

What is Recursion?

- Any function or method which calls itself is called recursion. A recursive method solves a problem by calling a copy of itself to work on a smaller problem. This is called the recursive step.
- The recursion step can result in many more such recursive calls.
- It is important to ensure that the recursion terminates at some point.
- Each time the function calls itself with a slightly simpler version of the original problem.
- The sequence of a smaller problems must eventually converge on the base case.

Why Recursion?

- Recursion is a useful technique borrowed from mathematics. Recursion code is generally shorter and easier to write than iterative code.
- Generally, loops are turned into recursive function when they are compiled and interpreted.
- Recursion is most useful for tasks that can be defined in terms of similar subtasks.
- For example: sort, search, and traversal problems often have simple recursive solutions.

Before, going deeper into recursion. Let's first discuss about functions.

- In almost all the programming languages, there is a built-in data structure that manages what happens when functions or methods are invoked. Generally, it's called as call stack or method stack.
- It's a **Stack** data structure. Any time a function is invoked it is placed (**pushed**) on the top of the call stack.

- When a method/function sees the return keyword or when the function ends, the compiler will remove (**pop**)

Two essential parts of a recursive function!

- Base Case
- Recursive Case

```
public static void countDown(int num) {
    if(num <= 0) {
        return;
    }
    System.out.println(num);
    countDown(--num);
}
```

Diagram illustrating the two essential parts of a recursive function:

- Base Case:** The condition `if(num <= 0) { return; }` is highlighted with a red box and labeled "Base Case".
- Recursive Case:** The recursive call `countDown(--num);` is highlighted with a red box and labeled "Recursive Case".

Format of a Recursive Function

- A recursive function performs a task in part by calling itself to perform the subtasks.
- At some point, the function encounters a subtask that it can perform without calling itself. This case where the function **does not recur** is called as **Base Case**.
- The former, where the function calls itself to perform a subtask, is referred to as the **Recursive Case**.

if(test for the base case)

return some base case value;

else if(test for another base case)

return some other base case value;

//the recursive case

else return(some work and then recursive call);

Calculate factorial of a positive integer?

```
public static int factorial(int n) {
    if(n == 1) {
        return 1;
    }
    return n * factorial(--n);
}
```

Recursion vs Iteration

A recursive approach makes it simpler to solve a problem, which may not have the most obvious of answers. But, recursion adds overhead for each recursive call (needs **space on the stack frame**).

<u>Recursion</u>	<u>Iteration</u>
Terminates when a base case is reached	Terminates when a condition is proven to be false
Each recursive call required extra space on the stack frame (memory)	Each iteration does not require any extra space
If we get infinite recursion, the program may run out of memory and give stack overflow	An infinite loop could run forever since there is no extra memory being created.
Solutions to some problems are easier to formulate recursively.	Iterative solutions to a problem may not always be as obvious as a recursive solution.

Notes on Recursion:

- Recursive algorithms have two types of cases: **base case** and **recursive case**.
- Every recursive function case must terminate at base case.
- Generally iterative solutions are more efficient than recursive solutions. Due to the overhead of function calls in recursion.

- A recursive algorithm can be implemented without recursive function calls using a stack. But, it's generally more trouble than its worth. That means any problem that can be solved recursively can also be solved iteratively.
- For some problems, there are no obvious iterative algorithms.
- Some problems are best suited for recursive solutions while others are not.

Example Algorithms of Recursion:

- Fibonacci Series, Factorial Finding
- Merge Sort, Quick Sort
- Binary Search
- Tree Traversal and many Tree Problems: InOrder, PreOrder, PostOrder
- Graph Traversal: DFS [Depth First Search] and BFS [Breadth First Search]
- Dynamic Programming Examples
- Divide and Conquer Algorithms
- Towers of Hanoi
- Backtracking algorithms

Examples of Recursion:

Example 1:

```
//recursion pattern
public static List<Integer> findOdds(List<Integer> arr) {
    ArrayList<Integer> oddList = new ArrayList<Integer>();
    oddReccur(arr, oddList);
    return oddList;
}
public static void oddReccur(List<Integer> list, List<Integer> res) {
    if(list.size() <= 0) {
        return;
    }
    if( (list.get(list.size()-1) % 2) != 0 ){
        res.add(list.get(list.size()-1));
    }
    int index = (int)list.size()-1;
    list.remove(index);
    oddReccur(list, res);
}
```

Example 2:

```
public static int sumRange(int n) {
    if(n == 1) {
        return 1;
    }
    return n + sumRange(--n);
}

public static int factorial(int n) {
    if(n == 1) {
        return 1;
    }
    return n * factorial(--n);
}

public static void countDown(int num) {
    if(num <= 0) {
        return;
    }
    System.out.println(num);
    countDown(--num);
}
```

```
public static long powerOf(long num, long power) {  
    if(power != 0) {  
        return num * powerOf(num, --power);  
    } else {  
        return 1;  
    }  
}
```