Boost.Graph tutorial

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1 Introduction

I needed this tutorial in 2006, when I started experimenting with Boost.Graph. More specifically, I needed a tutorial that:

- Orders concepts chronologically
- Increases complexity gradually
- Shows complete pieces of code

What I had were the book [2] and the Boost.Graph website, both did not satisfy these requirements. This tutorial is intended to take the reader to the level of understanding the book [2] and the Boost.Graph website require.

1.1 Code snippets

For every concept, I will show

- the 'do' function: a function that achieves a goal, for example 'create_empty_undirected_graph'
- the 'demo' function: a function that demonstrates how to call the first, for example 'demonstrate create empty undirected graph'

I enjoy to show concepts by putting those in (long-named) functions. These functions sometimes border the trivial, by, for example, only calling a Boost.Graph function. On the other hand, these functions have more English-sounding names, resulting in demonstration code that is readable.

All coding snippets are taken from compiled C++ code.

1.2 Coding style

I use the coding style from the Core C++ Guidelines. At the time of this writing, the Core C++ Guidelines were still in early development, so I can only hope the conventions I then chose to follow are still Good Ideas.

I prefer to use the keyword auto over doubling the lines of code for using statements. Because the 'do' functions return an explicit data type, these can be used for reference. If you really want to know a type, you can use the 'get_type_name' function (chapter 11.1). On the other hand, I am explicit of which data types I choose: I will prefix the types by thir namespace, so to distinguish between types like 'std::array' and 'boost::array'.

1.3 Feedback

I have tried hard to strictly follow the style as described above. If you find I deviated from these decisions somewhere, I would be grateful if you'd let know.

2 Building a graph without properties

Boost.Graph is about creating graphs. In this chapter we create the simplest of graphs, in which edges and nodes have no properties (e.g. having a name). We will build:

- An empty (directed) graph, which is the default type: see chapter 2.1
- An empty (undirected) graph: see chapter 2.2
- K_2 , an undirected graph with two vertices and one edge, chapter 2.12

In the process, some basic (sometimes bordering trivial) functions are shown:

- Adding a vertex: see chapter 2.3
- Getting all vertices: see chapter 2.5
- Getting all vertex descriptors: see chapter 2.6
- Adding an edge: see chapter 2.7
- Getting all edges: see chapter 2.9
- Getting all edge descriptors: see chapter 2.11

These functions are mostly there for completion and showing which data types are used.

2.1 Creating an empty (directed) graph

Let's create a trivial empty graph!

Algorithm 1 shows the function to create an empty (directed) graph.

Algorithm 1 Creating an empty (directed) graph

```
#include <boost/graph/adjacency_list.hpp>
boost::adjacency_list <>
create_empty_directed_graph() noexcept
{
   return boost::adjacency_list <> ();
}
```

Algorithm 2 demonstrates the 'create_empty_directed_graph' function.

Algorithm 2 Demonstration of 'create empty directed graph'

```
#include "create_empty_directed_graph.h"

void create_empty_directed_graph_demo() noexcept
{
   const auto g = create_empty_directed_graph();
}
```

Congratulations, you've just created a boost::adjacency_list with its default template arguments. For your reference, these default template argument denote that you've just created a graph, in which:

- The out edges are stored in a std::vector
- The vertices are stored in a std::vector
- The edges have a direction
- The vertices, edges and graph have no properties
- The edges are stored in a std::list

The boost::adjacency_list is the most commonly used graph type, the other is the boost::adjacency_matrix.

2.2 Creating an empty undirected graph

Let's create another trivial empty graph! This time, we make the graph undirected.

Algorith 3 shows how to create an undirected graph.

Algorithm 3 Creating an empty undirected graph

```
#include <boost/graph/adjacency_list.hpp>
boost:: adjacency_list <
   boost:: vecS,
  boost:: vecS,
  boost:: undirectedS
>
create_empty_undirected_graph() noexcept
{
  return boost:: adjacency_list <
   boost:: vecS,
   boost:: vecS,
   boost:: undirectedS
  >();
}
```

Algorithm 4 demonstrates the 'create empty undirected graph' function.

Algorithm 4 Demonstration of 'create_empty_undirected_graph'

```
#include "create_empty_undirected_graph.h"

void create_empty_undirected_graph_demo() noexcept
{
   const auto g = create_empty_undirected_graph();
}
```

Congratulations, you've just created an undirected graph in which:

- The out edges are stored in a std::vector. This way to store out edges is selected by the first 'boost::vecS'
- The vertices are stored in a std::vector. This way to store vertices is selected by the second 'boost::vecS'
- The graph is undirected. This directionality is selected for by the third template argument, 'boost::undirectedS'
- Vertices, edges and graph have no properties
- Edges are stored in a std::list

The difference between directed and undirected graphs is in the edges: in an undirected graph, an edge connects two vertices without any directionality. In a directed graph, an edge goes from a certain vertex, its source, to another (which may actually be the same), its target.

2.3 Add a vertex

Empty graphs are nice, now its time to add a vertex!

To add a vertex to a graph, the boost::add_vertex function is used as shows in algorithm 5.

Algorithm 5 Adding a vertex to a graph

```
#include <boost/graph/adjacency_list.hpp>
template <typename graph>
void add_vertex(graph& g)
{
   boost::add_vertex(g);
}
```

Algorithm 6 shows how to add a vertex to a directed and undirected graph.

Algorithm 6 Demonstration of the 'add vertex' function

```
#include "add_vertex.h"
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"

void add_vertex_demo() noexcept
{
   auto g = create_empty_undirected_graph();
   add_vertex(g);

auto h = create_empty_directed_graph();
   add_vertex(h);
}
```

Note that boost::add_vertex (in the 'add_vertex' function) returns a vertex descriptor, which is ignored for now. Vertex descriptors are looked at in more details at the chapter 2.4.

2.4 Vertex descriptors

A vertex descriptor is a handle to a vertex within a graph. Vertex descriptors can be obtained by:

• dereference a vertex iterator, see chapter 2.6

Vertex descriptors are used to:

- add and edge between two vertices, see chapter 2.7
- obtain properties of vertex a vertex, for example the vertex its out degrees (chapter 23), the vertex its name (chapter 33), or a custom vertex property (chapter 63)

In this tutorial, vertex descriptors have named prefixed with 'vd_', for example 'vd_1'.

2.5 Get the vertices

You cannot get the vertices. This may sound unexpected, as it must be possible to work on the vertices of a graph. Working on the vertices of a graph is done throught these steps:

- Obtain a vertex iterator pair from the graph
- Dereference a vertex iterator to obtain a vertex descriptor

boost::vertices is used to obtain a vertex iterator pair, as shown in algorithm 7. The first vertex iterator points to the first vertex (its descriptor, to be precise), the second points to beyond the last vertex. In this tutorial, vertex iterator pairs have named prefixed with 'vip_', for example 'vip_1'.

Algorithm 7 Get the vertex iterators of a graph

```
#include <boost/graph/adjacency_list.hpp>

template <class graph>
std::pair<
   typename graph::vertex_iterator,
   typename graph::vertex_iterator
>
get_vertices(const graph& g)
{
   return boost::vertices(g);
}
```

These vertex iterators can be dereferenced to obtain the vertex descriptors. Note that 'get_vertices' will not be used often in isolation: usually one obtains the vertex descriptors immediatly. Just for your references, algorithm 8 demonstrates of the 'get_vertices' function, by showing that the vertex iterators of an empty graph point to the same location.

Algorithm 8 Demonstration of 'get vertices'

```
#include <cassert>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_vertices.h"

void get_vertices_demo() noexcept
{
    const auto g = create_empty_undirected_graph();
    const auto vip_g = get_vertices(g);
    assert(vip_g.first == vip_g.second);

const auto h = create_empty_directed_graph();
    const auto vip_h = get_vertices(h);
    assert(vip_h.first == vip_h.second);
}
```

2.6 Get all vertex descriptors

Vertex descriptors are the way to manipulate those vertices. Let's get the all!

Vertex descriptors are obtained from dereferencing vertex iterators. Algorithm 9 shows how to obtain all vertex descriptors from a graph.

Algorithm 9 Get all vertex descriptors of a graph

```
#include <vector>
#include "boost/graph/graph_traits.hpp"

template <class graph>
std::vector<
    typename boost::graph_traits<graph>::vertex_descriptor
> get_vertex_descriptors(const graph& g) noexcept
{
    using boost::graph_traits;
    std::vector<
        typename graph_traits<graph>::vertex_descriptor
> v;
    for (auto vi = vertices(g);
        vi.first != vi.second;
        ++vi.first)
    {
        v.emplace_back(*vi.first);
    }
    return v;
}
```

The 'get_vertex_descripors' function shows an important concept of the Boost.Graph library: boost::vertices returns two vertex iterators, which in turn can be dereferenced to obtain the vertex descriptors. Algorithm 10 demonstrates that an empty graph has no vertex descriptors.

Algorithm 10 Demonstration of 'get vertex descriptors'

```
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_vertex_descriptors.h"

void get_vertex_descriptors_demo() noexcept
{
    const auto g = create_empty_undirected_graph();
    const auto vds_g = get_vertex_descriptors(g);
    assert(vds_g.empty());

const auto h = create_empty_directed_graph();
    const auto vds_h = get_vertex_descriptors(h);
    assert(vds_h.empty());
}
```

2.7 Add an edge

To add an edge to a graph, two vertex descriptors are needed. A vertex descriptor is a handle to the vertex with in graph (vertex descriptors are looked at in more details in chapter 2.4). Algorithm 11 adds two vertices to a graph, and connects these two using boost::add edge:

Algorithm 11 Adding (two vertices and) an edge to a graph

This algorithm only shows how to add an isolated edge to a graph, instead of allowing for graphs with higher connectivities. The function boost::add_vertex returns a vertex descriptor, which I prefix with 'vd'. The function boost::add_edge returns a std::pair, consisting of an edge descriptor and a boolean success indicator. In algorithm 11 we assert that this insertion was successfull. Insertion can fail if an edge is already present and duplicates are not allowed.

A demonstration of add_edge is shown in algorith 12, in which an edge is added to both a directed and undirected graph.

Algorithm 12 Demonstration of add edge

```
#include "add_edge.h"
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"

void add_edge_demo() noexcept
{
   auto g = create_empty_undirected_graph();
   add_edge(g);

   auto h = create_empty_directed_graph();
   add_edge(h);
}
```

2.8 boost::add edge result

When using the function 'boost::add_edge', a 'std::pair<edge_descriptor,bool>' is returned. It contains both the edge descriptor (see chapter 2.10) and a boolean indicating insertion success.

In this tutorial, boost::add_edge results have named prefixed with 'aer_', for example 'aer_1'.

2.9 Getting the edges

You cannot get the edges directly. Working on the edges of a graph is done throught these steps:

- Obtain an edge iterator pair from the graph
- Dereference an edge iterator to obtain an edge descriptor

boost::edges is used to obtain an edge iterator pair. The first edge iterator points to the first edge (its descriptor, to be precise), the second points to beyond the last edge. In this tutorial, edge iterator pairs have named prefixed with 'eip_', for example 'eip_1'.

Algorithm 13 Get the edge iterators of a graph

```
#include <boost/graph/adjacency_list.hpp>
template <class graph>
std::pair<
   typename graph::edge_iterator,
   typename graph::edge_iterator
>
get_edges(const graph& g)
{
   return boost::edges(g);
}
```

These edge iterators can be dereferenced to obtain the edge descriptors. Note that this function will not be used often in isolation: usually one obtains the edge descriptors immediatly.

Algorithm 14 demonstrates 'get_edges' by showing that both iterators of the edge iterator pair point to the same location, when the graph is empty.

Algorithm 14 Demonstration of get edges

```
#include <cassert>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_edges.h"

void get_edges_demo() noexcept
{
   const auto g = create_empty_undirected_graph();
   const auto eip_g = get_edges(g);
   assert(eip_g.first == eip_g.second);

auto h = create_empty_directed_graph();
   const auto eip_h = get_edges(h);
   assert(eip_h.first == eip_h.second);
}
```

2.10 Edge descriptors

An edge descriptor is a handle to an edge within a graph. Edge descriptors are used to:

• obtain the name, or other properties, of an edge

In this tutorial, edge descriptors have named prefixed with 'ed_', for example 'ed_1'.

2.11 Get all edge descriptors

Obtaining all edge descriptors is not as simple of a function as you'd guess:

Algorithm 15 Get all edge descriptors of a graph

```
#include <vector>
#include "boost/graph/graph_traits.hpp"

template <class graph>
std::vector<
    typename boost::graph_traits<graph>::edge_descriptor
> get_edge_descriptors(const graph& g) noexcept
{
    using boost::graph_traits;
    std::vector<
        typename graph_traits<graph>::edge_descriptor
> v;
    for (auto vi = edges(g);
        vi.first != vi.second;
        ++vi.first)
    {
        v.emplace_back(*vi.first);
    }
    return v;
}
```

This does show an important concept of the Boost.Graph library: boost::edges returns to vertex iterators, that can be dereferenced to obtain the vertex descriptors

Algorithm 16 demonstrates the 'get_edge_descriptor', by showing that empty graphs do not have any edge descriptors.

Algorithm 16 Demonstration of get edge descriptors

```
#include <cassert>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_edge_descriptors.h"

void get_edge_descriptors_demo() noexcept
{
   const auto g = create_empty_directed_graph();
   const auto eds_g = get_edge_descriptors(g);
   assert(eds_g.empty());

   const auto h = create_empty_undirected_graph();
   const auto eds_h = get_edge_descriptors(h);
   assert(eds_h.empty());
}
```

2.12 Creating K_2 , a fully connected graph with two vertices

Finally, we are going to create a graph!

To create a fully connected graph with two vertices (also called K_2), one needs two vertices and one (undirected) edge, as depicted in figure 1.



Figure 1: K_2 : a fully connected graph with two vertices named a and b

To create K_2 , the following code can be used:

Algorithm 17 Creating K_2 as depicted in figure 1

```
#include "create_empty_undirected_graph.h"

boost:: adjacency_list <
   boost:: vecS,
  boost:: vecS,
  boost:: undirectedS
>
create_k2_graph() noexcept
{
  auto g = create_empty_undirected_graph();
  const auto vd_a = boost:: add_vertex(g);
  const auto vd_b = boost:: add_vertex(g);
  const auto aer = boost:: add_edge(vd_a, vd_b, g);
  assert (aer.second);
  return g;
}
```

To save defining the type, we call the 'create_empty_undirected_graph' function. The vertex descriptors (see chapter 2.4) created by two boost::add_vertex calls are stored to add an edge to the graph. From boost::add_edge its return type (see chapter 2.8), it is only checked that insertion has been successfull.

Note that the graph lacks all properties: nodes do not have names, nor do edges.

Algorithm 18 demonstrates how to 'create_k2_graph' and uses all functions currently described by this tutorial.

Algorithm 18 Demonstration of 'create k2 graph'

```
#include <cassert>
#include <iostream>
#include "create k2 graph.h"
#include "get edge descriptors.h"
#include "get_edges.h"
#include "get_vertex_descriptors.h"
#include "get_vertices.h"
void create k2 graph demo() noexcept
  const auto g = create k2 graph();
  const auto vip = get_vertices(g);
  assert(vip.first != vip.second);
  const auto vds = get vertex descriptors(g);
  assert(vds.size() == 2);
  const auto eip = get edges(g);
  assert (eip. first != eip. second);
  const auto eds = get_edge_descriptors(g);
  assert(eds.size() == 1);
```

3 Working on a graph without properties

Graphs without edge and vertex properties have plenty of things to measure. These simple getters and setters will allow you to work with, test and debug your code:

- Counting the number of vertices: see chapter 3.1
- Counting the number of edges: see chapter 3.2
- Getting the vertices' out degrees: see chapter 3.3

3.1 Counting the number of vertices

Use boost::num vertices, as shown here:

Algorithm 19 Count the numbe of vertices

```
#include <boost/graph/adjacency_list.hpp>

///Get the number of vertices a graph has
template <class graph>
int get_n_vertices(const graph& g)
{
   return static_cast<int>(boost::num_vertices(g));
}
```

The function 'get_n_vertices' is demonstrated in algorithm 20, to measure the number of vertices of an empty (zero) and K_2 (two) graph.

Algorithm 20 Demonstration of the 'get n vertices' function

```
#include "get_n_vertices.h"

#include <cassert>

#include "create_empty_directed_graph.h"

#include "create_k2_graph.h"

#include "get_n_vertices.h"

void get_n_vertices_demo() noexcept
{
    const auto g = create_empty_directed_graph();
    assert(get_n_vertices(g) == 0);

    const auto h = create_k2_graph();
    assert(get_n_vertices(h) == 2);
}
```

3.2 Counting the number of edges

Use boost::num edges, as shown here:

Algorithm 21 Count the number of edges

```
#include <boost/graph/adjacency_list.hpp>

///Get the number of edges a graph has
template <class graph>
int get_n_edges(const graph& g)
{
   return static_cast<int>(boost::num_edges(g));
}
```

The function 'get_n_edges' is demonstrated in algorithm 22, to measure the number of vertices of an empty (zero) and K_2 (one) graph.

Algorithm 22 Demonstration of the 'get n edges' function

```
#include "get_n_edges.h"

#include <cassert>

#include "create_empty_directed_graph.h"

#include "create_k2_graph.h"

void get_n_edges_demo() noexcept
{
   const auto g = create_empty_directed_graph();
   assert(get_n_edges(g) == 0);

   const auto h = create_k2_graph();
   assert(get_n_edges(h) == 1);
}
```

3.3 Getting the vertices' out degree

The out degree of a vertex is the number of edges that originate at it.

Algorithm 23 Get the vertices' out degrees

```
#include <vector>
template <typename graph>
std::vector<int> get_vertex_out_degrees(const graph& g)
{
   std::vector<int> v;
   for (auto p = vertices(g);
      p.first != p.second;
      ++p.first) {
      v.emplace_back(out_degree(*p.first,g));
   }
   return v;
}
```

The out degrees of the vertices are obtained directly from the vertex descriptor and then put into a std::vector. Note that the std::vector has element type 'int', instead of 'graph::degree_size_type', as one should prefer using int (over unsigned int) in an interface [1]¹. Also, avoid using an unsigned an int for the sake of gaining that one more bit [3]².

Albeit K_2 is a simple graph, we can use it to demonstrate 'get_vertex_out_degrees' on, as shown in algorithm 24.

Algorithm 24 Demonstration of the 'get vertex out degrees' function

```
#include <cassert>
#include "create_k2_graph.h"
#include "get_vertex_out_degrees.h"

void get_vertex_out_degrees_demo() noexcept
{
   const auto g = create_k2_graph();
   const std::vector<int> expected_out_degrees{1,1};
   const std::vector<int> vertex_out_degrees{
        get_vertex_out_degrees(g)};
   assert(expected_out_degrees == vertex_out_degrees);
}
```

 $^{^{1}}$ Chapter 9.2.2

 $^{^2\}mathrm{Chapter}$ 4.4

3.4 Storing a graph as a .dot

Graph are easily saved to a .dot file:

Algorithm 25 Storing a graph as a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>

///Save a graph to a .dot file
template <typename graph>
void save_graph_to_dot(const graph& g, const std::string& filename)
{
   std::ofstream f(filename);
   boost::write_graphviz(f,g);
}
```

Algorithm 26 shows how to use this function.

Algorithm 26 Demonstration of the 'save graph to dot' function

```
#include "create_k2_graph.h"
#include "create_named_vertices_k2_graph.h"
#include "save_graph_to_dot.h"

void save_graph_to_dot_demo() noexcept
{
   const auto g = create_k2_graph();
   save_graph_to_dot(g, "save_graph_to_dot_k2_graph.dot");

   const auto h = create_named_vertices_k2_graph();
   save_graph_to_dot(h, "
        save_graph_to_dot_named_vertices_k2_graph.dot");
}
```

When using the 'create_k2_graph function' (algorithm 17) to create a K_2 graph, the .dot file created is displayed in algorithm 27:

Algorithm 27 .dot file created from the create_k2_graph function (algorithm 17)

```
graph G {
0;
1;
0--1;
}
```

This .dot file corresponds to figure 2:

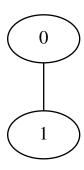


Figure 2: .svg file created from the create_k2_graph function (algorithm 17)

If you used the create_named_vertices_k2_graph function (algorithm 35) to produce a K_2 graph with named vertices, you see that the .dot file does not have stored the vertex names:

Algorithm 28 .dot file created from the create_named_vertices_k2_graph function (algorithm 35)

```
graph G {
0;
1;
0--1;
}
```

So, the 'save_graph_to_dot' function (algorithm 25) saves only the structure of the graph.

4 Building graphs with built-in properties

Up until now, the graphs created have had edges and vertices without any propery. In this chapter, graphs will be created, in which edges vertices can

have a (std::string) name. There are many more built-in properties edges and nodes can have (see the boost/graph/properties.hpp file for these).

In this chapter, we will build the following graphs:

- An empty (undirected) graph that allows for vertices with names: see chapter 4.1
- K_2 with named vertices: see chapter 4.4
- An empty (undirected) graph that allows for edges and vertices with names: see chapter 4.5
- K_3 with named edges and vertices: see chapter 4.8

In the process, some basic (sometimes bordering trivial) functions are shown:

- Adding a named vertex: see chapter 4.2
- Getting the vertices' names: see chapter 4.3
- Adding an named edge: see chapter 4.6
- Getting the edges' names: see chapter 4.7

These functions are mostly there for completion and showing which data types are used.

4.1 Creating an empty graph with named vertices

Let's create a trivial empty graph, in which the vertices can have a name:

Algorithm 29 Creating an empty graph with named vertices

```
#include <boost/graph/adjacency_list.hpp>
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex name t, std::string
>
create_empty_named vertices graph() noexcept
  return boost::adjacency list <
    boost :: vecS,
    boost :: vecS,
    boost::undirectedS,
    boost::property<
      boost::vertex name t, std::string
    ();
}
```

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)
- is undirected (due to the boost::undirectedS)
- The vertices have one property: they have a name, that is of data type std::string (due to the boost::property< boost::vertex_name_t,std::string>')
- Edges and graph have no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fourth template argument 'boost::property < boost::vertex_name_t,std::string>'. This can be read as: "vertices have the property 'boost::vertex_name_t', that is of data type 'std::string"'. Or simply: "vertices have a name that is stored as a std::string".

Algorithm 30 shows how to create this graph. Note that all the earlier functions defined in this tutorial keep working as expected.

Algorithm 30 Demonstration if the 'create_empty_named_vertices_graph' function

```
#include < cassert >
#include "create_empty_named_vertices_graph.h"
#include "get edge descriptors.h"
#include "get edges.h"
#include "get_vertex_descriptors.h"
#include "get vertices.h"
void create empty named vertices graph demo() noexcept
  const auto g = create empty named vertices graph();
  const auto vip = get vertices(g);
  assert (vip. first == vip. second);
  const auto vds = get_vertex_descriptors(g);
  assert (vds.empty());
  const auto eip = get edges(g);
  assert (eip. first == eip. second);
  const auto eds = get_edge_descriptors(g);
  assert (eds.empty());
```

4.2 Add a vertex with a name

Adding a vertex without a name was trivially easy (see chapter 5). Adding a vertex with a name is less easy:

Algorithm 31 Add a vertex with a name

```
#include <boost/graph/adjacency_list.hpp>
template <typename graph>
void add_named_vertex(graph& g, const std::string& name)
{
   const auto vd_a = boost::add_vertex(g);
   auto vertex_name_map = boost::get(boost::vertex_name,g)
   ;
   vertex_name_map[vd_a] = name;
}
```

Instead of calling 'boost::add_vertex' with an additional argument contain-

ing the name of the vertex³, multiple things need to be done. When adding a new vertex to the graph, the vertex descriptor (as describes in chapter 2.4) is stored. After obtaining the name map from the graph (using 'boost::get(boost::vertex_name,g)'), the name of the vertex is set using that vertex descriptor.

Using add_named_vertex is straightforward, as demonstrated by algorithm 32.

Algorithm 32 Demonstration of 'add named vertex'

```
#include <cassert>
#include "add_named_vertex.h"
#include "create_empty_named_vertices_graph.h"
#include "get_vertex_descriptors.h"

void add_named_vertex_demo() noexcept
{
   auto g = create_empty_named_vertices_graph();
   add_named_vertex(g,"Lex");
   assert(get_vertex_descriptors(g).size() == 1);
}
```

4.3 Getting the vertices' names

When the vertices of a graph have named vertices, one can extract them as such:

 $^{^3}$ I am unsure if this would have been a good interface. I am sure I expected this interface myself. I do see a problem with multiple properties and the order of initialization, but initialization can follow the same order as the the property list.

Algorithm 33 Get the vertices' names

```
#include <string>
#include <vector>
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>

//TODO: generalize to return any type
template <typename graph>
std::vector<std::string> get_vertex_names(const graph& g)
{
   std::vector<std::string> v;

   const auto vertex_name_map = get(boost::vertex_name,g);

   for (auto p = vertices(g);
      p.first != p.second;
      ++p.first) {
      v.emplace_back(get(vertex_name_map, *p.first));
   }
   return v;
}
```

The names of the vertices are obtained from a boost::property_map and then put into a std::vector. Note that the std::vector has element type 'std::string', instead of extracting the type from the graph. If you know how to do so, please email me.

When trying to get the vertices' names from a graph without vertices with names, you will get the error 'formed reference to void' (see chapter 12.1).

Algorithm 34 shows how to add two named vertices and how to get their names.

Algorithm 34 Demonstration of 'get vertex names'

```
#include <cassert>
#include "add named vertex.h"
#include "create_empty_named_vertices_graph.h"
#include "get vertex names.h"
void get_vertex_names_demo() noexcept
  auto g = create_empty_named_vertices_graph();
  const std::string vertex name 1{"Chip"};
  const std::string vertex_name_2{"Chap"};
  add_named_vertex(g,vertex_name_1);
  add_named_vertex(g,vertex_name_2);
  const std::vector<std::string> expected names{
     vertex name 1, vertex name 2};
  const std::vector<std::string> vertex names{
     get_vertex_names(g)};
  assert (expected names == vertex names);
}
```

4.4 Creating K_2 with named vertices

We extend K_2 of chapter 2.12 by naming the vertices 'from' and 'to', as depicted in figure 3:

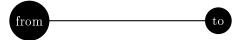


Figure 3: K_2 : a fully connected graph with two vertices with the text 'from' and 'to'

To create K_2 , the following code can be used:

Algorithm 35 Creating K_2 as depicted in figure 3

```
#include "create named vertices k2 graph.h"
#include "create_empty_named_vertices_graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property\!<\!boost::vertex\_name\_t\;,std::string\!>
create named vertices k2 graph() noexcept
  auto g = create_empty_named_vertices_graph();
  {f const\ auto\ vd\_a = boost:: add\_vertex(g);}
  const auto vd_b = boost::add_vertex(g);
  const auto aer = boost::add edge(
    vd a,
    vd_b,
    g
  );
  assert (aer.second);
  auto name map = boost::get(boost::vertex name,g);
  name map[vd a] = "from";
  name map[vd b] = "to";
  return g;
}
```

Most of the code is a repeat of algorithm 17. In the end, the names are obtained as a boost::property map and set.

Also the demonstration code (algorithm) is very similar to the demonstration code of the create k2 graph function ().

Algorithm 36 Demonstrating the 'create k2 graph' function

```
#include <cassert>
#include "create_named_vertices_k2_graph.h"
#include "get_vertex_names.h"

void create_named_vertices_k2_graph_demo() noexcept
{
    const auto g = create_named_vertices_k2_graph();
    const std::vector<std::string> expected_names{"from", "
        to"};
    const std::vector<std::string> vertex_names =
        get_vertex_names(g);
    assert(expected_names == vertex_names);
}
```

4.5 Creating an empty graph with named edges and vertices

Let's create a trivial empty graph, in which the both the edges and vertices can have a name:

Algorithm 37 Creating an empty graph with named edges and vertices

```
#include < string>
#include <boost/graph/adjacency_list.hpp>
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<boost::vertex name t, std::string>,
  boost::property<boost::edge name t,std::string>
create empty named edges and vertices graph() noexcept
  return boost::adjacency list <
    boost :: vecS,
    boost :: vecS,
    boost::undirectedS,
    boost::property<
      boost::vertex name t, std::string
    boost::property<
      boost::edge name t, std::string
    ();
}
```

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)
- is undirected (due to the boost::undirectedS)
- The vertices have one property: they have a name, that is of data type std::string (due to the boost::property< boost::vertex name t,std::string>')
- The edges have one property: they have a name, that is of data type std::string (due to the boost::property< boost::edge name t,std::string>')
- The graph has no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fifth template argument 'boost::property < boost::edge_name_t,std::string>'. This can be read as: "edges have the property 'boost::edge_name_t', that is of data type 'std::string"'. Or simply: "edges have a name that is stored as a std::string".

Algorithm 38 shows how to create this graph. Note that all the earlier functions defined in this tutorial keep working as expected.

```
38
Algorithm
                        Demonstration
                                                the
                                                         'cre-
ate\_empty\_named\_edges\_and\_vertices\_graph' function
#include <cassert>
#include "add_named_edge.h"
#include "create empty named edges and vertices graph.h"
#include "get edge names.h"
#include "get vertex names.h"
void create empty named edges and vertices graph demo()
   noexcept
  auto g = create empty named edges and vertices graph();
  add named edge(g, "Reed");
  const std::vector<std::string> expected vertex names{""
     ,""};
  const std::vector<std::string> vertex names =
     get vertex names(g);
  assert (expected vertex names = vertex names);
  const std::vector<std::string> expected edge names{"
     Reed"};
  const std::vector<std::string> edge_names =
     get edge names(g);
  assert (expected edge names = edge names);
}
```

4.6 Adding a named edge

Adding an edge with a name:

Algorithm 39 Add a vertex with a name

```
#include <boost/graph/adjacency_list.hpp>
#include <cassert>

template <typename graph>
void add_named_edge(graph& g, const std::string& edge_name)

{
   const auto vd_a = boost::add_vertex(g);
   const auto vd_b = boost::add_vertex(g);
   const auto aer = boost::add_edge(vd_a, vd_b, g);
   assert(aer.second);

auto edge_name_map = boost::get(boost::edge_name,g);
   edge_name_map[aer.first] = edge_name;
}
```

In this code snippet, the edge descriptor (see chapter 2.10 if you need to refresh your memory) when using 'boost::add_edge' is used as a key to change the edge its name map.

The algorithm 40 shows how to add a named edge to an empty graph. When trying to add named vertices to graph without this property, you will get the error 'formed reference to void' (see chapter 12.1).

Algorithm 40 Demonstration of the 'add named edge' function

```
#include <cassert>
#include "add_named_edge.h"
#include "create_empty_named_edges_and_vertices_graph.h"
#include "get_n_edges.h"

void add_named_edge_demo() noexcept
{
   auto g = create_empty_named_edges_and_vertices_graph();
   add_named_edge(g,"Richards");
   assert(get_n_edges(g) == 1);
}
```

4.7 Getting the edges' names

When the edges of a graph have named vertices, one can extract them as such:

Algorithm 41 Get the edges' names

```
#include < string>
#include <vector>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/graph traits.hpp>
#include <boost/graph/properties.hpp>
//TODO: generalize to return any type
template <typename graph>
std::vector<std::string> get_edge_names(const graph& g)
  std::vector<std::string> v;
  const auto edge name map = get(boost::edge name,g);
  for (auto p = boost :: edges(g);
    p.first != p.second;
    ++p.first) {
    v.emplace back(get(edge name map, *p.first));
  return v;
}
```

The names of the edges are obtained from a boost::property_map and then put into a std::vector. The algorithm 42 shows how to apply this function.

Would you dare to try to get the edges' names from a graph without vertices with names, you will get the error 'formed reference to void' (see chapter 12.1).

Algorithm 42 Demonstration of the 'get edge names' function

```
#include <cassert>
#include "add_named_edge.h"
#include "create_empty_named_edges_and_vertices_graph.h"
#include "get_edge_names.h"

void get_edge_names_demo() noexcept
{
    auto g = create_empty_named_edges_and_vertices_graph();
    const std::string edge_name_1{"Eugene"};
    const std::string edge_name_2{"Another_Eugene"};
    add_named_edge(g, edge_name_1);
    add_named_edge(g, edge_name_2);
    const std::vector<std::string> expected_names{
        edge_name_1, edge_name_2};
    const std::vector<std::string> edge_names{
        get_edge_names(g)};
    assert(expected_names == edge_names);
}
```

4.8 Creating K_3 with named edges and vertices

We extend the graph K_2 with named vertices of chapter 4.4 by adding names to the edges, as depicted in figure 4:

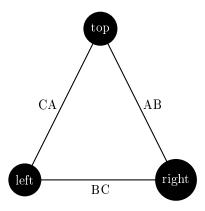


Figure 4: K_3 : a fully connected graph with three named edges and vertices

To create K_3 , the following code can be used:

Algorithm 43 Creating K_3 as depicted in figure 4

```
#include <boost/graph/adjacency list.hpp>
#include <string>
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<boost::vertex name t, std::string>,
  boost::property<boost::edge name t,std::string>
create_named_edges_and_vertices_k3_graph() noexcept
  auto g = create_empty_named_edges_and_vertices_graph();
  const auto vd_a = boost::add_vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto vd c = boost::add vertex(g);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer_bc = boost::add_edge(vd_b, vd_c, g);
  assert (aer bc.second);
  const auto aer ca = boost::add edge(vd c, vd a, g);
  assert (aer ca.second);
  //Add vertex names
  auto vertex_name_map = boost::get(boost::vertex_name,g)
  vertex name map[vd a] = "top";
  vertex_name_map[vd_b] = "right";
  vertex name map[vd c] = "left";
  //Add edge names
  auto edge name map = boost::get(boost::edge name,g);
  edge_name_map[aer_ab.first] = "AB";
  edge_name_map[aer_bc.first] = "BC";
  edge name map[aer ca.first] = "CA";
  return g;
}
```

Most of the code is a repeat of algorithm 35. In the end, the edge names are obtained as a boost::property_map and set. Algorithm 44 shows how to create the graph and measure its edge and vertex names.

Algorithm 44 Demonstration of the 'create_named_edges_and_vertices_k3' function

```
#include <cassert>
#include <iostream>
#include "create named edges and vertices k3 graph.h"
#include "get edge names.h"
#include "get vertex names.h"
void create named edges and vertices k3 graph demo()
   noexcept
  const auto g = create named edges and vertices k3 graph
  const std::vector<std::string> expected vertex names{"
     top", "right", "left"};
  const std::vector<std::string> vertex names{
     get vertex names(g);
  assert (expected vertex names = vertex names);
  const std::vector<std::string> expected edge names{"AB"
     , \quad "BC" \;, \quad "CA" \;\} \;;
  const std::vector<std::string> edge names{
     get edge names(g)};
  assert (expected edge names == edge names);
}
```

5 Working with graphs with named edges and vertices

Measuring simple traits of the graphs created allows

- Find a (named) vertex by its name: chapter 5.1
- Get a (named) vertex its name from its vertex descripto: chapter 5.2
- Set a (named) vertex its name using its vertex descripto: chapter
- Storing a graph with named vertices as a .dot: chapter 5.8
- Storing a graph with named edges and vertices as a .dot: chapter 5.9

Especially the first paragraph is important: 'find_first_vertex_by_name' shows how to obtain a vertex descriptor, which is used in later algorithms.

5.1 Find a vertex by its name

Where STL functions work with iterators, here we obtain a vertex descriptor (see chapter 2.4) to obtain a handle to the desired vertex. Algorithm 45 shows how to obtain a vertex descriptor to the first (name) vertex found with a specific name.

Algorithm 45 Find a vertex by its name

```
#include < string>
\#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
template <typename graph>
typename boost::graph traits<graph>::vertex descriptor
find_first_vertex_with_name(
  const std::string& name,
  const graph& g
{
  const auto vertex name map = get(boost::vertex name,g);
  for (auto p = vertices(g);
    p.first != p.second;
    ++p. first) {
    const std::string s{
      get (vertex name map, *p.first)
    if (s == name) { return *p.first; }
  return *vertices(g).second;
}
```

With the vertex descriptor obtained, one can read and modify the graph. Algorithm 46 shows some examples of how to do so.

Algorithm 46 Demonstration of the 'find first vertex by name' function

```
#include <cassert>
#include "create_named_vertices_k2_graph.h"
#include "find_first_vertex_with_name.h"

void find_first_vertex_with_name_demo() noexcept
{
   const auto g = create_named_vertices_k2_graph();
   const auto vd = find_first_vertex_with_name("from", g);
   assert(boost::out_degree(vd,g) == 1);
   assert(boost::in_degree(vd,g) == 1);
}
```

5.2 Get a (named) vertex its name from its vertex descriptor

This may seem a trivial paragraph, as chapter 4.3 describes the 'get_vertex_names' algorithm, in which we get all vertices' names. But it does not allow to first find a vertex of interest and subsequently getting only that one its name.

To obtain the name from a vertex descriptor, one needs to pull out the name map and then look up the vertex of interest (I like to compare it as such: the vertex descriptor is a last name, the name map is a phone book, the desired info a phone number).

Algorithm 47 Get a vertex its name from its vertex descriptor

```
#include <string>
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>

template <typename graph>
std::string get_vertex_name(
   const typename boost::graph_traits<graph>::
        vertex_descriptor&vd,
   const graph&g
)
{
   const auto vertex_name_map = get(boost::vertex_name,g);
   return vertex_name_map[vd];
}
```

To use 'get_vertex_name', one first needs to obtain a vertex descriptor.

Algorithm 48 Demonstration if the 'get vertex name' function

```
#include <cassert>
#include "add_named_vertex.h"
#include "create_empty_named_vertices_graph.h"
#include "find_first_vertex_with_name.h"
#include "get_vertex_name.h"

void get_vertex_name_demo() noexcept
{
    auto g = create_empty_named_vertices_graph();
    const std::string name{"Dex"};
    add_named_vertex(g,name);
    const auto vd = find_first_vertex_with_name(name,g);
    assert(get_vertex_name(vd,g) == name);
}
```

5.3 Set a (named) vertex its name from its vertex descriptor

If you know how to get the name from a vertex descriptor, setting it is just as easy, as shown in algorithm 49.

Algorithm 49 Set a vertex its name from its vertex descriptor

```
#include <string>
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>

template <typename graph>
void set_vertex_name(
    const std::string& name,
    const typename boost::graph_traits<graph>::
        vertex_descriptor& vd,
    graph& g
)
{
    auto vertex_name_map = get(boost::vertex_name,g);
    vertex_name_map[vd] = name;
}
```

To use 'set_vertex_name', one first needs to obtain a vertex descriptor. Algorithm 50 shows a simple example.

Algorithm 50 Demonstration if the 'set vertex name' function

```
#include <assert>
#include "add_named_vertex.h"
#include "create_empty_named_vertices_graph.h"
#include "find_first_vertex_with_name.h"
#include "get_vertex_name.h"

#include "set_vertex_name.h"

void set_vertex_name_demo() noexcept
{
    auto g = create_empty_named_vertices_graph();
    const std::string old_name{"Dex"};
    add_named_vertex(g,old_name);
    const auto vd = find_first_vertex_with_name(old_name,g)
    ;
    assert(get_vertex_name(vd,g) == old_name);
    const std::string new_name{"Diggy"};
    set_vertex_name(new_name, vd, g);
    assert(get_vertex_name(vd,g) == new_name);
}
```

5.4 Setting all vertices' names

When the vertices of a graph have named vertices and you want to set all their names at once:

Algorithm 51 Setting the vertices' names

```
#include < string>
#include < vector >
#include <boost/graph/graph traits.hpp>
#include <boost/graph/properties.hpp>
//TODO: generalize 'names'
template <typename graph>
void set_vertex_names(
  graph&g,
  const std::vector<std::string>& names
{
  const auto vertex name map = get(boost::vertex name,g);
  auto names begin = std::begin(names);
  const auto names end = std::end(names);
  for (auto vi = vertices (g);
    vi.first != vi.second;
    ++vi.first , ++names begin)
    assert (names begin != names end);
    put(vertex name map, *vi.first,*names begin);
```

An impressive feature is that getting the property map holding the graph its names is not a copy, but a reference. Otherwise, modifying 'name_map' (obtained by non-reference) would only modify a copy.

5.5 Clear the edges of a named vertex

A vertex descriptor can be used to clear all in/out/both edges connected to a vertex. It is necessary to remove these connections before the vertex itself can be removed. There are three functions to remove the edges connected to a vertex:

- boost::clear vertex: removes all edges to and from the vertex
- boost::clear_out_edges: removes all outgoing edges from the vertex (in directed graphs only, else you will get a 'error: no matching function for call to clear_out_edges', as described in chapter 12.2)
- boost::clear in edges: removes all incoming edges from the vertex (in

directed graphs only, else you will get a 'error: no matching function for call to clear in edges', as described in chapter 12.3)

In the algorithm 'clear_vertex_with_name' the 'boost::clear_vertex' algorithm is used, as the graph used is undirectional:

Algorithm 52 Clear a named vertex

```
#include <string>
#include <boost/graph/adjacency_list.hpp>
#include "find_first_vertex_with_name.h"

template <class graph>
void clear_vertex_with_name(
    const std::string& name,
    graph& g
)
{
    const auto vd = find_first_vertex_with_name(name,g);
    boost::clear_vertex(vd,g);
}
```

Algorithm 53 shows the clearing of a named vertex.

Algorithm 53 Demonstration of the 'clear vertex with name' function

```
#include <cassert>
#include "clear_vertex_with_name.h"
#include "create_named_vertices_k2_graph.h"
#include "get_n_edges.h"

void clear_vertex_with_name_demo() noexcept
{
   auto g = create_named_vertices_k2_graph();
   assert(get_n_edges(g) == 1);
   clear_vertex_with_name("from",g);
   assert(get_n_edges(g) == 0);
}
```

5.6 Remove a named vertex

remove named vertex

5.7 Remove a named edge

remove named vertex

- void remove_edge(vertex_descriptor u, vertex_descriptor v, adjacency_list&g) . Removes an edge from g
- \bullet void remove_edge(edge_descriptor e, adjacency_list& g) . Removes an edge from g

5.8 Storing a graph with named vertices as a .dot

If you used the create_named_vertices_k2_graph function (algorithm 35) to produce a K_2 graph with named vertices, you can store these names additionally with algorithm 54:

Algorithm 54 Storing a graph with named vertices as a .dot file

The .dot file created is displayed in algorithm 55:

Algorithm 55 .dot file created from the create_named_vertices_k2_graph function (algorithm 35)

```
graph G {
O[label=from];
1[label=to];
0--1;
}
```

This .dot file corresponds to figure 5:

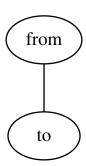


Figure 5: .svg file created from the create_k2_graph function (algorithm 35)

If you used the create_named_edges_and_vertices_k3_graph function (algorithm 43) to produce a K_3 graph with named edges and vertices, you see that the .dot file does not have stored the edge names:

```
Algorithm
                56
                       .dot
                               file
                                       created
                                                  from
                                                           the
                                                                   cre-
ate named edges and vertices k3 graph function (algorithm 43)
graph G {
0[label=top];
1[label=right];
2[label=left];
0--1;
1--2;
2--0;
}
```

So, the 'save_named_vertices_graph_to_dot' function (algorithm 25) saves only the structure of the graph and its vertex names.

5.9 Storing a graph with named vertices and edges as a .dot

If you used the create_named_edges_and_vertices_k3_graph function (algorithm 43) to produce a K_3 graph with named edges and vertices, you can store these names additionally with algorithm 57:

Algorithm 57 Storing a graph with named edges and vertices as a .dot file

```
#include < string>
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include <boost/graph/properties.hpp>
#include "get edge names.h"
#include "get vertex names.h"
///Save a graph with named vertices to a .dot file
template <typename graph>
void save named edges and vertices graph to dot(const
   graph& g, const std::string& filename)
{
  std::ofstream f(filename);
  const auto vertex names = get vertex names(g);
  const auto edge name map = boost::get(boost::edge name,
     g);
  boost::write graphviz(
    f,
    g,
    boost::make label writer(&vertex names[0]),
    [edge name map](std::ostream& out, const auto& e) {
      out << "[label=\"" << edge name map[e] << "\"]";
  );
}
```

Note that this algorithm uses C++17.

The .dot file created is displayed in algorithm 58:

```
Algorithm 58   .dot file created from the cre-
ate_named_edges_and_vertices_k3_graph function (algorithm 35)

graph G {
0[label=top];
1[label=right];
2[label=left];
0--1 [label="AB"];
1--2 [label="BC"];
2--0 [label="CA"];
}
```

This .dot file corresponds to figure 6:

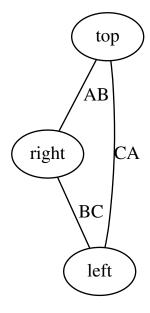


Figure 6: .svg file created from the create named edges and vertices k3 graph function (algorithm 35)

If you created a graph with edges more complex than just a name, you will still just write these to the .dot file. Chapter 9.1 shows how to write custom vertices to a .dot file.

So, the 'save_named_edges_and_vertices_graph_to_dot' function (algorithm 25) saves only the structure of the graph and its edge and vertex names.

6 Building graphs with custom properties

Up until now, the graphs created have had edges and vertices with the built-in name propery. In this chapter, graphs will be created, in which the edges and vertices can have a custom 'my edge' and 'my edge' type⁴.

- \bullet An empty (undirected) graph that allows for custom vertices: see chapter 6.1
- \bullet K_2 with custom vertices: see chapter 6.4
- \bullet An empty (undirected) graph that allows for custom edges and vertices: see chapter 6.5
- K_3 with custom edges and vertices: see chapter 6.7

In the process, some basic (sometimes bordering trivial) functions are shown:

 $^{^4\}mathrm{I}$ do not intend to be original in naming my data types

- Adding a custom vertex: see chapter 6.2
- Adding a custom edge: see chapter 6.6

These functions are mostly there for completion and showing which data types are used.

6.1 Create an empty graph with custom vertices

Say we want to use our own vertex class as graph nodes. This is done in multiple steps:

- 1. Create a custom vertex class, called 'my vertex'
- 2. Install a new property, called 'vertex custom type'
- 3. Use the new property in creating a boost::adjacency_list

6.1.1 Creating the custom vertex class

In this example, I create a custom vertex class. Here I will show the header file of it, as the implementation of it is not important yet.

Algorithm 59 Declaration of my_vertex

```
#ifndef MY VERTEX H
#define MY_VERTEX_H
#include <string>
class my vertex
public:
  my vertex (
    const std::string& name = "",
    const std::string& description = "",
    const double x = 0.0,
    const double y = 0.0
  ) noexcept;
  std::string m name;
  std::string m description;
  \mathbf{double} \ \ \mathbf{m}_{\underline{\phantom{a}}}\mathbf{x};
  double m y;
};
bool operator == (const my vertex& lhs, const my vertex&
    rhs) noexcept;
\#endif // MY VERTEX H
```

my_vertex is a class that has multiple properties: two doubles 'm_x' ('m_' stands for member) and 'm_y', and two std::strings m_name and m_description. my_vertex is copyable, but cannot trivially be converted to a std::string.

6.1.2 Installing the new property

Installing a new property would have been easier, if 'more C++ compilers were standards conformant' ([2], chapter 3.6, footnote at page 52). Boost.Graph uses the BOOST INSTALL PROPERTY macro to allow using a custom property:

Algorithm 60 Installing the vertex_custom_type property

```
#include <boost/graph/properties.hpp>
namespace boost {
   enum vertex_custom_type_t { vertex_custom_type = 314 };
   BOOST_INSTALL_PROPERTY(vertex, custom_type);
}
```

The enum value 314 must be unique.

6.1.3 Create the empty graph with custom vertices

Algorithm 61 Creating an empty graph with custom vertices

```
#include <boost/graph/adjacency list.hpp>
#include "install vertex custom type.h"
#include "my vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my vertex
create empty custom vertices graph() noexcept
  return boost::adjacency list<
    boost :: vecS,
    boost :: vecS,
    boost::undirectedS,
    boost::property<
      boost::vertex custom type t, my vertex
  >();
}
```

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)
- is undirected (due to the boost::undirectedS)
- The vertices have one property: they have a custom type, that is of data type my vertex (due to the boost::property< boost::vertex custom type t,my vertex>')
- The edges and graph have no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fourth template argument 'boost::property
boost::vertex_custom_type_t,my_vertex>'. This can be read as: "vertices

have the property 'boost::vertex_custom_type_t', which is of data type 'my_vertex"'. Or simply: "vertices have a custom type called my_vertex".

6.2 Add a custom vertex

Adding a custom vertex is very similar to adding a named vertex (chapter 4.2).

Algorithm 62 Add a custom vertex

```
#include <boost/graph/adjacency_list.hpp>
#include "install_vertex_custom_type.h"
#include "my_vertex.h"

template <typename graph>
void add_custom_vertex(graph& g, const my_vertex& v)
{
   const auto vd_a = boost::add_vertex(g);
   const auto my_vertex_map = boost::get(boost::
        vertex_custom_type,g);
   my_vertex_map[vd_a] = v;
}
```

When having added a new (abstract) vertex to the graph, the vertex descriptor is used to set the my_vertex in the graph its my_vertex map (using 'boost::get(boost::vertex custom type,g)').

6.3 Getting the vertices' my_vertexes⁵

When the vertices of a graph have any associated my_vertex, one can extract these as such:

 $^{^{5} \}rm{the}$ name 'my_vertexes' is chosen to indicate this function returns a container of my_vertex

Algorithm 63 Get the vertices' my vertexes

```
#include < vector>
\#include <boost/graph/graph_traits.hpp>
\#\mathbf{include} < \mathbf{boost} / \operatorname{graph} / \operatorname{properties} . hpp>
#include "install vertex custom type.h"
#include "my vertex.h"
//TODO: generalize to return any type
\mathbf{template} \ < \!\! \mathbf{typename} \ \mathbf{grap} \, h \!\! >
std::vector<my vertex> get vertex my vertexes(const graph
   & g)
  std::vector<my vertex> v;
  const auto my vertexes map = get (boost::
      vertex custom type,g);
  for (auto p = vertices(g);
     p.first != p.second;
    ++p.first) {
     v.emplace_back(get(my_vertexes_map, *p.first));
  return v;
```

The my_vertex object associated with the vertices are obtained from a boost::property map and then put into a std::vector.

When trying to get the vertices' my_vertex from a graph without my_vertex objects associated, you will get the error 'formed reference to void' (see chapter 12.1).

6.4 Creating K_2 with custom vertices

We reproduce the K_2 with named vertices of chapter 4.4 , but with our custom vertices intead:

Algorithm 64 Creating K_2 as depicted in figure 3

```
#include "install vertex custom type.h"
#include "my_vertex.h"
#include "create empty custom vertices graph.h"
#include <boost/graph/adjacency list.hpp>
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my vertex
>
create custom vertices k2 graph() noexcept
  auto g = create_empty_custom_vertices_graph();
  const auto vd a = boost::add vertex(g);
  const auto vd_b = boost::add_vertex(g);
  const auto aer = boost::add edge(vd a, vd b, g);
  assert (aer.second);
  //Add names
  auto my vertex name map = boost::get(boost::
     vertex_custom_type,g);
  my vertex name map[vd a]
   = my_vertex("from", "source", 0.0,0.0);
  my vertex name map[vd b]
    = my_vertex("to","target",3.14,3.14);
  return g;
```

Most of the code is a slight modification of algorithm 35. In the end, the my_vertices are obtained as a boost::property_map and set with two custom my_vertex objects.

6.5 Create an empty graph with custom edges and vertices

Say we want to use our own edge class as graph nodes. This is done in multiple steps:

1. Create a custom edge class, called 'my edge'

- 2. Install a new property, called 'edge custom type'
- 3. Use the new property in creating a boost::adjacency list

6.5.1 Creating the custom edge class

In this example, I create a custom edge class. Here I will show the header file of it, as the implementation of it is not important yet.

Algorithm 65 Declaration of my edge

```
#ifndef MY EDGE H
#define MY EDGE H
#include < string>
class my edge
public:
  my edge (
    const std::string& name = "",
    const std::string& description = "",
    const double width = 1.0,
    const double height = 1.0
  ) noexcept;
  std::string m name;
  std::string m description;
  double m_width;
  double m height;
};
bool operator == (const my edge& lhs, const my edge& rhs)
   noexcept;
#endif // MY EDGE H
```

my_edge is a class that has multiple properties: two doubles 'm_width' ('m_' stands for member) and 'm_height', and two std::strings m_name and m_description. my_edge is copyable, but cannot trivially be converted to a std::string.

6.5.2 Installing the new property

Installing a new property would have been easier, if 'more C++ compilers were standards conformant' ([2], chapter 3.6, footnote at page 52). Boost.Graph uses the BOOST INSTALL PROPERTY macro to allow using a custom property:

Algorithm 66 Installing the edge_custom_type property

```
#include <boost/graph/properties.hpp>
namespace boost {
  enum edge_custom_type_t { edge_custom_type = 3142 };
  BOOST_INSTALL_PROPERTY(edge, custom_type);
}
```

The enum value 3142 must be unique.

6.5.3 Create the empty graph with custom edges and vertices

Algorithm 67 Creating an empty graph with custom vertices

```
#include <boost/graph/adjacency list.hpp>
#include "install edge custom type.h"
#include "install vertex custom type.h"
#include "my_vertex.h"
#include "my edge.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my vertex
  boost::property<
    boost::edge custom type t,my edge
create empty custom edges and vertices graph() noexcept
  return boost::adjacency list <
    boost :: vecS,
    boost :: vecS,
    boost::undirectedS,
    boost::property<
      boost::vertex custom type t, my vertex
    boost::property<
      boost::edge custom type t,my edge
  >();
}
```

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)
- is undirected (due to the boost::undirectedS)
- The vertices have one property: they have a custom type, that is of data type my_vertex (due to the boost::property< boost::vertex_custom_type_t, my_vertex>')

- The edges have one property: they have a custom type, that is of data type my_edge (due to the boost::property< boost::edge_custom_type_t, my_edge>')
- The graph has no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fifth template argument 'boost::property < boost::edge_custom_type_t, my_edge>'. This can be read as: "edges have the property 'boost::edge_custom_type_t', which is of data type 'my_edge"'. Or simply: "edges have a custom type called my_edge".

6.6 Add a custom edge

Adding a custom edge is very similar to adding a named edge (chapter 4.6).

Algorithm 68 Add a custom edge

```
#include <cassert>
#include <boost/graph/adjacency_list.hpp>
#include "install_edge_custom_type.h"
#include "install_vertex_custom_type.h"
#include "my_vertex.h"
#include "my_edge.h"

template <typename graph>
void add_custom_edge(graph& g, const my_edge& v)
{
    const auto vd_a = boost::add_vertex(g);
    const auto vd_b = boost::add_vertex(g);

    const auto aer = boost::add_vertex(g);

    const auto aer = boost::add_edge(vd_a, vd_b, g);
    assert(aer.second);
    const auto my_edge_map = boost::get(boost::
        edge_custom_type,g);
    my_edge_map[aer.first] = v;
}
```

When having added a new (abstract) edge to the graph, the edge descriptor is used to set the my edge in the graph its my edge map (using 'boost::get(boost::edge custom type,g)').

6.7 Creating K_3 with custom edges and vertices

Instead of using edges with a name, or other properties, here we use a custom edge class called 'my edge'.

We reproduce the K_3 with named edges and vertices of chapter 4.8 , but with our custom edges and vertices intead:

Algorithm 69 Creating K_3 as depicted in figure 4

```
#include "install vertex custom type.h"
#include "my_vertex.h"
#include "create empty custom edges and vertices graph.h"
\# \mathbf{include} < \mathbf{boost} / \operatorname{graph} / \operatorname{adjacency\_list} . hpp>
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost:: vertex\_custom\_type\_t \ , my\_vertex
  >,
  boost::property<
    boost::edge custom type t,my edge
create custom edges and vertices k3 graph() noexcept
  auto g = create empty custom edges and vertices graph()
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost :: add vertex(g);
  const auto vd c = boost :: add <math>vertex(g);
  {f const\ auto}\ {f aer\_a}\ =\ {f boost}:: {f add\_edge}({f vd\_a},\ {f vd\_b},\ {f g}) \; ;
  const auto aer b = boost::add edge(vd b, vd c, g);
  const auto aer c = boost::add edge(vd c, vd a, g);
  assert (aer_a.second);
  assert (aer_b.second);
  assert (aer c.second);
  auto my_vertex_map = boost::get(boost::
      vertex custom type,g);
  my vertex map vd a
    = my_vertex("top", "source", 0.0, 0.0);
  my_vertex_map[vd_b]
    = my vertex ("right", "target", 3.14,0);
  my vertex map[vd c]
    = my vertex("left", "target", 0, 3.14);
  auto my edge map = boost::get(boost::edge custom type,g
      );
  my edge map[aer a.first]
    = my edge("AB", "first", 0.0, 0.0);
  my edge map [aer b.first]
    = my edge("BC", "second", 3.14, 3.14);
  my_edge_map[aer c.first]
                              59
    = my_edge("CA", "third", 3.14, 3.14);
  return g;
```

Most of the code is a slight modification of algorithm 43. In the end, the my_edges and my_vertices are obtained as a boost::property_map and set with the custom my_edge and my_vertex objects.

7 Measuring simple graphs traits of a graph with custom edges and vertices

7.1 Count vertex my vertex

 $count_vertex_my_vertex$

7.2 Find a my vertex

find_my_vertex

7.3 Find the vertices connected to a certain my_vertex

 $find_vertices_connected_to_my_vertex$

8 Modifying simple graphs traits

It is useful to be able to modify every aspect of a graph. Adding nodes and edges are found in earlier chapters.

8.1 Setting all vertices' my vertex objects

When the vertices of a graph are associated with my_vertex objects, one can set these my_vertexes as such:

Algorithm 70 Setting the vertices' my vertexes

```
#include < string>
#include < vector >
#include <boost/graph/graph traits.hpp>
\#\mathbf{include} < \mathbf{boost} / \operatorname{graph} / \operatorname{properties} . hpp>
#include "install vertex custom type.h"
#include "my_vertex.h"
//TODO: generalize 'my vertexes'
template <typename graph>
void set vertex my vertexes (
  graph&g,
  const std::vector<my vertex>& my vertexes
  {f const\ auto\ my\_vertex\_map\ =\ get\ (\ boost::
      vertex custom type,g);
  auto my vertexes begin = std::begin(my vertexes);
  const auto my_vertexes_end = std::end(my_vertexes);
  for (auto vi = vertices(g);
    vi.first != vi.second;
    ++vi.first, ++my vertexes begin)
    assert (my vertexes begin != my vertexes end);
    put(my vertex map, *vi.first,*my vertexes begin);
}
```

An impressive feature is that getting the property map holding the graph its names is not a copy, but a reference. Otherwise, modifying 'my_vertexes_map' (obtained by non-reference) would only modify a copy.

8.2 Remove a my vertex

remove my vertex

• void remove_vertex(vertex_descriptor u, adjacency_list&g). Removes a vertex from graph g (It is expected that all edges associated with this vertex have already been removed using clear_vertex or another appropriate function.)

9 Visualizing graphs

Before graphs are visualized, they are stored as a file first. Here, I use the .dot file format.

9.1 Storing a graph with custom vertices as a .dot

If you used the create_custom_vertices_k2_graph function (algorithm 64) to produce a K_2 graph with vertices associated with my_vertex objects, you can store these my_vertexes additionally with algorithm 71:

Algorithm 71 Storing a graph with custom vertices as a .dot file

```
#include < string>
#include <fstream>
#include <boost/graph/graphviz.hpp>
\#\mathbf{include} < \mathbf{boost} / \operatorname{graph} / \operatorname{properties} . hpp>
#include "get_vertex_my_vertexes.h"
///Save a graph with named vertices to a .dot file
template <typename graph>
void save_custom_vertices_graph_to_dot(const graph& g,
   const std::string& filename)
  std::ofstream f(filename);
  const auto my vertexes = get vertex my vertexes(g);
  boost::write_graphviz(
    f,
    g,
    [my vertexes](std::ostream& out, const auto& v) {
      const my_vertex m{my_vertexes[v]};
      out << "[label=\""
        << m.m_name
        << " ,"
        << m. m_description
        << ","
        << m.m.x
        << ","
        << m.m.y
        << "\"]";
  );
}
```

Note that this algorithm uses C++17. The .dot file created is displayed in algorithm 72:

```
Algorithm 72 .dot file created from the create_custom_vertices_k2_graph function (algorithm 35)
```

```
graph G {
0[label="from,source,0,0"];
1[label="to,target,3.14,3.14"];
0--1;
}
```

This .dot file corresponds to figure 72:

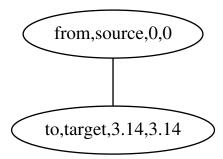


Figure 7: .svg file created from the create_custom_vertices_k2_graph function (algorithm 64)

10 Measuring more complex graphs traits

10.1 Count the number of self-loops

11 Misc functions

11.1 Getting a data type as a std::string

This function will only work under GCC.

Algorithm 73 Getting a data type its name as a std::string

```
#include < string>
#include <typeinfo>
#include < c st d lib >
#include < cxxabi.h>
//From\ http://stackoverflow.com/questions/1055452/c-get-
    name-of-type-in-template
//\mathit{Thanks} to \mathit{m-dudley} ( \mathit{http:}//\mathit{stackoverflow.com/users}
    /111327/m-dudley
template<typename T>
std::string get type name()
  std::string tname = typeid(T).name();
  int status = -1;
  char * const demangled name{
    abi::__cxa_demangle(tname.c_str(), NULL, NULL, &
        status)
  if(status = 0) {
    tname = demangled name;
    std::free(demangled name);
  return tname;
```

12 Errors

Some common errors.

12.1 Formed reference to void

This compile-time error occurs when you create a graph without a certain property, then subsequently reading that property, as in algorithm 74:

Algorithm 74 Creating the error 'formed reference to void'

```
#include "create_k2_graph.h"
#include "get_vertex_names.h"

void formed_reference_to_void() noexcept
{
    get_vertex_names(create_k2_graph());
}
```

In algorithm 74 a graph is created with vertices of no properties. Then the names of these vertices, which do not exists, are tried to be read. If you want to read the names of the vertices, supply a graph that has this property.

12.2 No matching function for call to 'clear out edges'

This compile-time error occurs when you want to clear the outward edges from a vertex in an undirected graph.

Algorithm 75 Creating the error 'formed reference to void'

```
#include "create_k2_graph.h"

void no_matching_function_for_call_to_clear_out_edges()
    noexcept
{
    auto g = create_k2_graph();
    const auto vd = *boost::vertices(g).first;
    boost::clear_in_edges(vd,g);
}
```

In algorithm 75 an undirected graph is created, a vertex descriptor is obtained, then its out edges are tried to be cleared. Either use a directed graph (which has out edges), or use the 'boost::clear vertex' function instead.

12.3 No matching function for call to 'clear_in_edges' See chapter 12.2.

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[1] John Lakos. Large-scale C++ software design, volume 10. Addison-Wesley Reading, 1996.

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