Integral Daily Challenge (@thecuriousmind22)

Shreenabh Agrawal

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1 Question

If

$$\int_{e}^{x} t f(t) dt = \sin x - x \cos x - \frac{x^{2}}{2},$$

Find $f(\pi/6)$.

2 Solution

By applying Leibniz Integral Rule,

$$xf(x) = \cos x - \cos x + x \sin x - x$$

$$f(x) = \sin x - 1$$

$$f\left(\frac{\pi}{6}\right) = \frac{1}{2} - 1$$

$$f\left(\frac{\pi}{6}\right) = -\frac{1}{2}$$