

---

# **NumBAT Documentation**

***Release 0.1***

**Bjorn Sturmborg**

**Oct 28, 2016**



## CONTENTS

<b>1</b>	<b>Introduction</b>	<b>3</b>
1.1	Introduction . . . . .	3
<b>2</b>	<b>Installation</b>	<b>5</b>
2.1	Installation . . . . .	5
<b>3</b>	<b>Guide</b>	<b>9</b>
3.1	Simulation Structure . . . . .	9
3.2	Screen Sessions . . . . .	10
3.3	Basic SBS Gain Calculation . . . . .	12
<b>4</b>	<b>Python Backend</b>	<b>15</b>
4.1	objects module . . . . .	15
4.2	materials module . . . . .	17
4.3	mode_calcs module . . . . .	18
4.4	integration module . . . . .	19
4.5	plotting module . . . . .	20
<b>5</b>	<b>Fortran Backends</b>	<b>21</b>
5.1	2D FEM Mode Solver . . . . .	21
5.2	2D FEM Mode Solver . . . . .	22
<b>6</b>	<b>Indices and tables</b>	<b>23</b>
	<b>Python Module Index</b>	<b>25</b>
	<b>Index</b>	<b>27</b>



Contents:



## INTRODUCTION

## Introduction

EMUstack is an open-source simulation package for calculating light propagation through multi-layered stacks of dispersive, lossy, nanostructured, optical media. It implements a generalised scattering matrix method, which extends the physical intuition of thin film optics to complex structures.

At the heart of the scattering matrix approach is the requirement that each layer is uniform in one direction, here labelled  $z$ . In this nomenclature the incident field is unconstrained in  $k_{\parallel} = k_{x,y}$  but must have  $k_{\perp} = k_z \neq 0$ .

In-plane each layer can be homogeneous, periodic in  $x$  or  $y$ , or double periodic (periodic in  $x$  and  $y$ ). The modes of periodic (structured layers) are calculated using the Finite Element Method in respectively 1 or 2 dimensions, while the modes of homogeneous media are calculated analytically. This approach maximises the speed and accuracy of the calculations. These layers can be stacked in arbitrary order.

An advantage of EMUstack over other scattering matrix methods (for example [CAMFR](#)) is that the fields in each layer are considered in their natural basis with transmission scattering matrices converting fields between them. The fields in homogeneous layers are expressed in terms of plane waves, while the natural basis in the periodically structured layers are Bloch modes. Expressing fields in their natural basis gives the terms of the scattering matrices intuitive meaning, providing access to greater physical insights. It is also advantages for the speed and accuracy of the numerical method.

EMUstack has been designed to handle lossy media with dispersive refractive indices, with the complex refractive index at each frequency being taken directly from tabulated results of experimental measurements. This is an advantage of frequency domain methods over time domain methods such as the Finite Difference Time Domain (FDTD) where refractive indices are included by analytic approximations such as the Drude model. It is also possible to include media with lossless and/or non-dispersive refractive indices and EMUstack comes with a built in Drude model.

Taking full advantage of the boundary-element nature of the scattering matrix method it is possible to vary the thickness of a layer by a single, numerically inexpensive, matrix multiplication. Furthermore, EMUstack recognises when interfaces are repeated so that their scattering matrices need not be recalculated but rather just retrieved from memory, which takes practically no computation time.

EMUstack is a completely open source package, utilising free, open source compilers, meshing programs and libraries. All user interaction with EMUstack is done using the dynamic and easy to script language of python. The low-level numerical routines are written in Fortran for optimal performance making use of the LAPACK, ARPACK, and UMFPACK libraries. The Fortran routines are compiled as python subroutines using f2py. EMUstack currently comes with template FEM mesh for 1D and 2D gratings, Nanowire/Nanohole arrays, elliptical inclusions and split ring resonators. The mesh of other structures may be easily created using the open source program [gmsh](#).





## INSTALLATION

### Installation

The source code for NumBAT is hosted [here on Github](#). Please download the latest release from here.

NumBAT has been developed on Ubuntu and is easiest to install on this platform. Simply ‘sudo apt-get install’ the packages listed in the dependencies.txt file and then run setup.sh.

```
$ sudo apt-get update
$ sudo apt-get -y install <dependencies>
$ /setup.sh
```

UPDATE: the current version of SuiteSparse is not fully compatible with 64 bit Linux... a solution to this is to backport [SuiteSparse 3.4 from Ubuntu 12.04](#) using the method described [here](#). Alternatively the pre-compiled libraries have been shown to work on Ubuntu 14.04

On other linux distributions either use the pre-compiled libraries or install them from the package manager or manually.

All that is required to use the pre-compiled libraries is to switch to a slightly modified Makefile and then run setup.sh.

```
$ cd backend/fortran/
$ mv Makefile Makefile_ubuntu
$ mv Makefile-pre_compiled_libs Makefile
$ cd ../../
$ /setup.sh
```

The Fortran components (NumBAT source code and libraries) have been successfully compiled with intel’s ifortran as well as open-source gfortran. In this documentation we use gfortran.

NOTE: different versions of gmsh can give errors in the final test. This is okay, provided the test simulation ran, i.e. the test gives E rather than F.

### SuiteSparse

The FEM routine used in NumBAT makes use of the highly optimised [UMFPACK](#) (Unsymmetric MultiFrontal Package) direct solver for sparse matrices developed by Prof. Timothy A. Davis. This is distributed as part of the SuiteSparse libraries under a GPL license. It can be downloaded from <https://www.cise.ufl.edu/research/sparse/SuiteSparse/>

This is the process I followed in my installations. They are provided as little more than tips...

Unpack SuiteSparse into NumBAT/backend/fortran/, it should create a directory there; SuiteSparse/ Make a directory where you want SuiteSparse installed, in my case SS\_installed

```
$ mkdir SS_installed/
```

edit SuiteSparse/SuiteSparse\_config/SuiteSparse\_config.mk for consistency across the whole build; i.e. if using intel fortran compiler

```
line 75 F77 = gfortran --> ifort
```

set path to install folder:

```
line 85 INSTALL_LIB = /$Path_to_EMustack/NumBAT/backend/fortran/SS_install/lib
line 86 INSTALL_INCLUDE = /$Path_to_EMustack/NumBAT/backend/fortran/SS_install/include
```

line 290ish commenting out all other references to these:

```
F77 = ifort
CC = icc
BLAS = -L/apps/intel-ct/12.1.9.293/mkl/lib/intel64 -lmkl_rt
LAPACK = -L/apps/intel-ct/12.1.9.293/mkl/lib/intel64 -lmkl_rt
```

Now make new directories for the paths you gave 2 steps back:

```
$ mkdir SS_installed/lib SS_installed/include
```

Download [metis-4.0](#) and unpack metis into SuiteSparse/ Now move to the metis directory:

```
$ cd SuiteSparse/metis-4.0
```

Optionally edit metis-4.0/Makefile.in as per SuiteSparse/README.txt plus with -fPIC:

```
CC = gcc
or
CC = icc
OPTFLAGS = -O3 -fPIC
```

Now make metis (still in SuiteSparse/metis-4.0/):

```
$ make
```

Now move back to NumBAT/backend/fortran/

```
$ cp SuiteSparse/metis-4.0/libmetis.a SS_install/lib/
```

and then move to SuiteSparse/ and execute the following:

```
$ make library
$ make install
$ cd SuiteSparse/UMFPACK/Demo
$ make fortran64
$ cp SuiteSparse/UMFPACK/Demo/umf4_f77wrapper64.o into SS_install/lib/
```

Copy the libraries into NumBAT/backend/fortran/Lib/ so that NumBAT/ is a complete package that can be moved across machine without alteration. This will override the pre-compiled libraries from the release (you may wish to save these somewhere).:

```
$ cp SS_install/lib/*.a NumBAT/backend/fortran/Lib/
$ cp SS_install/lib/umf4_f77wrapper64.o NumBAT/backend/fortran/Lib/
```

## NumBAT Makefile

Edit NumBAT/backend/fortran/Makefile to reflect what compiler you are using and how you installed the libraries. The Makefile has further details.

Then finally run the setup.sh script!



## Simulation Structure

Simulations with NumBAT are generally carried out using a python script file. This file is kept in its own directory which is placed in the NumBAT directory. All results of the simulation are automatically created within this directory. This directory then serves as a complete record of the calculation. Often, we will also save the simulation objects (scattering matrices, propagation constants etc.) within this folder for future inspection, manipulation, plotting, etc.

Traditionally the name of the python script file begins with simo-. This is convenient for setting terminal alias' for running the script. Throughout the tutorial the script file will be called simo.py.

To start a simulation open a terminal and change into the directory containing the simo.py file. To run this script:

```
$ python simo.py
```

To have direct access to the simulation objects upon the completion of the script use,:

```
$ python -i simo.py
```

This will return you into an interactive python session in which all simulation objects are accessible. In this session you can access the docstrings of objects, classes and methods. For example:

```
>>> from pydoc import help
>>> help(objects.Light)
```

where we have accessed the docstring of the Light class from objects.py

In the remainder of this chapter we go through a number of example simo.py files.

Another tip to mention before diving into the examples is running simulations within screen sessions, which allow you to disconnect from servers leaving them to continue your processes.

## Screen Sessions

```
screen
```

is an extremely useful little linux command. In the context of long-ish calculations it has two important applications; ensuring your calculation is unaffected if your connection to a remote machine breaks, and terminating calculations that have hung without closing the terminal. For more information see the manual:

```
$ man screen
```

or see online discussions [here](#), and [here](#).

The screen session or also called screen instance looks just like your regular terminal/putty, but you can disconnect from it (close putty, turn off your computer etc.) and later reconnect to the screen session and everything inside of this will have kept running. You can also reconnect to the session from a different computer via ssh.

## Basic Usage

To install screen:

```
$ sudo apt-get install screen
```

To open a new screen session:

```
$ screen
```

We can start a new calculation here:

```
$ cd NumBAT/examples/  
$ python simo_040-2D_array.py
```

We can then detach from the session (leaving everything in the screen running) by typing:

```
Ctrl +a  
Ctrl +d
```

We can now monitor the processes in that session:

```
$ top
```

Where we note the numerous running python processes that NumBAT has started. Watching the number of processes is useful for checking if a long simulation is near completion (which is indicated by the number of processes dropping to less than the specified `num_cores`).

We could now start another screen and run some more calculations in this terminal (or do anything else). If we want to access the first session we ‘reattach’ by typing:

```
Ctrl +a +r
```

Or entering the following into the terminal:

```
$ screen -r
```

If there are multiple sessions use:

```
$ screen -ls
```

to get a listing of the sessions and their ID numbers. To reattach to a particular screen, with ID 1221:

```
$ screen -r 1221
```

To terminate a screen from within type:

```
Ctrl+d
```

Or, taking the session ID from the previous example:

```
screen -X -S 1221 kill
```

## Terminating NumBAT simos

If a simulation hangs, we can kill all python instances upon the machine:

```
$ pkill python
```

If a calculation hangs from within a screen session one must first detach from that session then kill python, or if it affects multiple instances, you can kill screen. A more targeted way to kill processes is using their PID:

```
$ kill PID
```

Or if this does not suffice be a little more forceful:

```
$ kill -9 PID
```

The PID is found from one of two ways:

```
$ top  
$ ps -fe | grep username
```

## Basic SBS Gain Calculation

```
print "SBS_gain \n", SBS_gain[EM_ival1,EM_ival2,:]/alpha
import time
import datetime
import numpy as np
import sys
from multiprocessing import Pool
sys.path.append("../backend/")

import materials
import objects
import mode_calcs
import integration
import plotting
from fortran import NumBAT

# Naming conventions
# AC: acoustic
# EM: electromagnetic
# q_acoustic: acoustic wavenumber

# Geometric Parameters - all in nm.
wl_nm = 1550 # Wavelength of EM wave in vacuum.
# Unit cell must be large to ensure fields are zero at boundary.
unitcell_x = 2.5*1550
unitcell_y = unitcell_x
# Waveguide width (x direction).
inc_a_x = 314.7
# Waveguide height (y direction).
inc_a_y = 0.9*inc_a_x
# Shape of the waveguide could also be 'circular'.
inc_shape = 'rectangular'

# Optical Parameters
# Permittivity
eps = 12.25
# Number of electromagnetic modes to solve for.
num_EM_modes = 20
# Number of acoustic modes to solve for.
num_AC_modes = 20
# The first EM mode(s) for which to calculate interaction with AC modes.
# Can specify a mode number (zero has lowest propagation constant) or 'All'
EM_ival1=0
# The second EM mode(s) for which to calculate interaction with AC modes.
EM_ival2=EM_ival1
# The AC mode(s) for which to calculate interaction with EM modes.
AC_ival='All'

# Acoustic Parameters
# Density
s = 2330 # kg/m3
# Stiffness tensor components
c_11 = 165.7e9; c_12 = 63.9e9; c_44 = 79.6e9 # Pa
# Photoelastic tensor components
p_11 = -0.094; p_12 = 0.017; p_44 = -0.051
# Acoustic loss tensor components
eta_11 = 5.9e-3 ; eta_12 = 5.16e-3 ; eta_44 = 0.620e-3 # Pa
```



```

# Put acoustic parameters together for convenience.
inc_a_AC_props = [s, c_11, c_12, c_44, p_11, p_12, p_44,
                  eta_11, eta_12, eta_44]

# Use all specified parameters to create a waveguide object.
wguide = objects.Struct(unitcell_x, inc_a_x, unitcell_y, inc_a_y, inc_shape,
                        bkg_material=materials.Material(1.0 + 0.0j),
                        inc_a_material=materials.Material(np.sqrt(eps)),
                        loss=False, inc_a_AC=inc_a_AC_props,
                        lc_bkg=0.1, lc2=40.0, lc3=20.0)

# Calculate Electromagnetic Modes
sim_EM_wguide = wguide.calc_EM_modes(wl_nm, num_EM_modes)
# Print the wavevectors of EM modes.
print 'k_z of EM wave \n', sim_EM_wguide.Eig_value
# Plot the EM modes fields, important to specify this with EM_AC='EM'.
# Zoom in on the central region (of big unitcell) with xlim, ylim args.
plotting.plt_mode_fields(sim_EM_wguide, xlim=0.4, ylim=0.4, EM_AC='EM')

# Choose acoustic wavenumber to solve for
# Backward SBS
# AC mode couples EM modes on +ve to -ve lightline, hence factor 2.
q_acoustic = 2*np.real(sim_EM_wguide.Eig_value[0])
print 'AC wavenumber (1/m) \n', q_acoustic
# Forward (intramode) SBS
# EM modes on same lightline.
# q_acoustic = 0.0

# Calculate Acoustic Modes
sim_AC_wguide = wguide.calc_AC_modes(wl_nm, q_acoustic,
                                     num_AC_modes, EM_sim=sim_EM_wguide, shift_Hz=12e9)
# Print the frequencies of AC modes.
print 'Res freq of AC wave (GHz) \n', np.real(sim_AC_wguide.Eig_value)*1e-9
# Plot the AC modes fields, important to specify this with EM_AC='AC'.
# The AC modes are calculated on a subset of the full unitcell,
# which excludes vacuum regions, so no need to restrict area plotted.
plotting.plt_mode_fields(sim_AC_wguide, EM_AC='AC')

# Calculate interaction integrals
SBS_gain, Q_PE, Q_MB, alpha = integration.gain_and_qs(
    sim_EM_wguide, sim_AC_wguide, q_acoustic,
    EM_ival1=EM_ival1, EM_ival2=EM_ival2, AC_ival=AC_ival)
# Print the Backward SBS gain of the AC modes.
print "SBS_gain \n", SBS_gain[EM_ival1, EM_ival2, :]/alpha

```



## PYTHON BACKEND

## objects module

objects.py is a subroutine of NumBAT. It contains the Struct objects that represent the structure being simulated.

Copyright (C) 2016 Bjorn Sturmberg, Kokou Dossou, Christian Wolff.

**class** objects.**NumBAT**

Bases: object

```
class objects.Struct (unitcell_x,          inc_a_x,          unitcell_y=None,          inc_a_y=None,
                     inc_shape='rectangular',          slab_a_x=None,          slab_a_y=None,
                     slab_b_x=None,          slab_b_y=None,          coating_y=None,          inc_b_x=None,
                     inc_b_y=None,          two_inc_sep=None,          incs_y_offset=None,
                     bkg_material=<materials.Material object>, inc_a_material=<materials.Material
                     object>,          inc_b_material=<materials.Material object>,
                     slab_a_material=<materials.Material object>,
                     slab_a_bkg_material=<materials.Material object>,
                     slab_b_material=<materials.Material object>,
                     slab_b_bkg_material=<materials.Material object>,
                     coating_material=<materials.Material object>,          loss=True,          bkg_AC=None,
                     inc_a_AC=None,          slab_a_AC=None,          slab_a_bkg_AC=None,          slab_b_AC=None,
                     slab_b_bkg_AC=None,          make_mesh_now=True,          force_mesh=True,
                     mesh_file='NEED_FILE.mail', check_msh=False, lc_bkg=0.09, lc2=1.0, lc3=1.0,
                     lc4=1.0, lc5=1.0, lc6=1.0, plotting_fields=False, plot_real=1, plot_imag=0,
                     plot_abs=0, plot_field_conc=False)
```

Bases: object

Represents a structured layer.

**Parameters**

- **unitcell\_x** (*float*) – The horizontal period of the unit cell in nanometers.
- **inc\_a\_x** (*float*) – The horizontal diameter of the inclusion in nm.

**Keyword Arguments**

- **unitcell\_y** (*float*) – The vertical period of the unit cell in nanometers. If None, unitcell\_y = unitcell\_x.
- **inc\_a\_y** (*float*) – The vertical diameter of the inclusion in nm.
- **inc\_shape** (*str*) – Shape of inclusions that have template mesh, currently: 'circular', 'rectangular'. Rectangular is default.
- **slab\_a\_x** (*float*) – The horizontal diameter in nm of the slab directly below the inclusion.

- **slab\_a\_y** (*float*) – The vertical diameter in nm of the slab directly below the inclusion.
- **slab\_b\_x** (*float*) – The horizontal diameter in nm of the slab separated from the inclusion by slab\_a.
- **slab\_b\_y** (*float*) – The vertical diameter in nm of the slab separated from the inclusion by slab\_a.
- **two\_inc\_sep** (*float*) – Separation between edges of inclusions in nm.
- **incs\_y\_offset** (*float*) – Vertical offset between centers of inclusions in nm.
- **coating\_y** (*float*) – The thickness of any coating layer around the inclusion.
- **background** – A :Material: instance for the background medium.
- **inc\_a\_material** – A :Material: instance for the
- **inc\_b\_material** – A :Material: instance for the
- **slab\_a\_material** – A :Material: instance for the
- **slab\_a\_bkg\_material** – A :Material: instance for the
- **slab\_b\_material** – A :Material: instance for the
- **slab\_b\_bkg\_material** – A :Material: instance for the
- **coating\_material** – A :Material: instance for the
- **loss** (*bool*) – If False,  $\text{Im}(n) = 0$ , if True  $n$  as in :Material: instance.
- **make\_mesh\_now** (*bool*) – If True, program creates a FEM mesh with provided :NanoStruct: parameters. If False, must provide mesh\_file name of existing .mail that will be run despite :NanoStruct: parameters.
- **force\_mesh** (*bool*) – If True, a new mesh is created despite existence of mesh with same parameter. This is used to make mesh with equal period etc. but different lc refinement.
- **mesh\_file** (*str*) – If using a set pre-made mesh give its name including .mail if 2D\_array (eg. 600\_60.mail), or .txt if 1D\_array. It must be located in backend/fortran/msh/
- **lc\_bkg** (*float*) – Length constant of meshing of background medium (smaller = finer mesh)
- **lc2** (*float*) – factor by which lc\_bkg will be reduced on inclusion surfaces;  $\text{lc\_surface} = \text{lc\_bkg} / \text{lc2}$ .
- **lc3-6'** (*float*) – factor by which lc\_bkg will be reduced at center of inclusions.
- **plotting\_fields** (*bool*) – Unless set to true field data deleted. Also plots modes (ie. FEM solutions) in gmsh format. Plots  $\epsilon \cdot |\mathbf{E}|^2$  & choice of real/imag/abs of x,y,z components & field vectors. Fields are saved as gmsh files, but can be converted by running the .geo file found in Bloch\_fields/PNG/
- **plot\_real** (*bool*) – Choose to plot real part of modal fields.
- **plot\_imag** (*bool*) – Choose to plot imaginary part of modal fields.
- **plot\_abs** (*bool*) – Choose to plot absolute value of modal fields.

**calc\_AC\_modes** (*wl\_nm*, *q\_acoustic*, *num\_modes*, *shift\_Hz=None*, *EM\_sim=None*, *\*\*args*)

Run a simulation to find the Struct's acoustic modes.

#### Parameters

- **wl\_nm** (*float*) – Wavelength of AC wave in vacuum.
- **num\_modes** (*int*) – Number of AC modes to solve for.

**Keyword Arguments**

- **shift\_Hz** (*float*) – Guesstimated frequency of modes, will be origin of FEM search. NumBAT will make an educated guess if shift\_Hz=None. (Technically the shift and invert parameter).
- **EM\_sim** (– Simmo: object): Typically an acoustic simulation follows on from an optical one. Supply the EM :Simmo: object so the AC FEM mesh can be constructed from this. This is done by removing vacuum regions.

**Returns** Simmo: object

**calc\_EM\_modes** (*wl\_nm, num\_modes, shift\_Hz=None, \*\*args*)

Run a simulation to find the Struct's EM modes.

**Parameters**

- **wl\_nm** (*float*) – Wavelength of EM wave in vacuum.
- **num\_modes** (*int*) – Number of EM modes to solve for.

**Keyword Arguments** **shift\_Hz** (*float*) – Guesstimated frequency of modes, will be origin of FEM search. NumBAT will make an educated guess if shift\_Hz=None. (Technically the shift and invert parameter).

**Returns** Simmo: object

**make\_mesh** ()

Take the parameters specified in python and make a Gmsh FEM mesh. Creates a .geo and .msh file, then uses Fortran conv\_gmsh routine to convert .msh into .mail, which is used in NumBAT FEM routine.

**objects.dec\_float\_str** (*dec\_float*)

Convert float with decimal point into string with '\_' in place of '.'

## materials module

materials.py is a subroutine of NumBAT that defines Material objects, these represent dispersive lossy refractive indices and possess methods to interpolate  $n$  from tabulated data.

Copyright (C) 2016 Bjorn Sturmberg, Kokou Dossou

**class** materials.**Material** (*n*)

Bases: object

Represents a material with a refractive index  $n$ .

If the material is dispersive, the refractive index at a given wavelength is calculated by linear interpolation from the initially given data  $n$ . Materials may also have  $n$  calculated from a Drude model with input parameters.

**Parameters** **n** – Either a scalar refractive index, an array of values (*wavelength, n*), or (*wavelength, real(n), imag(n)*), or omega\_p, omega\_g, eps\_inf for Drude model.

Currently included materials are;

Semiconductors	Metals	Transparent oxides
Si_c	Au	TiO2
Si_a	Au_Palik	TiO2_anatase
SiO2	Ag	ITO
CuO	Ag_Palik	ZnO
Continued on next page		

Table 4.1 – continued from previous page

CdTe	Cu	SnO2
FeS2	Cu_Palik	FTO_Wenger
Zn3P2		FTO_Wengerk5
AlGaAs		
Al2O3		
Al2O3_PV		
GaAs		
InGaAs	<b>Drude</b>	<b>Other</b>
Si3N4	Au_drude	Air
MgF2		H2O
InP		Glass
InAs		Spiro
GaP		Spiro_nk
Ge		
AlN		
GaN		
MoO3		
ZnS		
AlN_PV		
		<b>Experimental incl.</b>
		CH3NH3PbI3
		Sb2S3
		Sb2S3_ANU2014
		Sb2S3_ANU2015
		GO_2014
		GO_2015
		rGO_2015
		SiON_Low
		SiON_High
		Low_Fe_Glass
		Perovskite_00
		Perovskite
		Perovskite_b2b
		Ge_Doped

**n** (*wl\_nm*)

Return n for the specified wavelength.

`materials.plot_n_data` (*data\_name*)

## mode\_calcs module

`mode_calcs.py` is a subroutine of NumBAT that contains methods to calculate the EM and Acoustic modes of a structure.

Copyright (C) 2016 Bjorn Sturmberg, Kokou Dossou

**class** `mode_calcs.NumBAT`

Bases: `object`

```
class mode_calcs.Simmo(structure, wl_nm, q_acoustic=None, num_modes=20, shift_Hz=None,
                        EM_sim=None)
```

Bases: object

Calculates the modes of a :Struc: object at a wavelength of wl\_nm.

```
calc_AC_modes()
```

Run a Fortran FEM calculation to find the acoustic modes.

Returns a :Simmo: object that now has these key values:

Eig\_value: a 1d array of Eigenvalues (frequencies) in [1/s]

**sol1: the associated Eigenvectors, ie. the fields, stored as** [field comp, node nu on element, Eig value, el nu]

```
calc_EM_modes()
```

Run a Fortran FEM calculation to find the optical modes.

Returns a :Simmo: object that now has these key values:

Eig\_value: a 1d array of Eigenvalues (propagation constants) in [1/m]

**sol1: the associated Eigenvectors, ie. the fields, stored as** [field comp, node nu on element, Eig value, el nu]

## integration module

mode\_calcs.py is a subroutine of NumBAT that contains methods to calculate the EM and Acoustic modes of a structure.

Copyright (C) 2016 Bjorn Sturmberg, Kokou Dossou

```
class integration.NumBAT
```

Bases: object

```
integration.gain_and_qs(sim_EM_wguide, sim_AC_wguide, q_acoustic, EM_ival1=0, EM_ival2=0,
                        AC_ival=0)
```

Calculate interaction integrals and SBS gain.

Implements Eqs. 33, 41, 45 of Wolff et al. PRA 92, 013836 (2015) doi/10.1103/PhysRevA.92.013836 These are for Q\_photoelastic, Q\_moving\_boundary, and the Acoustic loss “alpha” respectively.

### Parameters

- (*sim\_AC\_wguide*) – Simmo: object): Contains all info on EM modes
- (– Simmo: object): Contains all info on AC modes
- **q\_acoustic** (*float*) – Propagation constant of acoustic modes.

### Keyword Arguments

- **EM\_ival1** (*int/string*) – Specify mode number of EM mode 1 (pump mode) to calculate interactions for. Numbering is python index so runs from 0 to num\_EM\_modes-1, with 0 being fundamental mode (largest prop constant). Can also set to ‘All’ to include all modes.
- **EM\_ival2** (*int/string*) – Specify mode number of EM mode 2 (stokes mode) to calculate interactions for. Numbering is python index so runs from 0 to num\_EM\_modes-1, with 0 being fundamental mode (largest prop constant). Can also set to ‘All’ to include all modes.

- **AC\_ival** (*int/string*) – Specify mode number of AC mode to calculate interactions for. Numbering is python index so runs from 0 to num\_AC\_modes-1, with 0 being fundamental mode (largest prop constant). Can also set to ‘All’ to include all modes.

`integration.quad_triangle` (*nquad*)  
Implementation of quad\_triangle

Evalue les integrales elementaires des composantes convectives sur chaque triangle. on utilise ici la methode de hammer a seize points de gauss qui integre exactement des polynomes du huitieme degre.

Google Translate: Evaluates integrals elementary convective components on each triangle. here we use the method of a hammer sixteen points of gauss that integrates exactly the polynomials eighth degree.

Reference J. N. Lyness and D. Jespersen “Moderate Degree Symmetric Quadrature Rules for the Triangle” J. Inst. Math. Appl., 1975, 15(1), pp. 19-32 “J. Inst. Math. Appl.” is now Continued as “IMA J. Appl. Math.” J. Inst. Math. Appl. = Journal of the Institute of Mathematics and its Applications IMA J. Appl. Math. = IMA Journal of Applied Mathematics

`integration.symmetries` (*sim\_wguide, n\_points=10*)  
Plot EM mode fields.

**Parameters** `sim_wguide` – A :Struct: instance that has had calc\_modes calculated

**Keyword Arguments** `n_points` (*int*) – The number of points across unitcell to interpolate the field onto.

## plotting module

plotting.py is a subroutine of NumBAT that contains numerous plotting routines.

Copyright (C) 2016 Bjorn Sturmborg

`plotting.plot_msh` (*x\_arr, add\_name=''*)  
Plot EM mode fields.

**Parameters** `sim_wguide` – A :Struct: instance that has had calc\_modes calculated

**Keyword Arguments** `n_points` (*int*) – The number of points across unitcell to interpolate the field onto.

`plotting.plt_mode_fields` (*sim\_wguide, n\_points=500, quiver\_steps=50, xlim=None, ylim=None, EM\_AC='EM', pdf\_png='png', add\_name=''*)

Plot EM mode fields. NOTE: z component of EM field needs comes scaled by 1/(i beta), which must be reintroduced!

**Args:** `sim_wguide` : A :Struct: instance that has had calc\_modes calculated

**Keyword Args:** `n_points` (*int*): The number of points across unitcell to interpolate the field onto.

`xlim` (*float*): Limit plotted xrange to xlim:(1-xlim) of unitcell

`ylim` (*float*): Limit plotted yrange to ylim:(1-ylim) of unitcell

`plotting.zeros_int_str` (*zero\_int*)  
Convert integer into string with ‘0’ in place of ‘ ‘.



## FORTRAN BACKENDS

The intention of NumBAT is that the Fortran FEM routines are essentially black boxes. They are called from `mode_calcs.py` and return the modes (Eigenvalues) of a structured layer, as well as some matrices of overlap integrals that are then used to compute the scattering matrices.

There are however a few important things to know about the workings of these routines.

### 2D FEM Mode Solver

#### 2D Mesh

2D FEM mesh are created using the open source program [gmsh](#). In general they are created automatically by EMUs-tack using the templates files for each inclusion shape. These are stored in `backend/fortran/msh`. For an up to date list of templates see the ‘`inc_shape`’ entry in the NanoStruct docstring.

An advantage of using the FEM to calculate the modes of layers is that there is absolutely no constraints on the content of the unit cell. If you wish to create a different structure this can be done using `gmsh`, which is also used to view the mesh files (select files with the extension `.msh`).

Note that the area of the unit cell must always be unity! This has been assumed throughout the theoretical derivations.

#### FEM Errors

There are 2 errors that can be easily triggered within the Fortran FEM routines. These both cause them to simulation to abort and the terminal to be unresponsive (until you kill python or the screen session).

The first of these is

```
Error with _naupd, info_32 = -3
Check the documentation in _naupd.
Aborting...
```

Long story short, this indicates that the FEM mesh is too coarse for solutions for higher order Bloch modes (Eigenvalues) to converge. To see this run the simulation with `FEM_debug = 1` (in `mode_calcs.py`) and it will print the number of converged Eigenvalues `nconv != nval`. This error is easily fixed by increasing the mesh resolution. Decrease ‘`lc_bkg`’ and/or increase ‘`lc2`’ etc.

The second error is

```
Error with _naupd, info_32 = -8
Check the documentation in _naupd.
Aborting...
```

This is the opposite problem, when the mesh is so fine that the simulation is overloading the memory of the machine. More accurately the memory depends on the number of Eigenvalues being calculated as well as the number of FEM mesh points. The best solution to this is to increase 'lc\_bkg' and/or decrease 'lc2' etc.

## 2D FEM Mode Solver

### 2D Mesh

2D FEM mesh are created using the open source program [gmsh](#). In general they are created automatically by EMUs-tack using the templates files for each inclusion shape. These are stored in backend/fortran/msh. For an up to date list of templates see the 'inc\_shape' entry in the NanoStruct docstring.

An advantage of using the FEM to calculate the modes of layers is that there is absolutely no constraints on the content of the unit cell. If you wish to create a different structure this can be done using gmsh, which is also used to view the mesh files (select files with the extension .msh).

Note that the area of the unit cell must always be unity! This has been assumed throughout the theoretical derivations.

### FEM Errors

There are 2 errors that can be easily triggered within the Fortran FEM routines. These both cause them to simulation to abort and the terminal to be unresponsive (until you kill python or the screen session).

The first of these is

```
Error with _naupd, info_32 = -3
Check the documentation in _naupd.
Aborting...
```

Long story short, this indicates that the FEM mesh is too coarse for solutions for higher order Bloch modes (Eigenvalues) to converge. To see this run the simulation with FEM\_debug = 1 (in mode\_calcs.py) and it will print the number of converged Eigenvalues nconv != nval. This error is easily fixed by increasing the mesh resolution. Decrease 'lc\_bkg' and/or increase 'lc2' etc.

The second error is

```
Error with _naupd, info_32 = -8
Check the documentation in _naupd.
Aborting...
```

This is the opposite problem, when the mesh is so fine that the simulation is overloading the memory of the machine. More accurately the memory depends on the number of Eigenvalues being calculated as well as the number of FEM mesh points. The best solution to this is to increase 'lc\_bkg' and/or decrease 'lc2' etc.

## INDICES AND TABLES

- `genindex`
- `modindex`
- `search`



**i**

integration, [19](#)

**m**

materials, [17](#)

mode\_calcs, [18](#)

**o**

objects, [15](#)

**p**

plotting, [20](#)



**C**

calc\_AC\_modes() (mode\_calcs.Simmo method), 19  
 calc\_AC\_modes() (objects.Struct method), 16  
 calc\_EM\_modes() (mode\_calcs.Simmo method), 19  
 calc\_EM\_modes() (objects.Struct method), 17

**D**

dec\_float\_str() (in module objects), 17

**G**

gain\_and\_qs() (in module integration), 19

**I**

integration (module), 19

**M**

make\_mesh() (objects.Struct method), 17  
 Material (class in materials), 17  
 materials (module), 17  
 mode\_calcs (module), 18

**N**

n() (materials.Material method), 18  
 NumBAT (class in integration), 19  
 NumBAT (class in mode\_calcs), 18  
 NumBAT (class in objects), 15

**O**

objects (module), 15

**P**

plot\_msh() (in module plotting), 20  
 plot\_n\_data() (in module materials), 18  
 plotting (module), 20  
 plt\_mode\_fields() (in module plotting), 20

**Q**

quad\_triangle() (in module integration), 20

**S**

Simmo (class in mode\_calcs), 18

Struct (class in objects), 15

symmetries() (in module integration), 20

**Z**

zeros\_int\_str() (in module plotting), 20