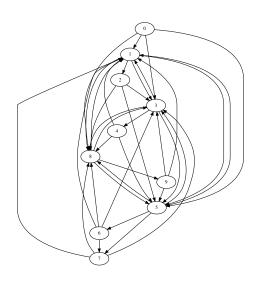
A well-connected C++11 Boost.Graph tutorial

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1 Introduction

This is 'A well-connected C++11 Boost.Graph tutorial', version 1.7.

1.1 Why this tutorial

I needed this tutorial already in 2006, when I started experimenting with Boost.Graph. More specifically, I needed a tutorial that:

- Orders concepts chronologically
- Increases complexity gradually
- Shows complete pieces of code

What I had were the book [8] and the Boost.Graph website, both did not satisfy these requirements.

This tutorial is intended to take the reader to the level of understanding the book [8] and the Boost.Graph website require. It is about basic graph manipulation, not the more advanced graph algorithms. An analogy with std::vector: it teaches the std::vector member functions, but not the algorithms that work on.

1.2 Code snippets

For every concept, I will show

- the 'do' function: a function that achieves a goal, for example 'create empty undirected graph'
- the 'demo' function: a function that demonstrates how to call the first, for example 'create_empty_undirected_graph_demo'

I enjoy to show concepts by putting those in (long-named) functions. These functions sometimes border the trivial, by, for example, only calling a single Boost.Graph function. On the other hand, these functions have more English-sounding names, resulting in demonstration code that is readable. Additionally, they explicitly mention their return type (in a simpler way), which may be considered informative.

All coding snippets are taken from compiled C++11 code. I chose to use C++11 because (1) C++14 was not installable on all my computers (2) the step to C++14 is small. All code is tested to compile cleanly under GCC at the highest warning level. The code, as well as this tutorial, can be downloaded from the GitHub at www.github.com/richelbilderbeek/BoostGraphTutorial.

1.3 Coding style

I use the coding style from the Core C++ Guidelines. At the time of this writing, the Core C++ Guidelines were still in early development, so I can only hope the conventions I then chose to follow are still Good Ideas.

It is important to add comments to code. In this tutorial, however, I have chosen not to put comments in code, as I already describe the function in the tutorial its text. This way, it prevents me from saying the same things twice.

It is good to write generic code. In this tutorial, however, I have chosen my functions to have no templated arguments for conciseness and readability. For example, a vertex name is std::string, the type for if a vertex is selected is a boolean, and the custom vertex type is of type 'my_custom_vertex'. I think these choises are reasonable and that the resulting increase in readability is worth it.

Due to my long function names and the limitation of ≈ 50 characters per line, sometimes the code does get to look a bit awkward. I am sorry for this.

I prefer to use the keyword auto over doubling the lines of code for using statements. Because the 'do' functions return an explicit data type, these can be used for reference (until 'decltype(auto)' gets into fashion as a return type). If you really want to know a type, you can use the 'get_type_name' function (chapter 23.1).

On the other hand, I am explicit in the namespaces of functions and classes I use, so to distinguish between types like 'std::array' and 'boost::array'. Some functions (for example, 'get') reside in the namespace of the graph to work on. In this tutorial, this is in the global namespace. Thus, I will write 'get', instead of 'boost::get', as the latter does not compile.

1.4 Tutorial style

In the index, I did first put all my long-named functions there literally, but this resulted in a very sloppy layout. Instead, the function 'do_something' can be found as 'Do something' in the index. On the other hand, STL and Boost functions like 'std::do_something' and 'boost::do_something' can be found as such in the index.

1.5 License

This tutorial is licensed under Creative Commons license 4.0. All C++ code is licensed under GPL 3.0.



Figure 1: Creative Commons license 4.0

1.6 Feedback

This tutorial is not intended to be perfect yet. For that, I need help and feedback from the community. All referenced feedback is welcome, as well as any constructive feedback.

I have tried hard to strictly follow the style as described above. If you find I deviated from these decisions somewhere, I would be grateful if you'd let know. Next to this, there are some sections that need to be coded or have its code improved.

1.7 Help

There are some pieces of code I could use help with:

• Issue #12: Loading a directed graph with a name, function 'load_directed_graph_with_graph_name_fr as shown in chapters 19.2. Perhaps the function 'save_graph_with_graph_name_to_dot' (chapter 19.1) needs to rewritten as well

I have already put the tests in place, so you/I can easily check if your solution works. If the program crashes with the message 'assertion failed: !"Fixed #"', a problem has been solved.

1.8 Acknowledgements

These are users that improved this tutorial and/or the code behind this tutorial, in chronological order:

- E. Kawashima
- mat69, https://www.reddit.com/user/mat69
- danielhj, https://www.reddit.com/user/danieljh
- sehe, http://stackoverflow.com/users/85371/sehe

1.9 Outline

The chapters of this tutorial are also like a well-connected graph (as shown in figure 2). To allow for quicker learners to skim chapters, or for beginners looking to find the patterns, some chapters are repetitions of each other (for example, getting an edge its name is very similar to getting a vertex its name)¹. This tutorial is not about being short, but being complete, at the risk of being called bloated.

The distinction between the chapter is in the type of edges and vertices. They can have:

• no properties: see chapter 2

¹There was even copy-pasting involved!

• have a name: see chapter 4

• have a bundled property: see chapter 8

• have a custom property: see chapter 12

The differences between graphs with bundled and custom prorties are shown in table 1:

	Bundled	Custom
Meaning	Edges/vertices are of your type	Edges/vertices have an
		additional custom
		$\operatorname{property}$
Interface	Directly	Via property map
Class members	Must be public	Can be private
File I/O mechanism	Via public class members	Via stream operators
File I/O success	Fails, please help!	Works, with
		${\rm encoding/decoding}$

Table 1: Difference between bundled and custom properties

Pivotal chapters are chapters like 'Finding the first vertex with ...', as this opens up the door to finding a vertex and manipulating it.

All chapters have a rather similar structure in themselves, as depicted in figure 3.

There are also some bonus chapters, that I have labeled with a . These chapters are added I needed these functions myself and adding them would not hurt. Just feel free to skip them, as there will be less theory explained.

2 Building graphs without properties

Boost.Graph is about creating graphs. In this chapter we create the simplest of graphs, in which edges and nodes have no properties (e.g. having a name).

Still, there are two types of graphs that can be constructed: undirected and directed graphs. The difference between directed and undirected graphs is in the edges: in an undirected graph, an edge connects two vertices without any directionality, as displayed in figure 4. In a directed graph, an edge goes from a certain vertex, its source, to another (which may actually be the same), its target. A directed graph is shown in figure 5.

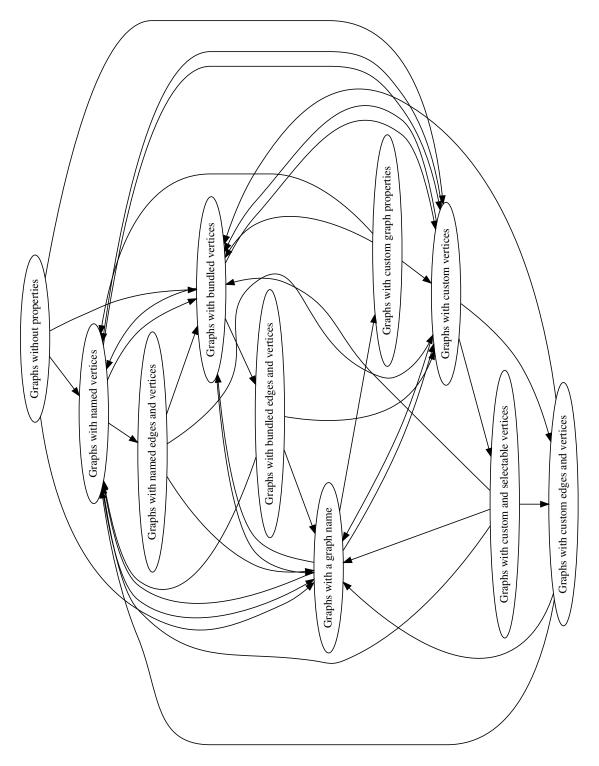


Figure 2: The relations between chapters



Figure 3: The relations between sub-chapters

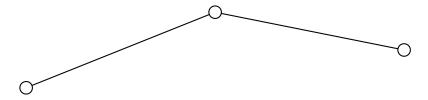


Figure 4: Example of an undirected graph

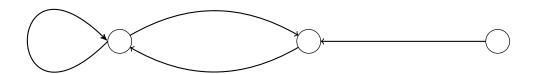


Figure 5: Example of a directed graph

In this chapter, we will build two directed and two undirected graphs:

- An empty (directed) graph, which is the default type: see chapter 2.1
- An empty (undirected) graph: see chapter 2.2
- A two-state Markov chain, a directed graph with two vertices and four edges, chapter 2.14
- K_2 , an undirected graph with two vertices and one edge, chapter 2.15

Creating an empty graph may sound trivial, it is not, thanks to the versatility of the Boost.Graph library.

In the process of creating graphs, some basic (sometimes bordering trivial) functions are encountered:

- Counting the number of vertices: see chapter 2.3
- Counting the number of edges: see chapter 2.4
- Adding a vertex: see chapter 2.5
- Getting all vertices: see chapter 2.7

- Getting all vertex descriptors: see chapter 2.8
- Adding an edge: see chapter 2.9
- Getting all edges: see chapter 2.11
- Getting all edge descriptors: see chapter 2.13

These functions are mostly there for completion and showing which data types are used.

The chapter also introduces some important concepts:

- Vertex descriptors: see chapter 2.6
- Edge insertion result: see chapter 2.10
- Edge descriptors: see chapter 2.12

After this chapter you may want to:

- Building graphs with named vertices: see chapter 4
- Building graphs with bundled vertices: see chapter 8
- Building graphs with custom vertices: see chapter 12
- Building graphs with a graph name: see chapter 18

2.1 Creating an empty (directed) graph

Let's create an empty graph!

Algorithm 1 shows the function to create an empty graph.

Algorithm 1 Creating an empty (directed) graph

```
#include <boost/graph/adjacency_list.hpp>
boost::adjacency_list<>
create_empty_directed_graph() noexcept
{
   return boost::adjacency_list<>>();
}
```

The code consists out of an #include and a function definition. The #include tells the compiler to read the header file 'adjacency_list.hpp'. A header file (often with a '.h' or '.hpp' extension) contains class and functions declarations and/or definitions. The header file 'adjacency_list.hpp' contains the boost::adjacency_list class definition. Without including this file, you will get compile errors like 'definition of boost::adjacency_list unknown'². The function 'create_empty_directed_graph' has:

²In practice, these compiler error messages will be longer, bordering the unreadable

- a return type: The return type is 'boost::adjacency_list<>', that is a 'boost::adjacency list with all template arguments set at their defaults
- a noexcept specification: the function should not throw³, so it is preferred to mark it noexcept ([10] chapter 13.7).
- a function body: all the function body does is create a 'boost::adjacency_list<>'
 by calling its constructor, by using the round brackets

Algorithm 2 demonstrates the 'create_empty_directed_graph' function. Note that it includes a header file with the same name as the function⁴ first, to be able to use it. 'auto' is used, as this is preferred over explicit type declarations ([10] chapter 31.6). The keyword 'auto' lets the compiler figure out the type itself.

Algorithm 2 Demonstration of 'create empty directed graph'

```
#include "create_empty_directed_graph.h"

void create_empty_directed_graph_demo() noexcept
{
   const auto g = create_empty_directed_graph();
}
```

Congratulations, you've just created a boost::adjacency_list with its default template arguments. The boost::adjacency_list is the most commonly used graph type, the other is the boost::adjacency_matrix. We do not do anything with it yet, but still, you've just created a graph, in which:

- The out edges and vertices are stored in a std::vector
- The edges have a direction
- The vertices, edges and graph have no properties
- The edges are stored in a std::list

It stores its edges, out edges and vertices in a two different STL⁵ containers. std::vector is the container you should use by default ([10] chapter 31.6, [11] chapter 76), as it has constant time look-up and back insertion. The std::list is used for storing the edges, as it is better suited at inserting elements at any position.

I use const to store the empty graph as we do not modify it. Correct use of const is called const-correct. Prefer to be const-correct ([9] chapter 7.9.3, [10] chapter 12.7, [7] item 3, [3] chapter 3, [11] item 15, [2] FAQ 14.05, [1] item 8, [4] 9.1.6).

³if the function would throw because it cannot allocate this little piece of memory, you are already in big trouble

⁴I do not think it is important to have creative names

⁵Standard Template Library, the standard library

2.2 Creating an empty undirected graph

Let's create another empty graph! This time, we even make it undirected! Algorith 3 shows how to create an undirected graph.

Algorithm 3 Creating an empty undirected graph

```
#include <boost/graph/adjacency_list.hpp>
boost:: adjacency_list <
   boost:: vecS ,
   boost:: vecS ,
   boost:: undirectedS
>
create_empty_undirected_graph() noexcept
{
   return boost:: adjacency_list <
      boost:: vecS ,
      boost:: vecS ,
      boost:: vecS ,
      boost:: undirectedS
>();
}
```

This algorith differs from the 'create_empty_directed_graph' function (algoritm 1) in that there are three template arguments that need to be specified in the creation of the boost::adjancency list:

- the first 'boost::vecS': select (that is what the 'S' means) that out edges are stored in a std::vector. This is the default way.
- the second 'boost::vecS': select that the graph vertices are stored in a std::vector. This is the default way.
- 'boost::undirectedS': select that the graph is undirected. This is all we needed to change. By default, this argument is boost::directed

Algorithm 4 demonstrates the 'create empty undirected graph' function.

Algorithm 4 Demonstration of 'create empty undirected graph'

```
#include "create_empty_undirected_graph.h"

void create_empty_undirected_graph_demo() noexcept
{
   const auto g = create_empty_undirected_graph();
}
```

Congratulations, with algorithm 4, you've just created an undirected graph in which:

- The out edges and vertices are stored in a std::vector
- The graph is undirected
- Vertices, edges and graph have no properties
- Edges are stored in a std::list

2.3 Counting the number of vertices

Let's count all zero vertices of an empty graph!

Algorithm 5 Count the number of vertices

```
#include <cassert>
#include <boost/graph/adjacency_list.hpp>

template <typename graph>
int get_n_vertices(const graph& g) noexcept
{
   const int n{
      static_cast<int>(boost::num_vertices(g))
   };
   assert(static_cast<unsigned long>(n)
      == boost::num_vertices(g)
   );
   return n;
}
```

The function 'get_n_vertices' takes the result of boost::num_vertices, converts it to int and checks if there was conversion error. We do so, as one should prefer using signed data types over unsigned ones in an interface ([4] chapter 9.2.2). To do so, in the function body its first stament, the unsigned long produced by boost::num_vertices get converted to an int using a static_cast. Using an unsigned integer over a (signed) integer for the sake of gaining that one more bit ([9] chapter 4.4) should be avoided. The integer 'n' is initialized using list-initialization, which is preferred over the other initialization syntaxes ([10] chapter 17.7.6).

The assert checks if the conversion back to unsigned long re-creates the original value, to check if no information has been lost. If information is lost, the program crashes. Use assert extensively ([9] chapter 24.5.18, [10] chapter 30.5, [11] chapter 68, [6] chapter 8.2, [5] hour 24, [4] chapter 2.6).

The function 'get_n_vertices' is demonstrated in algorithm 6, to measure the number of vertices of both the directed and undirected graph we are already able to create.

Algorithm 6 Demonstration of the 'get n vertices' function

```
#include <cassert>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_n_vertices.h"

void get_n_vertices_demo() noexcept
{
   const auto g = create_empty_directed_graph();
   assert(get_n_vertices(g) == 0);

   const auto h = create_empty_undirected_graph();
   assert(get_n_vertices(h) == 0);
}
```

Note that the type of graph does not matter here. One can count the number of vertices of every graph, as all graphs have vertices. Boost.Graph is very good at detecting operations that are not allowed, during compile time.

2.4 Counting the number of edges

Let's count all zero edges of an empty graph!

This is very similar to the previous chapter, only it uses boost::num_edges instead:

Algorithm 7 Count the number of edges

```
#include <cassert>
#include <boost/graph/adjacency_list.hpp>

template <typename graph>
int get_n_edges(const graph& g) noexcept
{
   const int n{
      static_cast<int>(boost::num_edges(g))
   };
   assert(static_cast<unsigned long>(n)
      == boost::num_edges(g)
   );
   return n;
}
```

This code is similar to the 'get_n_vertices' function (algorithm 5, see rationale there) except 'boost::num_edges' is used, instead of 'boost::num_vertices', which also returns an unsigned long.

The function 'get_n_edges' is demonstrated in algorithm 8, to measure the number of edges of an empty directed and undirected graph.

Algorithm 8 Demonstration of the 'get n edges' function

```
#include <cassert>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_n_edges.h"

void get_n_edges_demo() noexcept
{
   const auto g = create_empty_directed_graph();
   assert(get_n_edges(g) == 0);

   const auto h = create_empty_undirected_graph();
   assert(get_n_edges(h) == 0);
}
```

2.5 Adding a vertex

Empty graphs are nice, now its time to add a vertex!

To add a vertex to a graph, the boost::add_vertex function is used as shows in algorithm 9:

Algorithm 9 Adding a vertex to a graph

The static_assert at the top of the function checks during compiling if the function is called with a non-const graph. One can freely omit this static_assert: you will get a compiler error anyways, be it a less helpful one.

Note that boost::add_vertex (in the 'add_vertex' function) returns a vertex descriptor, which is ignored for now. Vertex descriptors are looked at in more details at the chapter 2.6, as we need these to add an edge. To allow for this already, 'add_vertex' also returns a vertex descriptor.

Algorithm 10 shows how to add a vertex to a directed and undirected graph.

Algorithm 10 Demonstration of the 'add vertex' function

```
#include "add_vertex.h"
#include "create_empty_directed_graph.h"

#include "create_empty_undirected_graph.h"

void add_vertex_demo() noexcept
{
   auto g = create_empty_undirected_graph();
   add_vertex(g);
   assert(boost::num_vertices(g) == 1);

auto h = create_empty_directed_graph();
   add_vertex(h);
   assert(boost::num_vertices(h) == 1);
}
```

This demonstration code creates two empty graphs, adds one vertex to each and then asserts that the number of vertices in each graph is one. This works for both types of graphs, as all graphs have vertices.

2.6 Vertex descriptors

A vertex descriptor is a handle to a vertex within a graph.

Vertex descriptors can be obtained by dereferencing a vertex iterator (see chapter 2.8). To do so, we first obtain some vertex iterators in chapter 2.7).

Vertex descriptors are used to:

- add and edge between two vertices, see chapter 2.9
- obtain properties of vertex a vertex, for example the vertex its out degrees (chapter 3.1), the vertex its name (chapter 4.4), or a custom vertex property (chapter 12.6)

In this tutorial, vertex descriptors have named prefixed with 'vd_', for example 'vd_1'.

2.7 Get the vertex iterators

You cannot get the vertices. This may sound unexpected, as it must be possible to work on the vertices of a graph. Working on the vertices of a graph is done throught these steps:

- Obtain a vertex iterator pair from the graph
- Dereferencing a vertex iterator to obtain a vertex descriptor

'vertices' (not 'boost::vertices') is used to obtain a vertex iterator pair, as shown in algorithm 11. The first vertex iterator points to the first vertex (its descriptor, to be precise), the second points to beyond the last vertex (its descriptor, to be precise). In this tutorial, vertex iterator pairs have named prefixed with 'vip_', for example 'vip_1'.

Algorithm 11 Get the vertex iterators of a graph

```
#include <boost/graph/adjacency_list.hpp>

template <typename graph>
std::pair <
    typename graph::vertex_iterator,
    typename graph::vertex_iterator
>
get_vertex_iterators(const graph& g) noexcept
{
    return vertices(g); //not boost::vertices
}
```

This is a somewhat trivial function, as it forwards the function call to 'vertices' (not 'boost::vertices').

These vertex iterators can be dereferenced to obtain the vertex descriptors. Note that 'get_vertex_iterators' will not be used often in isolation: usually one obtains the vertex descriptors immediatly. Just for your reference, algorithm 12 demonstrates of the 'get_vertices' function, by showing that the vertex iterators of an empty graph point to the same location.

Algorithm 12 Demonstration of 'get_vertex_iterators'

```
#include <cassert>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_vertex_iterators.h"

void get_vertex_iterators_demo() noexcept
{
   const auto g = create_empty_undirected_graph();
   const auto vip_g = get_vertex_iterators(g);
   assert(vip_g.first == vip_g.second);

const auto h = create_empty_directed_graph();
   const auto vip_h = get_vertex_iterators(h);
   assert(vip_h.first == vip_h.second);
}
```

2.8 Get all vertex descriptors

Vertex descriptors are the way to manipulate those vertices. Let's go get the all!

Vertex descriptors are obtained from dereferencing vertex iterators. Algorithm 13 shows how to obtain all vertex descriptors from a graph.

Algorithm 13 Get all vertex descriptors of a graph

```
#include <vector>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/graph_traits.hpp>

template <typename graph>
std::vector<
   typename boost::graph_traits<graph>::vertex_descriptor
> get_vertex_descriptors(const graph& g) noexcept
{
   using boost::graph_traits;
   using vd
   = typename graph_traits<graph>::vertex_descriptor;

   std::vector<vd> vds(boost::num_vertices(g));
   const auto vis = vertices(g); //not boost::vertices
   std::copy(vis.first, vis.second, std::begin(vds));
   return vds;
}
```

This is the first more complex piece of code. In the first lines, some 'using' statements allow for shorter type names⁶.

The std::vector to serve as a return value is created at the needed size, which is the number of vertices.

The function 'vertices' (not boost::vertices!) returns a vertex iterator pair. These iterators are used by std::copy to iterator over. std::copy is an STL algorithm to copy a half-open range. Prefer algorithm calls over hand-written for-loops ([9] chapter 18.12.1, [7] item 43).

In this case, we copy all vertex descriptors in the range produced by 'vertices' to the std::vector.

This function will not be used in practice: one iterates over the vertices directly instead, saving the cost of creating a std::vector. This function is only shown as an illustration.

Algorithm 14 demonstrates that an empty graph has no vertex descriptors:

⁶which may be necessary just to create a tutorial with code snippets that are readable

Algorithm 14 Demonstration of 'get vertex descriptors'

```
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_vertex_descriptors.h"

void get_vertex_descriptors_demo() noexcept
{
    const auto g = create_empty_undirected_graph();
    const auto vds_g = get_vertex_descriptors(g);
    assert(vds_g.empty());

const auto h = create_empty_directed_graph();
    const auto vds_h = get_vertex_descriptors(h);
    assert(vds_h.empty());
}
```

Because all graphs have vertices and thus vertex descriptors, the type of graph is unimportant for this code to compile.

2.9 Add an edge

To add an edge to a graph, two vertex descriptors are needed. A vertex descriptor is a handle to the vertex within a graph (vertex descriptors are looked at in more details in chapter 2.6). Algorithm 15 adds two vertices to a graph, and connects these two using boost::add_edge:

Algorithm 15 Adding (two vertices and) an edge to a graph

```
#include <cassert>
#include <type traits>
#include <boost/graph/adjacency list.hpp>
template <typename graph>
typename boost::graph traits<graph>::edge descriptor
add edge (graph& g) noexcept
  static assert (!std::is const<graph>::value,
    "graph_cannot_be_const"
  const auto vd a = boost :: add vertex(g);
 const auto vd b = boost::add vertex(g);
  const auto aer = boost::add edge(
   g
  );
  assert (aer.second);
  return aer.first;
```

Algorithm 15 shows how to add an isolated edge to a graph (instead of allowing for graphs with higher connectivities). First, two vertices are created, using the function 'boost::add_vertex'. 'boost::add_vertex' returns a vertex descriptor (which I prefix with 'vd'), both of which are stored. The vertex descriptors are used to add an edge to the graph, using 'boost::add_edge'. 'boost::add_edge' returns returns a std::pair, consisting of an edge descriptor and a boolean success indicator. The success of adding the edge is checked by an assert statement. Here we assert that this insertion was successfull. Insertion can fail if an edge is already present and duplicates are not allowed.

A demonstration of add_edge is shown in algorith 16, in which an edge is added to both a directed and undirected graph, after which the number of edges and vertices is checked.

Algorithm 16 Demonstration of 'add edge'

```
#include "add_edge.h"
#include "create_empty_directed_graph.h"

void add_edge_demo() noexcept
{
   auto g = create_empty_undirected_graph();
   add_edge(g);
   assert(boost::num_vertices(g) == 2);
   assert(boost::num_edges(g) == 1);

auto h = create_empty_directed_graph();
   add_edge(h);
   assert(boost::num_vertices(h) == 2);
   assert(boost::num_edges(h) == 1);
}
```

The graph type is unimportant: as all graph types have vertices and edges, edges can be added without possible compile problems.

2.10 boost::add_edge result

When using the function 'boost::add_edge', a 'std::pair<edge_descriptor,bool>' is returned. It contains both the edge descriptor (see chapter 2.12) and a boolean, which indicates insertion success.

In this tutorial, boost::add_edge results have named prefixed with 'aer_', for example 'aer_1'.

2.11 Getting the edge iterators

You cannot get the edges directly. Instead, working on the edges of a graph is done throught these steps:

- Obtain an edge iterator pair from the graph
- Dereference an edge iterator to obtain an edge descriptor

'edges' (not boost::edges!) is used to obtain an edge iterator pair. The first edge iterator points to the first edge (its descriptor, to be precise), the second points to beyond the last edge (its descriptor, to be precise). In this tutorial, edge iterator pairs have named prefixed with 'eip_', for example 'eip_1'. Algoritm 17 shows how to obtain these:

Algorithm 17 Get the edge iterators of a graph

```
#include <boost/graph/adjacency_list.hpp>
template <typename graph>
std::pair <
   typename graph::edge_iterator,
   typename graph::edge_iterator
>
get_edge_iterators(const graph& g) noexcept
{
   return edges(g); //not boost::edges
}
```

This is a somewhat trivial function, as all it does is forward to function call to 'edges' (not boost::edges!) These edge iterators can be dereferenced to obtain the edge descriptors. Note that this function will not be used often in isolation: usually one obtains the edge descriptors immediatly.

Algorithm 18 demonstrates 'get_edge_iterators' by showing that both iterators of the edge iterator pair point to the same location, when the graph is empty.

Algorithm 18 Demonstration of 'get edge iterators'

```
#include <cassert>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_edge_iterators.h"

void get_edge_iterators_demo() noexcept
{
    const auto g = create_empty_undirected_graph();
    const auto eip_g = get_edge_iterators(g);
    assert(eip_g.first == eip_g.second);

auto h = create_empty_directed_graph();
    const auto eip_h = get_edge_iterators(h);
    assert(eip_h.first == eip_h.second);
}
```

2.12 Edge descriptors

An edge descriptor is a handle to an edge within a graph. They are similar to vertex descriptors (chapter 2.6).

Edge descriptors are used to obtain the name, or other properties, of an edge In this tutorial, edge descriptors have named prefixed with 'ed_', for example 'ed_1'.

2.13 Get all edge descriptors

Obtaining all edge descriptors is similar to obtaining all vertex descriptors (algorithm 13), as shown in algorithm 19:

Algorithm 19 Get all edge descriptors of a graph

```
#include < vector >
#include <boost/graph/adjacency list.hpp>
#include "boost/graph/graph traits.hpp"
template <typename graph>
std::vector<
  typename boost::graph traits<graph>::edge descriptor
> get edge descriptors (const graph& g) noexcept
  using boost::graph_traits;
  using ed = typename graph traits<graph>::
     edge descriptor;
  std::vector<ed> eds;
  eds.reserve(boost::num edges(g));
  const auto ei = edges(g); //not boost::edges
  const auto j = ei.second;
  for (auto i = ei.first; i!=j; ++i) {
    eds.emplace back(*i);
  }
  return eds;
```

The only difference is that instead of the function 'vertices' (not boost::vertices!), 'edges' (not boost::edges!) is used.

Algorithm 20 demonstrates the 'get_edge_descriptor', by showing that empty graphs do not have any edge descriptors.

Algorithm 20 Demonstration of get edge descriptors

```
#include <cassert>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_edge_descriptors.h"

void get_edge_descriptors_demo() noexcept
{
    const auto g = create_empty_directed_graph();
    const auto eds_g = get_edge_descriptors(g);
    assert(eds_g.empty());

const auto h = create_empty_undirected_graph();
    const auto eds_h = get_edge_descriptors(h);
    assert(eds_h.empty());
}
```

2.14 Creating a directed graph

Finally, we are going to create a directed non-empty graph!

2.14.1 Graph

This directed graph is a two-state Markov chain, with two vertices and four edges, as depicted in figure 6:

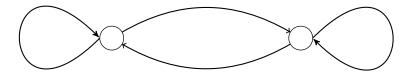


Figure 6: The two-state Markov chain

Note that directed graphs can have edges that start and end in the same vertex. These are called self-loops.

2.14.2 Function to create such a graph

To create this two-state Markov chain, the following code can be used:

Algorithm 21 Creating the two-state Markov chain as depicted in figure 6

```
#include <cassert>
#include "create empty directed graph.h"
boost::adjacency list <>
create markov chain() noexcept
  auto g = create_empty_directed_graph();
  const auto vd_a = boost::add_vertex(g);
  const auto vd_b = boost::add_vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer bb = boost::add edge(vd b, vd b, g);
  assert (aer bb.second);
  return g;
```

Instead of typing the complete type, we call the 'create_empty_directed_graph' function, and let auto figure out the type. The vertex descriptors (see chapter 2.6) created by two boost::add_vertex calls are stored to add an edge to the graph. Then boost::add_edge is called four times. Every time, its return type (see chapter 2.10) is checked for a successfull insertion.

Note that the graph lacks all properties: nodes do not have names, nor do edges.

2.14.3 Creating such a graph

Algorithm 22 demonstrates the 'create_markov_chain_graph' function and checks if it has the correct amount of edges and vertices:

Algorithm 22 Demonstration of the 'create markov chain'

```
#include <cassert>
#include "create_markov_chain.h"

void create_markov_chain_demo() noexcept
{
   const auto g = create_markov_chain();
   assert(boost::num_vertices(g) == 2);
   assert(boost::num_edges(g) == 4);
}
```

2.14.4 The .dot file produced

Running a bit ahead, this graph can be converted to a .dot file using the 'save_graph_to_dot' function (algorithm 48). The .dot file created is displayed in algorithm 23:

Algorithm 23 .dot file created from the 'create_markov_chain_graph' function (algorithm 21), converted from graph to .dot file using algorithm 48

```
digraph G {
0;
1;
0->0;
0->1;
1->0;
1->1;
1->0;
1->1;
```

From the .dot file one can already see that the graph is directed, because:

- The first word, 'digraph', denotes a directed graph (where 'graph' would have indicated an undirectional graph)
- The edges are written as '->' (where undirected connections would be written as '-')

2.14.5 The .svg file produced

The .svg file of this graph is shown in figure 7:



Figure 7: .svg file created from the 'create_markov_chain' function (algorithm 21) its .dot file and converted from .dot file to .svg using algorithm 279

This figure shows that the graph in directed, as the edges have arrow heads. The vertices display the node index, which is the default behavior.

2.15 Creating K_2 , a fully connected undirected graph with two vertices

Finally, we are going to create an undirected non-empty graph!

2.15.1 Graph

To create a fully connected undirected graph with two vertices (also called K_2), one needs two vertices and one (undirected) edge, as depicted in figure 8.



Figure 8: K_2 : a fully connected undirected graph with two vertices

2.15.2 Function to create such a graph

To create K_2 , the following code can be used:

Algorithm 24 Creating K_2 as depicted in figure 8

```
#include "create_empty_undirected_graph.h"

boost:: adjacency_list <
   boost:: vecS,
   boost:: vecS,
   boost:: undirectedS

create_k2_graph() noexcept
{
   auto g = create_empty_undirected_graph();
   const auto vd_a = boost:: add_vertex(g);
   const auto vd_b = boost:: add_vertex(g);
   const auto aer = boost:: add_edge(vd_a, vd_b, g);
   assert(aer.second);
   return g;
}</pre>
```

This code is very similar to the 'add_edge' function (algorithm 15). Instead of typing the graph its type, we call the 'create_empty_undirected_graph' function and let auto figure it out. The vertex descriptors (see chapter 2.6) created by two boost::add_vertex calls are stored to add an edge to the graph. From boost::add_edge its return type (see chapter 2.10), it is only checked that insertion has been successfull.

Note that the graph lacks all properties: nodes do not have names, nor do edges.

2.15.3 Creating such a graph

Algorithm 25 demonstrates how to 'create_k2_graph' and checks if it has the correct amount of edges and vertices:

Algorithm 25 Demonstration of 'create k2 graph'

```
#include <cassert>
#include "create_k2_graph.h"

void create_k2_graph_demo() noexcept
{
   const auto g = create_k2_graph();
   assert(boost::num_vertices(g) == 2);
   assert(boost::num_edges(g) == 1);
}
```

2.15.4 The .dot file produced

Running a bit ahead, this graph can be converted to the .dot file as shown in algorithm 26:

Algorithm 26 .dot file created from the 'create_k2_graph' function (algorithm 24), converted from graph to .dot file using algorithm 48

```
graph G {
0;
1;
0--1;
}
```

From the .dot file one can already see that the graph is undirected, because:

- The first word, 'graph', denotes an undirected graph (where 'digraph' would have indicated a directional graph)
- The edge between 0 and 1 is written as '-' (where directed connections would be written as '->', '<-' or '<>')

2.15.5 The .svg file produced

Continuing to running a bit ahead, this .dot file can be converted to the .svg as shown in figure 9:

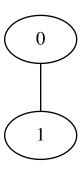


Figure 9: .svg file created from the 'create_k2_graph' function (algorithm 24) its .dot file, converted from .dot file to .svg using algorithm 279

Also this figure shows that the graph in undirected, otherwise the edge would have one or two arrow heads. The vertices display the node index, which is the default behavior.

2.16 \triangleright Creating K_3 , a fully connected undirected graph with three vertices

This is an extension of the previous chapter

2.16.1 Graph

To create a fully connected undirected graph with two vertices (also called K_2), one needs two vertices and one (undirected) edge, as depicted in figure 10.

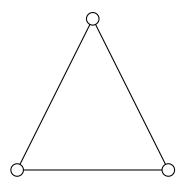


Figure 10: K_3 : a fully connected graph with three edges and vertices

2.16.2 Function to create such a graph

To create K_3 , the following code can be used:

Algorithm 27 Creating K_3 as depicted in figure 10

```
#include <cassert>
#include "create_empty_undirected_graph.h"
#include "create k3 graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS
create_k3_graph() noexcept
  auto g = create_empty_undirected_graph();
  const auto vd_a = boost::add_vertex(g);
  const auto vd_b = boost::add_vertex(g);
  const auto vd c = boost::add_vertex(g);
  const auto aer a = boost::add edge(vd a, vd b, g);
  assert (aer_a.second);
  const auto aer b = boost::add edge(vd b, vd c, g);
  assert (aer b.second);
  const auto aer c = boost::add edge(vd c, vd a, g);
  assert (aer c.second);
  return g;
```

2.16.3 Creating such a graph

Algorithm 28 demonstrates how to 'create_k2_graph' and checks if it has the correct amount of edges and vertices:

Algorithm 28 Demonstration of 'create k3 graph'

```
#include "create_k3_graph.h"

void create_k3_graph_demo() noexcept
{
  const auto g = create_k3_graph();
  assert(boost::num_edges(g) == 3);
  assert(boost::num_vertices(g) == 3);
}
```

2.16.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 29:

Algorithm 29 .dot file created from the 'create_k3_graph' function (algorithm 27), converted from graph to .dot file using algorithm 48

```
graph G {
0;
1;
2;
0--1;
1--2;
2--0;
}
```

2.16.5 The .svg file produced

Continuing to running a bit ahead, this .dot file can be converted to the .svg as shown in figure 11:

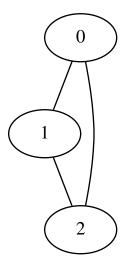


Figure 11: .svg file created from the 'create_k3_graph' function (algorithm 27) its .dot file, converted from .dot file to .svg using algorithm 279

2.17 ► Creating a path graph

A path graph is a linear graph without any branches

2.17.1 Graph

Here I show a path graph with four vertices (see figure 12):



Figure 12: A path graph with four vertices

2.17.2 Function to create such a graph

To create a path graph, the following code can be used:

Algorithm 30 Creating a path graph as depicted in figure 12

```
#include "create empty undirected graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS
create path graph(const int n vertices) noexcept
  assert(n vertices >= 2);
  auto g = create_empty_undirected_graph();
  auto vd 1 = boost :: add vertex(g);
  for (int i=1; i!=n vertices; ++i)
    auto vd_2 = boost::add_vertex(g);
    const auto aer = boost::add_edge(vd_1, vd_2, g);
    assert (aer.second);
    vd 1 = vd 2;
  return g;
}
```

2.17.3 Creating such a graph

Algorithm 31 demonstrates how to 'create_k2_graph' and checks if it has the correct amount of edges and vertices:

Algorithm 31 Demonstration of 'create path graph'

```
#include <cassert>
#include "create_path_graph.h"

void create_path_graph_demo() noexcept
{
   const auto g = create_path_graph(4);
   assert(boost::num_edges(g) == 3);
   assert(boost::num_vertices(g) == 4);
}
```

2.17.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 32:

Algorithm 32 .dot file created from the 'create_path_graph' function (algorithm 30), converted from graph to .dot file using algorithm 48

2.17.5 The .svg file produced

The .dot file can be converted to the .svg as shown in figure 13:

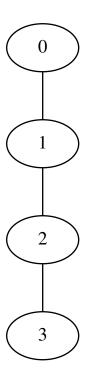


Figure 13: .svg file created from the 'create_path_graph' function (algorithm 30) its .dot file, converted from .dot file to .svg using algorithm 279

2.18 ► Creating a Peterson graph

This is an extension of the previous chapter.

2.18.1 Graph

To create a fully connected undirected graph with two vertices (also called K_2), one needs two vertices and one (undirected) edge, as depicted in figure 14.

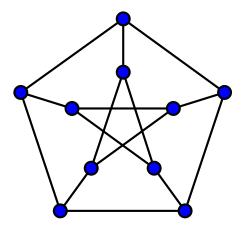


Figure 14: A Petersen graph (from https://en.wikipedia.org/wiki/Petersen_graph)

2.18.2 Function to create such a graph

To create a Petersen graph, the following code can be used:

```
#include <cassert>
#include "create_empty_undirected_graph.h"
boost::adjacency list <
  boost::vecS,
  boost :: vecS,
  boost::undirectedS
create petersen graph() noexcept
  auto g = create empty undirected graph();
  // Outer pentagon
  const auto vd oa = boost::add vertex(g);
  const auto vd ob = boost::add vertex(g);
  const auto vd oc = boost::add vertex(g);
  const auto vd_od = boost::add_vertex(g);
  const auto vd oe = boost::add vertex(g);
  //Inner pentagon
  const auto vd ia = boost::add vertex(g);
  const auto vd ib = boost::add vertex(g);
  const auto vd ic = boost::add vertex(g);
  const auto vd id = boost::add vertex(g);
  const auto vd ie = boost::add vertex(g);
  const auto aer 1 = boost::add edge(vd oa, vd ob, g);
  const auto aer 2 = boost::add edge(vd oa, vd ia, g);
  \mathbf{const} \ \mathbf{auto} \ \mathbf{aer} \_3 \ = \ \mathbf{boost} :: \mathbf{add} \_\mathbf{edge} ( \, \mathbf{vd} \_\mathbf{ob} \, , \ \, \mathbf{vd} \_\mathbf{oc} \, , \ \, \mathbf{g} ) \, ;
  {f const\ auto}\ {
m aer\_4}\ =\ {
m boost::add\_edge(vd\_ob,\ vd\_ib\,,\ g)}\,;
  const auto aer 5 = boost::add edge(vd oc, vd od, g);
  const auto aer_6 = boost::add_edge(vd_oc, vd_ic, g);
  const auto aer_7 = boost::add_edge(vd_od, vd_oe, g);
  const auto aer 8 = boost::add edge(vd_od, vd_id, g);
  const auto aer 9 = boost::add edge(vd_oe, vd_oa, g);
  const auto aer 10 = boost::add edge(vd oe, vd ie, g);
  const auto aer_11 = boost::add_edge(vd_ia, vd_ic, g);
  const auto aer 12 = boost::add edge(vd ib, vd id, g);
  const auto aer 13 = boost::add edge(vd ic, vd ie, g);
  const auto aer 14 = boost::add edge(vd id, vd ia, g);
  const auto aer 15 = boost::add edge(vd ie, vd ib, g);
  assert (aer 1.second);
  assert(aer_2.second);
  assert (aer_3.second);
  assert (aer 4. second);
  assert (aer 5. second);
                               44
  assert (aer_6.second);
  assert (aer_7.second);
  assert (aer 8. second);
  assert (aer 9. second);
  assert (aer_10.second);
  assert (aer 11. second);
  assert (aer_12.second);
```

assert (aer_13.second);

2.18.3 Creating such a graph

Algorithm 34 demonstrates how to use 'create_petersen_graph' and checks if it has the correct amount of edges and vertices:

Algorithm 34 Demonstration of 'create_k3_graph'

```
#include <cassert>
#include "create_petersen_graph.h"

void create_petersen_graph_demo() noexcept
{
   const auto g = create_petersen_graph();
   assert(boost::num_edges(g) == 15);
   assert(boost::num_vertices(g) == 10);
}
```

2.18.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 35:

Algorithm 35 .dot file created from the 'create_petersen_graph' function (algorithm 33), converted from graph to .dot file using algorithm 48

```
graph G {
0;
1;
2;
3;
4;
5;
6;
7;
8;
9;
0--1;
0--5;
1--2;
1--6;
2--3;
2--7;
3--4;
3--8;
4--0;
4--9;
5--7;
6--8;
7--9;
8--5;
9--6;
}
```

2.18.5 The .svg file produced

This . dot file can be converted to the .svg as shown in figure $15\colon$

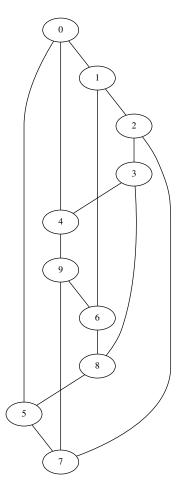


Figure 15: .svg file created from the 'create_petersen_graph' function (algorithm 33) its .dot file, converted from .dot file to .svg using algorithm 279

3 Working on graphs without properties

Now that we can build a graph, there are some things we can do.

- Getting the vertices' out degrees: see chapter 3.1
- Create a direct-neighbour subgraph from a vertex descriptor
- Create all direct-neighbour subgraphs from a graphs
- Saving a graph without properties to .dot file: see chapter 3.7
- \bullet Loading an undirected graph without properties from . dot file: see chapter 3.9

 \bullet Loading a directed graph without properties from . dot file: see chapter 3.8

3.1 Getting the vertices' out degree

Let's measure the out degree of all vertices in a graph!

The out degree of a vertex is the number of edges that originate at it.

The number of connections is called the 'degree' of the vertex. There are three types of degrees:

- in degree: the number of incoming connections, using 'in_degree' (not 'boost::in_edgree')
- out degree: the number of outgoing connections, using 'out_degree' (not 'boost::out edgree')
- degree: sum of the in degree and out degree, using 'degree' (not 'boost::edgree')

Algorithm 36 shows how to obtain these:

Algorithm 36 Get the vertices' out degrees

```
#include <boost/graph/adjacency list.hpp>
#include < vector >
\mathbf{template} \ < \!\! \mathbf{typename} \ \mathbf{graph} \!\! >
std::vector<int> get vertex out degrees(
  const graph& g
  noexcept
{
  std:: vector < int > v;
  v.reserve(boost::num vertices(g));
  const auto vis
    = vertices(g); //not boost::vertices
  const auto j = vis.second;
  for (auto i = vis.first; i!=j; ++i) {
    v.emplace back(
       out degree (*i,g) //not boost::out degree
    );
  }
  return v;
```

The structure of this algorithm is similar to 'get_vertex_descriptors' (algorithm 13), except that the out degrees from the vertex descriptors are stored. The out degree of a vertex iterator is obtained from the function 'out_degree' (not boost::out_degree!).

Albeit that the K_2 graph and the two-state Markov chain are rather simple, we can use it to demonstrate 'get_vertex_out_degrees' on, as shown in algorithm 37.

Algorithm 37 Demonstration of the 'get vertex out degrees' function

```
#include <cassert>
#include "create_k2_graph.h"
#include "create markov chain.h"
#include "get vertex out degrees.h"
void get vertex out degrees demo() noexcept
  const auto g = create_k2_graph();
  const std::vector<int> expected out degrees g\{1,1\};
  const std::vector<int> vertex out degrees g{
    get_vertex_out_degrees(g)
  };
  assert (expected_out_degrees_g
   == vertex out degrees g
  );
  const auto h = create_markov_chain();
  const std::vector<int> expected out degrees h\{2,2\};
  const std::vector<int> vertex_out_degrees_h{
    get vertex out degrees(h)
  };
  assert (expected_out_degrees_h
   == vertex_out_degrees_h
  );
```

It is expected that K_2 has one out-degree for every vertex, where the two-state Markov chain is expected to have two out-degrees per vertex.

3.2 Is there an edge between two vertices?

If you have two vertex descriptors, you can check if these are connected by an edge:

Algorithm 38 Check if there exists an edge between two vertices

```
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/graph_traits.hpp>

template <typename graph>
bool has_edge_between_vertices(
    const typename boost::graph_traits<graph>::
        vertex_descriptor&vd_1,
    const typename boost::graph_traits<graph>::
        vertex_descriptor&vd_2,
    const graph&g
) noexcept
{
    return edge( //not boost::edge
        vd_1, vd_2, g
      ).second;
}
```

This code uses the function 'edge' (not boost::edge: it returns a pair consisting of an edge descriptor and a boolean indicating if it is a valid edge descriptor. The boolean will be true if there exists an edge between the two vertices and false if not.

The demo shows that there is an edge between the two vertices of a K_2 graph, but there are no self-loops (edges that original and end at the same vertex).

Algorithm 39 Demonstration of the 'has edge between vertices' function

```
#include <cassert>
#include "create_k2_graph.h"
#include "has_edge_between_vertices.h"

void has_edge_between_vertices_demo() noexcept
{
   const auto g = create_k2_graph();
   const auto vd_1 = *vertices(g).first;
   const auto vd_2 = *(++vertices(g).first);
   assert( has_edge_between_vertices(vd_1, vd_2, g));
   assert(!has_edge_between_vertices(vd_1, vd_1, g));
}
```

3.3 Get the edge between two vertices

If you have two vertex descriptors, you can use these to find the edge between them.

Algorithm 40 Get the edge between two vertices

```
#include <boost/graph/adjacency list.hpp>
\# \mathbf{include}  " \mathbf{has} \_ \mathbf{edge} \_ \mathbf{between} \_ \mathbf{vertices} . \mathbf{h} "
template <
  typename graph,
  typename vertex_descriptor
typename boost::graph_traits<graph>::edge_descriptor
get edge between vertices (
  const vertex_descriptor& vd_from,
  const vertex _ descriptor& vd_to,
  const graph& g
  noexcept
  assert(has_edge_between_vertices(vd_from, vd_to, g));
  const auto er = edge(vd from, vd to, g);
  assert (er.second);
  return er.first;
}
```

This code does assume that there is an edge between the two vertices.

The demo shows how to get the edge between two vertices, deleting it, and checking for success.

Algorithm 41 Demonstration of the 'get edge between vertices' function

```
#include <cassert>
#include "create_k2_graph.h"
#include "get_edge_between_vertices.h"

void get_edge_between_vertices_demo() noexcept
{
    auto g = create_k2_graph();
    const auto vd_1 = *vertices(g).first;
    const auto vd_2 = *(++vertices(g).first);
    assert(has_edge_between_vertices(vd_1, vd_2, g));
    const auto ed = get_edge_between_vertices(vd_1, vd_2, g);
    boost::remove_edge(ed, g);
    assert(boost::num_edges(g) == 0);
}
```

3.4 Create a direct-neighbour subgraph from a vertex descriptor

Suppose you have a vertex of interest its vertex descriptor. Let's say you want to get a subgraph of that vertex and its direct neighbours only. This means that all vertices of that subgraph are adjacent vertices and that the edges go either from focal vertex to its neighbours, or from adjacent vertex to adjacent neighbour.

Here is the 'create direct neighbour subgraph' code:

```
#include <map>
#include <boost/graph/adjacency_list.hpp>
template < typename graph, typename vertex descriptor >
graph create direct neighbour subgraph (
  const vertex descriptor& vd,
  const graph& g
{
  graph h;
  \verb|std::map| < \verb|vertex_descriptor|, \verb|vertex_descriptor| > m;
    const auto vd_h = boost::add_vertex(h);
    m. insert (std::make pair (vd, vd h));
  //Copy vertices
    const auto vdsi = boost::adjacent_vertices(vd, g);
    std::transform(vdsi.first, vdsi.second,
      std::inserter(m, std::begin(m)),
      [&h] (const vertex descriptor& d)
         const auto vd h = boost :: add vertex(h);
         return std::make_pair(d,vd_h);
    );
  //Copy edges
  const auto eip = edges(g);
    std::for each(eip.first, eip.second,
      [g, \&h, m](const\ vertex\_descriptor\&\ vd)
         const auto vd\_from = source(vd, g);
         const auto vd to = target(vd, g);
         if \quad (m. find (vd from) != std :: end (m)
           \mathscr{E}\mathscr{E} m. find (vd to) != std :: end (m)
           const auto aer = boost :: add edge(m[vd from], m[
              vd to [, h];
           assert(aer.second);
                               53
    const auto j = eip.second;
    for (auto i = eip.first; i!=j; ++i)
      const auto vd_from = source(*i, g);
      const auto vd to = target(*i, g);
      if (m. find (vd from) = std :: end (m)) continue;
      if (m. find (vd to) == std :: end (m)) continue;
```

This demonstration code shows that the direct-neighbour graph of each vertex of a K2 graphs is ... a K2 graph!

Algorithm 43 Demo of the 'create_direct_neighbour_subgraph' function

3.5 Creating all direct-neighbour subgraphs from a graph without properties

Using the previous function, it is easy to create all direct-neighbour subgraphs from a graph without properties:

Algorithm 44 Create all direct-neighbour subgraphs from a graph without properties

```
#include < vector >
#include "create direct neighbour subgraph.h"
\mathbf{template} \ <\! \mathbf{typename} \ \mathbf{grap} \, h\! >\!
std::vector<graph> create_all_direct_neighbour_subgraphs(
  const graph g
) noexcept
{
  using vd = typename boost::graph traits<graph>::
      vertex descriptor;
  std::vector < graph > v;
  v.resize(boost::num_vertices(g));
  const auto vip = vertices(g);
  std::transform(
     vip.first , vip.second,
    std::begin(v),
     [g](const vd& d)
       return create_direct_neighbour_subgraph(
         d, g
       );
    }
  );
  {\bf return}\ v\,;
```

This demonstration code shows that all direct-neighbour graphs of a K2 graphs are ... K2 graphs!

Algorithm 45 Demo of the 'create_all_direct_neighbour_subgraphs' function

3.6 Are two graphs isomorphic?

You may want to check if two graphs are isomorphic. That is: if they have the same shape.

Algorithm 46 Check if two graphs are isomorphic

```
#include <boost/graph/isomorphism.hpp>

template <typename graph1, typename graph2>
bool is_isomorphic(
   const graph1 g,
   const graph2 h
) noexcept
{
   return boost::isomorphism(g,h);
}
```

This demonstration code shows that a K_3 graph is not equivalent to a 3-vertices path graph:

Algorithm 47 Demo of the 'is_isomorphic' function

```
#include <cassert>
#include "create_path_graph.h"
#include "create_k3_graph.h"
#include "is_isomorphic.h"

void is_isomorphic_demo() noexcept
{
   const auto g = create_path_graph(3);
   const auto h = create_k3_graph();
   assert(is_isomorphic(g,g));
   assert(!is_isomorphic(g,h));
}
```

3.7 Saving a graph to a .dot file

Graph are easily saved to a file, thanks to Graphviz. Graphviz (short for Graph Visualization Software) is a package of open-source tools for drawing graphs. It uses the DOT language for describing graphs, and these are commonly stored in (plain-text) .dot files (I show .dot file of every non-empty graph created, e.g. chapters 2.14.4 and 2.15.4)

Algorithm 48 Saving a graph to a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>

template <typename graph>
void save_graph_to_dot(
   const graph& g,
   const std::string& filename
) noexcept
{
   std::ofstream f(filename);
   boost::write_graphviz(f,g);
}
```

All the code does is create an std::ofstream (an output-to-file stream) and use boost::write_graphviz to write the DOT description of our graph to that stream. Instead of 'std::ofstream', one could use std::cout (a related output stream) to display the DOT language on screen directly.

Algorithm 49 shows how to use the 'save graph to dot' function:

Algorithm 49 Demonstration of the 'save graph to dot' function

```
#include "create_k2_graph.h"
#include "create_markov_chain.h"
#include "save_graph_to_dot.h"

void save_graph_to_dot_demo() noexcept
{
   const auto g = create_k2_graph();
   save_graph_to_dot(g, "create_k2_graph.dot");

   const auto h = create_markov_chain();
   save_graph_to_dot(h, "create_markov_chain.dot");
}
```

When using the 'save_graph_to_dot' function (algorithm 48), only the structure of the graph is saved: all other properties like names are not stored. Algorithm 91 shows how to do so.

3.8 Loading a directed graph from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph is loaded, as shown in algorithm 50:

Algorithm 50 Loading a directed graph from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create_empty_directed_graph.h"
#include "is_regular_file.h"

boost::adjacency_list <>
load_directed_graph_from_dot(
    const std::string& dot_filename));
    std::ifstream f(dot_filename.c_str());
    auto g = create_empty_directed_graph();
    boost::dynamic_properties p(
        boost::ignore_other_properties);
    boost::read_graphviz(f,g,p);
    return g;
}
```

In this algorithm, first it is checked if the file to load exists, using the 'is_regular_file' function (algorithm 280), after which an std::ifstream is opened. Then an empty directed graph is created, which saves us writing down the template arguments explicitly. Then, a boost::dynamic_properties is created with the 'boost::ignore_other_properties' in its constructor (using a default constructor here results in the run-time error 'property not found: node_id', see chapter 24.5). From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

Algorithm 51 shows how to use the 'load_directed_graph_from_dot' function:

Algorithm 51 Demonstration of the 'load_directed_graph_from_dot' function

```
#include <cassert>
#include "create_markov_chain.h"
#include "load_directed_graph_from_dot.h"

#include "save_graph_to_dot.h"

void load_directed_graph_from_dot_demo() noexcept
{
    using boost::num_edges;
    using boost::num_vertices;

    const auto g = create_markov_chain();
    const std::string filename{
        "create_markov_chain.dot"
    };
    save_graph_to_dot(g, filename);
    const auto h = load_directed_graph_from_dot(filename);
    assert(num_edges(g) == num_edges(h));
    assert(num_vertices(g) == num_vertices(h));
}
```

This demonstration shows how the Markov chain is created using the 'create_markov_chain_graph' function (algorithm 21), saved and then loaded. The loaded graph is then checked to be a two-state Markov chain.

3.9 Loading an undirected graph from a .dot file

Loading an undirected graph from a .dot file is very similar to loading a directed graph from a .dot file, as shown in chapter 3.8. Algorithm 52 show how to do so:

Algorithm 52 Loading an undirected graph from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create empty undirected graph.h"
#include "is regular file.h"
boost::adjacency_list <
  boost::vecS,
  boost :: vecS,
  boost:: undirected S\\
load undirected graph from dot (
  const std::string& dot_filename
{
  assert(is_regular_file(dot_filename));
  std::ifstream f(dot filename.c str());
  auto g = create_empty_undirected_graph();
  boost::dynamic_properties p(
    boost::ignore_other_properties
  boost::read graphviz(f,g,p);
  return g;
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 3.8 describes the rationale of this function.

Algorithm 53 shows how to use the 'load_undirected_graph_from_dot' function:

Algorithm 53 Demonstration of the 'load_undirected_graph_from_dot' function

This demonstration shows how the K_2 graph is created using the 'create_k2_graph' function (algorithm 24), saved and then loaded. The loaded graph is checked to be a K_2 graph.

4 Building graphs with named vertices

Up until now, the graphs created have had edges and vertices without any propery. In this chapter, graphs will be created, in which the vertices can have a name. This name will be of the std::string data type, but other types are possible as well. There are many more built-in properties edges and nodes can have (see chapter 25.1 for a list).

In this chapter, we will build the following graphs:

- An empty directed graph that allows for vertices with names: see chapter 4.1
- An empty undirected graph that allows for vertices with names: see chapter 4.2
- Two-state Markov chain with named vertices: see chapter 4.5
- K_2 with named vertices: see chapter 4.6

In the process, some basic (sometimes bordering trivial) functions are shown:

- Adding a named vertex: see chapter 4.3
- Getting the vertices' names: see chapter 4.4

After this chapter you may want to:

- Building graphs with named edges and vertices: see chapter 6
- Building graphs with bundled vertices: see chapter 8
- Building graphs with custom vertices: see chapter 12
- Building graphs with a graph name: see chapter 18

4.1 Creating an empty directed graph with named vertices

Let's create a trivial empty directed graph, in which the vertices can have a name:

Algorithm 54 Creating an empty directed graph with named vertices

```
#include < string >
#include <boost/graph/adjacency_list.hpp>
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS,
  boost::property<
    boost::vertex_name_t, std::string
create empty directed named vertices graph() noexcept
  return boost::adjacency list <
    boost :: vecS,
    boost :: vecS,
    boost::directedS,
    boost::property<
      boost::vertex name t, std::string
 > ();
```

Instead of using a boost::adjacency_list with default template argument, we will now have to specify four template arguments, where we only set the fourth to a non-default value.

Note there is some flexibility in this function: the data type of the vertex names is set to std::string by default, but can be of any other type if desired. This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)
- is directed (due to the boost::directedS)
- The vertices have one property: they have a name, which is of data type std::string (due to the boost::property
boost::vertex name t, std::string>')
- Edges and graph have no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fourth template argument 'boost::property < boost::vertex_name_t, std::string>'. This can be read as: "vertices have the property 'boost::vertex_name_t', that is of data type std::string". Or simply: "vertices have a name that is stored as a std::string".

Algorithm 55 shows how to create such a graph:

4.2 Creating an empty undirected graph with named vertices

Let's create a trivial empty undirected graph, in which the vertices can have a name:

Algorithm 56 Creating an empty undirected graph with named vertices

```
#include < string>
\#include < boost/graph/adjacency_list.hpp>
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex name t, std::string
create_empty_undirected_named_vertices_graph() noexcept
  return boost::adjacency_list<
    boost :: vecS,
    boost :: vecS,
    boost::undirectedS,
    boost::property<
      boost::vertex_name_t, std::string
 > ();
}
```

This code is very similar to the code described in chapter 4.1, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS). See chapter 4.1 for most of the explanation.

Algorithm 57 shows how to create such a graph:

```
Algorithm
                57
                        Demonstration
                                                 the
                                                          'cre-
ate_empty_undirected_named_vertices_graph' function
#include < cassert >
#include <boost/graph/adjacency_list.hpp>
#include "create_empty_undirected_named_vertices_graph.h"
void create_empty_undirected_named_vertices_graph_demo()
   noexcept
  const auto g
    = create empty undirected named vertices graph();
  assert(boost::num\_vertices(g) == 0);
  assert(boost::num edges(g) == 0);
}
```

4.3 Add a vertex with a name

Adding a vertex without a name was trivially easy (see chapter 2.5). Adding a vertex with a name takes slightly more work, as shown by algorithm 58:

Algorithm 58 Adding a vertex with a name

```
#include < string>
#include <type_traits>
#include <boost/graph/adjacency list.hpp>
template <typename graph>
typename boost::graph traits<graph>::vertex descriptor
add named vertex (
  const std::string& vertex name,
  graph& g
 noexcept
  static assert (!std::is const<graph>::value,
    "graph_cannot_be_const"
  const auto vd = boost::add_vertex(g);
  auto vertex name map
    = \gcd(\ //not\ boost::get
      boost::vertex name, g
    );
  put(vertex name map, vd, vertex name);
  return vd;
```

Instead of calling 'boost::add_vertex' with an additional argument containing the name of the vertex⁷, multiple things need to be done:

First, the static_assert at the top of the function checks during compiling if the function is called with a non-const graph. One can freely omit this static assert: you will get a compiler error anyways, be it a less helpful one.

When adding a new vertex to the graph, the vertex descriptor (as described in chapter 2.6) is stored. After obtaining the name map from the graph (using 'get(boost::vertex_name,g)'), the name of the vertex is set using that vertex descriptor. Note that 'get' has no 'boost::' prepending it, as it lives in the same (global) namespace the function is in. Using 'boost::get' will not compile.

Using 'add_named_vertex' is straightforward, as demonstrated by algorithm $59.\,$

⁷I am unsure if this would have been a good interface. I am sure I expected this interface myself. I do see a problem with multiple properties and the order of initialization, but initialization could simply follow the same order as the the property list.

Algorithm 59 Demonstration of 'add named vertex'

4.4 Getting the vertices' names

When the vertices of a graph have named vertices, one can extract them as such:

Algorithm 60 Get the vertices' names

```
#include < string>
#include < vector >
#include <boost/graph/adjacency list.hpp>
#include <boost/graph/properties.hpp>
#include <boost/graph/graph traits.hpp>
template <typename graph>
std::vector<std::string> get vertex names(
  const graph& g
  noexcept
  std::vector < std::string > v;
  v.reserve(boost::num vertices(g));
  const auto vertex name map = get (
    boost::vertex name, g
  );
  const auto vip
    = vertices (g); //not boost::vertices
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i) {
    v.emplace back(
      get( //not \ boost :: get
        vertex_name_map,
    );
  return v;
```

This code is very similar to 'get_vertex_out_degrees' (algorithm 36), as also there we iterated through all vertices, accessing all vertex descriptors sequentially.

The names of the vertices are obtained from a boost::property_map and then put into a std::vector.

The order of the vertex names may be different after saving and loading.

When trying to get the vertices' names from a graph without vertices with names, you will get the error 'formed reference to void' (see chapter 24.1).

Algorithm 61 shows how to add two named vertices, and check if the added names are retrieved as expected.

Algorithm 61 Demonstration of 'get vertex names'

```
#include <cassert>
#include "add named vertex.h"
#include "create empty undirected named vertices graph.h"
#include "get vertex names.h"
void get vertex names demo() noexcept
  auto g
    = create empty undirected named vertices graph();
  const std::string vertex name 1{"Chip"};
  const std::string vertex name 2{"Chap"};
  add_named_vertex(vertex_name_1, g);
  add named vertex (vertex name 2, g);
  const std::vector<std::string> expected names{
    {\tt vertex\_name\_1}\;,\;\;{\tt vertex\_name\_2}
  };
  const std::vector<std::string> vertex names{
    get_vertex_names(g)
  assert (expected names == vertex names);
}
```

4.5 Creating a Markov chain with named vertices

Let's create a directed non-empty graph with named vertices!

4.5.1 Graph

We extend the Markov chain of chapter 2.14 by naming the vertices 'Good' and 'Not bad', as depicted in figure 16:



Figure 16: A two-state Markov chain where the vertices have texts

The vertex names are nonsensical, but I choose these for a reason: one name is only one word, the other has two words (as it contains a space). This will have implications for file I/O.

4.5.2 Function to create such a graph

To create this Markov chain, the following code can be used:

Algorithm 62 Creating a Markov chain with named vertices as depicted in figure 16

```
#include <cassert>
#include "create_empty_directed_named_vertices_graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS ,
  boost::property<boost::vertex name t, std::string>
create named vertices markov chain() noexcept
  auto g
    = create empty directed named vertices graph();
  const auto vd_a = boost::add_vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer_ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer bb = boost::add edge(vd b, vd b, g);
  assert (aer bb.second);
  auto name_map = get( //not boost::get
    boost::vertex name, g
  name map[vd a] = "Good";
  name map[vd b] = "Not_bad";
  return g;
}
```

Most of the code is a repeat of algorithm 21, 'create_markov_chain_graph'. In the end of the function body, the names are obtained as a boost::property_map and set to the desired values.

4.5.3 Creating such a graph

Also the demonstration code (algorithm 63) is very similar to the demonstration code of the 'create markov chain graph' function (algorithm 22).

Algorithm 63 Demonstrating the 'create_named_vertices_markov_chain' function

4.5.4 The .dot file produced

Because the vertices now have a name, this should be visible in the .dot file:

Algorithm 64 .dot file created from the 'create_named_vertices_markov_chain' function (algorithm 62), converted from graph to .dot file using algorithm 48

```
digraph G {
0[label=Good];
1[label="Not bad"];
0->0;
1->0;
1->1;
1->1;
}
```

As one can see, the names are stored as a label. Note that if a vertex name contains a space, the name will be surrounded by quotes, for example '1[label="Not bad"];'.

4.5.5 The .svg file produced

Now that the vertices have names, this should be reflected in the .svg:

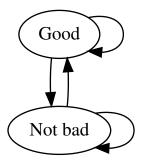


Figure 17: .svg file created from the 'create_named_vertices_markov_chain' function (algorithm 62) its .dot file, converted from .dot file to .svg using algorithm 279

The .svg now shows the vertex names, instead of the vertex indices.

4.6 Creating K_2 with named vertices

Let's create an undirected non-empty graph with named vertices!

4.6.1 Graph

We extend K_2 of chapter 2.15 by naming the vertices 'Me' and 'My computer', as depicted in figure 18:

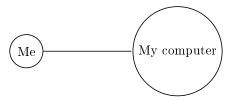


Figure 18: K_2 : a fully connected graph with two named vertices

4.6.2 Function to create such a graph

To create K_2 , the following code can be used:

Algorithm 65 Creating K_2 with named vertices as depicted in figure 18

```
#include <cassert>
#include "create_empty_undirected_named_vertices_graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property\!<\!boost::vertex\_name\_t\;,std::string\!>
create named vertices k2 graph() noexcept
  auto g
    = create_empty_undirected_named_vertices_graph();
  const auto vd_a = boost::add_vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer = boost::add edge(vd a, vd b, g);
  assert (aer.second);
  auto name_map = get( //not boost::get
    boost::vertex name, g
  name map[vd a] = "Me";
  name map[vd b] = "My_computer";
  return g;
}
```

Most of the code is a repeat of algorithm 24. In the end, the names are obtained as a boost::property map and set to the desired names.

4.6.3 Creating such a graph

Also the demonstration code (algorithm 66) is very similar to the demonstration code of the 'create_k2_graph function' (algorithm 24).

Algorithm 66 Demonstrating the 'create k2 graph' function

4.6.4 The .dot file produced

Because the vertices now have a name, this should be visible in the .dot file:

Algorithm 67 .dot file created from the 'create_named_vertices_k2' function (algorithm 65), converted from graph to .dot file using algorithm 91

```
graph G {
O[label=Me];
1[label="My computer"];
0--1;
}
```

As one can see, the names are stored as a label. Note that if a vertex name contains a space, the name will be surrounded by quotes, for example '1[label="My computer"];'.

4.6.5 The .svg file produced

Now that the vertices have names, this should be reflected in the .svg:

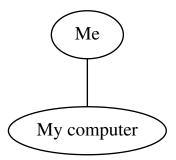


Figure 19: .svg file created from the 'create_named_vertices_k2_graph' function (algorithm 62) its .dot file, converted from .dot file to .svg using algorithm 91

The .svg now shows the vertex names, instead of the vertex indices.

4.7 ► Creating a path graph with named vertices

Here we create a path graph with names vertices

4.7.1 Graph

Here I show a path graph with four vertices (see figure 20):



Figure 20: A path graph with four vertices

4.7.2 Function to create such a graph

To create a path graph, the following code can be used:

Algorithm 68 Creating a path graph as depicted in figure 20

```
#include < vector >
#include "create_empty_undirected_named_vertices_graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex name t, std::string
create_named_vertices_path_graph(
  const std::vector<std::string>& names
) noexcept
{
  auto g = create empty undirected named vertices graph()
  if (names.size() == 0) \{ return g; \}
  auto vertex name map
    = get( //not boost::get
      boost::vertex name,
    );
  auto vd 1 = boost :: add vertex(g);
  vertex name map [vd 1] = *names.begin();
  if (names.size() == 1) return g;
  const auto j = std :: end (names);
  auto i = std :: begin(names);
  for (++i; i!=j; ++i) // Skip first
    auto vd 2 = boost :: add vertex(g);
    vertex name map [vd 2] = *i;
    const auto aer = boost :: add_edge(vd_1, vd_2, g);
    assert (aer.second);
    vd\_1 \ = \ vd \ \ 2 \, ;
  return g;
}
```

4.7.3 Creating such a graph

Algorithm 69 demonstrates how to create a path graph with named vertices and checks if it has the correct amount of edges and vertices:

Algorithm 69 Demonstration of 'create named vertices path graph'

4.7.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 70:

Algorithm 70 .dot file created from the 'create_named_vertices_path_graph' function (algorithm 68), converted from graph to .dot file using algorithm 48

4.7.5 The .svg file produced

The .dot file can be converted to the .svg as shown in figure 21:

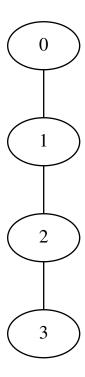


Figure 21: .svg file created from the 'create_named_vertices_path_graph' function (algorithm 68) its .dot file, converted from .dot file to .svg using algorithm 279

5 Working on graphs with named vertices

When vertices have names, this name gives a way to find a vertex and working with it. This chapter shows some basic operations on graphs with named vertices.

- Check if there exists a vertex with a certain name: chapter 5.1
- Find a vertex by its name: chapter 5.2
- Get a named vertex its degree, in degree and out degree: chapter: 5.3
- Get a vertex its name from its vertex descriptor: chapter 5.4
- Set a vertex its name using its vertex descriptor: chapter 5.5
- Setting all vertices' names: chapter 5.6
- Clear a named vertex its edges: chapter 5.7
- Remove a named vertex: chapter 5.8

- Removing an edge between two named vertices: chapter 5.9
- Saving an directed/undirected graph with named vertices to a .dot file: chapter 5.11
- \bullet Loading a directed graph with named vertices from a .dot file: chapter 5.12
- Loading an undirected graph with named vertices from a .dot file: chapter 5 13

Especially the 'find_first_vertex_by_name' function (chapter 5.2) is important, as it shows how to obtain a vertex descriptor, which is used in later algorithms.

5.1 Check if there exists a vertex with a certain name

Before modifying our vertices, let's first determine if we can find a vertex by its name in a graph. After obtaing a name map, we obtain the vertex iterators, dereference these to obtain the vertex descriptors and then compare each vertex its name with the one desired.

Algorithm 71 Find if there is vertex with a certain name

```
\#include <boost/graph/properties.hpp>
template <typename graph>
bool has vertex with name (
  const std::string& vertex name,
  const graph& g
  noexcept
  {\bf const\ auto\ } {\rm vertex\_name\_map}
    = get( //not boost::get
      boost::vertex name,
    );
  const auto vip
    = vertices (g); //not boost::vertices
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i) {
    if (
      get( //not \ boost::get
        vertex\_name\_map\;,
        * i
      ) == vertex name
    ) {
      return true;
  return false;
```

This function can be demonstrated as in algorithm 72, where a certain name cannot be found in an empty graph. After adding the desired name, it is found.

Algorithm 72 Demonstration of the 'has vertex with name' function

Note that this function only finds if there is at least one vertex with that name: it does not tell how many vertices with that name exist in the graph.

5.2 Find a vertex by its name

Where STL functions work with iterators, here we obtain a vertex descriptor (see chapter 2.6) to obtain a handle to the desired vertex. Algorithm 73 shows how to obtain a vertex descriptor to the first (name) vertex found with a specific name.

Algorithm 73 Find the first vertex by its name

```
#include <cassert>
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "has vertex with name.h"
template <typename graph>
typename boost::graph traits<graph>::vertex descriptor
find_first_vertex_with_name(
  const std::string& name,
  const graph& g
 noexcept
  assert(has_vertex_with_name(name, g));
  {\bf const\ auto\ vertex\_name\_map}
    = get(boost::vertex name,g);
  const auto vip
    = vertices (g); //not boost::vertices
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i) {
    const std::string s{
       get ( //not boost :: get
         vertex name map,
    };
    if (s == name) { return *i; }
  assert (!"Should_not_get_here");
  \mathbf{throw}\,;\ //\,\mathit{Will}\ \mathit{crash}\ \mathit{the}\ \mathit{program}
}
```

With the vertex descriptor obtained, one can read and modify the vertex and the edges surrounding it. Algorithm 74 shows some examples of how to do so.

Algorithm 74 Demonstration of the 'find first vertex with name' function

5.3 Get a (named) vertex its degree, in degree and out degree

We already obtained all out degrees of all vertices in chapter 3.1 by just collecting all vertex descriptors. Here, we will search for a vertex with a certain name, obtain its vertex descriptor and find the number of connections it has.

With a vertex descriptor, we can read a vertex its types of degrees. Algorithm 73 shows how to find a vertex, obtain its vertex descriptor and then obtain the out degree from it.

Algorithm 75 Get the first vertex with a certain name its out degree from its vertex descriptor

```
#include <cassert>
#include "find_first_vertex_with_name.h"
#include "has vertex with name.h"
\mathbf{template} \hspace{0.1cm} < \hspace{-0.1cm} \mathbf{typename} \hspace{0.1cm} \mathbf{graph} >
int get_first_vertex_with_name_out_degree(
  const std::string& name,
  const graph& g) noexcept
  assert (has vertex with name (name, g));
  const auto vd
     = find_first_vertex_with_name(name, g);
  const int od {
     static cast < int > (
       out_degree(vd, g) //not boost::out_degree
  };
  assert(static\_cast < unsigned long > (od)
    == out_degree(vd, g)
  return od;
```

Algorithm 76 shows how to use this function.

Algorithm 76 Demonstration of the 'get_first_vertex_with_name_out_degree' function

```
#include < cassert >
#include "create named vertices k2 graph.h"
#include "get_first_vertex_with_name_out_degree.h"
void get first vertex with name out degree demo()
   noexcept
{
  const auto g = create_named_vertices_k2_graph();
  assert (
    get first vertex with name out degree (
       ^{\prime\prime}\mathrm{Me^{\prime\prime}} , g
    = 1
  );
  assert (
    get first vertex with name out degree (
       "My_computer", g
    ) == 1
  );
}
```

5.4 Get a vertex its name from its vertex descriptor

This may seem a trivial paragraph, as chapter 4.4 describes the 'get_vertex_names' algorithm, in which we get all vertices' names. But it does not allow to first find a vertex of interest and subsequently getting only that one its name.

To obtain the name from a vertex descriptor, one needs to pull out the name map and then look up the vertex of interest.

Algorithm 77 Get a vertex its name from its vertex descriptor

```
#include <string>
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>

template <typename graph>
std::string get_vertex_name(
    const typename boost::graph_traits<graph>::
        vertex_descriptor&vd,
    const graph&g
) noexcept
{
    const auto vertex_name_map
        = get( //not boost::get
        boost::vertex_name,
        g
      );
    return vertex_name_map[vd];
}
```

To use 'get_vertex_name', one first needs to obtain a vertex descriptor. Algorithm 78 shows a simple example:

Algorithm 78 Demonstration if the 'get vertex name' function

5.5 Set a (named) vertex its name from its vertex descriptor

If you know how to get the name from a vertex descriptor, setting it is just as easy, as shown in algorithm 79.

Algorithm 79 Set a vertex its name from its vertex descriptor

```
#include <boost/graph/graph traits.hpp>
\#include <boost/graph/properties.hpp>
template <typename graph>
void set_vertex_name(
  const std::string& any vertex name,
  const typename boost::graph traits<graph>::
      vertex descriptor& vd,
  graph& g
  noexcept
  static \quad assert \; (\,!\,std:: is\_const\!<\!graph\!>:: value \;,
    "graph_cannot_be_const"
  auto vertex name map
    = get( //not boost::get
      boost::vertex name,
    );
  vertex_name_map[vd]
    = any_vertex_name;
}
```

To use 'set_vertex_name', one first needs to obtain a vertex descriptor. Algorithm 80 shows a simple example.

Algorithm 80 Demonstration if the 'set vertex name' function

```
#include <cassert>
#include "add named vertex.h"
#include "create empty undirected named vertices graph.h"
#include "find first vertex with name.h"
#include "get_vertex_name.h"
#include "set vertex name.h"
void set vertex_name_demo() noexcept
  auto g
    = create empty undirected named vertices graph();
  const std::string old_name{"Dex"};
  add named vertex (old name, g);
  const auto vd
    = find_first_vertex_with_name(old_name,g);
  assert(get\_vertex\_name(vd,g) = old\_name);
  const std::string new name{"Diggy"};
  set_vertex_name(new_name, vd, g);
  assert(get_vertex_name(vd,g) = new_name);
```

5.6 Setting all vertices' names

When the vertices of a graph have named vertices and you want to set all their names at once:

Algorithm 81 Setting the vertices' names

```
#include < string>
#include < vector >
#include <boost/graph/graph traits.hpp>
\# \mathbf{include} < \mathbf{boost} / \mathbf{graph} / \mathbf{properties} . \mathbf{hpp} >
template <typename graph>
void set_vertex_names(
  graph&g,
  const std::vector<std::string>& names
  noexcept
  static_assert(!std::is_const<graph>::value, "graph_
      cannot_be_const");
  const auto vertex name map
    = get(boost::vertex name,g);
  auto ni = std::begin(names);
  const auto names end = std::end(names);
  const auto vip
    = vertices(g); //not boost::vertices
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i, ++ni)
    assert (ni != names end);
    put(vertex name map, *i,*ni);
}
```

A new function makes its appearance here: 'put' (not 'boost::put'), which is the opposite of 'get' (not 'boost::get')

This is not a very usefull function if the graph is complex. But for just creating graphs for debugging, it may come in handy.

5.7 Clear the edges of a named vertex

A vertex descriptor can be used to clear all in/out/both edges connected to a vertex. It is necessary to remove these connections before the vertex itself can be removed. There are three functions to remove the edges connected to a vertex:

- boost::clear vertex: removes all edges to and from the vertex
- boost::clear out edges: removes all outgoing edges from the vertex (in

directed graphs only, else you will get a 'error: no matching function for call to clear out edges', as described in chapter 24.2)

• boost::clear_in_edges: removes all incoming edges from the vertex (in directed graphs only, else you will get a 'error: no matching function for call to clear in edges', as described in chapter 24.3)

In the algorithm 'clear_first_vertex_with_name' the 'boost::clear_vertex' algorithm is used, as the graph used is undirectional:

Algorithm 82 Clear the first vertex with a certain name

Algorithm 83 shows the clearing of the first named vertex found.

Algorithm 83 Demonstration of the 'clear first vertex with name' function

```
#include < cassert >
#include "clear_first_vertex_with_name.h"
#include "create_named_vertices_k2_graph.h"

void clear_first_vertex_with_name_demo() noexcept
{
   auto g = create_named_vertices_k2_graph();
   assert (boost::num_edges(g) == 1);
   clear_first_vertex_with_name("My_computer",g);
   assert (boost::num_edges(g) == 0);
}
```

5.8 Remove a named vertex

A vertex descriptor can be used to remove a vertex from a graph. It is necessary to remove these connections (e.g. using clear_first_vertex_with_name', algorithm 82) before the vertex itself can be removed.

Removing a named vertex goes as follows: use the name of the vertex to get a first vertex descriptor, then call 'boost::remove_vertex', shown in algorithm 5.8:

Algorithm 84 Remove the first vertex with a certain name

```
#include <boost/graph/adjacency list.hpp>
#include "find first vertex with name.h"
#include "has vertex with name.h"
template <typename graph>
void remove first vertex with name (
  const std::string& name,
  graph& g
 noexcept
  static assert (!std::is const<graph>::value,
    "graph_cannot_be_const"
  );
  assert (has vertex with name (name, g));
  const auto vd
    = find_first_vertex_with_name(name,g);
  assert(degree(vd,g) == 0); //not degree
  boost::remove vertex(vd,g);
}
```

Algorithm 85 shows the removal of the first named vertex found.

Algorithm 85 Demonstration of the 'remove_first_vertex_with_name' function

```
#include <cassert>
#include "clear_first_vertex_with_name.h"
#include "create_named_vertices_k2_graph.h"
#include "remove_first_vertex_with_name.h"

void remove_first_vertex_with_name_demo() noexcept
{
    auto g = create_named_vertices_k2_graph();
    clear_first_vertex_with_name(
        "My_computer",g
);
    remove_first_vertex_with_name(
        "My_computer",g
);
    assert(boost::num_edges(g) == 0);
    assert(boost::num_vertices(g) == 1);
}
```

Again, be sure that the vertex removed does not have any connections!

5.9 Removing the edge between two named vertices

Instead of looking for an edge descriptor, one can also remove an edge from two vertex descriptors (which is: the edge between the two vertices). Removing an edge between two named vertices named edge goes as follows: use the names of the vertices to get both vertex descriptors, then call 'boost::remove_edge' on those two, as shown in algorithm 86.

Algorithm 86 Remove the first edge with a certain name

```
#include "find first vertex with name.h"
\#include "has_vertex_with_name.h"
#include "has edge between vertices.h"
template <typename graph>
void remove_edge_between_vertices_with_names(
  const std::string& name 1,
  const std::string& name 2,
  graph& g
 noexcept
  static_assert(!std::is_const<graph>::value,
    "graph_cannot_be_const"
  assert (has vertex with name (name 1, g));
  assert (has_vertex_with_name(name_2, g));
  const auto vd 1
    = find_first_vertex_with_name(name_1, g);
  const auto vd 2
    = find_first_vertex_with_name(name_2, g);
  assert (has edge between vertices (vd 1, vd 2, g));
  boost::remove edge(vd 1, vd 2, g);
}
```

Algorithm 87 shows the removal of the first named edge found.

```
        Algorithm
        87
        Demonstration
        of
        the
        'remove_edge_between_vertices_with_names' function
```

```
#include <cassert>
#include "create_named_edges_and_vertices_k3_graph.h"
#include "remove_edge_between_vertices_with_names.h"

void remove_edge_between_vertices_with_names_demo()
    noexcept
{
    auto g = create_named_edges_and_vertices_k3_graph();
    assert(boost::num_edges(g) == 3);
    remove_edge_between_vertices_with_names("top","right",g
        );
    assert(boost::num_edges(g) == 2);
}
```

5.10 Are two graphs with named vertices isomorphic?

Strictly speaking, finding isomorphisms is about the shape of the graph, independent of vertex name, and is already done in chapter 3.6.

Here, it is checked if two graphs with named vertices are 'label isomorphic' (please email me a better term if you know one). That is: if they have the same shape with the same vertex names at the same places.

To do this, there are two steps needed:

- 1. Map all vertex names to an unsigned int.
- 2. Compare the two graphs with that map

Below the class 'named_vertex_invariant' is shown. Its std::map maps the vertex names to an unsigned integer, which is done in the member function 'collect_names'. The purpose of this, is that is is easier to compare integers that std::strings.

Algorithm 88 The named_vertex_invariant functor

```
\#include <map>
#include <boost/graph/adjacency list.hpp>
#include <boost/graph/isomorphism.hpp>
template <class graph>
struct named_vertex_invariant {
  using str to int map = std :: map < std :: string, size t >;
  using result_type = size_t;
  using argument_type
    = typename boost::graph traits<graph>::
        vertex descriptor;
  const graph& m_graph;
  str to int map& m mappings;
  size t operator()(argument type u) const {
      return m mappings.at(boost::get(boost::vertex name,
           m graph, u));
  size_t max() const noexcept { return m_mappings.size();
  void collect names() noexcept {
    for (auto vd : boost::make iterator range(boost::
        vertices (m_graph))) {
      size t next id = m mappings.size();
      auto ins = m mappings.insert(
        { boost::get(boost::vertex name, m graph, vd),
            next id}
      );
      if (ins.second)  {
          std::cout \stackrel{'}{<<} "Mapped" '' << ins.first-> first <<
          "', to " << ins. first -> second <math><< "|n";
    }
  }
};
```

To check for 'label isomorphism', multiple things need to be put in place for 'boost::isomorphism' to work with:

Algorithm 89 Check if two graphs with named vertices are isomorphic

```
#include "named vertex invariant.h"
#include <boost/graph/vf2 sub graph iso.hpp>
#include <boost/graph/graph utility.hpp>
template <typename graph>
bool is named vertices isomorphic (
  const graph &g,
  const graph &h
) noexcept {
  using vd = typename boost::graph traits<graph>::
     vertex descriptor;
  auto vertex_index_map = get(boost::vertex_index, g);
  std::vector<vd> iso(boost::num vertices(g));
  typename named_vertex_invariant<graph>::str_to_int_map
     shared names;
  named_vertex_invariant<graph> inv1{g, shared_names};
  named_vertex_invariant<graph> inv2{h, shared_names};
  inv1.collect names();
  inv2.collect names();
  return boost::isomorphism(g, h,
    boost::isomorphism map (
      make iterator property map (
        iso.begin(),
        vertex index map
    )
    .vertex_invariant1(inv1)
    .vertex_invariant2(inv2)
  );
}
```

This demonstration code creates three path graphs, of which two are 'label isomorphic':

Algorithm 90 Demo of the 'is named vertices isomorphic' function

5.11 Saving an directed/undirected graph with named vertices to a .dot file

If you used the 'create_named_vertices_k2_graph' function (algorithm 65) to produce a K_2 graph with named vertices, you can store these names in multiple ways:

- Using boost::make label writer
- Using a C++11 lambda function

I show both ways, because you may need all of them.

The created .dot file is shown at algorithm 67.

You can use all characters in the vertex without problems (for example: comma's, quotes, whitespace). This will not hold anymore for bundled and custom vertices in later chapters.

The 'save_named_vertices_graph_to_dot' functions below only save the structure of the graph and its vertex names. It ignores other edge and vertex properties.

5.11.1 Using boost::make label writer

The first implemention uses boost::make_label_writer, as shown in algorithm 91:

Algorithm 91 Saving a graph with named vertices to a .dot file

```
#include <fstream>
\# \mathbf{include} < \mathbf{boost} / \operatorname{graph} / \operatorname{graphviz} . hpp>
#include <boost/graph/properties.hpp>
#include "get vertex names.h"
template <typename graph>
void save_named_vertices_graph_to_dot(
  const graph& g,
  const std::string& filename
  noexcept
  std::ofstream f(filename);
  const auto names = get_vertex_names(g);
  boost::write graphviz(
    f,
    g,
    boost::make label writer(&names[0])
  );
}
```

Here, the function boost::write_graphviz is called with a new, third argument. After collecting all names, these are used by boost::make_label_writer to write the names as labels.

5.11.2 Using a C++11 lambda function

An equivalent algorithm is algorithm 92:

Algorithm 92 Saving a graph with named vertices to a .dot file using a lambda expression

```
#include < string>
#include <ostream>
\#include <boost / graph / graphviz . hpp>
#include <boost/graph/properties.hpp>
#include "get vertex names.h"
template <typename graph>
void save named vertices graph to dot using lambda (
  const graph& g,
  const std::string& filename
  noexcept
{
  using vd t = typename graph::vertex descriptor;
  std::ofstream f(filename);
  const auto name_map = get(boost::vertex_name,g);
  boost::write graphviz (
    f,
    g,
    [name map](std::ostream& os, const vd t& vd) {
      const std::string s{name map[vd]};
      if (s.find(',') == std::string::npos) {
        //No\ space, no quotes around string
        os << "[label=" << s << "]";
      }
      else {
        //Has\ space, put\ quotes\ around\ string
        os << "[label=\"" << s << "\"]";
    }
  );
}
```

In this code, a lambda function is used as a third argument.

A lambda function is an on-the-fly function that has these parts:

- the capture brackets '[]', to take variables within the lambda function
- the function argument parentheses '()', to put the function arguments in
- the function body '{}', where to write what it does

First we create a shorthand for the vertex descriptor type, that we'll need to use a lambda function argument (in C++14 you can use auto).

We then create a vertex name map at function scope (in C++17 this can be at lambda function scope) and pass it to the lambda function using its capture section.

The lambda function arguments need to be two: a std::ostream& (a reference to a general out-stream) and a vertex descriptor. In the function body, we get the name of the vertex the same as the 'get_vertex_name' function (algorithm 77) and stream it to the out stream.

5.11.3 Demonstration

Algorithm 93 shows how to use (one of) the 'save_named_vertices_graph_to_dot' function(s):

 ${\bf Algorithm~93~Demonstration~of~the~'s ave_named_vertices_graph_to_dot'} \\ {\bf function}$

```
#include "create_named_vertices_k2_graph.h"
#include "create_named_vertices_markov_chain.h"
#include "save_named_vertices_graph_to_dot.h"

void save_named_vertices_graph_to_dot_demo() noexcept
{
   const auto g = create_named_vertices_k2_graph();
   save_named_vertices_graph_to_dot(
      g, "create_named_vertices_k2_graph.dot"
);

const auto h = create_named_vertices_markov_chain();
   save_named_vertices_graph_to_dot(
      h, "create_named_vertices_markov_chain.dot"
);
}
```

When using the 'save_named_vertices_graph_to_dot' function (algorithm 91), only the structure of the graph and the vertex names are saved: all other properties like edge name are not stored. Algorithm 122 shows how to do so.

5.12 Loading a directed graph with named vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with named vertices is loaded, as shown in algorithm 94:

Algorithm 94 Loading a directed graph with named vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create empty directed named vertices graph.h"
#include "is regular file.h"
boost::adjacency list <
  boost::vecS,
  boost :: vecS,
  boost :: directedS,
  boost::property<
    boost::vertex name t, std::string
load_directed_named_vertices_graph_from_dot(
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g = create_empty_directed_named_vertices_graph();
  boost::dynamic_properties p; //\_do\_ default construct
  p.property("node id", get(boost::vertex name, g));
  p.property("label", get(boost::vertex name, g));
  boost::read graphviz(f,g,p);
  return g;
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Next to this, a boost::dynamic_properties is created with its default constructor, after which we direct the boost::dynamic_properties to find a 'node_id' and 'label' in the vertex name map. From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

Algorithm 95 shows how to use the 'load_directed_graph_from_dot' function:

Algorithm 95 Demonstration of the 'load_directed_named_vertices_graph_from_dot' function

```
#include "create named vertices markov chain.h"
#include "load directed named vertices graph from dot.h"
#include "save_named_vertices_graph_to_dot.h"
#include "get_vertex_names.h"
void load directed named vertices graph from dot demo()
   noexcept
  using boost::num edges;
  using boost::num_vertices;
  const auto g
    = create_named_vertices_markov chain();
  const std::string filename{
    "create named vertices markov chain.dot"
  save named vertices graph to dot(g, filename);
  const auto h
    = load directed named vertices graph from dot (
      filename
    );
  assert(num edges(g) == num edges(h));
  assert(num \ vertices(g) == num \ vertices(h));
  assert (get vertex names (g) == get vertex names (h));
```

This demonstration shows how the Markov chain is created using the 'create_named_vertices_markov_chain' function (algorithm 21), saved and then loaded. The loaded graph is checked to be a directed graph similar to the Markov chain with the same vertex names (using the 'get_vertex_names' function, algorithm 60).

5.13 Loading an undirected graph with named vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with named vertices is loaded, as shown in algorithm 96: Algorithm 96 Loading an undirected graph with named vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create_empty_undirected_named_vertices_graph.h"
#include "is_regular_file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex name t, std::string
load_undirected_named_vertices_graph_from_dot(
  const std::string& dot filename
  assert(is_regular_file(dot_filename));
  std::ifstream f(dot filename.c str());
  auto g = create_empty_undirected_named_vertices_graph()
  boost::dynamic properties p; // do default construct
  p.property("node id", get(boost::vertex name, g));
  p.property("label", get(boost::vertex name, g));
  boost::read_graphviz(f,g,p);
  return g;
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 5.12 describes the rationale of this function.

Algorithm 97 shows how to use the 'load_undirected_graph_from_dot' function:

Algorithm 97 Demonstration of the 'load_undirected_graph_from_dot' function

```
#include "create named vertices k2 graph.h"
#include "load undirected named vertices graph from dot.h
#include "save_named_vertices_graph to dot.h"
#include "get vertex names.h"
void load undirected named vertices graph from dot demo()
    noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create_named_vertices_k2_graph();
  const std::string filename{
    "create named vertices k2 graph.dot"
  save named vertices graph to dot(g, filename);
  const auto h
    = load undirected named vertices graph from dot(
      filename
    );
  assert(num edges(g) == num edges(h));
  assert (num vertices (g) == num vertices (h));
  assert(get\_vertex\_names(g) == get\_vertex\_names(h));
```

This demonstration shows how K_2 with named vertices is created using the 'create_named_vertices_k2_graph' function (algorithm 65), saved and then loaded. The loaded graph is checked to be an undirected graph similar to K_2 , with the same vertex names (using the 'get_vertex_names' function, algorithm 60).

6 Building graphs with named edges and vertices

Up until now, the graphs created have had edges and vertices without any propery. In this chapter, graphs will be created, in which edges vertices can have a name. This name will be of the std::string data type, but other types are possible as well. There are many more built-in properties edges and nodes can have (see the boost/graph/properties.hpp file for these).

In this chapter, we will build the following graphs:

- ullet An empty directed graph that allows for edges and vertices with names: see chapter 6.1
- An empty undirected graph that allows for edges and vertices with names: see chapter 6.2
- Markov chain with named edges and vertices: see chapter 6.5
- K_3 with named edges and vertices: see chapter 6.6

In the process, some basic (sometimes bordering trivial) functions are shown:

- Adding an named edge: see chapter 6.3
- Getting the edges' names: see chapter 6.4

These functions are mostly there for completion and showing which data types are used.

6.1 Creating an empty directed graph with named edges and vertices

Let's create a trivial empty directed graph, in which the both the edges and vertices can have a name:

Algorithm 98 Creating an empty directed graph with named edges and vertices

```
#include < string>
#include <boost/graph/adjacency_list.hpp>
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<boost::vertex name t, std::string>,
  boost::property<boost::edge name t, std::string>
create empty directed named edges and vertices graph()
   noexcept
{
  return boost::adjacency list<
    boost :: vecS,
    boost :: vecS,
    boost :: directedS,
    boost::property<
      boost::vertex_name_t, std::string
    boost::property<
      boost::edge name t, std::string
 > ();
}
```

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)
- is directed (due to the boost::directedS)
- The vertices have one property: they have a name, that is of data type std::string (due to the boost::property< boost::vertex name t,std::string>')
- The edges have one property: they have a name, that is of data type std::string (due to the boost::property< boost::edge name t,std::string>')
- The graph has no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fifth template argument 'boost::property < boost::edge_name_t,std::string>'. This can be read as: "edges have the property 'boost::edge_name_t', that is of data type 'std::string''. Or simply: "edges have a name that is stored as a std::string".

Algorithm 99 shows how to create this graph. Note that all the earlier functions defined in this tutorial keep working as expected.

```
99
                                         if
Algorithm
                        Demonstration
                                                the
                                                         'cre-
ate empty directed named edges and vertices graph' function
#include <cassert>
#include "add named edge.h"
#include "
   create_empty_directed_named_edges_and_vertices_graph.h
#include "get edge names.h"
#include "get vertex names.h"
void
   create empty directed named edges and vertices graph demo
   () noexcept
  using strings = std::vector<std::string>;
  auto g
       create empty directed named edges and vertices graph
  add named edge("Reed", g);
  const strings expected vertex names{"",""};
  const strings vertex_names = get_vertex_names(g);
  assert (expected vertex names = vertex names);
  const strings expected edge names{"Reed"};
  const strings edge names = get edge names(g);
  assert (expected edge names = edge names);
```

6.2 Creating an empty undirected graph with named edges and vertices

Let's create a trivial empty undirected graph, in which the both the edges and vertices can have a name:

Algorithm 100 Creating an empty undirected graph with named edges and vertices

```
#include <string>
#include <boost/graph/adjacency list.hpp>
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<boost::vertex_name_t, std::string>,
  boost::property<boost::edge name t, std::string>
create_empty_undirected_named_edges and vertices graph()
   noexcept
  return boost::adjacency list <
    boost :: vecS,
    boost :: vecS,
    boost::undirectedS,
    boost::property<
      boost::vertex name t, std::string
    boost::property<
      boost::edge name t, std::string
    ();
}
```

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)
- is undirected (due to the boost::undirectedS)
- The vertices have one property: they have a name, that is of data type std::string (due to the boost::property < boost::vertex name t,std::string>')
- The edges have one property: they have a name, that is of data type std::string (due to the boost::property< boost::edge_name_t,std::string>')
- The graph has no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fifth template argument 'boost::property < boost::edge_name_t,std::string>'. This can be read as: "edges have the property 'boost::edge_name_t', that is of data type 'std::string''. Or simply: "edges have a name that is stored as a std::string".

Algorithm 101 shows how to create this graph. Note that all the earlier functions defined in this tutorial keep working as expected.

```
101
Algorithm
                        Demonstration
                                                 the
                                                         'cre-
ate empty undirected named edges and vertices graph' function
#include < cassert >
#include "add named edge.h"
#include "
   create\_empty\_undirected\_named\_edges\_and\_vertices\_graph
#include "get edge names.h"
#include "get vertex names.h"
   create empty undirected named edges and vertices graph demo
   () noexcept
  using strings = std::vector<std::string>;
  auto g
       create empty undirected named edges and vertices graph
  add named edge("Reed", g);
  const strings expected_vertex_names{"",""};
  const strings vertex names = get vertex names(g);
  assert(expected_vertex_names == vertex_names);
  const strings expected edge names{"Reed"};
  const strings edge names = get edge names(g);
  assert (expected edge names == edge names);
}
```

6.3 Adding a named edge

Adding an edge with a name:

Algorithm 102 Add a vertex with a name

```
#include < cassert >
#include < string>
#include <boost/graph/adjacency list.hpp>
template <typename graph>
typename boost::graph traits<graph>::edge descriptor
add named edge (
  const std::string& edge name,
  graph& g
) noexcept
  static_assert(!std::is_const<graph>::value,
    "graph_cannot_be_const"
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer = boost::add_edge(vd_a, vd_b, g);
  assert (aer.second);
  auto edge name map
    = get( //not boost::get
      boost::edge name,g
    );
  put(edge name map, aer.first, edge name);
  return aer.first;
}
```

In this code snippet, the edge descriptor (see chapter 2.12 if you need to refresh your memory) when using 'boost::add_edge' is used as a key to change the edge its name map.

The algorithm 103 shows how to add a named edge to an empty graph. When trying to add named vertices to graph without this property, you will get the error 'formed reference to void' (see chapter 24.1).

Algorithm 103 Demonstration of the 'add named edge' function

6.4 Getting the edges' names

When the edges of a graph have named vertices, one can extract them as such:

Algorithm 104 Get the edges' names

```
#include < string>
#include < vector >
#include <boost/graph/adjacency list.hpp>
#include <boost/graph/properties.hpp>
template <typename graph>
std::vector<std::string> get edge names(const graph& g)
   noexcept
  std::vector<std::string> v;
  v.reserve(boost::num edges(g));
  const auto edge_name_map = get(boost::edge_name,g);
  const auto eip = edges(g); //not boost::edges
  const auto j = eip.second;
  for (auto i = eip.first; i!=j; ++i) {
    v.emplace back(
      get( //not \ boost::get
        edge_name_map,
        * i
    );
  {\bf return}\ v\,;
```

The names of the edges are obtained from a boost::property_map and then put into a std::vector. The algorithm 105 shows how to apply this function.

The order of the edge names may be different after saving and loading.

Would you dare to try to get the edges' names from a graph without vertices with names, you will get the error 'formed reference to void' (see chapter 24.1).

Algorithm 105 Demonstration of the 'get edge names' function

```
#include <cassert>
#include "add named edge.h"
#include "
   create empty undirected named edges and vertices graph
   . h"
#include "get edge names.h"
void get edge names demo() noexcept
  auto g
       create\_empty\_undirected\_named\_edges\_and\_vertices\_graph
  const std::string edge_name_1{"Eugene"};
  const std::string edge name 2{"Another_Eugene"};
  add_named_edge(edge_name_1, g);
  add named edge (edge name 2, g);
  const std::vector<std::string> expected names{
    edge_name_1, edge_name_2
  const std::vector<std::string> edge names{
    get_edge_names(g)
  assert (expected_names == edge_names);
```

6.5 Creating Markov chain with named edges and vertices

6.5.1 Graph

We build this graph:

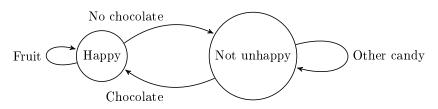


Figure 22: A two-state Markov chain where the edges and vertices have texts

6.5.2 Function to create such a graph

Here is the code:

Algorithm 106 Creating the two-state Markov chain as depicted in figure 22

```
#include < string>
#include "
   create empty directed named edges and vertices graph.h
boost::adjacency list <
  boost::vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<boost::vertex name t, std::string>,
  boost::property<boost::edge name t, std::string>
create named edges and vertices markov chain () noexcept
  auto g
        create empty directed named edges and vertices graph
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  {f const\ auto}\ {f aer}\ bb\ =\ boost:: add\_edge(vd\_b,\ vd\_b,\ g);
  assert (aer bb.second);
  auto vertex name map = get ( //not \ boost :: get
    boost::vertex name, g
  vertex_name_map[vd a] = "Happy";
  vertex name map[vd b] = "Not_unhappy";
  {f auto}\ {f edge\_name\_map}\ =\ {f get}\ (\ \ // {\it not}\ \ {\it boost}:: {\it get}
    boost::edge name, g
  );
  edge name map[aer aa.first] = "Fruit";
  edge name map[aer ab.first] = "No_chocolate";
  edge name map[aer ba.first] = "Chocolate";
  edge name map[aer bb.first] = "Other_candy";
  return g;
}
```

6.5.3 Creating such a graph

Here is the demo:

Algorithm 107 Demo of the 'create_named_edges_and_vertices_markov_chain' function (algorithm 106)

```
#include <cassert>
#include <iostream>
#include "create_named_edges_and_vertices_markov_chain.h"
#include "get edge names.h"
#include "get vertex names.h"
void create named edges and vertices markov chain demo()
   noexcept
  using strings = std::vector<std::string>;
  const auto g
    =\ create\_named\_edges\_and\_vertices\_markov\_chain\,()\;;
  const strings expected_vertex_names{
    "Happy", "Not_unhappy"
  const strings vertex names {
    get vertex names(g)
  assert (expected vertex names == vertex names);
  const strings expected edge names{
    " Fruit " , "No_{\circ} chocolate " , " Chocolate " , " Other _{\circ} candy "
  const strings edge_names{get_edge_names(g)};
  assert (expected edge names = edge names);
}
```

6.5.4 The .dot file produced

Algorithm 108 .dot file created from the 'create_named_edges_and_vertices_markov_chain' function (algorithm 106), converted from graph to .dot file using algorithm 48

```
digraph G {
    O[label=Happy];
    1[label="Not unhappy"];
    O->0 [label="Fruit"];
    O->1 [label="No chocolate"];
    1->0 [label="Chocolate"];
    1->1 [label="Other candy"];
}
```

6.5.5 The .svg file produced

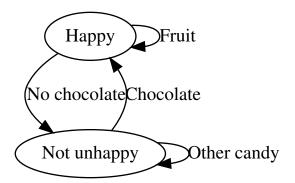


Figure 23: .svg file created from the 'create_named_edges_and_vertices_markov_chain' function (algorithm 106) its .dot file, converted from .dot file to .svg using algorithm 279

6.6 Creating K_3 with named edges and vertices

6.6.1 Graph

We extend the graph K_2 with named vertices of chapter 4.6 by adding names to the edges, as depicted in figure 24:

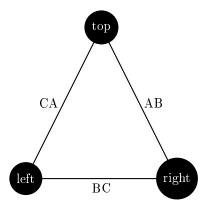


Figure 24: K_3 : a fully connected graph with three named edges and vertices

6.6.2 Function to create such a graph

To create K_3 , the following code can be used:

Algorithm 109 Creating K_3 as depicted in figure 24

```
#include < string>
#include <boost/graph/adjacency list.hpp>
#include "
   create empty undirected named edges and vertices graph
    . h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property < boost::vertex name t, std::string >,
  boost::property<boost::edge name t,std::string>
create_named_edges_and_vertices_k3_graph() noexcept
  auto g
        create empty undirected named edges and vertices graph
  const auto vd a = boost::add vertex(g);
  \mathbf{const} \ \mathbf{auto} \ \mathrm{vd\_b} = \ \mathrm{boost} :: \mathrm{add\_vertex} \, (\, \mathrm{g}) \, ;
  const auto vd c = boost::add vertex(g);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer bc = boost::add edge(vd b, vd c, g);
  assert (aer bc.second);
  const auto aer ca = boost::add edge(vd c, vd a, g);
  assert (aer ca.second);
  auto vertex name map = get (boost::vertex name,g);
  vertex name map[vd a] = "top";
  vertex_name_map[vd_b] = "right";
  vertex name map[vd c] = "left";
  auto edge name map = get (boost::edge name,g);
  edge_name_map[aer_ab.first] = "AB";
  edge_name_map[aer_bc.first] = "BC";
  edge name map[aer ca.first] = "CA";
  return g;
```

Most of the code is a repeat of algorithm 65. In the end, the edge names are

obtained as a boost::property map and set.

6.6.3 Creating such a graph

Algorithm 110 shows how to create the graph and measure its edge and vertex names.

```
Algorithm 110 Demonstration of the 'create_named_edges_and_vertices_k3' function

#include <cassert>
#include <iostream>
#include "create_named_edges_and_vertices_k3_graph.h"

#include "get_edge_names.h"
```

```
#include "get_vertex_names.h"
void create named edges and vertices k3 graph demo()
   noexcept
{
  using strings = std::vector<std::string>;
  const auto g
    = create named edges and vertices k3 graph();
  const strings expected vertex names {
    "top", "right", "left"
  };
  const strings vertex names{
    get_vertex_names(g)
  };
  assert (expected vertex names = vertex names);
  const strings expected edge names {
    "AB", "BC", "CA"
  };
  const strings edge names{get edge names(g)};
```

assert (expected_edge_names == edge_names);

}

6.6.4 The .dot file produced

Algorithm 111 .dot file created from the 'create_named_edges_and_vertices_k3_graph' function (algorithm 109), converted from graph to .dot file using algorithm 48

```
graph G {
0[label=top];
1[label=right];
2[label=left];
0--1 [label="AB"];
1--2 [label="BC"];
2--0 [label="CA"];
}
```

6.6.5 The .svg file produced

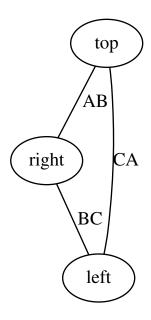


Figure 25: .svg file created from the 'create_named_edges_and_vertices_k3_graph' function (algorithm 109) its .dot file, converted from .dot file to .svg using algorithm 279

7 Working on graphs with named edges and vertices

Working with named edges...

- Check if there exists an edge with a certain name: chapter 7.1
- Find a (named) edge by its name: chapter 7.2
- Get a (named) edge its name from its edge descriptor: chapter 7.3
- Set a (named) edge its name using its edge descriptor: chapter 7.4
- Remove a named edge: chapter 7.5
- Saving a graph with named edges and vertices to a .dot file: chapter 7.6
- Loading a directed graph with named edges and vertices from a .dot file: chapter 7.7
- \bullet Loading an undirected graph with named edges and vertices from a .dot file: chapter 7.8

Especially chapter 7.2 with the 'find_first_edge_by_name' algorithm shows how to obtain an edge descriptor, which is used in later algorithms.

7.1 Check if there exists an edge with a certain name

Before modifying our edges, let's first determine if we can find an edge by its name in a graph. After obtaing a name map, we obtain the edge iterators, dereference these to obtain the edge descriptors and then compare each edge its name with the one desired.

Algorithm 112 Find if there is an edge with a certain name

```
#include < string>
#include <boost/graph/properties.hpp>
template <typename graph>
bool has_edge_with_name(
  const std::string& name,
  const graph& g
) noexcept
  const auto edge name map
    = get( //not boost::get
      boost::edge_name,
      g
    );
  const auto eip
    = \operatorname{edges}( // not \ boost :: edges
    g
  );
  const auto j = eip.second;
  for (auto i = eip.first; i!=j; ++i) {
    if (get(edge name map, *i) = name) {
      return true;
    }
  return false;
```

This function can be demonstrated as in algorithm 113, where a certain name cannot be found in an empty graph. After adding the desired name, it is found.

Algorithm 113 Demonstration of the 'has edge with name' function

Note that this function only finds if there is at least one edge with that name: it does not tell how many edges with that name exist in the graph.

7.2 Find an edge by its name

Where STL functions work with iterators, here we obtain an edge descriptor (see chapter 2.12) to obtain a handle to the desired edge. Algorithm 114 shows how to obtain an edge descriptor to the first (name) edge found with a specific name.

Algorithm 114 Find the first edge by its name

```
#include < string>
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "has edge with name.h"
template <typename graph>
typename boost::graph traits<graph>::edge descriptor
find_first_edge_with_name(
  const std::string& name,
  const graph& g
 noexcept
  assert (has edge with name (name, g));
  const auto edge name map
    = get( //not boost::get
      boost::edge_name, g
    );
  const auto eip
    = \operatorname{edges}(g); //not boost:: edges
  const auto j = eip.second;
  for (auto i = eip.first; i!=j; ++i) {
    const std::string s{
       get (edge name map, *i)
    \acute{\mathbf{i}}\acute{\mathbf{f}} (s == name) { \mathbf{return} *i; }
  assert (!"Should_not_get_here");
  throw; // Will crash the program
```

With the edge descriptor obtained, one can read and modify the graph. Algorithm 115 shows some examples of how to do so.

Algorithm 115 Demonstration of the 'find first edge by name' function

7.3 Get a (named) edge its name from its edge descriptor

This may seem a trivial paragraph, as chapter 6.4 describes the 'get_edge_names' algorithm, in which we get all edges' names. But it does not allow to first find an edge of interest and subsequently getting only that one its name.

To obtain the name from an edgedescriptor, one needs to pull out the name map and then look up the edge of interest.

Algorithm 116 Get an edge its name from its edge descriptor

```
#include < string>
#include <boost/graph/graph traits.hpp>
\#\mathbf{include} < \mathbf{boost} / \operatorname{graph} / \operatorname{properties} . hpp>
\mathbf{template} \ <\! \mathbf{typename} \ \mathrm{grap} \, h\! >\!
std::string get edge name(
  const typename boost::graph traits<graph>::
       edge descriptor& ed,
  const graph& g
  noexcept
  const auto edge name map
     = get( //not boost::get
        boost::edge name,
        g
     );
  return edge_name_map[ed];
}
```

To use 'get_edge_name', one first needs to obtain an edge descriptor. Algorithm 117 shows a simple example.

Algorithm 117 Demonstration if the 'get edge name' function

7.4 Set a (named) edge its name from its edge descriptor

If you know how to get the name from an edge descriptor, setting it is just as easy, as shown in algorithm 118.

Algorithm 118 Set an edge its name from its edge descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>

template <typename graph>
void set_edge_name(
    const std::string& any_edge_name,
    const typename boost::graph_traits<graph>::
        edge_descriptor& vd,
    graph& g
) noexcept
{
    static_assert(!std::is_const<graph>::value,
        "graph_cannot_be_const"
);

    auto edge_name_map = get(boost::edge_name,g);
    edge_name_map[vd] = any_edge_name;
}
```

To use 'set_edge_name', one first needs to obtain an edge descriptor. Algorithm 119 shows a simple example.

Algorithm 119 Demonstration if the 'set edge name' function

```
#include <cassert>
#include "add named edge.h"
#include "
   create empty undirected named edges and vertices graph
   . h"
#include "find first edge with name.h"
#include "get_edge_name.h"
#include "set edge name.h"
void set edge name demo() noexcept
  auto g =
     create empty undirected named edges and vertices graph
  const std::string old name{"Dex"};
  add named edge(old name, g);
  const auto vd = find first edge with name(old name,g);
  assert(get\_edge\_name(vd,g) = old\_name);
  const std::string new_name{"Diggy"};
  set - edge\_name(new\_name, - vd, - g);
  assert(get edge name(vd,g) = new name);
```

7.5 Removing the first edge with a certain name

An edge descriptor can be used to remove an edge from a graph.

Removing a named edge goes as follows: use the name of the edge to get a first edge descriptor, then call 'boost::remove_edge', shown in algorithm 84:

Algorithm 120 Remove the first edge with a certain name

```
#include <boost/graph/adjacency list.hpp>
#include "find_first_edge_with_name.h"
#include "has edge with name.h"
template <typename graph>
void remove first edge with name (
  const std::string& name,
  graph& g
 noexcept
  static assert (!std::is const<graph>::value,
    "graph_cannot_be_const"
  );
  assert (has edge with name (name, g));
  const auto vd
    = find_first_edge_with_name(name,g);
  boost::remove edge(vd,g);
}
```

Algorithm 121 shows the removal of the first named edge found.

Algorithm 121 Demonstration of the 'remove_first_edge_with_name' function

```
#include <cassert>
#include "create_named_edges_and_vertices_k3_graph.h"
#include "remove_first_edge_with_name.h"

void remove_first_edge_with_name_demo() noexcept
{
    auto g = create_named_edges_and_vertices_k3_graph();
    assert(boost::num_edges(g) == 3);
    assert(boost::num_vertices(g) == 3);
    remove_first_edge_with_name("AB",g);
    assert(boost::num_edges(g) == 2);
    assert(boost::num_vertices(g) == 3);
}
```

7.6 Saving an undirected graph with named edges and vertices as a .dot

If you used the create_named_edges_and_vertices_k3_graph function (algorithm 109) to produce a K_3 graph with named edges and vertices, you can store these names additionally with algorithm 122:

Algorithm 122 Saving an undirected graph with named edges and vertices to a .dot file

```
#include < string>
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include <boost/graph/properties.hpp>
#include "get edge names.h"
#include "get vertex names.h"
template <typename graph>
void save_named_edges_and_vertices_graph_to_dot(
  const graph& g,
  const std::string& filename
  using my edge descriptor = typename graph::
     edge_descriptor;
  std::ofstream f(filename);
  const auto vertex names = get vertex names(g);
  const auto edge name map = boost::get(boost::edge name,
  boost::write_graphviz(
    f,
    boost::make label writer(&vertex names[0]),
    [edge name map](std::ostream& out, const
       my_edge_descriptor& e) {
      out << "[label=\"" << edge name map[e] << "\"]";
  );
}
```

If you created a graph with edges more complex than just a name, you will still just write these to the .dot file. Chapter 13.6 shows how to write custom vertices to a .dot file.

So, the 'save_named_edges_and_vertices_graph_to_dot' function (algorithm 48) saves only the structure of the graph and its edge and vertex names.

7.7 Loading a directed graph with named edges and vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with named edges and vertices is loaded, as shown in algorithm 123:

Algorithm 123 Loading a directed graph with named edges and vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create_empty_directed_named_edges_and_vertices_graph.h
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex name t, std::string
  >,
  boost::property<
    boost::edge name t, std::string
load directed named edges and vertices graph from dot (
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g =
     create empty directed named edges and vertices graph
     ();
  boost::dynamic_properties p; //_do_ default construct
  p.property("node_id", get(boost::vertex_name, g));
  p.property("label", get(boost::vertex_name, g));
  {\tt p.property("edge\_id", get(boost::edge\_name, g));}\\
  p.property("label", get(boost::edge_name, g));
  boost::read graphviz(f,g,p);
  return g;
}
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Next to this, a boost::dynamic_properties is created with its default constructor, after which we direct the boost::dynamic_properties to find a 'node_id' and 'label' in the vertex name map, 'edge_id' and 'label to the edge name map. From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

Algorithm 124 shows how to use the 'load_directed_graph_from_dot' function:

Algorithm 124 Demonstration of the 'load_directed_named_edges_and_vertices_graph_from_dot'

```
#include "create named edges and vertices markov chain.h"
#include "
   load directed named edges and vertices graph from dot.
#include "save named edges and vertices graph to dot.h"
\#include "get vertex names.h"
void
   load directed named edges and vertices graph from dot demo
   () noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create named edges and vertices markov chain();
  const std::string filename{
    "create named edges and vertices markov chain.dot"
  save named edges and vertices graph to dot(g, filename)
  const auto h
       load directed named edges and vertices graph from dot
      filename
     );
  assert(num edges(g) == num edges(h));
  assert(num \ vertices(g) == num \ vertices(h));
  assert(get vertex names(g) = get vertex names(h));
```

This demonstration shows how the Markov chain is created using the 'create_named_edges_and_vertices_markov_chain' function (algorithm 106), saved and then loaded. The loaded graph is checked to be a directed graph similar to the Markov chain with the same edge and vertex names (using the 'get_edge_names' function, algorithm 104, and the 'get_vertex_names' function, algorithm 60).

7.8 Loading an undirected graph with named edges and vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with named edges and vertices is loaded, as shown in algorithm 125:

Algorithm 125 Loading an undirected graph with named edges and vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create empty undirected named edges and vertices graph
    . h"
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex name t, std::string
  >,
  boost::property<
    boost::edge name t, std::string
load undirected named edges and vertices graph from dot (
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g =
     create empty undirected named edges and vertices graph
  boost::dynamic_properties p; //_do_ default construct
  p. property("node id", get(boost::vertex name, g));
  p.property("label", get(boost::vertex name, g));
  p. property("edge_id", get(boost::edge_name, g));
p. property("label", get(boost::edge_name, g));
  boost::read graphviz(f,g,p);
  return g;
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 7.7 describes the rationale of this function.

Algorithm 126 shows how to use the 'load_undirected_graph_from_dot' function:

Algorithm 126 Demonstration of the 'load_undirected_named_edges_and_vertices_graph_from_dot' function

```
#include "create named edges and vertices k3 graph.h"
#include "
   load undirected named edges and vertices graph from dot
   . h"
\#include "save_named_edges_and_vertices_graph_to_dot.h"
#include "get_vertex names.h"
void
   load undirected named edges and vertices graph from dot demo
   () noexcept
{
  using boost::num edges;
  using boost::num_vertices;
  const auto g
    = create named edges and vertices k3 graph();
  const std::string filename{
    "create named edges and vertices k3 graph.dot"
  };
  save named edges and vertices graph to dot(g, filename)
  const auto h
       load undirected named edges and vertices graph from dot
      filename
    );
  assert(num\_edges(g) == num\_edges(h));
  assert (num_vertices(g) == num_vertices(h));
  assert(get vertex names(g) = get vertex names(h));
```

This demonstration shows how K_3 with named edges and vertices is created using the 'create_named_edges_and_vertices_k3_graph' function (algorithm 109), saved and then loaded. The loaded graph is checked to be an undirected graph similar to K_3 , with the same edge and vertex names (using the 'get_edge_names' function, algorithm 104, and the 'get_vertex_names'

function, algorithm 60).

8 Building graphs with bundled vertices

Up until now, the graphs created have had edges and vertices with the built-in name propery. In this chapter, graphs will be created, in which the vertices can have a bundled 'my_bundled_vertex' type⁸. The following graphs will be created:

- An empty directed graph that allows for bundled vertices: see chapter 128
- An empty undirected graph that allows for bundled vertices: see chapter 8.2
- A two-state Markov chain with bundled vertices: see chapter 8.6
- K_2 with bundled vertices: see chapter 8.7

In the process, some basic (sometimes bordering trivial) functions are shown:

- Create the vertex class, called 'my_bundled_vertex': see chapter 8.1
- Adding a 'my bundled vertex': see chapter 8.4
- Getting the vertices 'my bundled vertex'-es: see chapter 8.5

These functions are mostly there for completion and showing which data types are used.

8.1 Creating the bundled vertex class

Before creating an empty graph with bundled vertices, that bundled vertex class must be created. In this tutorial, it is called 'my_bundled_vertex'. 'my_bundled_vertex' is a class that is nonsensical, but it can be replaced by any other class type.

Here I will show the header file of 'my_bundled_vertex', as the implementation of it is not important:

⁸I do not intend to be original in naming my data types

Algorithm 127 Declaration of my bundled vertex

```
#include < string>
#include <iosfwd>
#include <boost/property map/dynamic property map.hpp>
struct my bundled vertex
  explicit my bundled vertex (
    const std::string& name = "",
    const std::string& description = "",
    const double x = 0.0,
    const double y = 0.0
  ) noexcept;
  std::string m_name;
  std::string m description;
  double m x;
  double m y;
};
bool operator == (const my bundled vertex& lhs, const
   my_bundled_vertex& rhs) noexcept;
bool operator! = (const my_bundled_vertex& lhs, const
   my bundled vertex& rhs) noexcept;
```

'my bundled vertex' is a class that has multiple properties:

- It has four public member variables: the double 'm_x' ('m_' stands for member), the double 'm_y', the std::string m_name and the std::string m_description. These variables must be public
- It has a default constructor
- It is copyable
- It is comparable for equality (it has operator==), which is needed for searching

'my_bundled_vertex' does not have to have the stream operators defined for file I/O, as this goes via the public member variables.

8.2 Create the empty directed graph with bundled vertices

Algorithm 128 Creating an empty directed graph with bundled vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_vertex.h"

boost:: adjacency_list <
   boost:: vecS,
   boost:: vecS,
   boost:: directedS,
   my_bundled_vertex
>
create_empty_directed_bundled_vertices_graph() noexcept
{
   return boost:: adjacency_list <
      boost:: vecS,
      boost:: vecS,
      boost:: vecS,
      boost:: directedS,
      my_bundled_vertex
   >();
}
```

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)
- is directed (due to the boost::directedS)
- The vertices have one property: they have a bundled type, that is of data type 'my bundled vertex'
- The edges and graph have no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fourth template argument 'my_bundled_vertex'. This can be read as: "vertices have the bundled property 'my_bundled_vertex". Or simply: "vertices have a bundled type called my_bundled_vertex".

8.3 Create the empty undirected graph with bundled vertices

Algorithm 129 Creating an empty undirected graph with bundled vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_vertex.h"

boost:: adjacency_list <
   boost:: vecS ,
   boost:: vecS ,
   boost:: undirectedS ,
   my_bundled_vertex
>
create_empty_undirected_bundled_vertices_graph() noexcept
{
   return boost:: adjacency_list <
      boost:: vecS ,
      boost:: vecS ,
      boost:: vecS ,
      boost:: undirectedS ,
      my_bundled_vertex
>();
}
```

This code is very similar to the code described in chapter 8.2, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS).

8.4 Add a bundled vertex

Adding a bundled vertex is very similar to adding a named vertex (chapter 4.3).

Algorithm 130 Add a bundled vertex

When having added a new (abstract) vertex to the graph, the vertex descriptor is used to set the 'my bundled vertex' in the graph.

8.5 Getting the bundled vertices' my vertexes⁹

When the vertices of a graph have any bundled 'my_bundled_vertex', one can extract these as such:

 $^{^9{\}rm the\ name\ 'my_vertexes'}$ is chosen to indicate this function returns a container of my_vertex

Algorithm 131 Get the bundled vertices' my vertexes

```
#include < vector>
#include <boost/graph/adjacency_list.hpp>
\#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "my bundled vertex.h"
template <typename graph>
std::vector < my\_bundled\_vertex >
   get bundled vertex my vertexes (
  const graph& g
 noexcept
  std::vector<my_bundled_vertex> v;
  v.reserve(boost::num vertices(g));
  const auto vip
    = vertices (g); //not boost::vertices
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i) {
    v.emplace back(g[*i]);
  return v;
```

The 'my_bundled_vertex' bundled in each vertex is obtained from a vertex descriptor and then put into a std::vector.

The order of the 'my_bundled_vertex' objects may be different after saving and loading.

When trying to get the vertices' my_bundled_vertex from a graph without these, you will get the error 'formed reference to void' (see chapter 24.1).

8.6 Creating a two-state Markov chain with bundled vertices

8.6.1 Graph

Figure 26 shows the graph that will be reproduced:

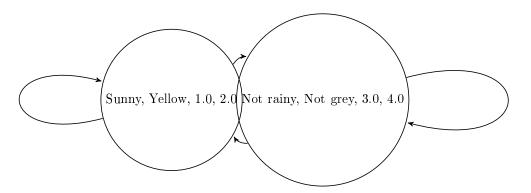


Figure 26: A two-state Markov chain where the vertices have bundled properies and the edges have no properties. The vertices' properties are nonsensical

8.6.2 Function to create such a graph

Here is the code creating a two-state Markov chain with bundled vertices:

Algorithm 132 Creating the two-state Markov chain as depicted in figure 26

```
#include <cassert>
#include "create_empty_directed_bundled_vertices_graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  my bundled vertex
create bundled vertices markov chain () noexcept
  auto g
    = create_empty_directed_bundled_vertices_graph();
  const auto vd_a = boost::add_vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer_aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer_ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer bb = boost::add edge(vd b, vd b, g);
  assert (aer bb.second);
  g[vd_a] = my\_bundled\_vertex("Sunny",
    "Yellow", 1.0, 2.0
  g[vd_b] = my_bundled_vertex("Not_rainy",
    "Not_grey", 3.0, 4.0
  );
  return g;
```

8.6.3 Creating such a graph

Here is the demo:

Algorithm 133 Demo of the 'create_bundled_vertices_markov_chain' function (algorithm 132)

```
#include <cassert>
#include "create bundled vertices markov chain.h"
#include "get bundled vertex my vertexes.h"
#include "my bundled vertex.h"
void create_bundled_vertices_markov_chain_demo() noexcept
  const auto g
    = create bundled vertices markov chain();
  const std::vector<my bundled vertex>
     expected my vertexes {
    my_bundled_vertex("Sunny","Yellow",1.0,2.0),
    \label{local_normalisation} \verb|my_bundled_vertex("Not\_rainy","Not\_grey",3.0,4.0)|
  };
  const std::vector<my bundled vertex> vertex my vertexes
    get_bundled_vertex_my_vertexes(g)
  };
  assert (expected my vertexes == vertex my vertexes);
}
```

8.6.4 The .dot file produced

Algorithm 134 .dot file created from the 'create_bundled_vertices_markov_chain' function (algorithm 132), converted from graph to .dot file using algorithm 147

digraph G {

```
digraph G {
0[label="Sunny",comment="Yellow",width=1,height=2];
1[label="Not$$$SPACE$$$rainy",comment="Not$$$SPACE$$$grey",width=3,height=4];
0->0;
0->1;
1->0;
1->1;
```

8.6.5 The .svg file produced

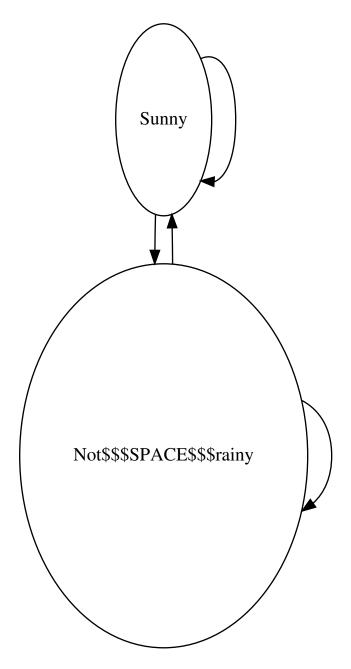


Figure 27: .svg file created from the 'create_bundled_vertices_markov_chain' function (algorithm 132) its .dot file, converted from .dot file to .svg using algorithm 279

8.7 Creating K_2 with bundled vertices

8.7.1 Graph

We reproduce the K_2 with named vertices of chapter 4.6 , but with our bundled vertices intead, as show in figure 28:



Figure 28: K_2 : a fully connected graph with two bundled vertices

8.7.2 Function to create such a graph

Algorithm 135 Creating K_2 as depicted in figure 18

```
#include "create empty undirected bundled vertices graph.
   h"
boost::adjacency_list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  my bundled vertex
create_bundled_vertices_k2_graph() noexcept
  auto g = create_empty_undirected_bundled_vertices_graph
      ();
  const auto vd_a = boost::add_vertex(g);
  const auto vd b = boost :: add vertex(g);
  const auto aer = boost::add_edge(vd_a, vd_b, g);
  assert (aer.second);
  g[vd \ a] = my \ bundled \ vertex(
    "Me", "Myself", 1.0, 2.0
  g[vd_b] = my_bundled_vertex(
    "My_computer", "Not_me", 3.0, 4.0
  );
  return g;
```

Most of the code is a slight modification of the 'create_named_vertices_k2_graph' function (algorithm 65). In the end, (references to) the my_bundled_vertices are obtained and set with two bundled my_bundled_vertex objects.

8.7.3 Creating such a graph

Demo:

Algorithm 136 Demo of the 'create_bundled_vertices_k2_graph' function (algorithm 135)

```
#include <cassert>
#include "create_bundled_vertices_k2_graph.h"
#include "has_bundled_vertex_with_my_vertex.h"

void create_bundled_vertices_k2_graph_demo() noexcept
{
    const auto g = create_bundled_vertices_k2_graph();
    assert(boost::num_edges(g) == 1);
    assert(boost::num_vertices(g) == 2);
    assert(has_bundled_vertex_with_my_vertex(
        my_bundled_vertex("Me","Myself",1.0,2.0), g)
    );
    assert(has_bundled_vertex_with_my_vertex(
        my_bundled_vertex("My_computer","Not_me",3.0,4.0), g)
    );
}
```

8.7.4 The .dot file produced

Algorithm 137 .dot file created from the 'create_bundled_vertices_k2_graph' function (algorithm 135), converted from graph to .dot file using algorithm 48

8.7.5 The .svg file produced

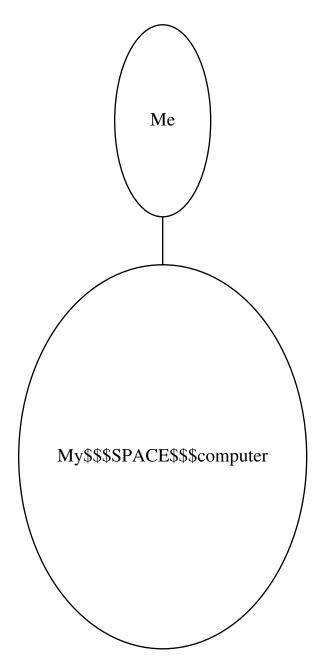


Figure 29: .svg file created from the 'create_bundled_vertices_k2_graph' function (algorithm 135) its .dot file, converted from .dot file to .svg using algorithm 279

9 Working on graphs with bundled vertices

When using graphs with bundled vertices, their state gives a way to find a vertex and working with it. This chapter shows some basic operations on graphs with bundled vertices.

- Check if there exists a vertex with a certain 'my_bundled_vertex': chapter 9.1
- Find a vertex with a certain 'my bundled vertex': chapter 9.2
- Get a vertex its 'my_bundled_vertex' from its vertex descriptor: chapter 9.3
- Set a vertex its 'my_bundled_vertex' using its vertex descriptor: chapter 9.4
- Setting all vertices their 'my_bundled_vertex'-es: chapter 9.5
- Storing an directed/undirected graph with bundled vertices as a .dot file: chapter 9.6
- Loading a directed graph with bundled vertices from a .dot file: chapter 9.7
- Loading an undirected directed graph with bundled vertices from a .dot file: chapter 9.8

9.1 Has a bundled vertex with a my bundled vertex

Before modifying our vertices, let's first determine if we can find a vertex by its bundled type ('my_bundled_vertex') in a graph. After obtain the vertex iterators, we can dereference each these to obtain the vertex descriptors and then compare each vertex its 'my bundled vertex' with the one desired.

Algorithm 138 Find if there is vertex with a certain my bundled vertex

This function can be demonstrated as in algorithm 139, where a certain my_bundled_vertex cannot be found in an empty graph. After adding the desired my_bundled_vertex, it is found.

Algorithm 139 Demonstration of the 'has_bundled_vertex_with_my_vertex' function

```
#include <cassert>
#include <iostream>
#include "add bundled vertex.h"
#include "create empty undirected bundled vertices graph.
   h "
#include "has bundled vertex with my vertex.h"
#include "my_bundled_vertex.h"
void has bundled vertex with my vertex demo() noexcept
  auto g = create empty undirected bundled vertices graph
     ();
  assert (! has_bundled_vertex_with_my_vertex(
     my bundled vertex("Felix"),g));
  add bundled vertex(my bundled vertex("Felix"),g);
  assert (has bundled vertex with my vertex (
     my bundled vertex("Felix"),g));
}
```

Note that this function only finds if there is at least one bundled vertex with that my_bundled_vertex: it does not tell how many bundled vertices with that my_bundled_vertex exist in the graph.

9.2 Find a bundled vertex with a certain my bundled vertex

Where STL functions work with iterators, here we obtain a vertex descriptor (see chapter 2.6) to obtain a handle to the desired vertex. Algorithm 140 shows how to obtain a vertex descriptor to the first vertex found with a specific 'my bundled vertex' value.

Algorithm 140 Find the first vertex with a certain my bundled vertex

```
#include <cassert>
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "has bundled vertex with my vertex.h"
#include "my bundled vertex.h"
template <typename graph>
typename boost::graph\_traits < graph >::vertex\_descriptor
find_first_bundled_vertex_with_my_vertex(
  const my bundled vertex& v,
  const graph& g
 noexcept
  assert (has bundled vertex with my vertex (v, g));
  const auto vip
    = vertices(g); //not boost::vertices
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i) {
    if (g[*i] == v) { return *i; }
  assert (!"Should_not_get_here");
  throw; // Will crash the program
```

With the vertex descriptor obtained, one can read and modify the vertex and the edges surrounding it. Algorithm 141 shows some examples of how to do so.

Algorithm 141 Demonstration of the 'find_first_bundled_vertex_with_my_vertex' function

```
#include <cassert>
#include "create_bundled_vertices_k2_graph.h"
#include "find_first_bundled_vertex_with_my_vertex.h"

void find_first_bundled_vertex_with_my_vertex_demo()
    noexcept
{
    const auto g = create_bundled_vertices_k2_graph();
    const auto vd =
        find_first_bundled_vertex_with_my_vertex(
        my_bundled_vertex("Me","Myself",1.0,2.0);
        g
    );
    assert(out_degree(vd,g) == 1); //not_boost::out_degree
    assert(in_degree(vd,g) == 1); //not_boost::in_degree
}
```

9.3 Get a bundled vertex its 'my bundled vertex'

To obtain the 'my_bundled_vertex' from a vertex descriptor is simple:

Algorithm 142 Get a bundled vertex its my vertex from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "my_bundled_vertex.h"

template <typename graph>
my_bundled_vertex get_bundled_vertex_my_vertex(
    const typename boost::graph_traits<graph>::
        vertex_descriptor& vd,
    const graph& g
) noexcept
{
    return g[vd];
}
```

One can just use the graph as a property map and let it be looked-up.

To use 'get_bundled_vertex_my_vertex', one first needs to obtain a vertex descriptor. Algorithm 143 shows a simple example.

Algorithm 143 Demonstration if the 'get_bundled_vertex_my_vertex' function

9.4 Set a bundled vertex its my_vertex

If you know how to get the 'my_bundled_vertex' from a vertex descriptor, setting it is just as easy, as shown in algorithm 144.

Algorithm 144 Set a bundled vertex its my vertex from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "my_bundled_vertex.h"

template <typename graph>
void set_bundled_vertex_my_vertex(
    const my_bundled_vertex& v,
    const typename boost::graph_traits<graph>::
        vertex_descriptor& vd,
    graph& g
) noexcept
{
    static_assert(!std::is_const<graph>::value, "graph_cannot_be_const");

    g[vd] = v;
}
```

To use 'set_bundled_vertex_my_vertex', one first needs to obtain a vertex descriptor. Algorithm 145 shows a simple example.

Algorithm 145 Demonstration if the 'set_bundled_vertex_my_vertex' function

```
#include < cassert >
#include "add bundled vertex.h"
#include "create empty undirected bundled vertices graph.
#include "find_first_bundled_vertex_with_my_vertex.h"
#include "get bundled vertex my vertex.h"
#include "set bundled vertex my vertex.h"
void set_bundled_vertex_my_vertex_demo() noexcept
  auto g = create empty undirected bundled vertices graph
     ();
  const my bundled vertex old name{"Dex"};
  add bundled vertex (old name, g);
  {f const} auto {
m vd} =
     find_first_bundled_vertex_with_my_vertex(old_name,g)
  assert (get bundled vertex my vertex(vd,g) = old name);
  const my bundled vertex new name{"Diggy"};
  set_bundled_vertex_my_vertex(new_name, vd, g);
  assert (get_bundled_vertex_my_vertex(vd,g) == new_name);
}
```

9.5 Setting all bundled vertices' my vertex objects

When the vertices of a graph are 'my_bundled_vertex' objects, one can set these as such:

Algorithm 146 Setting the bundled vertices' 'my bundled vertex'-es

```
#include < string>
#include < vector >
#include <boost/graph/graph traits.hpp>
#include <boost/graph/properties.hpp>
#include "my bundled vertex.h"
template <typename graph>
void set_bundled_vertex_my_vertexes(
  graph&g,
  const std::vector<my bundled vertex>& my vertexes
 noexcept
  static\_assert (!std::is\_const < graph > :: value,
    "graph_cannot_be_const"
  );
  auto my vertexes begin = std::begin(my vertexes);
  const auto my vertexes end = std::end(my vertexes);
  const auto vip = vertices(g); //not boost::vertices
  const auto j = vip.second;
  for (
    auto i = vip.first;
    i!=j; ++i,
   ++my_vertexes_begin
    assert (my vertexes begin != my vertexes end);
    g[*i] = *my \text{ vertexes begin};
}
```

9.6 Storing a graph with bundled vertices as a .dot

If you used the 'create_bundled_vertices_k2_graph' function (algorithm 135) to produce a K_2 graph with vertices associated with 'my_bundled_vertex' objects, you can store these with algorithm 147:

Algorithm 147 Storing a graph with bundled vertices as a .dot file

This code looks small, because we call the 'make_bundled_vertices_writer' function, which is shown in algorithm 148:

Algorithm 148 The 'make bundled vertices writer' function

```
template <typename graph>
inline bundled_vertices_writer<graph>
make_bundled_vertices_writer(
   const graph& g
)
{
   return bundled_vertices_writer<
      graph
   >(g);
}
```

Also this function is forwarding the real work to the 'bundled_vertices_ writer', shown in algorithm 149:

Algorithm 149 The 'bundled_vertices_writer' function

```
#include <ostream>
#include "graphviz_encode.h"
template <
  typename graph
class bundled_vertices_writer {
public:
  bundled_vertices_writer(
    graph g
    : m_g\{g\}
  template <class vertex descriptor>
  void operator()(
    std::ostream& out,
    const vertex descriptor& vd
  ) const noexcept {
    out
      << " [ label = \""
        << graphviz encode(</pre>
          m_g[vd].m_name
      << " \ " , comment = \ " "
        << graphviz encode(</pre>
          m_g[vd].m_description
      << "\", width="
        << m_g[vd].m_x
      << ", height="
        << m_g[vd].m_y
      << "]"
  }
private:
  graph m_g;
};
```

Here, some interesting things are happening: the writer needs the bundled property maps to work with and thus copies the whole graph to its internals. I have chosen to map the 'my_bundled_vertex' member variables to Graphviz attributes (see chapter 25.2 for most Graphviz attributes) as shown in table 2:

my_bundled_vertex variable	C++ data type	Graphviz data type	Graphviz attribute
m_name	std::string	string	label
${ m m_description}$	std::string	string	comment
m_x	double	double	width
m_y	double	double	height

Table 2: Mapping of my_bundled_vertex member variable and Graphviz attributes

Important in this mapping is that the C++ and the Graphviz data types match. I also chose attributes that matched as closely as possible.

The writer also encodes the std::string of the name and description to a Graphviz-friendly format. When loading the .dot file again, this will have to be undone again.

9.7 Loading a directed graph with bundled vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with bundled vertices is loaded, as shown in algorithm 150:

 $\bf Algorithm~150$ Loading a directed graph with bundled vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create_empty_directed_bundled_vertices_graph.h"
#include "graphviz decode.h"
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS,
  my bundled vertex
load directed bundled vertices graph from dot (
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g = create empty directed bundled vertices graph()
  boost::dynamic properties p; // do default construct
  p.property("node id", get(&my bundled vertex::m name, g)
  p.property("label",get(&my_bundled_vertex::m_name, g));
  p.property("comment", get(&my bundled vertex::
     m_description, g));
  \begin{array}{lll} \texttt{p.property("width", get(\&my\_bundled\_vertex::m\_x, g));} \end{array}
  p.property("height", get(&my bundled vertex::m y, g));
  boost::read graphviz(f,g,p);
  //Decode vertices
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i)
    g[*i].m_name = graphviz_decode(g[*i].m_name);
    g[*i].m description = graphviz decode(g[*i]).
        m description);
  return g;
}
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created, to save typing the typename explicitly.

Then a boost::dynamic_properties is created with its default constructor, after which we set it to follow the same mapping as in the previous chapter. From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

At the moment the graph is created, all 'my_bundled_vertex' their names and description are in a Graphviz-friendly format. By obtaining all vertex iterators and vertex descriptors, the encoding is made undone.

Algorithm 151 shows how to use the 'load_directed_bundled_vertices_graph_from_dot' function:

Algorithm 151 Demonstration of the 'load_directed_bundled_vertices_graph_from_dot' function

```
#include "create bundled vertices markov chain.h"
#include "load directed bundled vertices graph from dot.h
#include "save bundled vertices graph to dot.h"
#include "get bundled vertex my vertexes.h"
void load directed bundled vertices graph from dot demo()
    noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create bundled vertices markov chain();
  const std::string filename{
    "create bundled vertices markov chain.dot"
  save bundled vertices graph to dot(g, filename);
  const auto h
    = load directed bundled vertices graph from dot(
       filename);
  assert(num\_edges(g) == num\_edges(h));
  assert(num \ vertices(g) == num \ vertices(h));
  assert (get bundled vertex my vertexes (g)
    == get bundled vertex my vertexes(h)
  );
}
```

This demonstration shows how the Markov chain is created using the 'create bundled vertices markov chain' function (algorithm 132), saved and then

loaded. The loaded graph is checked to be the same as the original.

9.8 Loading an undirected graph with bundled vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with bundled vertices is loaded, as shown in algorithm 152:

 $\bf Algorithm~152~{\rm Loading~an}$ undirected graph with bundled vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create_empty_undirected_bundled_vertices_graph.
   h "
#include "graphviz decode.h"
#include "is_regular_file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  my bundled vertex
load _ undirected _ bundled _ vertices _ graph _ from _ dot (
  const std::string& dot filename
{
  assert(is_regular_file(dot_filename));
  std::ifstream f(dot filename.c str());
  auto g = create_empty_undirected_bundled_vertices_graph
     ();
  boost::dynamic_properties p; //_do_ default construct
  p.property("node_id",get(&my_bundled_vertex::m_name, g)
     );
  p.property("label", get(&my bundled vertex::m name, g));
  p.property("comment", get(&my bundled vertex::
     m description, g));
  p.property("width", get(&my_bundled_vertex::m_x, g));
  p.property("height", get(&my bundled vertex::m y, g));
  boost::read graphviz(f,g,p);
  //Decode vertices
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i)
    g[*i].m_name = graphviz_decode(g[*i].m_name);
    g[*i].m description = graphviz decode(g[*i]).
       m description);
  return g;
}
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 9.7 describes the rationale of this function.

Algorithm 153 shows how to use the 'load_undirected_bundled_vertices_graph_from_dot' function:

Algorithm 153 Demonstration of the 'load_undirected_bundled_vertices_graph_from_dot' function

```
#include < cassert >
#include "create bundled vertices k2 graph.h"
#include "load undirected bundled vertices graph from dot
   . h"
#include "save_bundled_vertices_graph_to_dot.h"
#include "get bundled vertex my vertexes.h"
void load undirected bundled vertices graph from dot demo
   () noexcept
{
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create bundled_vertices_k2_graph();
  const std::string filename{
    "create\_bundled\_vertices\_k2\_graph.dot"
  save bundled vertices graph to dot(g, filename);
  const auto h
    = load undirected bundled vertices graph from dot(
       filename);
  assert(num edges(g) == num edges(h));
  assert(num \ vertices(g) == num \ vertices(h));
  assert (get_bundled_vertex_my_vertexes(g)
    == get bundled vertex my vertexes(h)
  );
```

This demonstration shows how K_2 with bundled vertices is created using the 'create_bundled_vertices_k2_graph' function (algorithm 135), saved and then loaded. The loaded graph is checked to be the same as the original.

10 Building graphs with bundled edges and vertices

Up until now, the graphs created have had only bundled vertices. In this chapter, graphs will be created, in which both the edges and vertices have a bundled 'my bundled edge' and 'my bundled edge' type¹⁰.

- \bullet An empty directed graph that allows for bundled edges and vertices: see chapter 10.2
- An empty undirected graph that allows for bundled edges and vertices: see chapter 10.3
- A two-state Markov chain with bundled edges and vertices: see chapter 10.6
- K_3 with bundled edges and vertices: see chapter 10.7

In the process, some basic (sometimes bordering trivial) functions are shown:

- Creating the 'my bundled edge' class: see chapter 10.1
- Adding a bundled 'my bundled edge': see chapter 10.4

These functions are mostly there for completion and showing which data types are used.

10.1 Creating the bundled edge class

In this example, I create a 'my_bundled_edge' class. Here I will show the header file of it, as the implementation of it is not important yet.

¹⁰I do not intend to be original in naming my data types

Algorithm 154 Declaration of my bundled edge

```
#include < string>
#include <iosfwd>
class my bundled edge
public:
  explicit my bundled edge (
    const std::string& name = "",
    const std::string& description = "",
    const double width = 1.0,
    const double height = 1.0
  ) noexcept;
  std::string m_name;
  std::string m description;
  double m width;
  double m_height;
};
bool operator == (const my bundled edge& lhs, const
   my bundled_edge& rhs) noexcept;
\mathbf{bool\ operator!} \!=\! (\mathbf{const}\ \mathrm{my\_bundled\_edge\&\ lhs}\ ,\ \mathbf{const}
   my bundled edge& rhs) noexcept;
```

my_bundled_edge is a class that has multiple properties: two doubles 'm_width' ('m_' stands for member) and 'm_height', and two std::strings m_name and m_description. 'my_bundled_edge' is copyable, but cannot trivially be converted to a std::string.' 'my_bundled_edge' is comparable for equality (that is, operator== is defined).

'my_bundled_edge' does not have to have the stream operators defined for file I/O, as this goes via the public member variables.

10.2 Create an empty directed graph with bundled edges and vertices

Algorithm 155 Creating an empty directed graph with bundled edges and vertices

```
#include <boost/graph/adjacency list.hpp>
#include "my_bundled_edge.h"
#include "my bundled vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  my_bundled_vertex,
  my bundled edge
create empty directed bundled edges and vertices graph()
   noexcept
  return boost::adjacency list<
    boost :: vecS,
    boost :: vecS,
    boost::directedS,
    my bundled vertex,
    my_bundled_edge
  >();
}
```

This code is very similar to the code described in chapter 12.3, except that there is a new, fifth template argument:

```
boost::property<boost::edge bundled type t, my edge>
```

This can be read as: "edges have the property 'boost::edge_bundled_type_t', which is of data type 'my_bundled_edge". Or simply: "edges have a bundled type called my_bundled_edge".

Demo:

```
Algorithm
                 156
                          Demonstration
                                                     the
                                                              'cre-
ate\_empty\_directed\_bundled\_edges\_and\_vertices\_graph' function
#include "
    create\_empty\_directed\_bundled\_edges\_and\_vertices\_graph
    . h"
void
    create\_empty\_directed\_bundled\_edges\_and\_vertices\_graph\_demo
    () noexcept
  const auto g =
      create_empty_directed_bundled_edges_and_vertices_graph
  assert(boost::num\_edges(g) == 0);
  assert(boost::num\_vertices(g) == 0);
}
```

10.3 Create an empty undirected graph with bundled edges and vertices

Algorithm 157 Creating an empty undirected graph with bundled edges and vertices

```
#include <boost/graph/adjacency list.hpp>
#include "my_bundled_edge.h"
#include "my_bundled vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  my_bundled_vertex,
  my bundled edge
create empty undirected bundled edges and vertices graph
   () noexcept
  return boost::adjacency_list<
    boost :: vecS,
    boost :: vecS,
    boost::undirectedS,
    my_bundled_vertex,
    my\_bundled\_edge
  >();
}
```

This code is very similar to the code described in chapter 10.2, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS). Demo:

```
Algorithm
                 158
                          Demonstration
                                             of
                                                    the
                                                              'cre-
ate\_empty\_undirected\_bundled\_edges\_and\_vertices\_graph' function
#include <cassert>
#include "
   create_empty_undirected_bundled_edges_and_vertices_graph
void
   create\_empty\_undirected\_bundled\_edges\_and\_vertices\_graph\_demo
    () noexcept
  const auto g
        create\_empty\_undirected\_bundled\_edges\_and\_vertices\_graph
  assert(boost::num\_edges(g) == 0);
  assert (boost::num vertices(g) == 0);
```

10.4 Add a bundled edge

Adding a bundled edge is very similar to adding a named edge (chapter 6.3).

Algorithm 159 Add a bundled edge

```
#include < cassert >
#include <boost/graph/adjacency_list.hpp>
#include "my bundled edge h"
template <typename graph>
\mathbf{typename} \hspace{0.2cm} \texttt{boost} :: \mathtt{graph\_traits} \negthinspace < \negthinspace \mathtt{graph} \negthinspace > \negthinspace :: \mathtt{edge\_descriptor}
add bundled edge (
   const my_bundled_edge& v,
   graph& g
) noexcept
   static_assert(!std::is_const<graph>::value, "graph_
       cannot_be_const");
   const auto vd a = boost::add vertex(g);
   const auto vd b = boost::add vertex(g);
   \mathbf{const} \ \mathbf{auto} \ \mathbf{aer} \ = \ \mathbf{boost} :: \mathbf{add\_edge}(\mathbf{vd\_a}, \ \mathbf{vd\_b}, \ \mathbf{g}) \, ;
   assert (aer.second);
   g[aer.first] = v; //Cannot use put here
   return aer.first;
}
```

When having added a new (abstract) edge to the graph, the edge descriptor is used to set the my edge in the graph.

Here is the demo:

Algorithm 160 Demo of 'add bundled edge'

```
#include < cassert >
#include "add bundled edge.h"
#include "
   create_empty_directed_bundled_edges_and_vertices_graph
   . h"
#include "
   create_empty_undirected_bundled_edges_and_vertices_graph
   . h"
void add bundled edge demo() noexcept
  auto g =
     create\_empty\_directed\_bundled\_edges\_and\_vertices\_graph
  add bundled edge(my bundled edge("X"), g);
  assert(boost::num \ vertices(g) == 2);
  assert(boost::num edges(g) == 1);
  auto h =
     create_empty_undirected_bundled_edges_and_vertices_graph
  add_bundled_edge(my_bundled_edge("Y"), h);
  assert (boost::num vertices(h) == 2);
  assert(boost::num edges(h) == 1);
}
```

10.5 Getting the bundled edges my edges

When the edges of a graph are 'my_bundled_edge' objects, one can extract these all as such:

Algorithm 161 Get the edges' my bundled edges

```
#include < vector>
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_edge.h"
template <typename graph>
std::vector<my_bundled_edge> get_bundled_edge_my_edges(
  const graph& g
) noexcept
  std::vector<my bundled edge> v;
  v.reserve(boost::num edges(g));
  const auto eip
    = \operatorname{edges}(g); //not \ boost:: edges
  const auto j = eip.second;
  for (auto i = eip.first; i!=j; ++i) {
    v.emplace back(g[*i]);
  return v;
}
```

The 'my_bundled_edge' object associated with the edges are obtained from the graph its property_map and then put into a std::vector.

Note: the order of the my_bundled_edge objects may be different after saving and loading.

When trying to get the edges' my_bundled_edge objects from a graph without bundled edges objects associated, you will get the error 'formed reference to void' (see chapter 24.1).

10.6 Creating a Markov-chain with bundled edges and vertices

10.6.1 Graph

Figure 30 shows the graph that will be reproduced:



Figure 30: A two-state Markov chain where the edges and vertices have bundled properies. The edges' and vertices' properties are nonsensical

10.6.2 Function to create such a graph

Here is the code creating a two-state Markov chain with bundled edges and vertices:

```
#include <cassert>
#include "
   create empty directed bundled edges and vertices graph
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS,
  my bundled vertex,
  my bundled edge
create bundled edges and vertices markov chain () noexcept
  auto g
        create empty directed bundled edges and vertices graph
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  {f const\ auto}\ {f aer\_ba} = {f boost}:: {f add\_edge}({f vd\_b},\ {f vd\_a},\ {f g}) \; ;
  assert (aer ba.second);
  const auto aer bb = boost::add edge(vd b, vd b, g);
  assert (aer bb.second);
  g [vd a]
    = my bundled vertex("Stable", "Right", 1.0, 2.0);
  g[vd b]
    = my bundled vertex("Not_unstable", "Not_left"
        ,3.0,4.0);
  g[aer aa.first]
    = my bundled edge("Red", "Heat", 1.0, 2.0);
  g[aer ab.first]
    = my bundled edge("Orange", "Lose_heat", 3.0,4.0);
  g[aer ba.first]
    = my bundled edge("Yellow_cold", "Heat", 5.0, 6.0);
  g[aer bb.first]
    = my bundled edge("Green_cold", "Stay_cool", 7.0, 8.0);
  return g;
```

10.6.3 Creating such a graph

Here is the demo:

};

const std::vector<my bundled edge> expected my edges{

 $\label{low_bundled_edge} $$ my_bundled_edge("Orange", "Lose_heat", 3.0, 4.0), $$ my_bundled_edge("Yellow_cold", "Heat", 5.0, 6.0), $$ my_bundled_edge("Green_cold", "Stay_cool", 7.0, 8.0)$

my bundled edge("Red", "Heat", 1.0, 2.0),

assert (edge my edges == expected my edges);

10.6.4 The .dot file produced

get bundled edge my edges(g)

```
Algorithm
               164
                       .dot
                                                 from
                                                         the
                                                                 'cre-
ate bundled edges and vertices markov chain'
                                                function
                                                           (algorithm
162), converted from graph to .dot file using algorithm 48
digraph G {
0[label="Stable",comment="Right",width=1,height=2];
1[label="Not$$$SPACE$$$unstable",comment="Not$$$SPACE$$$left",width=3,height=4];
0->0 [label="Red",comment="Heat",width=1,height=2];
0->1 [label="Orange",comment="Lose$$$SPACE$$$heat",width=3,height=4];
1->0 [label="Yellow$$$SPACE$$$cold",comment="Heat",width=5,height=6];
1->1 [label="Green$$$SPACE$$$cold",comment="Stay$$$SPACE$$$cool",width=7,height=8];
```

10.6.5 The .svg file produced

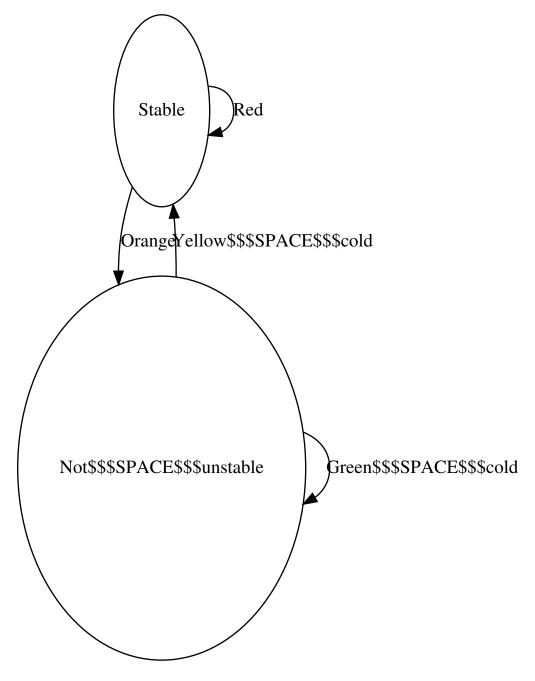


Figure 31: .svg file created from the 'create_bundled_edges_and_vertices_markov_chain' function (algorithm 191) its .dot file, converted from .dot file to .svg using algorithm 279

10.7 Creating K_3 with bundled edges and vertices

Instead of using edges with a name, or other properties, here we use a bundled edge class called 'my_bundled_edge'.

10.7.1 Graph

We reproduce the K_3 with named edges and vertices of chapter 6.6, but with our bundled edges and vertices intead:

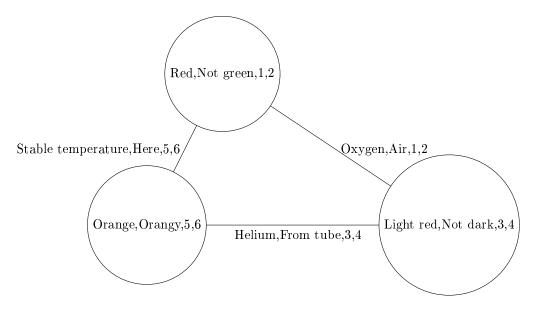


Figure 32: K_3 : a fully connected graph with three named edges and vertices

Algorithm 165 Creating K_3 as depicted in figure 24

```
#include "
   create empty undirected bundled edges and vertices graph
    . h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  my bundled vertex,
  my bundled edge
create_bundled_edges_and_vertices_k3_graph() noexcept
  auto g
        create empty undirected bundled edges and vertices graph
  const auto vd_a = boost::add_vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto vd c = boost::add vertex(g);
  const auto aer a = boost::add edge(vd a, vd b, g);
  const auto aer b = boost::add edge(vd b, vd c, g);
  {f const\ auto}\ {f aer\_c}\ =\ {f boost}:: {f add\_edge}\left({f vd\_c}\,,\ {f vd\_a},\ {f g}\right);
  assert (aer a.second);
  assert (aer b.second);
  assert (aer c.second);
  g[vd a]
    = my_bundled_vertex("Red","Not_green",1.0,2.0);
  g[vd b]
    = my bundled vertex("Light_red", "Not_dark", 3.0, 4.0);
  g[vd c]
    = my bundled vertex("Orange", "Orangy", 5.0, 6.0);
  g[aer a.first]
    = my bundled edge("Oxygen", "Air", 1.0, 2.0);
  g[aer b.first]
    = my bundled edge("Helium", "From_tube", 3.0, 4.0);
  g | aer c. first |
    = my bundled edge("Stable_temperature", "Here"
        ,5.0,6.0);
  return g;
}
```

Most of the code is a slight modification of algorithm 109. In the end, the my_edges and my_vertices are obtained as the graph its property_map and set with the 'my_bundled_edge' and 'my_bundled_vertex' objects.

10.7.3 Creating such a graph

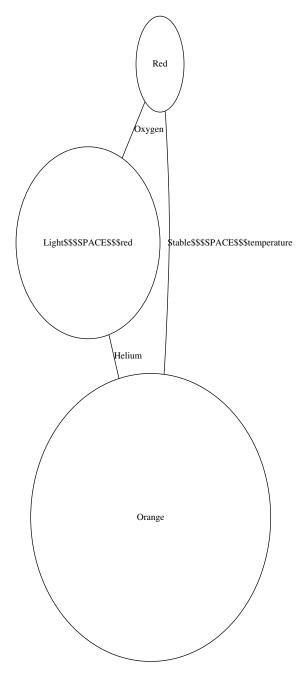
Here is the demo:

Algorithm 166 Demo of the 'create_bundled_edges_and_vertices_k3_graph' function (algorithm 165)

10.7.4 The .dot file produced

```
Algorithm
                               file
               167
                       .dot
                                      created
                                                 from
                                                          the
                                                                 'cre-
ate bundled edges and vertices markov chain'
                                                 function
                                                            (algorithm
165), converted from graph to .dot file using algorithm 48
graph G {
O[label="Red",comment="Not$$$SPACE$$$green",width=1,height=2];
1[label="Light$$$SPACE$$$red",comment="Not$$$SPACE$$$dark",width=3,height=4];
2[label="Orange",comment="Orangy",width=5,height=6];
0--1 [label="Oxygen",comment="Air",width=1,height=2];
1--2 [label="Helium",comment="From$$$SPACE$$$tube",width=3,height=4];
2--0 [label="Stable$$$PACE$$$temperature",comment="Here",width=5,height=6];
}
```

10.7.5 The .svg file produced



11 Working on graphs with bundled edges and vertices

$11.1 \quad Has \ a \ my_bundled_edge$

Before modifying our edges, let's first determine if we can find an edge by its bundled type ('my_bundled_edge') in a graph. After obtaing a my_bundled_edge map, we obtain the edge iterators, dereference these to obtain the edge descriptors and then compare each edge its my_bundled_edge with the one desired.

Algorithm 168 Find if there is a bundled edge with a certain my bundled edge

```
\#include <boost/graph/properties.hpp>
#include "my bundled edge.h"
template <typename graph>
bool has_bundled_edge_with_my_edge(
  const my bundled edge& e,
  const graph& g
  noexcept
  const auto eip
    = \operatorname{edges}(g); //not boost:: edges
  const auto j = eip.second;
  for (auto i = eip.first; i!=j; ++i) {
    if (g[*i] = e) {
      return true;
    }
  }
  return false;
```

This function can be demonstrated as in algorithm 169, where a certain 'my_bundled_edge' cannot be found in an empty graph. After adding the desired my_bundled_edge, it is found.

Algorithm 169 Demonstration of the 'has_bundled_edge_with_my_edge' function

```
#include <cassert>
#include "add bundled edge.h"
#include "
   create_empty_undirected_bundled_edges_and_vertices_graph
   . h"
#include "has bundled edge with my edge.h"
void has bundled edge with my edge demo() noexcept
{
  auto g
       create empty undirected bundled edges and vertices graph
  assert (
    ! has bundled edge with my edge (
      my bundled edge("Edward"),g
  );
  add_bundled_edge(my_bundled_edge("Edward"),g);
  assert (
    has_bundled_edge_with_my_edge(
      my bundled edge ("Edward"), g
  );
}
```

Note that this function only finds if there is at least one edge with that my_bundled_edge: it does not tell how many edges with that my_bundled_edge exist in the graph.

11.2 Find a my bundled edge

Where STL functions work with iterators, here we obtain an edge descriptor (see chapter 2.12) to obtain a handle to the desired edge. Algorithm 170 shows how to obtain an edge descriptor to the first edge found with a specific my bundled edge value.

Algorithm 170 Find the first bundled edge with a certain my_bundled_edge

```
#include <cassert>
#include <boost/graph/graph_traits.hpp>
#include "has bundled edge with my edge.h"
#include "has custom edge with my edge.h"
#include "my bundled edge.h"
template <typename graph>
typename boost::graph_traits<graph>::edge_descriptor
find_first_bundled_edge_with_my_edge(
  const my bundled edge& e,
  const graph& g
  noexcept
  assert (has bundled edge with my edge (e, g));
  const auto eip = edges(g); //not boost::edges
  const auto j = eip.second;
  for (auto i = eip.first; i!=j; ++i) {
    if (g[*i] = e) {
      return *i;
    }
  assert (!"Should_not_get_here");
  throw; // Will crash the program
```

With the edge descriptor obtained, one can read and modify the edge and the vertices surrounding it. Algorithm 171 shows some examples of how to do so.

Algorithm 171 Demonstration of the 'find_first_bundled_edge_with_my_edge' function

11.3 Get an edge its my_bundled_edge

To obtain the my_edeg from an edge descriptor, one needs to pull out the my_bundled_edges map and then look up the my_edge of interest.

Algorithm 172 Get a vertex its my bundled vertex from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include "install_edge_custom_type.h"
#include "my_custom_edge.h"
template <typename graph>
my_custom_edge_get_custom_edge_my_edge(
  const typename boost::graph_traits<graph>::
      edge_descriptor& vd,
  const graph& g
) noexcept
  const auto my edge map
    = \gcd(\ //\mathit{not}\ boost::get
      boost::edge custom type,
      g
    );
  return my_edge_map[vd];
}
```

To use 'get_bundled_edge_my_bundled_edge', one first needs to obtain an edge descriptor. Algorithm 173 shows a simple example.

Algorithm 173 Demonstration if the 'get bundled edge my edge' function

$11.4 \quad {\bf Set \ an \ edge \ its \ my_bundled_edge}$

If you know how to get the my_bundled_edge from an edge descriptor, setting it is just as easy, as shown in algorithm 174.

Algorithm 174 Set a bundled edge its my_bundled_edge from its edge descriptor

```
#include <boost/graph/properties.hpp>
#include "my_bundled_edge.h"

template <typename graph>
void set_bundled_edge_my_edge(
   const my_bundled_edge& name,
   const typename boost::graph_traits<graph>::
        edge_descriptor& ed,
        graph& g
) noexcept
{
   static_assert(!std::is_const<graph>::value,
        "graph_cannot_be_const"
);
   g[ed] = name;
}
```

To use 'set_bundled_edge_my_edge', one first needs to obtain an edge descriptor. Algorithm 175 shows a simple example.

Algorithm 175 Demonstration if the 'set bundled edge my edge' function

```
#include <cassert>
#include "add bundled edge.h"
#include "
   create empty undirected bundled edges and vertices graph
   . h"
#include "find first bundled edge with my edge.h"
#include "get bundled edge my edge.h"
#include "set_bundled edge my edge.h"
void set bundled edge my edge demo() noexcept
  auto g
       create empty undirected bundled edges and vertices graph
  const my_bundled_edge old_edge{"Dex"};
  add bundled edge(old edge, g);
  {f const} auto {f vd}
    = find first bundled edge with my edge(old edge,g);
  assert (get bundled edge my edge (vd,g)
    = old edge
  );
  const my bundled edge new edge{"Diggy"};
  set_bundled_edge_my_edge(new_edge, vd, g);
  assert (get bundled edge my edge (vd,g)
    == new edge
  );
}
```

11.5 Storing a graph with bundled edges and vertices as a .dot

If you used the 'create_bundled_edges_and_vertices_k3_graph' function (algorithm 165) to produce a K_3 graph with edges and vertices associated with my_bundled_edge and my_bundled_vertex objects, you can store these my_bundled_edges and my_bundled_vertex-es additionally with algorithm 176:

Algorithm 176 Storing a graph with bundled edges and vertices as a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "make bundled vertices writer.h"
#include "make bundled edges writer.h"
template <typename graph>
void save bundled edges and vertices graph to dot (
  const graph& g,
  const std::string& filename
  std::ofstream f(filename);
  write graphviz (
    f,
    make bundled vertices writer(g),
    make bundled edges writer(g)
  );
}
\#include < fstream >
\#include < string >
\#include = \langle boost/graph/graphviz.hpp 
angle
\#include < boost/graph/properties . hpp > i
#include "get bundled edge my edge.h"
#include "get bundled vertex my vertexes.h"
template < typename graph >
void save bundled edges and vertices graph to dot (
  const\ graph \mathcal{E}\ g,
  const std::string & filename
{
  using my vertex descriptor = typename graph::
      vertex\_descriptor;
  using my edge descriptor = typename graph::
      edge descriptor;
  std::ofstream \ f(filename);
  boost::write graphviz
    f,
    g,
    [g](
       std::ostream \mathcal{C} out,
       const my vertex descriptor& v
       const\ my\_bundled\_vert \frac{1}{2} 2m\{g[v]\};
       out << " f l a b e l = | ""
         << m.m_name
         << ","
         << m.m\_description
         << ","
         << m.m.x
         << "."
```

11.6 Load a directed graph with bundled edges and vertices from a .dot file

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with bundled edges and vertices is loaded, as shown in algorithm 177:

Algorithm 177 Loading a directed graph with bundled edges and vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create _ empty _ directed _ bundled _ edges _ and _ vertices _ graph
    . h"
#include "is regular file.h"
#include "graphviz decode.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  my bundled vertex,
  my\_bundled\_edge
load directed bundled edges and vertices graph from dot (
  const std::string& dot filename
  assert (is_regular_file (dot_filename));
  std::ifstream f(dot_filename.c_str());
  auto g =
     create empty directed bundled edges and vertices graph
  boost::dynamic properties p; // do default construct
  p.property("node_id",get(&my_bundled_vertex::m_name, g)
     );
  p.property("label",get(&my_bundled_vertex::m_name, g));
  p.property("comment", get(&my bundled vertex::
      m_description, g));
  \begin{array}{lll} & p.\ property \ ("width", \ get \ (\&my\_bundled\_vertex :: m\_x, \ g)) \ ; \end{array}
  p.property("height", get(&my bundled vertex::m y, g));
  {\tt p.property\,("edge\_id",get(\&my\_bundled\_edge::m\_name,~g));}\\
  p.property("label",get(&my_bundled_edge::m_name, g));
  p.property("comment", get(&my_bundled_edge::
      m_description, g));
  p.property("width", get(&my_bundled_edge::m_width, g));
  p.property("height", get(&my bundled edge::m height, g)
  boost::read graphviz(f,g,p);
  //Decode vertices
    const auto vip = vertices(g);
    const auto j = vip.seconl94
    for (auto i = vip.first; i!=j; ++i)
      g[*i].m_name = graphviz_decode(g[*i].m_name);
      g[*i].m description = graphviz decode(g[*i].
          m description);
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Next to this, a boost::dynamic_properties is created with its default constructor, after which we direct the boost::dynamic_properties to find a 'node_id' and 'label' in the vertex name map, 'edge_id' and 'label to the edge name map. From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

 $Algorithm\ 178\ shows\ how\ to\ use\ the\ 'load_directed_bundled_edges_and_vertices_graph_from_dot'\ function:$

 ${\bf Algorithm~178~Demonstration~of~the~'load_directed_bundled_edges_and_vertices_graph_from_dot'~function}$

```
#include "create bundled edges and vertices markov chain.
   h"
#include "get_sorted_bundled_vertex_my vertexes.h"
#include
   load directed bundled edges and vertices graph from dot
   . h"
#include "save bundled edges and vertices graph to dot.h"
void
   load directed bundled edges and vertices graph from dot demo
   () noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create bundled edges and vertices markov chain();
  const std::string filename{
    "create bundled edges and vertices markov chain.dot"
  save bundled edges and vertices graph to dot(g,
     filename);
  const auto h
       load directed bundled edges and vertices graph from dot
      filename
    );
  assert(num edges(g) == num edges(h));
  assert(num \ vertices(g) == num \ vertices(h));
  assert (get sorted bundled vertex my vertexes (g)
    == get sorted bundled vertex my vertexes(h)
  );
}
```

This demonstration shows how the Markov chain is created using the 'create_bundled_edges_and_vertices_markov_chain' function (algorithm 162), saved and then loaded.

11.7 Load an undirected graph with bundled edges and vertices from a .dot file

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with bundled edges and vertices is loaded, as shown in algorithm 179:

 ${\bf Algorithm~179}$ Loading an undirected graph with bundled edges and vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create_empty_undirected_bundled_edges_and_vertices_graph
    . h"
#include "is regular file.h"
#include "graphviz decode.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  my bundled vertex,
  my\_bundled\_edge
load undirected bundled edges and vertices graph from dot
  const std::string& dot filename
  assert(is_regular_file(dot_filename));
  std::ifstream f(dot filename.c str());
  auto g =
     create empty undirected bundled edges and vertices graph
      ();
  boost::dynamic_properties p; //_do_ default construct
  \verb|p.property| ( \verb|"node_id", get(\&my\_bundled\_vertex::m_name, g) \\
     );
  p.property("label",get(&my_bundled_vertex::m_name, g));
  {\tt p.property("comment", get(\&my\_bundled\_vertex::}
      m_description, g));
  p.property("width", get(&my_bundled_vertex::m_x, g));
  {\tt p.property("height", get(\&my\_bundled\_vertex::m\_y, g));}\\
  p.property("edge_id",get(&my_bundled_edge::m_name, g));
  \verb|p.property| ( \verb|"label", get(&my\_bundled\_edge::m\_name, g) ) ; \\
  p.property("comment", get(&my_bundled_edge::
      m_description, g));
  \verb|p.property("width", get(\&my\_bundled\_edge::m\_width, g));|\\
  p.property("height", get(&my_bundled_edge::m_height, g)
     );
  boost:: read\_graphviz(f,g,p);
  //Decode\ vertices
    const auto vip = verticel98g);
    const auto j = vip.second;
    for (auto i = vip.first; i!=j; ++i)
      g[*i].m name = graphviz decode(g[*i].m name);
      g[*i].m description = graphviz decode(g[*i].
          m description);
    }
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 11.6 describes the rationale of this function

 $Algorithm\ 180\ shows\ how\ to\ use\ the\ 'load_undirected_bundled_vertices_graph_from_dot'\ function:$

 $\overline{\textbf{Algorithm 180}} \ Demonstration \ of the \ 'load_undirected_bundled_edges_and_vertices_graph_from_dot' function$

```
#include "create bundled edges and vertices k3 graph.h"
#include "get sorted bundled vertex my vertexes.h"
#include "
   load undirected bundled edges and vertices graph from dot
   . h"
#include "save bundled edges and vertices graph to dot.h"
void
   load undirected bundled edges and vertices graph from dot demo
   () noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create_bundled_edges_and_vertices_k3_graph();
  const std::string filename{
    "create bundled edges and vertices k3 graph.dot"
  save bundled edges and vertices graph to dot(g,
     filename);
  const auto h
       load undirected bundled edges and vertices graph from dot
      filename
    );
  assert(num\_edges(g) == num\_edges(h));
  assert(num \ vertices(g) == num \ vertices(h));
  assert (get sorted bundled vertex my vertexes (g)
    == get_sorted_bundled_vertex_my_vertexes(h)
  );
}
```

This demonstration shows how K_2 with bundled vertices is created using the 'create_bundled_vertices_k2_graph' function (algorithm 194), saved and

then loaded. The loaded graph is checked to be a graph similar to the original.

12 Building graphs with custom vertices

Instead of using bundled properties, you can also add a new custom property. The difference is that instead of having a class as a vertex, vertices have an additional property where the 'my_custom_vertex' is stored, next to properties like vertex name, edge delay (see chapter 25.1 for all properties). The following graphs will be created:

- An empty directed graph that allows for custom vertices: see chapter 183
- An empty undirected graph that allows for custom vertices: see chapter 12.3
- A two-state Markov chain with custom vertices: see chapter 12.7
- K_2 with custom vertices: see chapter 12.8

In the process, some basic (sometimes bordering trivial) functions are shown:

- Installing a new vertex property, called 'vertex_custom_type': chapter 12.2
- Adding a custom vertex: see chapter 12.5
- Getting the custom vertices my_vertex-es: see chapter 12.6

These functions are mostly there for completion and showing which data types are used.

12.1 Creating the vertex class

Before creating an empty graph with custom vertices, that custom vertex class must be created. In this tutorial, it is called 'my_custom_vertex'. 'my_custom_vertex' is a class that is nonsensical, but it can be replaced by any other class type.

Here I will show the header file of 'my_custom_vertex', as the implementation of it is not important:

Algorithm 181 Declaration of my custom vertex

```
#include < string>
#include <iosfwd>
class my custom vertex
public:
  explicit my custom vertex (
    const std::string& name = "",
    const std::string& description = "",
    const double x = 0.0,
    const double y = 0.0
  ) noexcept;
  const std::string& get_description() const noexcept;
  const std::string& get name() const noexcept;
  double get_x() const noexcept;
  \mathbf{double} \ \mathtt{get} \_ \mathtt{y} \, (\,) \ \mathbf{const} \ \mathtt{noexcept} \, ;
private:
  std::string m name;
  std::string m description;
  double m x;
  double m y;
};
bool operator == (const my_custom_vertex& lhs, const
   my_custom_vertex& rhs) noexcept;
bool operator!=(const my custom vertex& lhs, const
   my custom vertex& rhs) noexcept;
std::ostream& operator << (std::ostream& os, const
   my custom vertex& v) noexcept;
std::istream& operator>>(std::istream& os,
   my custom vertex& v) noexcept;
```

'my custom vertex' is a class that has multiple properties:

- It has four private member variables: the double 'm_x' ('m_' stands for member), the double 'm_y', the std::string m_name and the std::string m_description. These variables are private, but there are getters supplied
- It has a default constructor
- It is copyable
- It is comparable for equality (it has operator==), which is needed for searching

• It can be streamed (it has both operator << and operator>>), which is needed for file I/O.

Special characters like comma's, quotes and whitespace cannot be streamed without problems. The function 'graphviz_encode' (algorithm 276) can convert the elements to be streamed to a Graphviz-friendly version, which can be decoded by 'graphviz' decode' (algorithm 277).

12.2 Installing the new vertex property

Before creating an empty graph with custom vertices, this type must be installed as a vertex property. Installing a new property would have been easier, if 'more C++ compilers were standards conformant' ([8] chapter 3.6). Boost.Graph uses the BOOST_INSTALL_PROPERTY macro to allow using a custom property:

Algorithm 182 Installing the vertex_custom_type property

```
#include <boost/graph/properties.hpp>
namespace boost {
   enum vertex_custom_type_t { vertex_custom_type = 314 };
   BOOST_INSTALL_PROPERTY(vertex, custom_type);
}
```

The enum value 314 must be unique.

12.3 Create the empty directed graph with custom vertices

Algorithm 183 Creating an empty directed graph with custom vertices

```
#include <boost/graph/adjacency list.hpp>
#include "install_vertex_custom_type.h"
\#include "my_custom_vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS,
  boost::property<
    boost::vertex_custom_type_t, my_custom_vertex
create_empty_directed_custom_vertices_graph() noexcept
  return boost::adjacency list<
    boost :: vecS,
    boost :: vecS,
    boost::directedS,
    boost::property<
      boost:: vertex\_custom\_type\_t \;, \; my\_custom\_vertex
  >();
```

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)
- is directed (due to the boost::directedS)
- The vertices have one property: they have a custom type, that is of data type my vertex (due to the boost::property< boost::vertex custom type t,my vertex>')
- The edges and graph have no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fourth template argument 'boost::property
boost::vertex_custom_type_t,my_vertex>'. This can be read as: "vertices

have the property 'boost::vertex_custom_type_t', which is of data type 'my_vertex"'. Or simply: "vertices have a custom type called my_vertex".

The demo:

Algorithm 184 Demo how to create an empty directed graph with custom vertices

12.4 Create the empty undirected graph with custom vertices

Algorithm 185 Creating an empty undirected graph with custom vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "install vertex custom type.h"
#include "my_custom_vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
>
create_empty_undirected_custom_vertices_graph() noexcept
  return boost::adjacency_list<
    boost :: vecS,
    boost :: vecS,
    boost::undirectedS,
    boost::property<
      boost::vertex_custom_type_t, my_custom_vertex
  >();
```

This code is very similar to the code described in chapter 12.3, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS). The demo:

Algorithm 186 Demo how to create an empty undirected graph with custom vertices

12.5 Add a custom vertex

Adding a custom vertex is very similar to adding a named vertex (chapter 4.3).

Algorithm 187 Add a custom vertex

```
#include <type traits>
#include <boost/graph/adjacency_list.hpp>
#include "install_vertex_custom_type.h"
#include "my custom vertex.h"
template <typename graph>
typename boost::graph traits<graph>::vertex descriptor
\verb| add_custom_vertex| (
  const my custom vertex& v,
  graph& g
) noexcept
  static _ assert (! std :: is _ const < graph >:: value,
    "graph_cannot_be_const"
  );
  const auto vd = boost::add_vertex(g);
  const auto my custom vertex map
    = get( //not boost::get)
      boost::vertex custom type,
    );
  put (my custom vertex map, vd, v);
  return vd;
```

When having added a new (abstract) vertex to the graph, the vertex descriptor is used to set the my_vertex in the graph its my_vertex map (using 'get(boost::vertex custom type,g)').

Here is the demo:

Algorithm 188 Demo of 'add custom vertex'

```
#include <cassert>
#include "add custom vertex.h"
#include "create empty directed custom vertices graph.h"
#include "create empty undirected custom vertices graph.h
void add custom vertex demo() noexcept
  auto g
    = create empty directed custom vertices graph();
  assert(boost::num \ vertices(g) == 0);
  assert(boost::num edges(g) == 0);
  add_custom_vertex(my_custom_vertex("X"), g);
  assert(boost::num \ vertices(g) == 1);
  assert(boost::num edges(g) == 0);
  auto h
    = create empty undirected custom vertices graph();
  assert(boost::num \ vertices(h) == 0);
  assert(boost::num\_edges(h) == 0);
  add_custom_vertex(my_custom_vertex("X"), h);
  assert(boost::num vertices(h) == 1);
  assert(boost::num edges(h) == 0);
```

12.6 Getting the vertices' my_vertexes¹¹

When the vertices of a graph have any associated my_vertex, one can extract these as such:

¹¹the name 'my_vertexes' is chosen to indicate this function returns a container of my_vertex

Algorithm 189 Get the vertices' my_vertexes

```
#include < vector>
#include <boost/graph/adjacency_list.hpp>
#include "install vertex custom type.h"
#include "my custom vertex.h"
template <typename graph>
std::vector<my custom vertex>
   get_custom_vertex_my_vertexes(
  const graph& g
 noexcept
  std::vector<my custom vertex> v;
  v.reserve(boost::num_vertices(g));
  const auto my custom vertexes map
    = \gcd( //not \ boost::get
      boost::vertex custom type, g
    );
  const auto vip
    = vertices (g); //not boost::vertices
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i) {
    v.emplace_back(
      get( //not \ boost::get
        my custom vertexes map, *i
    );
  return v;
}
```

The my_vertex object associated with the vertices are obtained from a boost::property_map and then put into a std::vector.

The order of the 'my_custom_vertex' objects may be different after saving and loading.

When trying to get the vertices' my_vertex from a graph without my_vertex objects associated, you will get the error 'formed reference to void' (see chapter 24.1).

Demo:

Algorithm 190 Demo how to the vertices' my custom vertex objects

```
#include <cassert>
#include "create_custom_vertices_k2_graph.h"
#include "get_custom_vertex_my_vertexes.h"

void get_custom_vertex_my_vertexes_demo() noexcept
{
    const auto g = create_custom_vertices_k2_graph();
    const std::vector<my_custom_vertex>
        expected_my_custom_vertexes{
        my_custom_vertex("A","source",0.0,0.0),
        my_custom_vertex("B","target",3.14,3.14)
    };
    const std::vector<my_custom_vertex> vertexes{
        get_custom_vertex_my_vertexes(g)
    };
    assert(expected_my_custom_vertexes == vertexes);
}
```

12.7 Creating a two-state Markov chain with custom vertices

12.7.1 Graph

Figure 34 shows the graph that will be reproduced:



Figure 34: A two-state Markov chain where the vertices have custom properies and the edges have no properties. The vertices' properties are nonsensical

12.7.2 Function to create such a graph

Here is the code creating a two-state Markov chain with custom vertices:

Algorithm 191 Creating the two-state Markov chain as depicted in figure 34

```
#include <cassert>
#include "create_empty_directed_custom_vertices_graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
create custom vertices markov chain() noexcept
{
  auto g
   = create empty directed custom vertices graph();
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer bb = boost::add edge(vd b, vd b, g);
  assert (aer bb.second);
  auto my custom vertex map = get ( //not \ boost :: get)
    boost::vertex custom type, g
  );
  put (my custom vertex map, vd a,
    my_custom_vertex("Sunny","Yellow_thing",1.0,2.0)
  put (my custom vertex map, vd b,
    my custom vertex ("Rainy", "Grey_things", 3.0, 4.0)
  return g;
}
```

12.7.3 Creating such a graph

Here is the demo:

Algorithm 192 Demo of the 'create_custom_vertices_markov_chain' function (algorithm 191)

```
#include <cassert>
#include "create custom vertices markov chain.h"
#include "get custom vertex my vertexes.h"
void create custom vertices markov chain demo() noexcept
  const auto g
    = create_custom_vertices_markov_chain();
  const std::vector<my custom vertex>
    expected my custom vertexes {
    my custom vertex ("Sunny", "Yellow_thing", 1.0, 2.0),
    my_custom_vertex("Rainy","Grey_things",3.0,4.0)
  };
  const std::vector<my custom vertex>
    vertex my custom vertexes{
    get custom vertex my vertexes (g)
  };
  assert (expected_my_custom_vertexes
    == vertex my custom vertexes
  );
}
```

12.7.4 The .dot file produced

Algorithm 193 .dot file created from the 'create_custom_vertices_markov_chain' function (algorithm 191), converted from graph to .dot file using algorithm 206

```
digraph G {
    O[label="Sunny,Yellow$$$SPACE$$$thing,1,1"];
    1[label="Rainy,Grey$$$SPACE$$$things,3,3"];
    0->0;
    ->1;
    1->0;
    1->1;
}
```

This .dot file may look unexpectedly different: instead of a space, there is this '[[:SPACE:]]' thing. This is because the function 'graphviz_encode' (algorithm 276) made this conversion. In this example, I could have simply surrounded the content by quotes, and this would have worked. I chose to use 'graphviz_encode'

because it works in all contexts.

12.7.5 The .svg file produced

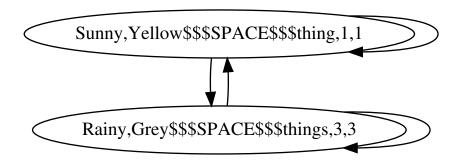


Figure 35: .svg file created from the 'create_custom_vertices_markov_chain' function (algorithm 191) its .dot file, converted from .dot file to .svg using algorithm 279

This .svg file may look unexpectedly different: instead of a space, there is this '[[:SPACE:]]' thing. This is because the function 'graphviz_encode' (algorithm 276) made this conversion.

12.8 Creating K_2 with custom vertices

12.8.1 Graph

We reproduce the K_2 with named vertices of chapter 4.6 , but with our custom vertices intead.

12.8.2 Function to create such a graph

Algorithm 194 Creating K_2 as depicted in figure 18

```
#include "create empty undirected custom vertices graph.h
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
>
create custom vertices k2 graph() noexcept
  auto g = create_empty_undirected_custom_vertices_graph
     ();
  const auto vd_a = boost::add_vertex(g);
  const auto vd b = boost::add_vertex(g);
  const auto aer = boost::add edge(vd a, vd b, g);
  assert (aer.second);
  auto my_custom_vertex_map = get( //not boost::get
    boost::vertex custom type, g
  );
  put (my custom vertex map, vd a,
    my_custom_vertex("A", "source", 0.0, 0.0)
  put(my_custom_vertex_map, vd_b,
    my_custom_vertex("B","target",3.14,3.14)
  );
  return g;
```

Most of the code is a slight modification of the 'create_named_vertices_k2_graph' function (algorithm 65). In the end, the my_vertices are obtained as a boost::property_map and set with two custom my_vertex objects.

12.8.3 Creating such a graph

Demo:

Algorithm 195 Demo of the 'create_custom_vertices_k2_graph' function (algorithm 194)

```
#include <cassert>
#include "create_custom_vertices_k2_graph.h"
#include "create_custom_vertex_with_my_vertex.h"

void create_custom_vertices_k2_graph_demo() noexcept
{
   const auto g = create_custom_vertices_k2_graph();
   assert(boost::num_edges(g) == 1);
   assert(boost::num_vertices(g) == 2);
   assert(has_custom_vertex_with_my_custom_vertex(
        my_custom_vertex("A", "source",0.0,0.0), g)
   );
   assert(has_custom_vertex_with_my_custom_vertex(
        my_custom_vertex("B", "target",3.14, 3.14), g)
   );
}
```

12.8.4 The .dot file produced

Algorithm 196 .dot file created from the 'create_custom_vertices_k2_graph' function (algorithm 194), converted from graph to .dot file using algorithm 48 graph G {
0[label="A,source,0,0"];
1[label="B,target,3.14,3.14"];
0--1;
}

12.8.5 The .svg file produced

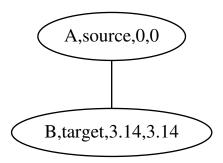


Figure 36: .svg file created from the 'create_custom_vertices_k2_graph' function (algorithm 194) its .dot file, converted from .dot file to .svg using algorithm 279

Working on graphs with custom vertices (as a custom property)

When using graphs with custom vertices, their state gives a way to find a vertex and working with it. This chapter shows some basic operations on graphs with custom vertices.

- Check if there exists a vertex with a certain 'my vertex': chapter 13.1
- Find a vertex with a certain 'my vertex': chapter 13.2
- Get a vertex its 'my vertex' from its vertex descriptor: chapter 13.3
- Set a vertex its 'my vertex' using its vertex descriptor: chapter 13.4
- Setting all vertices their 'my vertex'es: chapter 13.5
- \bullet Storing an directed/undirected graph with custom vertices as a .dot file: chapter 13.6
- Loading a directed graph with custom vertices from a .dot file: chapter 13.7
- \bullet Loading an undirected directed graph with custom vertices from a .dot file: chapter 13.8

13.1 Has a custom vertex with a my vertex

Before modifying our vertices, let's first determine if we can find a vertex by its custom type ('my vertex') in a graph. After obtaing a my vertex map, we

obtain the vertex iterators, dereference these to obtain the vertex descriptors and then compare each vertex its my_vertex with the one desired.

Algorithm 197 Find if there is vertex with a certain my vertex

```
#include < string>
#include <boost/graph/properties.hpp>
#include "install vertex custom type.h"
#include "my_custom_vertex.h"
template <typename graph>
bool has custom vertex with my custom vertex (
  const my custom vertex& v,
  const graph& g
 noexcept
  const auto my custom vertexes map
    = get(boost::vertex_custom_type, g);
  const auto vip
    = vertices(g); //not boost::vertices
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i) {
    if (
      get( //not \ boost::get
        my\_custom\_vertexes\_map\;,
        * i
      ) == v) \{
      return true;
  return false;
```

This function can be demonstrated as in algorithm 198, where a certain my_vertex cannot be found in an empty graph. After adding the desired my_vertex, it is found.

Algorithm 198 Demonstration of the 'has_custom_vertex_with_my_vertex' function

```
#include <cassert>
#include <iostream>
#include "add custom vertex.h"
#include "create empty undirected custom vertices graph.h
#include "has custom vertex with my vertex.h"
#include "install vertex custom type.h"
#include "my custom vertex.h"
void has custom vertex with my custom vertex demo()
   noexcept
{
  {\bf auto} \ \ {\bf g} \ = \ {\bf create\_empty\_undirected\_custom\_vertices\_graph}
  assert (! has custom vertex with my custom vertex (
     my custom vertex("Felix"),g));
  add_custom_vertex(my_custom_vertex("Felix"),g);
  assert (has custom vertex with my_custom_vertex (
     my custom vertex("Felix"),g));
}
```

Note that this function only finds if there is at least one custom vertex with that my_vertex: it does not tell how many custom vertices with that my_vertex exist in the graph.

13.2 Find a custom vertex with a certain my vertex

Where STL functions work with iterators, here we obtain a vertex descriptor (see chapter 2.6) to obtain a handle to the desired vertex. Algorithm 199 shows how to obtain a vertex descriptor to the first vertex found with a specific my_vertex value.

Algorithm 199 Find the first vertex with a certain my vertex

```
#include <cassert>
\#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "has custom vertex with my vertex.h"
#include "install vertex custom type.h"
#include "my custom vertex.h"
template <typename graph>
typename boost::graph traits<graph>::vertex descriptor
find first custom vertex with my vertex (
  const my custom vertex& v,
  const graph& g
  noexcept
{
  assert (has custom vertex with my custom vertex (v, g));
  const auto my custom vertexes map = get(boost::
      vertex_custom_type, g);
  const auto vip
    = vertices (g); //not boost::vertices
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i) {
    const auto w
      = \gcd(\ //not\ boost::get
        my_custom_vertexes_map,
    \mathbf{if}(\mathbf{w} = \mathbf{v}) \ \{ \mathbf{return} \ *i; \}
  assert (!"Should_not_get_here");
  throw; // Will crash the program
```

With the vertex descriptor obtained, one can read and modify the vertex and the edges surrounding it. Algorithm 200 shows some examples of how to do so.

Algorithm 200 Demonstration of the 'find_first_custom_vertex_with_my_vertex' function

13.3 Get a custom vertex its my vertex

To obtain the name from a vertex descriptor, one needs to pull out the $my_vertexes^{12}$ map and then look up the vertex of interest.

 $^{^{12} \}mathtt{Bad}$ English intended: my_vertexes = multiple my_vertex objects, vertices = multiple graph nodes

Algorithm 201 Get a custom vertex its my_vertex from its vertex descriptor

To use 'get_custom_vertex_my_vertex', one first needs to obtain a vertex descriptor. Algorithm 202 shows a simple example.

Algorithm 202 Demonstration if the 'get_custom_vertex_my_vertex' function

13.4 Set a custom vertex its my vertex

If you know how to get the my_vertex from a vertex descriptor, setting it is just as easy, as shown in algorithm 203.

Algorithm 203 Set a custom vertex its my vertex from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "install_vertex_custom_type.h"
#include "my custom vertex.h"
\mathbf{template} \ < \!\! \mathbf{typename} \ \mathbf{graph} \!\! >
void set_custom_vertex_my_custom_vertex(
  const my_custom_vertex& v,
  const typename boost::graph traits<graph>::
      vertex descriptor& vd,
  graph& g
  noexcept
  static\_assert\;(!\,std::is\_const\!<\!graph\!>::value\;,
    "graph_cannot_be_const"
  );
  const auto my custom vertexes map
    = \gcd(\ //not\ boost::get
       boost::vertex_custom_type, g
    );
  my custom vertexes map[vd] = v;
```

To use 'set_vertex_my_vertex', one first needs to obtain a vertex descriptor. Algorithm 204 shows a simple example.

Algorithm 204 Demonstration if the 'set_custom_vertex_my_vertex' function

```
#include <cassert>
#include "add custom vertex.h"
#include "create_empty_undirected_custom_vertices_graph.h
#include "find_first_custom_vertex_with_my_vertex.h"
#include "get custom vertex my vertex.h"
#include "set custom vertex my vertex.h"
void set custom vertex my custom vertex demo() noexcept
{
  auto g
    = create empty undirected custom vertices graph();
  const my_custom_vertex old_vertex{"Dex"};
  add custom vertex (old vertex, g);
  const auto vd
    = find first custom vertex with my vertex (old vertex,
  assert (get custom vertex my custom vertex (vd,g)
    == old vertex
  );
  const my custom vertex new vertex{"Diggy"};
  set custom vertex my custom vertex (
    new vertex, vd, g
  );
  assert (get custom vertex my custom vertex (vd,g)
    == new_vertex
}
```

13.5 Setting all custom vertices' my vertex objects

When the vertices of a graph are associated with my_vertex objects, one can set these my_vertexes as such:

Algorithm 205 Setting the custom vertices' my_vertexes

```
#include < string>
#include < vector >
#include <boost/graph/graph traits.hpp>
\# \mathbf{include} < \mathbf{boost} / \mathbf{graph} / \mathbf{properties} . \mathbf{hpp} >
#include "install vertex custom type.h"
#include "my_custom_vertex.h"
template <typename graph>
{f void} set_custom_vertex_my_custom_vertexes(
  graph& g,
  const std::vector<my_custom_vertex>& my_custom_vertexes
  noexcept
{
  static assert (!std::is const<graph>::value, "graph_
      cannot_be_const");
  {\bf const\ auto\ my\_custom\_vertex\_map}
    = get( //not boost::get
      boost::vertex custom type, g
    );
  auto my_custom_vertexes_begin = std::begin(
      my_custom_vertexes);
  const auto my custom vertexes end = std::end(
     my custom vertexes);
  const auto vip = vertices (g); //not boost::vertices
  const auto j = vip.second;
  for (
    auto i = vip.first;
    i!=j; ++i,
    ++my_custom_vertexes begin
    assert (my custom vertexes begin !=
        my_custom_vertexes_end);
    put (my custom vertex map, *i,*
        my custom vertexes begin);
}
```

An impressive feature is that getting the property map holding the graph its names is not a copy, but a reference. Otherwise, modifying 'my vertexes map'

(obtained by non-reference) would only modify a copy.

13.6 Storing a graph with custom vertices as a .dot

If you used the create_custom_vertices_k2_graph function (algorithm 194) to produce a K_2 graph with vertices associated with my_vertex objects, you can store these my_vertexes additionally with algorithm 206:

Algorithm 206 Storing a graph with custom vertices as a .dot file

```
#include <fstream>
#include < string>
#include <boost/graph/graphviz.hpp>
#include <boost/graph/properties.hpp>
#include "get custom vertex my vertexes.h"
template <typename graph>
void save custom vertices graph to dot (
  const graph& g,
  const std::string& filename
  using my_custom_vertex_descriptor
   = typename graph::vertex descriptor;
  std::ofstream f(filename);
  {\bf const\ auto\ my\_custom\_vertexes\_map}
    = get( //not boost::get
      boost::vertex custom type,g
  boost::write graphviz(
    f,
    g,
    [my_custom_vertexes_map](
      std::ostream& out,
      const my custom vertex descriptor& v
      const my_custom_vertex m{my_custom_vertexes_map[v
      out << "[label=\"" << m << "\"]";
 );
}
```

13.7 Loading a directed graph with custom vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with custom vertices is loaded, as shown in algorithm 207:

Algorithm 207 Loading a directed graph with custom vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create empty directed custom vertices graph.h"
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
load directed custom vertices graph from dot (
  const std::string& dot filename
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g = create empty directed custom vertices graph();
  boost::dynamic_properties p; //\_do\_ default construct
  p.property("node id", get(boost::vertex custom type, g)
     );
  p.property("label", get(boost::vertex custom type, g));
  boost::read graphviz(f,g,p);
  return g;
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Next to this, a boost::dynamic_properties is created with its default constructor, after which we direct the boost::dynamic_properties to find a 'node_id' and 'label' in the vertex name map, 'edge_id' and 'label to the edge name map. From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

 $Algorithm\ 208\ shows\ how\ to\ use\ the\ 'load_directed_custom_vertices_graph_from_dot'\ function:$

Algorithm 208 Demonstration of the 'load_directed_custom_vertices_graph_from_dot' function

```
#include "create custom vertices markov chain.h"
#include "load directed custom_vertices_graph_from_dot.h"
#include "save_custom_vertices_graph_to_dot.h"
#include "get custom vertex my vertexes.h"
void load directed custom vertices graph from dot demo()
   noexcept
  using boost::num edges;
  using boost::num_vertices;
  const auto g
    = create_custom_vertices_markov_chain();
  const std::string filename{
    "create custom vertices markov chain.dot"
  };
  save custom vertices graph to dot(g, filename);
  const auto h
    = load directed custom vertices graph from dot(
       filename);
  assert(num\_edges(g) == num\_edges(h));
  assert (num vertices (g) == num vertices (h));
  assert (get custom vertex my vertexes (g)
    == get custom vertex my vertexes(h)
  );
}
```

This demonstration shows how the Markov chain is created using the 'create_custom_vertices_markov_chain' function (algorithm 191), saved and then loaded. The loaded graph is then checked to be identical to the original.

13.8 Loading an undirected graph with custom vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with custom vertices is loaded, as shown in algorithm 209:

 ${\bf Algorithm~209~Loading~an~undirected~graph~with~custom~vertices~from~a~.dot~file}$

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create_empty_undirected_custom_vertices_graph.h
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
load undirected custom vertices graph from dot (
  const std::string& dot filename
  assert(is_regular_file(dot_filename));
  std::ifstream f(dot_filename.c_str());
  auto g = create empty undirected custom vertices graph
     ();
  boost::dynamic_properties p; //_do_ default construct
  p.property("node_id", get(boost::vertex_custom_type, g)
  {\tt p.property("label", get(boost::vertex\_custom\_type, g));}\\
  boost::read graphviz(f,g,p);
  return g;
}
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 13.7 describes the rationale of this function

 $Algorithm\ 210\ shows\ how\ to\ use\ the\ 'load_undirected_custom_vertices_graph_from_dot' function:$

Algorithm 210 Demonstration of the 'load_undirected_custom_vertices_graph_from_dot' function

```
#include <cassert>
#include "create custom vertices k2 graph.h"
#include "load_undirected_custom_vertices_graph_from_dot.
   h "
#include "save custom vertices_graph_to_dot.h"
#include "get custom vertex my vertexes.h"
void load undirected custom vertices graph from dot demo
   () noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create custom vertices k2 graph();
  const std::string filename{
    "create custom vertices k2 graph.dot"
  save custom vertices graph to dot(g, filename);
  const auto h
    = load undirected custom vertices graph from dot(
       filename);
  assert(num edges(g) == num edges(h));
  assert (num vertices (g) == num vertices (h));
  assert (get_custom_vertex_my_vertexes(g) ==
     get custom vertex my vertexes(h));
}
```

This demonstration shows how K_2 with custom vertices is created using the 'create_custom_vertices_k2_graph' function (algorithm 194), saved and then loaded. The loaded graph is then checked to be identical to the original.

14 Building graphs with custom and selectable vertices

We have added one custom vertex property, here we add a second: if the vertex is selected.

- An empty directed graph that allows for custom and selectable vertices: see chapter 14.2
- An empty undirected graph that allows for custom and selectable vertices:

see chapter 14.3

- A two-state Markov chain with custom and selectable vertices: see chapter 14.5
- K_3 with custom and selectable vertices: see chapter 14.6

In the process, some basic (sometimes bordering trivial) functions are shown:

- Installing the new edge property: see chapter 14.1
- Adding a custom and selectable vertex: see chapter 14.4

These functions are mostly there for completion and showing which data types are used.

14.1 Installing the new is selected property

Installing a new property would have been easier, if 'more C++ compilers were standards conformant' ([8], chapter 3.6, footnote at page 52). Boost.Graph uses the BOOST INSTALL PROPERTY macro to allow using a custom property:

Algorithm 211 Installing the vertex is selected property

```
#include <boost/graph/properties.hpp>
namespace boost {
  enum vertex_is_selected_t { vertex_is_selected = 31416
     };
  BOOST_INSTALL_PROPERTY(vertex, is_selected);
}
```

The enum value 31415 must be unique.

14.2 Create an empty directed graph with custom and selectable vertices

Algorithm 212 Creating an empty directed graph with custom and selectable vertices

```
#include <boost/graph/adjacency list.hpp>
#include "install_vertex_custom_type.h"
#include "install vertex is selected.h"
#include "my_custom_vertex.h"
boost::adjacency list <
  boost::vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex custom type t, my custom vertex,
    boost::property<
      boost::vertex is selected t, bool
create empty directed custom and selectable vertices graph
   () noexcept
  return boost::adjacency list <
    boost :: vecS,
    boost :: vecS,
    boost::directedS,
    boost::property<
      boost::vertex custom type t, my custom vertex,
      boost::property<
        boost::vertex is selected t, bool
  >();
```

This code is very similar to the code described in chapter 12.3, except that there is a new, fourth template argument:

```
boost::property<boost::vertex_custom_type_t, my_custom_vertex,
   boost::property<boost::vertex_is_selected_t, bool,
>
```

This can be read as: "vertices have two properties: an associated custom type (of type my_custom_vertex) and an associated is_selected property (of type bool)".

Demo:

```
Algorithm
                213
                                                            cre-
                          Demonstration
                                                   the
ate empty directed custom and selectable vertices graph' function
#include "
   create\_empty\_directed\_custom\_and\_selectable\_vertices\_graph
    . h"
void
   create\_empty\_directed\_custom\_and\_selectable\_vertices\_graph\_demo
    () noexcept
  const auto g
        create empty directed custom and selectable vertices graph
  assert(boost::num edges(g) == 0);
  assert(boost::num\_vertices(g) == 0);
```

14.3 Create an empty undirected graph with custom and selectable vertices

Algorithm 214 Creating an empty undirected graph with custom and selectable vertices

```
#include <boost/graph/adjacency list.hpp>
#include "install_vertex_custom_type.h"
#include "install vertex is selected.h"
#include "my_custom_vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my custom vertex,
    boost::property<
      boost::vertex is selected t, bool
create empty undirected custom and selectable vertices graph
   () noexcept
  return boost::adjacency_list<
    boost :: vecS,
    boost :: vecS,
    boost::undirectedS,
    boost::property<
      boost::vertex custom type t, my custom vertex,
      boost::property<
        boost::vertex is selected t, bool
  >();
```

This code is very similar to the code described in chapter 14.2, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS). Demo:

```
Algorithm
                 215
                          Demonstration
                                                    the
                                                              'cre-
ate\_empty\_undirected\_custom\_and\_selectable\_vertices\_graph' function
#include "
   create\_empty\_undirected\_custom\_and\_selectable\_vertices\_graph
    . h"
void
   create_empty_undirected_custom_and_selectable_vertices_graph_demo
    () noexcept
  const auto g
        create\_empty\_undirected\_custom\_and\_selectable\_vertices\_graph
  assert(boost::num\_edges(g) == 0);
  assert(boost::num \ vertices(g) == 0);
```

14.4 Add a custom and selectable vertex

Adding a custom and selectable vertex is very similar to adding a custom vertex (chapter 12.5).

Algorithm 216 Add a custom and selectable vertex

```
#include <type traits>
#include <boost/graph/adjacency_list.hpp>
#include "install vertex custom type.h"
#include "install vertex is selected.h"
#include "my_custom_vertex.h"
template <typename graph>
\textbf{typename} \hspace{0.2cm} \textbf{boost} :: \texttt{graph\_traits} \negthinspace < \negthinspace \texttt{graph} \negthinspace > \negthinspace :: \texttt{vertex\_descriptor}
add custom and selectable vertex (
  const my custom vertex& v,
  const bool is selected,
  graph& g
  noexcept
{
  static assert (!std::is const<graph>::value,
     "graph_cannot_be_const"
  );
  const auto vd = boost::add_vertex(g);
  {\bf const\ auto\ my\_custom\_vertex\_map}
     = get( //not boost::get
       boost::vertex custom type,
       g
     );
  put(my_custom_vertex_map, vd, v);
  const auto is selected map
     = get( //not boost::get)
       boost::vertex is selected,
  put (is selected map, vd, is selected);
  return vd;
```

When having added a new (abstract) vertex to the graph, the vertex descriptor is used to set the my_custom_vertex and the selectedness in the graph its my_custom_vertex and is_selected map.

Here is the demo:

Algorithm 217 Demo of 'add custom and selectable vertex'

```
#include <cassert>
#include "add_custom_and_selectable_vertex.h"
#include "
   create empty directed custom and selectable vertices graph
   . h"
#include "
   create_empty_undirected_custom_and_selectable_vertices_graph
   . h"
void add custom and selectable vertex demo() noexcept
  auto g
       create empty directed custom and selectable vertices graph
       ();
  assert(boost::num \ vertices(g) == 0);
  assert(boost::num edges(g) == 0);
  add custom and selectable vertex (
    my_custom_vertex("X"),
    true,
    g
  );
  assert (boost::num vertices(g) == 1);
  assert(boost::num edges(g) == 0);
  auto h
       create empty undirected custom and selectable vertices graph
       ();
  assert(boost::num vertices(h) == 0);
  assert(boost::num edges(h) == 0);
  add custom and selectable vertex (
    my custom vertex ("X"),
    false,
    h
  );
  assert (boost::num vertices(h) == 1);
  assert(boost::num edges(h) == 0);
```

14.5 Creating a Markov-chain with custom and selectable vertices

14.5.1 Graph

Figure 37 shows the graph that will be reproduced:



Figure 37: A two-state Markov chain where the edges and vertices have custom properies. The edges' and vertices' properties are nonsensical

14.5.2 Function to create such a graph

Here is the code creating a two-state Markov chain with custom edges and vertices:

Algorithm 218 Creating the two-state Markov chain as depicted in figure 37

```
#include <cassert>
#include "
   create empty directed custom and selectable vertices graph
boost::adjacency list <
  boost::vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex_custom_type_t, my_custom_vertex,
    boost::property<
      boost::vertex is selected t, bool
 >
create custom and selectable vertices markov chain()
   noexcept
  auto g
        create empty directed custom and selectable vertices graph
  const auto vd_a = boost :: add_vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer aa.second);
  const auto aer ab = boost :: add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer_bb = boost::add_edge(vd_b, vd_b, g);
  assert (aer bb.second);
  auto my custom vertex map
    = get( //not boost::get
    boost::vertex custom type, g
  );
  put (my custom vertex map, vd a,
    my custom vertex ("Sunny", "Yellow_thing", 1.0, 2.0)
  put (my custom vertex map, vd b,
    \label{linear_relation} \verb|my_custom_vertex| ("Rainy", "Grey_things", 3.0, 4.0)
  auto is selected map
    = get( //not boost::get
    boost::vertex is selecte<sup>239</sup>, g
  put(is_selected_map, vd_a, true);
  put(is selected map, vd b, false);
  return g;
}
```

14.5.3 Creating such a graph

Here is the demo:

Algorithm 219 Demo of the 'create_custom_and_selectable_vertices_markov_chain' function (algorithm 218)

```
#include < cassert >
#include "
    create_custom_and_selectable_vertices_markov_chain.h"
#include "get_vertex_selectednesses.h"
void
    create\_custom\_and\_selectable\_vertices\_markov\_chain\_demo
    () noexcept
  const auto g
    = create_custom_and_selectable_vertices_markov_chain
         ();
  \mathbf{const} \ \mathrm{std} :: \mathrm{vector} \! < \! \mathbf{bool} \! >
    expected selectednesses {
    true, false
  const std::vector<bool>
    vertex selectednesses {
     get_vertex_selectednesses(g)
  assert (expected selectednesses
    == vertex selectednesses
```

14.5.4 The .dot file produced

```
Algorithm
                220
                         .dot
                                 file
                                         created
                                                    from
                                                              the
                                                                      'cre-
ate\_custom\_and\_selectable\_vertices\_markov\_chain' \quad function \quad (algorithm
218), converted from graph to .dot file using algorithm 48
digraph G {
O[label="Sunny, Yellow$$$SPACE$$$thing,1,1", regular="1"];
1[label="Rainy,Grey$$$SPACE$$$things,3,3", regular="0"];
0->0 ;
0->1;
1->0;
1->1;
```

14.5.5 The .svg file produced

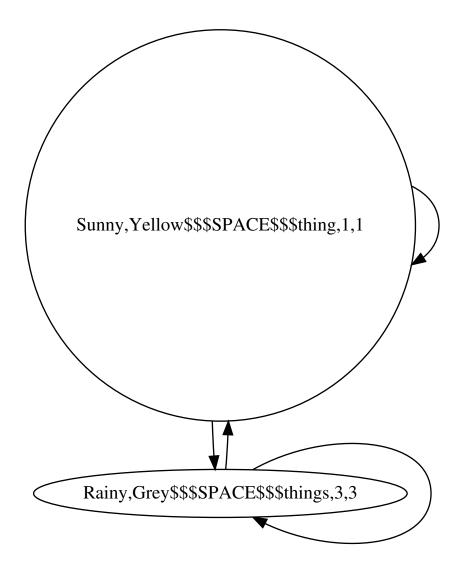


Figure 38: .svg file created from the 'create_custom_and_selectable_vertices_markov_chain' function (algorithm 191) its .dot file, converted from .dot file to .svg using algorithm 279

Note how the .svg changed it appearance due to the Graphviz 'regular' property (see chapter 25.2): the vertex labeled 'Sunny' is drawn according to the Graphviz 'regular' attribute, which makes it a circle. The other vertex, labeled 'Rainy' is not drawn as such and retained its ellipsoid appearance.

14.6 Creating K_2 with custom and selectable vertices

14.6.1 Graph

We reproduce the K_2 with custom vertices of chapter 12.8 , but now are vertices can be selected as well:

[graph here]

Algorithm 221 Creating K_3 as depicted in figure 24

```
#include "
   create empty undirected custom and selectable vertices graph
   . h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my custom vertex,
    boost::property<
      boost::vertex_is_selected_t, bool
>
create custom and selectable vertices k2 graph() noexcept
  auto g
       create empty undirected custom and selectable vertices graph
  const auto vd_a = boost::add_vertex(g);
  const auto vd_b = boost::add_vertex(g);
  const auto aer = boost::add edge(vd a, vd b, g);
  assert (aer.second);
  auto my custom vertexes map
    = get( //not boost::get)
    boost::vertex_custom_type,
    g
  );
  put (my custom vertexes map, vd a,
    my custom vertex ("A", "source", 0.0, 0.0)
  );
  put (my custom vertexes map, vd b,
    my custom vertex ("B", "target", 3.14, 3.14)
  );
  auto is selected map
    = get( //not boost::get)
    boost::vertex_is_selected,
    g
  );
  put(is_selected_map, vd_a<sub>24</sub>true);
  put(is_selected_map, vd_b, false);
  return g;
}
```

Most of the code is a slight modification of algorithm 194. In the end, the associated my_custom_vertex and is_selected properties are obtained as boost::property_maps and set with the desired my_custom_vertex objects and selectednesses.

14.6.3 Creating such a graph

Here is the demo:

```
Algorithm 222 Demo of the 'create custom and selectable vertices k2 graph'
function (algorithm 221)
#include <cassert>
#include "create custom and selectable vertices k2 graph.
                 h"
#include "has_custom_vertex_with_my_vertex.h"
void create custom and selectable vertices k2 graph demo
                  () noexcept
 {
          const auto g =
                           create custom and selectable vertices k2 graph();
            assert(boost::num edges(g) == 1);
            assert(boost::num \ vertices(g) == 2);
            assert \ (has\_custom\_vertex\_with\_my\_custom\_vertex \ (has\_custom\_vertex) \ (has\_custom\_
                    my_custom_vertex("A", "source",0.0, 0.0), g)
          );
            assert (has custom vertex with my custom vertex (
```

my custom vertex ("B", "target", 3.14, 3.14), g)

14.6.4 The .dot file produced

);

```
Algorithm 223 .dot file created from the 'create_custom_and_selectable_vertices_k2_graph' function (algorithm 221), converted from graph to .dot file using algorithm 48

graph G {
0[label="A,source,0,0", regular="1"];
1[label="B,target,3.14,3.14", regular="0"];
0--1;
}
```

14.6.5 The .svg file produced

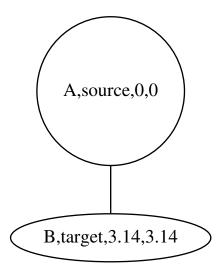


Figure 39: .svg file created from the 'create_custom_and_selectable_vertices_k2_graph' function (algorithm 191) its .dot file, converted from .dot file to .svg using algorithm 279

Note how the .svg changed it appearance due to the Graphviz 'regular' property (see chapter 25.2): the vertex labeled 'A' is drawn according to the Graphviz 'regular' attribute, which makes it a circle. The other vertex, labeled 'B' is not drawn as such and retained its ellipsoid appearance.

15 Working on graphs with custom and selectable vertices

This chapter shows some basic operations to do on graphs with custom and selectable vertices.

- Storing an directed/undirected graph with custom and selectable vertices as a .dot file: chapter 15.1
- \bullet Loading a directed graph with custom and selectable vertices from a .dot file: chapter 15.2
- \bullet Loading an undirected directed graph with custom and selectable vertices from a .dot file: chapter 15.3

15.1 Storing a graph with custom and selectable vertices as a .dot

If you used the 'create_custom_and_selectable_vertices_k2_graph' function (algorithm 221) to produce a K_2 graph with vertices associated with (1) my_custom_vertex objects, and (2) a boolean indicating its selectedness, you can store such graphs with algorithm 224:

 ${\bf Algorithm~224~Storing~a~graph~with~custom~and~selectable~vertices~as~a~.dot~file}$

```
#include <fstream>
#include < string>
#include <boost/graph/graphviz.hpp>
#include "install_vertex_custom_type.h"
#include "install vertex is selected.h"
#include "make custom and selectable vertices writer.h"
\#include "my custom vertex.\overline{h}"
template <typename graph>
void save_custom_and_selectable_vertices_graph_to_dot(
  const graph& g,
  const std::string& filename
  std::ofstream f(filename);
  write graphviz (f, g,
    make_custom_and_selectable vertices writer(
      get(boost::vertex_custom_type,g),
      get (boost::vertex is selected, g)
  );
}
```

This code looks small, because we call the 'make_custom_and_selectable_vertices_writer' function, which is shown in algorithm 225:

Algorithm 225 The 'make_custom_and_selectable_vertices_writer' function

```
template <
  typename my_custom_vertex_map,
  typename is_selected_map
inline custom and selectable vertices writer<
  my_custom_vertex_map,
  is selected map
make\_custom\_and\_selectable\_vertices\_writer (
  \mathbf{const} \ \mathrm{my\_custom\_vertex\_map} \& \ \mathrm{any\_my\_custom\_vertex\_map} \ ,
  const is selected map& any is selected map
{
  return custom and selectable vertices writer<</pre>
    my\_custom\_vertex\_map,
    is selected map
    any_my_custom_vertex_map,
    any_is_selected_map
  );
}
```

Also this function is forwarding the real work to the 'custom_ and _ selectable _ vertices _ writer', shown in algorithm 226:

```
#include <ostream>
template <
  typename my custom vertex map,
  typename is selected map
class custom and selectable vertices writer {
public:
  custom and selectable vertices writer (
    my custom vertex map any my custom vertex map,
    is selected map any is selected map
   : m my custom vertex map{any my custom vertex map},
      m is selected map { any is selected map }
  template <class vertex descriptor>
  void operator()(
    std::ostream& out,
    const vertex_descriptor& vd
  ) const noexcept {
    out << "[label=\"" << m my custom vertex map[vd]
      << "\", _ regular = \"" << m_is_selected_map[vd]</pre>
      << "\"]"
  }
private:
  my custom vertex map m my custom vertex map;
  is selected map m is selected map;
};
```

Here, some interesting things are happening: the writer needs both property maps to work with (that is, the 'my_custom_vertex' and is_selected maps). The 'my_custom_vertex' are written to the Graphviz 'label' attribute, and the is_selected is written to the 'regular' attribute (see chapter 25.2 for most Graphviz attributes).

15.2 Loading a directed graph with custom and selectable vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with custom and selectable vertices is loaded, as shown in algorithm 227:

Algorithm 227 Loading a directed graph with custom vertices from a .dot file

```
#include <fstream>
\# \mathbf{include} < \mathbf{boost} / \operatorname{graph} / \operatorname{graphviz} . hpp>
#include "
   create empty directed custom and selectable vertices graph
    . h"
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex_custom_type_t, my_custom_vertex,
    boost::property<
      boost::vertex is selected t, bool
  >
load_directed_custom_and_selectable_vertices_graph_from_dot
  const std::string& dot filename
  assert(is_regular_file(dot_filename));
  std::ifstream f(dot filename.c str());
  auto g =
     create empty directed custom and selectable vertices graph
  boost::dynamic_properties p; //_do_ default construct
  p.property("node id", get(boost::vertex custom type, g)
     );
  p.property("label", get(boost::vertex_custom_type, g));
  p.property("regular", get(boost::vertex is selected, g)
  boost::read graphviz(f,g,p);
  return g;
}
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Then, a boost::dynamic_properties is created with its default constructor, after which

• The Graphviz attribute 'node_id' (see chapter 25.2 for most Graphviz attributes) is connected to a vertex its 'my custom vertex' property

- The Graphviz attribute 'label' is connected to a vertex its 'my_custom_vertex' property
- The Graphviz attribute 'regular' is connected to a vertex its 'is_selected' vertex property

Algorithm 228 shows how to use the 'load_directed_custom_vertices_graph_from_dot' function:

Algorithm 228 Demonstration of the 'load_directed_custom_and_selectable_vertices_graph_from_dot' function

```
#include <cassert>
#include "
   create_custom_and_selectable vertices markov chain.h"
#include "is regular file.h"
#include "
   save custom and selectable vertices graph to dot.h"
void
   load directed custom and selectable vertices graph from dot demo
   () noexcept
  const auto g
    = create custom and selectable vertices markov chain
  const std::string filename{
    "create custom and selectable vertices markov chain.
       dot"
  };
  save custom and selectable vertices graph to dot (
    filename
  assert (is regular file (filename));
}
```

This demonstration shows how the Markov chain is created using the 'create_custom_vertices_markov_chain' function (algorithm 191), saved and then checked to exist.

15.3 Loading an undirected graph with custom and selectable vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with custom and selectable vertices is loaded, as shown in algorithm 229:

 ${\bf Algorithm~229~Loading~an~undirected~graph~with~custom~vertices~from~a~.dot~file}$

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create_empty_undirected_custom_and_selectable_vertices_graph
   . h"
#include "install vertex custom type.h"
#include "is regular file.h"
#include "my_custom_vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex_custom_type_t, my_custom_vertex,
    boost::property<
      boost::vertex is selected t, bool
load_undirected_custom_and_selectable_vertices_graph from dot
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g =
     create empty undirected custom and selectable vertices graph
  boost::dynamic_properties p; //_do_ default construct
  p.property("node_id", get(boost::vertex_custom_type, g)
  p.property("label", get(boost::vertex custom type, g));
  p.property("regular", get(boost::vertex_is_selected, g)
  boost::read_graphviz(f,g,p);
  return g;
}
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 15.2 describes the rationale of this func-

tion.

Algorithm 230 shows how to use the 'load_undirected_custom_vertices_graph_from_dot' function:

Algorithm 230 Demonstration of the 'load_undirected_custom_and_selectable_vertices_graph_from_dot function

```
#include <cassert>
#include "create custom and selectable vertices k2 graph.
#include "is regular file.h"
#include "
   save custom and selectable vertices graph to dot.h"
void
   load undirected custom and selectable vertices graph from dot demo
   () noexcept
{
  const auto g
    = create custom and selectable vertices k2 graph();
  const std::string filename{
    "create custom and selectable vertices k2 graph.dot"
  save\_custom\_and\_selectable\_vertices\_graph\_to\_dot(
    filename
  );
  assert (is regular file (filename));
```

This demonstration shows how K_2 with custom vertices is created using the 'create_custom_vertices_k2_graph' function (algorithm 194), saved and then checked to exist.

16 Building graphs with custom edges and vertices

Up until now, the graphs created have had edges and vertices with the built-in name propery. In this chapter, graphs will be created, in which the edges and vertices can have a custom 'my custom edge' and 'my custom edge' type¹³.

 \bullet An empty directed graph that allows for custom edges and vertices: see chapter 16.3

¹³I do not intend to be original in naming my data types

- ullet An empty undirected graph that allows for custom edges and vertices: see chapter 16.4
- \bullet A two-state Markov chain with custom edges and vertices: see chapter 16.7
- K_3 with custom edges and vertices: see chapter 16.8

In the process, some basic (sometimes bordering trivial) functions are shown:

- Creating the custom edge class: see chapter 16.1
- Installing the new edge property: see chapter 16.2
- Adding a custom edge: see chapter 16.5

These functions are mostly there for completion and showing which data types are used.

16.1 Creating the custom edge class

In this example, I create a custom edge class. Here I will show the header file of it, as the implementation of it is not important yet.

Algorithm 231 Declaration of my_custom_edge

```
#include < string>
#include <iosfwd>
class my custom edge
public:
  explicit my custom edge(
    const std::string& name = "",
    const std::string& description = "",
    const double width = 1.0,
    const double height = 1.0
  ) noexcept;
  const std::string& get_description() const noexcept;
  const std::string& get name() const noexcept;
  double get_width() const noexcept;
  double get height() const noexcept;
  private:
  std::string m name;
  std::string m description;
  double m width;
  double m height;
};
bool operator == (const my custom edge& lhs, const
   my custom edge& rhs) noexcept;
bool operator!=(const my custom edge& lhs, const
   my custom edge& rhs) noexcept;
std::ostream& operator<<(std::ostream& os, const
   my custom edge& v) noexcept;
std::istream& operator>>(std::istream& os, my custom edge
   & v) noexcept;
```

my_custom_edge is a class that has multiple properties: two doubles 'm_width' ('m_' stands for member) and 'm_height', and two std::strings m_name and m_description. 'my_custom_edge' is copyable, but cannot trivially be converted to a std::string.' 'my_custom_edge' is comparable for equality (that is, operator== is defined).

Special characters like comma's, quotes and whitespace cannot be streamed without problems. The function 'graphviz_encode' (algorithm 276) can convert the elements to be streamed to a Graphviz-friendly version, which can be decoded by 'graphviz' decode' (algorithm 277).

16.2 Installing the new edge property

Installing a new property would have been easier, if 'more C++ compilers were standards conformant' ([8], chapter 3.6, footnote at page 52). Boost.Graph uses the BOOST_INSTALL_PROPERTY macro to allow using a custom property:

Algorithm 232 Installing the edge custom type property

```
#include <boost/graph/properties.hpp>
namespace boost {
  enum edge_custom_type_t { edge_custom_type = 3142 };
  BOOST_INSTALL_PROPERTY(edge, custom_type);
}
```

The enum value 3142 must be unique.

16.3 Create an empty directed graph with custom edges and vertices

 ${\bf Algorithm~233~Creating~an~empty~directed~graph~with~custom~edges~and~vertices}$

```
#include <boost/graph/adjacency list.hpp>
#include "install_edge_custom_type.h"
#include "install vertex custom type.h"
#include "my custom edge.h"
#include "my custom vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
  boost::property<
    boost::edge custom type t, my custom edge
create empty directed custom edges and vertices graph()
   noexcept
  return boost::adjacency list <
    boost :: vecS,
    boost :: vecS,
    boost :: directedS,
    boost::property<
      boost::vertex custom type t, my custom vertex
    boost::property<
      boost::edge custom type t, my custom edge
  >();
}
```

This code is very similar to the code described in chapter 12.3, except that there is a new, fifth template argument:

```
boost::property<br/>boost::edge custom type t, my edge>
```

This can be read as: "edges have the property 'boost::edge_custom_type_t', which is of data type 'my_custom_edge''. Or simply: "edges have a custom

 $\begin{array}{c} \text{type called } \text{my_custom_edge"}. \\ \text{Demo:} \end{array}$

```
Algorithm
                 234
                           Demonstration
                                                       the
                                                                 'cre-
ate\_empty\_directed\_custom\_edges\_and\_vertices\_graph' function
#include "
    create\_empty\_directed\_custom\_edges\_and\_vertices\_graph\,.
\mathbf{void}
    create\_empty\_directed\_custom\_edges\_and\_vertices\_graph\_demo
    () noexcept
{
  const auto g =
      create\_empty\_directed\_custom\_edges\_and\_vertices\_graph
  assert(boost::num\_edges(g) == 0);
  assert (boost :: num_vertices (g) = 0);
```

16.4 Create an empty undirected graph with custom edges and vertices

Algorithm 235 Creating an empty undirected graph with custom edges and vertices

```
#include <boost/graph/adjacency list.hpp>
#include "install_edge_custom_type.h"
#include "install vertex custom type.h"
#include "my custom vertex.h"
#include "my custom edge.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost:: vertex \quad custom\_type\_t \;, \quad my\_custom\_vertex
  >,
  boost::property<
    boost::edge_custom_type_t, my_custom_edge
create empty undirected custom edges and vertices graph()
    noexcept
{
  return boost::adjacency list <
    boost :: vecS,
    boost :: vecS,
    boost :: undirected S ,
    boost::property<
      boost::vertex_custom_type_t, my_custom_vertex
    boost::property<
      boost::edge custom type t, my custom edge
  >();
```

This code is very similar to the code described in chapter 16.3, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS). Demo:

```
Algorithm
                236
                          Demonstration
                                                   the
                                                            'cre-
ate_empty_undirected_custom_edges_and_vertices_graph' function
#include <cassert>
#include "
   create_empty_undirected_custom_edges_and_vertices_graph
void
   create\_empty\_undirected\_custom\_edges\_and\_vertices\_graph\_demo
    () noexcept
  const auto g
        create\_empty\_undirected\_custom\_edges\_and\_vertices\_graph
  assert(boost::num edges(g) == 0);
  assert (boost::num vertices(g) == 0);
```

16.5 Add a custom edge

Adding a custom edge is very similar to adding a named edge (chapter 6.3).

Algorithm 237 Add a custom edge

```
#include < cassert >
#include <boost/graph/adjacency_list.hpp>
#include "install edge custom type.h"
#include "my custom edge.h"
template <typename graph>
typename boost::graph traits<graph>::edge descriptor
add custom edge (
  const my custom edge& v,
  graph& g
 noexcept
{
  static_assert(!std::is_const<graph>::value, "graph_
     cannot_be_const");
  const auto vd a = boost::add vertex(g);
  const auto vd_b = boost::add_vertex(g);
  const auto aer
    = boost::add edge(vd a, vd b, g);
  assert (aer.second);
  const auto my edge map
    = get( //not boost::get
      boost::edge custom type, g
    );
  put(my edge map, aer.first, v);
  return aer.first;
```

When having added a new (abstract) edge to the graph, the edge descriptor is used to set the my_edge in the graph its my_custom_edge map (using 'get(boost::edge_custom_type,g)').

Here is the demo:

Algorithm 238 Demo of 'add custom edge'

```
#include < cassert >
#include "add custom edge.h"
#include "
   create empty directed custom edges and vertices graph.
   h "
#include "
   create_empty_undirected_custom_edges_and_vertices_graph
   . h"
void add custom edge demo() noexcept
  auto g =
     create\_empty\_directed\_custom\_edges\_and\_vertices\_graph
  add custom edge(my custom edge("X"), g);
  assert(boost::num\_vertices(g) == 2);
  assert(boost::num edges(g) == 1);
  auto h =
     create_empty_undirected_custom_edges_and_vertices_graph
  add custom edge(my custom edge("Y"), h);
  assert (boost::num vertices(h) == 2);
  assert(boost::num edges(h) == 1);
```

16.6 Getting the custom edges my edges

When the edges of a graph have an associated 'my_custom_edge', one can extract these all as such:

Algorithm 239 Get the edges' my_custom_edges

```
#include < vector>
#include <boost/graph/adjacency_list.hpp>
#include "install_edge_custom_type.h"
#include "my custom edge.h"
template <typename graph>
std::vector<my custom edge> get custom edge my edges(
  const graph& g
 noexcept
{
  std::vector<my custom edge> v;
  v.reserve(boost::num edges(g));
  const auto my custom edges map
    = get( //not boost::get
      boost::edge custom type,g
    );
  const auto eip
    = \operatorname{edges}(g); //not boost:: edges
  const auto j = eip.second;
  for (auto i = eip.first; i!=j; ++i) {
    v.emplace back(
      get( //not \ boost::get
        my_custom_edges_map, *i
    );
  return v;
}
```

The 'my_custom_edge' object associated with the edges are obtained from a boost::property map and then put into a std::vector.

Note: the order of the my_custom_edge objects may be different after saving and loading.

When trying to get the edges' my_custom_edge objects from a graph without custom edges objects associated, you will get the error 'formed reference to void' (see chapter 24.1).

16.7 Creating a Markov-chain with custom edges and vertices

16.7.1 Graph

Figure 40 shows the graph that will be reproduced:

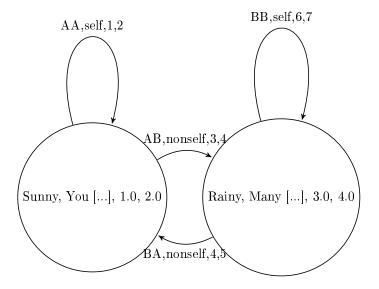


Figure 40: A two-state Markov chain where the edges and vertices have custom properies. The edges' and vertices' properties are nonsensical

16.7.2 Function to create such a graph

Here is the code creating a two-state Markov chain with custom edges and vertices:

```
#include <cassert>
#include "
    create empty directed custom edges and vertices graph.
boost::adjacency list <
  boost::vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
  boost::property<
    boost::edge_custom_type_t, my_custom_edge
create_custom_edges_and_vertices_markov_chain() noexcept
{
  auto g
        create empty directed custom edges and vertices graph
        ();
  const auto vd a = boost :: add vertex(g);
  const \ auto \ vd \ b = boost :: add_vertex(g);
  {f const\ auto}\ {f aer\_aa}\ =\ {f boost}:: {f add\_edge}\left({f vd\_a},\ {f vd\_a},\ {f g}\right);
  assert (aer aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer bb = boost::add edge(vd b, vd b, g);
  assert (aer bb.second);
  {\bf auto} \ {\tt my\_custom\_vertexes\_map} \ = \ {\tt get} \left( \ \ /\!/ \, not \ \ b \, oost :: g \, et \right.
    boost::vertex custom type, g
  );
  put (my custom vertexes map, vd a,
    my custom vertex ("Sunny", "Yellow_thing", 1.0, 2.0)
  put (my_custom_vertexes_map, vd_b,
    my_custom_vertex("Rainy","Grey_things",3.0,4.0)
  auto my edges map = get ( //not \ boost :: get)
    boost::edge custom type,g
  put (my_edges_map, aer aa. 265st.
    my_custom_edge("Sometimes","20%",1.0,2.0)
  put (my edges map, aer ab. first
    my_custom_edge("Often","80%",3.0,4.0)
  put (my_edges_map, aer_ba.first,
    my\_custom\_edge("Rarely","10\%",5.0,6.0)
```

16.7.3 Creating such a graph

Here is the demo:

);

```
Algorithm 241 Demo of the 'create custom edges and vertices markov chain'
function (algorithm 240)
#include <cassert>
#include "create custom edges and vertices markov chain.h
#include "get custom vertex my vertexes.h"
#include "install vertex custom type.h"
#include "my custom vertex.h"
void create custom edges and vertices markov chain demo()
    noexcept
  const auto g
    = create custom edges and vertices markov chain();
  const std::vector<my_custom_vertex>
    expected my custom vertexes {
    my\_custom\_vertex("Sunny",
      "Yellow_thing", 1.0, 2.0
    my custom vertex ("Rainy",
      "Grey_things", 3.0, 4.0
  };
  const std::vector<my custom vertex>
    vertex_my_custom_vertexes{
    get_custom_vertex_my_vertexes(g)
  };
```

assert (expected my_custom_vertexes == vertex_my_custom_vertexes

16.7.4 The .dot file produced

```
Algorithm
                242
                                file
                        .dot
                                                  from
                                                           the
                                                                   cre-
                                       created
ate_custom_edges_and_vertices_markov_chain' function (algorithm 240),
converted from graph to .dot file using algorithm 48
digraph G {
O[label="Sunny, Yellow$$$SPACE$$$thing, 1, 1"];
1[label="Rainy,Grey$$$SPACE$$$things,3,3"];
0->0 [label="Sometimes,20%,1,2"];
0->1 [label="Often,80%,3,4"];
1->0 [label="Rarely,10%,5,6"];
1->1 [label="Mostly,90%,7,8"];
```

16.7.5 The .svg file produced

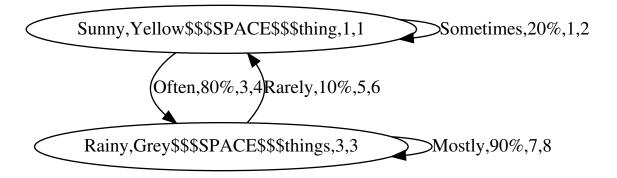


Figure 41: .svg file created from the 'create_custom_edges_and_vertices_markov_chain' function (algorithm 191) its .dot file, converted from .dot file to .svg using algorithm 279

16.8 Creating K_3 with custom edges and vertices

Instead of using edges with a name, or other properties, here we use a custom edge class called 'my_custom_edge'.

16.8.1 Graph

We reproduce the K_3 with named edges and vertices of chapter 6.6, but with our custom edges and vertices intead:

[graph here]

Algorithm 243 Creating K_3 as depicted in figure 24

```
#include "
   create empty undirected custom edges and vertices graph
    . h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
  >,
  boost::property<
    boost::edge_custom_type_t, my_custom_edge
create custom edges and vertices k3 graph() noexcept
  auto g
        create empty undirected custom edges and vertices graph
  const auto vd_a = boost::add_vertex(g);
  const \ auto \ vd_b = boost :: add_vertex(g);
  const auto vd c = boost :: add <math>vertex(g);
  const auto aer a = boost::add edge(vd a, vd b, g);
  {f const\ auto}\ {f aer\_b}\ =\ {f boost}:: {f add\_edge}({f vd\_b},\ {f vd\_c},\ {f g}) \; ;
  const auto aer c = boost :: add edge(vd c, vd a, g);
  assert (aer a.second);
  assert (aer b.second);
  assert (aer_c.second);
  auto my_custom_vertex_map
    = get( //not boost::get
      boost::vertex_custom_type,g
  put (my custom vertex map, vd a,
    my\_custom\_vertex("top","source",0.0,0.0)
  put (my custom vertex map, vd b,
    my_custom_vertex("right","target",3.14,0)
  );
  put (my custom vertex map, vd c,
    my custom vertex ("left", "target", 0, 3.14)
  );
  auto my_edge_map = get(boost::edge_custom_type,g);
  put (my_edge_map, aer_a.first,
    my custom edge("AB", "first", 0.0, 0.0)
  put (my edge map, aer b. first,
    my_custom_edge("BC", "second", 3.14, 3.14)
```

Most of the code is a slight modification of algorithm 109. In the end, the my_edges and my_vertices are obtained as a boost::property_map and set with the 'my_custom_edge' and 'my_custom_vertex' objects.

16.8.3 Creating such a graph

Here is the demo:

Algorithm 244 Demo of the 'create_custom_edges_and_vertices_k3_graph' function (algorithm 243)

16.8.4 The .dot file produced

```
graph G {
0[label="top,source,0,0"];
1[label="right,target,3.14,3.14"];
2[label="left,target,0,0"];
0--1 [label="AB,first,0,0"];
1--2 [label="BC,second,3.14,3.14"];
2--0 [label="CA,third,3.14,3.14"];
}
```

16.8.5 The .svg file produced

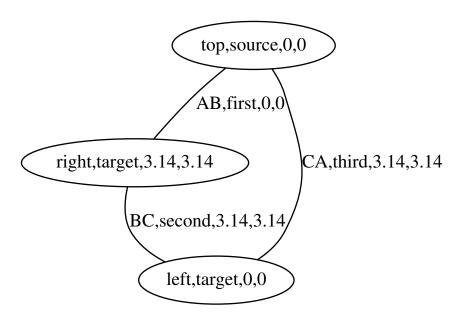


Figure 42: .svg file created from the 'create_custom_edges_and_vertices_k3_graph' function (algorithm 191) its .dot file, converted from .dot file to .svg using algorithm 279

17 Working on graphs with custom edges and vertices

17.1 Has a my_custom_edge

Before modifying our edges, let's first determine if we can find an edge by its custom type ('my_custom_edge') in a graph. After obtaing a my_custom_edge map, we obtain the edge iterators, dereference these to obtain the edge descriptors and then compare each edge its my_custom_edge with the one desired.

Algorithm 246 Find if there is a custom edge with a certain my custom edge

```
\# \mathbf{include} < \mathbf{boost} / \mathbf{graph} / \mathbf{properties} . \mathbf{hpp} >
#include "install_edge_custom_type.h"
#include "my_custom_edge.h"
template <typename graph>
bool has_custom_edge_with_my_edge(
  const my_custom_edge& e,
  const graph& g
 noexcept
  const auto my edges map
    = get(boost::edge custom type,g);
  const auto eip
    = \operatorname{edges}(g); //not boost:: edges
  const auto j = eip.second;
  for (auto i = eip.first; i!=j; ++i) {
    if (
       get( //not \ boost::get
         my_edges_map,
         * i
       = e 
       return true;
  return false;
```

This function can be demonstrated as in algorithm 247, where a certain 'my_custom_edge' cannot be found in an empty graph. After adding the desired my_custom_edge, it is found.

Algorithm 247 Demonstration of the 'has_custom_edge_with_my_edge' function

```
#include <cassert>
#include "add custom edge.h"
#include "
   create_empty_undirected_custom_edges_and_vertices_graph
   . h"
#include "has_custom_edge with my edge.h"
void has_custom_edge_with_my_edge_demo() noexcept
{
  auto g
       create empty undirected custom edges and vertices graph
  assert (
    !has custom edge with my edge(
      my custom edge("Edward"),g
  );
  add custom edge(my custom edge("Edward"),g);
  assert (
    has_custom_edge_with_my_edge(
      my custom edge("Edward"),g
  );
}
```

Note that this function only finds if there is at least one edge with that my_custom_edge: it does not tell how many edges with that my_custom_edge exist in the graph.

17.2 Find a my custom edge

Where STL functions work with iterators, here we obtain an edge descriptor (see chapter 2.12) to obtain a handle to the desired edge. Algorithm 248 shows how to obtain an edge descriptor to the first edge found with a specific my custom edge value.

Algorithm 248 Find the first custom edge with a certain my custom edge

```
#include <cassert>
#include <boost/graph/graph_traits.hpp>
#include "has custom edge with my edge.h"
#include "install edge custom type.h"
#include "my custom edge.h"
template <typename graph>
typename boost::graph_traits<graph>::edge_descriptor
find_first_custom_edge_with_my_edge(
  const my custom edge& e,
  const graph& g
 noexcept
  assert (has custom edge with my edge (e, g));
  const auto my edges map = get (boost :: edge custom type,
  const auto eip = edges(g); //not boost::edges
  const auto j = eip.second;
  for (auto i = eip.first; i!=j; ++i) {
      get ( //not boost :: get
        my_edges_map,
        * i
      ) == e) {
      return *i;
    }
  assert (!"Should_not_get_here");
  throw; // Will crash the program
}
```

With the edge descriptor obtained, one can read and modify the edge and the vertices surrounding it. Algorithm 249 shows some examples of how to do so.

Algorithm 249 Demonstration of the 'find_first_custom_edge_with_my_edge' function

17.3 Get an edge its my_custom_edge

To obtain the my_edeg from an edge descriptor, one needs to pull out the my_custom_edges map and then look up the my_edge of interest.

Algorithm 250 Get a vertex its my custom vertex from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include "install_edge_custom_type.h"
#include "my_custom_edge.h"
template <typename graph>
my_custom_edge_get_custom_edge_my_edge(
  const typename boost::graph_traits<graph>::
      edge_descriptor& vd,
  const graph& g
) noexcept
  const auto my edge map
    = \gcd(\ //\mathit{not}\ boost::get
      boost::edge custom type,
      g
    );
  return my_edge_map[vd];
}
```

To use 'get_custom_edge_my_custom_edge', one first needs to obtain an edge descriptor. Algorithm 251 shows a simple example.

Algorithm 251 Demonstration if the 'get custom edge my edge' function

17.4 Set an edge its my_custom_edge

If you know how to get the my_custom_edge from an edge descriptor, setting it is just as easy, as shown in algorithm 252.

Algorithm 252 Set a custom edge its my_custom_edge from its edge descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "install_edge_custom_type.h"
#include "my_custom_edge.h"
template <typename graph>
void set custom edge my edge (
  const my_custom_edge& name,
  const typename boost::graph traits<graph>::
     edge descriptor& vd,
  graph& g
  noexcept
  static_assert(!std::is_const<graph>::value, "graph_
     cannot_be_const");
  auto my edge map = get(boost::edge custom type, g);
  my edge map[vd] = name;
}
```

To use 'set_custom_edge_my_edge', one first needs to obtain an edge descriptor. Algorithm 253 shows a simple example.

Algorithm 253 Demonstration if the 'set custom edge my edge' function

```
#include <cassert>
#include "add custom edge.h"
#include "
   create empty undirected custom edges and vertices graph
   . h"
#include "find first custom edge with my edge.h"
#include "get custom edge my edge.h"
#include "set custom edge my edge.h"
void set custom edge my edge demo() noexcept
  auto g
       create empty undirected custom edges and vertices graph
  const my custom edge old edge{"Dex"};
  add custom edge(old edge, g);
  {f const} auto {f vd}
    = find_first_custom_edge_with_my_edge(old_edge,g);
  assert (get custom edge my edge (vd,g)
   = old edge
  );
  const my custom edge new edge{"Diggy"};
  set_custom_edge_my_edge(new_edge, vd, g);
  assert (get custom edge my edge (vd,g)
    == new edge
  );
}
```

17.5 Storing a graph with custom edges and vertices as a .dot

If you used the create_custom_edges_and_vertices_k3_graph function (algorithm 243) to produce a K_3 graph with edges and vertices associated with my_custom_edge and my_custom_vertex objects, you can store these my_custom_edges and my_custom_vertex-es additionally with algorithm 254:

Algorithm 254 Storing a graph with custom edges and vertices as a .dot file

```
#include <fstream>
#include < string>
#include <boost/graph/graphviz.hpp>
#include <boost/graph/properties.hpp>
#include "get custom edge my edge.h"
#include "get custom vertex my vertexes.h"
template <typename graph>
void save custom edges and vertices graph to dot (
  const graph& g,
  const std::string& filename
{
  using my_vertex_descriptor = typename graph::
      vertex descriptor;
  using my edge descriptor = typename graph::
      edge descriptor;
  std::ofstream f(filename);
  const auto my_custom_vertexes =
      get custom vertex my vertexes(g);
  boost::write graphviz(
    f,
    g,
    [my custom vertexes](
       std::ostream& out,
       const my vertex descriptor& v
      \mathbf{const} \ \mathrm{my\_custom\_vertex} \ \mathrm{mfmy\_custom} \ \mathrm{vertexes} \left[ \left. \mathrm{v} \right| \right\};
       out << "[label=\"" << m << "\"]";
    [g](std::ostream& out,
        const my_edge_descriptor& e
       const my custom edge m{get custom edge my edge(e,g)
      out << "[label=\"" << m << "\"]";
    }
  );
}
```

17.6 Load a directed graph with custom edges and vertices from a .dot file

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with custom edges and vertices is loaded, as shown in algorithm 255:

Algorithm 255 Loading a directed graph with custom edges and vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create empty directed custom edges and vertices graph.
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex custom_type_t, my_custom_vertex
  >,
  boost::property<
    boost::edge custom type t, my custom edge
load directed custom edges and vertices_graph_from_dot(
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g =
     create empty directed custom edges and vertices graph
     ();
  boost::dynamic_properties p; //_do_ default construct
  p.property("node id", get(boost::vertex custom type, g)
     );
  p.property("label", get(boost::vertex_custom_type, g));
  p.property("edge_id", get(boost::edge_custom_type, g));
  {\tt p.property("label", get(boost::edge\_custom\_type, g));}\\
  boost::read graphviz(f,g,p);
  return g;
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Next to this, a boost::dynamic_properties is created with its default constructor, after which we direct the boost::dynamic_properties to find a 'node_id' and 'label' in the vertex name map, 'edge_id' and 'label to the edge name map. From this and the empty graph, 'boost::read graphviz' is

called to build up the graph.

 $Algorithm\ 256\ shows\ how\ to\ use\ the\ 'load_directed_custom_edges_and_vertices_graph_from_dot'\ function:$

Algorithm 256 Demonstration of the 'load_directed_custom_edges_and_vertices_graph_from_dot' function

```
#include "create_custom_edges_and_vertices_markov_chain.h
#include "get custom vertex my vertexes.h"
#include "
   load directed custom edges and vertices graph from dot
    . h"
#include "save custom edges and vertices graph to dot.h"
void
   load directed custom edges and vertices graph from dot demo
   () noexcept
{
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create custom edges and vertices markov chain();
  const std::string filename{
    "create custom edges and vertices markov chain.dot"
  };
  save custom edges and vertices graph to dot(g, filename
     );
  const auto h
       load directed custom edges and vertices graph from dot
      filename
    );
  assert(num\_edges(g) == num\_edges(h));
  assert(num\_vertices(g) == num\_vertices(h));
  assert (get custom vertex my vertexes (g)
    == get custom vertex my vertexes(h)
  );
}
```

This demonstration shows how the Markov chain is created using the 'create_custom_edges_and_vertices_markov_chain' function (algorithm 240), saved and then loaded.

17.7 Load an undirected graph with custom edges and vertices from a .dot file

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with custom edges and vertices is loaded, as shown in algorithm 257:

 ${\bf Algorithm~257}$ Loading an undirected graph with custom edges and vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create empty undirected custom edges and vertices graph
    . h"
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom_type_t, my_custom_vertex
  >,
  boost::property<
    boost::edge custom type t, my custom edge
load undirected custom edges and vertices graph from dot (
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g =
     create empty undirected custom edges and vertices graph
      ();
  \verb|boost|:: \verb|dynamic_properties|| p; //\_do\_|| \textit{default}|| \textit{construct}||
  p.property("node id", get(boost::vertex custom type, g)
     );
  {\tt p.property("label", get(boost::vertex\_custom\_type, g));}\\
  p.property("edge_id", get(boost::edge_custom_type, g));
  {\tt p.property("label", get(boost::edge\_custom\_type, g));}\\
  boost::read graphviz(f,g,p);
  return g;
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 17.6 describes the rationale of this function.

 $Algorithm\ 258\ shows\ how\ to\ use\ the\ 'load_undirected_custom_vertices_graph_from_dot'\ function:$

Algorithm 258 Demonstration of the 'load_undirected_custom_edges_and_vertices_graph_from_dot' function

```
#include "create custom edges and vertices k3 graph.h"
#include "
   load undirected custom edges and vertices graph from dot
   . h"
#include "save custom edges and vertices graph to dot.h"
#include "get custom vertex my vertexes.h"
void
   load undirected custom edges and vertices graph from dot demo
   () noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create custom edges and vertices k3 graph();
  const std::string filename{
    "create custom edges and vertices k3 graph.dot"
  save_custom_edges_and_vertices_graph_to_dot(g, filename
     );
  const auto h
       load undirected custom edges and vertices graph from dot
       (filename);
  assert(num edges(g) == num edges(h));
  assert (num vertices (g) == num vertices (h));
  assert (get custom vertex my vertexes (g) ==
     get custom vertex my vertexes(h));
}
```

This demonstration shows how K_2 with custom vertices is created using the 'create_custom_vertices_k2_graph' function (algorithm 194), saved and then loaded. The loaded graph is checked to be a graph similar to the original.

18 Building graphs with a graph name

Up until now, the graphs created have had no properties themselves. Sure, the edges and vertices have had properties, but the graph itself has had none. Until now.

In this chapter, graphs will be created with a graph name of type std::string

- An empty directed graph with a graph name: see chapter
- An empty undirected graph with a graph name: see chapter
- A two-state Markov chain with a graph name: see chapter
- K_3 with a graph name: see chapter

In the process, some basic (sometimes bordering trivial) functions are shown:

- Getting a graph its name: see chapter
- Setting a graph its name: see chapter

18.1 Create an empty directed graph with a graph name property

Algorithm 259 shows the function to create an empty directed graph with a graph name.

Algorithm 259 Creating an empty directed graph with a graph name

```
#include <boost/graph/adjacency list.hpp>
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::no property,
  boost::no_property ,
  boost::property<
    boost::graph name t, std::string
create empty directed graph with graph name() noexcept
  return boost::adjacency list<
    boost :: vecS,
    boost :: vecS,
    boost::directedS,
    boost::no property,
    boost::no property,
    boost::property<
      boost::graph name t, std::string
  >();
}
```

This boost::adjacency list is of the following type:

- the first 'boost::vecS': select (that is what the 'S' means) that out edges are stored in a std::vector. This is the default way.
- the second 'boost::vecS': select that the graph vertices are stored in a std::vector. This is the default way.
- 'boost::directedS': select that the graph is directed. This is the default selectedness
- the first 'boost::no_property': the vertices have no properties. This is the default (non-)property
- the second 'boost::no_property': the vertices have no properties. This is the default (non-)propert
- 'boost::property
boost::graph_name_t, std::string>': the graph itself has a single property: its boost::graph_name has type std::string

Algorithm 260 demonstrates the 'create_empty_directed_graph_with_graph_name' function.

Algorithm 260 Demonstration of 'create empty directed graph with graph name'

18.2 Create an empty undirected graph with a graph name property

assert (boost :: num_edges(g) == 0); assert (boost :: num_vertices(g) == 0);

Algorithm 261 shows the function to create an empty undirected graph with a graph name.

Algorithm 261 Creating an empty undirected graph with a graph name

```
#include <boost/graph/adjacency_list.hpp>
boost:: adjacency\_list <
  boost::vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::no_property,
  boost::no_property ,
  boost::property<
    boost::graph name t, std::string
>
create_empty_undirected_graph_with_graph_name() noexcept
  return boost::adjacency list<
    boost :: vecS,
    boost :: vecS,
    boost::undirectedS,
    boost::no_property ,
    boost::no_property ,
    boost::property<
      boost::graph_name_t, std::string
  >();
}
```

This code is very similar to the code described in chapter 259, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS).

Algorithm 262 demonstrates the 'create_empty_undirected_graph_with_graph_name' function.

18.3 Get a graph its name property

Algorithm 263 Get a graph its name

```
#include <string>
#include <boost/graph/properties.hpp>

template <typename graph>
std::string get_graph_name(
    const graph& g
) noexcept
{
    return
        get_property( //not boost::get_property
            g, boost::graph_name
        );
}
```

Algorithm 264 demonstrates the 'get graph name' function.

Algorithm 264 Demonstration of 'get graph name'

```
#include <cassert>
#include "create_empty_directed_graph_with_graph_name.h"
#include "get_graph_name.h"
#include "set_graph_name.h"

void get_graph_name_demo() noexcept
{
   auto g = create_empty_directed_graph_with_graph_name();
   const std::string name{"Dex"};
   set_graph_name(name, g);
   assert(get_graph_name(g) == name);
}
```

18.4 Set a graph its name property

Algorithm 265 Set a graph its name

Algorithm 266 demonstrates the 'set graph name' function.

Algorithm 266 Demonstration of 'set graph name'

```
#include <cassert>
#include "create_empty_directed_graph_with_graph_name.h"
#include "get_graph_name.h"
#include "set_graph_name.h"

void set_graph_name_demo() noexcept
{
   auto g = create_empty_directed_graph_with_graph_name();
   const std::string name{"Dex"};
   set_graph_name(name, g);
   assert(get_graph_name(g) == name);
}
```

18.5 Create a directed graph with a graph name property

18.5.1 Graph

See figure 6.

18.5.2 Function to create such a graph

Algorithm 267 shows the function to create an empty directed graph with a graph name.

Algorithm 267 Creating a two-state Markov chain with a graph name

```
#include <cassert>
#include "create_empty_directed_graph_with_graph_name.h"
#include "set graph name.h"
boost::adjacency list <
  boost::vecS,
  boost :: vecS,
  boost::directedS,
  boost::no property,
  boost::no_property ,
  boost::property<boost::graph name t, std::string>
create markov chain with graph name() noexcept
  auto g = create empty directed graph with graph name();
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer_aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer bb = boost::add edge(vd b, vd b, g);
  assert (aer bb.second);
  set graph name("Two-state_Markov_chain", g);
  return g;
}
```

18.5.3 Creating such a graph

Algorithm 268 demonstrates the 'create_markov_chain_with_graph_name' function.

#include <cassert> #include "create_markov_chain_with_graph_name.h" #include "create_markov_chain_with_graph_name.h" #include "get_graph_name.h" void create_markov_chain_with_graph_name_demo() noexcept { const auto g = create_markov_chain_with_graph_name(); assert(boost::num_vertices(g) == 2); assert(boost::num_edges(g) == 4); assert(get_graph_name(g) == "Two-state_Markov_chain");

18.5.4 The .dot file produced

```
Algorithm
                269
                        .dot
                                file
                                        created
                                                   from
                                                            the
                                                                    'cre-
ate markov chain with graph name' function (algorithm 267), converted
from graph to .dot file using algorithm 48
digraph G {
name="Two-state Markov chain";
0;
1;
0->0;
0 - > 1;
1->0;
1->1;
}
```

18.5.5 The .svg file produced

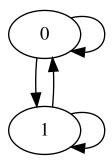


Figure 43: .svg file created from the 'create_markov_chain_with_graph_name' function (algorithm 267) its .dot file, converted from .dot file to .svg using algorithm 279

18.6 Create an undirected graph with a graph name property

18.6.1 Graph

See figure 8.

18.6.2 Function to create such a graph

Algorithm 270 shows the function to create K2 graph with a graph name.

Algorithm 270 Creating a K2 graph with a graph name

```
#include "create empty undirected graph with graph name.h
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::no_property ,
  boost::no property,
  boost::property<br/>boost::graph name t,std::string>
create_k2_graph_with_graph_name() noexcept
  auto g = create_empty_undirected_graph_with_graph_name
     ();
  const auto vd a = boost::add vertex(g);
  const auto vd_b = boost::add_vertex(g);
  const auto aer = boost::add_edge(vd_a, vd_b, g);
  assert (aer.second);
  get_property( //not boost::get_property
    g, boost::graph name
  = "K2";
  return g;
```

18.6.3 Creating such a graph

Algorithm 271 demonstrates the 'create_k2_graph_with_graph_name' function.

Algorithm 271 Demonstration of 'create k2 graph with graph name'

```
#include <cassert>
#include "create_k2_graph_with_graph_name.h"
#include "get_graph_name.h"

void create_k2_graph_with_graph_name_demo() noexcept
{
   const auto g = create_k2_graph_with_graph_name();
   assert(boost::num_vertices(g) == 2);
   assert(boost::num_edges(g) == 1);
   assert(get_graph_name(g) == "K2");
}
```

18.6.4 The .dot file produced

Algorithm 272 .dot file created from the 'create_k2_graph_with_graph_name' function (algorithm 270), converted from graph to .dot file using algorithm 48

```
graph G {
name="K2";
0;
1;
0--1;
}
```

18.6.5 The .svg file produced

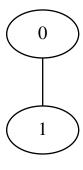


Figure 44: .svg file created from the 'create_k2_graph_with_graph_name' function (algorithm 270) its .dot file, converted from .dot file to .svg using algorithm 279

19 Working on graphs with a graph name

19.1 Storing a graph with a graph name property as a .dot file

I am unsure if this results in a .dot file that can produce a graph with a graph name, but this is what I came up with.

Algorithm 273 Storing a graph with a graph name as a .dot file

```
#include < string>
#include <fstream>
\#include <boost / graph / graphviz . hpp>
#include <boost/graph/properties.hpp>
#include "get graph name.h"
template <typename graph>
void save_graph_with_graph_name_to_dot(
  const graph& g,
  const std::string& filename
{
  std::ofstream f(filename);
  boost::write_graphviz(
    f,
    boost :: default_writer(),
    boost :: default_writer(),
    //Unsure if this results in a graph
    //that can be loaded correctly
    //from a .dot file
    [g](std::ostream \& os) {
      os << "name=\""
        << get graph name(g)
        << " \ "; \ n ";
  );
}
```

19.2 Loading a directed graph with a graph name property from a .dot file

This will result in a directed graph without a name [ISSUE #12]. Please email me if you know how to do this correctly.

${\bf Algorithm~274}$ Loading a directed graph with a graph name from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create empty directed graph with graph name.h"
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS,
  boost::no property,
  boost::no property,
  boost::property<
    boost::graph name t, std::string
load directed graph with graph name from dot (
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g = create empty directed graph with graph name();
  #ifdef TODO KNOW HOW TO LOAD A GRAPH ITS NAME
  boost::dynamic_properties p; //_do_ default construct
  p.property("name",get_property(g,boost::graph_name));
     //AFAIK, this should work
  #else
  boost::dynamic_properties p(
    boost::ignore other properties
  );
  #endif
  boost::read graphviz(f,g,p);
  return g;
```

Note the part that I removed using #ifdef: I read that that is a valid approach, according to the Boost.Graph documentation (see http://www.boost.org/doc/libs/1_60_0/libs/graph/doc/read_graphviz.html), but it failed to compile.

19.3 Loading an undirected graph with a graph name property from a .dot file

This will result in an undirected graph without a name. [ISSUE #12] Please email me if you know how to do this correctly.

 ${f Algorithm~275}$ Loading an undirected graph with a graph name from a .dot file

```
#include <fstream>
#include < string>
#include <boost/graph/graphviz.hpp>
#include "create_empty_undirected_graph_with_graph_name.h
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::no property,
  boost::no_property,
  boost::property<
    boost::graph name t, std::string
load undirected graph with graph name from dot(
  const std::string& dot filename
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g = create empty undirected graph with graph name
     ();
  #ifdef TODO KNOW HOW TO LOAD A GRAPH ITS NAME
  boost::dynamic_properties p; //_do_ default construct
  p.property("name", get_property(g, boost::graph_name));
     //AFAIK, this should work
  \#else
  boost::dynamic_properties p(
    boost::ignore other properties
  );
  #endif
  boost::read graphviz(f,g,p);
  return g;
```

Note the part that I removed using #ifdef: I read that that is a valid approach, according to the Boost.Graph documentation (see http://www.boost.org/doc/libs/1_60_0/libs/graph/doc/read_graphviz.html), but it failed

to compile.

20 Building graphs with custom graph properties

I will write this chapter if and only if I can save and load a graph with a graph name (as in chapter 18). That is, if Issue #12 is fixed.

21 Working on graphs with custom graph properties

I will write this chapter if and only if I can save and load a graph with a graph name (as in chapter 18). That is, if Issue #12 is fixed.

22 Other graph functions

Some functions that did not fit in

22.1 Encode a std::string to a Graphviz-friendly format

You may want to use a label with spaces, comma's and/or quotes. Saving and loading these, will result in problem. This function replaces these special characters by a rare combination of ordinary characters.

Algorithm 276 Encode a std::string to a Graphviz-friendly format

```
#include <boost/algorithm/string/replace.hpp>

std::string graphviz_encode(std::string s) noexcept
{
   boost::algorithm::replace_all(s,",",","$$$COMMA$$$");
   boost::algorithm::replace_all(s,",",","$$$SPACE$$$");
   boost::algorithm::replace_all(s,"\"","$$$QUOTE$$$");
   return s;
}
```

22.2 Decode a std::string from a Graphviz-friendly format

This function undoes the 'graphviz_encode' function (algorithm 276) and thus converts a Graphviz-friendly std::string to the original human-friendly std::string.

Algorithm 277 Decode a std::string from a Graphviz-friendly format to a human-friendly format

```
#include <boost/algorithm/string/replace.hpp>

std::string graphviz_decode(std::string s) noexcept
{
   boost::algorithm::replace_all(s,"$$$COMMA$$$",",");
   boost::algorithm::replace_all(s,"$$$PACE$$$","_");
   boost::algorithm::replace_all(s,"$$$QUOTE$$$","\"");
   return s;
}
```

23 Misc functions

These are some function I needed for creating this tutorial. Although they are not important for working with graphs, I used these heavily. These functions may be compiler-dependent, platform-dependent and/or there may be superior alternatives. I just add them for completeness.

23.1 Getting a data type as a std::string

This function will only work under GCC. I found this code at: http://stackoverflow.com/questions/1055452/c-get-name-of-type-in-template. Thanks to 'mdudley' (Stack Overflow userpage at http://stackoverflow.com/users/111327/m-dudley).

Algorithm 278 Getting a data type its name as a std::string

```
#include < c stdlib >
#include < string>
#include <typeinfo>
#include < cxxabi.h>
template<typename T>
std::string get_type_name() noexcept
  std::string tname = typeid(T).name();
  int status = -1;
  char * const demangled name{
    abi::__cxa_demangle(
      tname.c_str(), NULL, NULL, &status
  };
  if(status = 0) {
    tname = demangled name;
    std::free(demangled name);
  return tname;
```

23.2 Convert a .dot to .svg

All illustrations in this tutorial are created by converting .dot to a .svg ('Scalable Vector Graphic') file. This function assumes the program 'dot' is installed, which is part of Graphviz.

Algorithm 279 Convert a .dot file to a .svg

```
#include <cassert>
#include < string>
#include <sstream>
#include "has dot.h"
#include "is_regular_file.h"
#include "is_valid_dot_file.h"
void convert_dot_to_svg(
   const std::string& dot filename,
  const std::string& svg filename
   assert (has dot());
   assert(is_valid_dot_file(dot_filename));
   std::stringstream cmd;
  \operatorname{cmd} << \operatorname{"dot}_{\smile} - \operatorname{Tsvg}_{\smile} = << \operatorname{dot} \operatorname{filename} << \operatorname{"}_{\smile} - \operatorname{o}_{\smile} = <<
       svg_filename;
   std::system(cmd.str().c str());
   assert(is_regular_file(svg_filename));
}
```

'convert_dot_to_svg' makes a system call to the prgram 'dot' to convert the .dot file to an .svg file.

23.3 Check if a file exists

Not the most smart way perhaps, but it does only use the STL.

Algorithm 280 Check if a file exists

```
#include <fstream>
bool is_regular_file(const std::string& filename)
    noexcept
{
    std::fstream f;
    f.open(filename.c_str(),std::ios::in);
    return f.is_open();
}
```

24 Errors

Some common errors.

24.1 Formed reference to void

This compile-time error occurs when you create a graph without a certain property, then subsequently reading that property, as in algorithm 281:

Algorithm 281 Creating the error 'formed reference to void'

```
#include "create_k2_graph.h"
#include "get_vertex_names.h"

void formed_reference_to_void() noexcept
{
    get_vertex_names(create_k2_graph());
}
```

In algorithm 281 a graph is created with vertices of no properties. Then the names of these vertices, which do not exists, are tried to be read. If you want to read the names of the vertices, supply a graph that has this property.

24.2 No matching function for call to 'clear out edges'

This compile-time error occurs when you want to clear the outward edges from a vertex in an undirected graph.

```
#include "create_k2_graph.h"

void no_matching_function_for_call_to_clear_out_edges()
    noexcept
{
    auto g = create_k2_graph();
    const auto vd = *vertices(g).first; //not boost::
        vertices
    boost::clear_in_edges(vd,g);
}
```

In algorithm 282 an undirected graph is created, a vertex descriptor is obtained, then its out edges are tried to be cleared. Either use a directed graph (which has out edges), or use the 'boost::clear_vertex' function instead.

24.3 No matching function for call to 'clear_in_edges'

See chapter 24.2.

${\bf 24.4} \quad {\bf Undefined\ reference\ to\ boost:: detail::graph::read_graphviz_new}$

You will have to link against the Boost.Graph and Boost.Regex libraries. In Qt Creator, this is achieved by adding these lines to your Qt Creator project file:

LIBS += -lboost graph - lboost regex

24.5 Property not found: node id

When loading a graph from file (as in chapter 3.9) you will be using boost::read_graphviz. boost::read_graphviz needs a third argument, of type boost::dynamic_properties. When a graph does not have properties, do not use a default constructed version, but initializate with 'boost::ignore_other_properties' as a constructor argument instead. Algorithm 283 shows how to trigger this run-time error.

Algorithm 283 Creating the error 'Property not found: node_id'

```
#include <cassert>
#include <fstream>
#include "is regular file.h"
#include "create empty undirected graph.h"
#include "create k2 graph.h"
#include "save_graph_to_dot.h"
void property_not_found_node_id() noexcept
  const std::string dot filename{"
     property not found node id.dot"};
  //Create a file
    const auto g = create k2 graph();
    save graph to dot(g, dot filename);
    assert (is regular file (dot filename));
  //Try to read that file
  std::ifstream f(dot filename.c str());
  auto g = create_empty_undirected_graph();
  //Line\ below\ should\ have\ been
  // boost:: dynamic\_properties p(boost::
     ignore\_other\_properties);
  boost::dynamic properties p; //Error
  try {
    boost::read graphviz(f,g,p);
  catch (std::exception&) {
    return; //Should get here
  assert (!"Should_not_get_here");
}
```

25 Appendix

25.1 List of all edge, graph and vertex properties

The following list is obtained from the file 'boost/graph/properties.hpp'.

Edge	Graph	Vertex
edge_all	graph_all	vertex_all
edge_bundle	$graph_bundle$	vertex_bundle
edge_capacity	graph_name	vertex_centrality
edge_centrality	graph_visitor	vertex_color
edge_color		vertex_current_degree
edge_discover_time		vertex_degree
$edge_finished$		vertex_discover_time
edge_flow		vertex_distance
$edge_global$		vertex_distance2
$edge_index$		$vertex_finish_time$
edge_local		vertex_global
$edge_local_index$		vertex_in_degree
$edge_name$		vertex_index
$edge_owner$		vertex_index1
edge_residual_capacity		$vertex_index2$
$edge_reverse$		vertex_local
$edge_underlying$		$vertex_local_index$
edge_update		$vertex_lowpoint$
$edge_weight$		$vertex_name$
edge_weight2		vertex_out_degree
		$vertex_owner$
		vertex_potential
		vertex_predecessor
		vertex_priority
		vertex_rank
		vertex_root
		$vertex_underlying$
		vertex_update

25.2 Graphviz attributes

List created from www.graphviz.org/content/attrs, where only the attributes that are supported by all formats are listed:

Edge	Graph	Vertex
arrowhead	background	color
arrowsize	bgcolor	colorscheme
arrowtail	center	$\operatorname{comment}$
color	charset	distortion
colorscheme	color	fillcolor
comment	colorscheme	fixedsize
decorate	comment	fontcolor
dir	concentrate	fontname
fillcolor	fillcolor	fontsize
fontcolor	fontcolor	gradientangle
fontname	fontname	height
fontsize	fontpath	image
gradientangle	fontsize	imagescale
headclip	forcelabels	label
headlabel	gradientangle	labelloc
headport	imagepath	layer
label	label	margin
labelangle	labeljust	nojustify
labeldistance	labelloc	orientation
labelfloat	landscape	penwidth
labelfontcolor	layerlistsep	peripheries
labelfontname	layers	pos
labelfontsize	layerselect	regular
layer	layersep	sample points
nojustify	layout	$_{ m shape}$
penwidth	margin	shapefile
pos	$\operatorname{nodesep}$	sides
style	nojustify	skew
tailclip	orientation	sortv
taillabel	outputorder	style
tailport	pack	width
weight	packmode	xlabel
xlabel	pad	Z
	page	
	pagedir	
	penwidth	
	quantum	
	ratio	
	rotate	
	size	
	sortv	
	splines	
	style	
	viewport	

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