



# Chapter 3

## Single-Stage Amplifiers

中科大

微电子学院

教材：拉扎维《模拟CMOS集成电路设计》



# contents

- Four types of amplifiers (MOSFET, 小信号输入输出公共端):
  - Common-source topology
  - Common-gate topology
  - Source followers
  - Cascode(共源共栅) configuration
- Large-signal characteristics
- Small-signal characteristics (Low frequency behavior)



## 3.1 basic concepts

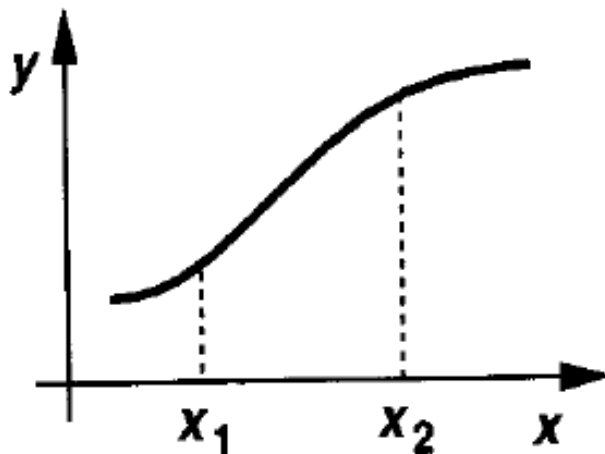
- The input-output characteristic of an amplifier:

$$y(t) = a_0 + a_1 x(t) + a_2 x^2(t) + \cdots + a_n x^n(t), \quad x_1 \leq x \leq x_2$$

- So long as  $x(t)$  is small enough, reasonable approximation

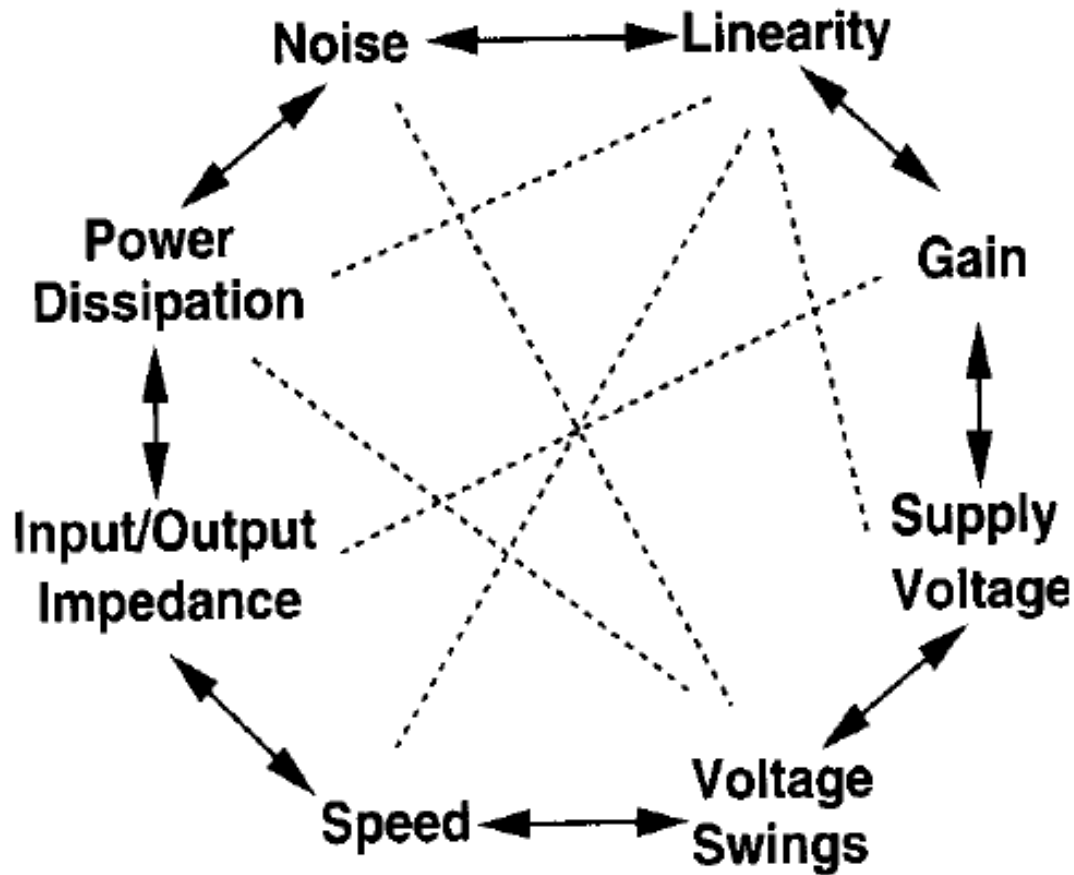
$$y(t) \approx a_0 + a_1 x(t)$$

- when  $a_1 x(t) \ll a_0$  the bias point (偏置点  $a_0$ ) is disturbed negligibly. (受到的扰动忽略不计)。





# Analog circuits design octagon

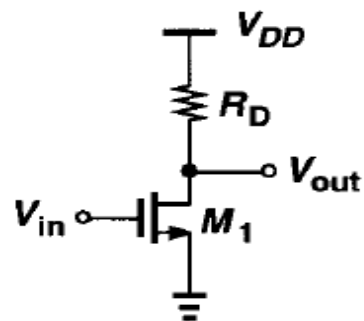


**trade-off ( compromise)**

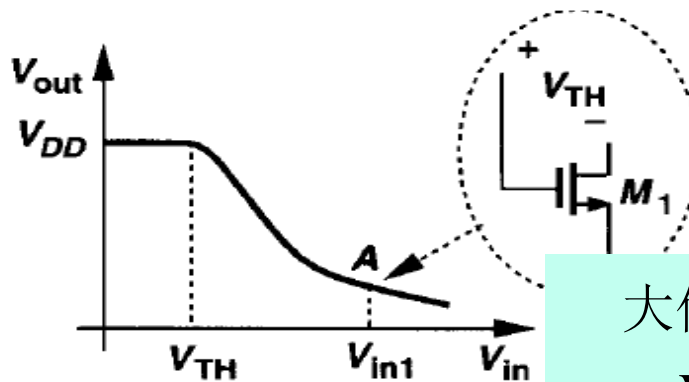


## 3.2 Common-source (CS) Stage

### • 3.2.1 Common-source stage with resistive load



(a)

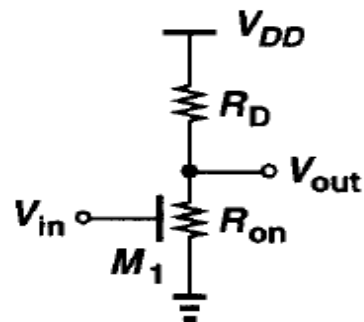


(b)

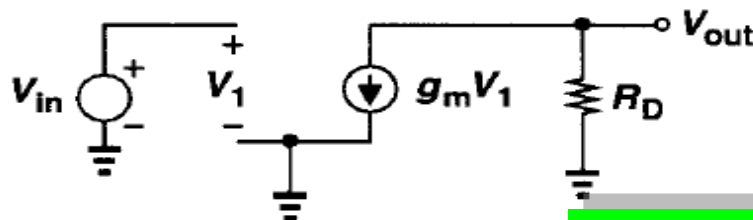
大信号（包括直流）

$$V_{in} - V_{TH} > V_{out}$$

triode region:  $V_{in} > V_{in1}$



(c)



(d)

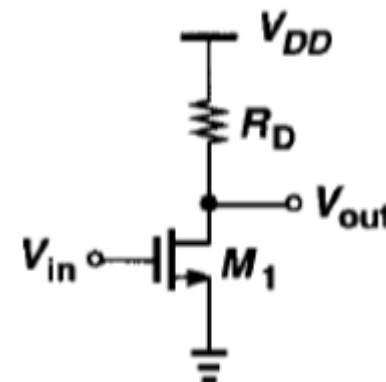
小信号：交变，无直流  
忽略寄生电容，仅限低频

**Figure 3.3** (a) Common-source stage, (b) input-output characteristic, (c) equivalent circuit in deep triode region, (d) small-signal model for the saturation region.



# 1.采用大信号分析方法：IV公式推导

- By virtue of(借助) trans-conductance , MOSFET convert variations in its gate-source voltage to a small drain current.



In saturation region :  $V_{out} > V_{in} - V_{Th}$

$$V_{out} = V_{DD} - R_D I_{Dn} = V_{DD} - R_D \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{Th})^2$$

手算时忽略沟道长度调制效应,  $L' = L_{eff} = L_{drawn} - 2LD$   
( $LD$ =漏/源与栅极的交叠长度) .

Note that the input impedance of the circuit is very high **at low frequencies** .

仿真时 $R_D$ 可先用analogLib库中res, 然后用流片工艺库中电阻代替。



# 大信号分析方法(续)

A点(饱和区最小 $V_{DS}$ ) $V_{in1}$ , 输入信号的上限

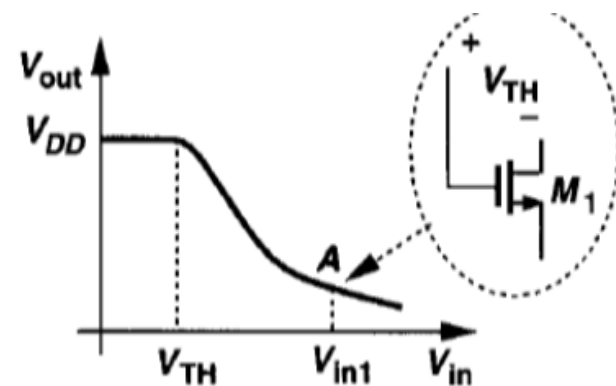
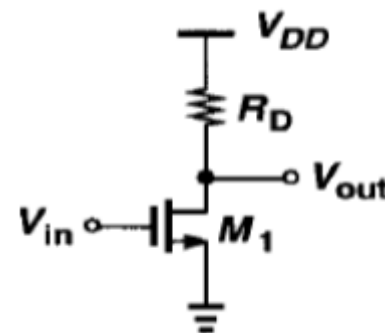
$$\begin{aligned} V_{out} &= V_{in1} - V_{Tn} = V_{DD} - R_D \frac{1}{2} \mu_n C_{OX} \frac{W}{L} (V_{in1} - V_{Tn})^2 \\ &= V_{DD} - R_D \frac{1}{2} \mu_n C_{OX} \frac{W}{L_{eff}} (V_{in1} - V_{Tn})^2 (1 + \lambda V_{DS}) \end{aligned}$$

解出  $V_{in1}$ 。手算时  $\lambda V_{DS} \approx 0$

In the triode region

$V_{in} > V_{in1}$ , 即  $V_{in} - V_{TH} > V_{out}$

$$\begin{aligned} V_{out} &= V_{DD} - R_D \times \mu_n C_{OX} \frac{W}{L_{eff}} \left[ (V_{in1} - V_{Tn}) V_{DS} - \frac{1}{2} V_{DS}^2 \right] \\ &= V_{DD} - R_D \times \frac{1}{2} \mu_n C_{OX} \frac{W}{L_{eff}} \left[ 2(V_{in1} - V_{Tn}) V_{out} - V_{out}^2 \right] \end{aligned}$$



三极管区仍能工作，  
但跨导小，且与 $V_{DS}$ 有关



# 得到small-signal gain of common source

$$V_{out} = V_{DD} - R_D \frac{1}{2} \mu_n C_{ox} \frac{W}{L_{eff}} (V_{in} - V_{Tn})^2 (1 + \lambda V_{DS})$$

$$A_v = \frac{\partial V_{out}}{\partial V_{in}} = -R_D \times \mu_n C_{ox} \frac{W}{L_{eff}} (V_{in} - V_{Tn}) (1 + \lambda V_{DS}) = -g_m R_D$$

$$\text{式中 } g_m = \frac{\partial I_D}{\partial V_{GS}} = \mu_n C_{ox} (W / L_{eff}) (V_{GS} - V_{Tn}) (1 + \lambda V_{DS})$$

The dependence of the gain upon the signal level leads to nonlinearity

基本概念：（1）放大倍数（增益）仅是对交变信号，不包括直流部分（工作点）；

（2）CS负增益表示输入与输出中的交变信号反向；

（3）负载 $R_D$ 可泛指一切有源器件（含受控电压或电流源的器件，如MOS、三极管）和无源器件(RLC)。





# Example 3.1

Sketch the drain current and transconductance as a function of the input voltage.

Solution:

$$\text{饱和区 } I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L_{eff}} (V_{in} - V_{Th})^2 (1 + \lambda V_{out})$$

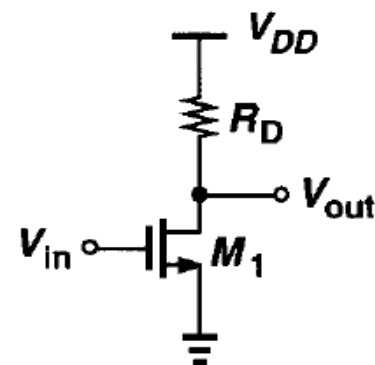
$$g_m = \frac{\partial I_D}{\partial V_{GS}} = \mu_n C_{ox} (W / L_{eff}) (V_{in} - V_{Th}) (1 + \lambda V_{out})$$

$$V_{in1} = V_{out} + V_{Th}$$

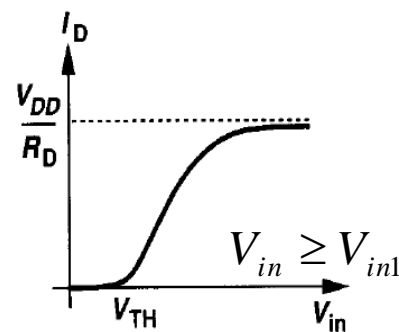
三极管（线性电阻）区：  $V_{out} < V_{in} - V_{Th}$

$$I_D = \mu_n C_{ox} \frac{W}{L_{eff}} \left[ (V_{in} - V_{Th}) V_{out} - \frac{1}{2} V_{out}^2 \right]$$

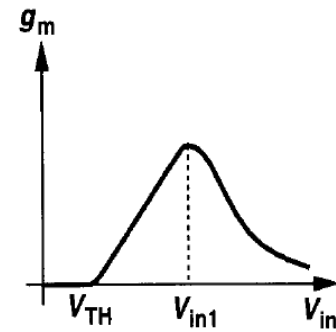
$$g_m = \frac{\partial I_D}{\partial V_{GS}} = \frac{\partial I_D}{\partial V_{in}} = \mu_n C_{ox} \frac{W}{L_{eff}} V_{out}$$



还须满足RD上的VI关系



(a)



(b)

Figure 3.4

$$A_v = \frac{\partial V_{out}}{\partial V_{in}} = -g_m R_D$$



# 沟道长度调制对增益的影响

$$V_{out} = V_{DD} - R_D \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH})^2 (1 + \lambda V_{out})$$

$$\begin{aligned} \frac{\partial V_{out}}{\partial V_{in}} = & -R_D \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH}) (1 + \lambda V_{out}) \\ & - R_D \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{TH})^2 \lambda \frac{\partial V_{out}}{\partial V_{in}}. \end{aligned}$$

$$I_D \approx (1/2) \mu_n C_{ox} (W/L) (V_{in} - V_{TH})^2$$

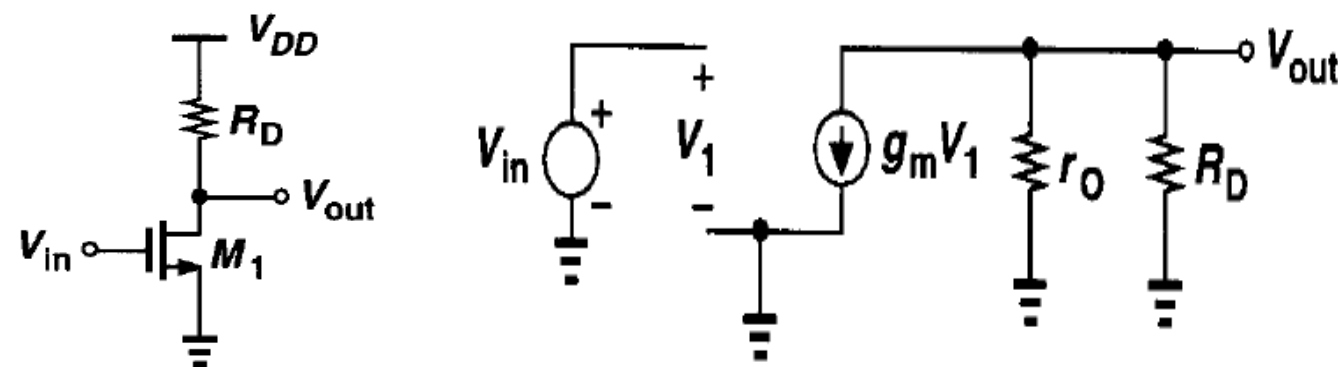
$$A_v = -R_D g_m - R_D I_D \lambda A_v \qquad A_v = -\frac{g_m R_D}{1 + R_D \lambda I_D}$$

$$\text{Since } \lambda I_D = 1/r_o \quad A_v = -\frac{g_m R_D}{1 + R_D \lambda I_D} = -g_m \frac{r_o R_D}{r_o + R_D} = -g_m (r_o \parallel R_D)$$

沟道长度调制效应( $r_o=r_{ds}$ )使得gain减小



## 2.采用交变小信号模型计算方法



$r_o$ 代表了沟道长度调制效应。如负载  $R_D$  较小(小于几K欧), 可忽略  $r_o$ 。

**Figure 3.5** Small-signal model of CS stage including the transistor output resistance.

$$g_m V_1 (r_o \parallel R_D) = -V_{out}$$

$$V_1 = V_{in}$$

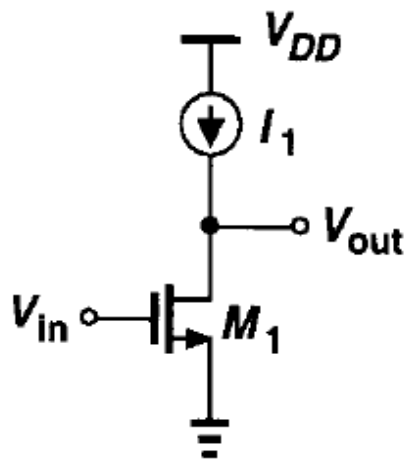
$$V_{out} / V_{in} = -g_m (r_o \parallel R_D)$$

采用小信号模型, 计算结果与大信号方法相同( $V_{in}$ 和 $V_{out}$ 是交变小信号)。

信号流分析可省略小信号模型。直观方法:  $M1$ 通过跨导 $g_m$ 将 $V_{in}$ 转换成漏极受控电流源变化, 该电流变化通过总输出阻抗转换成输出电压变化 $V_{out}$



# 本征增益 $g_m r_o$



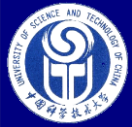
理想电流源具有无穷大输出阻抗。

$$\begin{aligned} I_{D1} &= \frac{1}{2} \mu_n C_{ox} (V_{in} - V_{TH})^2 (1 + \lambda V_{out}) \\ &= I_1, \end{aligned}$$

电压增益 $= -g_m r_o$

“intrinsic gain” represent the maximum voltage gain that can be achieved using a single device.

应 $g_m r_o \gg 1$ , thus usually  $1/g_m \ll r_o$

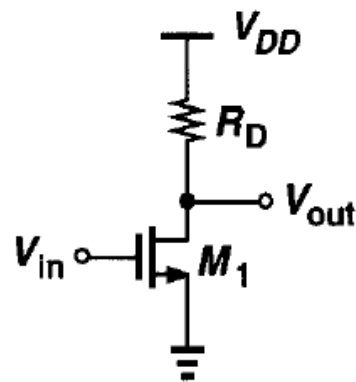


# 例:

已知:  $C_{ox} = 10 \times 10^{-7} \text{ F/cm}^2$ ,  $\mu_n = 300 \text{ cm}^2/(\text{V} \cdot \text{s})$ ,  $V_{Tn} = 0.5\text{V}$

$V_{DD} = 1.8\text{V}$ ,  $V_{in, DC} = 0.7\text{V}$ , 设  $\lambda_n = 0.1/V$ ,  $I_D = 100\mu\text{A}$ ,  $V_{out} = 1\text{V}$ ,

$0.5\mu\text{m}$  工艺漏 / 源与栅极交叠  $LD \approx 0.1\mu\text{m}$ , 计算  $\frac{W}{L_{eff}}$ ,  $R_D$ ,  $g_m r_o$ ,  $A_v$ .



解:  $I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L_{eff}} (V_{in} - V_{Tn})^2 (1 + \lambda V_{out})$ , 已知过驱动电压和电流可用此式得  $\frac{W}{L_{eff}}$

$$100 \times 10^{-6} \text{ A} = \frac{1}{2} \times 300 \text{ cm}^2/(\text{V} \cdot \text{s}) \times 10 \times 10^{-7} \text{ F/cm}^2 \times \frac{W}{L_{eff}} \times 0.2^2 \text{ V}^2 \times 1.1$$

得到:  $\frac{W}{L_{eff}} = \frac{100}{6.6} \approx \frac{4.5}{0.3}$ , 取  $L_{drawn} = 0.5\mu\text{m}$

$$R_D = \frac{V_{DD} - V_{out}}{I_D} = \frac{1.8\text{V} - 1\text{V}}{100 \times 10^{-6} \text{ A}} = 8\text{k}\Omega, \quad r_o = \frac{1}{\lambda I_D} = \frac{1}{0.1/V \times 100 \times 10^{-6} \text{ A}} = 100\text{k}\Omega$$

$$g_m = \mu_n C_{ox} (W / L_{eff}) (V_{in} - V_{Tn}) (1 + \lambda V_{out}) = 300 \times 10 \times 10^{-7} \times \frac{4.5}{0.3} \times 0.2 \times 1.1 \approx 1 \frac{\text{mA}}{\text{V}}$$

$$g_m r_o = 100, \quad A_v = -g_m (R_D || r_o) = -10^{-3} \times (8 || 100) \times 10^3 = -7.4$$



# 动态范围（大信号=直流+交变小信号）

饱和区  $V_{in,min}=V_{Tn}$ ,  $V_{out,max}=V_{DD}$

$$V_{in,max}=V_{out,min}+V_{Tn},$$

$$V_{out,min} = V_{DD} - R_D \frac{1}{2} \mu_n C_{OX} \frac{W}{L_{eff}} (V_{in,max} - V_{Tn})^2 (1 + \lambda V_{out,min})$$

$$\approx V_{DD} - R_D \frac{1}{2} \mu_n C_{OX} \frac{W}{L_{eff}} V_{out,min}^2, \quad (\because \lambda V_{out,min} \approx 0, V_{out} \geq V_{in,max} - V_{Tn})$$

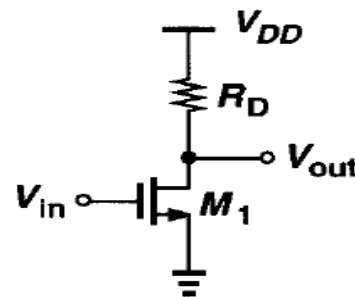
$$= 1.8V - 8 \times 10^3 \Omega \times \frac{1}{2} \times 300 \frac{cm^2}{(V \cdot s)} \times 10 \times 10^{-7} \frac{F}{cm^2} \times \frac{4.5}{0.3} \times V_{out,min}^2$$

$$= 1.8V - 18V_{out,min}^2 \times \Omega \cdot V \cdot \frac{F}{s} = 1.8V - 18V_{out,min}^2$$

$$(\because Q = CV = It, \text{故量纲 } FV = As, \therefore \Omega \cdot V \cdot \frac{F}{s} = \Omega A = V)$$

$$\text{得到: } V_{out,min} = \frac{-1 + \sqrt{1^2 - 4 \times 18 \times (-1.8)}}{2 \times 18} = \frac{10.43}{36} \approx 0.3V$$

$$V_{in,max} \approx V_{out,min} + V_{Tn} \approx 0.8V$$



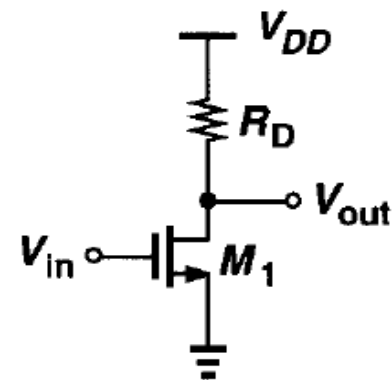


# 例：改变直流电流进行比较

已知：  $C_{ox} = 10 \times 10^{-7} \text{ F/cm}^2$ ,  $\mu_n = 300 \text{ cm}^2/(\text{V} \cdot \text{s})$ ,  $V_{Tn} = 0.5\text{V}$

$V_{DD} = 1.8\text{V}$ ,  $V_{in} = 0.7\text{V}$ , 设  $\lambda_n = 0.1/V$ , 改变  $I_D = 20\mu\text{A}$ ,  $V_{out} = 1\text{V}$ ,

采用  $0.5\mu\text{m}$  工艺  $L_D \approx 0.1\mu\text{m}$ , 重新计算  $\frac{W}{L_{eff}}$ ,  $R_D$ ,  $g_m r_o$ ,  $A_v$ .



$$\text{解: } I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L_{eff}} (V_{in} - V_{Tn})^2 (1 + \lambda V_{out})$$

$$20 \times 10^{-6} \text{ A} = \frac{1}{2} \times 300 \text{ cm}^2/(\text{V} \cdot \text{s}) \times 10 \times 10^{-7} \text{ F/cm}^2 \times \frac{W}{L_{eff}} \times 0.2^2 \text{ V}^2 \times 1.1$$

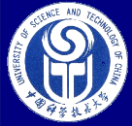
$$\text{得到: } \frac{W}{L_{eff}} = \frac{20}{6.6} \approx \frac{0.9}{0.3}, \text{ 取 } L_{drawn} = 0.5\mu\text{m}$$

$$R_D = \frac{V_{DD} - V_{out}}{I_D} = \frac{1.8\text{V} - 1\text{V}}{20 \times 10^{-6} \text{ A}} = 40 \text{ k}\Omega, \quad r_o = \frac{1}{\lambda I_D} = \frac{1}{0.1/V \times 20 \times 10^{-6} \text{ A}} = 500 \text{ k}\Omega$$

$$g_m = \mu_n C_{ox} (W / L_{eff}) (V_{in} - V_{Tn}) (1 + \lambda V_{out}) = 300 \times 10 \times 10^{-7} \times \frac{0.9}{0.3} \times 0.2 \times 1.1 \approx 0.2 \frac{\text{mA}}{\text{V}}$$

$$g_m r_o = 100, \quad A_v = -g_m (R_D || r_o) = -0.2 \times 10^{-3} \times (40 || 500) \times 10^3 = -7.4$$

该例如何提高增益？



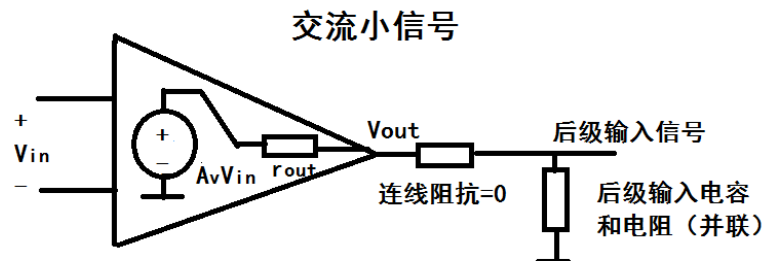
# 单级CS放大器：实际电阻 $R_D$ 做为负载

- 增益不太。原因： $R_D$ 受到直流电流和工作点电压限制，不能很大，如在高频（需大电流）和大动态范围（直流输出电平为1/2电源）时。
- 大交变信号时，应注意 $V_{DS}$ 避免进入线性区。
- 实际设计应注意考虑后级电路，避免影响工作点。
- 增益等参数仿真时须有后级电路的交流等效输入阻抗做为本级load。

负载 $C_L$ =后级电路的输入电容（高频时与后级增益和器件尺寸有关）+长连线的寄生电容。

放大电路建模：受控电压源 $A_v V_{in}$ 或  
电流源 $G_m V_{in}$ ，交流小信号！

问题： $r_{out}=R_D \parallel r_o$ 大或小比较好？







# 实际电阻（例smic18mmrf工艺）

(1) POLY电阻（栅多晶硅）：

1) 高阻：1000欧/方块，例rhrpo, rpposab,...

2) 普通：几欧/方块, rppo, rnpo,

(2) 扩散区电阻(N+,P+,NW)：几百欧/方块电阻

例： rpdif, rndif, rnwaa, rndifsab,...

(3) 金属(M1~M<sub>TOP</sub>)：几毫欧~几十毫欧/方块

设计时检查电流密度：金属层（顶层除外）：<0.5~1mA/微米宽  
硅（POLY,扩散区）：<0.3~0.5mA/微米宽

电阻宽度有最低限制，如0.4~2um，大电阻面积大，有寄生电容

电阻值不太准确，误差达20%,且温度系数大。

设计电路时，最好是采用2个电阻成比例计算的结构，  
单个电阻应用在电路时应在系统设计上采取鲁棒性设计。

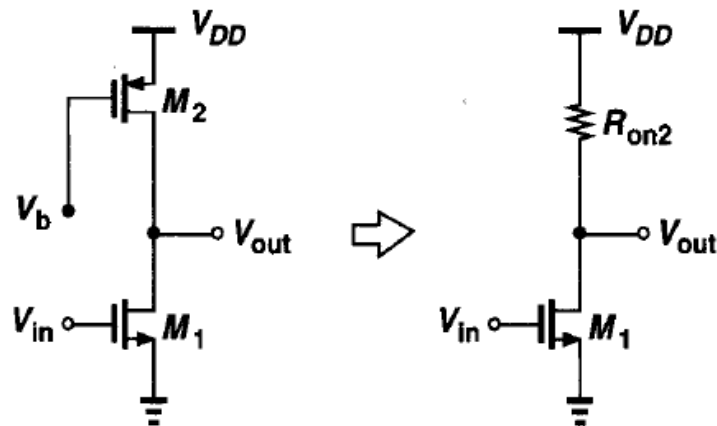


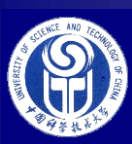
## 3.2.2 CS with Triode MOSFET Load

- 深线性区工作的MOS器件，伏安特性为电阻。

$$R_{on2} = \frac{1}{\mu_p C_{ox} \left( \frac{W}{L} \right)_2 (V_{DD} - V_b - |V_{THP}|)}$$

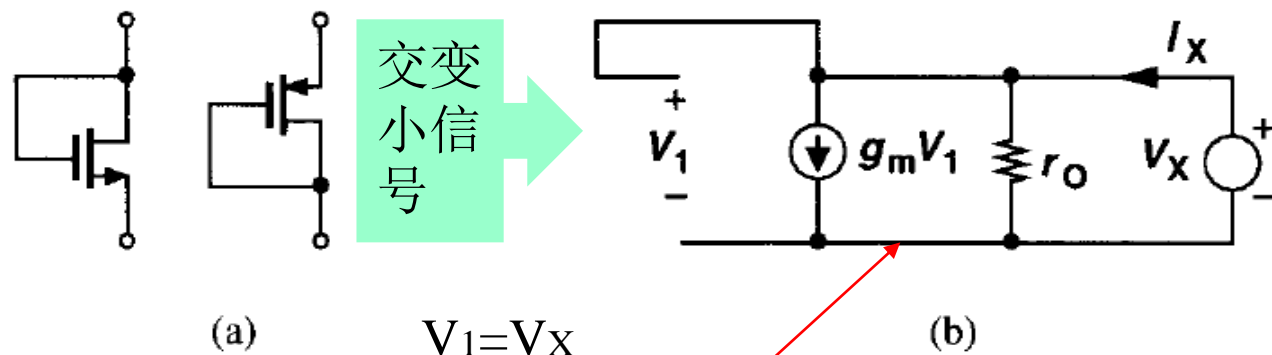
- 缺点：  $V_{DD} - V_b$  噪声较大。





### 3.2.3 CS Stage with diode-Connected Load

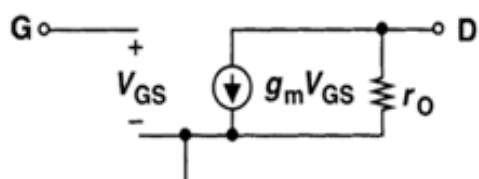
MOS 管连接成二极管做负载电阻，总是工作在饱和区，直流与交流电阻不同。先不考虑体效应 ( $g_{mb}$ )。设直流工作点由外电路确定。



输出电阻（作为信号来源电路的负载）

增益和输出电阻均是指交变小信号

**Figure 3.7** (a) Diode-connected NMOS and PMOS devices, (b) small-signal equivalent circuit.



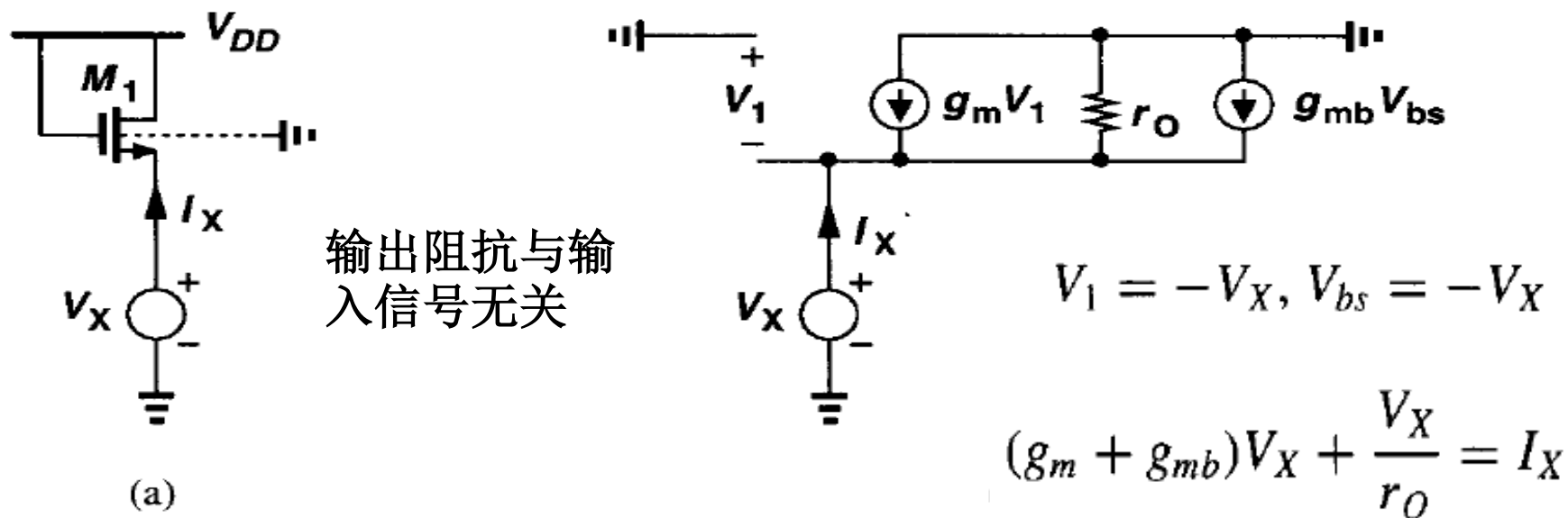
$$\text{交变信号 } I_X = \frac{V_X}{r_o} + g_m V_X \quad g_m r_o \gg 1$$

$$\text{二极管作为电阻: } r_{\text{out}} = \frac{V_X}{I_X} = \frac{1}{\frac{1}{r_o} + g_m} = r_o \parallel \frac{1}{g_m} \approx \frac{1}{g_m}$$

二极管负载等效于电阻  $1/g_m$ ，多为~几百欧。S/D无方向性



# 输出阻抗： If Body effect exists



**Figure 3.8** (a) Arrangement for measuring the equivalent resistance of a diode-connected MOSFET, (b) small-signal equivalent circuit.

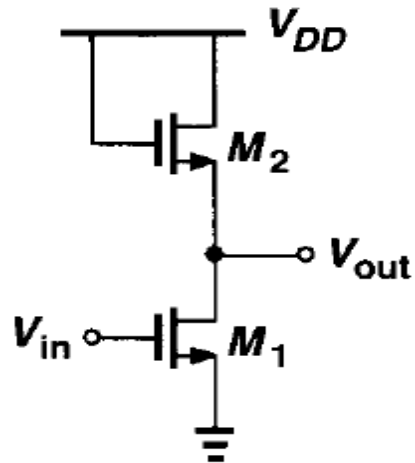
二极管输出电阻：

$$r_{out} = \frac{V_X}{I_X} = \frac{1}{g_m + g_{mb} + \frac{1}{r_o}} = r_o \parallel \frac{1}{g_m + g_{mb}} \approx \frac{1}{g_m + g_{mb}}$$

体效应使 $r_{out}$ 减小。如何设计使得电路无体效应？



# Study CS Stage with diode-Connected Load



$$A_v = -g_m R_D \quad \text{若可忽略沟道长度调制效应 ( } L_1 \text{ 不太小)}$$

$$A_v = -g_{m1} \frac{1}{g_{m2} + g_{mb2}}$$

由式2.42:

$$\eta = \frac{\partial V_{TH}}{\partial V_{SB}} = \frac{\gamma}{2} \cdot \frac{1}{\sqrt{2\Phi_F + V_{SB}}}$$

$$= -\frac{g_{m1}}{g_{m2}} \frac{1}{1 + \eta}, \quad \text{式(3.26)}$$

$$g_m = \sqrt{2\mu_n C_{ox} \frac{W}{L} I_D (1 + \lambda V_{DS})} \quad \rightarrow \quad A_v = -\frac{\sqrt{2\mu_n C_{ox} (W/L)_1 I_{D1}}}{\sqrt{2\mu_n C_{ox} (W/L)_2 I_{D2}}} \frac{1}{1 + \eta}$$

$$\text{since } I_{D1} = I_{D2} \quad A_v = -\sqrt{\frac{(W/L)_1}{(W/L)_2}} \frac{1}{1 + \eta} \quad (3.28)$$

So long as M1 stays in saturation, the gain is independent of the bias currents and voltages. The input-output characteristic is linear.



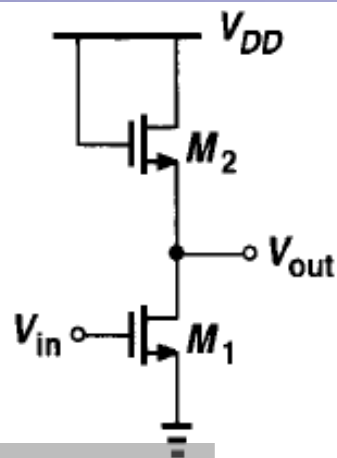
# Large-signal analysis

同样可以由大信号V/A分析，证明其具有线性特点。  
Neglecting channel-length modulation for simplicity.

$$\frac{1}{2}\mu_n C_{ox} \left(\frac{W}{L}\right)_1 (V_{in} - V_{TH1})^2 = \frac{1}{2}\mu_n C_{ox} \left(\frac{W}{L}\right)_2 (V_{DD} - V_{out} - V_{TH2})^2$$

$$\sqrt{\left(\frac{W}{L}\right)_1} (V_{in} - V_{TH1}) = \sqrt{\left(\frac{W}{L}\right)_2} (V_{DD} - V_{out} - V_{TH2})$$

Vin与Vout成线性特性



对  $V_{in}$  求偏导:  $\sqrt{\left(\frac{W}{L}\right)_1} = \sqrt{\left(\frac{W}{L}\right)_2} \left( -\frac{\partial V_{out}}{\partial V_{in}} - \frac{\partial V_{TH2}}{\partial V_{in}} \right)$

$$\therefore \frac{\partial V_{TH2}}{\partial V_{in}} = \frac{\partial V_{TH2}}{\partial V_{out}} \frac{\partial V_{out}}{\partial V_{in}} = \frac{\partial V_{TH2}}{\partial V_{SB2}} \frac{\partial V_{out}}{\partial V_{in}} = \eta_2 \frac{\partial V_{out}}{\partial V_{in}} \quad \therefore \sqrt{\left(\frac{W}{L}\right)_1} = -\sqrt{\left(\frac{W}{L}\right)_2} (1 + \eta_2) \frac{\partial V_{out}}{\partial V_{in}}$$

→  $A_v = -\sqrt{\frac{\left(\frac{W}{L}\right)_1}{\left(\frac{W}{L}\right)_2}} \times \frac{1}{1 + \eta_2}$ , 与小信号分析相同。 $\sqrt{\quad}$  是缺点!  $\eta_2 = \frac{g_{mb2}}{g_{m2}}$



# 直流工作点

$M_2$ 始终在饱和区  $I_{D2} = \frac{1}{2} \mu_n C_{OX} \frac{W_2}{L_2} (V_{GS2} - V_{TH2})^2 = I_{D1}$

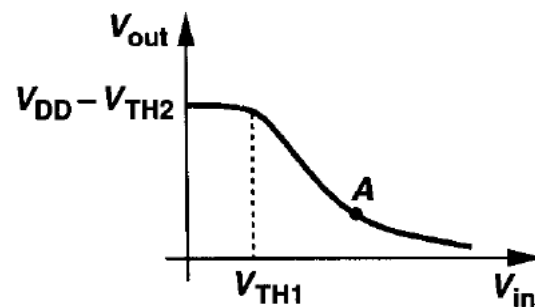
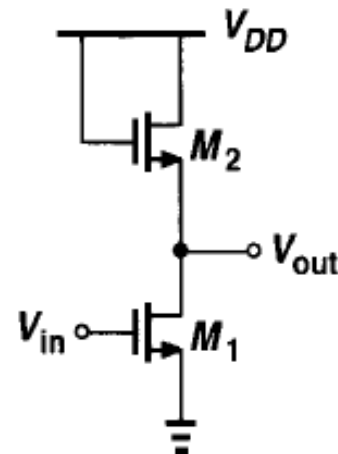
(1)  $V_{in} < V_{TH1}$  , 则  $I_{D1} = 0 = \frac{1}{2} \mu_n C_{OX} \frac{W_2}{L_2} (V_{GS2} - V_{TH2})^2$ ,

得  $V_{GS2} = V_{TH2}$ ,  $\therefore V_{out} = V_{DD} - V_{TH2} = V_{DD} - V_{TH2}$

(2)  $V_{in} > V_{TH1}$  时:  $\frac{1}{2} \mu_n C_{OX} \frac{W_1}{L_1} (V_{in} - V_{TH1})^2 = \frac{1}{2} \mu_n C_{OX} \frac{W_2}{L_2} (V_{DD} - V_{out} - V_{TH2})^2$

$$V_{out} = V_{DD} - V_{TH2} + \sqrt{\left(\frac{W/L}{W/L}\right)_1} V_{TH1} - \sqrt{\left(\frac{W/L}{W/L}\right)_2} V_{in}$$

(3)  $V_{in} > V_{out} + V_{TH1}$  (beyond point A),  $M_1$  enters the triode region, the characteristic becomes nonlinear.



**Figure 3.11** Input-output characteristic of a CS stage with diode-connected load.



# PMOS as diode-connected load

This circuit is free from body effect!

$$\mu_n \left( \frac{W}{L} \right)_1 (V_{GS1} - V_{TH1})^2 \approx \mu_p \left( \frac{W}{L} \right)_2 (V_{GS2} - V_{TH2})^2$$

channel-length modulation is neglected

$$A_v = \frac{\partial V_{out}}{\partial V_{in}} = - \frac{\partial V_{GS2}}{\partial V_{in}} = - \sqrt{\frac{\mu_n \left( \frac{W}{L} \right)_1}{\mu_p \left( \frac{W}{L} \right)_2}}$$

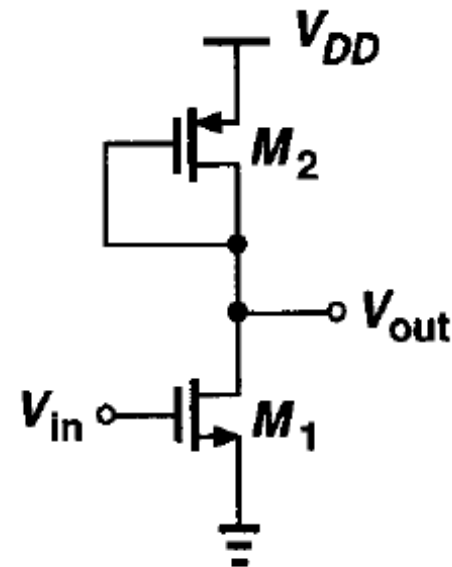


Fig. 3.12 CS stage with diode connected PMOS device

增益比NMOS二极管大！

结论：高增益需要大的输入MOS和小的负载MOS。

二极管负载的共源级放大线性度较好（大信号）。





# Fault of CS with diode-connected load

$$\mu_n \left( \frac{W}{L} \right)_1 (V_{GS1} - V_{TH1})^2 \approx \mu_p \left( \frac{W}{L} \right)_2 (V_{GS2} - V_{TH2})^2$$

$$\therefore A_v = - \sqrt{\frac{\mu_n \left( \frac{W}{L} \right)_1}{\mu_p \left( \frac{W}{L} \right)_2}} = - \frac{|V_{GS2} - V_{TH2}|}{V_{GS1} - V_{TH1}}, \text{ 过驱动电压之比!}$$

式(3.35)

$$\therefore \mu_n \left( \frac{W}{L} \right)_1 = A_v^2 \mu_p \left( \frac{W}{L} \right)_2, \text{ and}$$

$$|V_{GS2} - V_{TH2}| = -(V_{GS2} - V_{TH2}) = -(V_{out} - V_{DD} - V_{TH2})$$

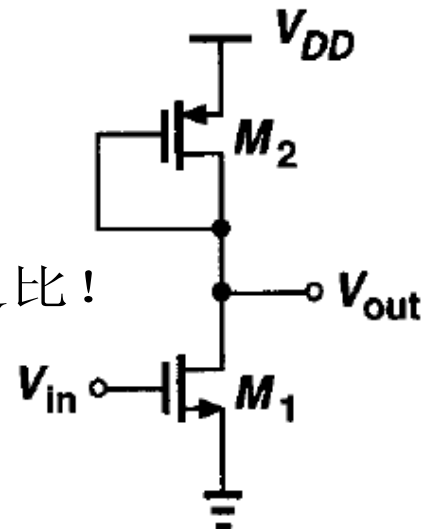
$$= -V_{out} + V_{DD} + V_{TH2} = -A_v (V_{GS1} - V_{TH1})$$

$$\text{得 } V_{out} = V_{DD} + V_{TH2} + A_v (V_{GS1} - V_{TH1})$$

例:  $A_v = -10$ ,  $V_{DD} = 3V$ ,  $V_{GS1} - V_{TH1} = 0.2V$ ,  $V_{TH2} = -0.7V$ 。求输出?

解:  $V_{out} = 3 - 0.7 - 10 \times 0.2 = 0.3V$ , 即  $V_{GS2} = 2.7V$  很大, 不好!

$V_{DS1} = 0.3V > V_{GS1} - V_{TH1} = 0.2V$ , 虽在饱和区, 但输出允许摆幅很小





# How to explain the paradox

由Equation (3.26)

(3.35)

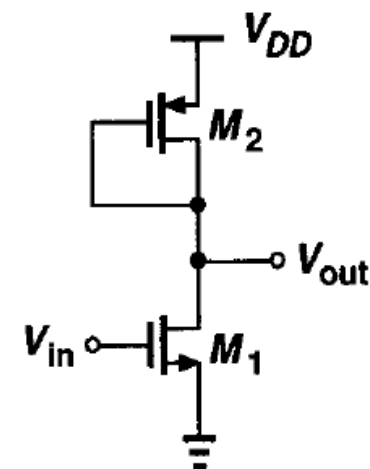
矛盾?

$$A_v \approx -\frac{g_{m1}}{g_{m2}} = -\frac{\mu_n \left(\frac{W}{L}\right)_1 (V_{GS1} - V_{TH1})}{\mu_p \left(\frac{W}{L}\right)_2 |V_{GS2} - V_{TH2}|}$$

$$A_v = -\sqrt{\frac{\mu_n \left(\frac{W}{L}\right)_1}{\mu_p \left(\frac{W}{L}\right)_2}} = -\frac{|V_{GS2} - V_{TH2}|}{V_{GS1} - V_{TH1}}$$

$V_{GS2}=V_{DS2}$ 不是独立变化的,而是与 $V_{GS1}$ 联动

$$\mu_n \left(\frac{W}{L}\right)_1 (V_{GS1} - V_{TH1})^2 \approx \mu_p \left(\frac{W}{L}\right)_2 (V_{GS2} - V_{TH2})^2$$



$$\frac{V_{GS1} - V_{TH1}}{|V_{GS2} - V_{TH2}|} = \sqrt{\frac{\mu_p \left(\frac{W}{L}\right)_2}{\mu_n \left(\frac{W}{L}\right)_1}}$$

$$A_v = -\frac{\mu_n \left(\frac{W}{L}\right)_1 (V_{GS1} - V_{TH1})}{\mu_p \left(\frac{W}{L}\right)_2 |V_{GS2} - V_{TH2}|}$$

$$= -\frac{\mu_n \left(\frac{W}{L}\right)_1}{\mu_p \left(\frac{W}{L}\right)_2} \sqrt{\frac{\mu_p \left(\frac{W}{L}\right)_2}{\mu_n \left(\frac{W}{L}\right)_1}} = -\sqrt{\frac{\mu_n \left(\frac{W}{L}\right)_1}{\mu_p \left(\frac{W}{L}\right)_2}} = -\frac{|V_{GS2} - V_{TH2}|}{V_{GS1} - V_{TH1}}$$



# Example 3.3 : 增加gain的思路

减小负载管电流，增加负载电阻（ $1/g_{m2}$ ）。

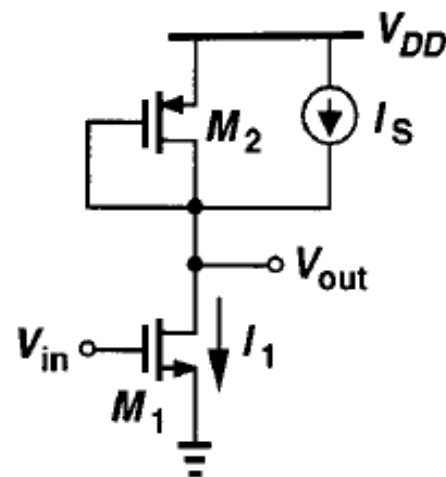
$M_2$ 电流减小到 $I_1$ 的  $1/K$ ，即增加电流源  $I_S = \frac{K-1}{K} I_1$

$$\mu_n \left( \frac{W}{L} \right)_1 (V_{GS1} - V_{TH1})^2 \approx K \mu_p \left( \frac{W}{L} \right)_2 (V_{GS2} - V_{TH2})^2, \text{ 未考虑 } \lambda$$

得到: 
$$\sqrt{\frac{\mu_n \left( \frac{W}{L} \right)_1}{\mu_p \left( \frac{W}{L} \right)_2}} = \sqrt{K} \frac{|V_{GS2} - V_{TH2}|}{V_{GS1} - V_{TH1}}$$

$$A_v \approx -g_{m1} \times \frac{1}{g_{m2}} = - \frac{\sqrt{2\mu_n C_{ox} \left( \frac{W}{L} \right)_1 I_{D1}}}{\sqrt{2\mu_p C_{ox} \left( \frac{W}{L} \right)_2 I_{D2}}}$$

$$= - \sqrt{\frac{\mu_n \left( \frac{W}{L} \right)_1 K}{\mu_p \left( \frac{W}{L} \right)_2}} = K \frac{|V_{GS2} - V_{TH2}|}{V_{GS1} - V_{TH1}}$$

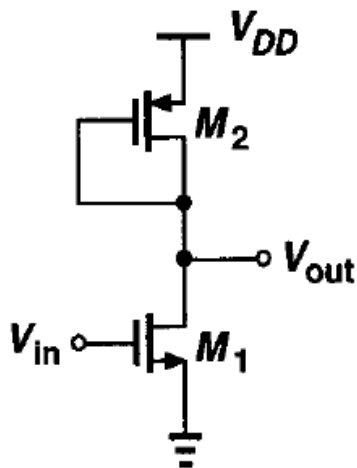


电流源输出电阻无穷大

不仅增加增益，而且减小了 $M_2$ 过驱动电压，相当于扩大了输出动态范围



# 沟道长度调制效应等效于 $r_o$ 阻抗



$$A_v \approx -g_{m1} \times R_D = -g_{m1} \left( \frac{1}{g_{m2}} \parallel r_{o1} \parallel r_{o2} \right)$$



## 3.2.4 CS Stage with current-source Load

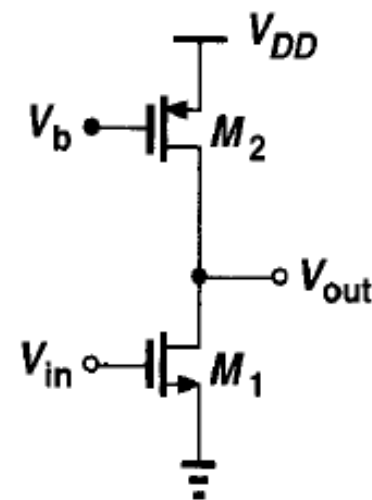
实际电阻做负载，限制了直流电流和工作点，一般情况下不能很大。

饱和区M2电流源（ $L_2$ 大）做CS负载，其等效阻抗为  $r_{o2}$  很大（理想为无穷大）。

交变小信号增益： $A_v = -g_m(r_{o1} \parallel r_{o2})$

输出直流工作点电压可变化范围很大：

$$V_b + |V_{TH2}| > V_{out} > V_{in} - V_{TH1}$$



$$L \uparrow \Rightarrow r_o \uparrow \Rightarrow A_v \uparrow$$

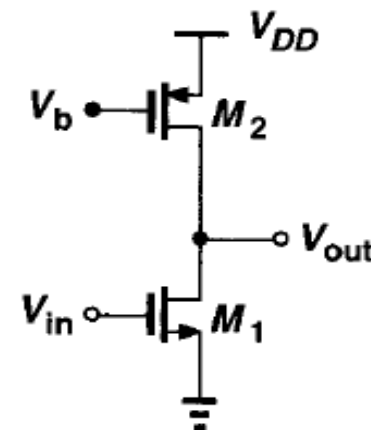
缺点：电流源负载CS放大电路的输出DC电位需要通过其他方法确定。

- Intrinsic gain(本征增益):

$$g_{m1}r_{o1} = \sqrt{2 \left( \frac{W}{L} \right)_1 \mu_n C_{ox} I_D} \frac{1}{\lambda I_D}$$

$$r_{o1} \approx \frac{1}{\lambda I_D} \propto \frac{L_1}{I_D}$$

$$\therefore g_{m1}r_{o1} \propto \sqrt{2\mu_p C_{ox} \frac{W_1 L_1}{I_D}}$$



输入管（信号放大管）本征增益  
会随着  $I_D$  减小或 MOSFET 栅极面积增加而增加。



## 3.2.5 CS with source degeneration

- 源极负反馈(源简并)

$$V_{out} = V_{DD} - I_D R_D$$

设计思想：采用负反馈，  
减小 $I_D$ 与 $V_{in}$ 之间的非线性。

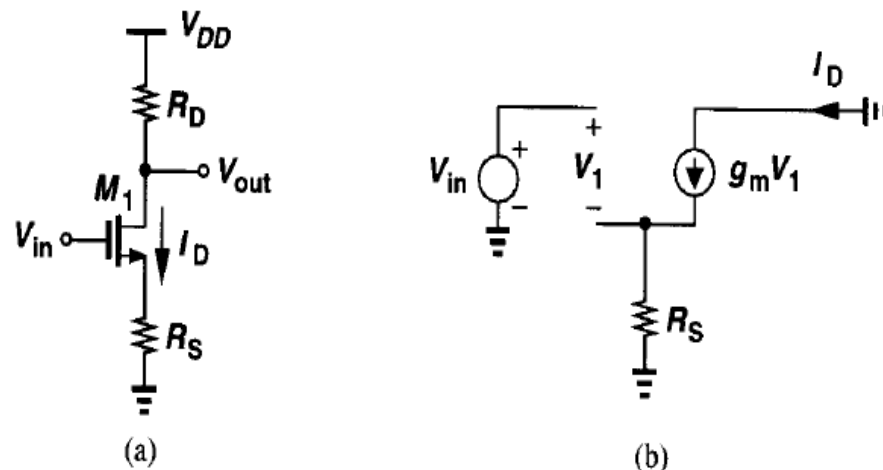
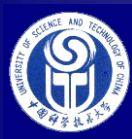


图3.16 带源极负反馈的共源极

输入电压 $V_{in}$ 一部分损失在 $R_S$ 上，  
 $V_{GS}$ 减小，使得  $I_D$ 非线性项减小。

$R_S = 0$ 时：  $A_v = -g_m R_D$ ,  $g_m$ 定义为MOSFET的跨导

$$g_m = \frac{\partial I_D}{\partial V_{GS}} = \mu_n C_{ox} (W / L) (V_{GS} - V_{TH}) = \sqrt{2\mu_n C_{ox} \frac{W}{L} I_D}$$



# 小信号电压增益与电路等效跨导

$R_S \neq 0$ 时:  $V_{GS} = V_{in} - I_D R_S$ , 设  $I_D = f(V_{GS})$

定义电路跨导  $G_m = \frac{\partial I_D}{\partial V_{in}} = \frac{\partial I_D}{\partial V_{GS}} \frac{\partial V_{GS}}{\partial V_{in}} = \frac{\partial I_D}{\partial V_{GS}} (1 - \frac{\partial I_D}{\partial V_{in}} R_S) = g_m (1 - G_m R_S)$

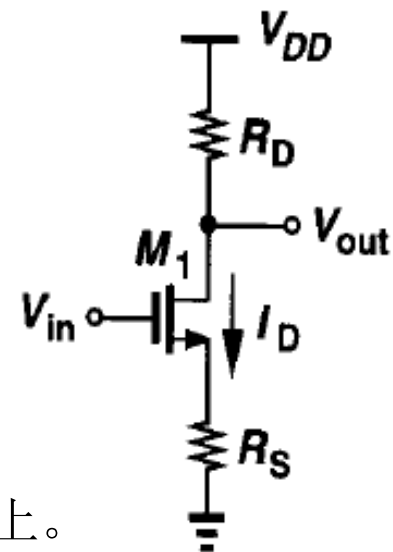
得到:  $G_m = \frac{g_m}{1 + g_m R_S} = \frac{1}{\frac{1}{g_m} + R_S}$

不考虑 $\lambda$ 时  $A_v = \frac{\partial V_{out}}{\partial V_{in}} = -\frac{\partial I_D}{\partial V_{in}} R_D = -G_m R_D = \frac{-g_m R_D}{1 + g_m R_S}$

当  $g_m R_S \gg 1$  时,  $A_v = -G_m R_D \approx -\frac{R_D}{R_S}$ ,  $\therefore G_m \approx \frac{1}{R_S}$

此时  $\Delta V_{in} = \frac{\Delta I_D}{G_m} \approx R_S \Delta I_D$ , 表明输入的变化信号基本都加在  $R_S$  上。

交变输出电流  $\Delta I_D$  以及电压  $\Delta V_{out}$  的线性变好, 代价是增益变小。







# 求有源极反馈电阻CS增益的简便方法

$$A_v = -G_m R_D = -\frac{g_m}{1 + g_m R_S} R_D = -\frac{R_D}{\frac{1}{g_m} + R_S}$$

忽略沟道长度调制效应

- 增益=漏极通路电阻/源极通路从地向上看到的电阻

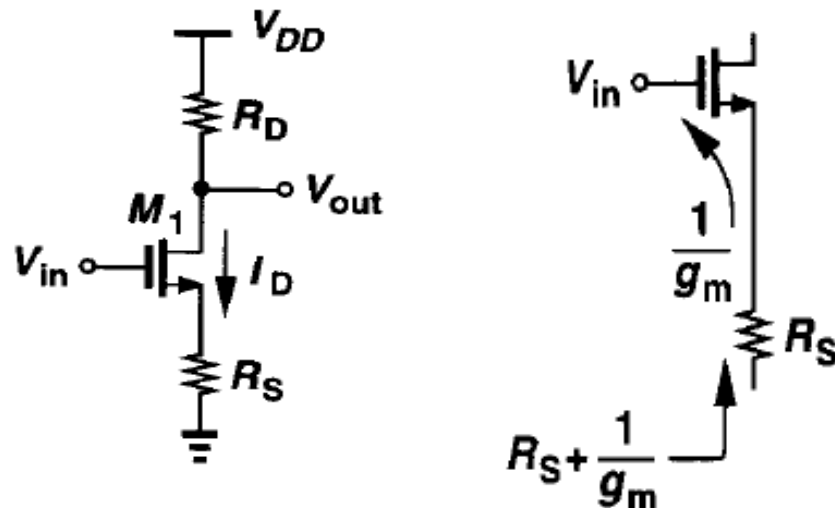
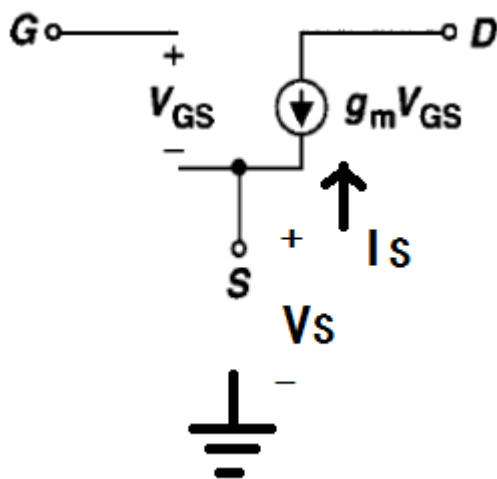


Figure 3.20 resistance seen in the source path



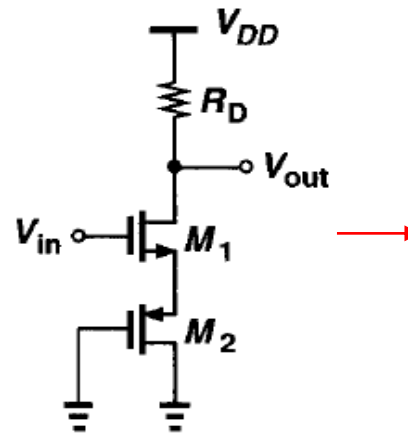
$$\text{MOS的} S \text{极小信号电阻} = \frac{V_S}{I_S} = \frac{-V_{GS}}{-g_m V_{GS}} = \frac{1}{g_m}$$

( $\because$  求输出阻抗时输入电压 = 0, 即  $G$  交流接地)

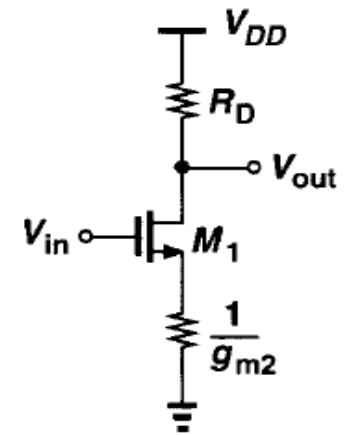


# Example 3.5

- Assuming  $\lambda = \gamma = 0$
- solution



(a)



(b)

$$A_v = -\frac{R_D}{\frac{1}{g_{m1}} + \frac{1}{g_{m2}}}$$



## 辅助定律（电路基本理论）

在线性电路中，开路电压增益等于 $-G_m R_{out}$ ，其中 $G_m$ 表示**输出与地短接（恒压）**时的**电路跨导**（ $G_m = I_{out}/V_{in}$ ）。 $R_{out}$ 表示当输入电压为零时（ $I_{out} = G_m V_{in} = 0$ ）电路的输出电阻。

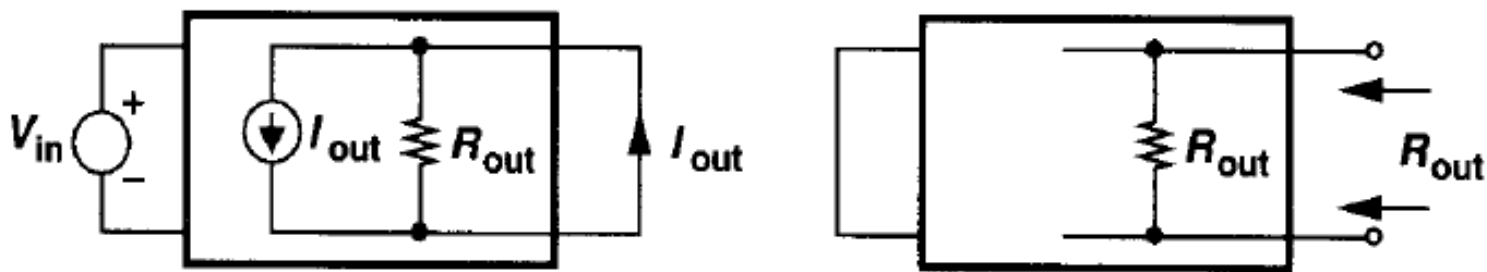


Figure 3.25 Modeling output port of an amplifier by a Norton equivalent.

输出开路（不接负载）电压： $V_{out} = -I_{out} R_{out} = -G_m V_{in} R_{out}$

带负载 $R_D$ 时输出电压： $V_{out} = -I_{out} (R_{out} \parallel R_D)$

$= -V_{in} G_m (R_{out} \parallel R_D)$

负载可后加计算

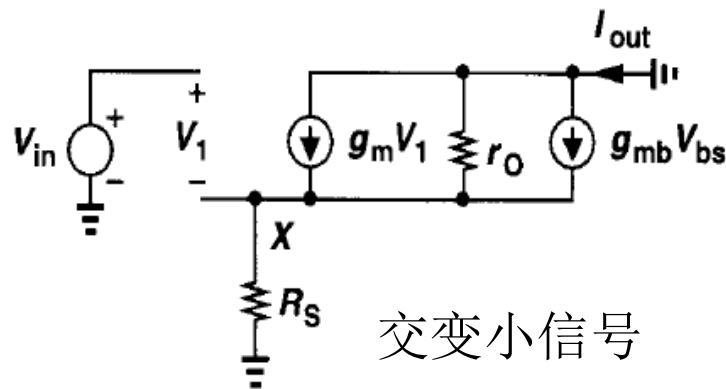


# Gm with body effect and channel-length modulation

前例图3.16:  $V_{in} = V_1 + I_{out}R_S$

考虑沟道长度调制和体效应。

如何求电路交变小信号跨导:  $G_m = \frac{I_{out}}{V_{in}}$  ?



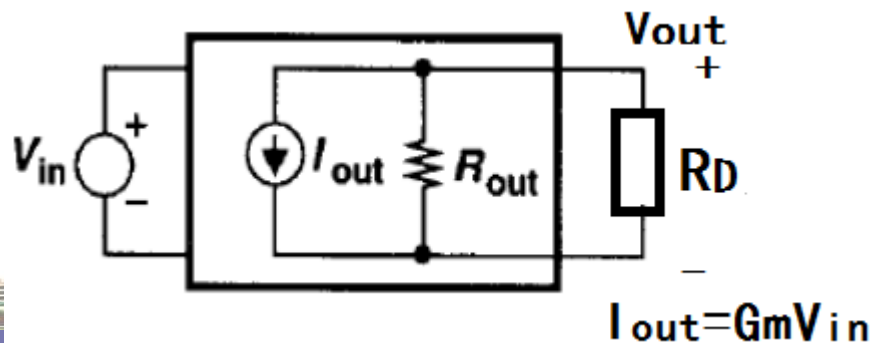
$$\text{输出短路交变电流 } I_{out} = g_m V_1 + g_{mb} V_{bs} - \frac{V_X}{r_o} = g_m V_1 - g_{mb} V_X - \frac{V_X}{r_o}$$

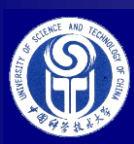
$$= g_m V_1 - g_{mb} I_X R_S - \frac{I_X R_S}{r_o} = g_m (V_{in} - I_{out} R_S) - g_{mb} I_{out} R_S - \frac{I_{out} R_S}{r_o}$$

$$\longrightarrow G_m = \frac{I_{out}}{V_{in}} = \frac{g_m r_o}{R_S + [1 + (g_m + g_{mb}) R_S] r_o}, \text{ 式 (3.55)}$$

$$A_v = -G_m (R_{out} \parallel R_D) \approx -G_m R_D$$

**Rout**见式 (3.60)





# Output resistance of degenerated CS

$$R_{out} = \frac{V_x}{I_x} \quad \text{令 } V_{in} = 0, \text{ 先不考虑 } R_D$$

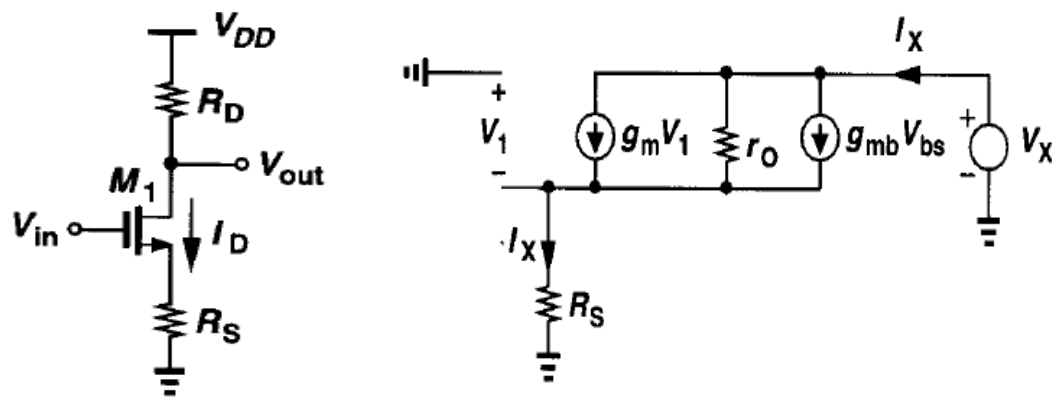
$$V_{bs} = V_1 = -I_x R_S$$

$$\begin{aligned} V_X &= r_0 [I_X - g_m V_1 - g_{mb} V_{bs}] + I_X R_S \\ &= r_0 [I_X + (g_m + g_{mb}) I_X R_S] + I_X R_S \end{aligned}$$

$$R_{out} = \frac{V_x}{I_x} = [1 + (g_m + g_{mb}) R_S] r_0 + R_S = [1 + (g_m + g_{mb}) r_0] R_S + r_0, \text{ 式(3.60)}$$

$$\because (g_m + g_{mb}) r_0 \gg 1$$

$$\therefore R_{out} \approx (g_m + g_{mb}) r_0 \times R_S + r_0$$

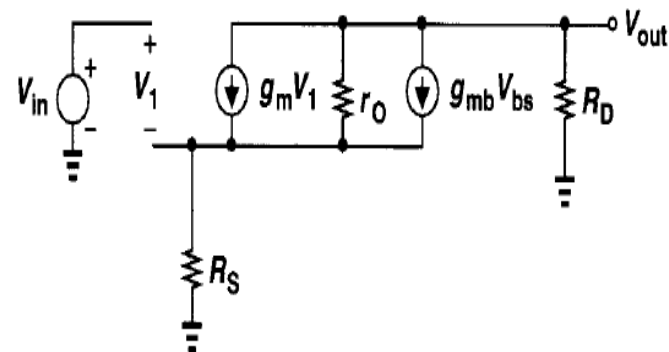


**Figure 3.22** Equivalent circuit for calculating the output resistance of a degenerated CS stage.

源极负反馈:增大共源级的输出电阻。



# 验证：包含 $R_D$ 的公式推导



$$I_{RS} = -I_{RD} = -\frac{V_{out}}{R_D}$$

$$V_{bs} = -V_{RS}$$

$$I_{ro} = -I_{RD} - (g_m V_1 + g_{mb} V_{bs}) = -\frac{V_{out}}{R_D} - [g_m (V_{in} - V_{RS}) - g_{mb} V_{RS}]$$

$$= -\frac{V_{out}}{R_D} - [g_m (V_{in} + \frac{V_{out}}{R_D} R_S) + g_{mb} \frac{V_{out}}{R_D} R_S]$$

$$V_{out} = I_{ro} r_o + V_{RS} = I_{ro} r_o - \frac{V_{out}}{R_D} R_S$$

$$= -\frac{V_{out}}{R_D} r_o - [g_m (V_{in} + \frac{V_{out}}{R_D} R_S) + g_{mb} \frac{V_{out}}{R_D} R_S] r_o - \frac{V_{out}}{R_D} R_S$$

$$A_v = \frac{V_{out}}{V_{in}} = -\frac{g_m R_D r_o}{R_D + R_S + r_o + (g_m + g_{mb}) R_S r_o} = -\frac{g_m R_D r_o}{R_D + \{[1 + (g_m + g_{mb}) r_o] R_S + r_o\}}$$

(3.71)



# 验证：包含 $R_D$ 的公式推导（续）

分析 $A_v$ 分母大括号项（=带负反馈共源极的输出电阻 $R_{out}$ ）。

$$R_{out} = [1 + (g_m + g_{mb})r_o]R_S + r_o, \text{ 式(3.60)}$$

$$\begin{aligned} A_v &= - \frac{g_m R_D r_o}{R_D + \{[1 + (g_m + g_{mb})r_o]R_S + r_o\}} \cdot \frac{[1 + (g_m + g_{mb})r_o]R_S + r_o}{[1 + (g_m + g_{mb})r_o]R_S + r_o} \\ &= - \frac{g_m r_o}{[1 + (g_m + g_{mb})r_o]R_S + r_o} \cdot \frac{R_D \{[1 + (g_m + g_{mb})r_o]R_S + r_o\}}{R_D + [1 + (g_m + g_{mb})r_o]R_S + r_o} \\ &= -G_m(R_D \parallel R_{out}) \end{aligned}$$

与先不计算 $R_D$ ，再将 $R_D$ 加入电路的计算方法结果一致

# Gain of a degenerated CS

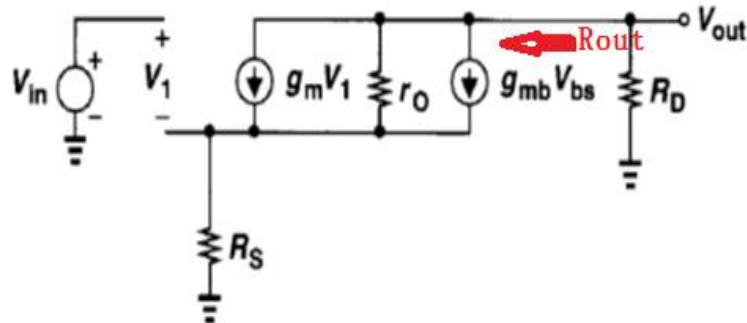
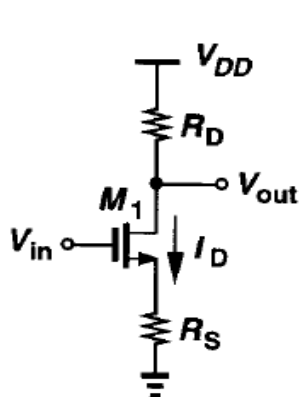
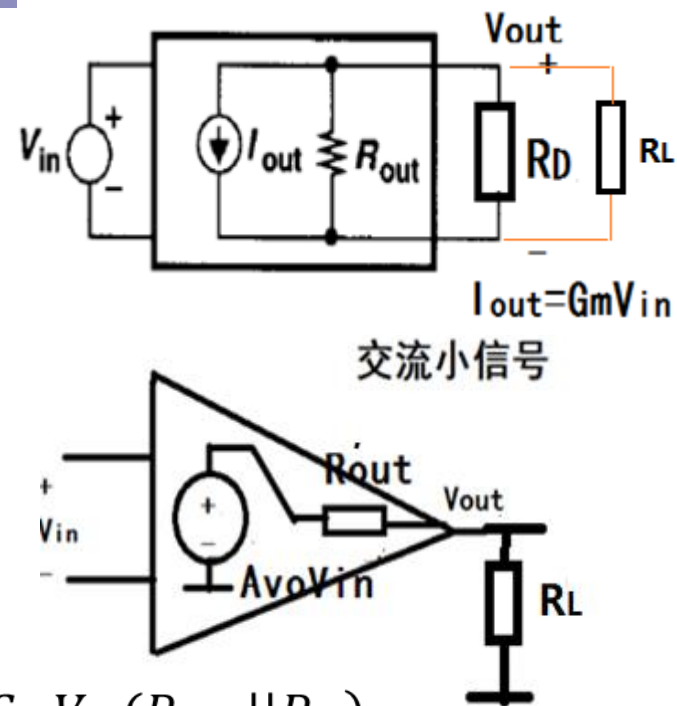


Figure 3.24 Small-signal model of degenerated CS stage with finite output resistance.



负载 $R_L$ 开路输出:  $V_{outO} = -I_{out}(R_{out} \parallel R_D) = -G_m V_{in}(R_{out} \parallel R_D)$

$R_{out}$ 是向MOS漏极看进去的输出阻抗。

$G_m$ 为输出短路电路跨导, 式3.55

总输出阻抗为 $R'_{out} = R_{out} \parallel R_D$

记负载开路电压增益 $A_{vo} = -G_m(R_{out} \parallel R_D) = -G_m R'_{out}$

带负载 $R_L$ ?  $R_L$ 与 $R_D$ 并联, 或 $A_v = A_{vo} \frac{R_L}{R'_{out} + R_L} = -G_m(R'_{out} \parallel R_L)$





## 例 3.6 calculate the voltage gain

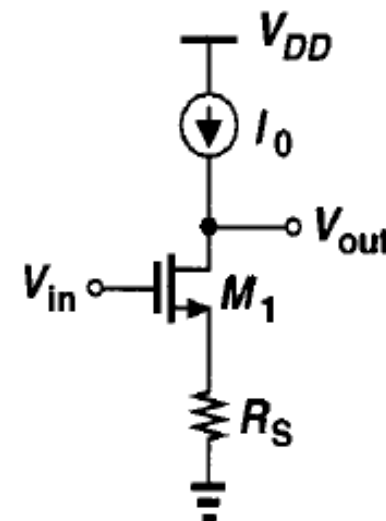
**Solution**

$$A_v = - \frac{g_m R_D r_o}{R_D + \{[1 + (g_m + g_{mb})r_o]R_S + r_o\}}$$
$$= -g_m r_o, \text{ 式(3.71)中 } R_D = \infty$$

$$\text{或 } A_v = -G_m (R_{out} \parallel R_D) = -G_m R_{out}$$

$$= - \frac{g_m r_o}{[1 + (g_m + g_{mb})r_o]R_S + r_o} \bullet \{[1 + (g_m + g_{mb})r_o]R_S + r_o\}$$
$$= -g_m r_o$$

与 $R_S$ 无关。原因是电流不变， $R_S$ 上的小信号（变化）压降=0





## 3.3 source follower 源跟随器

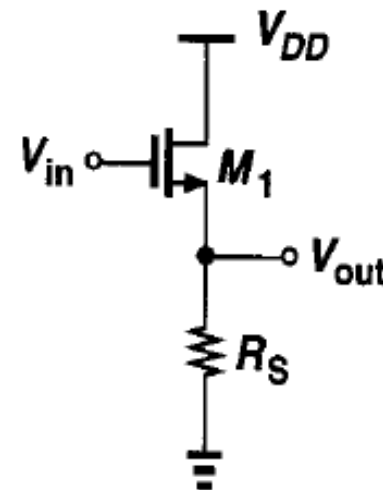
common-drain stage

- 特点:

小信号电压近似等于输入电压;

低频输入阻抗大,

输出阻抗小  $(1/g_m) \parallel R_S$ 。



作用:

当两级放大器级联时, 若前级输出电阻大, 或后级输入电阻小, 则在两级放大器之间插入源跟随器, 可以提高多级放大器的电压增益。



# Large-signal & Small-signal behavior

忽略沟道长度调制效应

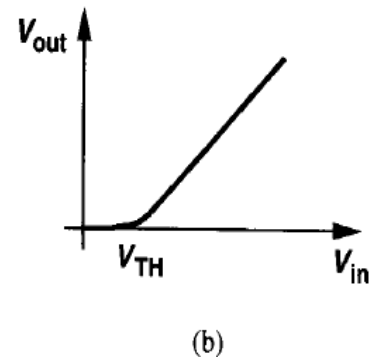
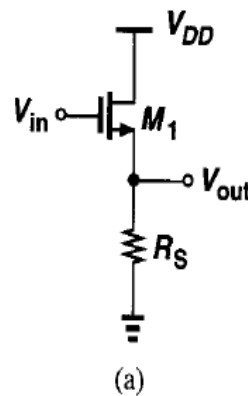
$$V_{out} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{out} - V_{TH})^2 R_S$$

$$\text{小信号 } A_v = \frac{\partial V_{out}}{\partial V_{in}}$$

$$= \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{out} - V_{TH}) \left(1 - \frac{\partial V_{out}}{\partial V_{in}} - \frac{\partial V_{TH}}{\partial V_{in}}\right) R_S$$

$$\text{由式(2.42)得 } \frac{\partial V_{TH}}{\partial V_{in}} = \frac{\partial V_{TH}}{\partial V_{SB}} \frac{\partial V_{SB}}{\partial V_{in}} = \eta \frac{\partial V_{out}}{\partial V_{in}} = \eta A_v$$

$$\therefore A_v = \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{out} - V_{TH}) (1 - A_v - \eta A_v) R_S$$



**Figure 3.27** (a) Source follower, and (b) its input-output characteristic.

$$\eta = \frac{g_{mb}}{g_m} = \frac{\frac{\partial I_D}{\partial V_{BS}}}{\frac{\partial I_D}{\partial V_{GS}}}$$



# Gain of Source Follower

$$A_v = \frac{\partial V_{out}}{\partial V_{in}} = \frac{\mu_n C_{ox} \frac{W}{L} (V_{in} - V_{out} - V_{TH}) R_S}{1 + \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{out} - V_{TH}) R_S (1 + \eta)} = \frac{g_m R_S}{1 + (g_m + g_{mb}) R_S} < 1$$

$$g_m = \mu_n C_{ox} \frac{W}{L} (V_{in} - V_{out} - V_{TH})$$

$$g_{mb} = \eta g_m = \frac{\gamma}{2\sqrt{2\Phi_F + V_{SB}}} g_m, \text{ 式 (2.44)}$$



# 小信号等效电路得到相同结果

$$V_1 = V_{in} - V_{out}$$

$$V_{bs} = -V_{sb} = -V_{out} \quad \text{为何} r_o \text{可忽略?}$$

$$\therefore g_m V_1 + g_{mb} V_{bs} = g_m (V_{in} - V_{out}) - g_{mb} V_{out} = \frac{V_{out}}{R_S}$$

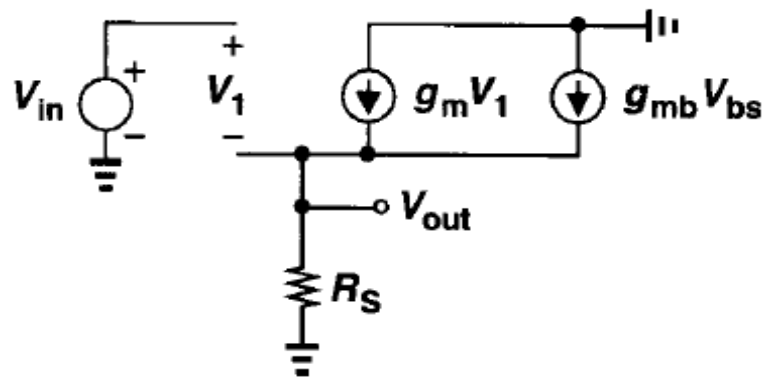
$$A_v = \frac{\partial V_{out}}{\partial V_{in}} \quad (\text{即等效电路图中 } \frac{V_{out}}{V_{in}})$$

$$= \frac{g_m R_S}{1 + (g_m + g_{mb}) R_S} < 1$$

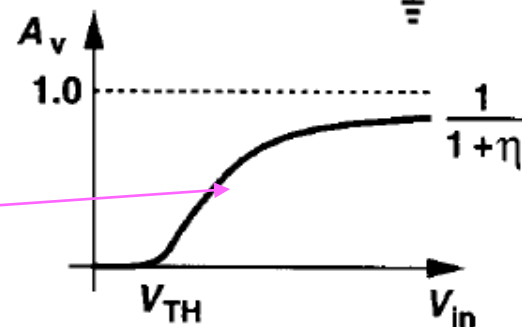
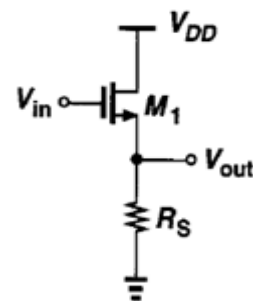
$$\eta = \frac{g_{mb}}{g_m} \text{ 可取 } 0.2 \text{ 估算}$$

当  $g_m R_S \gg 1$  时

$$A_v \approx \frac{g_m R_S}{(g_m + g_{mb}) R_S} = \frac{1}{1 + \eta} \text{ 达到“不变”的最大增益}$$

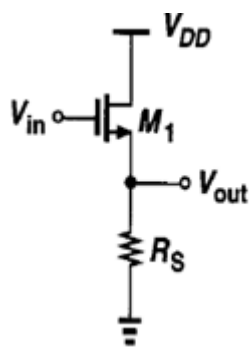


**Figure 3.28** Small-signal equivalent circuit of source follower.





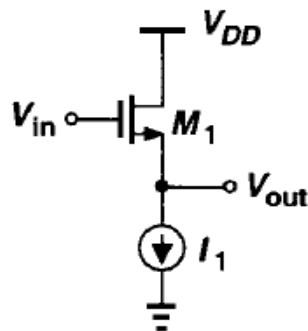
# 采用电流源的源跟随器



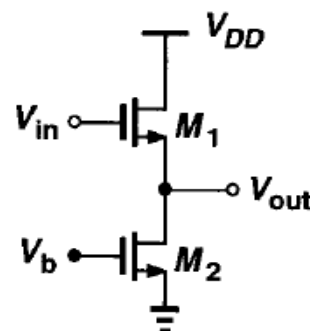
$R_S = \infty$  时

$$A_v = \frac{g_m R_S}{1 + (g_m + g_{mb}) R_S} = \frac{1}{1 + \eta}$$

最大增益=本征增益



(a)



(b)

**Figure 3.30** Source follower using an NMOS transistor as current source.

- 保证M2处于饱和区。  $V_b - V_{out} < V_{TH2}$

设计注意事项:

1. 体效应导致 $V_{TH}$ 变化, 导致输入输出之间的非线性 (大输入范围时);
2. 直流电平移动导致电压余度(headroom)减少。



# 源跟随器的输出电阻

sup pose :  $\lambda \approx 0$

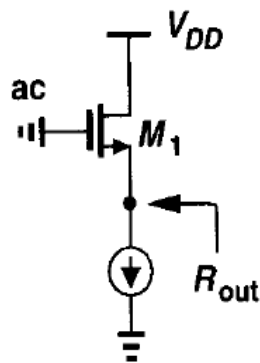
$$V_1 = -V_X,$$

$$I_X + g_m V_1 + g_{mb} V_{bs}$$

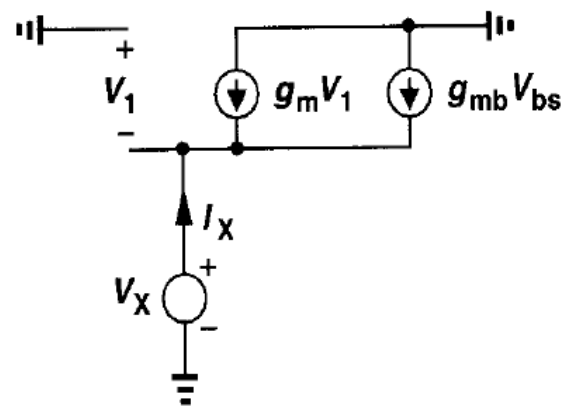
$$= I_X - g_m V_X - g_{mb} V_X = 0$$

$$R_{out} = \frac{V_X}{I_X} = \frac{1}{g_m + g_{mb}} = \frac{1}{g_m} \parallel \frac{1}{g_{mb}}$$

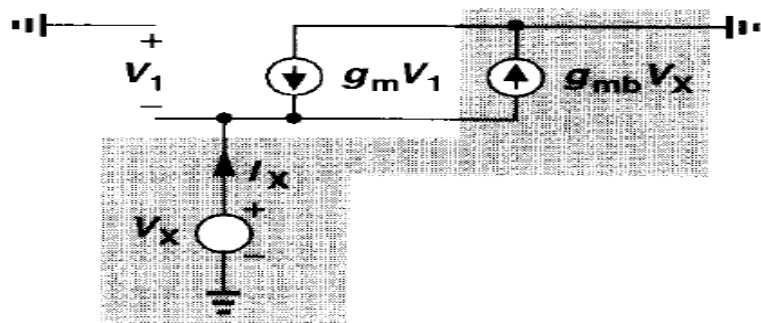
与二极管相同!几十欧~几千欧.



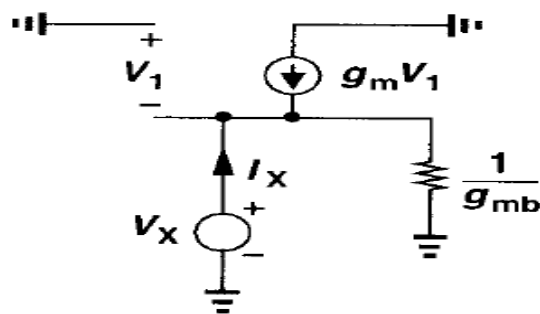
(a)



(b)



(a)

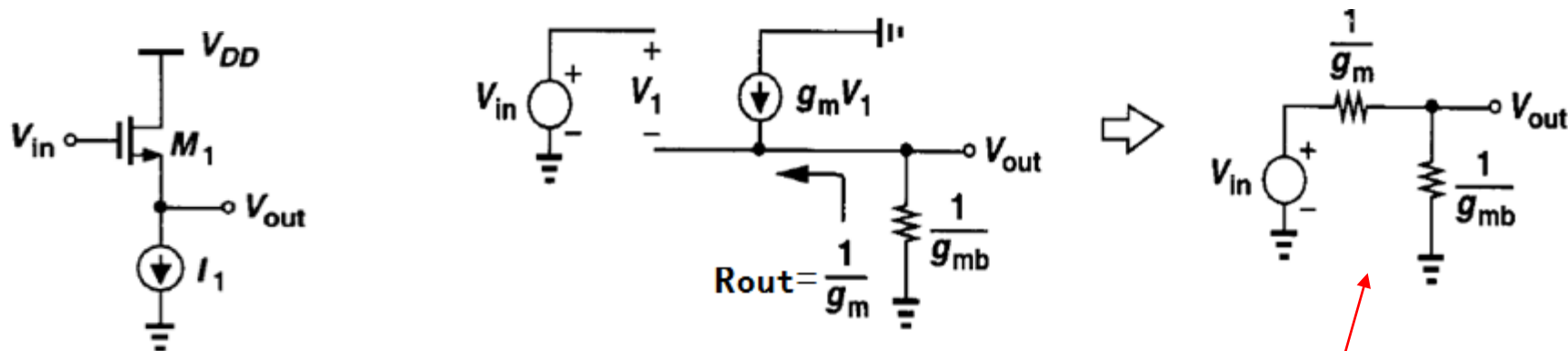


(b)

Figure 3.32 Source follower including body effect.



# 另一种方法：用辅助定理求Intrinsic gain of SF



**Figure 3.33** Representation of intrinsic source follower by a Thevenin equivalent.

求 $R_{out}$ : 令 $V_{in} = 0$ , 则 $V_{out} = -V_1$

$$R_{out} = \frac{V_{out}}{-g_m V_1} = \frac{1}{g_m}$$

总结：源跟随器MOS看成有一内阻 $1/g_m$  串联 $1/g_{mb}$ 。  
若有负载阻抗，则与 $1/g_{mb}$ 并联。

交流输出短路 ( $V_1 = V_{in}$ ) 电流:  $I_{SC} = g_m V_1 = g_m V_{in}$

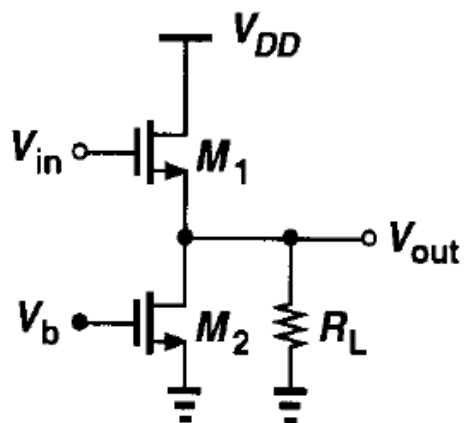
开路输出电压:  $V_{OC} = R_{out} I_{SC} = \frac{1}{g_m} g_m V_{in} = V_{in}$

$$A_v = \frac{V_{out}}{V_{in}} = \frac{\frac{1}{g_{mb}}}{\frac{1}{g_m} + \frac{1}{g_{mb}}} = \frac{g_m}{g_m + g_{mb}} = \frac{1}{1 + \eta}, \text{ 无负载时}$$

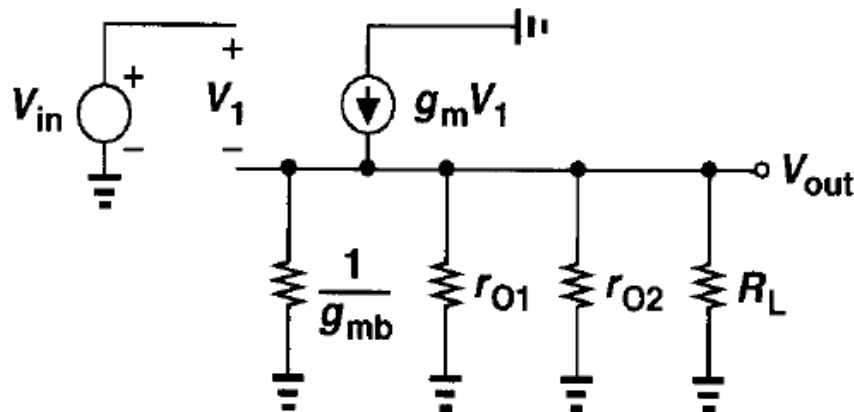




# 考虑体效应和沟道长度调制效应的SF



(a)



(b)

**Figure 3.34** (a) Source follower driving load resistance, (b) small-signal equivalent circuit.

( $V_{in} > V_{GS1} + V_b - V_{TH2}$ )

$g_{mb}$ 指 $g_{mb1}$

$$A_v = \frac{\frac{1}{g_{mb}} \parallel r_{O1} \parallel r_{O2} \parallel R_L}{\frac{1}{g_{mb}} \parallel r_{O1} \parallel r_{O2} \parallel R_L + \frac{1}{g_m}}$$

公式中的 $g_m$ 和 $g_{mb}$ 是M1参数.

(3.90)

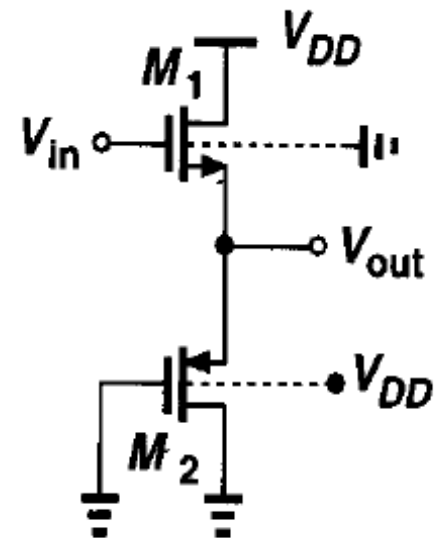


# 例3.8

- M2为二极管，由式（3.24）和（3.90）

$$A_v = \frac{\frac{1}{g_{mb1}} \parallel r_{o1} \parallel r_{o2} \parallel \frac{1}{g_{m2} + g_{mb2}}}{\frac{1}{g_{mb1}} \parallel r_{o1} \parallel r_{o2} \parallel \frac{1}{g_{m2} + g_{mb2}} + \frac{1}{g_{m1}}}$$

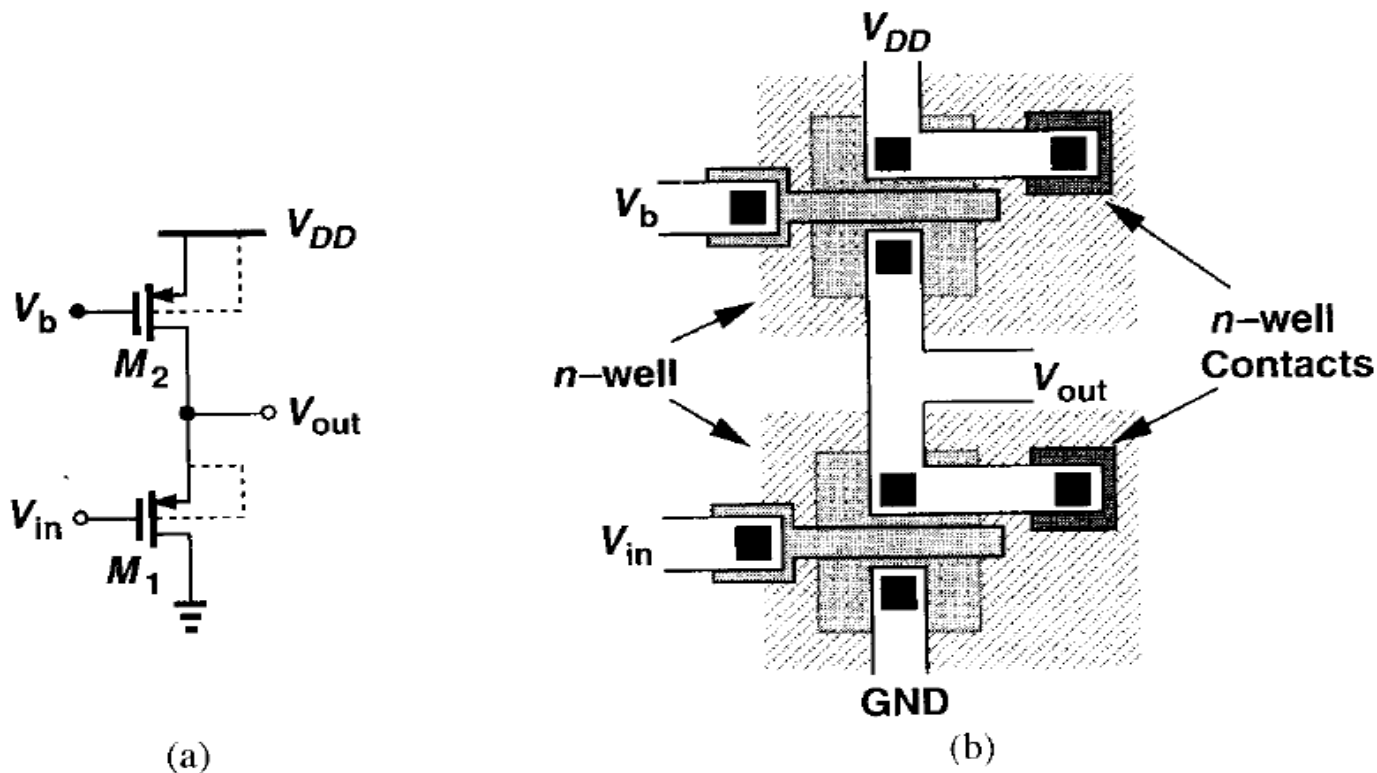
$$= \frac{\frac{1}{g_{mb1}} \parallel \frac{1}{g_{m2} + g_{mb2}}}{\frac{1}{g_{mb1}} \parallel \frac{1}{g_{m2} + g_{mb2}} + \frac{1}{g_{m1}}}, \text{ M2电阻小, 不好}$$



NMOS SF输出电平低于输入至少 $V_{TH}$

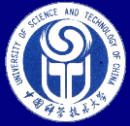


# PMOS的SF:消除体效应的非线性

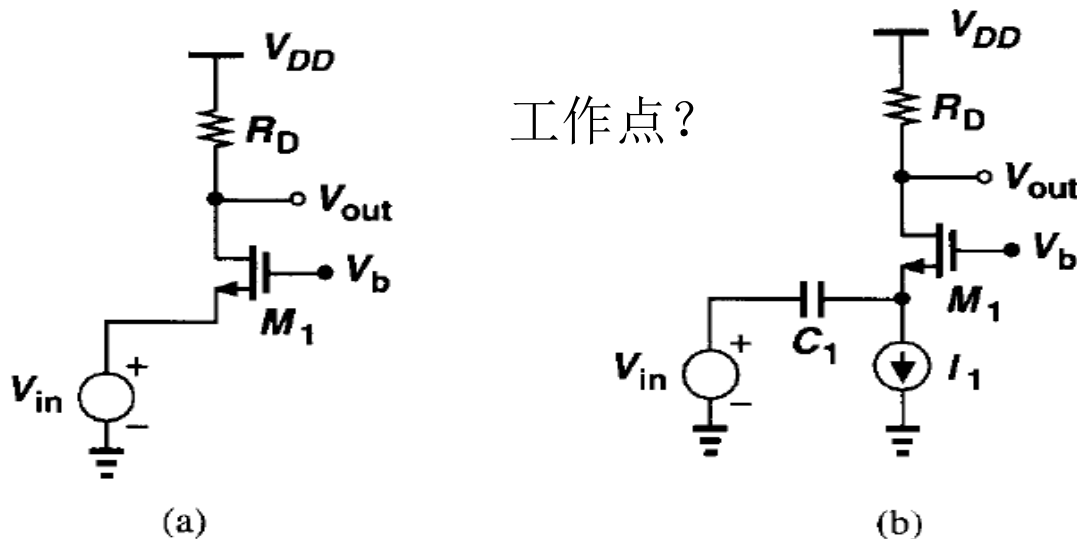


**Figure 3.36** PMOS source follower with no body effect.

PMOS SF输出电平高于输入至少 $V_{TH}$



## 3.4 Common-gate stage



工作点?

信号从源端输入，从漏极输出。小信号输入输出共栅

M1可用恒流源偏置，高频信号通过C耦合；也可直接低频输入信号源。

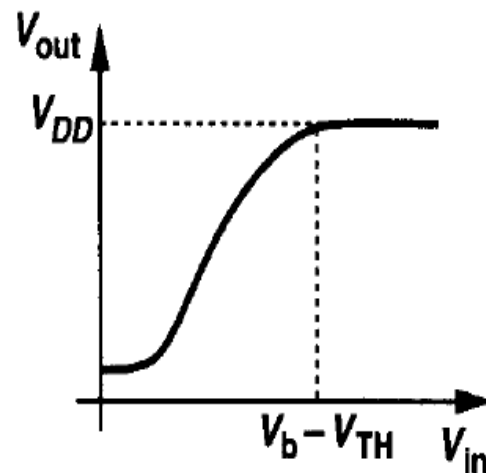
**Figure 3.40** (a) Common-gate stage with direct coupling at input, (b) CG stage with capacitive coupling at input.

饱和区  $V_{in} \downarrow \Rightarrow I_D \uparrow \Rightarrow V_{out} \downarrow$ ，同向放大

$$\text{当 } V_{out} = V_{DD} - \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_b - V_{in} - V_{TH})^2 R_D$$

降到  $V_b - V_{TH}$  时进入线性区

图(a): For  $V_{in} > V_b - V_{TH}$   
M1 is off,  $V_{out} = V_{DD}$





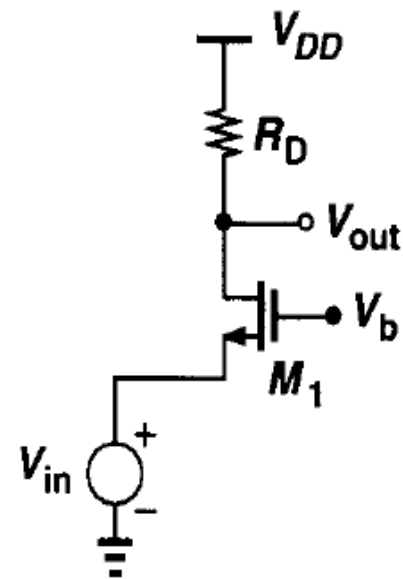
# Gain of CG

$$V_{out} = V_{DD} - \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_b - V_{in} - V_{TH})^2 R_D, \text{ 忽略 } \lambda$$

$$\frac{\partial V_{out}}{\partial V_{in}} = -\mu_n C_{ox} \frac{W}{L} (V_b - V_{in} - V_{TH}) \left(-1 - \frac{\partial V_{TH}}{\partial V_{in}}\right) R_D$$

$$\therefore \frac{\partial V_{TH}}{\partial V_{in}} = \frac{\partial V_{TH}}{\partial V_{SB}} = \eta$$

$$\therefore \frac{\partial V_{out}}{\partial V_{in}} = \mu_n C_{ox} \frac{W}{L} (V_b - V_{in} - V_{TH}) (1 + \eta) R_D = g_m (1 + \eta) R_D$$



虽然体效应使共栅级的等效跨导变大，但并不会带来好的性能。

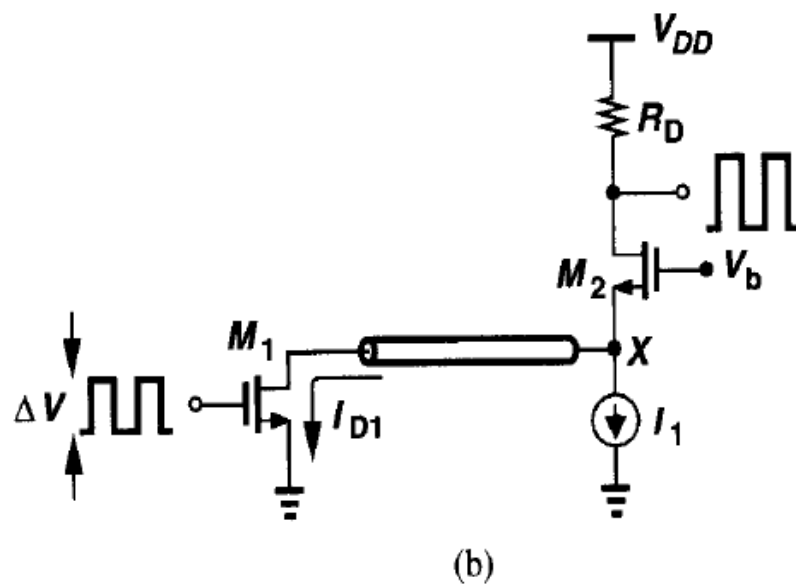
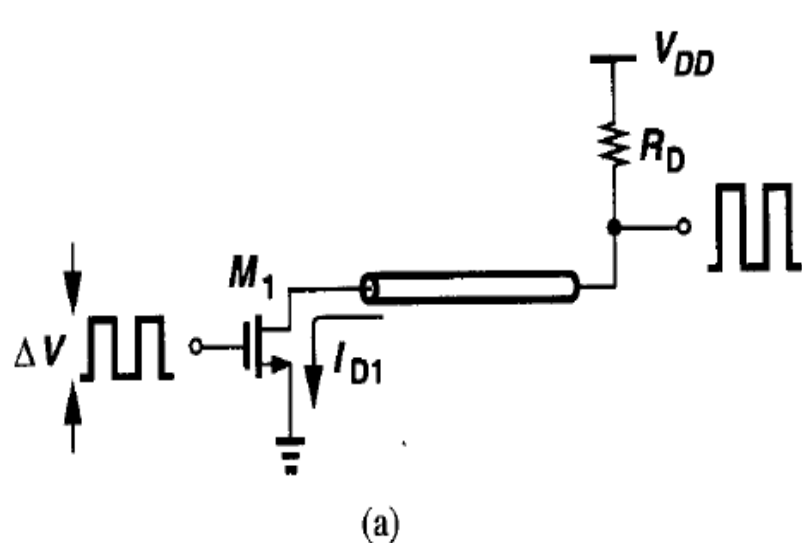
设  $\lambda \approx 0$  即  $\Delta V_{DS}$  对  $I_D$  交变无影响，

或  $R_D$  不太大 ( $I_D$  不恒定) 时：

$$\text{输入阻抗} \approx \frac{1}{g_m + g_{mb}}, \text{ 即 } \frac{1}{g_m} \parallel \frac{1}{g_{mb}}$$

共栅级电路应用在  
低输入阻抗的场合

# 例3.10



传输线电阻50欧， $R_D=50$ 欧，忽略沟道长度调制和体效应。

- (a) 两种接法的低频增益（忽略MOS寄生电容）。
- (b) X点反射最小的条件？（即M2源极看到的交流电阻为 50欧）



## 例3.10 续

解：(a)两种接法输入 $V_{in}$ 变化 $\Delta V$ ,  $\Delta I_{D1} = g_m \Delta V$  相同,

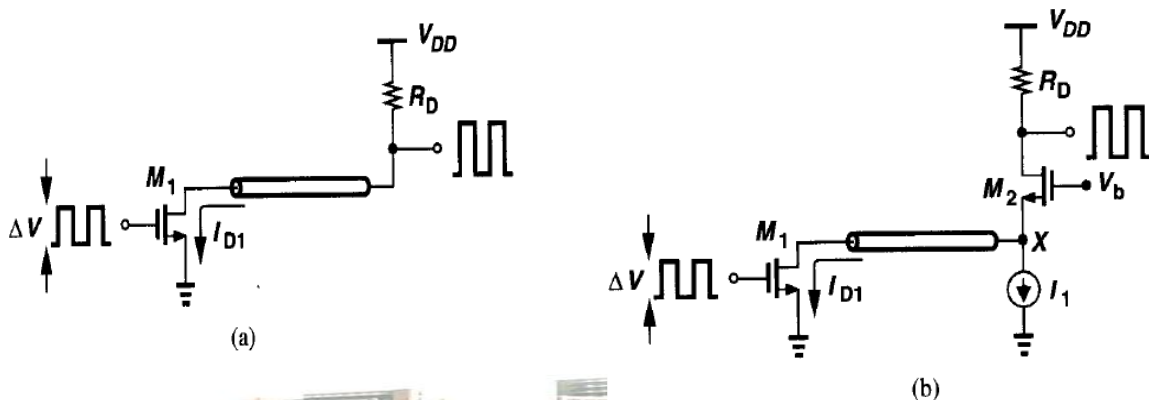
$$A_v = \frac{\partial V_{out}}{\partial V_{in}} = -g_m R_D \quad \text{公式形式相同, (a) 图 } R_D \text{ 为 } 50\Omega.$$

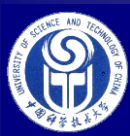
注意：图(b)共栅级电路M2的输入信号采用的是电流，而不是电压。

(b) 图X点看M2源极的小信号（交流）电阻  $\frac{\Delta V_X}{\Delta I_X} = \frac{1}{g_{m2} + g_{mb2}} = 50\Omega$

$$g_m = \sqrt{2\mu_n C_{ox} \frac{W}{L} I_D}$$

图(b) 由于M2的隔离，  
 $R_D$ 可远大于 50欧，  
提供更高的增益。





# 考虑MOS输出阻抗和信号源内阻情况下的CG

以下V表示交流小信号。

$$V_{out} = r_o \left( \frac{-V_{out}}{R_D} - g_m V_1 - g_{mb} V_{bs} \right) - \frac{V_{out}}{R_D} R_S + V_{in}$$

$$V_{bs} = V_1$$

$$V_1 - \frac{V_{out}}{R_D} R_S + V_{in} = 0$$

$$A_v = \frac{V_{out}}{V_{in}} = \frac{r_o (g_m + g_{mb}) + 1}{r_o + (g_m + g_{mb}) r_o R_S + R_S + R_D} R_D \quad (3.104)$$

若  $r_o = \infty, \quad g_m + g_{mb} \approx g_m$  则  $A_v = \frac{R_D}{\frac{1}{g_m} + R_S}$

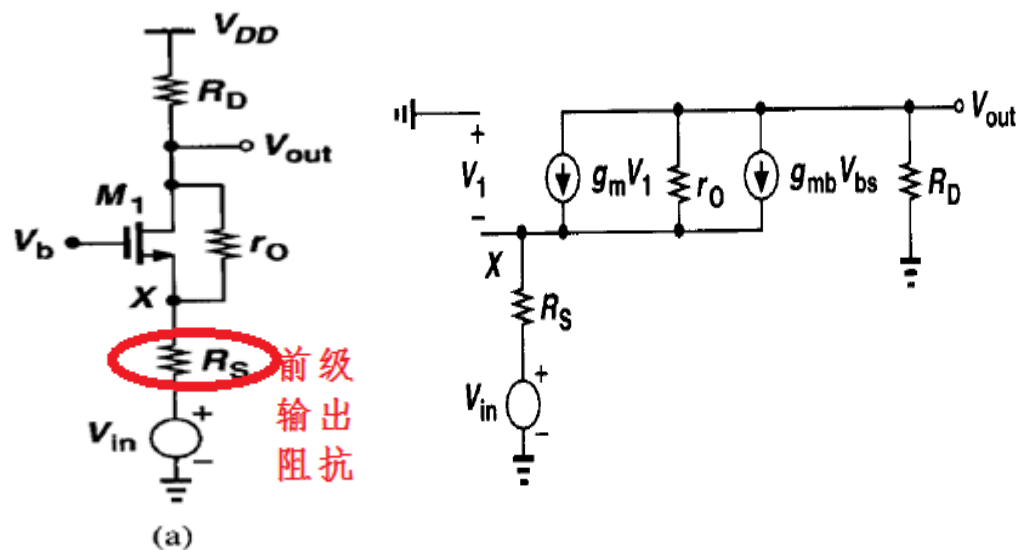
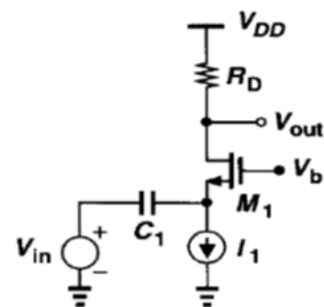


图3.43 输出电阻有限的共栅级



$$(3.999)$$





# CG 比较CS

- CS 
$$A_v = \frac{V_{out}}{V_{in}} = \frac{-r_o g_m}{r_o + (g_m + g_{mb})r_o R_S + R_S + R_D} R_D \quad (3.71)$$

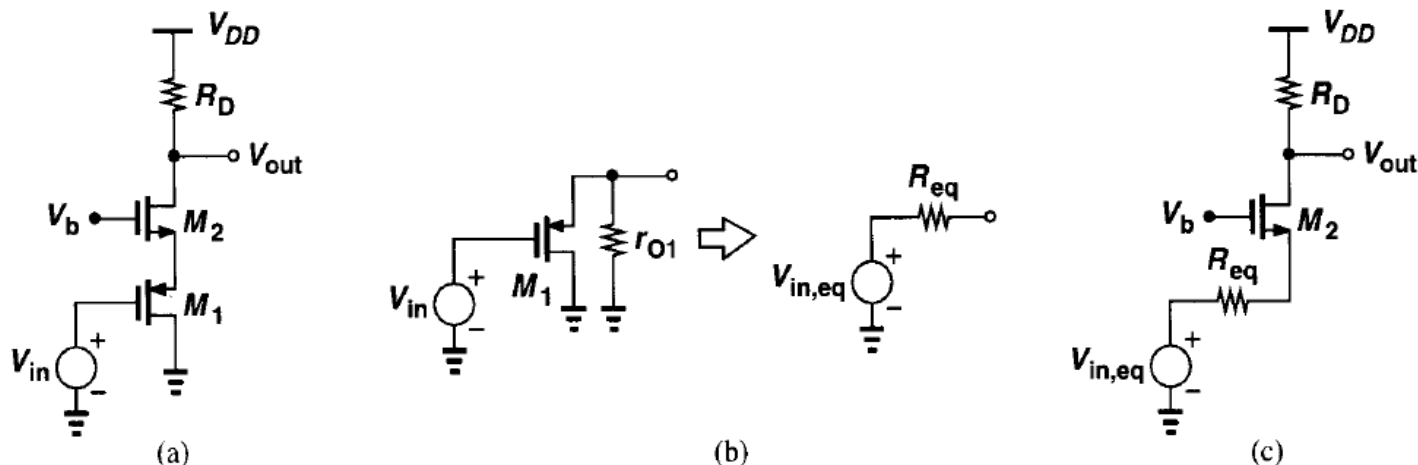
- CG 
$$A_v = \frac{V_{out}}{V_{in}} = \frac{r_o (g_m + g_{mb}) + 1}{r_o + (g_m + g_{mb})r_o R_S + R_S + R_D} R_D \quad (3.104)$$

CG增益略高一些，CG噪声比较大。



# 例3.11求电压增益

$\lambda \neq 0, \gamma \neq 0$



M1为PMOS源跟随器。将M1等效成戴维南电路，化为标准电路形式  
求M1的戴维南电路的等效电阻时， $V_{in}=0$ ，则M1成二极管，由式（3.24）

$$R_{eq} = \frac{1}{g_{m1}} \parallel r_{o1}$$

M1输出短路电流为  $g_{m1}V_{in}$ ，  
PMOS管  $g_{mb1}$  一般为0

$$M_1 \text{ 的开路输出电压 } V_{in,eq} = (g_{m1}V_{in}) R_{eq} = g_{m1} \frac{\frac{1}{g_{m1}} \times r_{o1}}{\frac{1}{g_{m1}} + r_{o1}} V_{in} \approx V_{in}$$

跟随器



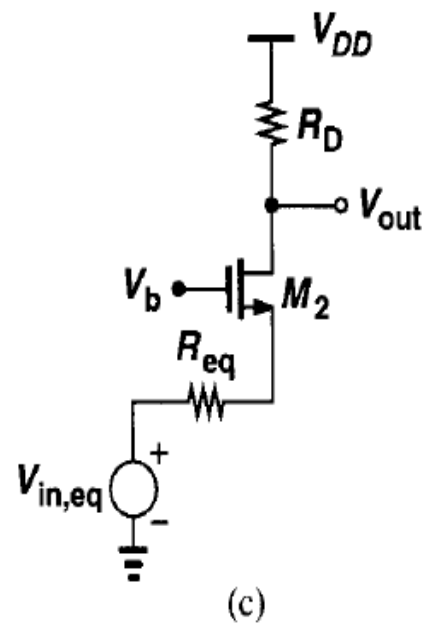
## 例3.11续

$$R_{eq} = \frac{1}{g_{m1}} \parallel r_{o1} = \text{公式中 } R_S$$

由CG:  $A_v = \frac{V_{out}}{V_{in}} = \frac{r_o(g_m + g_{mb}) + 1}{r_o + (g_m + g_{mb})r_o R_S + R_S + R_D} R_D$  (3.104)

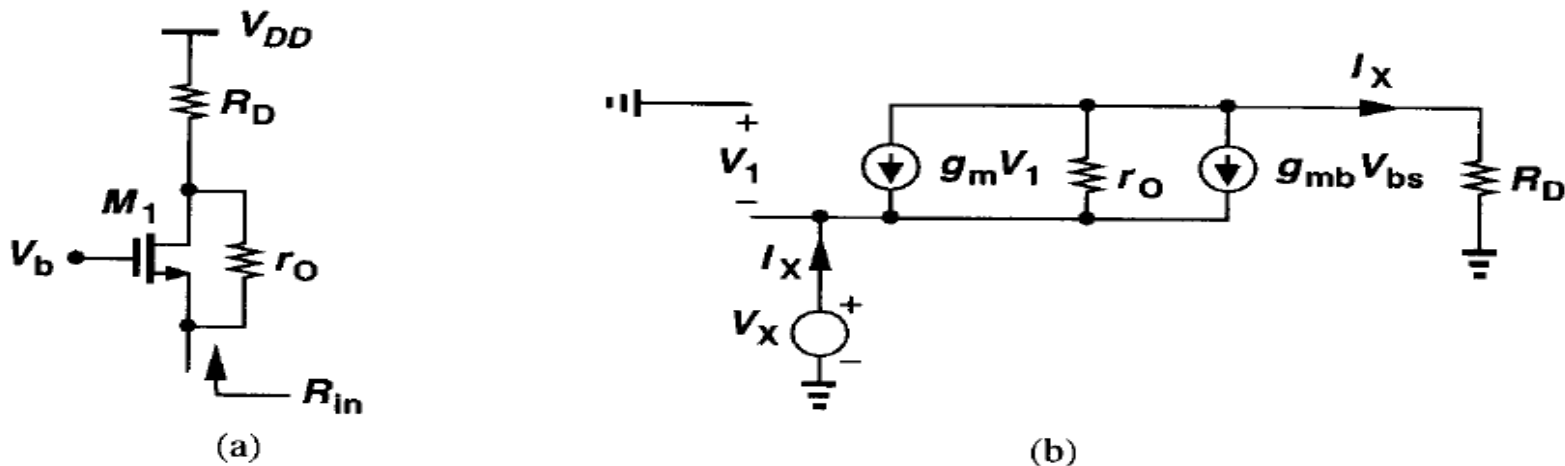
得:  $A_v = \frac{V_{out}}{V_{in}} = \frac{V_{out}}{V_{in,eq}} \times \frac{V_{in,eq}}{V_{in}}$

$$= \frac{r_{o2}(g_{m2} + g_{mb2}) + 1}{r_{o2} + [1 + (g_{m2} + g_{mb2})r_{o2}](\frac{1}{g_{m1}} \parallel r_{o1}) + R_D} R_D$$





# 共栅级输入电阻



**Figure 3.45** (a) Input resistance of a CG stage, (b) small-signal equivalent circuit.

$$V_1 = V_{bs} = -V_X \quad (\text{V小信号})$$

从下往上流过 $r_o$ 的电流:

$$\begin{aligned} I_X + g_m V_1 + g_{mb} V_{bs} &= I_X + g_m V_1 + g_{mb} V_1 \\ &= I_X - (g_m + g_{mb}) V_X \end{aligned}$$

$$V_X = [I_X - (g_m + g_{mb}) V_X] r_o + I_X R_D$$

共栅级输入电阻 (从源极端往MOS看)

$$R_{in} = \frac{V_X}{I_X} = \frac{R_D + r_o}{1 + (g_m + g_{mb}) r_o} \quad (3.109)$$



# CG极端情况: $R_D=0$ 和无穷大

$$R_{in} = \frac{V_X}{I_X} = \frac{R_D + r_o}{1 + (g_m + g_{mb})r_o}$$

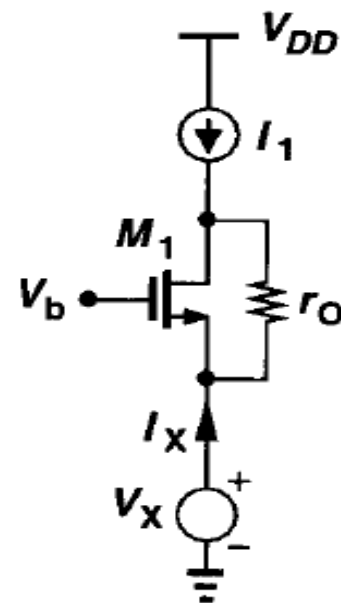
$$(1) R_D = 0 \text{ 或 } r_o \text{ 很大时 } R_{in} \approx \frac{1}{g_m + g_{mb}}$$

比较源跟随器输出阻抗 (3.85) 式相同

$$(2) \text{ 图3.46, } R_D = \infty \text{ 时 } R_{in} = \infty$$

原因: 交变小信号  $I_X = 0$

只有 $R_D$ 不很大情况下,  
共栅级输入电阻才会较小。



**Figure 3.46** Input resistance of a CG stage with ideal current source load.



## 例3.12 电流源负载CG的电压增益

直接耦合的共栅极。  $R_D = \infty$

由式 (3.104 )

$$\begin{aligned} A_v &= \frac{V_{out}}{V_{in}} \\ &= \frac{r_o(g_m + g_{mb}) + 1}{r_o + (g_m + g_{mb})r_oR_S + R_S + R_D} R_D \\ &= r_o(g_m + g_{mb}) + 1 \end{aligned}$$

与 $R_S$ 无关。

the small-signal voltage at node X is equal to  $V_{in}$

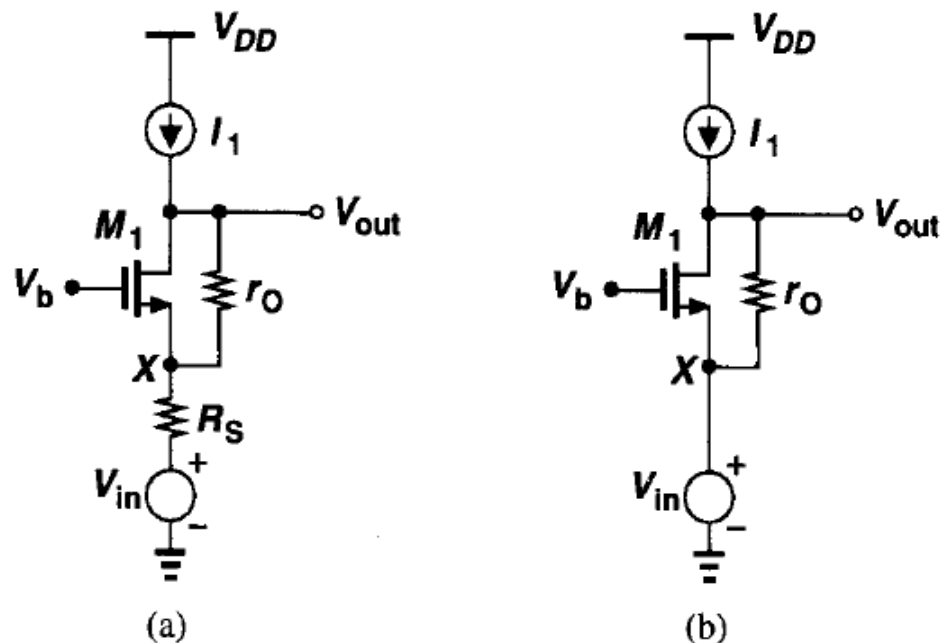
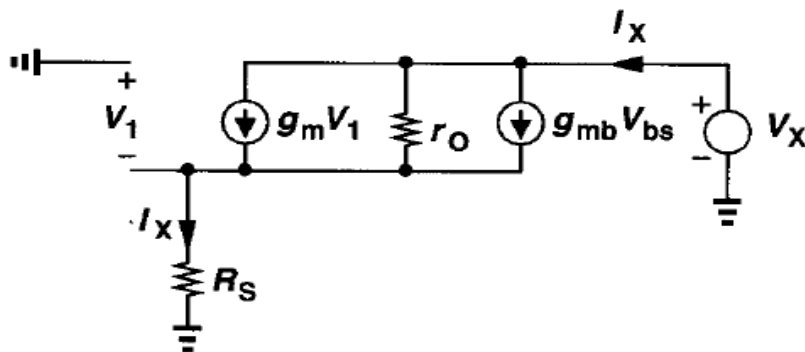


Figure 3.47



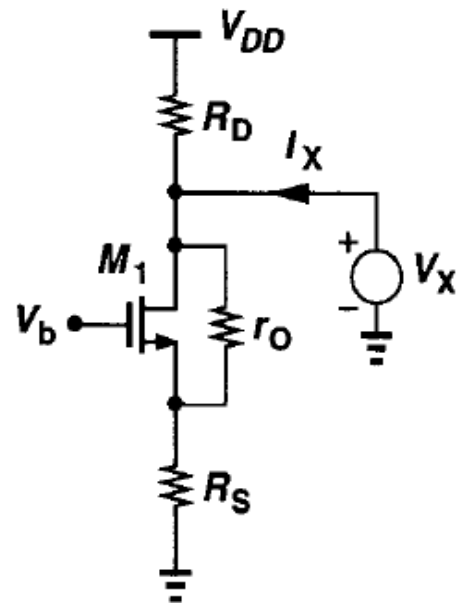
# output impedance of common-gate stage

与图3.22相同。



$$\text{式(3.62): } R_{out} = [1 + (g_m + g_{mb})r_o]R_S + r_o$$

Same as Degenerated CS



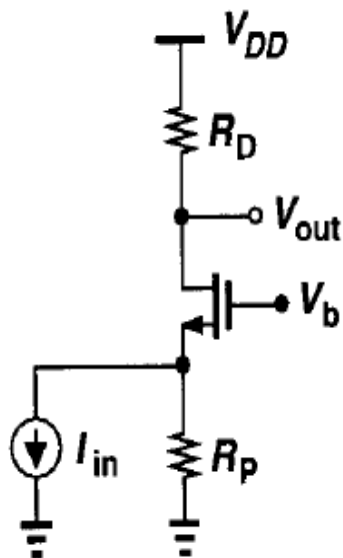
**Figure 3.48** Calculation of output resistance of a CG stage.

$$\text{共栅CG: } R_{out} = \frac{V_X}{I_X} = \{ [1 + (g_m + g_{mb})r_o]R_S + r_o \} \parallel R_D$$



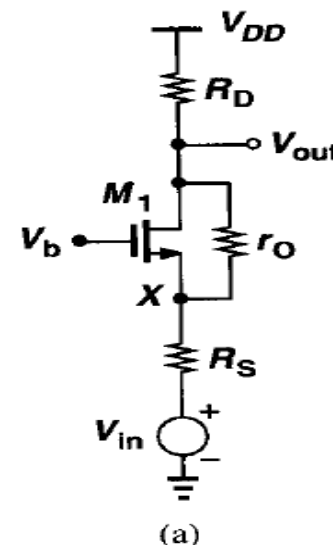
# 例3.13

Calculate  $V_{out}/I_{in}$  and the output impedance



已知右图，有式 (3.104) :  $A_v = \frac{V_{out}}{V_{in}}$

$$= \frac{r_o(g_m + g_{mb}) + 1}{r_o + (g_m + g_{mb})r_o R_S + R_S + R_D} R_D$$



$$\therefore \frac{V_{out}}{I_{in}} = \frac{V_{out}}{V_{in}} \frac{V_{in}}{I_{in}} = \frac{r_o(g_m + g_{mb}) + 1}{r_o + (g_m + g_{mb})r_o R_P + R_P + R_D} R_D \times R_P \quad (3.114)$$

$$R_{out} = \{ [1 + (g_m + g_{mb})r_o] R_P + r_o \} \parallel R_D$$





## 3.5 Cascode Stage(共源共栅)

输入器件M1将 $V_{in}$ 转换成漏电流。M2什么作用？

M2增大了从 $V_{out}$ 向下看的输出阻抗！

设计偏置 $V_b$ ，保证M1和M2（cascode器件）工作在饱和区：

$$V_X = V_b - V_{GS2}, \text{ 且 } V_X \geq V_{in} - V_{TH1}$$

$$\text{即 } V_b - V_{GS2} \geq V_{in} - V_{TH1}$$

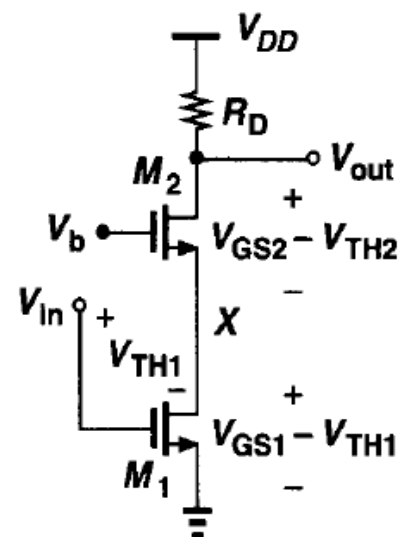
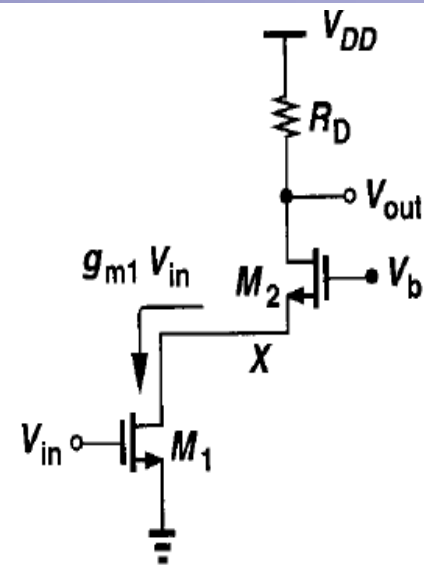
$$\therefore V_b \geq V_{in} - V_{TH1} + V_{GS2}$$

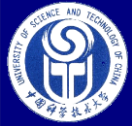
$$\therefore V_{out} \geq V_b - V_{TH2} \geq V_{in} - V_{TH1} + V_{GS2} - V_{TH2}$$

$$\text{即 } V_{out} \geq M1\text{过驱动电压} + M2\text{过驱动电压}$$

**直筒式CASCODE.**

输入器件和cascode器件是同一类型MOS





# 分析: $V_{in}$ 从 $0 \Rightarrow V_{DD}$

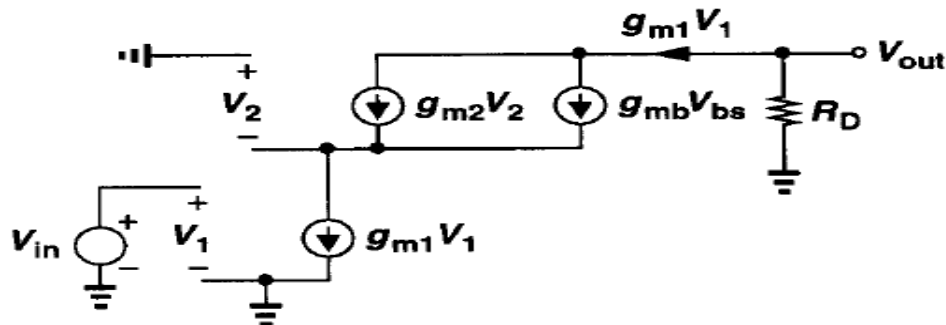
(1)  $V_{in} \leq V_{TH1}$ ,  $M_1$ 和 $M_2$ 截止,  $V_{out} = V_{DD}$

$$I_D = 0, \quad V_{GS2} - V_{TH} = 0$$

$$\therefore V_X = V_b - V_{TH2}$$

(2)  $V_{in} \geq V_{TH1}$ , 当 $V_{in} \uparrow \Rightarrow I_D \uparrow \Rightarrow V_{out} \downarrow$  &  $V_{GS2} \uparrow \Rightarrow V_X \downarrow$

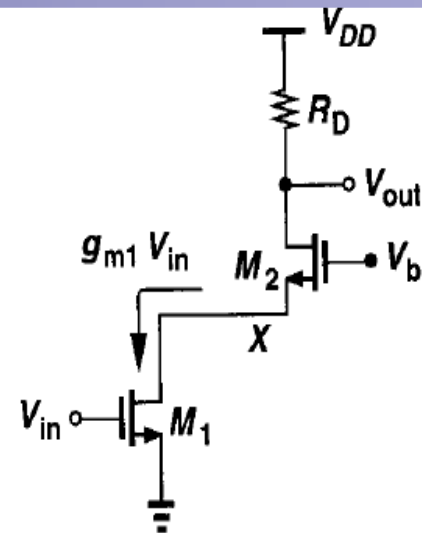
$M_1$ 和 $M_2$ 在饱和区时:  $A_v = -g_m R_D$ , 与CS相同



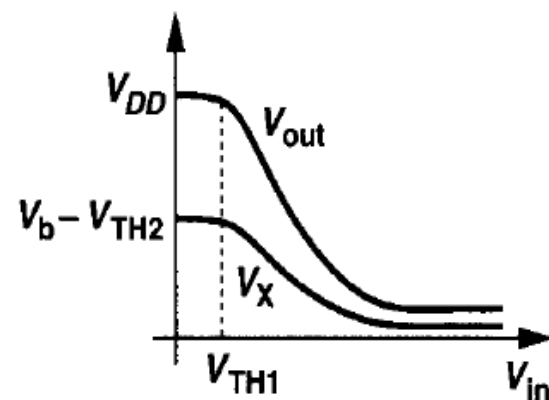
**Figure 3.53** Small-signal equivalent circuit of cascode stage.

(3)  $V_{in}$ 增加到很大时,  $M_1$ 或 $M_2$ 进入线性区。  
 $V_b$ 比较小时,  $M_1$ 先进入线性区。

$M_2$ 进入线性区时  $V_{out} \approx V_X$



$$I_D = \frac{\mu_n C_{ox}}{2} \frac{W}{L} (V_{GS} - V_{TH})^2$$





## 例3.14 calculate the voltage gain

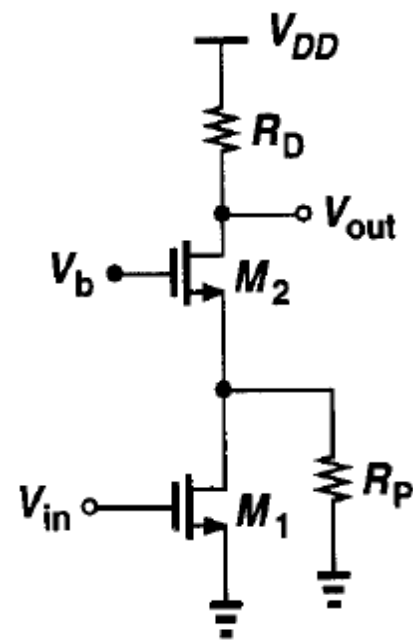
M<sub>1</sub>的小信号漏电流（受控电流源） $g_{m1}V_{in}$ ，被 $R_p$ （例如 $r_{o1}$ ，或节点寄生电容）和向M<sub>2</sub>源极看进去的阻抗 $1/(g_{m2}+g_{mb2})$ 分流。

$$\text{小信号 } I_{D2} = g_{m1}V_{in} \frac{R_p}{\frac{1}{g_{m2} + g_{mb2}} + R_p} = g_{m1}V_{in} \frac{(g_{m2} + g_{mb2})R_p}{1 + (g_{m2} + g_{mb2})R_p}$$

$$A_v = \frac{-I_{D2}(R_D || R_{out})}{V_{in}} \approx \frac{-I_{D2}R_D}{V_{in}}$$

$$= -g_{m1} \frac{(g_{m2} + g_{mb2})R_p R_D}{1 + (g_{m2} + g_{mb2})R_p},$$

$V_{out}$ 向下看的输出阻抗 $R_{out}$ 很大





# cascode结构的重要特性：输出阻抗大

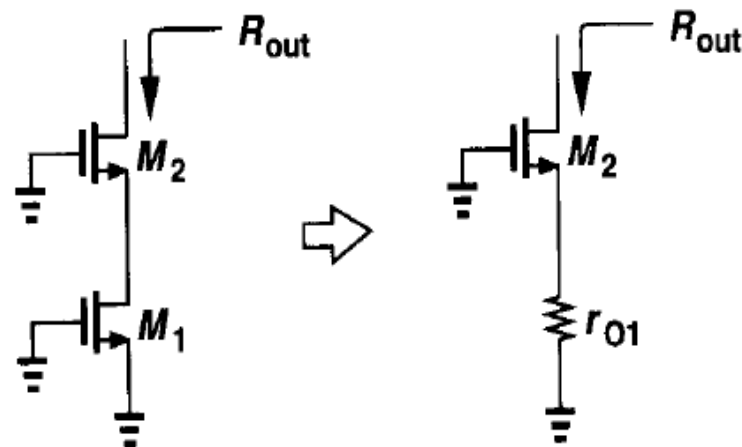
式 (3.60) :

$$R_{out} = [1 + (g_{m2} + g_{mb2})r_{o2}]r_{o1} + r_{o2}$$

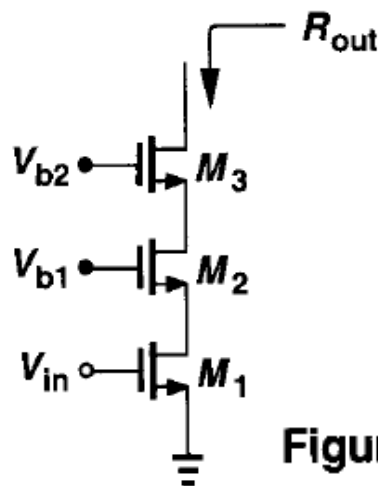
$$\approx (g_{m2} + g_{mb2})r_{o2}r_{o1}$$

将共源 $M_1$ 输出电阻 $r_{o1}$ 提高

了 $(g_{m2} + g_{mb2})r_{o2}$



**Figure 3.55** Calculation of output resistance of cascode stage.



将共源 $M_1$ 输出电阻 $r_{o1}$ 提高

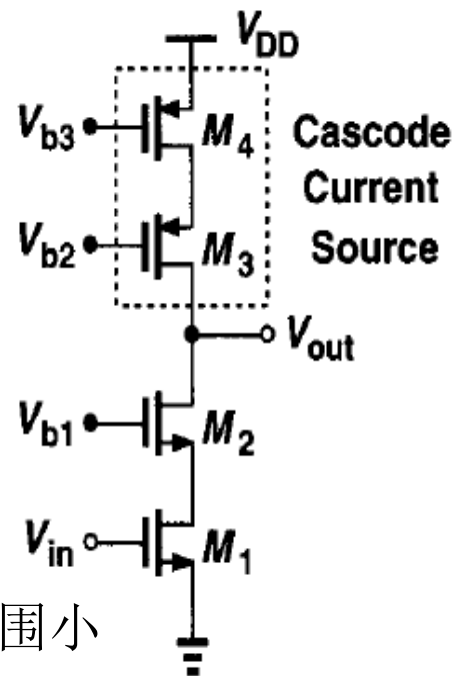
$$(g_{m3} + g_{mb3})r_{o3}(g_{m2} + g_{mb2})r_{o2}$$

但现代工艺电源电压很低，此结构难以应用

**Figure 3.56** Triple cascode.



$$A_v \approx -g_{m1}R_{out} = -g_{m1}[g_{m2}r_{o2}r_{o1} \parallel g_{m3}r_{o3}r_{o4}]$$



## 直流输入电压动态范围小

**Figure 3.60** NMOS cascode amplifier with PMOS cascode load.



# Shielding property

设 $M_1M_2$ 相同,  $M_3M_4$ 相同, 都是饱和区。

图 (a) :  $V_X - V_Y = \Delta V$

$$I_{D1} - I_{D2} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_b - V_{TH})^2 (\lambda V_{DS1} - \lambda V_{DS2})$$

$$= \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_b - V_{TH})^2 \lambda \Delta V_{XY}$$

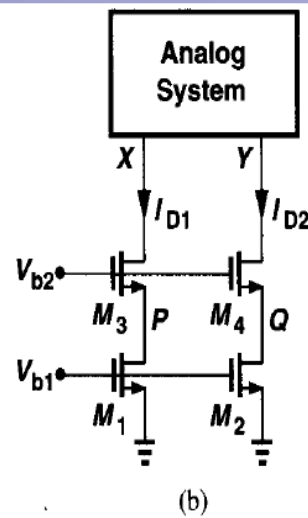
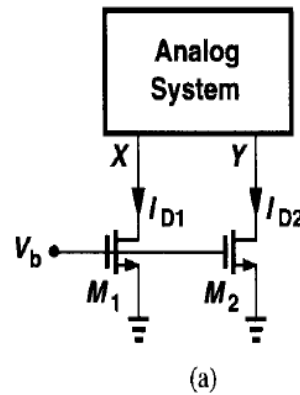


Figure 3.61

图 (b) :  $\Delta V_{PQ} = \Delta V_{XY} \frac{r_{o1}}{R_{Xout}} = \Delta V_{XY} \frac{r_{o1}}{[1 + (g_{m3} + g_{mb3})r_{o3}]r_{o1} + r_{o3}}$

$\approx \Delta V_{XY} \frac{1}{(g_{m3} + g_{mb3})r_{o3}}$ , PQ变化小, 即 $M_3$ 屏蔽了X点对P点的影响。

$$I_{D1} - I_{D2} = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_b - V_{TH})^2 \lambda \Delta V_{PQ}$$

$$= \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_b - V_{TH})^2 \lambda \Delta V_{XY} \frac{1}{(g_{m3} + g_{mb3})r_{o3}}$$

**CASCODE结**  
构使电流失配  
大大减少。



# 折叠式共源共栅 Folded cascode

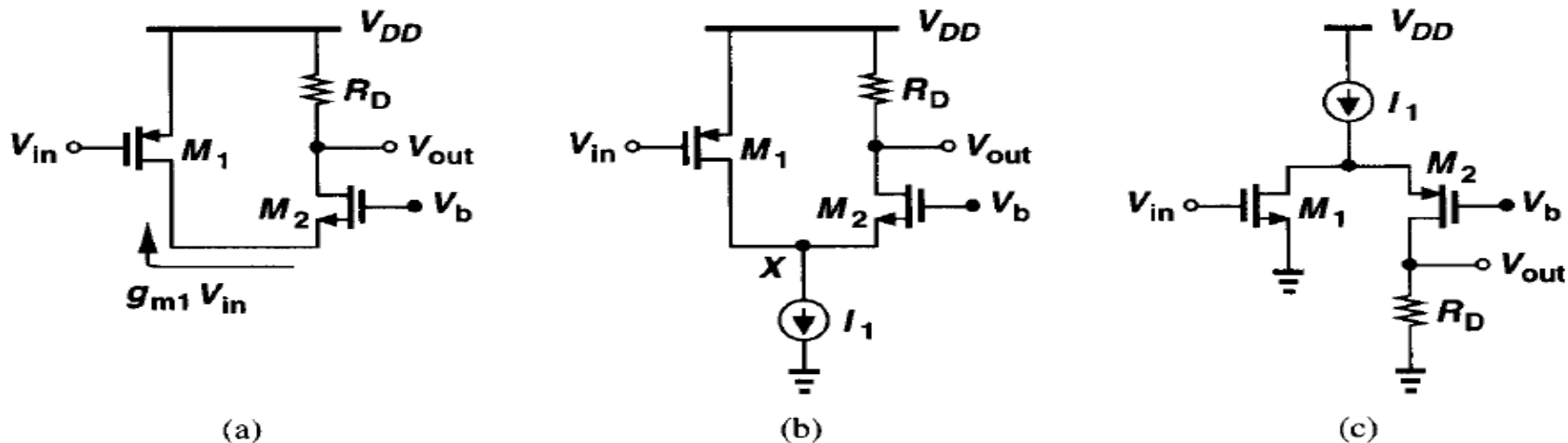


图3.63 (a) PMOS和NMOS组成折叠CASCODE（小信号电流回路）

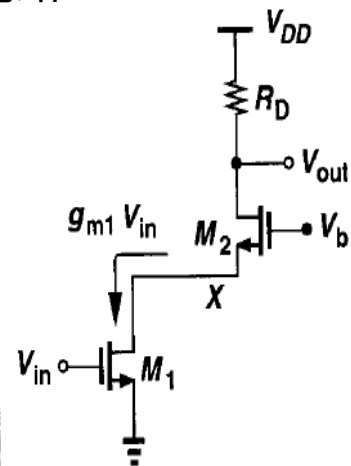
(b)有直流通路的 PMOS作输入器件的折叠式共源共栅电路

(c)有直流通路的NMOS作输入器件的折叠式共源共栅电路

输入器件和cascode器件不是同一类型。

由于 $I_1$ 电流源，若 $I_{D1}$ 增大则 $I_{D2}$ 减小。

输入电压范围比直筒式cascode大。





# Folded cascade 大信号分析

(1)  $V_{in} > V_{DD} - |V_{TH1}|$ ,  $M_1$ 截止。电流源 $I_1$ 全部流过 $R_D$ ,  $V_{out}$ 最低。  $V_{out} = V_{DD} - I_1 R_D$

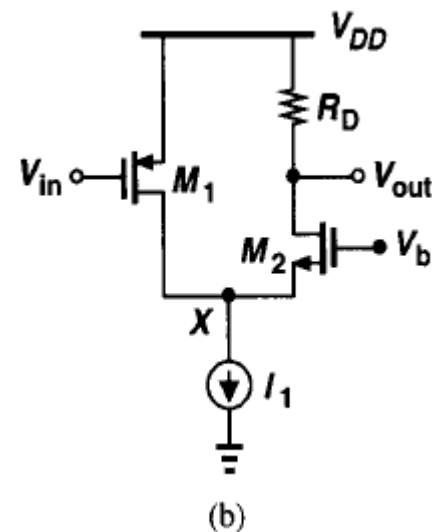
$I_1 R_D$ 不能过大, 否则 $M_2$ 易进入线性区

(2)  $V_{in} < V_{DD} - |V_{TH1}|$  时,  $M_1$ 工作在饱和区。

$$I_{D2} = I_1 - \frac{1}{2} \mu_p C_{ox} \left( \frac{W}{L} \right)_1 (V_{DD} - V_{in} - |V_{TH1}|)^2$$

$$V_{out} = V_{DD} - I_{D2} R_D$$

$$= V_{DD} - I_1 R_D - \frac{1}{2} \mu_p C_{ox} \left( \frac{W}{L} \right)_1 (V_{DD} - V_{in} - |V_{TH1}|)^2 R_D$$



$$I_{D1} + I_{D2} = I_1$$

当 $V_{in}$ 下降使 $I_{D2} = 0$ 时,  $V_{out} = V_{DD}$

$$I_1 - \frac{1}{2} \mu_p C_{ox} \left( \frac{W}{L} \right)_1 (V_{DD} - V_{in1} - |V_{TH1}|)^2 = 0$$

$$\text{最小输入 } V_{in1} = V_{DD} - \sqrt{\frac{2I_1}{\mu_p C_{ox} \left( \frac{W}{L} \right)_1}} - |V_{TH1}|$$

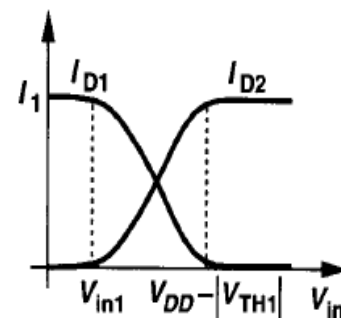
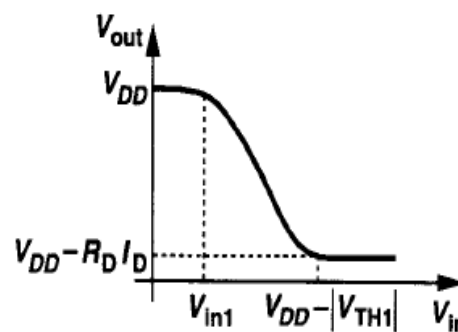


Figure 3.64 Large-signal characteristics of folded cascode.





# 折叠管的输出阻抗

Calculate the output impedance of the folded cascode shown in Fig. 3.65 where  $M_3$  operates as a current source.

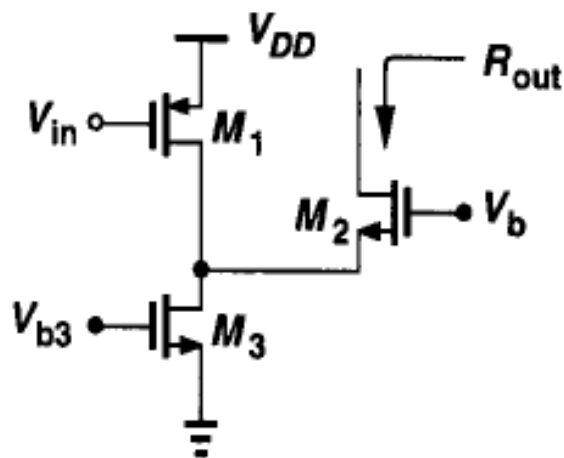
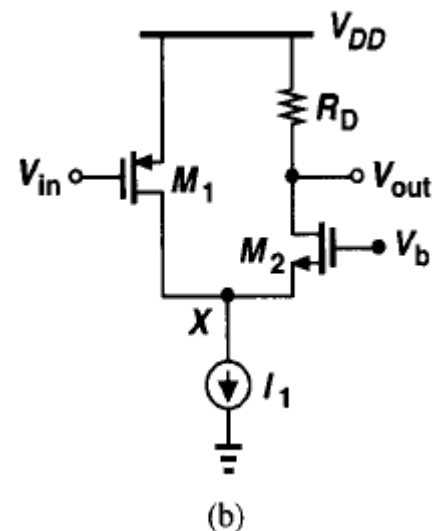


Figure 3.65



## Solution

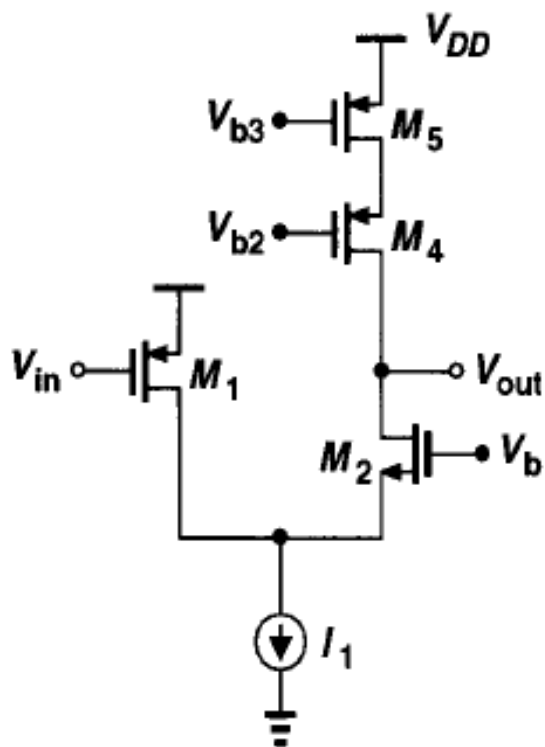
Using (3.60), we have

$$R_{out} = [1 + (g_{m2} + g_{mb2})r_{o2}](r_{o1} \parallel r_{o3}) + r_{o2}. \quad (3.136)$$

Thus, the circuit exhibits an output impedance lower than that of a nonfolded cascode.



# The load of a folded cascode



记 $M3$ 组成尾电流源:  $I_1$

$$R_{out} = \{ [1 + (g_{m2} + g_{mb2})r_{o2}](r_{o1} \parallel r_{o3}) + r_{o2} \} \\ \parallel \{ [1 + g_{m4}r_{o4}]r_{o5} + r_{o4} \} \\ \approx (g_{m2} + g_{mb2})r_{o2}(r_{o1} \parallel r_{o3}) \parallel g_{m4}r_{o4}r_{o5}$$

$$A_v = -g_{m1}R_{out} \\ = -g_{m1} \mathbf{[ (g_{m2} + g_{mb2})r_{o2}(r_{o1} \parallel r_{o3}) \parallel g_{m4}r_{o4}r_{o5} ]}$$

**Figure 3.66** Folded cascode with cascode load.



# 本章知识要点

- 共源CS、源跟随器SF、CASCODE的低频增益和输出电阻
- 共栅CG的低频增益、输入与输出电阻
- MOS二极管的等效电阻
- CS各种负载情况的优缺点