# **NumBAT Documentation**

Release 0.1

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### INTRODUCTION

### Introduction

EMUstack is an open-source simulation package for calculating light propagation through multi-layered stacks of dispersive, lossy, nanostructured, optical media. It implements a generalised scattering matrix method, which extends the physical intuition of thin film optics to complex structures.

At the heart of the scattering matrix approach is the requirement that each layer is uniform in one direction, here labelled z. In this nomenclature the incident field is unconstrained in  $k_{\parallel}=k_{x,y}$  but must have  $k_{\perp}=k_{z}\neq0$ .

In-plane each layer can be homogeneous, periodic in x or y, or double periodic (periodic in x and y). The modes of periodic (structured layers) are calculated using the Finite Element Method in respectively 1 or 2 dimensions, while the modes of homogeneous media are calculated analytically. This approach maximises the speed and accuracy of the calculations. These layers can be stacked in arbitrary order.

An advantage of EMUstack over other scattering matrix methods (for example CAMFR) is that the fields in each layer are considered in their natural basis with transmission scattering matrices converting fields between them. The fields in homogeneous layers are expressed in terms of plane waves, while the natural basis in the periodically structured layers are Bloch modes. Expressing fields in their natural basis gives the terms of the scattering matrices intuitive meaning, providing access to greater physical insights. It is also advantages for the speed and accuracy of the numerical method.

EMUstack has been designed to handle lossy media with dispersive refractive indices, with the complex refractive index at each frequency being taken directly from tabulated results of experimental measurements. This is an advantage of frequency domain methods over time domain methods such as the Finite Difference Time Domain (FDTD) where refractive indices are included by analytic approximations such as the Drude model. It is also possible to include media with lossless and/or non-dispersive refractive indices and EMUstack comes with a built in Drude model.

Taking full advantage of the boundary-element nature of the scattering matrix method it is possible to vary the thickness of a layer by a single, numerically inexpensive, matrix multiplication. Furthermore, EMUstack recognises when interfaces are repeated so that their scattering matrices need not be recalculated but rather just retrieved from memory, which takes practically no computation time.

EMUstack is a completely open source package, utilising free, open source compilers, meshing programs and libraries. All user interaction with EMUstack is done using the dynamic and easy to script language of python. The low-level numerical routines are written in Fortran for optimal performance making use of the LAPACK, ARPACK, and UMFPACK libraries. The Fortran routines are compiled as python subroutines using f2py. EMUstack currently comes with template FEM mesh for 1D and 2D gratings, Nanowire/Nanohole arrays, elliptical inclusions and split ring resonators. The mesh of other structures may be easily created using the open source program gmsh.

**TWO** 

### INSTALLATION

# Installation

The source code for NumBAT is hosted here on Github. Please download the latest release from here.

NumBAT has been developed on Ubuntu and is easiest to install on this platform. Simply 'sudo apt-get install' the packages listed in the dependencies.txt file and then run setup.sh.

```
$ sudo apt-get update
$ sudo apt-get -y install <dependencies>
$ /setup.sh
```

UPDATE: the current version of SuiteSparse is not fully compatible with 64 bit Linux... a solution to this is to backport SuiteSparse 3.4 from Ubuntu 12.04 using the method described here. Alternatively the pre-compiled libraries have been shown to work on Ubuntu 14.04

On other linux distributions either use the pre-compiled libraries of install them from the package manager or manually.

All that is required to use the pre-compiled libraries is to switch to a slightly modified Makefile and then run setup.sh.

```
$ cd backend/fortran/
$ mv Makefile Makefile_ubuntu
$ mv Makefile-pre_compiled_libs Makefile
$ cd ../../
$ /setup.sh
```

The Fortran components (NumBAT source code and libraries) have been successfully compiled with intel's ifortran as well as open-source gfortran. In this documentation we use gfortran.

NOTE: different versions of gmsh can give errors in the final test. This is okay, provided the test simulation ran, i.e. the test gives E rather than F.

# **SuiteSparse**

The FEM routine used in NumBAT makes use of the highly optimised UMFPACK (Unsymmetric MultiFrontal Package) direct solver for sparse matrices developed by Prof. Timothy A. Davis. This is distributed as part of the SuiteSparse libraries under a GPL license. It can be downloaded from https://www.cise.ufl.edu/research/sparse/SuiteSparse/

This is the process I followed in my installations. They are provided as little more than tips...

Unpack SuiteSparse into NumBAT/backend/fortran/, it should create a directory there; SuiteSparse/ Make a directory where you want SuiteSparse installed, in my case SS installed

```
$ mkdir SS_installed/
```

edit SuiteSparse/SuiteSparse\_config/SuiteSparse\_config.mk for consistency across the whole build; i.e. if using intel fortran compiler

```
line 75 F77 = gfortran --> ifort
```

set path to install folder:

```
line 85 INSTALL_LIB = /$Path_to_EMustack/NumBAT/backend/fortran/SS_install/lib
line 86 INSTALL_INCLUDE = /$Path_to_EMustack/NumBAT/backend/fortran/SS_install/include
```

line 290ish commenting out all other references to these:

```
F77 = ifort
CC = icc
BLAS = -L/apps/intel-ct/12.1.9.293/mkl/lib/intel64 -lmkl_rt
LAPACK = -L/apps/intel-ct/12.1.9.293/mkl/lib/intel64 -lmkl_rt
```

Now make new directories for the paths you gave 2 steps back:

```
$ mkdir SS_installed/lib SS_installed/include
```

Download metis-4.0 and unpack metis into SuiteSparse/ Now move to the metis directory:

```
$ cd SuiteSparse/metis-4.0
```

Optionally edit metis-4.0/Makefile.in as per SuiteSparse/README.txt plus with -fPIC:

```
CC = gcc
or
CC = icc
OPTFLAGS = -03 -fPIC
```

Now make metis (still in SuiteSparse/metis-4.0/):

```
$ make
```

Now move back to NumBAT/backend/fortran/

```
$ cp SuiteSparse/metis-4.0/libmetis.a SS_install/lib/
```

and then move to SuiteSparse/ and execute the following:

```
$ make library
$ make install
$ cd SuiteSparse/UMFPACK/Demo
$ make fortran64
$ cp SuiteSparse/UMFPACK/Demo/umf4_f77zwrapper64.o into SS_install/lib/
```

Copy the libraries into NumBAT/backend/fortran/Lib/ so that NumBAT/ is a complete package that can be moved across machine without alteration. This will override the pre-compiled libraries from the release (you may wish to save these somewhere).:

```
$ cp SS_install/lib/*.a NumBAT/backend/fortran/Lib/
$ cp SS_install/lib/umf4_f77zwrapper64.o NumBAT/backend/fortran/Lib/
```

# **NumBAT Makefile**

Edit NumBAT/backend/fortran/Makefile to reflect what compiler you are using and how you installed the libraries. The Makefile has further details.

Then finally run the setup.sh script!

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# **GUIDE**

# **Simulation Structure**

Simulations with NumBAT are generally carried out using a python script file. This file is kept in its own directory which is placed in the NumBAT directory. All results of the simulation are automatically created within this directory. This directory then serves as a complete record of the calculation. Often, we will also save the simulation objects (scattering matrices, propagation constants etc.) within this folder for future inspection, manipulation, plotting, etc.

Traditionally the name of the python script file begins with simo-. This is convenient for setting terminal alias' for running the script. Throughout the tutorial the script file will be called simo.py.

To start a simulation open a terminal and change into the directory containing the simo.py file. To run this script:

```
$ python simo.py
```

To have direct access to the simulation objects upon the completion of the script use,:

```
$ python -i simo.py
```

This will return you into an interactive python session in which all simulation objects are accessible. In this session you can access the docstrings of objects, classes and methods. For example:

```
>>> from pydoc import help
>>> help(objects.Light)
```

where we have accessed the docstring of the Light class from objects.py

In the remainder of this chapter we go through a number of example simo.py files.

Another tip to mention before diving into the examples is running simulations within screen seshions, which allow you to disconnect from servers leaving them to continue your processes.

# **Screen Sessions**

screen

is an extremely useful little linux command. In the context of long-ish calculations it has two important applications; ensuring your calculation is unaffected if your connection to a remote machine breaks, and terminating calculations that have hung without closing the terminal. For more information see the manual:

```
$ man screen
```

or see online discussions here, and here.

The screen session or also called screen instance looks just like your regular terminal/putty, but you can disconnect from it (close putty, turn off your computer etc.) and later reconnect to the screen session and everything inside of this will have kept running. You can also reconnect to the session from a different computer via ssh.

# **Basic Usage**

To install screen:

```
$ sudo apt-get install screen
```

To open a new screen session:

```
$ screen
```

We can start a new calculation here:

```
$ cd NumBAT/examples/
$ python simo_040-2D_array.py
```

We can then detach from the session (leaving everything in the screen running) by typing:

```
Ctrl +a
Ctrl +d
```

We can now monitor the processes in that session:

```
$ top
```

Where we note the numerous running python processes that NumBAT has started. Watching the number of processes is useful for checking if a long simulation is near completion (which is indicated by the number of processes dropping to less than the specified num\_cores).

We could now start another screen and run some more calculations in this terminal (or do anything else). If we want to access the first session we 'reattach' by typing:

```
Ctrl +a +r
```

Or entering the following into the terminal:

```
$ screen -r
```

If there are multiple sessions use:

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```
$ screen -ls
```

to get a listing of the sessions and their ID numbers. To reattach to a particular screen, with ID 1221:

```
$ screen -r 1221
```

To terminate a screen from within type:

```
Ctrl+d
```

Or, taking the session ID from the previous example:

```
screen -X -S 1221 kill
```

# **Terminating NumBAT simos**

If a simulation hangs, we can kill all python instances upon the machine:

```
$ pkill python
```

If a calculation hangs from within a screen session one must first detach from that session then kill python, or if it affects multiple instances, you can kill screen. A more targeted way to kill processes is using their PID:

```
$ kill PID
```

Or if this does not suffice be a little more forceful:

```
$ kill -9 PID
```

The PID is found from one of two ways:

```
$ top
$ ps -fe | grep username
```

3.2. Screen Sessions

# **Basic SBS Gain Calculation**

```
print "SBS_gain \n", SBS_gain[EM_ival1,EM_ival2,:]/alpha
import time
import datetime
import numpy as np
import sys
from multiprocessing import Pool
sys.path.append("../backend/")
import materials
import objects
import mode_calcs
import integration
import plotting
from fortran import NumBAT
# Naming conventions
# AC: acoustic
# EM: electromagnetic
# q_acoustic: acoustic wavenumber
# Geometric Parameters - all in nm.
wl_nm = 1550 # Wavelength of EM wave in vacuum.
# Unit cell must be large to ensure fields are zero at boundary.
unitcell_x = 2.5*1550
unitcell_y = unitcell_x
# Waveguide width (x direction).
inc_a_x = 314.7
# Waveguide height (y direction).
inc_a_y = 0.9 * inc_a_x
# Shape of the waveguide could also be 'circular'.
inc_shape = 'rectangular'
# Optical Parameters
# Permittivity
eps = 12.25
# Number of electromagnetic modes to solve for.
num\_EM\_modes = 20
# Number of acoustic modes to solve for.
num\_AC\_modes = 20
# The first EM mode(s) for which to calculate interaction with AC modes.
# Can specify a mode number (zero has lowest propagation constant) or 'All'
EM ival1=0
# The second EM mode(s) for which to calculate interaction with AC modes.
EM_ival2=EM_ival1
\# The AC mode(s) for which to calculate interaction with EM modes.
AC_ival='All'
# Acoustic Parameters
# Density
s = 2330 \# kg/m3
# Stiffness tensor components
c_11 = 165.7e9; c_12 = 63.9e9; c_44 = 79.6e9 # Pa
# Photoelastic tensor components
p_11 = -0.094; p_12 = 0.017; p_44 = -0.051
# Acoustic loss tensor components
eta_11 = 5.9e-3 ; eta_12 = 5.16e-3 ; eta_44 = 0.620e-3 # Pa
```

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```
# Put acoustic parameters together for convenience.
inc_a_AC_props = [s, c_11, c_12, c_44, p_11, p_12, p_44,
                  eta_11, eta_12, eta_44]
# Use all specified parameters to create a wavequide object.
wguide = objects.Struct(unitcell_x,inc_a_x,unitcell_y,inc_a_y,inc_shape,
                        bkg_material=materials.Material(1.0 + 0.0j),
                        inc_a_material=materials.Material(np.sqrt(eps)),
                        loss=False, inc_a_AC=inc_a_AC_props,
                        lc_bkg=0.1, lc2=40.0, lc3=20.0)
# Calculate Electromagnetic Modes
sim_EM_wguide = wguide.calc_EM_modes(wl_nm, num_EM_modes)
# Print the wavevectors of EM modes.
print 'k_z of EM wave \n', sim_EM_wguide.Eig_value
# Plot the EM modes fields, important to specify this with EM_AC='EM'.
# Zoom in on the central region (of big unitcell) with xlim, ylim args.
plotting.plt_mode_fields(sim_EM_wguide, xlim=0.4, ylim=0.4, EM_AC='EM')
# Choose acoustic wavenumber to solve for
# Backward SBS
# AC mode couples EM modes on +ve to -ve lightline, hence factor 2.
q_acoustic = 2*np.real(sim_EM_wguide.Eig_value[0])
print 'AC wavenumber (1/m) \ n', q_acoustic
# Forward (intramode) SBS
# EM modes on same lightline.
\# q_acoustic = 0.0
# Calculate Acoustic Modes
sim_AC_wguide = wguide.calc_AC_modes(wl_nm, q_acoustic,
   num_AC_modes, EM_sim=sim_EM_wguide, shift_Hz=12e9)
# Print the frequencies of AC modes.
print 'Res freq of AC wave (GHz) \n', np.real(sim_AC_wguide.Eig_value) *1e-9
# Plot the AC modes fields, important to specify this with EM_AC='AC'.
# The AC modes are calculated on a subset of the full unitcell,
# which excludes vacuum regions, so no need to restrict area plotted.
plotting.plt_mode_fields(sim_AC_wguide, EM_AC='AC')
# Calculate interaction integrals
SBS_gain, Q_PE, Q_MB, alpha = integration.gain_and_qs(
    sim_EM_wguide, sim_AC_wguide, q_acoustic,
   EM_ival1=EM_ival1, EM_ival2=EM_ival2, AC_ival=AC_ival)
# Print the Backward SBS gain of the AC modes.
print "SBS_gain \n", SBS_gain[EM_ival1,EM_ival2,:]/alpha
```

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# **PYTHON BACKEND**

# objects module

# materials module

materials.py is a subroutine of NumBAT that defines Material objects, these represent dispersive lossy refractive indices and possess methods to interpolate n from tabulated data.

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class materials.Material(n)

Bases: object

Represents a material with a refractive index n.

If the material is dispersive, the refractive index at a given wavelength is calculated by linear interpolation from the initially given data n. Materials may also have n calculated from a Drude model with input parameters.

**Parameters**  $\mathbf{n}$  – Either a scalar refractive index, an array of values (*wavelength*, n), or (*wavelength*, real(n), imag(n)), or omega\_p, omega\_g, eps\_inf for Drude model.

Currently included materials are;

Semiconductors	Metals	Transparent oxides
Si_c	Au	TiO2
Si_a	Au_Palik	TiO2_anatase
SiO2	Ag	ITO
CuO	Ag_Palik	ZnO
CdTe	Cu	SnO2
FeS2	Cu_Palik	FTO_Wenger
Zn3P2		FTO_Wengerk5
AlGaAs		
Al2O3		
Al2O3_PV		
GaAs		
InGaAs	Drude	Other
Si3N4	Au_drude	Air
MgF2		H2O
InP		Glass
InAs		Spiro
GaP		Spiro_nk
	Con	tinued on next page

Ge         AIN           GaN         MoO3           ZnS         Experimental incl.           AIN_PV         Experimental incl.           CH3NH3PbI3         Sb2S3           Sb2S3_ANU2014         Sb2S3_ANU2015           GO_2014         GO_2015           rGO_2015         rGO_2015           SiON_Low         SiON_High           Low_Fe_Glass         Perovskite_00           Perovskite         Perovskite_b2b           Ge_Doped         Ge_Doped	rable 4.1 – continued from previous page		
GaN   MoO3   ZnS   AlN_PV   Experimental incl.   CH3NH3PbI3   Sb2S3   Sb2S3_ANU2014   Sb2S3_ANU2015   GO_2014   GO_2015   rGO_2015   SiON_Low   SiON_High   Low_Fe_Glass   Perovskite_00   Perovskite_b2b	Ge		
MoO3   ZnS	AlN		
ZnS AlN_PV  Experimental incl. CH3NH3PbI3 Sb2S3 Sb2S3_ANU2014 Sb2S3_ANU2015 GO_2014 GO_2015 rGO_2015 rGO_2015 SiON_Low SiON_High Low_Fe_Glass Perovskite_00 Perovskite Perovskite_b2b	GaN		
AIN_PV  Experimental incl.  CH3NH3PbI3  Sb2S3  Sb2S3_ANU2014  Sb2S3_ANU2015  GO_2014  GO_2015  rGO_2015  rGO_2015  siON_Low  SiON_High  Low_Fe_Glass  Perovskite_00  Perovskite  Perovskite_b2b	MoO3		
Experimental incl.   CH3NH3PbI3   Sb2S3   Sb2S3_ANU2014   Sb2S3_ANU2015   GO_2014   GO_2015   rGO_2015   SiON_Low   SiON_High   Low_Fe_Glass   Perovskite_00   Perovskite_b2b	ZnS		
CH3NH3PbI3 Sb2S3 Sb2S3_ANU2014 Sb2S3_ANU2015 GO_2014 GO_2015 rGO_2015 SiON_Low SiON_High Low_Fe_Glass Perovskite_00 Perovskite Perovskite_b2b	AlN_PV		
Sb2S3   Sb2S3_ANU2014   Sb2S3_ANU2014   Sb2S3_ANU2015   GO_2014   GO_2015   rGO_2015   SiON_Low   SiON_High   Low_Fe_Glass   Perovskite_00   Perovskite   Perovskite_b2b		Experimental incl.	
Sb2S3_ANU2014   Sb2S3_ANU2015   GO_2014   GO_2015   rGO_2015   SiON_Low   SiON_High   Low_Fe_Glass   Perovskite_00   Perovskite		CH3NH3PbI3	
Sb2S3_ANU2015   GO_2014   GO_2015   rGO_2015   SiON_Low   SiON_High   Low_Fe_Glass   Perovskite_00   Perovskite		Sb2S3	
GO_2014 GO_2015 GO_2015 rGO_2015 SiON_Low SiON_High Low_Fe_Glass Perovskite_00 Perovskite Perovskite_b2b		Sb2S3_ANU2014	
GO_2015 rGO_2015 SiON_Low SiON_High Low_Fe_Glass Perovskite_00 Perovskite Perovskite_b2b		Sb2S3_ANU2015	
rGO_2015 SiON_Low SiON_High Low_Fe_Glass Perovskite_00 Perovskite Perovskite_b2b		GO_2014	
SiON_Low SiON_High Low_Fe_Glass Perovskite_00 Perovskite Perovskite_b2b		GO_2015	
SiON_High Low_Fe_Glass Perovskite_00 Perovskite Perovskite_b2b		rGO_2015	
Low_Fe_Glass Perovskite_00 Perovskite Perovskite_b2b		SiON_Low	
Perovskite_00 Perovskite Perovskite_b2b		SiON_High	
Perovskite Perovskite_b2b		Low_Fe_Glass	
Perovskite_b2b		Perovskite_00	
		Perovskite	
Ge_Doped		Perovskite_b2b	
		Ge_Doped	

Table 4.1 – continued from previous page

 $\mathbf{n}$  (wl nm)

Return n for the specified wavelength.

materials.plot\_n\_data(data\_name)

# mode calcs module

mode\_calcs.py is a subroutine of NumBAT that contains methods to calculate the EM and Acoustic modes of a structure.

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class mode\_calcs.NumBAT

Bases: object

Bases: object

Calculates the modes of a :Struc: object at a wavelength of wl\_nm.

calc\_AC\_modes()

Run a Fortran FEM calculation to find the acoustic modes.

Returns a :Simmo: object that now has these key values:

Eig\_value: a 1d array of Eigenvalues (frequencies) in [1/s]

sol1: the associated Eigenvectors, ie. the fields, stored as [field comp, node nu on element, Eig value, el nu]

calc\_EM\_modes()

Run a Fortran FEM calculation to find the optical modes.

Returns a :Simmo: object that now has these key values:

Eig\_value: a 1d array of Eigenvalues (propagation constants) in [1/m]

sol1: the associated Eigenvectors, ie. the fields, stored as [field comp, node nu on element, Eig value, el nu]

# integration module

mode\_calcs.py is a subroutine of NumBAT that contains methods to calculate the EM and Acoustic modes of a structure

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class integration.NumBAT

Bases: object

integration.gain\_and\_qs ( $sim\_EM\_wguide$ ,  $sim\_AC\_wguide$ ,  $q\_acoustic$ ,  $EM\_ival1=0$ ,  $EM\_ival2=0$ ,  $AC\_ival=0$ )

Calculate interaction integrals and SBS gain.

Implements Eqs. 33, 41, 45 of Wolff et al. PRA 92, 013836 (2015) doi/10.1103/PhysRevA.92.013836 These are for Q\_photoelastic, Q\_moving\_boundary, and the Acoustic loss "alpha" respectively.

#### **Parameters**

- ((sim\_AC\_wguide) Simmo: object): Contains all info on EM modes
- ( Simmo: object): Contains all info on AC modes
- q\_acoustic (float) Propagation constant of acoustic modes.

#### **Keyword Arguments**

- **EM\_ival1** (*int/string*) Specify mode number of EM mode 1 (pump mode) to calculate interactions for. Numbering is python index so runs from 0 to num\_EM\_modes-1, with 0 being fundamental mode (largest prop constant). Can also set to 'All' to include all modes.
- EM\_ival2 (int/string) Specify mode number of EM mode 2 (stokes mode) to calculate interactions for. Numbering is python index so runs from 0 to num\_EM\_modes-1, with 0 being fundamental mode (largest prop constant). Can also set to 'All' to include all modes.
- AC\_ival (int/string) Specify mode number of AC mode to calculate interactions for. Numbering is python index so runs from 0 to num\_AC\_modes-1, with 0 being fundamental mode (largest prop constant). Can also set to 'All' to include all modes.

integration.quad\_triangle(nquad)

Implementation of quad\_triangle

Evalue les integrales elementaires des composantes convectives sur chaque triangle. on utilise ici la methode de hammer a seize points de gauss qui integre exactement des polynomes du huitieme degre.

Google Translate: Evaluates integrals elementary convective components on each triangle. here we use the method of a hammer sixteen points of gauss that integrates exactly the polynomials eighth degree.

Reference J. N. Lyness and D. Jespersen "Moderate Degree Symmetric Quadrature Rules for the Triangle" J. Inst. Math. Appl., 1975, 15(1), pp. 19-32 "J. Inst. Math. Appl." is now Continued as "IMA J. Appl. Math." J. Inst. Math. Appl. = Journal of the Institute of Mathematics and its Applications IMA J. Appl. Math. = IMA Journal of Applied Mathematics

```
integration.symmetries (sim_wguide, n_points=10)
Plot EM mode fields.
```

**Parameters** sim\_wguide - A :Struct: instance that has had calc\_modes calculated

**Keyword Arguments n\_points** (*int*) – The number of points across unitcell to interpolate the field onto.

# plotting module

plotting.py is a subroutine of NumBAT that contains numerous plotting routines.

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```
plotting.plot_msh(x_arr, add_name='')
Plot EM mode fields.
```

**Parameters** sim\_wguide - A :Struct: instance that has had calc\_modes calculated

**Keyword Arguments n\_points** (*int*) – The number of points across unitcell to interpolate the field onto.

```
plotting.plt_mode_fields (sim_wguide, n_points=500, quiver_steps=50, xlim=None, ylim=None, EM AC='EM', pdf png='png', add name='')
```

Plot EM mode fields. NOTE: z component of EM field needs comes scaled by 1/(i beta), which must be reintroduced!

**Args:** sim\_wguide : A :Struct: instance that has had calc\_modes calculated

**Keyword Args:** n\_points (int): The number of points across unitcell to interpolate the field onto.

xlim (float): Limit plotted xrange to xlim:(1-xlim) of unitcell

ylim (float): Limit plotted yrange to ylim:(1-ylim) of unitcell

```
plotting.zeros_int_str(zero_int)
```

Convert integer into string with '0' in place of ' '.

**FIVE** 

### FORTRAN BACKENDS

The intention of NumBAT is that the Fortran FEM routines are essentially black boxes. They are called from mode\_calcs.py and return the modes (Eigenvalues) of a structured layer, as well as some matrices of overlap integrals that are then used to compute the scattering matrices.

There are however a few important things to know about the workings of these routines.

### 2D FEM Mode Solver

#### 2D Mesh

2D FEM mesh are created using the open source program gmsh. In general they are created automatically by EMUstack using the templates files for each inclusion shape. These are stored in backend/fortran/msh. For an up to date list of templates see the 'inc\_shape' entry in the NanoStruct docstring.

An advantage of using the FEM to calculate the modes of layers is that there is absolutely no constraints on the content of the unit cell. If you wish to create a different structure this can be done using gmsh, which is also used to view the mesh files (select files with the extension .msh).

Note that the area of the unit cell must always be unity! This has been assumed throughout the theoretical derivations.

#### **FEM Errors**

There are 2 errors that can be easily triggered within the Fortran FEM routines. These both cause them to simulation to abort and the terminal to be unresponsive (until you kill python or the screen session).

The first of these is

```
Error with _naupd, info_32 = -3
Check the documentation in _naupd.
Aborting...
```

Long story short, this indicates that the FEM mesh is too coarse for solutions for higher order Bloch modes (Eigenvaules) to converge. To see this run the simulation with FEM\_debug = 1 (in mode\_calcs.py) and it will print the number of converged Eigenvalues nconv!= nval. This error is easily fixed by increasing the mesh resolution. Decrease 'lc\_bkg' and/or increase 'lc2' etc.

The second error is

```
Error with _naupd, info_32 = -8
Check the documentation in _naupd.
Aborting...
```

This is the opposite problem, when the mesh is so fine that the simulation is overloading the memory of the machine. More accurately the memory depends on the number of Eigenvalues being calculated as well as the number of FEM mesh points. The best solution to this is to increase 'lc\_bkg' and/or decrease 'lc2' etc.

## 2D FEM Mode Solver

### 2D Mesh

2D FEM mesh are created using the open source program gmsh. In general they are created automatically by EMUstack using the templates files for each inclusion shape. These are stored in backend/fortran/msh. For an up to date list of templates see the 'inc shape' entry in the NanoStruct docstring.

An advantage of using the FEM to calculate the modes of layers is that there is absolutely no constraints on the content of the unit cell. If you wish to create a different structure this can be done using gmsh, which is also used to view the mesh files (select files with the extension .msh).

Note that the area of the unit cell must always be unity! This has been assumed throughout the theoretical derivations.

#### **FEM Errors**

There are 2 errors that can be easily triggered within the Fortran FEM routines. These both cause them to simulation to abort and the terminal to be unresponsive (until you kill python or the screen session).

The first of these is

```
Error with _naupd, info_32 = -3
Check the documentation in _naupd.
Aborting...
```

Long story short, this indicates that the FEM mesh is too coarse for solutions for higher order Bloch modes (Eigenvaules) to converge. To see this run the simulation with FEM\_debug = 1 (in mode\_calcs.py) and it will print the number of converged Eigenvalues nconv!= nval. This error is easily fixed by increasing the mesh resolution. Decrease 'lc\_bkg' and/or increase 'lc2' etc.

The second error is

```
Error with _naupd, info_32 = -8
Check the documentation in _naupd.
Aborting...
```

This is the opposite problem, when the mesh is so fine that the simulation is overloading the memory of the machine. More accurately the memory depends on the number of Eigenvalues being calculated as well as the number of FEM mesh points. The best solution to this is to increase 'lc\_bkg' and/or decrease 'lc2' etc.

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