$$\sqrt{\frac{N^2 \left(\left(N^4 \, q^2 + 2 \, N^2 \, q^5 \right) + q^8 \right)}{N^4 \, q^2}}$$

$$N = \sqrt{\frac{N^2 ((N^4 q^2 + 2 N^2 q^5) + q^8)}{N^4 q^2}}$$

N = N_guess

q is the smallest Prime factor

Plug in guess q to get an N_guess that equals the given N.

test N = 85, q = 5.

In[9]:=
$$N = 85$$

$$q=5$$

$$\sqrt{\frac{N^2 \left(\left(N^4 \, q^2 + 2 \, N^2 \, q^5 \right) + q^8 \right)}{N^4 \, q^2}}$$

Set::wrsym : Symbol N is Protected. \gg

Out[9]= 85

Out[10]= 5

Out[11]=
$$\frac{1}{5} \sqrt{\frac{390 625 + 6250 N^2 + 25 N^4}{N^2}}$$

$$\ln[13] := Simplify \left[\sqrt{\frac{N^2 \left(\left(N^4 \ q^2 + 2 \ N^2 \ q^5 \right) + q^8 \right)}{N^4 \ q^2}} \right]$$

$$\sqrt{\frac{\left(125+N^2\right)^2}{N^2}}$$

85 = approximate
$$\sqrt{\frac{\left(125+N^2\right)^2}{N^2}}$$