99746$$

under mars sphere of influence

$$V_p \text{ arrival} = \sqrt{(V_{\infty} \text{ arrival})^2 + \frac{2 \cdot N_{\text{mars}}}{r}}$$

$$V_{\infty} \text{ arrival} = 4.7639 \text{ km/s}$$

$$= 6.737 \text{ km/s}$$

$$V_p \text{ ellipse} = \sqrt{\frac{N_{\text{mars}}}{r} (1 + e_{\text{ellipse}})}$$

$$= 4.76 \text{ km/s}$$

$$\Delta V_{\text{arrival}} = V_p \text{ arrival} - V_p \text{ ellipse} = 1.976 \text{ km/s}$$

$$\text{total } \Delta V: \Delta V_{\text{departure}} + \Delta V_{\text{arrival}} = 5.873 \text{ km/s}$$

### Example 8.8

Departure:

Planet: 3  
Year : 2014  
Month : 1  
Day : 3  
Hour : 0  
Minute: 0  
Second: 0

Julian day: 2456680.500

Planet position vector (km) = [-7.95404e+07 1.23908e+08 -3259.1]  
Magnitude = 1.47241e+08

Planet velocity (km/s) = [-25.5531 -16.204 0.000658356]  
Magnitude = 30.2578

Spacecraft velocity (km/s) = [-29.2794 -14.8606 -0.675751]  
Magnitude = 32.8417

v-infinity at departure (km/s) = [-3.72631 1.34348 -0.67641]  
Magnitude = 4.01843

vp)departure = 11.5649

vc)departure (circular parking orbit) = 7.66807

delta-v1 = 3.89681

Time of flight = 192 days

Arrival:

Planet: 4  
Year : 2014  
Month : 8  
Day : 3  
Hour : 0  
Minute: 0  
Second: 0

Julian day: 2456872.500

Planet position vector (km) = [-5.04776e+07 -2.16231e+08 -3.29122e+06]  
Magnitude = 1.47241e+08

Planet velocity (km/s) = [24.5112 -3.42719 -0.674036]  
Magnitude = 24.7588

Spacecraft Velocity (km/s) = [20.7883 -6.23805 0.292504]  
Magnitude = 21.7061

v-infinity at arrival (km/s) = [-3.72285 -2.81086 0.96654]  
Magnitude = 4.7639  
vp arrival = 6.73719  
vp ellipse = 4.76091  
delta-v2 = 1.97628  
total delta-v = 5.87309  
eccentricity of ellipse = 0.997468  
radius of periapsis at Mars = 3774.41  
semimajor axis at mars SOI = 2.279e+08  
radius of periapsis at Mars SOI = 577100

Orbital elements of flight trajectory:

Angular momentum (km<sup>2</sup>/s) = 4.81099e+09  
Eccentricity = 0.220102  
Right ascension of the ascending node (deg) = 302.636  
Inclination to the ecliptic (deg) = 1.18491  
Argument of perihelion (deg) = 147.01  
True anomaly at departure (deg) = 33.051  
True anomaly at arrival (deg) = 167.207  
  
Semimajor axis (km) = 1.83284e+08  
Characteristic energy at departure = 16.1478  
Period (days) = 495.331

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