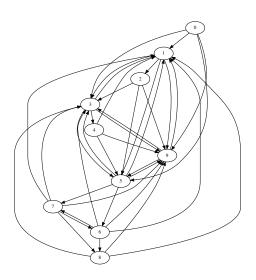
A well-connected C++11 Boost.Graph tutorial

Richèl Bilderbeek

March 11, 2016



Contents

1	\mathbf{Intr}	oduction	11
	1.1	Why this tutorial	11
	1.2	Tutorial style	11
	1.3	Code snippets	12
	1.4	Coding style	12
	1.5	License	13
	1.6	Feedback	14
	1.7	Acknowledgements	14
	1.8	Outline	14
2	Buil	lding graphs without properties	15
	2.1	Creating an empty (directed) graph	19
	2.2	Creating an empty undirected graph	20
	2.3	Counting the number of vertices	22
	2.4	Counting the number of edges	23
	2.5	Adding a vertex	24

	2.6	Vertex descriptors
	2.7	Get the vertex iterators
	2.8	Get all vertex descriptors
	2.9	Add an edge
	2.10	boost::add_edge result
	2.11	Getting the edge iterators
	2.12	Edge descriptors
	2.13	Get all edge descriptors
	2.14	Creating a directed graph
		2.14.1 Graph
		2.14.2 Function to create such a graph
		2.14.3 Creating such a graph
		2.14.4 The .dot file produced
		2.14.5 The .svg file produced
	2.15	Creating K_2 , a fully connected undirected graph with two vertices 36
		2.15.1 Graph
		2.15.2 Function to create such a graph
		2.15.3 Creating such a graph
		2.15.4 The .dot file produced
		2.15.5~ The .svg file produced
	2.16	$ ightharpoonup$ Creating K_3 , a fully connected undirected graph with three
		vertices
		2.16.1 Graph
		2.16.2 Function to create such a graph
		2.16.3 Creating such a graph
		2.16.4 The .dot file produced
		$2.16.5~$ The .svg file produced \hdots
	2.17	Creating a path graph
		2.17.1 Graph
		2.17.2 Function to create such a graph
		2.17.3 Creating such a graph
		2.17.4 The .dot file produced $\dots \dots \dots$
		2.17.5 The .svg file produced
	2.18	Creating a Peterson graph
		2.18.1 Graph
		2.18.2 Function to create such a graph
		2.18.3 Creating such a graph
		2.18.4 The .dot file produced
		2.18.5 The .svg file produced
3	Wor	king on graphs without properties 49
	3.1	Getting the vertices' out degree
	3.2	Is there an edge between two vertices?
	3.3	Get the edge between two vertices
	3.4	Create a direct-neighbour subgraph from a vertex descriptor . 54

	3.5		ating all direct-neighbour subgraphs from a graph without	_
			ties	
	3.6	_	two graphs isomorphic?	
	3.7	_	nt the number of connected components in an directed graph 5	9
	3.8		int the number of connected components in an undirected	
		graph		
	3.9	Saving	a graph to a .dot file	3
			g a directed graph from a .dot 6	
	3.11	Loadin	g an undirected graph from a .dot file 6	6
4	Buil		raphs with named vertices 68	
	4.1		$_{ m log}$ an empty directed graph with named vertices 60	
	4.2		$_{ m log}$ an empty undirected graph with named vertices $_{ m c}$. $_{ m c}$	0
	4.3		vertex with a name	
	4.4	Gettin	g the vertices' names $\dots \dots \dots$	
	4.5	Creatin	ng a Markov chain with named vertices	5
		4.5.1	Graph	5
		4.5.2	Function to create such a graph	6
		4.5.3	Creating such a graph	6
		4.5.4	The .dot file produced	7
		4.5.5	The .svg file produced	7
	4.6	Creating	$1 ext{ng } K_2 ext{ with named vertices } \dots $	8
		4.6.1	Graph	8
		4.6.2	Function to create such a graph	8
		4.6.3	Creating such a graph	9
		4.6.4	The .dot file produced	0
		4.6.5	The .svg file produced	0
	4.7	► Cre	ating K_3 with named vertices	1
		4.7.1	Graph	1
		4.7.2	Function to create such a graph	1
		4.7.3	Creating such a graph	2
		4.7.4	The .dot file produced	3
		4.7.5	The .svg file produced	3
	4.8	► Cre	ating a path graph with named vertices	4
		4.8.1	Graph	4
		4.8.2	Function to create such a graph	4
		4.8.3	Creating such a graph	5
		4.8.4	The .dot file produced	6
		4.8.5	The .svg file produced	
	4.9		ating a Petersen graph with named vertices 8	
		4.9.1	Graph	
		4.9.2	Function to create such a graph	
		4.9.3	Creating such a graph	
		4.9.4	The .dot file produced	
		4.9.5	The svg file produced	
				•

5	Wor	king on graphs with named vertices	92
	5.1	Check if there exists a vertex with a certain name	93
	5.2	Find a vertex by its name	95
	5.3	Get a (named) vertex its degree, in degree and out degree	96
	5.4	Get a vertex its name from its vertex descriptor	98
	5.5	Set a (named) vertex its name from its vertex descriptor	100
	5.6	Setting all vertices' names	101
	5.7	Clear the edges of a named vertex	102
	5.8	Remove a named vertex	104
	5.9	Adding an edge between two named vertices	105
	5.10	► Removing the edge between two named vertices	107
	5.11	Count the vertices with a certain name	109
	5.12	Create a direct-neighbour subgraph from a vertex descriptor	
			111
	5.13	Creating all direct-neighbour subgraphs from a graph with	
		named vertices	113
	5.14	Are two graphs with named vertices isomorphic?	116
	5.15	Saving an directed/undirected graph with named vertices to a	
		.dot file	119
		5.15.1 Using boost::make_label_writer	
		5.15.2 Using a C++11 lambda function	
		5.15.3 Demonstration	
		Loading a directed graph with named vertices from a .dot	
	5.17	Loading an undirected graph with named vertices from a .dot $aaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaaa$	124
6	Buil	Iding graphs with named edges and vertices	L 26
Ū	6.1	Creating an empty directed graph with named edges and vertices	
	6.2	Creating an empty undirected graph with named edges and vertices:	
	6.3	Adding a named edge	
	6.4	Adding a named edge between vertices	
	6.5	Getting the edges' names	
	6.6	Creating Markov chain with named edges and vertices	
		6.6.1 Graph	
		6.6.2 Function to create such a graph	
		6.6.3 Creating such a graph	
		6.6.4 The .dot file produced	
		6.6.5 The svg file produced	
	6.7	Creating K_2 with named edges and vertices	
		6.7.1 Graph	138
			139
		6.7.3 Creating such a graph	140
		6.7.4 The .dot file produced	141
			142
	6.8		142
		6.8.1 Graph	142
		6.8.2 Function to create such a graph	142

		6.8.3 Creating such a graph	143
		6.8.4 The .dot file produced	
		6.8.5 The .svg file produced	145
	6.9	Creating a path graph with named edges and vertices	145
		6.9.1 Graph	146
		6.9.2 Function to create such a graph	146
		6.9.3 Creating such a graph	
		6.9.4 The .dot file produced	
			148
	6.10		
		6.10.1 Graph	149
		6.10.2 Function to create such a graph	150
		6.10.3 Creating such a graph	
		6.10.4 The .dot file produced	
		6.10.5 The svg file produced	
		original interest in the produced and the control of the control o	100
7	Wor	king on graphs with named edges and vertices	154
	7.1	Check if there exists an edge with a certain name	155
	7.2	Find an edge by its name	156
	7.3	Get a (named) edge its name from its edge descriptor	158
	7.4	Set a (named) edge its name from its edge descriptor	159
	7.5	Removing the first edge with a certain name	161
	7.6	Create a direct-neighbour subgraph from a vertex descriptor	
		of a graph with named edges and vertices	163
	7.7	Creating all direct-neighbour subgraphs from a graph with	
		named edges and vertices	165
	7.8	Saving an undirected graph with named edges and vertices as a	
		.dot	168
	7.9	Loading a directed graph with named edges and vertices from a	
		.dot	170
	7.10		
	0	a .dot	172
8		lding graphs with bundled vertices	175
	8.1	Creating the bundled vertex class	
	8.2	Create the empty directed graph with bundled vertices	
	8.3	Create the empty undirected graph with bundled vertices	
	8.4	Add a bundled vertex	178
	8.5	Getting the bundled vertices' my_vertexes	179
	8.6	Creating a two-state Markov chain with bundled vertices	180
		8.6.1 Graph	180
		8.6.2 Function to create such a graph	180
		8.6.3 Creating such a graph	181
		8.6.4 The .dot file produced	182
		8.6.5 The svg file produced	184
	8.7	Creating K_2 with bundled vertices	185

		8.7.1 Graph	186 186 187
9	9.1 9.2 9.3 9.4 9.5 9.6 9.7	king on graphs with bundled vertices Has a bundled vertex with a my_bundled_vertex Find a bundled vertex with a certain my_bundled_vertex Get a bundled vertex its 'my_bundled_vertex' Set a bundled vertex its my_vertex Setting all bundled vertices' my_vertex objects Storing a graph with bundled vertices as a .dot Loading a directed graph with bundled vertices from a .dot	190 190 192 194 195 196 197 200
10	9.8	Loading an undirected graph with bundled vertices from a .dot .	
	10.1 10.2 10.3 10.4 10.5 10.6	ding graphs with bundled edges and vertices Creating the bundled edge class. Create an empty directed graph with bundled edges and vertices Create an empty undirected graph with bundled edges and vertices Add a bundled edge Getting the bundled edges my_edges. Creating a Markov-chain with bundled edges and vertices 10.6.1 Graph 10.6.2 Function to create such a graph 10.6.3 Creating such a graph 10.6.4 The .dot file produced 10.6.5 The .svg file produced Creating K_3 with bundled edges and vertices 10.7.1 Graph 10.7.2 Function to create such a graph 10.7.3 Creating such a graph 10.7.4 The .dot file produced 10.7.5 The .svg file produced	208 \$209 210 212 213 214 216 218 219 221 222 222 224
11		0 0 1	225
	11.2 11.3 11.4 11.5 11.6	Has a my_bundled_edge	
		a dot file	236

12		ding graphs with custom vertices	239
	12.1	Creating the vertex class	239
	12.2	Installing the new vertex property	241
		Create the empty directed graph with custom vertices	
		Create the empty undirected graph with custom vertices	
	12.5	$Add\ a\ custom\ vertex\ \dots$	244
	12.6	Getting the vertices' my_vertexes	245
	12.7	Creating a two-state Markov chain with custom vertices	
		12.7.1 Graph	
		12.7.2 Function to create such a graph	
		12.7.3 Creating such a graph	
		12.7.4 The dot file produced	
		12.7.5 The svg file produced	
	12.8	Creating K_2 with custom vertices	250
		12.8.1 Graph	
		12.8.2 Function to create such a graph	
		12.8.3 Creating such a graph	
		12.8.4 The .dot file produced	
		12.8.5 The svg file produced	
	12.9	Creating a path graph with custom vertices	
		12.9.1 Graph	
		12.9.2 Function to create such a graph	
		12.9.3 Creating such a graph	254
		12.9.4 The .dot file produced	
		12.9.5 The svg file produced	255
13	Wor	king on graphs with custom vertices (as a custom property)	256
		Has a custom vertex with a my vertex	
		Find a custom vertex with a certain my vertex	
	13.3	Get a custom vertex its my_vertex	260
	13.4	Set a custom vertex its my_vertex	262
		Setting all custom vertices' my_vertex objects	
	13.6	Adding an edge between two custom vertices	266
		Create a direct-neighbour subgraph from a vertex descriptor	
		of a graph with custom vertices	267
	13.8	Creating all direct-neighbour subgraphs from a graph with	
		${\bf custom\ vertices\ }\ldots\ldots\ldots\ldots\ldots\ldots\ldots\ldots\ldots$	
		Are two graphs with custom vertices isomorphic?	
		Storing a graph with custom vertices as a .dot	
		Loading a directed graph with custom vertices from a .dot	
	13.12	Loading an undirected graph with custom vertices from a .dot	278

14	Buil	ding graphs with custom and selectable vertices	280
	14.1	Installing the new is selected property	281
	14.2	Create an empty directed graph with custom and selectable vertices	s282
	14.3	Create an empty undirected graph with custom and selectable	
		vertices	284
	14.4	Add a custom and selectable vertex	285
	14.5	Creating a Markov-chain with custom and selectable vertices	288
		14.5.1 Graph	288
		14.5.2 Function to create such a graph	288
		14.5.3 Creating such a graph	290
		14.5.4 The .dot file produced	291
			292
	14.6	Creating K_2 with custom and selectable vertices	
		14.6.1 Graph	293
		14.6.2 Function to create such a graph	
		14.6.3 Creating such a graph	
		14.6.4 The .dot file produced	294
		14.6.5 The .svg file produced	
15	Wor	king on graphs with custom and selectable vertices	295
		• Getting the vertices with a certain selectedness	
		Counting the vertices with a certain selectedness	
		Adding an edge between two selected vertices	
		Create a direct-neighbour subgraph from a vertex descriptor	
		of a graph with custom and selectable vertices	299
	15.5	Creating all direct-neighbour subgraphs from a graph with	
		custom and selectable vertices	301
	15.6	Storing a graph with custom and selectable vertices as a .dot	
		Loading a directed graph with custom and selectable vertices	001
	10.1	from a .dot	308
	15.8	Loading an undirected graph with custom and selectable vertices	300
		from a .dot	311
16	Buil	ding graphs with custom edges and vertices	313
		Creating the custom edge class	
		Installing the new edge property	
		Create an empty directed graph with custom edges and vertices .	
		Create an empty undirected graph with custom edges and vertices	
		Add a custom edge	320
		Getting the custom edges my edges	322
		Creating a Markov-chain with custom edges and vertices	323
	10.1	16.7.1 Graph	323
		16.7.2 Function to create such a graph	324
		16.7.3 Creating such a graph	324
		16.7.4 The .dot file produced	
		16.7.5 The syg file produced	$\frac{327}{327}$

	16.8	Creating K_3 with custom edges and vertices	
		16.8.1 Graph	
		16.8.2 Function to create such a graph	
		16.8.3 Creating such a graph	
		16.8.4 The .dot file produced	
		16.8.5 The svg file produced	330
17		0 0 1	330
		$Has\ a\ my_custom_edge\ .\ .\ .\ .\ .\ .\ .\ .\ .\ .\ .\ .$	
		Find a my_custom_edge	
		Get an edge its my_custom_edge	
	17.4	Set an edge its my_custom_edge	336
	17.5	Counting the edges with a certain selectedness	338
	17.6	Create a direct-neighbour subgraph from a vertex descriptor	
		of a graph with custom edges and vertices	340
	17.7	Creating all direct-neighbour subgraphs from a graph with	
		custom edges and vertices	342
	17.8	Storing a graph with custom edges and vertices as a .dot	345
	17.9	Load a directed graph with custom edges and vertices from a .dot	
		$file \ \dots $	346
	17.10	DLoad an undirected graph with custom edges and vertices from a	
		dot file	349
10	ъ .1		0 - 1
18		ding graphs with custom and selectable edges and vertices	
		Installing the new is_selected property	33Z
	10.2	and vertices	252
	109	Create an empty undirected graph with custom and selectable	555
	10.5	edges and vertices	255
	10 /	Add a custom and selectable edge	
		Creating a Markov-chain with custom and selectable vertices	
	10.0	18.5.1 Graph	
		18.5.2 Function to create such a graph	
		18.5.3 Creating such a graph	
		18.5.4 The .dot file produced	
		18.5.5 The svg file produced	
	18.6	Creating K_2 with custom and selectable edges and vertices \dots	
	10.0	18.6.1 Graph	
		18.6.2 Function to create such a graph	
		18.6.3 Creating such a graph	
		18.6.4 The .dot file produced	
		18.6.5 The syg file produced	

19	Wor	Working on graphs with custom and selectable edges and ver-			
	tices		368		
	19.1	► Create a direct-neighbour subgraph from a vertex descriptor of a graph with custom and selectable edges and vertices	369		
	19.2	Creating all direct-neighbour subgraphs from a graph with custom and selectable edges and vertices	372		
		Storing a graph with custom and selectable edges and vertices as a .dot $\dots \dots \dots$	374		
		Loading a directed graph with custom and selectable edges and vertices from a .dot	375		
	19.5	Loading an undirected graph with custom and selectable edges and vertices from a .dot	378		
20	Buil	ding graphs with a graph name	381		
	20.1	Create an empty directed graph with a graph name property	381		
		Create an empty undirected graph with a graph name property .			
		Get a graph its name property			
		Set a graph its name property			
		Create a directed graph with a graph name property			
		20.5.1 Graph			
		20.5.2 Function to create such a graph			
		20.5.3 Creating such a graph			
		20.5.4 The .dot file produced	387		
		20.5.5 The .svg file produced			
	20.6	Create an undirected graph with a graph name property			
		20.6.1 Graph			
		20.6.2 Function to create such a graph			
		20.6.3 Creating such a graph			
		20.6.4 The .dot file produced			
		20.6.5 The svg file produced			
21		king on graphs with a graph name	391		
	21.1	Storing a graph with a graph name property as a .dot file	391		
	21.2	Loading a directed graph with a graph name property from a .dot			
		file	391		
	21.3	Loading an undirected graph with a graph name property from a .dot file	393		
f 22	Oth	er graph functions	395		
		Encode a std::string to a Graphviz-friendly format			
		Decode a std::string from a Graphviz-friendly format			
		Check if a std. string is Graphviz-friendly			

23	\mathbf{Mis}	c functions	396
	23.1	Getting a data type as a std::string	396
	23.2	Convert a .dot to .svg	397
	23.3	Check if a file exists	398
24	Erro	ors	399
	24.1	Formed reference to void	399
	24.2	No matching function for call to 'clear_out_edges'	399
	24.3	No matching function for call to 'clear_in_edges'	400
	24.4	Undefined reference to boost::detail::graph::read graphviz new.	400
	24.5	Property not found: node id	400
	24.6	Stream zeroes	401
25	App	pendix	403
	25.1	List of all edge, graph and vertex properties	403
	25.2	Graphviz attributes	403

1 Introduction

This is 'A well-connected C++11 Boost.Graph tutorial', version 1.10.

1.1 Why this tutorial

I needed this tutorial already in 2006, when I started experimenting with Boost.Graph. More specifically, I needed a tutorial that:

- Orders concepts chronologically
- Increases complexity gradually
- Shows complete pieces of code

What I had were the book [8] and the Boost.Graph website, both did not satisfy these requirements.

1.2 Tutorial style

Readable for beginners This tutorial is aimed at the beginner programmer. This tutorial is intended to take the reader to the level of understanding the book [8] and the Boost.Graph website require. It is about basic graph manipulation, not the more advanced graph algorithms.

High verbosity This tutorial is intended to be as verbose, such that a beginner should be able to follow every step, from reading the tutorial from beginning to end chronologically. Especially in the earlier chapters, the rationale behind the code presented is given, including references to the literature. Chapters marked with '▶' are optional, less verbose and bring no new information to the storyline.

Repetitiveness This tutorial is intended to be as repetitive, such that a beginner can spot the patterns in the code snippets their increasing complexity. Extending code from this tutorial should be as easy as extending the patterns.

Index In the index, I did first put all my long-named functions there literally, but this resulted in a very sloppy layout. Instead, the function 'do_something' can be found as 'Do something' in the index. On the other hand, STL and Boost functions like 'std::do_something' and 'boost::do_something' can be found as such in the index.

1.3 Code snippets

For every concept, I will show

- the 'do' function: a function that achieves a goal, for example 'create empty undirected graph'
- the 'demo' function: a function that demonstrates how to call the first, for example 'create empty undirected graph demo'

I enjoy to show concepts by putting those in (long-named) functions. These functions sometimes border the trivial, by, for example, only calling a single Boost.Graph function. On the other hand, these functions have more English-sounding names, resulting in demonstration code that is readable. Additionally, they explicitly mention their return type (in a simpler way), which may be considered informative.

All coding snippets are taken from compiled C++11 code. I chose to use C++11 because (1) C++14 was not installable on all my computers (2) the step to C++14 is small. All code is tested to compile cleanly under GCC at the highest warning level. The code, as well as this tutorial, can be downloaded from the GitHub at www.github.com/richelbilderbeek/BoostGraphTutorial.

1.4 Coding style

Coding standard I use the coding style from the Core C++ Guidelines. At the time of this writing, the Core C++ Guidelines were still in early development, so I can only hope the conventions I then chose to follow are still Good Ideas.

No comments in code It is important to add comments to code. In this tutorial, however, I have chosen not to put comments in code, as I already describe the function in the tutorial its text. This way, it prevents me from saying the same things twice.

Trade-off between generic code and readability It is good to write generic code. In this tutorial, however, I have chosen my functions to have no templated arguments for conciseness and readability. For example, a vertex name is std::string, the type for if a vertex is selected is a boolean, and the

custom vertex type is of type 'my_custom_vertex'. I think these choises are reasonable and that the resulting increase in readability is worth it.

Long function names and readability Due to my long function names and the limitation of ≈ 50 characters per line, sometimes the code does get to look a bit awkward. I am sorry for this.

Use of auto I prefer to use the keyword auto over doubling the lines of code for using statements. Often the 'do' functions return an explicit data type, these can be used for reference. Sometime I deduce the return type using decltype and a function with the same return type. When C++17 gets accessible, I will use 'decltype(auto)'. If you really want to know a type, you can use the 'get type name' function (chapter 23.1).

Explicity use of namespaces On the other hand, I am explicit in the namespaces of functions and classes I use, so to distinguish between types like 'std::array' and 'boost::array'. Some functions (for example, 'get') reside in the namespace of the graph to work on. In this tutorial, this is in the global namespace. Thus, I will write 'get', instead of 'boost::get', as the latter does not compile.

Use of STL algorithms I try to use STL algorithms wherever I can. Also you should prefer algorithm calls over hand-written for-loops ([9] chapter 18.12.1, [7] item 43). Sometimes using these algorithms becomes a burden on the lines of code. This is because in C++11, a lambda function argument (use by the algorithm) must have its data type specified. It may take multiple lines of 'using' statements being able to do so. In C++14 one can use 'auto' there as well. So, only if it shortens the number of lines significantly, I use raw for-loops, even though you shouldn't.

Re-use of functions The functions I develop in this tutorial are re-used from that moment on. This improves to readability of the code and decreases the number of lines.

1.5 License

This tutorial is licensed under Creative Commons license 4.0. All C++ code is licensed under GPL 3.0.



Figure 1: Creative Commons license 4.0

1.6 Feedback

This tutorial is not intended to be perfect yet. For that, I need help and feedback from the community. All referenced feedback is welcome, as well as any constructive feedback.

I have tried hard to strictly follow the style as described above. If you find I deviated from these decisions somewhere, I would be grateful if you'd let know. Next to this, there are some sections that need to be coded or have its code improved.

1.7 Acknowledgements

These are users that improved this tutorial and/or the code behind this tutorial, in chronological order:

- m-dudley, http://stackoverflow.com/users/111327/m-dudley
- E. Kawashima
- mat69, https://www.reddit.com/user/mat69
- danielhj, https://www.reddit.com/user/danieljh
- sehe, http://stackoverflow.com/users/85371/sehe
- cv and me, http://stackoverflow.com/users/2417774/cv-and-he

1.8 Outline

The chapters of this tutorial are also like a well-connected graph (as shown in figure 2). To allow for quicker learners to skim chapters, or for beginners looking to find the patterns.

The distinction between the chapter is in the type of edges and vertices. They can have:

- no properties: see chapter 2
- have a name: see chapter 4
- have a bundled property: see chapter 8
- have a custom property: see chapter 12

The differences between graphs with bundled and custom properties are shown in table 1:

	$\operatorname{Bundled}$	Custom
Meaning	Edges/vertices are of your type	Edges/vertices have an additional custom property
Interface	Directly	Via property map
Class members	Must be public	Can be private
File I/O mechanism	Via public class members	Via stream operators
File I/O constraints	Restricted to Graphviz attributes	Need encoding and decoding

Table 1: Difference between bundled and custom properties

Pivotal chapters are chapters like 'Finding the first vertex with ...', as this opens up the door to finding a vertex and manipulating it.

All chapters have a rather similar structure in themselves, as depicted in figure 3.

There are also some bonus chapters, that I have labeled with a '▶'. These chapters are added I needed these functions myself and adding them would not hurt. Just feel free to skip them, as there will be less theory explained.

2 Building graphs without properties

Boost.Graph is about creating graphs. In this chapter we create the simplest of graphs, in which edges and nodes have no properties (e.g. having a name).

Still, there are two types of graphs that can be constructed: undirected and directed graphs. The difference between directed and undirected graphs is in the edges: in an undirected graph, an edge connects two vertices without any directionality, as displayed in figure 4. In a directed graph, an edge goes from a certain vertex, its source, to another (which may actually be the same), its target. A directed graph is shown in figure 5.

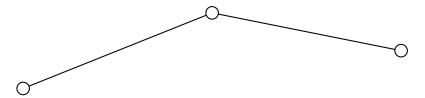


Figure 4: Example of an undirected graph

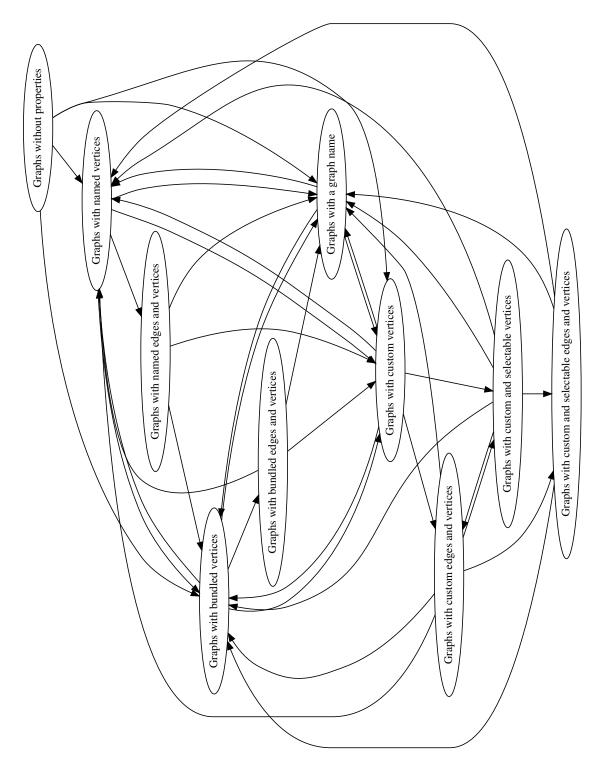


Figure 2: The relations between chapters

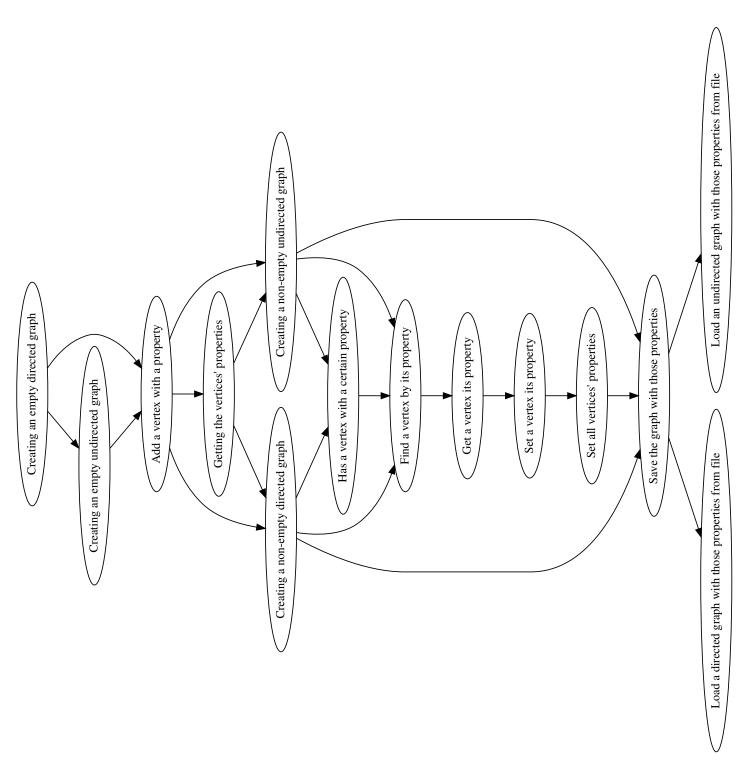


Figure 3: The relations between sub-chapters

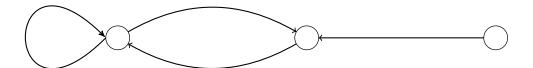


Figure 5: Example of a directed graph

In this chapter, we will build two directed and two undirected graphs:

- An empty (directed) graph, which is the default type: see chapter 2.1
- An empty (undirected) graph: see chapter 2.2
- A two-state Markov chain, a directed graph with two vertices and four edges, chapter 2.14
- K_2 , an undirected graph with two vertices and one edge, chapter 2.15

Creating an empty graph may sound trivial, it is not, thanks to the versatility of the Boost.Graph library.

In the process of creating graphs, some basic (sometimes bordering trivial) functions are encountered:

- Counting the number of vertices: see chapter 2.3
- Counting the number of edges: see chapter 2.4
- Adding a vertex: see chapter 2.5
- Getting all vertices: see chapter 2.7
- Getting all vertex descriptors: see chapter 2.8
- Adding an edge: see chapter 2.9
- Getting all edges: see chapter 2.11
- Getting all edge descriptors: see chapter 2.13

These functions are mostly there for completion and showing which data types are used.

The chapter also introduces some important concepts:

- Vertex descriptors: see chapter 2.6
- Edge insertion result: see chapter 2.10
- Edge descriptors: see chapter 2.12

After this chapter you may want to:

- Building graphs with named vertices: see chapter 4
- Building graphs with bundled vertices: see chapter 8
- Building graphs with custom vertices: see chapter 12
- Building graphs with a graph name: see chapter 20

2.1 Creating an empty (directed) graph

Let's create an empty graph!

Algorithm 1 shows the function to create an empty graph.

Algorithm 1 Creating an empty (directed) graph

```
#include <boost/graph/adjacency_list.hpp>
boost::adjacency_list<>
create_empty_directed_graph() noexcept
{
   return {};
}
```

The code consists out of an #include and a function definition. The #include tells the compiler to read the header file 'adjacency_list.hpp'. A header file (often with a '.h' or '.hpp' extension) contains class and functions declarations and/or definitions. The header file 'adjacency_list.hpp' contains the boost::adjacency_list class definition. Without including this file, you will get compile errors like 'definition of boost::adjacency_list unknown'¹. The function 'create empty directed graph' has:

- a return type: The return type is 'boost::adjacency_list<>', that is a 'boost::adjacency_list' with all template arguments set at their defaults
- a noexcept specification: the function should not throw², so it is preferred to mark it noexcept ([10] chapter 13.7).

¹In practice, these compiler error messages will be longer, bordering the unreadable ²if the function would throw because it cannot allocate this little piece of memory, you are already in big trouble

• a function body: all the function body does is implicitly create its return type by using the '{}'. An alternative syntax would be 'return boost::adjacency list<>()', which is needlessly longer

Algorithm 2 demonstrates the 'create_empty_directed_graph' function. Note that it includes a header file with the same name as the function³ first, to be able to use it. 'auto' is used, as this is preferred over explicit type declarations ([10] chapter 31.6). The keyword 'auto' lets the compiler figure out the type itself.

Algorithm 2 Demonstration of 'create empty directed graph'

```
#include "create_empty_directed_graph.h"

void create_empty_directed_graph_demo() noexcept
{
   const auto g = create_empty_directed_graph();
}
```

Congratulations, you've just created a boost::adjacency_list with its default template arguments. The boost::adjacency_list is the most commonly used graph type, the other is the boost::adjacency_matrix. We do not do anything with it yet, but still, you've just created a graph, in which:

- The out edges and vertices are stored in a std::vector
- The edges have a direction
- The vertices, edges and graph have no properties
- The edges are stored in a std::list

It stores its edges, out edges and vertices in a two different STL⁴ containers. std::vector is the container you should use by default ([10] chapter 31.6, [11] chapter 76), as it has constant time look-up and back insertion. The std::list is used for storing the edges, as it is better suited at inserting elements at any position.

I use const to store the empty graph as we do not modify it. Correct use of const is called const-correct. Prefer to be const-correct ([9] chapter 7.9.3, [10] chapter 12.7, [7] item 3, [3] chapter 3, [11] item 15, [2] FAQ 14.05, [1] item 8, [4] 9.1.6).

2.2 Creating an empty undirected graph

Let's create another empty graph! This time, we even make it undirected!

³I do not think it is important to have creative names

⁴Standard Template Library, the standard library

Algorithm 3 Creating an empty undirected graph

```
#include <boost/graph/adjacency_list.hpp>
boost:: adjacency_list <
   boost:: vecS ,
   boost:: vecS ,
   boost:: undirectedS
>
create_empty_undirected_graph() noexcept
{
   return {};
}
```

This algorith differs from the 'create_empty_directed_graph' function (algoritm 1) in that there are three template arguments that need to be specified in the creation of the boost::adjancency list:

- the first 'boost::vecS': select (that is what the 'S' means) that out edges are stored in a std::vector. This is the default way.
- the second 'boost::vecS': select that the graph vertices are stored in a std::vector. This is the default way.
- 'boost::undirectedS': select that the graph is undirected. This is all we needed to change. By default, this argument is boost::directed

Algorithm 4 demonstrates the 'create_empty_undirected_graph' function.

Algorithm 4 Demonstration of 'create empty undirected graph'

```
#include "create_empty_undirected_graph.h"

void create_empty_undirected_graph_demo() noexcept
{
   const auto g = create_empty_undirected_graph();
}
```

Congratulations, with algorithm 4, you've just created an undirected graph in which:

- The out edges and vertices are stored in a std::vector
- The graph is undirected

- Vertices, edges and graph have no properties
- Edges are stored in a std::list

2.3 Counting the number of vertices

Let's count all zero vertices of an empty graph!

Algorithm 5 Count the number of vertices

```
#include <cassert>
#include <boost/graph/adjacency_list.hpp>

template <typename graph>
int get_n_vertices(const graph& g) noexcept
{
   const int n{
      static_cast<int>(boost::num_vertices(g))
   };
   assert(static_cast<unsigned long>(n)
      == boost::num_vertices(g)
   );
   return n;
}
```

The function 'get_n_vertices' takes the result of boost::num_vertices, converts it to int and checks if there was conversion error. We do so, as one should prefer using signed data types over unsigned ones in an interface ([4] chapter 9.2.2). To do so, in the function body its first stament, the unsigned long produced by boost::num_vertices get converted to an int using a static_cast. Using an unsigned integer over a (signed) integer for the sake of gaining that one more bit ([9] chapter 4.4) should be avoided. The integer 'n' is initialized using list-initialization, which is preferred over the other initialization syntaxes ([10] chapter 17.7.6).

The assert checks if the conversion back to unsigned long re-creates the original value, to check if no information has been lost. If information is lost, the program crashes. Use assert extensively ([9] chapter 24.5.18, [10] chapter 30.5, [11] chapter 68, [6] chapter 8.2, [5] hour 24, [4] chapter 2.6).

The function 'get_n_vertices' is demonstrated in algorithm 6, to measure the number of vertices of both the directed and undirected graph we are already able to create.

Algorithm 6 Demonstration of the 'get n vertices' function

```
#include <cassert>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_n_vertices.h"

void get_n_vertices_demo() noexcept
{
   const auto g = create_empty_directed_graph();
   assert(get_n_vertices(g) == 0);

   const auto h = create_empty_undirected_graph();
   assert(get_n_vertices(h) == 0);
}
```

Note that the type of graph does not matter here. One can count the number of vertices of every graph, as all graphs have vertices. Boost.Graph is very good at detecting operations that are not allowed, during compile time.

2.4 Counting the number of edges

Let's count all zero edges of an empty graph!

This is very similar to the previous chapter, only it uses boost::num_edges instead:

Algorithm 7 Count the number of edges

```
#include <cassert>
#include <boost/graph/adjacency_list.hpp>

template <typename graph>
int get_n_edges(const graph& g) noexcept
{
   const int n{
      static_cast<int>(boost::num_edges(g))
   };
   assert(static_cast<unsigned long>(n)
      == boost::num_edges(g)
   );
   return n;
}
```

This code is similar to the 'get_n_vertices' function (algorithm 5, see rationale there) except 'boost::num_edges' is used, instead of 'boost::num_vertices',

which also returns an unsigned long.

The function 'get_n_edges' is demonstrated in algorithm 8, to measure the number of edges of an empty directed and undirected graph.

Algorithm 8 Demonstration of the 'get n edges' function

```
#include <cassert>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_n_edges.h"

void get_n_edges_demo() noexcept
{
   const auto g = create_empty_directed_graph();
   assert(get_n_edges(g) == 0);

   const auto h = create_empty_undirected_graph();
   assert(get_n_edges(h) == 0);
}
```

2.5 Adding a vertex

Empty graphs are nice, now its time to add a vertex!

To add a vertex to a graph, the boost::add_vertex function is used as shows in algorithm 9:

Algorithm 9 Adding a vertex to a graph

```
#include <type_traits>
#include <boost/graph/adjacency_list.hpp>

template <typename graph>
typename boost::graph_traits<graph>::vertex_descriptor
add_vertex(graph& g) noexcept
{
    static_assert(!std::is_const<graph>::value,
        "graph_cannot_be_const"
);
    const auto vd = boost::add_vertex(g);
    return vd;
}
```

The static_assert at the top of the function checks during compiling if the

function is called with a non-const graph. One can freely omit this static_assert: you will get a compiler error anyways, be it a less helpful one.

Note that boost::add_vertex (in the 'add_vertex' function) returns a vertex descriptor, which is ignored for now. Vertex descriptors are looked at in more details at the chapter 2.6, as we need these to add an edge. To allow for this already, 'add_vertex' also returns a vertex descriptor.

Algorithm 10 shows how to add a vertex to a directed and undirected graph.

Algorithm 10 Demonstration of the 'add vertex' function

```
#include "add_vertex.h"
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"

void add_vertex_demo() noexcept
{
   auto g = create_empty_undirected_graph();
   add_vertex(g);
   assert(boost::num_vertices(g) == 1);

auto h = create_empty_directed_graph();
   add_vertex(h);
   assert(boost::num_vertices(h) == 1);
}
```

This demonstration code creates two empty graphs, adds one vertex to each and then asserts that the number of vertices in each graph is one. This works for both types of graphs, as all graphs have vertices.

2.6 Vertex descriptors

A vertex descriptor is a handle to a vertex within a graph.

Vertex descriptors can be obtained by dereferencing a vertex iterator (see chapter 2.8). To do so, we first obtain some vertex iterators in chapter 2.7).

Vertex descriptors are used to:

- add and edge between two vertices, see chapter 2.9
- obtain properties of vertex a vertex, for example the vertex its out degrees (chapter 3.1), the vertex its name (chapter 4.4), or a custom vertex property (chapter 12.6)

In this tutorial, vertex descriptors have named prefixed with 'vd_', for example 'vd_1'.

2.7 Get the vertex iterators

You cannot get the vertices. This may sound unexpected, as it must be possible to work on the vertices of a graph. Working on the vertices of a graph is done throught these steps:

- Obtain a vertex iterator pair from the graph
- Dereferencing a vertex iterator to obtain a vertex descriptor

'vertices' (not 'boost::vertices') is used to obtain a vertex iterator pair, as shown in algorithm 11. The first vertex iterator points to the first vertex (its descriptor, to be precise), the second points to beyond the last vertex (its descriptor, to be precise). In this tutorial, vertex iterator pairs have named prefixed with 'vip_', for example 'vip_1'.

Algorithm 11 Get the vertex iterators of a graph

```
#include <boost/graph/adjacency_list.hpp>

template <typename graph>
std::pair <
    typename graph::vertex_iterator,
    typename graph::vertex_iterator
>
get_vertex_iterators(const graph& g) noexcept
{
    return vertices(g);
}
```

This is a somewhat trivial function, as it forwards the function call to 'vertices' (not 'boost::vertices').

These vertex iterators can be dereferenced to obtain the vertex descriptors. Note that 'get_vertex_iterators' will not be used often in isolation: usually one obtains the vertex descriptors immediatly. Just for your reference, algorithm 12 demonstrates of the 'get_vertices' function, by showing that the vertex iterators of an empty graph point to the same location.

Algorithm 12 Demonstration of 'get vertex iterators'

```
#include <cassert>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_vertex_iterators.h"

void get_vertex_iterators_demo() noexcept
{
   const auto g = create_empty_undirected_graph();
   const auto vip_g = get_vertex_iterators(g);
   assert(vip_g.first == vip_g.second);

   const auto h = create_empty_directed_graph();
   const auto vip_h = get_vertex_iterators(h);
   assert(vip_h.first == vip_h.second);
}
```

2.8 Get all vertex descriptors

Vertex descriptors are the way to manipulate those vertices. Let's go get the all!

Vertex descriptors are obtained from dereferencing vertex iterators. Algorithm 13 shows how to obtain all vertex descriptors from a graph.

Algorithm 13 Get all vertex descriptors of a graph

```
#include <vector>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/graph_traits.hpp>

template <typename graph>
std::vector<
    typename boost::graph_traits<graph>::vertex_descriptor
>
get_vertex_descriptors(const graph& g) noexcept
{
    using vd = typename graph::vertex_descriptor;

    std::vector<vd> vds(boost::num_vertices(g));
    const auto vis = vertices(g);
    std::copy(vis.first, vis.second, std::begin(vds));
    return vds;
}
```

This is the first more complex piece of code. In the first lines, some 'using' statements allow for shorter type names⁵.

The std::vector to serve as a return value is created at the needed size, which is the number of vertices.

The function 'vertices' (not boost::vertices!) returns a vertex iterator pair. These iterators are used by std::copy to iterator over. std::copy is an STL algorithm to copy a half-open range. Prefer algorithm calls over hand-written for-loops ([9] chapter 18.12.1, [7] item 43).

In this case, we copy all vertex descriptors in the range produced by 'vertices' to the std::vector.

This function will not be used in practice: one iterates over the vertices directly instead, saving the cost of creating a std::vector. This function is only shown as an illustration.

Algorithm 14 demonstrates that an empty graph has no vertex descriptors:

Algorithm 14 Demonstration of 'get vertex descriptors'

```
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_vertex_descriptors.h"

void get_vertex_descriptors_demo() noexcept
{
   const auto g = create_empty_undirected_graph();
   const auto vds_g = get_vertex_descriptors(g);
   assert(vds_g.empty());

   const auto h = create_empty_directed_graph();
   const auto vds_h = get_vertex_descriptors(h);
   assert(vds_h.empty());
}
```

Because all graphs have vertices and thus vertex descriptors, the type of graph is unimportant for this code to compile.

2.9 Add an edge

To add an edge to a graph, two vertex descriptors are needed. A vertex descriptor is a handle to the vertex within a graph (vertex descriptors are looked at in more details in chapter 2.6). Algorithm 15 adds two vertices to a graph, and connects these two using boost::add edge:

⁵which may be necessary just to create a tutorial with code snippets that are readable

Algorithm 15 Adding (two vertices and) an edge to a graph

```
#include <cassert>
#include <type_traits>
#include <boost/graph/adjacency_list.hpp>

template <typename graph>
typename boost::graph_traits<graph>::edge_descriptor
add_edge(graph& g) noexcept
{
    static_assert(!std::is_const<graph>::value,
        "graph_cannot_be_const"
);
    const auto vd_a = boost::add_vertex(g);
    const auto vd_b = boost::add_vertex(g);
    const auto aer = boost::add_edge(
        vd_a, vd_b, g
);
    assert(aer.second);
    return aer.first;
}
```

Algorithm 15 shows how to add an isolated edge to a graph (instead of allowing for graphs with higher connectivities). First, two vertices are created, using the function 'boost::add_vertex'. 'boost::add_vertex' returns a vertex descriptor (which I prefix with 'vd'), both of which are stored. The vertex descriptors are used to add an edge to the graph, using 'boost::add_edge'. 'boost::add_edge' returns returns a std::pair, consisting of an edge descriptor and a boolean success indicator. The success of adding the edge is checked by an assert statement. Here we assert that this insertion was successfull. Insertion can fail if an edge is already present and duplicates are not allowed.

A demonstration of add_edge is shown in algorith 16, in which an edge is added to both a directed and undirected graph, after which the number of edges and vertices is checked.

Algorithm 16 Demonstration of 'add edge'

```
#include "add_edge.h"
#include "create_empty_directed_graph.h"

void add_edge_demo() noexcept
{
   auto g = create_empty_undirected_graph();
   add_edge(g);
   assert(boost::num_vertices(g) == 2);
   assert(boost::num_edges(g) == 1);

auto h = create_empty_directed_graph();
   add_edge(h);
   assert(boost::num_vertices(h) == 2);
   assert(boost::num_dedges(h) == 1);
}
```

The graph type is unimportant: as all graph types have vertices and edges, edges can be added without possible compile problems.

2.10 boost::add_edge result

When using the function 'boost::add_edge', a 'std::pair<edge_descriptor,bool>' is returned. It contains both the edge descriptor (see chapter 2.12) and a boolean, which indicates insertion success.

In this tutorial, boost::add_edge results have named prefixed with 'aer_', for example 'aer_1'.

2.11 Getting the edge iterators

You cannot get the edges directly. Instead, working on the edges of a graph is done throught these steps:

- Obtain an edge iterator pair from the graph
- Dereference an edge iterator to obtain an edge descriptor

'edges' (not boost::edges!) is used to obtain an edge iterator pair. The first edge iterator points to the first edge (its descriptor, to be precise), the second points to beyond the last edge (its descriptor, to be precise). In this tutorial, edge iterator pairs have named prefixed with 'eip_', for example 'eip_1'. Algoritm 17 shows how to obtain these:

Algorithm 17 Get the edge iterators of a graph

```
#include <boost/graph/adjacency_list.hpp>

template <typename graph>
std::pair <
   typename graph::edge_iterator,
   typename graph::edge_iterator
>
get_edge_iterators(const graph& g) noexcept
{
   return edges(g);
}
```

This is a somewhat trivial function, as all it does is forward to function call to 'edges' (not boost::edges!) These edge iterators can be dereferenced to obtain the edge descriptors. Note that this function will not be used often in isolation: usually one obtains the edge descriptors immediatly.

Algorithm 18 demonstrates 'get_edge_iterators' by showing that both iterators of the edge iterator pair point to the same location, when the graph is empty.

Algorithm 18 Demonstration of 'get edge iterators'

```
#include <cassert>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_edge_iterators.h"

void get_edge_iterators_demo() noexcept
{
   const auto g = create_empty_undirected_graph();
   const auto eip_g = get_edge_iterators(g);
   assert(eip_g.first == eip_g.second);

auto h = create_empty_directed_graph();
   const auto eip_h = get_edge_iterators(h);
   assert(eip_h.first == eip_h.second);
}
```

2.12 Edge descriptors

An edge descriptor is a handle to an edge within a graph. They are similar to vertex descriptors (chapter 2.6).

Edge descriptors are used to obtain the name, or other properties, of an edge In this tutorial, edge descriptors have named prefixed with 'ed_', for example 'ed_1'.

2.13 Get all edge descriptors

Obtaining all edge descriptors is similar to obtaining all vertex descriptors (algorithm 13), as shown in algorithm 19:

Algorithm 19 Get all edge descriptors of a graph

```
#include <vector>
#include <boost/graph/adjacency_list.hpp>
#include "boost/graph/graph_traits.hpp"

template <typename graph>
std::vector<
   typename boost::graph_traits<graph>::edge_descriptor
> get_edge_descriptors(const graph& g) noexcept
{
   using boost::graph_traits;
   using ed = typename graph_traits<graph>::
        edge_descriptor;
   std::vector<ed> v(boost::num_edges(g));
   const auto eip = edges(g);
   std::copy(eip.first, eip.second, std::begin(v));
   return v;
}
```

The only difference is that instead of the function 'vertices' (not boost::vertices!), 'edges' (not boost::edges!) is used.

Algorithm 20 demonstrates the 'get_edge_descriptor', by showing that empty graphs do not have any edge descriptors.

Algorithm 20 Demonstration of get edge descriptors

```
#include <cassert>
#include "create_empty_directed_graph.h"
#include "create_empty_undirected_graph.h"
#include "get_edge_descriptors.h"

void get_edge_descriptors_demo() noexcept
{
    const auto g = create_empty_directed_graph();
    const auto eds_g = get_edge_descriptors(g);
    assert(eds_g.empty());

const auto h = create_empty_undirected_graph();
    const auto eds_h = get_edge_descriptors(h);
    assert(eds_h.empty());
}
```

2.14 Creating a directed graph

Finally, we are going to create a directed non-empty graph!

2.14.1 Graph

This directed graph is a two-state Markov chain, with two vertices and four edges, as depicted in figure 6:

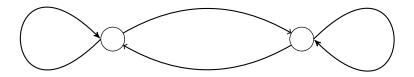


Figure 6: The two-state Markov chain

Note that directed graphs can have edges that start and end in the same vertex. These are called self-loops.

2.14.2 Function to create such a graph

To create this two-state Markov chain, the following code can be used:

Algorithm 21 Creating the two-state Markov chain as depicted in figure 6

```
#include <cassert>
#include "create empty directed graph.h"
boost::adjacency list <>
create markov chain() noexcept
  auto g = create_empty_directed_graph();
  const auto vd_a = boost::add_vertex(g);
  const auto vd_b = boost::add_vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer bb = boost::add edge(vd b, vd b, g);
  assert (aer bb.second);
  return g;
```

Instead of typing the complete type, we call the 'create_empty_directed_graph' function, and let auto figure out the type. The vertex descriptors (see chapter 2.6) created by two boost::add_vertex calls are stored to add an edge to the graph. Then boost::add_edge is called four times. Every time, its return type (see chapter 2.10) is checked for a successfull insertion.

Note that the graph lacks all properties: nodes do not have names, nor do edges.

2.14.3 Creating such a graph

Algorithm 22 demonstrates the 'create_markov_chain_graph' function and checks if it has the correct amount of edges and vertices:

Algorithm 22 Demonstration of the 'create markov chain'

```
#include <cassert>
#include "create_markov_chain.h"

void create_markov_chain_demo() noexcept
{
   const auto g = create_markov_chain();
   assert(boost::num_vertices(g) == 2);
   assert(boost::num_edges(g) == 4);
}
```

2.14.4 The .dot file produced

Running a bit ahead, this graph can be converted to a .dot file using the 'save_graph_to_dot' function (algorithm 52). The .dot file created is displayed in algorithm 23:

Algorithm 23 .dot file created from the 'create_markov_chain_graph' function (algorithm 21), converted from graph to .dot file using algorithm 52

```
digraph G {
0;
1;
0->0;
0->1;
1->0;
1->1;
1->1;
```

From the .dot file one can already see that the graph is directed, because:

- The first word, 'digraph', denotes a directed graph (where 'graph' would have indicated an undirectional graph)
- The edges are written as '->' (where undirected connections would be written as '-')

2.14.5 The .svg file produced

The .svg file of this graph is shown in figure 7:



Figure 7: .svg file created from the 'create_markov_chain' function (algorithm 21) its .dot file and converted from .dot file to .svg using algorithm 361

This figure shows that the graph in directed, as the edges have arrow heads. The vertices display the node index, which is the default behavior.

2.15 Creating K_2 , a fully connected undirected graph with two vertices

Finally, we are going to create an undirected non-empty graph!

2.15.1 Graph

To create a fully connected undirected graph with two vertices (also called K_2), one needs two vertices and one (undirected) edge, as depicted in figure 8.



Figure 8: K_2 : a fully connected undirected graph with two vertices

2.15.2 Function to create such a graph

To create K_2 , the following code can be used:

Algorithm 24 Creating K_2 as depicted in figure 8

```
#include "create_empty_undirected_graph.h"

boost:: adjacency_list <
   boost:: vecS,
  boost:: vecS,
  boost:: undirectedS
>
create_k2_graph() noexcept
{
  auto g = create_empty_undirected_graph();
  const auto vd_a = boost::add_vertex(g);
  const auto vd_b = boost::add_vertex(g);
  const auto aer = boost::add_edge(vd_a, vd_b, g);
  assert(aer.second);
  return g;
}
```

This code is very similar to the 'add_edge' function (algorithm 15). Instead of typing the graph its type, we call the 'create_empty_undirected_graph' function and let auto figure it out. The vertex descriptors (see chapter 2.6) created by two boost::add_vertex calls are stored to add an edge to the graph. From boost::add_edge its return type (see chapter 2.10), it is only checked that insertion has been successfull.

Note that the graph lacks all properties: nodes do not have names, nor do edges.

2.15.3 Creating such a graph

Algorithm 25 demonstrates how to 'create_k2_graph' and checks if it has the correct amount of edges and vertices:

Algorithm 25 Demonstration of 'create k2 graph'

```
#include <cassert>
#include "create_k2_graph.h"

void create_k2_graph_demo() noexcept
{
   const auto g = create_k2_graph();
   assert(boost::num_vertices(g) == 2);
   assert(boost::num_edges(g) == 1);
}
```

2.15.4 The .dot file produced

Running a bit ahead, this graph can be converted to the .dot file as shown in algorithm 26:

Algorithm 26 .dot file created from the 'create_k2_graph' function (algorithm 24), converted from graph to .dot file using algorithm 52

```
graph G {
0;
1;
0--1;
}
```

From the .dot file one can already see that the graph is undirected, because:

- The first word, 'graph', denotes an undirected graph (where 'digraph' would have indicated a directional graph)
- The edge between 0 and 1 is written as '-' (where directed connections would be written as '->', '<-' or '<>')

2.15.5 The .svg file produced

Continuing to running a bit ahead, this .dot file can be converted to the .svg as shown in figure 9:

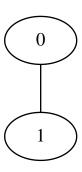


Figure 9: .svg file created from the 'create_k2_graph' function (algorithm 24) its .dot file, converted from .dot file to .svg using algorithm 361

Also this figure shows that the graph in undirected, otherwise the edge would have one or two arrow heads. The vertices display the node index, which is the default behavior.

2.16 \triangleright Creating K_3 , a fully connected undirected graph with three vertices

This is an extension of the previous chapter

2.16.1 Graph

To create a fully connected undirected graph with two vertices (also called K_2), one needs two vertices and one (undirected) edge, as depicted in figure 10.

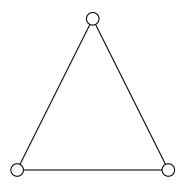


Figure 10: K_3 : a fully connected graph with three edges and vertices

2.16.2 Function to create such a graph

To create K_3 , the following code can be used:

Algorithm 27 Creating K_3 as depicted in figure 10

```
#include <cassert>
#include "create_empty_undirected_graph.h"
#include "create k3 graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS
create_k3_graph() noexcept
  auto g = create_empty_undirected_graph();
  const auto vd_a = boost::add_vertex(g);
  const auto vd_b = boost::add_vertex(g);
  const auto vd c = boost::add_vertex(g);
  const auto aer a = boost::add edge(vd a, vd b, g);
  assert (aer_a.second);
  const auto aer b = boost::add edge(vd b, vd c, g);
  assert (aer b.second);
  const auto aer c = boost::add edge(vd c, vd a, g);
  assert (aer c.second);
  return g;
```

2.16.3 Creating such a graph

Algorithm 28 demonstrates how to 'create_k2_graph' and checks if it has the correct amount of edges and vertices:

Algorithm 28 Demonstration of 'create k3 graph'

```
#include "create_k3_graph.h"

void create_k3_graph_demo() noexcept
{
  const auto g = create_k3_graph();
  assert(boost::num_edges(g) == 3);
  assert(boost::num_vertices(g) == 3);
}
```

2.16.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 29:

Algorithm 29 .dot file created from the 'create_k3_graph' function (algorithm 27), converted from graph to .dot file using algorithm 52

```
graph G {
0;
1;
2;
0--1;
1--2;
2--0;
}
```

2.16.5 The .svg file produced

Continuing to running a bit ahead, this .dot file can be converted to the .svg as shown in figure 11:

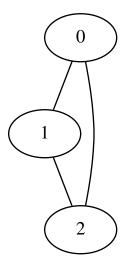


Figure 11: .svg file created from the 'create_k3_graph' function (algorithm 27) its .dot file, converted from .dot file to .svg using algorithm 361

2.17 Creating a path graph

A path graph is a linear graph without any branches

2.17.1 Graph

Here I show a path graph with four vertices (see figure 12):



Figure 12: A path graph with four vertices

2.17.2 Function to create such a graph

To create a path graph, the following code can be used:

Algorithm 30 Creating a path graph as depicted in figure 12

```
#include "create empty undirected graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS
create path graph(const int n vertices) noexcept
  assert(n vertices >= 2);
  auto g = create_empty_undirected_graph();
  auto vd 1 = boost :: add vertex(g);
  for (int i=1; i!=n vertices; ++i)
    auto vd_2 = boost::add_vertex(g);
    const auto aer = boost::add_edge(vd_1, vd_2, g);
    assert (aer.second);
    vd 1 = vd 2;
  return g;
}
```

2.17.3 Creating such a graph

Algorithm 31 demonstrates how to 'create_k2_graph' and checks if it has the correct amount of edges and vertices:

Algorithm 31 Demonstration of 'create path graph'

```
#include <cassert>
#include "create_path_graph.h"

void create_path_graph_demo() noexcept
{
   const auto g = create_path_graph(4);
   assert(boost::num_edges(g) == 3);
   assert(boost::num_vertices(g) == 4);
}
```

2.17.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 32:

Algorithm 32 .dot file created from the 'create_path_graph' function (algorithm 30), converted from graph to .dot file using algorithm 52

```
graph G {
0;
1;
2;
3;
0--1;
1--2;
2--3;
}
```

2.17.5 The .svg file produced

The .dot file can be converted to the .svg as shown in figure 13:

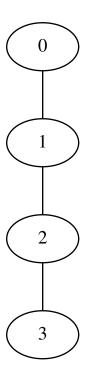


Figure 13: .svg file created from the 'create_path_graph' function (algorithm 30) its .dot file, converted from .dot file to .svg using algorithm 361

2.18 ► Creating a Peterson graph

A Petersen graph is the first graph with interesting properties.

2.18.1 Graph

To create a Petersen graph, one needs five vertices and five undirected edges, as depicted in figure 14.

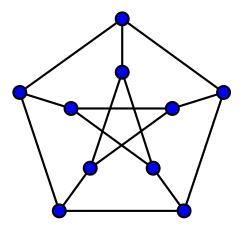


Figure 14: A Petersen graph (from https://en.wikipedia.org/wiki/Petersen_graph)

2.18.2 Function to create such a graph

To create a Petersen graph, the following code can be used:

Algorithm 33 Creating Petersen graph as depicted in figure 14

```
#include < cassert >
#include < vector >
#include "create empty undirected graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS
create petersen graph() noexcept
  using vd = decltype(create_empty_undirected_graph())::
     vertex descriptor;
  auto g = create empty undirected graph();
  std::vector < vd > v; //Outer
  for (int i = 0; i! = 5; ++i) {
    v.push_back(boost::add_vertex(g));
  std:: vector < vd > w; //Inner
  for (int i = 0; i! = 5; ++i) {
    w.push back(boost::add vertex(g));
  // Outer ring
  for (int i=0; i!=5; ++i) {
    const auto aer
      = boost::add edge(v[i], v[(i+1) \% 5], g);
    assert (aer.second);
  //Spoke
  for (int i = 0; i! = 5; ++i) {
    const auto aer
      = boost::add\_edge(v[i], w[i], g);
    assert (aer.second);
  }
  //Inner pentagram
  for (int i = 0; i! = 5; ++i) {
    const auto aer
      = boost::add edge(w[i], w[(i + 2) % 5], g);
    assert (aer.second);
  return g;
}
```

2.18.3 Creating such a graph

Algorithm 34 demonstrates how to use 'create_petersen_graph' and checks if it has the correct amount of edges and vertices:

Algorithm 34 Demonstration of 'create_k3_graph'

```
#include <cassert>
#include "create_petersen_graph.h"

void create_petersen_graph_demo() noexcept
{
   const auto g = create_petersen_graph();
   assert(boost::num_edges(g) == 15);
   assert(boost::num_vertices(g) == 10);
}
```

2.18.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 35:

Algorithm 35 .dot file created from the 'create_petersen_graph' function (algorithm 33), converted from graph to .dot file using algorithm 52

```
graph G {
0;
1;
2;
3;
4;
5;
6;
7;
8;
9;
0--1;
1--2;
2--3;
3--4;
4--0;
0--5;
1--6;
2--7;
3--8;
4--9;
5--7;
6--8;
7--9;
8--5;
9--6;
}
```

2.18.5 The .svg file produced

This . dot file can be converted to the .svg as shown in figure $15\colon$

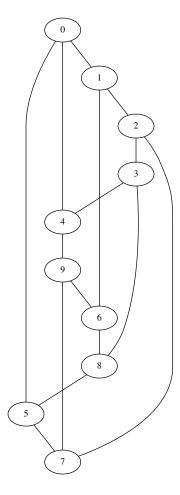


Figure 15: .svg file created from the 'create_petersen_graph' function (algorithm 33) its .dot file, converted from .dot file to .svg using algorithm 361

3 Working on graphs without properties

Now that we can build a graph, there are some things we can do.

- Getting the vertices' out degrees: see chapter 3.1
- Create a direct-neighbour subgraph from a vertex descriptor
- Create all direct-neighbour subgraphs from a graphs
- Saving a graph without properties to .dot file: see chapter 3.9
- \bullet Loading an undirected graph without properties from . dot file: see chapter 3.11

 Loading a directed graph without properties from .dot file: see chapter 3.10

3.1 Getting the vertices' out degree

Let's measure the out degree of all vertices in a graph!

The out degree of a vertex is the number of edges that originate at it.

The number of connections is called the 'degree' of the vertex. There are three types of degrees:

- in degree: the number of incoming connections, using 'in_degree' (not 'boost::in_edgree')
- out degree: the number of outgoing connections, using 'out_degree' (not 'boost::out edgree')
- degree: sum of the in degree and out degree, using 'degree' (not 'boost::edgree')

Algorithm 36 shows how to obtain these:

Algorithm 36 Get the vertices' out degrees

```
#include <boost/graph/adjacency_list.hpp>
#include <vector>

template <typename graph>
std::vector<int> get_vertex_out_degrees(
    const graph& g
) noexcept
{
    using vd = typename graph::vertex_descriptor;

    std::vector<int> v(boost::num_vertices(g));
    const auto vip = vertices(g);
    std::transform(vip.first, vip.second, std::begin(v),
        [g](const vd& d) {
        return out_degree(d,g);
    }
    );
    return v;
}
```

The structure of this algorithm is similar to 'get_vertex_descriptors' (algorithm 13), except that the out degrees from the vertex descriptors are stored. The out degree of a vertex iterator is obtained from the function 'out_degree' (not boost::out_degree!).

Albeit that the K_2 graph and the two-state Markov chain are rather simple, we can use it to demonstrate 'get_vertex_out_degrees' on, as shown in algorithm 37.

Algorithm 37 Demonstration of the 'get vertex out degrees' function

```
#include <cassert>
#include "create_k2_graph.h"
#include "create markov chain.h"
#include "get vertex out degrees.h"
void get vertex out degrees demo() noexcept
  const auto g = create_k2_graph();
  const std::vector<int> expected out degrees g\{1,1\};
  const std::vector<int> vertex out degrees g{
    get_vertex_out_degrees(g)
  };
  assert (expected_out_degrees_g
   == vertex out degrees g
  );
  const auto h = create_markov_chain();
  const std::vector<int> expected out degrees h\{2,2\};
  const std::vector<int> vertex_out_degrees_h{
    get vertex out degrees(h)
  };
  assert (expected_out_degrees_h
   == vertex_out_degrees_h
  );
```

It is expected that K_2 has one out-degree for every vertex, where the two-state Markov chain is expected to have two out-degrees per vertex.

3.2 Is there an edge between two vertices?

If you have two vertex descriptors, you can check if these are connected by an edge:

Algorithm 38 Check if there exists an edge between two vertices

```
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/graph_traits.hpp>

template <typename graph>
bool has_edge_between_vertices(
   const typename boost::graph_traits<graph>::
        vertex_descriptor&vd_1,
   const typename boost::graph_traits<graph>::
        vertex_descriptor&vd_2,
   const graph&g
) noexcept
{
   return edge(vd_1, vd_2, g).second;
}
```

This code uses the function 'edge' (not boost::edge: it returns a pair consisting of an edge descriptor and a boolean indicating if it is a valid edge descriptor. The boolean will be true if there exists an edge between the two vertices and false if not.

The demo shows that there is an edge between the two vertices of a K_2 graph, but there are no self-loops (edges that original and end at the same vertex).

Algorithm 39 Demonstration of the 'has edge between vertices' function

```
#include <cassert>
#include "create_k2_graph.h"
#include "has_edge_between_vertices.h"

void has_edge_between_vertices_demo() noexcept
{
   const auto g = create_k2_graph();
   const auto vd_1 = *vertices(g).first;
   const auto vd_2 = *(++vertices(g).first);
   assert( has_edge_between_vertices(vd_1, vd_2, g));
   assert(!has_edge_between_vertices(vd_1, vd_1, g));
}
```

3.3 E Get the edge between two vertices

If you have two vertex descriptors, you can use these to find the edge between them.

Algorithm 40 Get the edge between two vertices

```
#include <boost/graph/adjacency list.hpp>
#include "has_edge_between_vertices.h"
template <
  typename graph,
  typename vertex descriptor
typename boost::graph traits<graph>::edge descriptor
get edge between vertices (
  const vertex descriptor & vd from,
  const vertex descriptor& vd to,
  const graph& g
 noexcept
{
  assert (has edge between vertices (vd from, vd to, g));
  const auto er = edge(vd from, vd to, g);
  assert (er.second);
  return er.first;
```

This code does assume that there is an edge between the two vertices.

The demo shows how to get the edge between two vertices, deleting it, and checking for success.

Algorithm 41 Demonstration of the 'get edge between vertices' function

```
#include <cassert>
#include "create_k2_graph.h"
#include "get_edge_between_vertices.h"

void get_edge_between_vertices_demo() noexcept
{
    auto g = create_k2_graph();
    const auto vd_1 = *vertices(g).first;
    const auto vd_2 = *(++vertices(g).first);
    assert(has_edge_between_vertices(vd_1, vd_2, g));
    const auto ed = get_edge_between_vertices(vd_1, vd_2, g);
    boost::remove_edge(ed, g);
    assert(boost::num_edges(g) == 0);
}
```

3.4 Create a direct-neighbour subgraph from a vertex descriptor

Suppose you have a vertex of interest its vertex descriptor. Let's say you want to get a subgraph of that vertex and its direct neighbours only. This means that all vertices of that subgraph are adjacent vertices and that the edges go either from focal vertex to its neighbours, or from adjacent vertex to adjacent neighbour.

Here is the 'create direct neighbour subgraph' code:

Algorithm 42 Get the direct-neighbour subgraph from a vertex descriptor

```
#include <map>
\#include <boost / graph / adjacency \_ list . hpp>
template < typename graph, typename vertex descriptor >
graph create_direct_neighbour_subgraph(
  const vertex_descriptor& vd,
  const graph& g
{
  graph h;
  std::map<vertex_descriptor, vertex_descriptor> m;
    const auto vd_h = boost::add_vertex(h);
    m. insert (std::make pair (vd, vd h));
  //Copy vertices
    const auto vdsi = boost::adjacent_vertices(vd, g);
    std::transform(vdsi.first, vdsi.second,
      std :: inserter(m, std :: begin(m)),
      [&h] (const vertex descriptor& d)
        const auto vd h = boost :: add vertex(h);
        return std::make_pair(d,vd_h);
    );
  //Copy edges
    const auto eip = edges(g);
    const auto j = eip.second;
    for (auto i = eip.first; i!=j; ++i)
      const auto vd from = source(*i, g);
      const auto vd_to = target(*i, g);
      if (m. find (vd from) = std :: end (m)) continue;
      if (m. find (vd to) == std :: end (m)) continue;
      const auto aer = boost::add edge(m[vd from],m[vd to
          ], h);
      assert (aer.second);
    }
  return h;
}
```

This demonstration code shows that the direct-neighbour graph of each vertex of a K_2 graphs is ... a K_2 graph!

Algorithm 43 Demo of the 'create_direct_neighbour subgraph' function

3.5 Creating all direct-neighbour subgraphs from a graph without properties

Using the previous function, it is easy to create all direct-neighbour subgraphs from a graph without properties:

Algorithm 44 Create all direct-neighbour subgraphs from a graph without properties

```
#include < vector >
#include "create direct neighbour subgraph.h"
template <typename graph>
std::vector<graph> create_all_direct_neighbour_subgraphs(
  const graph g
) noexcept
{
  using vd = typename graph::vertex descriptor;
  std::vector < graph > v;
  v.resize(boost::num_vertices(g));
  const auto vip = vertices(g);
  std::transform(
    vip.first , vip.second,
    std :: begin(v),
    [g](const vd& d)
      return create_direct_neighbour_subgraph(
        d, g
      );
    }
  );
  {\bf return}\ v\,;
```

This demonstration code shows that all two direct-neighbour graphs of a K_2 graphs are ... K_2 graphs!

Algorithm 45 Demo of the 'create_all_direct_neighbour_subgraphs' function

3.6 Are two graphs isomorphic?

You may want to check if two graphs are isomorphic. That is: if they have the same shape.

Algorithm 46 Check if two graphs are isomorphic

```
#include <boost/graph/isomorphism.hpp>

template <typename graph1, typename graph2>
bool is_isomorphic(
   const graph1 g,
   const graph2 h
) noexcept
{
   return boost::isomorphism(g,h);
}
```

This demonstration code shows that a K_3 graph is not equivalent to a 3-vertices path graph:

Algorithm 47 Demo of the 'is_isomorphic' function

```
#include <cassert >
#include "create_path_graph.h"
#include "create_k3_graph.h"
#include "is_isomorphic.h"

void is_isomorphic_demo() noexcept
{
   const auto g = create_path_graph(3);
   const auto h = create_k3_graph();
   assert(is_isomorphic(g,g));
   assert(!is_isomorphic(g,h));
}
```

3.7 Count the number of connected components in an directed graph

A directed graph may consist out of two components, that are connect within each, but unconnected between them. Take for example, a graph of two isolated edges, with four vertices.

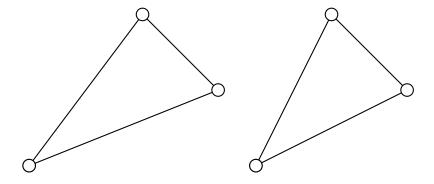


Figure 16: Example of a directed graph with two components

This algorithm counts the number of connected components:

Algorithm 48 Count the number of connected components

```
#include <vector>
#include <boost/graph/adjacency_list.hpp>
#include <boost/graph/strong_components.hpp>

template <typename graph>
int count_directed_graph_connected_components(
    const graph& g
) noexcept
{
    std::vector < int > c(boost::num_vertices(g));
    const int n = boost::strong_components(g,
        boost::make_iterator_property_map(
        std::begin(c),
        get(boost::vertex_index, g)
    )
    );
    return n;
}
```

The complexity of this algorithm is O(|V| + |E|).

This demonstration code shows that two solitary edges are correctly counted as being two components:

Algorithm 49 Demo of the 'count_directed_graph_connected_components' function

```
#include <cassert>
#include "create empty directed graph.h"
#include "add_edge.h"
#include "count_directed_graph_connected_components.h"
void count directed graph connected components demo()
   noexcept
  auto g = create empty directed graph();
  assert (count directed graph connected components (g) ==
     0);
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto vd c = boost :: add vertex(g);
  boost::add edge(vd a, vd b, g);
  boost::add edge(vd b, vd c, g);
  boost::add_edge(vd_c, vd_a, g);
  assert (count_directed_graph_connected_components(g) ==
  const auto vd d = boost::add vertex(g);
  const auto vd_e = boost::add_vertex(g);
  const auto vd f = boost::add vertex(g);
  boost::add edge(vd d, vd e, g);
  boost::add edge(vd e, vd f, g);
  boost::add_edge(vd_f, vd_d, g);
  assert (count directed graph connected components (g) ==
     2);
}
```

3.8 Count the number of connected components in an undirected graph

An undirected graph may consist out of two components, that are connect within each, but unconnected between them. Take for example, a graph of two isolated edges, with four vertices.

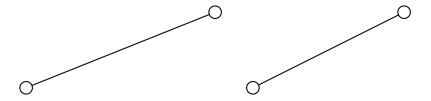


Figure 17: Example of an undirected graph with two components

This algorithm counts the number of connected components:

Algorithm 50 Count the number of connected components

```
#include < vector >
#include <boost/graph/adjacency list.hpp>
#include <boost/graph/isomorphism.hpp>
\#include <boost/graph/connected_components.hpp>
template <typename graph>
int count undirected graph connected components (
  const graph& g
 noexcept
  std::vector < int> c(boost::num_vertices(g));
  const int n = boost::connected components(g,
    boost::make_iterator_property_map(
      std::begin(c),
      get(boost::vertex_index, g)
    )
  );
  return n;
```

The complexity of this algorithm is O(|V| + |E|).

This demonstration code shows that two solitary edges are correctly counted as being two components:

Algorithm 51 Demo of the 'count_undirected_graph_connected_components' function

```
#include < cassert >
#include "create empty undirected graph.h"
#include "add edge.h"
#include "count_undirected_graph_connected_components.h"
void count undirected graph connected components demo()
   noexcept
{
    auto g = create empty undirected graph();
    assert (count undirected graph connected components (g)
        == 0);
    add edge(g);
    assert (count undirected graph connected components (g)
        == 1);
    add edge(g);
    assert (count undirected graph connected components (g)
        == 2);
}
```

3.9 Saving a graph to a .dot file

Graph are easily saved to a file, thanks to Graphviz. Graphviz (short for Graph Visualization Software) is a package of open-source tools for drawing graphs. It uses the DOT language for describing graphs, and these are commonly stored in (plain-text) .dot files (I show .dot file of every non-empty graph created, e.g. chapters 2.14.4 and 2.15.4)

Algorithm 52 Saving a graph to a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>

template <typename graph>
void save_graph_to_dot(
   const graph& g,
   const std::string& filename
) noexcept
{
   std::ofstream f(filename);
   boost::write_graphviz(f,g);
}
```

All the code does is create an std::ofstream (an output-to-file stream) and use boost::write_graphviz to write the DOT description of our graph to that stream. Instead of 'std::ofstream', one could use std::cout (a related output stream) to display the DOT language on screen directly.

Algorithm 53 shows how to use the 'save graph to dot' function:

Algorithm 53 Demonstration of the 'save graph to dot' function

```
#include "create_k2_graph.h"
#include "create_markov_chain.h"
#include "save_graph_to_dot.h"

void save_graph_to_dot_demo() noexcept
{
  const auto g = create_k2_graph();
  save_graph_to_dot(g, "create_k2_graph.dot");

  const auto h = create_markov_chain();
  save_graph_to_dot(h, "create_markov_chain.dot");
}
```

When using the 'save_graph_to_dot' function (algorithm 52), only the structure of the graph is saved: all other properties like names are not stored. Algorithm 109 shows how to do so.

3.10 Loading a directed graph from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph is loaded, as shown in algorithm 54:

Algorithm 54 Loading a directed graph from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create_empty_directed_graph.h"
#include "is_regular_file.h"

boost::adjacency_list <>
load_directed_graph_from_dot(
    const std::string& dot_filename));
    std::ifstream f(dot_filename.c_str());
    auto g = create_empty_directed_graph();
    boost::dynamic_properties dp(
        boost::ignore_other_properties
);
    boost::read_graphviz(f,g,dp);
    return g;
}
```

In this algorithm, first it is checked if the file to load exists, using the 'is_regular_file' function (algorithm 362), after which an std::ifstream is opened. Then an empty directed graph is created, which saves us writing down the template arguments explicitly. Then, a boost::dynamic_properties is created with the 'boost::ignore_other_properties' in its constructor (using a default constructor here results in the run-time error 'property not found: node_id', see chapter 24.5). From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

Algorithm 55 shows how to use the 'load_directed_graph_from_dot' function:

Algorithm 55 Demonstration of the 'load_directed_graph_from_dot' function

```
#include < cassert >
#include "create markov chain.h"
#include "load_directed_graph_from_dot.h"
#include "save_graph_to_dot.h"
void load directed graph from dot demo() noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g = create markov chain();
  const std::string filename{
    "create markov chain.dot"
  };
  save graph to dot(g, filename);
  const auto h = load_directed_graph from dot(filename);
  assert(num edges(g) == num edges(h));
  assert(num \ vertices(g) == num \ vertices(h));
}
```

This demonstration shows how the Markov chain is created using the 'create_markov_chain_graph' function (algorithm 21), saved and then loaded. The loaded graph is then checked to be a two-state Markov chain.

3.11 Loading an undirected graph from a .dot file

Loading an undirected graph from a .dot file is very similar to loading a directed graph from a .dot file, as shown in chapter 3.10. Algorithm 56 show how to do so:

Algorithm 56 Loading an undirected graph from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create empty undirected graph.h"
#include "is regular file.h"
boost::adjacency list <
  boost::vecS,
  boost :: vecS,
  boost::undirectedS
load undirected graph from dot (
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g = create_empty_undirected_graph();
  boost::dynamic_properties p(
    boost::ignore_other_properties
  boost::read graphviz(f,g,p);
  return g;
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 3.10 describes the rationale of this function

Algorithm 57 shows how to use the 'load_undirected_graph_from_dot' function:

Algorithm 57 Demonstration of the 'load_undirected_graph_from_dot' function

This demonstration shows how the K_2 graph is created using the 'create_k2_graph' function (algorithm 24), saved and then loaded. The loaded graph is checked to be a K_2 graph.

4 Building graphs with named vertices

Up until now, the graphs created have had edges and vertices without any propery. In this chapter, graphs will be created, in which the vertices can have a name. This name will be of the std::string data type, but other types are possible as well. There are many more built-in properties edges and nodes can have (see chapter 25.1 for a list).

In this chapter, we will build the following graphs:

- \bullet An empty directed graph that allows for vertices with names: see chapter 4.1
- An empty undirected graph that allows for vertices with names: see chapter 4.2
- Two-state Markov chain with named vertices: see chapter 4.5
- K_2 with named vertices: see chapter 4.6

In the process, some basic (sometimes bordering trivial) functions are shown:

- Adding a named vertex: see chapter 4.3
- Getting the vertices' names: see chapter 4.4

After this chapter you may want to:

- Building graphs with named edges and vertices: see chapter 6
- Building graphs with bundled vertices: see chapter 8
- Building graphs with custom vertices: see chapter 12
- Building graphs with a graph name: see chapter 20

4.1 Creating an empty directed graph with named vertices

Let's create a trivial empty directed graph, in which the vertices can have a name:

Algorithm 58 Creating an empty directed graph with named vertices

```
#include <string>
#include <boost/graph/adjacency_list.hpp>

boost:: adjacency_list <
   boost:: vecS ,
   boost:: vecS ,
   boost:: directedS ,
   boost:: property <
       boost:: vertex_name_t , std:: string
   >
   create_empty_directed_named_vertices_graph() noexcept
{
   return {};
}
```

Instead of using a boost::adjacency_list with default template argument, we will now have to specify four template arguments, where we only set the fourth to a non-default value.

Note there is some flexibility in this function: the data type of the vertex names is set to std::string by default, but can be of any other type if desired.

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)

- is directed (due to the boost::directedS)
- The vertices have one property: they have a name, which is of data type std::string (due to the boost::property
boost::vertex name t, std::string>')
- Edges and graph have no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fourth template argument 'boost::property
boost::vertex_name_t, std::string>'. This can be read as: "vertices have the
property 'boost::vertex_name_t', that is of data type 'std::string"'. Or simply: "vertices have a name that is stored as a std::string".

Algorithm 59 shows how to create such a graph:

```
Algorithm
                \mathbf{59}
                         Demonstration
                                           of
                                                  the
                                                           'cre-
ate empty directed named vertices graph' function
#include <cassert>
#include <boost/graph/adjacency list.hpp>
#include "create empty directed named vertices graph.h"
void create empty named directed vertices graph demo()
   noexcept
{
  const auto g
    = create empty directed named vertices graph();
  assert (boost:: num vertices (g) = 0);
  assert(boost::num edges(g) == 0);
```

4.2 Creating an empty undirected graph with named vertices

Let's create a trivial empty undirected graph, in which the vertices can have a name:

Algorithm 60 Creating an empty undirected graph with named vertices

```
#include <string>
#include <boost/graph/adjacency_list.hpp>

boost:: adjacency_list <
   boost:: vecS ,
   boost:: vecS ,
   boost:: undirectedS ,
   boost:: property <
      boost:: vertex_name_t , std:: string
>
create_empty_undirected_named_vertices_graph() noexcept
{
   return {};
}
```

This code is very similar to the code described in chapter 4.1, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS). See chapter 4.1 for most of the explanation.

Algorithm 61 shows how to create such a graph:

4.3 Add a vertex with a name

Adding a vertex without a name was trivially easy (see chapter 2.5). Adding a vertex with a name takes slightly more work, as shown by algorithm 62:

Algorithm 62 Adding a vertex with a name

```
#include < string>
#include <type_traits>
#include <boost/graph/adjacency list.hpp>
template <typename graph>
typename boost::graph traits<graph>::vertex descriptor
add named vertex (
  const std::string& vertex name,
  graph& g
 noexcept
  static assert (!std::is const<graph>::value,
    "graph_cannot_be_const"
  const auto vd = boost::add vertex(g);
  auto vertex name map = get (
      boost::vertex name, g
    );
  put(vertex name map, vd, vertex name);
  return vd;
}
```

Instead of calling 'boost::add_vertex' with an additional argument containing the name of the vertex⁶, multiple things need to be done:

First, the static_assert at the top of the function checks during compiling if the function is called with a non-const graph. One can freely omit this static_assert: you will get a compiler error anyways, be it a less helpful one.

When adding a new vertex to the graph, the vertex descriptor (as described in chapter 2.6) is stored.

The name map is obtained from the graph using 'get'. 'get' (not boost::get) allow to obtain a property map. In this case, 'get(boost::vertex_name,g)' denotes that we want to obtain the property map associated with 'boost::vertex_name' from the graph. 'get' has no 'boost::' prepending it, as it lives in the same (global) namespace the function is in. Using 'boost::get' will not compile.

With a name map and a vertex descriptor, the name of a vertex can be set using 'put' (not boost::put). 'put' is the opposite of 'get'. In this case 'put(vertex_name_map, vd, vertex_name)' is read as: in the vertex name map, look up the spot where the vertex we have the descriptor of, and put the new vertex name there. An alternative syntax is 'vertex_name_map[vd] =

⁶I am unsure if this would have been a good interface. I am sure I expected this interface myself. I do see a problem with multiple properties and the order of initialization, but initialization could simply follow the same order as the the property list.

vertex_name'. Because 'put' is more general, it is chosen to be the preferred syntax for this tutorial.

Using 'add_named_vertex' is straightforward, as demonstrated by algorithm 63.

Algorithm 63 Demonstration of 'add_named_vertex'

4.4 Getting the vertices' names

When the vertices of a graph have named vertices, one can extract them as such:

Algorithm 64 Get the vertices' names

```
#include < string>
#include < vector >
#include <boost/graph/adjacency list.hpp>
#include <boost/graph/properties.hpp>
#include <boost/graph/graph traits.hpp>
template <typename graph>
std::vector<std::string> get vertex names(
  const graph& g
 noexcept
{
  using vd = typename graph::vertex descriptor;
  std::vector<std::string> v(boost::num_vertices(g));
  const auto vip = vertices(g);
  std::transform(vip.first, vip.second, std::begin(v),
    [g](const vd& d)
      const auto vertex_name_map = get (
        boost::vertex name, g
      return get (vertex name map, d);
    }
  );
  {\bf return}\ v\,;
```

This code is very similar to 'get_vertex_out_degrees' (algorithm 36), as also there we iterated through all vertices, accessing all vertex descriptors sequentially.

The names of the vertices are obtained from a boost::property_map and then put into a std::vector.

The order of the vertex names may be different after saving and loading.

When trying to get the vertices' names from a graph without vertices with names, you will get the error 'formed reference to void' (see chapter 24.1).

Algorithm 65 shows how to add two named vertices, and check if the added names are retrieved as expected.

Algorithm 65 Demonstration of 'get vertex names'

```
#include <cassert>
#include "add named vertex.h"
#include "create empty undirected named vertices graph.h"
#include "get vertex names.h"
void get vertex names demo() noexcept
  auto g
    = create empty undirected named vertices graph();
  const std::string vertex name 1{"Chip"};
  const std::string vertex name 2{"Chap"};
  add_named_vertex(vertex_name_1, g);
  add named vertex (vertex name 2, g);
  const std::vector<std::string> expected names{
    vertex name 1, vertex name 2
  };
  const std::vector<std::string> vertex names{
    get_vertex_names(g)
  assert (expected names == vertex names);
}
```

4.5 Creating a Markov chain with named vertices

Let's create a directed non-empty graph with named vertices!

4.5.1 Graph

We extend the Markov chain of chapter 2.14 by naming the vertices 'Good' and 'Not bad', as depicted in figure 18:

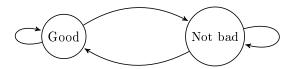


Figure 18: A two-state Markov chain where the vertices have texts

The vertex names are nonsensical, but I choose these for a reason: one name is only one word, the other has two words (as it contains a space). This will have implications for file I/O.

4.5.2 Function to create such a graph

To create this Markov chain, the following code can be used:

Algorithm 66 Creating a Markov chain with named vertices as depicted in figure 18

```
#include <cassert>
#include "add named vertex.h"
#include "create empty directed named vertices graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS,
  boost::property<boost::vertex name t, std::string>
create named vertices markov chain() noexcept
{
  auto g
    = create_empty_directed_named_vertices_graph();
  const auto vd_a = add_named_vertex("Good", g);
  const auto vd b = add named vertex("Not_bad", g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer_bb = boost::add_edge(vd_b, vd_b, g);
  assert (aer bb.second);
  return g;
}
```

Most of the code is a repeat of algorithm 21, 'create_markov_chain_graph'. In the end of the function body, the names are obtained as a boost::property_map and set to the desired values.

4.5.3 Creating such a graph

Also the demonstration code (algorithm 67) is very similar to the demonstration code of the 'create markov chain graph' function (algorithm 22).

Algorithm 67 Demonstrating the 'create_named_vertices_markov_chain' function

4.5.4 The .dot file produced

Because the vertices now have a name, this should be visible in the .dot file:

Algorithm 68 .dot file created from the 'create_named_vertices_markov_chain' function (algorithm 66), converted from graph to .dot file using algorithm 52

```
digraph G {
0[label=Good];
1[label="Not bad"];
0->0;
0->1;
1->0;
1->1;
```

As one can see, the names are stored as a label. Note that if a vertex name contains a space, the name will be surrounded by quotes, for example '1[label="Not bad"];'.

4.5.5 The .svg file produced

Now that the vertices have names, this should be reflected in the .svg:

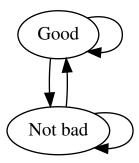


Figure 19: .svg file created from the 'create_named_vertices_markov_chain' function (algorithm 66) its .dot file, converted from .dot file to .svg using algorithm 361

The .svg now shows the vertex names, instead of the vertex indices.

4.6 Creating K_2 with named vertices

Let's create an undirected non-empty graph with named vertices!

4.6.1 Graph

We extend K_2 of chapter 2.15 by naming the vertices 'Me' and 'My computer', as depicted in figure 20:

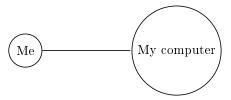


Figure 20: K_2 : a fully connected graph with two named vertices

4.6.2 Function to create such a graph

To create K_2 , the following code can be used:

Algorithm 69 Creating K_2 with named vertices as depicted in figure 20

```
#include <cassert>
#include "create_empty_undirected_named_vertices_graph.h"
#include "add named vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property\!<\!boost::vertex\_name\_t\;,std::string\!>
create named vertices k2 graph() noexcept
  auto g
    = create_empty_undirected_named_vertices_graph();
  const std::string va("Me");
  const std::string vb("My_computer");
  const auto vd_a = add_named_vertex(va, g);
  const auto vd b = add named vertex(vb, g);
  const auto aer = boost::add_edge(vd_a, vd_b, g);
  assert (aer.second);
  return g;
}
```

Most of the code is a repeat of algorithm 24. In the end, the names are obtained as a boost::property_map and set to the desired names.

4.6.3 Creating such a graph

Also the demonstration code (algorithm 70) is very similar to the demonstration code of the 'create k2 graph function' (algorithm 24).

Algorithm 70 Demonstrating the 'create k2 graph' function

4.6.4 The .dot file produced

Because the vertices now have a name, this should be visible in the .dot file:

Algorithm 71 .dot file created from the 'create_named_vertices_k2' function (algorithm 69), converted from graph to .dot file using algorithm 109

```
graph G {
O[label=Me];
1[label="My computer"];
0--1;
}
```

As one can see, the names are stored as a label. Note that if a vertex name contains a space, the name will be surrounded by quotes, for example '1[label="My computer"];'.

4.6.5 The .svg file produced

Now that the vertices have names, this should be reflected in the .svg:

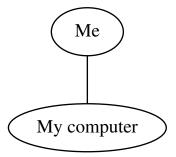


Figure 21: .svg file created from the 'create_named_vertices_k2_graph' function (algorithm 66) its .dot file, converted from .dot file to .svg using algorithm 109

The .svg now shows the vertex names, instead of the vertex indices.

4.7 \triangleright Creating K_3 with named vertices

Here we create a K_3 graph with names vertices

4.7.1 Graph

Here I show a K_3 graph with named vertices (see figure 22):

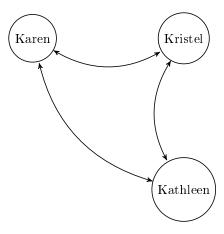


Figure 22: A K_3 graph with named vertices

4.7.2 Function to create such a graph

To create a K_3 graph with named vertices, the following code can be used:

Algorithm 72 Creating a K_3 graph as depicted in figure 22

```
#include <cassert>
#include "create_empty_undirected_named_vertices_graph.h"
#include "add named vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<boost::vertex name t, std::string>
create named vertices k3 graph() noexcept
  auto g
    = create_empty_undirected_named_vertices_graph();
  const std::string a("Karen");
  const std::string b("Kristel");
  const std::string c("Kathleen");
  const auto vd a = add named vertex(a, g);
  const auto vd_b = add_named_vertex(b, g);
  const \ auto \ vd_c = add_named_vertex(c, g);
  const auto aer a = boost::add edge(vd a, vd b, g);
  assert (aer a.second);
  {f const\ auto}\ {f aer\_b}\ =\ {f boost}:: {f add\_edge}\left({f vd\_b},\ {f vd\_c},\ {f g}\right);
  assert (aer_b.second);
  {f const\ auto}\ {f aer\_c}\ =\ {f boost}:: {f add\_edge}\left({f vd\_c}\,,\ {f vd\_a},\ {f g}\right);
  assert (aer c.second);
  return g;
```

4.7.3 Creating such a graph

Algorithm 73 demonstrates how to create a K_3 graph with named vertices and checks if it has the correct amount of edges and vertices:

Algorithm 73 Demonstration of 'create named vertices k3 graph'

```
#include <cassert>
#include "create_named_vertices_k3_graph.h"
#include "get_vertex_names.h"

void create_named_vertices_k3_graph_demo() noexcept
{
    const auto g = create_named_vertices_k3_graph();
    const std::vector<std::string> expected_names{
        "Karen", "Kristel", "Kathleen"
    };
    const std::vector<std::string> vertex_names =
        get_vertex_names(g);
    assert(expected_names == vertex_names);
}
```

4.7.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 74:

```
Algorithm 74 .dot file created from the 'create_named_vertices_k3_graph'
function (algorithm 72), converted from graph to .dot file using algorithm 52
graph G {
    [label=Karen];
    [label=Kristel];
    2[label=Kathleen];
    0--1;
    1--2;
    2--0;
}
```

4.7.5 The .svg file produced

The .dot file can be converted to the .svg as shown in figure 23:

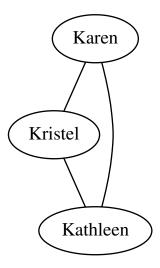


Figure 23: .svg file created from the 'create_named_vertices_k3_graph' function (algorithm 72) its .dot file, converted from .dot file to .svg using algorithm 361

4.8 Creating a path graph with named vertices

Here we create a path graph with names vertices

4.8.1 Graph

Here I show a path graph with four vertices (see figure 24):



Figure 24: A path graph with four vertices

4.8.2 Function to create such a graph

To create a path graph, the following code can be used:

Algorithm 75 Creating a path graph as depicted in figure 24

```
#include < vector >
\#include "add_named_vertex.h"
#include "create empty undirected named vertices graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex name t, std::string
>
create_named_vertices_path_graph(
  const std::vector<std::string>& names
) noexcept
  auto g = create empty undirected named vertices graph()
  if (names.size() == 0) \{ return g; \}
  auto vd_1 = add_named_vertex(*names.begin(), g);
  if (names.size() == 1) return g;
  const auto j = std::end(names);
  auto i = std::begin(names);
  for (++i; i!=j; ++i) // Skip first
    auto vd 2 = add named vertex(*i, g);
    const auto aer = boost::add edge(vd 1, vd 2, g);
    assert (aer.second);
    vd_1 = vd_2;
  return g;
```

4.8.3 Creating such a graph

Algorithm 76 demonstrates how to create a path graph with named vertices and checks if it has the correct amount of edges and vertices:

Algorithm 76 Demonstration of 'create named vertices path graph'

4.8.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 77:

Algorithm 77 .dot file created from the 'create_named_vertices_path_graph' function (algorithm 75), converted from graph to .dot file using algorithm 52

4.8.5 The .svg file produced

The .dot file can be converted to the .svg as shown in figure 25:

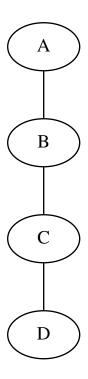


Figure 25: .svg file created from the 'create_named_vertices_path_graph' function (algorithm 75) its .dot file, converted from .dot file to .svg using algorithm 361

4.9 Creating a Petersen graph with named vertices

Here we create a Petersen graph with names vertices.

4.9.1 Graph

Here I show a Petersen graph (see figure 26):

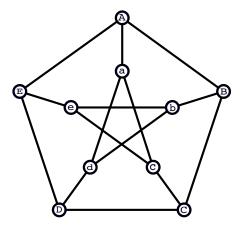


Figure 26: A Petersen graph with named vertices (modified from https://en.wikipedia.org/wiki/Petersen_graph)

4.9.2 Function to create such a graph

To create a Petersen graph with named vertices, the following code can be used:

Algorithm 78 Creating a Petersen graph as depicted in figure 26

```
#include <cassert>
#include < vector >
#include "add named vertex.h"
#include "create empty undirected named vertices graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex name t, std::string
create_named_vertices_petersen_graph() noexcept
  auto g = create empty undirected named vertices graph()
  using vd = decltype(
     create_empty_undirected_named_vertices_graph())::
      vertex descriptor;
  std:: vector < vd > v; //Outer
  for (int i = 0; i! = 5; ++i) {
    v.push back (
      add named vertex (std::string(1,'A' + i), g)
    );
  }
  std::vector < vd > w; //Inner
  for (int i = 0; i! = 5; ++i) {
    w.push_back(
      add_named_vertex(std::string(1,'a' + i), g)
    );
  }
  // Outer ring
  for (int i = 0; i! = 5; ++i) {
    const auto aer
      = boost::add edge(v[i], v[(i+1) \% 5], g);
    assert (aer.second);
  //Spoke
  for (int i = 0; i! = 5; ++i) {
    const auto aer
      = boost::add edge(v[i], w[i], g);
    assert (aer.second);
                              89
  //Inner pentagram
  for (int i = 0; i! = 5; ++i) {
    const auto aer
      = boost::add edge(w[i], w[(i + 2) % 5], g);
    assert (aer.second);
  return g;
```

4.9.3 Creating such a graph

Algorithm 79 demonstrates how to create a path graph with named vertices and checks if it has the correct amount of edges and vertices:

```
#include <cassert >
#include "create_named_vertices_petersen_graph.h"

void create_named_vertices_petersen_graph_demo() noexcept
{
  const auto g = create_named_vertices_petersen_graph();
  assert(boost::num_edges(g) == 15);
  assert(boost::num_vertices(g) == 10);
}
```

4.9.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 80:

```
ate_named_vertices_petersen_graph' function (algorithm 78), converted
from graph to .
dot file using algorithm 52
graph G {
0[label=A];
1[label=B];
2[label=C];
3[label=D];
4[label=E];
5[label=a];
6[label=b];
7[label=c];
8[label=d];
9[label=e];
0--1;
1--2;
2--3;
```

file

created

from

the

'cre-

4.9.5 The .svg file produced

Algorithm

3-4; 4-0; 0-5; 1-6; 2-7; 3-8; 4-9; 5-7; 6-8; 7-9; 8-5; 9-6; 80

.dot

The .dot file can be converted to the .svg as shown in figure 27:

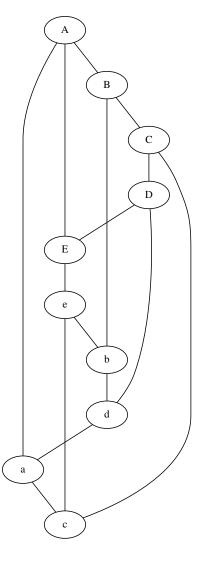


Figure 27: .svg file created from the 'create_named_vertices_petersen_graph' function (algorithm 78) its .dot file, converted from .dot file to .svg using algorithm 361

5 Working on graphs with named vertices

When vertices have names, this name gives a way to find a vertex and working with it. This chapter shows some basic operations on graphs with named vertices.

• Check if there exists a vertex with a certain name: chapter 5.1

- Find a vertex by its name: chapter 5.2
- Get a named vertex its degree, in degree and out degree: chapter: 5.3
- Get a vertex its name from its vertex descriptor: chapter 5.4
- Set a vertex its name using its vertex descriptor: chapter 5.5
- Setting all vertices' names: chapter 5.6
- Clear a named vertex its edges: chapter 5.7
- Remove a named vertex: chapter 5.8
- Removing an edge between two named vertices: chapter 5.10
- \bullet Saving an directed/undirected graph with named vertices to a .dot file: chapter 5.15
- Loading a directed graph with named vertices from a .dot file: chapter 5.16
- \bullet Loading an undirected graph with named vertices from a .dot file: chapter 5.17

Especially the 'find_first_vertex_by_name' function (chapter 5.2) is important, as it shows how to obtain a vertex descriptor, which is used in later algorithms.

5.1 Check if there exists a vertex with a certain name

Before modifying our vertices, let's first determine if we can find a vertex by its name in a graph. After obtaing a name map, we obtain the vertex iterators, dereference these to obtain the vertex descriptors and then compare each vertex its name with the one desired.

Algorithm 81 Find if there is vertex with a certain name

This function can be demonstrated as in algorithm 82, where a certain name cannot be found in an empty graph. After adding the desired name, it is found.

Algorithm 82 Demonstration of the 'has vertex with name' function

Note that this function only finds if there is at least one vertex with that

name: it does not tell how many vertices with that name exist in the graph.

5.2 Find a vertex by its name

Where STL functions work with iterators, here we obtain a vertex descriptor (see chapter 2.6) to obtain a handle to the desired vertex. Algorithm 83 shows how to obtain a vertex descriptor to the first (name) vertex found with a specific name.

Algorithm 83 Find the first vertex by its name

```
#include < cassert >
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "has vertex with name.h"
template <typename graph>
typename boost::graph traits<graph>::vertex descriptor
find_first_vertex_with_name(
  const std::string& name,
  const graph& g
 noexcept
  using vd = typename graph::vertex descriptor;
  const auto vip = vertices(g);
  const auto i = std :: find if (
    vip.first , vip.second ,
    [g, name](const vd d) {
      const auto vertex_name_map = get(boost::vertex_name
      return get (vertex name map, d) == name;
    }
  );
  assert(i != vip.second);
  return *i;
```

With the vertex descriptor obtained, one can read and modify the vertex and the edges surrounding it. Algorithm 84 shows some examples of how to do so.

Algorithm 84 Demonstration of the 'find first vertex with name' function

5.3 Get a (named) vertex its degree, in degree and out degree

We already obtained all out degrees of all vertices in chapter 3.1 by just collecting all vertex descriptors. Here, we will search for a vertex with a certain name, obtain its vertex descriptor and find the number of connections it has.

With a vertex descriptor, we can read a vertex its types of degrees. Algorithm 83 shows how to find a vertex, obtain its vertex descriptor and then obtain the out degree from it.

Algorithm 85 Get the first vertex with a certain name its out degree from its vertex descriptor

```
\#include < cassert >
#include "find_first_vertex_with_name.h"
\#include "has_vertex_with_name.\overline{h}"
\mathbf{template} \hspace{0.1cm} < \hspace{-0.1cm} \mathbf{typename} \hspace{0.1cm} \mathbf{graph} >
int get_first_vertex_with_name_out_degree(
  const std::string& name,
  const graph& g) noexcept
  const auto vd
     = find_first_vertex_with_name(name, g);
  const int od {
     static cast < int > (
        out_degree(vd, g)
  };
   assert (static cast<unsigned long>(od)
    == out_degree(vd, g)
  return od;
}
```

Algorithm 86 shows how to use this function.

Algorithm 86 Demonstration of the 'get_first_vertex_with_name_out_degree' function

```
#include <cassert>
#include "create named vertices k2 graph.h"
#include "get_first_vertex_with_name_out_degree.h"
void get first vertex with name out degree demo()
   noexcept
{
  const auto g = create_named_vertices_k2_graph();
  assert (
    get first vertex with name out degree (
       ^{\prime\prime}\mathrm{Me^{\prime\prime}} , g
    = 1
  );
  assert (
    get first vertex with name out degree (
       "My_computer", g
    ) == 1
  );
}
```

5.4 Get a vertex its name from its vertex descriptor

This may seem a trivial paragraph, as chapter 4.4 describes the 'get_vertex_names' algorithm, in which we get all vertices' names. But it does not allow to first find a vertex of interest and subsequently getting only that one its name.

To obtain the name from a vertex descriptor, one needs to pull out the name map and then look up the vertex of interest.

Algorithm 87 Get a vertex its name from its vertex descriptor

```
#include <string>
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>

template <typename graph>
std::string get_vertex_name(
    const typename boost::graph_traits<graph>::
        vertex_descriptor&vd,
    const graph&g
) noexcept
{
    const auto vertex_name_map
        = get(boost::vertex_name, g
        );
    return get(vertex_name_map, vd);
}
```

To use 'get_vertex_name', one first needs to obtain a vertex descriptor. Algorithm 88 shows a simple example:

Algorithm 88 Demonstration if the 'get vertex name' function

5.5 Set a (named) vertex its name from its vertex descriptor

If you know how to get the name from a vertex descriptor, setting it is just as easy, as shown in algorithm 89.

Algorithm 89 Set a vertex its name from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>

template <typename graph>
void set_vertex_name(
    const std::string& any_vertex_name,
    const typename boost::graph_traits<graph>::
        vertex_descriptor& vd,
    graph& g
) noexcept
{
    static_assert(!std::is_const<graph>::value,
        "graph_cannot_be_const"
);

    auto vertex_name_map
        = get(boost::vertex_name, g);
    put(vertex_name_map, vd, any_vertex_name);
}
```

To use 'set_vertex_name', one first needs to obtain a vertex descriptor. Algorithm 90 shows a simple example.

Algorithm 90 Demonstration if the 'set vertex name' function

```
#include <cassert>
#include "add named vertex.h"
#include "create empty undirected named vertices graph.h"
#include "find first vertex with name.h"
#include "get_vertex_name.h"
#include "set vertex name.h"
void set vertex_name_demo() noexcept
  auto g
    = create empty undirected named vertices graph();
  const std::string old_name{"Dex"};
  add named vertex (old name, g);
  const auto vd
    = find_first_vertex_with_name(old_name,g);
  assert(get\_vertex\_name(vd,g) = old\_name);
  const std::string new name{"Diggy"};
  set_vertex_name(new_name, vd, g);
  assert(get_vertex_name(vd,g) = new_name);
```

5.6 Setting all vertices' names

When the vertices of a graph have named vertices and you want to set all their names at once:

Algorithm 91 Setting the vertices' names

```
#include < string>
#include < vector >
#include <boost/graph/graph traits.hpp>
#include <boost/graph/properties.hpp>
template <typename graph>
void set_vertex_names(
  graph&g,
  const std::vector<std::string>& names
 noexcept
  static_assert(!std::is_const<graph>::value, "graph_
     cannot_be_const");
  const auto vertex name map
    = get(boost::vertex name,g);
  auto ni = std::begin(names);
  const auto names end = std::end(names);
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i, ++ni)
    assert (ni != names end);
    put(vertex name map, *i, *ni);
}
```

A new function makes its appearance here: 'put' (not 'boost::put'), which is the opposite of 'get' (not 'boost::get')

This is not a very usefull function if the graph is complex. But for just creating graphs for debugging, it may come in handy.

5.7 Clear the edges of a named vertex

A vertex descriptor can be used to clear all in/out/both edges connected to a vertex. It is necessary to remove these connections before the vertex itself can be removed. There are three functions to remove the edges connected to a vertex:

- boost::clear vertex: removes all edges to and from the vertex
- boost::clear_out_edges: removes all outgoing edges from the vertex (in directed graphs only, else you will get a 'error: no matching function for

call to clear_out_edges', as described in chapter 24.2)

• boost::clear_in_edges: removes all incoming edges from the vertex (in directed graphs only, else you will get a 'error: no matching function for call to clear in edges', as described in chapter 24.3)

In the algorithm 'clear_first_vertex_with_name' the 'boost::clear_vertex' algorithm is used, as the graph used is undirectional:

Algorithm 92 Clear the first vertex with a certain name

Algorithm 93 shows the clearing of the first named vertex found.

Algorithm 93 Demonstration of the 'clear first vertex with name' function

```
#include <cassert>
#include "clear_first_vertex_with_name.h"
#include "create_named_vertices_k2_graph.h"

void clear_first_vertex_with_name_demo() noexcept
{
   auto g = create_named_vertices_k2_graph();
   assert(boost::num_edges(g) == 1);
   clear_first_vertex_with_name("My_computer",g);
   assert(boost::num_edges(g) == 0);
}
```

5.8 Remove a named vertex

A vertex descriptor can be used to remove a vertex from a graph. It is necessary to remove these connections (e.g. using 'clear_first_vertex_with_name', algorithm 92) before the vertex itself can be removed.

Removing a named vertex goes as follows: use the name of the vertex to get a first vertex descriptor, then call 'boost::remove_vertex', shown in algorithm 5.8:

Algorithm 94 Remove the first vertex with a certain name

```
#include <boost/graph/adjacency list.hpp>
#include "find first vertex with name.h"
#include "has vertex with name.h"
template <typename graph>
void remove first vertex with name (
  const std::string& name,
  graph& g
  noexcept
  static _ assert (! std :: is _ const < graph >:: value,
    "graph_cannot_be_const"
  );
  assert (has vertex with name (name, g));
  const auto vd
    = find_first_vertex_with_name(name,g);
  assert(degree(vd,g) == 0);
  boost::remove vertex(vd,g);
```

Algorithm 95 shows the removal of the first named vertex found.

Algorithm 95 Demonstration of the 'remove_first_vertex_with_name' function

```
#include <cassert>
#include "clear_first_vertex_with_name.h"
#include "create_named_vertices_k2_graph.h"
#include "remove_first_vertex_with_name.h"

void remove_first_vertex_with_name_demo() noexcept
{
    auto g = create_named_vertices_k2_graph();
    clear_first_vertex_with_name(
        "My_computer",g
);
    remove_first_vertex_with_name(
        "My_computer",g
);
    assert(boost::num_edges(g) == 0);
    assert(boost::num_vertices(g) == 1);
}
```

Again, be sure that the vertex removed does not have any connections!

5.9 Adding an edge between two named vertices

Instead of looking for an edge descriptor, one can also add an edge from two vertex descriptors. Adding an edge between two named vertices named edge goes as follows: use the names of the vertices to get both vertex descriptors, then call 'boost::add edge' on those two, as shown in algorithm 96.

Algorithm 96 Adding an edge between two named vertices

```
#include <cassert>
#include < string>
#include <boost/graph/adjacency list.hpp>
#include "has vertex with name.h"
#include "find first vertex with name.h"
template <typename graph>
\mathbf{typename} \hspace{0.2cm} \texttt{boost} :: \mathtt{graph\_traits} \negthinspace < \negthinspace \mathtt{graph} \negthinspace > \negthinspace :: \mathtt{edge\_descriptor}
add edge between named vertices (
  const std::string& vertex name 1,
  const std::string& vertex name 2,
  graph& g
  noexcept
  assert (has vertex with name (vertex name 1, g));
  assert (has vertex with name (vertex name 2, g));
  const auto vd_1 = find_first_vertex_with_name(
      vertex_name_1, g);
  const auto vd_2 = find_first_vertex_with_name(
      vertex_name_2, g);
  const auto aer = boost::add edge(vd 1, vd 2, g);
  assert (aer.second);
  return aer.first;
```

Algorithm 97 shows how to add an edge between two named vertices:

Algorithm 97 Demonstration of the 'add_edge_between_named_vertices' function

```
#include <cassert>
#include "add_edge_between_named_vertices.h"
#include "add_named_vertex.h"
#include "create_empty_undirected_named_vertices_graph.h"

void add_edge_between_named_vertices_demo() noexcept
{
   auto g = create_empty_undirected_named_vertices_graph()
    ;
   add_named_vertex("Bert", g);
   add_named_vertex("Ernie", g);
   add_edge_between_named_vertices("Bert", "Ernie", g);
   assert(boost::num_edges(g) == 1);
}
```

5.10 Removing the edge between two named vertices

Instead of looking for an edge descriptor, one can also remove an edge from two vertex descriptors (which is: the edge between the two vertices). Removing an edge between two named vertices named edge goes as follows: use the names of the vertices to get both vertex descriptors, then call 'boost::remove_edge' on those two, as shown in algorithm 98.

Algorithm 98 Remove the first edge with a certain name

```
#include "find first vertex with name.h"
\#include "has_vertex_with_name.h"
#include "has edge between vertices.h"
template <typename graph>
void remove_edge_between_vertices_with_names(
  const std::string& name 1,
  const std::string& name 2,
  graph& g
 noexcept
  static_assert(!std::is_const<graph>::value,
    "graph_cannot_be_const"
  assert (has vertex with name (name 1, g));
  assert (has_vertex_with_name(name_2, g));
  const auto vd 1
    = find_first_vertex_with_name(name_1, g);
  const auto vd 2
    = find_first_vertex_with_name(name_2, g);
  assert (has edge between vertices (vd 1, vd 2, g));
  boost::remove edge(vd 1, vd 2, g);
}
```

Algorithm 99 shows the removal of the first named edge found.

```
      Algorithm
      99
      Demonstration of move_edge_between_vertices_with_names' function
      the 'remove_redge_between_vertices_with_names' function
```

5.11 Count the vertices with a certain name

How often is a vertex with a certain name present? Here we'll find out.

Algorithm 100 Find the first vertex by its name

```
#include < string>
#include <boost/graph/properties.hpp>
template <typename graph>
int count vertices with name (
  const std::string& name,
  const graph& g
) noexcept
  using vd = typename graph::vertex descriptor;
  const auto vip = vertices(g);
  const auto cnt = std::count if (
    vip.first, vip.second,
    [g, name](const vd\& d)
      {\bf const\ auto\ vertex\_name\_map}
        = get (boost :: vertex_name, g);
      \mathbf{return} name
        == get (vertex name map, d);
    }
  );
  return static cast<int>(cnt);
```

Here we use the STL std::count_if algorithm to count how many vertices have a name equal to the desired name.

Algorithm 101 shows some examples of how to do so.

Algorithm 101 Demonstration of the 'find_first_vertex_with_name' function

5.12 Create a direct-neighbour subgraph from a vertex descriptor of a graph with named vertices

Suppose you have a vertex of interest its vertex descriptor. Let's say you want to get a subgraph of that vertex and its direct neighbours only. This means that all vertices of that subgraph are adjacent vertices and that the edges go either from focal vertex to its neighbours, or from adjacent vertex to adjacent neighbour.

Here is the 'create direct neighbour subgraph' code:

Algorithm 102 Get the direct-neighbour named vertices subgraph from a vertex descriptor

```
#include <map>
#include <boost/graph/adjacency list.hpp>
#include "add named vertex.h"
#include "get_vertex_name.h"
template < typename graph, typename vertex descriptor >
graph create direct neighbour named vertices subgraph (
  const vertex descriptor& vd,
  const graph& g
{
  graph h;
  std::map<vertex_descriptor, vertex_descriptor> m;
    const auto vd h = add named vertex (
      get vertex name(vd, g), h
    m. insert (std::make_pair(vd,vd_h));
   I/Copy\ \ vertices
    const auto vdsi = boost::adjacent vertices (vd, g);
    std::transform(vdsi.first, vdsi.second,
      std::inserter(m, std::begin(m)),
      [g, &h](const vertex_descriptor&d)
        const auto vd h = add named vertex (
           get\_vertex\_name(d,g), h
        return std::make_pair(d,vd h);
    );
   /\mathit{Copy} edges
    const auto eip = edges(g);
    {f const\ auto\ j\ =\ eip.second\ ;}
    for (auto i = eip.first; i!=j; ++i)
      const auto vd_from = source(*i, g);
      const auto vd to = target(*i, g);
      if (m. find (vd_from) = std :: end (m)) continue;
      if (m. find (vd to) == std::end(m)) continue;
      const auto aer = boost::add edge(m[vd from],m[vd to
          ], h);
                             112
      assert (aer.second);
    }
  }
  return h;
```

This demonstration code shows that the direct-neighbour graph of each vertex of a K_2 graphs is ... a K_2 graph!

Algorithm 103 Demo of the 'create_direct_named_vertices_neighbour_subgraph' function

```
#include "create direct neighbour named vertices subgraph
   . h"
#include "create_named_vertices_k2_graph.h"
#include "get vertex names.h"
void create_direct_neighbour_named_vertices_subgraph_demo
   () noexcept
  const auto g = create named vertices k2 graph();
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (auto i=vip.first; i!=j; ++i) {
    const auto h =
       create direct neighbour named vertices subgraph (
      *i,g
    );
    assert(boost::num\_vertices(h) == 2);
    assert(boost::num edges(h) == 1);
    const auto v = get vertex names(h);
    std :: set < std :: string > names(std :: begin(v), std :: end(v)
    assert (names.count ("Me") == 1);
    assert (names.count ("My_computer") == 1);
  }
}
```

5.13 Creating all direct-neighbour subgraphs from a graph with named vertices

Using the previous function, it is easy to create all direct-neighbour subgraphs from a graph with named vertices:

Algorithm 104 Create all direct-neighbour subgraphs from a graph with named vertices

```
#include < vector >
#include "create_direct_neighbour_subgraph.h"
#include "create_direct_neighbour_named_vertices_subgraph
   . h"
template <typename graph>
std::vector<graph>
   create_all_direct_neighbour_named_vertices_subgraphs(
  const graph g
 noexcept
  using vd = typename graph::vertex descriptor;
  std::vector<graph> v;
  v.resize(boost::num_vertices(g));
  const auto vip = vertices(g);
  std::transform(
    vip.first , vip.second,
    std::begin(v),
    [g](const vd& d)
      return
         create direct neighbour named vertices subgraph (
      );
    }
  );
  return v;
```

This demonstration code shows that all two direct-neighbour graphs of a K_2 graphs are ... K_2 graphs!

Algorithm 105 Demo of the 'create_all_direct_neighbour_named_vertices_subgraphs' function

The sub-graphs are shown here:

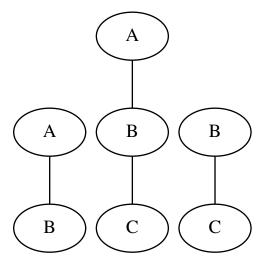


Figure 28: All subgraphs created

5.14 Are two graphs with named vertices isomorphic?

Strictly speaking, finding isomorphisms is about the shape of the graph, independent of vertex name, and is already done in chapter 3.6.

Here, it is checked if two graphs with named vertices are 'label isomorphic' (please email me a better term if you know one). That is: if they have the same shape with the same vertex names at the same places.

To do this, there are two steps needed:

- 1. Map all vertex names to an unsigned int.
- 2. Compare the two graphs with that map

Below the class 'named_vertex_invariant' is shown. Its std::map maps the vertex names to an unsigned integer, which is done in the member function 'collect_names'. The purpose of this, is that is is easier to compare integers than std::strings.

Algorithm 106 The named vertex invariant functor

```
\#include <map>
#include <boost/graph/adjacency list.hpp>
#include <boost/graph/isomorphism.hpp>
template <class graph>
struct named_vertex_invariant {
  using str to int map = std::map < std::string, size t >;
  using result_type = size_t;
  using argument type = typename graph::vertex descriptor
  const graph& m graph;
  str_to_int_map& m_mappings;
  size t operator()(argument type u) const {
      return m mappings.at(boost::get(boost::vertex name,
           m graph, u));
  size_t max() const noexcept { return m_mappings.size();
}
  void collect names() noexcept {
    for (const auto vd : boost::make iterator range(boost
        :: vertices (m_graph))) {
      const size_t next_id = m_mappings.size();
      const auto ins = m mappings.insert (
         { boost::get(boost::vertex name, m graph, vd),
            next id}
      );
       if (ins.second) {
         //\operatorname{std}::\operatorname{cout}<< "Mapped" '" << \operatorname{ins.first} -> \operatorname{first}
             "'' to " << ins. first -> second <math><< "|n";
};
```

To check for 'label isomorphism', multiple things need to be put in place for 'boost::isomorphism' to work with:

Algorithm 107 Check if two graphs with named vertices are isomorphic

```
#include "named vertex invariant.h"
#include <boost/graph/vf2 sub graph iso.hpp>
#include <boost/graph/graph utility.hpp>
template <typename graph>
bool is named vertices isomorphic (
  const graph &g,
  const graph &h
) noexcept {
  using vd = typename graph::vertex descriptor;
  auto vertex_index_map = get(boost::vertex_index, g);
  std::vector<vd> iso(boost::num_vertices(g));
  typename named vertex invariant < graph > :: str to int map
     shared names;
  named_vertex_invariant<graph> inv1{g, shared_names};
  named_vertex_invariant<graph> inv2{h, shared_names};
  inv1.collect_names();
  inv2.collect names();
  return boost::isomorphism(g, h,
    boost::isomorphism map (
      make_iterator_property_map(
        iso.begin(),
        vertex index map
    )
    .vertex_invariant1(inv1)
    .vertex_invariant2(inv2)
  );
```

This demonstration code creates three path graphs, of which two are 'label isomorphic':

Algorithm 108 Demo of the 'is named vertices isomorphic' function

5.15 Saving an directed/undirected graph with named vertices to a .dot file

If you used the 'create_named_vertices_k2_graph' function (algorithm 69) to produce a K_2 graph with named vertices, you can store these names in multiple ways:

- Using boost::make label writer
- Using a C++11 lambda function

I show both ways, because you may need all of them.

The created .dot file is shown at algorithm 71.

You can use all characters in the vertex without problems (for example: comma's, quotes, whitespace). This will not hold anymore for bundled and custom vertices in later chapters.

The 'save_named_vertices_graph_to_dot' functions below only save the structure of the graph and its vertex names. It ignores other edge and vertex properties.

5.15.1 Using boost::make label writer

The first implemention uses boost::make_label_writer, as shown in algorithm 109:

Algorithm 109 Saving a graph with named vertices to a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include <boost/graph/properties.hpp>
#include "get vertex names.h"
#include "is_graphviz_friendly.h"
template <typename graph>
void save_named_vertices_graph_to_dot(
  const graph& g,
  const std::string& filename
  noexcept
  std::ofstream f(filename);
  const auto names
    = get\_vertex\_names(g); //Can be Graphviz-unfriendly
  boost::write graphviz(
    f,
    boost::make_label_writer(&names[0])
  );
}
```

Here, the function boost::write_graphviz is called with a new, third argument. After collecting all names, these are used by boost::make_label_writer to write the names as labels.

5.15.2 Using a C++11 lambda function

An equivalent algorithm is algorithm 110:

Algorithm 110 Saving a graph with named vertices to a .dot file using a lambda expression

```
#include < string>
#include <ostream>
\#include <boost / graph / graphviz . hpp>
#include <boost/graph/properties.hpp>
#include "get vertex names.h"
template <typename graph>
void save named vertices graph to dot using lambda (
  const graph& g,
  const std::string& filename
 noexcept
{
  using vd t = typename graph::vertex descriptor;
  std::ofstream f(filename);
  const auto name_map = get(boost::vertex_name,g);
  boost::write graphviz (
    f,
    g,
    [name map](std::ostream& os, const vd t& vd) {
      const std::string s{name map[vd]};
      if (s.find(',') == std::string::npos) {
        //No\ space, no quotes around string
        os << "[label=" << s << "]";
      else {
        //Has\ space, put\ quotes\ around\ string
        os << "[label=\"" << s << "\"]";
    }
  );
}
```

In this code, a lambda function is used as a third argument.

A lambda function is an on-the-fly function that has these parts:

- the capture brackets '[]', to take variables within the lambda function
- the function argument parentheses '()', to put the function arguments in
- the function body '{}', where to write what it does

First we create a shorthand for the vertex descriptor type, that we'll need to use a lambda function argument (in C++14 you can use auto).

We then create a vertex name map at function scope (in C++17 this can be at lambda function scope) and pass it to the lambda function using its capture section.

The lambda function arguments need to be two: a std::ostream& (a reference to a general out-stream) and a vertex descriptor. In the function body, we get the name of the vertex the same as the 'get_vertex_name' function (algorithm 87) and stream it to the out stream.

5.15.3 Demonstration

Algorithm 111 shows how to use (one of) the 'save_named_vertices_graph_to_dot' function(s):

 ${\bf Algorithm~111~Demonstration~of~the~`save_named_vertices_graph_to_dot'} \\ {\bf function}$

```
#include "create_named_vertices_k2_graph.h"
#include "create_named_vertices_markov_chain.h"
#include "save_named_vertices_graph_to_dot.h"

void save_named_vertices_graph_to_dot_demo() noexcept
{
   const auto g = create_named_vertices_k2_graph();
   save_named_vertices_graph_to_dot(
      g, "create_named_vertices_k2_graph.dot"
);

const auto h = create_named_vertices_markov_chain();
   save_named_vertices_graph_to_dot(
      h, "create_named_vertices_markov_chain.dot"
);
}
```

When using the 'save_named_vertices_graph_to_dot' function (algorithm 109), only the structure of the graph and the vertex names are saved: all other properties like edge name are not stored. Algorithm 155 shows how to do so.

5.16 Loading a directed graph with named vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with named vertices is loaded, as shown in algorithm 112:

Algorithm 112 Loading a directed graph with named vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create empty directed named vertices graph.h"
#include "is regular file.h"
boost::adjacency list <
  boost::vecS,
  boost :: vecS,
  boost :: directedS,
  boost::property<
    boost::vertex name t, std::string
load_directed_named_vertices_graph_from_dot(
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot_filename.c_str());
  auto g = create_empty_directed_named_vertices_graph();
  boost::dynamic_properties dp(boost::
     ignore_other_properties);
  dp.property("label", get(boost::vertex_name, g));
  boost::read graphviz(f,g,dp);
  return g;
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Next to this, a boost::dynamic_properties is created with its default constructor, after which we direct the boost::dynamic_properties to find a 'node_id' and 'label' in the vertex name map. From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

Algorithm 113 shows how to use the 'load _ directed _ graph _ from _ dot' function:

Algorithm 113 Demonstration of the 'load_directed_named_vertices_graph_from_dot' function

```
#include "create named vertices markov chain.h"
#include "load directed named vertices graph from dot.h"
#include "save_named_vertices_graph_to_dot.h"
#include "get_vertex_names.h"
void load directed named vertices graph from dot demo()
   noexcept
  using boost::num edges;
  using boost::num_vertices;
  const auto g
    = create named vertices markov chain();
  const std::string filename{
    "create named vertices markov chain.dot"
  save named vertices graph to dot(g, filename);
  const auto h
    = load directed named vertices graph from dot (
      filename
    );
  assert(num edges(g) == num edges(h));
  assert(num \ vertices(g) == num \ vertices(h));
  assert (get vertex names (g) == get vertex names (h));
```

This demonstration shows how the Markov chain is created using the 'create_named_vertices_markov_chain' function (algorithm 21), saved and then loaded. The loaded graph is checked to be a directed graph similar to the Markov chain with the same vertex names (using the 'get_vertex_names' function, algorithm 64).

5.17 Loading an undirected graph with named vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with named vertices is loaded, as shown in algorithm 114:

Algorithm 114 Loading an undirected graph with named vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create_empty_undirected_named_vertices_graph.h"
#include "is_regular_file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex name t, std::string
load_undirected_named_vertices_graph_from_dot(
  const std::string& dot filename
  assert(is_regular_file(dot_filename));
  std::ifstream f(dot filename.c str());
  auto g = create_empty_undirected_named_vertices_graph()
  boost::dynamic properties dp(boost::
     ignore_other_properties);
 dp.property("label", get(boost::vertex_name, g));
  boost::read_graphviz(f,g,dp);
  return g;
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 5.16 describes the rationale of this function.

Algorithm 115 shows how to use the 'load_undirected_graph_from_dot' function:

Algorithm 115 Demonstration of the 'load_undirected_graph_from_dot' function

```
#include "create named vertices k2 graph.h"
#include "load undirected named vertices graph from dot.h
#include "save_named_vertices_graph to dot.h"
#include "get vertex names.h"
void load undirected named vertices graph from dot demo()
    noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create_named_vertices_k2_graph();
  const std::string filename{
    "create named vertices k2 graph.dot"
  save named vertices graph to dot(g, filename);
  const auto h
    = load undirected named vertices graph from dot(
      filename
    );
  assert(num edges(g) == num edges(h));
  assert (num vertices (g) == num vertices (h));
  assert(get\_vertex\_names(g) == get\_vertex\_names(h));
```

This demonstration shows how K_2 with named vertices is created using the 'create_named_vertices_k2_graph' function (algorithm 69), saved and then loaded. The loaded graph is checked to be an undirected graph similar to K_2 , with the same vertex names (using the 'get_vertex_names' function, algorithm 64).

6 Building graphs with named edges and vertices

Up until now, the graphs created have had edges and vertices without any propery. In this chapter, graphs will be created, in which edges vertices can have a name. This name will be of the std::string data type, but other types are possible as well. There are many more built-in properties edges and nodes can have (see the boost/graph/properties.hpp file for these).

In this chapter, we will build the following graphs:

- An empty directed graph that allows for edges and vertices with names: see chapter 6.1
- An empty undirected graph that allows for edges and vertices with names: see chapter 6.2
- Markov chain with named edges and vertices: see chapter 6.6
- K_3 with named edges and vertices: see chapter 6.8

In the process, some basic (sometimes bordering trivial) functions are shown:

- Adding an named edge: see chapter 6.3
- Getting the edges' names: see chapter 6.5

These functions are mostly there for completion and showing which data types are used.

6.1 Creating an empty directed graph with named edges and vertices

Let's create a trivial empty directed graph, in which the both the edges and vertices can have a name:

Algorithm 116 Creating an empty directed graph with named edges and vertices

```
#include <string>
#include <boost/graph/adjacency_list.hpp>

boost:: adjacency_list <
   boost:: vecS ,
   boost:: vecS ,
   boost:: directedS ,
   boost:: property < boost:: vertex_name_t , std:: string > ,
   boost:: property < boost:: edge_name_t , std:: string > >
   create_empty_directed_named_edges_and_vertices_graph()
        noexcept
{
    return {};
}
```

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)

- is directed (due to the boost::directedS)
- The vertices have one property: they have a name, that is of data type std::string (due to the boost::property< boost::vertex name t,std::string>')
- The edges have one property: they have a name, that is of data type std::string (due to the boost::property< boost::edge name t,std::string>')
- The graph has no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fifth template argument 'boost::property < boost::edge_name_t,std::string>'. This can be read as: "edges have the property 'boost::edge_name_t', that is of data type 'std::string"'. Or simply: "edges have a name that is stored as a std::string".

Algorithm 117 shows how to create this graph. Note that all the earlier functions defined in this tutorial keep working as expected.

```
        Algorithm
        117
        Demonstration
        if
        the
        'create_empty_directed_named_edges_and_vertices_graph' function
```

```
#include < cassert >
#include "add named edge.h"
#include "
   create empty directed named edges and vertices graph.h
#include "get edge names.h"
#include "get vertex names.h"
void
   create_empty_directed_named_edges_and_vertices_graph_demo
   () noexcept
  using strings = std::vector<std::string>;
  auto g
       create empty directed named edges and vertices graph
  add named edge("Reed", g);
  const strings expected vertex names{"",""};
  const strings vertex names = get vertex names(g);
  assert (expected vertex names = vertex names);
  const strings expected_edge_names{"Reed"};
  const strings edge names = get edge names(g);
  assert (expected edge names == edge names);
}
```

6.2 Creating an empty undirected graph with named edges and vertices

Let's create a trivial empty undirected graph, in which the both the edges and vertices can have a name:

Algorithm 118 Creating an empty undirected graph with named edges and vertices

```
#include <string>
#include <boost/graph/adjacency_list.hpp>

boost:: adjacency_list <
   boost:: vecS ,
   boost:: vecS ,
   boost:: undirectedS ,
   boost:: property < boost:: vertex_name_t , std:: string > ,
   boost:: property < boost:: edge_name_t , std:: string > >
   create_empty_undirected_named_edges_and_vertices_graph()
        noexcept
{
    return {};
}
```

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)
- is undirected (due to the boost::undirectedS)
- The vertices have one property: they have a name, that is of data type std::string (due to the boost::property< boost::vertex name t,std::string>')
- The edges have one property: they have a name, that is of data type std::string (due to the boost::property < boost::edge name t,std::string>')
- The graph has no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fifth template argument 'boost::property < boost::edge_name_t,std::string>'. This can be read as: "edges have the property 'boost::edge_name_t', that is of data type 'std::string''. Or simply: "edges have a name that is stored as a std::string".

Algorithm 119 shows how to create this graph. Note that all the earlier functions defined in this tutorial keep working as expected.

```
Algorithm
                 119
                           Demonstration
                                                      the
                                                                'cre-
ate\_empty\_undirected\_named\_edges\_and\_vertices\_graph' function
#include <cassert>
#include "add named edge.h"
#include "
    create\_empty\_undirected\_named\_edges\_and\_vertices\_graph
    . h"
#include "get_edge_names.h"
#include "get vertex names.h"
    create empty undirected named edges and vertices graph demo
    () noexcept
{
  \mathbf{using} \ \mathtt{strings} \ = \ \mathtt{std} :: \mathtt{vector} \! < \! \mathtt{std} :: \mathtt{string} \! > ;
  auto g
    =
        create empty undirected named edges and vertices graph
  add_named_edge("Reed", g);
  const strings expected_vertex_names{"",""};
  const strings vertex names = get vertex names(g);
  assert (expected vertex names = vertex names);
  const strings expected_edge_names{"Reed"};
  const strings edge_names = get_edge_names(g);
  assert (expected edge names == edge names);
}
```

6.3 Adding a named edge

Adding an edge with a name:

Algorithm 120 Add a vertex with a name

```
#include < cassert >
#include < string>
#include <boost/graph/adjacency list.hpp>
template <typename graph>
typename boost::graph traits<graph>::edge descriptor
add named edge (
  const std::string& edge_name,
  graph& g
) noexcept
  static_assert(!std::is_const<graph>::value,
    "graph_cannot_be_const"
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer = boost::add_edge(vd_a, vd_b, g);
  assert (aer.second);
  auto edge name map = get (
      boost::edge name, g
    );
  put(edge name map, aer.first, edge name);
  return aer.first;
```

In this code snippet, the edge descriptor (see chapter 2.12 if you need to refresh your memory) when using 'boost::add_edge' is used as a key to change the edge its name map.

The algorithm 121 shows how to add a named edge to an empty graph. When trying to add named vertices to graph without this property, you will get the error 'formed reference to void' (see chapter 24.1).

Algorithm 121 Demonstration of the 'add named edge' function

```
#include <cassert>
#include "add_named_edge.h"
#include "
    create_empty_undirected_named_edges_and_vertices_graph
    .h"

void add_named_edge_demo() noexcept
{
    auto g
    =
        create_empty_undirected_named_edges_and_vertices_graph
        ();
    add_named_edge("Richards", g);
    assert(boost::num_edges(g) == 1);
}
```

6.4 Adding a named edge between vertices

When having two vertex descriptors, you can add a named edge between those.

Algorithm 122 Add a vertex with a name between vertices

```
#include < cassert >
#include < string>
#include <boost/graph/adjacency_list.hpp>
#include "set edge name.h"
template <typename graph, typename vertex descriptor>
typename boost::graph traits<graph>::edge descriptor
add named edge between vertices (
  const std::string& edge name,
  const vertex_descriptor from ,
  const vertex descriptor to,
  graph& g
 noexcept
  const auto aer = boost::add edge(from, to, g);
  assert (aer.second);
  set edge name(edge name, aer.first, g);
  return aer.first;
}
```

In this code snippet, the edge is added between the two vertex descriptors,

after which the name of the edge is set.

A demonstration is given by algorithm 123:

Algorithm 123 Demonstration of the 'add_named_edge_between_vertices' function

```
#include <cassert>
#include "add_named_edge.h"
#include "
    create_empty_undirected_named_edges_and_vertices_graph
    .h"

void add_named_edge_demo() noexcept
{
    auto g
    =
        create_empty_undirected_named_edges_and_vertices_graph
        ();
    add_named_edge("Richards", g);
    assert(boost::num_edges(g) == 1);
}
```

6.5 Getting the edges' names

When the edges of a graph have named vertices, one can extract them as such:

Algorithm 124 Get the edges' names

```
#include < string>
#include < vector >
#include <boost/graph/adjacency list.hpp>
#include <boost/graph/properties.hpp>
template <typename graph>
std::vector<std::string> get edge names(const graph& g)
    noexcept
  using boost::graph traits;
  using ed = typename graph traits < graph >::
      edge descriptor;
  std::vector<std::string> v(boost::num edges(g));
  const auto eip = edges(g);
  std::transform(eip.first, eip.second, std::begin(v),
    [g](\mathbf{const} \ \mathrm{ed} \& \ \mathrm{d})
      const auto edge name map = get(boost::edge name,g);
      return get (edge_name_map, d);
    }
  );
  return v;
```

The names of the edges are obtained from a boost::property_map and then put into a std::vector. The algorithm 125 shows how to apply this function.

The order of the edge names may be different after saving and loading.

Would you dare to try to get the edges' names from a graph without vertices with names, you will get the error 'formed reference to void' (see chapter 24.1).

Algorithm 125 Demonstration of the 'get edge names' function

```
#include <cassert>
#include "add named edge.h"
#include "
   create empty undirected named edges and vertices graph
   . h"
#include "get edge names.h"
void get edge names demo() noexcept
  auto g
       create\_empty\_undirected\_named\_edges\_and\_vertices\_graph
  const std::string edge_name_1{"Eugene"};
  const std::string edge name 2{"Another_Eugene"};
  add_named_edge(edge_name_1, g);
  add named edge (edge name 2, g);
  const std::vector<std::string> expected names{
    edge_name_1, edge_name_2
  const std::vector<std::string> edge names{
    get_edge_names(g)
  assert (expected_names == edge_names);
```

6.6 Creating Markov chain with named edges and vertices

6.6.1 Graph

We build this graph:

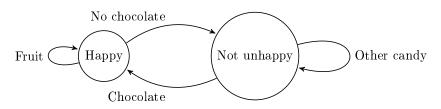


Figure 29: A two-state Markov chain where the edges and vertices have texts

6.6.2 Function to create such a graph

Here is the code:

Algorithm 126 Creating the two-state Markov chain as depicted in figure 29

```
#include <string>
#include "
   create empty directed named edges and vertices graph.h
#include "add named vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<boost::vertex name t, std::string>,
  boost::property<boost::edge name t,std::string>
create named edges and vertices markov chain() noexcept
{
  auto g
        create empty directed named edges and vertices graph
        ();
  const auto vd a = add named vertex("Happy", g);
  const auto vd b = add named vertex("Not_unhappy", g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer_aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer_ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer bb = boost::add edge(vd b, vd b, g);
  assert (aer bb.second);
  \mathbf{auto} edge name map = \mathbf{get} (
    boost::edge name,g
  );
  put (edge_name_map, aer_aa.first, "Fruit");
  put(edge_name_map, aer_ab.first, "No_chocolate");
  \verb"put(edge_name_map", aer_ba.first", "Chocolate");
  {\tt put}\left({\tt edge\_name\_map}\,,\ {\tt aer\_bb.first}\ ,\ "Other\_candy"\right);
  return g;
}
```

6.6.3 Creating such a graph

Here is the demo:

Algorithm 127 Demo of the 'create_named_edges_and_vertices_markov_chain' function (algorithm 126)

```
#include <cassert>
#include <iostream>
#include "create_named_edges_and_vertices_markov_chain.h"
#include "get edge names.h"
#include "get vertex names.h"
void create named edges and vertices markov chain demo()
   noexcept
  using strings = std::vector<std::string>;
  const auto g
    =\ create\_named\_edges\_and\_vertices\_markov\_chain\,()\;;
  const strings expected_vertex_names{
    "Happy", "Not_unhappy"
  const strings vertex names {
    get vertex names(g)
  assert (expected vertex names == vertex names);
  const strings expected edge names{
    " Fruit " , "No_{\circ} chocolate " , " Chocolate " , " Other _{\circ} candy "
  const strings edge_names{get_edge_names(g)};
  assert (expected edge names == edge names);
}
```

6.6.4 The .dot file produced

Algorithm 128 .dot file created from the 'create_named_edges_and_vertices_markov_chain' function (algorithm 126), converted from graph to .dot file using algorithm 52

```
digraph G {
    O[label=Happy];
    1[label="Not unhappy"];
    O->0 [label="Fruit"];
    O->1 [label="No chocolate"];
    1->0 [label="Chocolate"];
    1->1 [label="Other candy"];
}
```

6.6.5 The .svg file produced

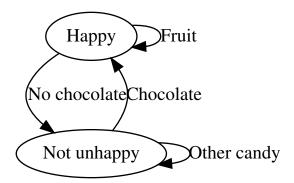


Figure 30: .svg file created from the 'create_named_edges_and_vertices_markov_chain' function (algorithm 126) its .dot file, converted from .dot file to .svg using algorithm 361

6.7 Creating K_2 with named edges and vertices

6.7.1 Graph

We extend the graph K_2 with named vertices of chapter 4.6 by adding names to the edges, as depicted in figure 31:

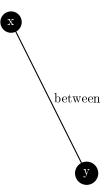


Figure 31: K_2 : a fully connected graph with three named edges and vertices

6.7.2 Function to create such a graph

To create K_2 , the following code can be used:

Algorithm 129 Creating K_2 as depicted in figure 31

```
#include < string>
#include <boost/graph/adjacency_list.hpp>
#include "
    create empty undirected named edges and vertices graph
    . h"
\#include "add_named_vertex.h"
#include "add named edge between vertices.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<boost::vertex name t, std::string>,
  boost::property<boost::edge name t,std::string>
>
create named edges and vertices k2 graph() noexcept
  auto g
        create_empty_undirected_named_edges_and_vertices_graph
  const std::string va("x");
  const std::string vb("y");
  const std::string ea("between");
  {f const\ auto\ vd\_a\ =\ add\_named\_vertex(\,va\,,\ g)}\,;
  \mathbf{const} \ \mathbf{auto} \ \mathrm{vd\_b} \ = \ \mathrm{add\_named\_vertex} \left( \mathrm{vb} \ , \ \ \mathbf{g} \right);
  add_named_edge_between_vertices(ea,vd_a,vd_b, g);
  return g;
```

Most of the code is a repeat of algorithm 69. In the end, the edge names are obtained as a boost::property map and set.

6.7.3 Creating such a graph

Algorithm 130 shows how to create the graph and measure its edge and vertex names.

```
      Algorithm
      130
      Demonstration
      of
      the
      'create_named_edges_and_vertices_k2' function
```

```
#include <cassert>
#include <iostream>
#include "create named edges and vertices k2 graph.h"
#include "get edge names.h"
#include "get_vertex_names.h"
void create named edges and vertices k2 graph demo()
   noexcept
  using strings = std::vector<std::string>;
  const auto g
    = create named edges and vertices k2 graph();
  const strings expected vertex names {
    "x", "y"
  };
  const strings vertex_names{
    get_vertex_names(g)
  assert (expected vertex names = vertex names);
  const strings expected edge names {
    "between"
  };
  const strings edge names{get edge names(g)};
  assert (expected edge names == edge names);
}
```

6.7.4 The .dot file produced

Algorithm 131 .dot file created from the 'create_named_edges_and_vertices_k2_graph' function (algorithm 129), converted from graph to .dot file using algorithm 52

```
graph G {
0[label=x];
1[label=y];
0--1 [label="between"];
}
```

6.7.5 The .svg file produced

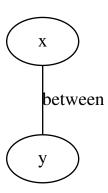


Figure 32: .svg file created from the 'create_named_edges_and_vertices_k2_graph' function (algorithm 129) its .dot file, converted from .dot file to .svg using algorithm 361

6.8 Creating K_3 with named edges and vertices

6.8.1 Graph

We extend the graph K_2 with named vertices of chapter 4.6 by adding names to the edges, as depicted in figure 33:

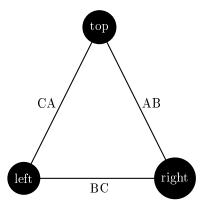


Figure 33: K_3 : a fully connected graph with three named edges and vertices

6.8.2 Function to create such a graph

To create K_3 , the following code can be used:

Algorithm 132 Creating K_3 as depicted in figure 33

```
#include < string>
#include <boost/graph/adjacency list.hpp>
#include "
   create empty undirected named edges and vertices graph
   . h"
\#include "add named vertex.h"
#include "add named edge between vertices.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<boost::vertex name t, std::string>,
  boost::property\!<\!boost::edge\_name\_t\,,std::string\!>
create named edges and vertices k3 graph() noexcept
  auto g
       create empty undirected named edges and vertices graph
  const std::string va("top");
  const std::string vb("right");
  const std::string vc("left");
  const std::string ea("AB");
  const std::string eb("BC");
  const std::string ec("CA");
  const auto vd a = add named vertex(va, g);
  const auto vd_b = add_named_vertex(vb, g);
  const auto vd c = add named vertex(vc, g);
  add_named_edge_between_vertices(ea, vd_a, vd_b, g);
  add_named_edge_between_vertices(eb, vd_b, vd_c, g);
  add named edge between vertices (ec, vd c, vd a, g);
  return g;
```

Most of the code is a repeat of algorithm 69. In the end, the edge names are obtained as a boost::property map and set.

6.8.3 Creating such a graph

Algorithm 133 shows how to create the graph and measure its edge and vertex names.

 Algorithm
 133
 Demonstration
 of
 the
 'create_named_edges_and_vertices_k3' function

```
#include < cassert >
#include <iostream>
#include "create named edges and vertices k3 graph.h"
#include "get edge names.h"
#include "get_vertex_names.h"
void create_named_edges_and_vertices_k3_graph_demo()
   noexcept
  using strings = std::vector<std::string>;
  const auto g
    = create_named_edges_and_vertices_k3_graph();
  const strings expected vertex names{
    "top", "right", "left"
  };
  \mathbf{const} \ \mathtt{strings} \ \mathtt{vertex\_names} \{
    get_vertex_names(g)
  assert (expected vertex names = vertex names);
  const strings expected edge names {
    "AB", "BC", "CA"
  };
  const strings edge names{get edge names(g)};
  assert (expected edge names == edge names);
}
```

6.8.4 The .dot file produced

```
Algorithm
                134
                        .dot
                                 file
                                        created
                                                   from
                                                             the
                                                                    'cre-
ate_named_edges_and_vertices_k3_graph'
                                            function
                                                       (algorithm
                                                                    132),
converted from graph to .
dot file using algorithm 52
graph G {
0[label=top];
1[label=right];
2[label=left];
0--1 [label="AB"];
1--2 [label="BC"];
2--0 [label="CA"];
```

6.8.5 The .svg file produced

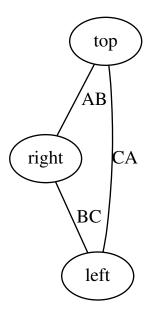


Figure 34: .svg file created from the 'create_named_edges_and_vertices_k3_graph' function (algorithm 132) its .dot file, converted from .dot file to .svg using algorithm 361

6.9 Creating a path graph with named edges and vertices

Here we create a path graph with names edges and vertices

6.9.1 Graph

Here I show a path graph with four vertices (see figure 35):



Figure 35: A path graph with four vertices

6.9.2 Function to create such a graph

To create a path graph, the following code can be used:

Algorithm 135 Creating a path graph as depicted in figure 35

```
#include < vector >
#include "add_named_edge_between_vertices.h"
#include "add named vertex.h"
#include "
   create empty undirected named edges and vertices graph
   . h "
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<boost::vertex name t, std::string>,
  boost::property<boost::edge name t,std::string>
>
create named edges and vertices path graph (
  const std::vector<std::string>& edge names,
  const std::vector<std::string>& vertex names
 noexcept
{
  assert (vertex names.empty()
    | | vertex names.size() = edge names.size() + 1
  );
  auto g =
     create empty undirected named edges and vertices graph
     ();
  if (vertex names.size() = 0) { return g; }
  auto vd 1 = add named vertex(*vertex names.begin(), g);
  if (vertex names.size() == 1) return g;
  const auto j = std::end(vertex names);
  auto vertex name = std::begin(vertex names);
  auto edge name = std::begin(edge names);
  for (++vertex_name; vertex_name!=j; ++vertex_name, ++
     edge name) //Skip first vertex name
    auto vd 2 = add named vertex (*vertex name, g);
    add_named_edge_between_vertices(
      *edge name, vd 1, vd 2, g
    );
    vd 1 = vd 2;
  return g;
}
```

6.9.3 Creating such a graph

Algorithm 136 demonstrates how to create a path graph with named edges and vertices and checks if it has the correct amount of edges and vertices:

Algorithm 136 Demonstration of 'create named edges and vertices path graph'

```
#include < cassert >
#include "create named edges and vertices path graph.h"
#include "get edge names.h"
#include "get vertex names.h"
void create named edges and vertices path graph demo()
   noexcept
  const std::vector<std::string> vertex names
    = \{ \text{"A"}, \text{"B"}, \text{"C"}, \text{"D"} \};
  const std::vector<std::string> edge names
    = \{ "1", "2", "3" \};
  const auto g =
     create_named_edges_and_vertices_path_graph(
    edge names, vertex names
  );
  assert(boost::num edges(g) == 3);
  assert (boost::num vertices(g) == 4);
  assert(get edge names(g) = edge names);
  assert(get vertex names(g) = vertex names);
```

6.9.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 137:

Algorithm 137 .dot file created from the 'create_named_edges_and_vertices_path_graph' function (algorithm 135), converted from graph to .dot file using algorithm 52

6.9.5 The .svg file produced

The .dot file can be converted to the .svg as shown in figure 36:

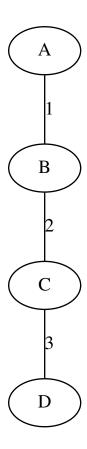


Figure 36: .svg file created from the 'create_named_edges_and_vertices_path_graph' function (algorithm 135) its .dot file, converted from .dot file to .svg using algorithm 361

6.10 Creating a Petersen graph with named edges and vertices

Here we create a Petersen graph with named edges and vertices.

6.10.1 Graph

Here I show a Petersen graph (see figure 37):

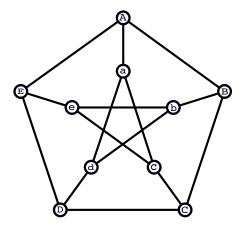


Figure 37: A Petersen graph with named edges and vertices (modified from https://en.wikipedia.org/wiki/Petersen_graph)

6.10.2 Function to create such a graph

To create a Petersen graph with named edges and vertices, the following code can be used:

Algorithm 138 Creating a Petersen graph as depicted in figure 37

```
#include <cassert>
#include < vector >
#include "add named vertex.h"
#include "create empty undirected named vertices graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex name t, std::string
create_named_vertices_petersen_graph() noexcept
  auto g = create empty undirected named vertices graph()
  using vd = decltype(
     create_empty_undirected_named_vertices_graph())::
      vertex descriptor;
  std:: vector < vd > v; //Outer
  for (int i = 0; i! = 5; ++i) {
    v.push back (
      add_named_vertex(std::string(1,'A' + i), g)
    );
  }
  std::vector < vd > w; //Inner
  for (int i = 0; i! = 5; ++i) {
    w.push_back(
      add_named_vertex(std::string(1,'a' + i), g)
    );
  }
  //Outer ring
  for (int i=0; i!=5; ++i) {
    const auto aer
      = boost::add edge(v[i], v[(i+1) \% 5], g);
    assert (aer.second);
  //Spoke
  for (int i = 0; i! = 5; ++i) {
    const auto aer
      = boost::add edge(v[i], w[i], g);
    assert (aer.second);
                             151
  //Inner pentagram
  for (int i = 0; i! = 5; ++i) {
    const auto aer
      = boost::add edge(w[i], w[(i + 2) % 5], g);
    assert (aer.second);
  return g;
```

6.10.3 Creating such a graph

Algorithm 139 demonstrates how to create a path graph with named vertices and checks if it has the correct amount of edges and vertices:

```
#include <cassert >
#include "create_named_vertices_petersen_graph'

void create_named_vertices_petersen_graph_demo() noexcept

const auto g = create_named_vertices_petersen_graph();
assert(boost::num_edges(g) == 15);
assert(boost::num_vertices(g) == 10);
}
```

6.10.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 140:

```
Algorithm
               140
                        .dot
                                file
                                       created
                                                  from
                                                           the
                                                                   'cre-
ate_named_edges_and_vertices_petersen_graph'
                                                  function
                                                             (algorithm
138), converted from graph to .dot file using algorithm 52
graph G {
0[label=A];
1[label=B];
2[label=C];
3[label=D];
4[label=E];
5[label=a];
6[label=b];
7[label=c];
8[label=d];
9[label=e];
0--1 [label="F"];
1--2 [label="G"];
2--3 [label="H"];
3--4 [label="I"];
4--0 [label="J"];
0--5 [label="0"];
1--6 [label="1"];
2--7 [label="2"];
3--8 [label="3"];
4--9 [label="4"];
5--7 [label="f"];
6--8 [label="g"];
7--9 [label="h"];
8--5 [label="i"];
9--6 [label="j"];
```

6.10.5 The .svg file produced

The .dot file can be converted to the .svg as shown in figure 38:

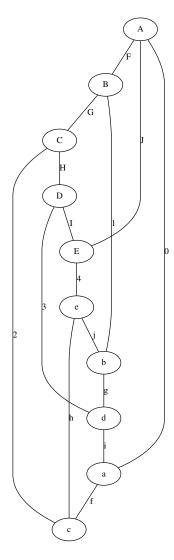


Figure 38: .svg file created from the 'create_named_edges_and_vertices_petersen_graph' function (algorithm 138) its .dot file, converted from .dot file to .svg using algorithm 361

7 Working on graphs with named edges and vertices

Working with named edges...

• Check if there exists an edge with a certain name: chapter 7.1

- Find a (named) edge by its name: chapter 7.2
- Get a (named) edge its name from its edge descriptor: chapter 7.3
- Set a (named) edge its name using its edge descriptor: chapter 7.4
- Remove a named edge: chapter 7.5
- Saving a graph with named edges and vertices to a .dot file: chapter 7.8
- Loading a directed graph with named edges and vertices from a .dot file: chapter 7.9
- \bullet Loading an undirected graph with named edges and vertices from a .dot file: chapter 7.10

Especially chapter 7.2 with the 'find_first_edge_by_name' algorithm shows how to obtain an edge descriptor, which is used in later algorithms.

7.1 Check if there exists an edge with a certain name

Before modifying our edges, let's first determine if we can find an edge by its name in a graph. After obtaing a name map, we obtain the edge iterators, dereference these to obtain the edge descriptors and then compare each edge its name with the one desired.

Algorithm 141 Find if there is an edge with a certain name

```
#include < string>
#include <boost/graph/properties.hpp>
template <typename graph>
bool has edge with name (
  const std::string& edge_name,
  const graph& g
 noexcept
{
  using ed = typename boost::graph traits<graph>::
     edge descriptor;
  const auto eip = edges(g);
  return std::find if (eip.first, eip.second,
    [edge name, g](const ed& d)
      const auto edge name map
        = get (boost::edge name, g);
      return get(edge_name_map, d) == edge_name;
  != eip.second;
}
```

This function can be demonstrated as in algorithm 142, where a certain name cannot be found in an empty graph. After adding the desired name, it is found.

Algorithm 142 Demonstration of the 'has edge with name' function

Note that this function only finds if there is at least one edge with that name: it does not tell how many edges with that name exist in the graph.

7.2 Find an edge by its name

Where STL functions work with iterators, here we obtain an edge descriptor (see chapter 2.12) to obtain a handle to the desired edge. Algorithm 143 shows how to obtain an edge descriptor to the first (name) edge found with a specific name.

Algorithm 143 Find the first edge by its name

```
#include < string>
\#include < boost/graph/graph_traits.hpp>
\#\mathbf{include} < \mathbf{boost} / \operatorname{graph} / \operatorname{properties} . hpp>
template <typename graph>
typename boost::graph traits<graph>::edge descriptor
find first edge with name (
  {f const} std::string& name,
  const graph& g
) noexcept
  using ed = typename boost::graph traits<graph>::
      edge descriptor;
  const auto eip = edges(g);
  const auto i = std::find if (
    eip.first, eip.second,
    [g, name](const ed d) {
       const auto edge name map = get(boost::edge name, g)
       return get (edge name map, d) == name;
    }
  );
  assert (i != eip.second);
  return *i;
```

With the edge descriptor obtained, one can read and modify the graph. Algorithm 144 shows some examples of how to do so.

Algorithm 144 Demonstration of the 'find first edge by name' function

7.3 Get a (named) edge its name from its edge descriptor

This may seem a trivial paragraph, as chapter 6.5 describes the 'get_edge_names' algorithm, in which we get all edges' names. But it does not allow to first find an edge of interest and subsequently getting only that one its name.

To obtain the name from an edgedescriptor, one needs to pull out the name map and then look up the edge of interest.

Algorithm 145 Get an edge its name from its edge descriptor

To use 'get edge name', one first needs to obtain an edge descriptor. Al-

Algorithm 146 Demonstration if the 'get edge name' function

7.4 Set a (named) edge its name from its edge descriptor

If you know how to get the name from an edge descriptor, setting it is just as easy, as shown in algorithm 147.

Algorithm 147 Set an edge its name from its edge descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>

template <typename graph>
void set_edge_name(
    const std::string& any_edge_name,
    const typename boost::graph_traits<graph>::
        edge_descriptor& vd,
    graph& g
) noexcept
{
    static_assert(!std::is_const<graph>::value,
        "graph_cannot_be_const"
);

    auto edge_name_map = get(boost::edge_name,g);
    put(edge_name_map, vd, any_edge_name);
}
```

To use 'set_edge_name', one first needs to obtain an edge descriptor. Algorithm 148 shows a simple example.

Algorithm 148 Demonstration if the 'set_edge_name' function

```
#include <cassert>
#include "add named edge.h"
#include "
   create empty undirected named edges and vertices graph
   . h"
#include "find first edge with name.h"
#include "get_edge_name.h"
#include "set edge name.h"
void set edge name demo() noexcept
  {\bf auto} \ \ {\bf g} \ =
     create empty undirected named edges and vertices graph
  const std::string old name{"Dex"};
  add named edge(old name, g);
  const auto vd = find first edge with name(old name,g);
  assert(get\_edge\_name(vd,g) = old\_name);
  const std::string new_name{"Diggy"};
  set \quad edge\_name(new\_name, \ vd, \ g);
  assert(get edge name(vd,g) = new name);
```

7.5 Removing the first edge with a certain name

An edge descriptor can be used to remove an edge from a graph.

Removing a named edge goes as follows: use the name of the edge to get a first edge descriptor, then call 'boost::remove_edge', shown in algorithm 94:

Algorithm 149 Remove the first edge with a certain name

```
#include <boost/graph/adjacency list.hpp>
#include "find_first_edge_with_name.h"
#include "has edge with name.h"
template <typename graph>
void remove first edge with name (
  const std::string& name,
  graph& g
 noexcept
  static assert (!std::is const<graph>::value,
    "graph_cannot_be_const"
  );
  assert (has edge with name (name, g));
  const auto vd
    = find_first_edge_with_name(name,g);
  boost::remove edge(vd,g);
}
```

Algorithm 150 shows the removal of the first named edge found.

 ${\bf Algorithm~150~Demonstration~of~the~`remove_first_edge_with_name'~function}$

```
#include <cassert>
#include "create_named_edges_and_vertices_k3_graph.h"
#include "remove_first_edge_with_name.h"

void remove_first_edge_with_name_demo() noexcept
{
    auto g = create_named_edges_and_vertices_k3_graph();
    assert (boost::num_edges(g) == 3);
    assert (boost::num_vertices(g) == 3);
    remove_first_edge_with_name("AB",g);
    assert (boost::num_edges(g) == 2);
    assert (boost::num_vertices(g) == 3);
}
```

7.6 Create a direct-neighbour subgraph from a vertex descriptor of a graph with named edges and vertices

Suppose you have a vertex of interest its vertex descriptor. Let's say you want to get a subgraph of that vertex and its direct neighbours only. This means that all vertices of that subgraph are adjacent vertices and that the edges go either from focal vertex to its neighbours, or from adjacent vertex to adjacent neighbour.

Here is the 'create direct neighbour subgraph' code:

Algorithm 151 Get the direct-neighbour named edges and vertices subgraph from a vertex descriptor

```
\#include <map>
#include <boost/graph/adjacency list.hpp>
#include "add named edge between vertices.h"
#include "add_named vertex.h"
\#include "get_edge_name.h"
#include "get vertex name.h"
template <typename graph, typename vertex_descriptor>
graph
   create direct neighbour named edges and vertices subgraph
  const vertex descriptor & vd,
  const graph& g
{
  graph h;
  std::map<vertex descriptor, vertex descriptor> vds;
    const auto vd h = add named vertex(get vertex name(vd
        ,g),h);
    vds.insert(std::make pair(vd,vd h));
  //Copy vertices
    const auto vdsi = boost::adjacent vertices (vd, g);
    std::transform(vdsi.first, vdsi.second,
      std::inserter(vds, std::begin(vds)),
      [g, &h](const vertex_descriptor&d)
        const auto vd_h = add_named vertex(
           get\_vertex\_name(d,g), h);
        return std::make pair(d,vd h);
    );
  //Copy edges
    const auto eip = edges(g);
    const auto j = eip.second;
    for (auto i = eip.first; i!=j; ++i)
      const auto vd_from = source(*i, g);
      const auto vd to = target(*i, g);
      if (vds.find(vd from) = std::end(vds)) continue;
      if (vds.find(vd to) = std::end(vds)) continue;
      add_named_edge_betwe\frac{1}{2} vertices (
        get\_edge\_name(*i, g),
        vds[vd_from], vds[vd_to], h
      );
    }
  return h;
```

This demonstration code shows that the direct-neighbour graph of each vertex of a K_2 graphs is ... a K_2 graph!

Algorithm 152 Demo of the 'create_direct_neighbour_named_edges_and_vertices_subgraph' function

```
#include "
   create direct neighbour named edges and vertices subgraph
#include "create named edges and vertices k2 graph.h"
#include "get edge names.h"
#include "get vertex names.h"
void
   create direct neighbour named edges and vertices subgraph demo
   () noexcept
{
  const auto g = create named edges and vertices k2 graph
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (auto i=vip.first; i!=j; ++i) {
    const auto h =
       create direct neighbour named edges and vertices subgraph
      *\,\mathrm{i}, g
    );
    assert(boost::num\_vertices(h) == 2);
    assert(boost::num edges(h) == 1);
    const auto v = get vertex names(h);
    std::set<std::string> vs(std::begin(v),std::end(v));
    assert(vs.count("x") == 1);
    assert(vs.count("y") == 1);
    const auto e = get edge names(h);
    std::set<std::string> es(std::begin(e),std::end(e));
    assert (es.count ("between") == 1);
}
```

7.7 Creating all direct-neighbour subgraphs from a graph with named edges and vertices

Using the previous function, it is easy to create all direct-neighbour subgraphs from a graph with named edges and vertices:

Algorithm 153 Create all direct-neighbour subgraphs from a graph with named edges and vertices

```
#include < vector >
#include "
   create\_direct\_neighbour\_named\_edges\_and\_vertices\_subgraph
template <typename graph>
std::vector < graph >
   create all direct neighbour named edges and vertices subgraphs
  const graph g
) noexcept
{
  using vd = typename graph::vertex_descriptor;
  std::vector<graph> v;
  v.resize(boost::num_vertices(g));
  const auto vip = vertices(g);
  std::transform(
    vip.first , vip.second ,
    std::begin(v),
    [g](const vd& d)
      return
          create\_direct\_neighbour\_named\_edges\_and\_vertices\_subgraph
          (
        d, g
      );
    }
  );
  return v;
```

This demonstration code shows that all two direct-neighbour graphs of a K_2 graphs are ... K_2 graphs!

Algorithm 154 Demo of the 'create_all_direct_neighbour_named_edges_and_vertices_subgraphs' function

All sub-graphs of a path graph are shown here:

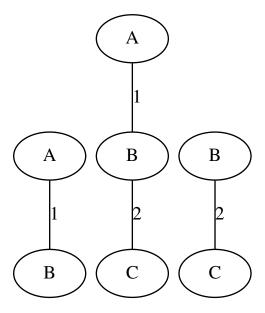


Figure 39: All subgraphs created

7.8 Saving an undirected graph with named edges and vertices as a .dot

If you used the create_named_edges_and_vertices_k3_graph function (algorithm 132) to produce a K_3 graph with named edges and vertices, you can store these names additionally with algorithm 155:

Algorithm 155 Saving an undirected graph with named edges and vertices to a .dot file

```
#include < string>
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include <boost/graph/properties.hpp>
#include "get edge names.h"
#include "get vertex names.h"
template <typename graph>
void save named edges and vertices graph to dot (
  const graph& g,
  const std::string& filename
  using my edge descriptor = typename graph::
     edge descriptor;
  std::ofstream f(filename);
  const auto vertex names = get_vertex_names(g);
  const auto edge name map = boost::get(boost::edge name,
     g);
  boost::write graphviz(
    f,
    boost::make_label_writer(&vertex_names[0]),
    [edge name map](std::ostream& out, const
       my edge descriptor& e) {
      out << "[label=\"" << edge name map[e] << "\"]";
    }
 );
}
```

If you created a graph with edges more complex than just a name, you will still just write these to the .dot file. Chapter 13.10 shows how to write custom vertices to a .dot file.

So, the 'save_named_edges_and_vertices_graph_to_dot' function (algorithm 52) saves only the structure of the graph and its edge and vertex names.

7.9 Loading a directed graph with named edges and vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with named edges and vertices is loaded, as shown in algorithm 156:

Algorithm 156 Loading a directed graph with named edges and vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create empty directed named edges and vertices graph.h
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex name t, std::string
  >,
  boost::property<
    boost::edge name t, std::string
load directed named edges and vertices graph from dot (
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g =
     create empty directed named edges and vertices graph
  boost::dynamic_properties dp(boost::
     ignore other properties);
  dp.property("label", get(boost::vertex name, g));
  dp.property("edge_id", get(boost::edge_name, g));
dp.property("label", get(boost::edge_name, g));
  boost::read graphviz(f,g,dp);
  return g;
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Next to this, a boost::dynamic_properties is created with its default constructor, after which we direct the boost::dynamic_properties to find a 'node_id' and 'label' in the vertex name map, 'edge_id' and 'label' to the edge name map. From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

Algorithm 157 shows how to use the 'load _ directed _ graph _ from _ dot' function:

Algorithm 157 Demonstration of the 'load_directed_named_edges_and_vertices_graph_from_dot' function

```
#include "create named edges and vertices markov chain.h"
#include
   load directed named edges and vertices graph from dot.
#include "save named edges and vertices graph to dot.h"
#include "get vertex names.h"
void
   load directed named edges and vertices graph from dot demo
   () noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create_named_edges_and_vertices_markov_chain();
  const std::string filename{
    "create named edges and vertices markov chain.dot"
  save named edges and vertices graph to dot(g, filename)
  const auto h
       load directed named edges and vertices graph from dot
      filename
     );
  assert(num edges(g) == num edges(h));
  assert(num \ vertices(g) == num \ vertices(h));
  assert(get\_vertex\_names(g) == get\_vertex\_names(h));
```

This demonstration shows how the Markov chain is created using the 'cre-

ate_named_edges_and_vertices_markov_chain' function (algorithm 126), saved and then loaded. The loaded graph is checked to be a directed graph similar to the Markov chain with the same edge and vertex names (using the 'get_edge_names' function, algorithm 124, and the 'get_vertex_names' function, algorithm 64).

7.10 Loading an undirected graph with named edges and vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with named edges and vertices is loaded, as shown in algorithm 158:

 ${\bf Algorithm~158}$ Loading an undirected graph with named edges and vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create_empty_undirected_named_edges_and_vertices_graph
   . h"
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex\_name\_t\,,std::string
  >,
  boost::property<
    boost::edge name t, std::string
load undirected named edges and vertices graph from dot (
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g =
     create empty undirected named edges and vertices graph
     ();
  boost::dynamic properties dp(boost::
     ignore_other_properties);
  dp.property("label", get(boost::vertex name, g));
 dp.property("edge_id", get(boost::edge_name, g));
  dp.property("label", get(boost::edge_name, g));
  boost::read graphviz(f,g,dp);
  return g;
}
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 7.9 describes the rationale of this function.

Algorithm 159 shows how to use the 'load_undirected_graph_from_dot' function:

Algorithm 159 Demonstration of the 'load_undirected_named_edges_and_vertices_graph_from_dot' function

```
#include "create named edges and vertices k3 graph.h"
#include "
   load_undirected_named_edges_and_vertices_graph_from_dot
   . h"
#include "save named edges and vertices graph to dot.h"
#include "get vertex names.h"
void
   load undirected named edges and vertices graph from dot demo
   () noexcept
{
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create named edges and vertices k3 graph();
  const std::string filename{
    "create named edges and vertices k3 graph.dot"
  save_named_edges_and_vertices_graph_to_dot(g, filename)
  const auto h
       load undirected named edges and vertices graph from dot
      filename
    );
  assert(num edges(g) == num edges(h));
  assert (num vertices (g) == num vertices (h));
  assert(get vertex names(g) = get vertex names(h));
}
```

This demonstration shows how K_3 with named edges and vertices is created using the 'create_named_edges_and_vertices_k3_graph' function (algorithm 132), saved and then loaded. The loaded graph is checked to be an undirected graph similar to K_3 , with the same edge and vertex names (using the 'get_edge_names' function, algorithm 124, and the 'get_vertex_names' function, algorithm 64).

8 Building graphs with bundled vertices

Up until now, the graphs created have had edges and vertices with the built-in name propery. In this chapter, graphs will be created, in which the vertices can have a bundled 'my_bundled_vertex' type⁷. The following graphs will be created:

- An empty directed graph that allows for bundled vertices: see chapter 161
- An empty undirected graph that allows for bundled vertices: see chapter 8.2
- A two-state Markov chain with bundled vertices: see chapter 8.6
- K_2 with bundled vertices: see chapter 8.7

In the process, some basic (sometimes bordering trivial) functions are shown:

- Create the vertex class, called 'my bundled vertex': see chapter 8.1
- Adding a 'my bundled vertex': see chapter 8.4
- Getting the vertices 'my bundled vertex'-es: see chapter 8.5

These functions are mostly there for completion and showing which data types are used.

8.1 Creating the bundled vertex class

Before creating an empty graph with bundled vertices, that bundled vertex class must be created. In this tutorial, it is called 'my_bundled_vertex'. 'my_bundled_vertex' is a class that is nonsensical, but it can be replaced by any other class type.

Here I will show the header file of 'my_bundled_vertex', as the implementation of it is not important:

⁷I do not intend to be original in naming my data types

Algorithm 160 Declaration of my bundled vertex

```
#include < string>
#include <iosfwd>
#include <boost/property map/dynamic property map.hpp>
struct my bundled vertex
  explicit my bundled vertex (
    const std::string& name = "",
    const std::string& description = "",
    const double x = 0.0,
    const double y = 0.0
  ) noexcept;
  std::string m_name;
  std::string m description;
  double m x;
  double m y;
};
bool operator == (const my bundled vertex& lhs, const
   my_bundled_vertex& rhs) noexcept;
bool operator! = (const my_bundled_vertex& lhs, const
   my bundled vertex& rhs) noexcept;
```

'my bundled vertex' is a class that has multiple properties:

- It has four public member variables: the double 'm_x' ('m_' stands for member), the double 'm_y', the std::string m_name and the std::string m_description. These variables must be public
- It has a default constructor
- It is copyable
- It is comparable for equality (it has operator==), which is needed for searching

'my_bundled_vertex' does not have to have the stream operators defined for file I/O, as this goes via the public member variables.

8.2 Create the empty directed graph with bundled vertices

Algorithm 161 Creating an empty directed graph with bundled vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_vertex.h"

boost:: adjacency_list <
   boost:: vecS,
   boost:: vecS,
   boost:: directedS,
   my_bundled_vertex
>
create_empty_directed_bundled_vertices_graph() noexcept
{
   return {};
}
```

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)
- is directed (due to the boost::directedS)
- The vertices have one property: they have a bundled type, that is of data type 'my_bundled_vertex'
- The edges and graph have no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fourth template argument 'my_bundled_vertex'. This can be read as: "vertices have the bundled property 'my_bundled_vertex". Or simply: "vertices have a bundled type called my_bundled_vertex".

8.3 Create the empty undirected graph with bundled vertices

Algorithm 162 Creating an empty undirected graph with bundled vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_vertex.h"

boost:: adjacency_list <
   boost:: vecS ,
   boost:: vecS ,
   boost:: undirectedS ,
   my_bundled_vertex
>
create_empty_undirected_bundled_vertices_graph() noexcept
{
   return {};
}
```

This code is very similar to the code described in chapter 8.2, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS).

8.4 Add a bundled vertex

Adding a bundled vertex is very similar to adding a named vertex (chapter 4.3).

Algorithm 163 Add a bundled vertex

```
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_vertex.h"

template <typename graph>
typename boost::graph_traits<graph>::vertex_descriptor
add_bundled_vertex(const my_bundled_vertex& v, graph& g)
    noexcept
{
    static_assert(!std::is_const<graph>::value,
        "graph_cannot_be_const"
);

    const auto vd = boost::add_vertex(g);
    g[vd] = v;
    return vd;
}
```

When having added a new (abstract) vertex to the graph, the vertex descriptor is used to set the 'my bundled vertex' in the graph.

8.5 Getting the bundled vertices' my vertexes⁸

When the vertices of a graph have any bundled 'my_bundled_vertex', one can extract these as such:

Algorithm 164 Get the bundled vertices' my vertexes

```
#include < vector >
#include <boost/graph/adjacency list.hpp>
#include <boost/graph/graph traits.hpp>
#include <boost/graph/properties.hpp>
#include "my bundled vertex.h"
template <typename graph>
std::vector<my bundled vertex> get my bundled vertexes(
  const graph& g
) noexcept
  using vd = typename graph::vertex descriptor;
  std::vector<my bundled vertex> v(boost::num vertices(g)
     );
  const auto vip = vertices(g);
  std::transform(vip.first, vip.second, std::begin(v),
    [g](\mathbf{const} \ vd\& \ d) \ \{ \ \mathbf{return} \ g[d]; \ \}
  );
  return v;
}
```

The 'my_bundled_vertex' bundled in each vertex is obtained from a vertex descriptor and then put into a std::vector.

The order of the 'my_bundled_vertex' objects may be different after saving and loading.

When trying to get the vertices' my_bundled_vertex from a graph without these, you will get the error 'formed reference to void' (see chapter 24.1).

 $^{^8{\}rm the\ name\ 'my_vertexes'}$ is chosen to indicate this function returns a container of my_vertex

8.6 Creating a two-state Markov chain with bundled vertices

8.6.1 Graph

Figure 40 shows the graph that will be reproduced:

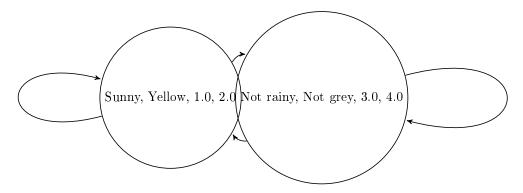


Figure 40: A two-state Markov chain where the vertices have bundled properies and the edges have no properties. The vertices' properties are nonsensical

8.6.2 Function to create such a graph

Here is the code creating a two-state Markov chain with bundled vertices:

Algorithm 165 Creating the two-state Markov chain as depicted in figure 40

```
#include <cassert>
#include "create_empty_directed_bundled_vertices_graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  my bundled vertex
create bundled vertices markov chain () noexcept
  auto g
    = create_empty_directed_bundled_vertices_graph();
  const auto vd_a = boost::add_vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer_aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer_ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer bb = boost::add edge(vd b, vd b, g);
  assert (aer bb.second);
  g[vd_a] = my\_bundled\_vertex("Sunny",
    "Yellow", 1.0, 2.0
  g[vd_b] = my_bundled_vertex("Not_rainy",
    "Not_grey", 3.0, 4.0
  );
  return g;
```

8.6.3 Creating such a graph

Here is the demo:

Algorithm 166 Demo of the 'create_bundled_vertices_markov_chain' function (algorithm 165)

8.6.4 The .dot file produced

Algorithm 167 .dot file created from the 'create_bundled_vertices_markov_chain' function (algorithm 165), converted from graph to .dot file using algorithm 180

```
digraph G {
0[label="Sunny",comment="Yellow",width=1,height=2];
1[label="Not$$$SPACE$$$rainy",comment="Not$$$SPACE$$$grey",width=3,height=4];
0->0;
0->1;
1->0;
1->1;
}
```

8.6.5 The .svg file produced

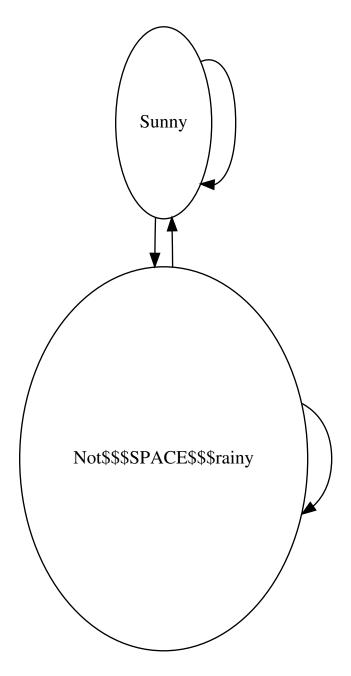


Figure 41: .svg file created from the 'create_bundled_vertices_markov_chain' function (algorithm 165) its .dot file, converted from .dot file to .svg using algorithm 361

8.7 Creating K_2 with bundled vertices

8.7.1 Graph

We reproduce the K_2 with named vertices of chapter 4.6 , but with our bundled vertices intead, as show in figure 42:



Figure 42: K_2 : a fully connected graph with two bundled vertices

8.7.2 Function to create such a graph

Algorithm 168 Creating K_2 as depicted in figure 20

```
#include "create empty undirected bundled vertices graph.
   h"
boost::adjacency_list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  my bundled vertex
create_bundled_vertices_k2_graph() noexcept
  auto g = create_empty_undirected_bundled_vertices_graph
      ();
  const auto vd_a = boost::add_vertex(g);
  const auto vd b = boost :: add vertex(g);
  const auto aer = boost::add_edge(vd_a, vd_b, g);
  assert (aer.second);
  g[vd \ a] = my \ bundled \ vertex(
    "Me", "Myself", 1.0, 2.0
  g[vd_b] = my_bundled_vertex(
    "My_computer", "Not_me", 3.0, 4.0
  );
  return g;
```

Most of the code is a slight modification of the 'create_named_vertices_k2_graph' function (algorithm 69). In the end, (references to) the my_bundled_vertices are obtained and set with two bundled my_bundled_vertex objects.

8.7.3 Creating such a graph

Demo:

Algorithm 169 Demo of the 'create_bundled_vertices_k2_graph' function (algorithm 168)

```
#include <cassert>
#include "create_bundled_vertices_k2_graph.h"
#include "has_bundled_vertex_with_my_vertex.h"

void create_bundled_vertices_k2_graph_demo() noexcept
{
    const auto g = create_bundled_vertices_k2_graph();
    assert(boost::num_edges(g) == 1);
    assert(boost::num_vertices(g) == 2);
    assert(has_bundled_vertex_with_my_vertex(
        my_bundled_vertex("Me","Myself",1.0,2.0), g)
    );
    assert(has_bundled_vertex_with_my_vertex(
        my_bundled_vertex("My_computer","Not_me",3.0,4.0), g)
    );
}
```

8.7.4 The .dot file produced

Algorithm 170 .dot file created from the 'create_bundled_vertices_k2_graph' function (algorithm 168), converted from graph to .dot file using algorithm 52

8.7.5 The .svg file produced

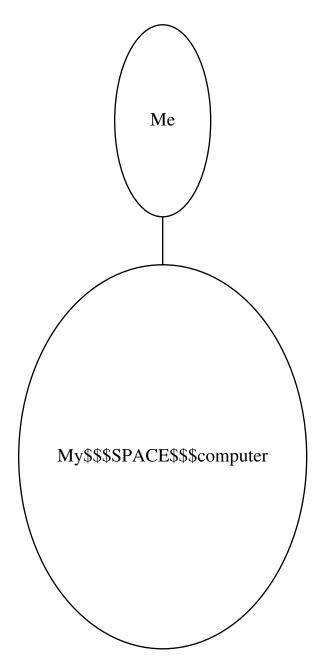


Figure 43: .svg file created from the 'create_bundled_vertices_k2_graph' function (algorithm 168) its .dot file, converted from .dot file to .svg using algorithm 361

9 Working on graphs with bundled vertices

When using graphs with bundled vertices, their state gives a way to find a vertex and working with it. This chapter shows some basic operations on graphs with bundled vertices.

- Check if there exists a vertex with a certain 'my_bundled_vertex': chapter 9.1
- Find a vertex with a certain 'my bundled vertex': chapter 9.2
- Get a vertex its 'my_bundled_vertex' from its vertex descriptor: chapter 9.3
- Set a vertex its 'my_bundled_vertex' using its vertex descriptor: chapter 9.4
- Setting all vertices their 'my_bundled_vertex'-es: chapter 9.5
- Storing an directed/undirected graph with bundled vertices as a .dot file: chapter 9.6
- Loading a directed graph with bundled vertices from a .dot file: chapter 9.7
- Loading an undirected directed graph with bundled vertices from a .dot file: chapter 9.8

9.1 Has a bundled vertex with a my bundled vertex

Before modifying our vertices, let's first determine if we can find a vertex by its bundled type ('my_bundled_vertex') in a graph. After obtain the vertex iterators, we can dereference each these to obtain the vertex descriptors and then compare each vertex its 'my bundled vertex' with the one desired.

Algorithm 171 Find if there is vertex with a certain my_bundled_vertex

```
#include <string>
#include <boost/graph/properties.hpp>
#include "my_bundled_vertex.h"

template <typename graph>
bool has_bundled_vertex_with_my_vertex(
    const my_bundled_vertex& v,
    const graph& g
) noexcept
{
    using vd = typename graph::vertex_descriptor;

    const auto vip = vertices(g);
    return std::find_if(vip.first, vip.second,
        [v, g](const vd& d)
        {
        return g[d] == v;
        }
    ) != vip.second;
}
```

This function can be demonstrated as in algorithm 172, where a certain my_bundled_vertex cannot be found in an empty graph. After adding the desired my_bundled_vertex, it is found.

Algorithm 172 Demonstration of the 'has_bundled_vertex_with_my_vertex' function

```
#include <cassert>
#include <iostream>
#include "add bundled vertex.h"
#include "create empty undirected bundled vertices graph.
   h "
#include "has bundled vertex with my vertex.h"
#include "my_bundled_vertex.h"
void has bundled vertex with my vertex demo() noexcept
  auto g = create empty undirected bundled vertices graph
     ();
  assert (! has_bundled_vertex_with_my_vertex(
     my bundled vertex("Felix"),g));
  add bundled vertex(my bundled vertex("Felix"),g);
  assert (has bundled vertex with my vertex (
     my bundled vertex("Felix"),g));
}
```

Note that this function only finds if there is at least one bundled vertex with that my_bundled_vertex: it does not tell how many bundled vertices with that my_bundled_vertex exist in the graph.

$9.2 \quad Find \ a \ bundled \ vertex \ with \ a \ certain \ my_bundled_vertex$

Where STL functions work with iterators, here we obtain a vertex descriptor (see chapter 2.6) to obtain a handle to the desired vertex. Algorithm 173 shows how to obtain a vertex descriptor to the first vertex found with a specific 'my bundled vertex' value.

Algorithm 173 Find the first vertex with a certain my bundled vertex

```
#include <cassert>
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "has bundled vertex with my vertex.h"
#include "my_bundled vertex.h"
template <typename graph>
typename boost::graph\_traits < graph >:: vertex\_descriptor
find_first_bundled_vertex_with_my_vertex(
  const my bundled vertex& v,
  const graph& g
) noexcept
  using vd = typename graph::vertex descriptor;
  const auto vip = vertices(g);
  const auto i = std::find if (
    vip.first , vip.second ,
    [v,g](\mathbf{const}\ vd\ d) \ \{\ \mathbf{return}\ g[d] == v; \ \}
  );
  assert(i != vip.second);
  return *i;
}
```

With the vertex descriptor obtained, one can read and modify the vertex and the edges surrounding it. Algorithm 174 shows some examples of how to do so.

Algorithm 174 Demonstration of the 'find_first_bundled_vertex_with_my_vertex' function

```
#include <cassert>
#include "create_bundled_vertices_k2_graph.h"
#include "find_first_bundled_vertex_with_my_vertex.h"

void find_first_bundled_vertex_with_my_vertex_demo()
    noexcept
{
    const auto g = create_bundled_vertices_k2_graph();
    const auto vd =
        find_first_bundled_vertex_with_my_vertex(
        my_bundled_vertex("Me","Myself",1.0,2.0),
        g
    );
    assert(out_degree(vd,g) == 1);
    assert(in_degree(vd,g) == 1);
}
```

9.3 Get a bundled vertex its 'my_bundled_vertex'

To obtain the 'my_bundled_vertex' from a vertex descriptor is simple:

Algorithm 175 Get a bundled vertex its my vertex from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "my_bundled_vertex.h"

template <typename graph>
my_bundled_vertex get_my_bundled_vertex(
    const typename boost::graph_traits<graph>::
        vertex_descriptor& vd,
    const graph& g
) noexcept
{
    return g[vd];
}
```

One can just use the graph as a property map and let it be looked-up.

To use 'get_bundled_vertex_my_vertex', one first needs to obtain a vertex descriptor. Algorithm 176 shows a simple example.

Algorithm 176 Demonstration if the 'get_bundled_vertex_my_vertex' function

9.4 Set a bundled vertex its my vertex

If you know how to get the 'my_bundled_vertex' from a vertex descriptor, setting it is just as easy, as shown in algorithm 177.

Algorithm 177 Set a bundled vertex its my vertex from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "my_bundled_vertex.h"

template <typename graph>
void set_my_bundled_vertex(
    const my_bundled_vertex& v,
    const typename boost::graph_traits<graph>::
        vertex_descriptor& vd,
    graph& g
) noexcept
{
    static_assert(!std::is_const<graph>::value,"graph_cannot_be_const");
    g[vd] = v;
}
```

To use 'set_bundled_vertex_my_vertex', one first needs to obtain a vertex descriptor. Algorithm 178 shows a simple example.

Algorithm 178 Demonstration if the 'set_bundled_vertex_my_vertex' function

```
#include < cassert >
#include "add bundled vertex.h"
#include "create empty undirected bundled vertices graph.
#include "find_first_bundled_vertex_with_my_vertex.h"
#include "get my bundled vertex.h"
#include "set my bundled vertex.h"
void set_my_bundled_vertex_demo() noexcept
  auto g = create empty undirected bundled vertices graph
     ();
  const my bundled vertex old name{"Dex"};
  add bundled vertex (old name, g);
  {f const} auto {
m vd} =
     find_first_bundled_vertex_with_my_vertex(old_name,g)
  assert (get my bundled vertex (vd, g) == old name);
  const my bundled vertex new name{"Diggy"};
  set my bundled vertex (new name, vd, g);
  assert (get_my_bundled_vertex(vd, g) == new_name);
}
```

9.5 Setting all bundled vertices' my vertex objects

When the vertices of a graph are 'my_bundled_vertex' objects, one can set these as such:

Algorithm 179 Setting the bundled vertices' 'my bundled vertex'-es

```
#include < string>
#include < vector >
#include <boost/graph/graph traits.hpp>
#include <boost/graph/properties.hpp>
#include "my bundled vertex.h"
template <typename graph>
void set_my_bundled_vertexes(
  graph&g,
  const std::vector<my bundled vertex>& my vertexes
 noexcept
  static\_assert (!std::is\_const < graph > :: value,
    "graph_cannot_be_const"
  );
  auto my vertexes begin = std::begin(my vertexes);
  const auto my vertexes end = std::end(my vertexes);
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (
    auto i = vip.first;
    i!=j; ++i,
   ++my_vertexes_begin
    assert (my vertexes begin != my vertexes end);
    g[*i] = *my \text{ vertexes begin};
}
```

9.6 Storing a graph with bundled vertices as a .dot

If you used the 'create_bundled_vertices_k2_graph' function (algorithm 168) to produce a K_2 graph with vertices associated with 'my_bundled_vertex' objects, you can store these with algorithm 180:

Algorithm 180 Storing a graph with bundled vertices as a .dot file

This code looks small, because we call the 'make_bundled_vertices_writer' function, which is shown in algorithm 181:

Algorithm 181 The 'make bundled vertices writer' function

```
template <typename graph>
inline bundled_vertices_writer<graph>
make_bundled_vertices_writer(
   const graph& g
)
{
   return bundled_vertices_writer<
      graph
   >(g);
}
```

Also this function is forwarding the real work to the 'bundled_vertices_ writer', shown in algorithm 182:

Algorithm 182 The 'bundled vertices writer' function

```
#include <ostream>
#include "graphviz_encode.h"
#include "is_graphviz_friendly.h"
template <
  typename graph
class bundled_vertices_writer {
public:
  bundled vertices writer (
    graph g
    : m_g\{g\}
  template < class vertex descriptor>
  void operator()(
    std::ostream& out,
    const vertex_descriptor& vd
  ) const noexcept {
    out
      << " [ label = \""
        << graphviz_encode(</pre>
           m_g[vd].m_name
      << "\", comment =\""
        << graphviz encode(</pre>
          m_g[vd].m_description
      << " \ " , w i d t h="
        << m_g[vd].m_x
      << ", height="
        << m_g[vd].m_y
      << " ] "
private:
  graph m g;
};
```

Here, some interesting things are happening: the writer needs the bundled property maps to work with and thus copies the whole graph to its internals. I have chosen to map the 'my bundled vertex' member variables to Graphviz

attributes (see chapter 25.2 for most Graphviz attributes) as shown in table 2:

my_bundled_vertex variable	C++ data type	Graphviz data type	Graphviz attribute
m_name	std::string	string	label
$m_description$	std::string	string	comment
m_x	double	double	width
m_y	double	double	height

Table 2: Mapping of my_bundled_vertex member variable and Graphviz attributes

Important in this mapping is that the C++ and the Graphviz data types match. I also chose attributes that matched as closely as possible.

The writer also encodes the std::string of the name and description to a Graphviz-friendly format. When loading the .dot file again, this will have to be undone again.

9.7 Loading a directed graph with bundled vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with bundled vertices is loaded, as shown in algorithm 183:

 $\bf Algorithm~183$ Loading a directed graph with bundled vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create_empty_directed_bundled_vertices_graph.h"
#include "graphviz decode.h"
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  my bundled vertex
load directed bundled vertices graph from dot (
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g = create empty directed bundled vertices graph()
  boost::dynamic properties dp(boost::
     ignore_other_properties);
  dp.property("label",get(&my_bundled_vertex::m_name, g))
  dp.property("comment", get(&my bundled vertex::
     m_description, g));
  dp.property("width", get(&my_bundled_vertex::m_x, g));
  dp.property("height", get(&my bundled vertex::m y, g));
  boost::read graphviz(f,g,dp);
  //Decode vertices
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i)
    g[*i].m_name = graphviz_decode(g[*i].m_name);
    g[*i].m description = graphviz decode(g[*i].
       m description);
  return g;
}
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created, to save typing the typename explicitly.

Then a boost::dynamic_properties is created with its default constructor, after which we set it to follow the same mapping as in the previous chapter. From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

At the moment the graph is created, all 'my_bundled_vertex' their names and description are in a Graphviz-friendly format. By obtaining all vertex iterators and vertex descriptors, the encoding is made undone.

Algorithm 184 shows how to use the 'load_directed_bundled_vertices_graph_from_dot' function:

Algorithm 184 Demonstration of the 'load_directed_bundled_vertices_graph_from_dot' function

```
#include "create bundled vertices markov chain.h"
#include "load directed bundled vertices graph from dot.h
#include "save bundled vertices graph to dot.h"
#include "get my bundled vertexes.h"
void load directed bundled vertices graph from dot demo()
    noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create bundled vertices markov chain();
  const std::string filename{
    "create bundled vertices markov chain.dot"
  save bundled vertices graph to dot(g, filename);
  const auto h
    = load directed bundled vertices graph from dot(
       filename);
  assert(num\_edges(g) == num\_edges(h));
  assert(num \ vertices(g) == num \ vertices(h));
  assert (get my bundled vertexes (g) ==
     get my bundled vertexes(h));
}
```

This demonstration shows how the Markov chain is created using the 'create_bundled_vertices_markov_chain' function (algorithm 165), saved and then loaded. The loaded graph is checked to be the same as the original.

9.8 Loading an undirected graph with bundled vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with bundled vertices is loaded, as shown in algorithm 185:

 ${\bf Algorithm~185~Loading~an~undirected~graph~with~bundled~vertices~from~a~.dot~file}$

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create_empty_undirected_bundled_vertices_graph.
   h "
#include "graphviz decode.h"
#include "is_regular_file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  my bundled vertex
load_undirected_bundled_vertices_graph_from_dot(
  const std::string& dot filename
{
  assert(is_regular_file(dot_filename));
  std::ifstream f(dot filename.c str());
  auto g = create_empty_undirected_bundled_vertices_graph
     ();
  boost::dynamic properties dp(boost::
     ignore other properties);
  dp.property("label", get(&my_bundled_vertex::m_name, g))
  dp.property("comment", get(&my_bundled_vertex::
     m description, g));
  dp.property("width", get(&my_bundled_vertex::m_x, g));
  dp.property("height", get(&my bundled vertex::m y, g));
  boost::read graphviz(f,g,dp);
  //Decode vertices
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (auto i = vip.first; i!=j; ++i)
    g[*i].m_name = graphviz_decode(g[*i].m_name);
    g[*i].m description = graphviz decode(g[*i]).
       m description);
  return g;
}
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 9.7 describes the rationale of this function.

Algorithm 186 shows how to use the 'load_undirected_bundled_vertices_graph_from_dot' function:

Algorithm 186 Demonstration of the 'load_undirected_bundled_vertices_graph_from_dot' function

```
#include < cassert >
#include "create bundled vertices k2 graph.h"
#include "load undirected bundled vertices graph from dot
   . h"
#include "save bundled_vertices_graph_to_dot.h"
#include "get my bundled vertexes.h"
void load undirected bundled vertices graph from dot demo
   () noexcept
{
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create_bundled_vertices_k2_graph();
  const std::string filename{
    "create\_bundled\_vertices\_k2\_graph.dot"
  save bundled vertices graph to dot(g, filename);
  const auto h
    = load undirected bundled vertices graph from dot(
       filename);
  assert (get my bundled vertexes (g)
    == get my bundled vertexes(h)
  );
}
```

This demonstration shows how K_2 with bundled vertices is created using the 'create_bundled_vertices_k2_graph' function (algorithm 168), saved and then loaded. The loaded graph is checked to be the same as the original.

10 Building graphs with bundled edges and vertices

Up until now, the graphs created have had only bundled vertices. In this chapter, graphs will be created, in which both the edges and vertices have a bundled

'my bundled edge' and 'my bundled edge' type⁹.

- An empty directed graph that allows for bundled edges and vertices: see chapter 10.2
- An empty undirected graph that allows for bundled edges and vertices: see chapter 10.3
- \bullet A two-state Markov chain with bundled edges and vertices: see chapter 10 6
- K_3 with bundled edges and vertices: see chapter 10.7

In the process, some basic (sometimes bordering trivial) functions are shown:

- Creating the 'my bundled edge' class: see chapter 10.1
- Adding a bundled 'my_bundled_edge': see chapter 10.4

These functions are mostly there for completion and showing which data types are used.

10.1 Creating the bundled edge class

In this example, I create a 'my_bundled_edge' class. Here I will show the header file of it, as the implementation of it is not important yet.

⁹I do not intend to be original in naming my data types

Algorithm 187 Declaration of my bundled edge

```
#include < string>
#include <iosfwd>
class my bundled edge
public:
  explicit my bundled edge (
    const std::string& name = "",
    const std::string& description = "",
    const double width = 1.0,
    const double height = 1.0
  ) noexcept;
  std::string m_name;
  std::string m description;
  double m width;
  double m_height;
};
bool operator == (const my bundled edge& lhs, const
   my bundled edge& rhs) noexcept;
{\bf bool\ operator!} = ({\bf const\ my\_bundled\_edge\&\ lhs}\;,\;\; {\bf const}
   my bundled edge& rhs) noexcept;
```

my_bundled_edge is a class that has multiple properties: two doubles 'm_width' ('m_' stands for member) and 'm_height', and two std::strings m_name and m_description. 'my_bundled_edge' is copyable, but cannot trivially be converted to a 'std::string.' 'my_bundled_edge' is comparable for equality (that is, operator== is defined).

'my_bundled_edge' does not have to have the stream operators defined for file I/O, as this goes via the public member variables.

10.2 Create an empty directed graph with bundled edges and vertices

Algorithm 188 Creating an empty directed graph with bundled edges and vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_edge.h"
#include "my_bundled_vertex.h"

boost:: adjacency_list <
    boost:: vecS,
    boost:: vecS,
    boost:: directedS,
    my_bundled_vertex,
    my_bundled_edge
>
create_empty_directed_bundled_edges_and_vertices_graph()
    noexcept
{
    return {};
}
```

This code is very similar to the code described in chapter 12.3, except that there is a new, fifth template argument:

```
boost::property<boost::edge_bundled_type_t, my_edge>
```

This can be read as: "edges have the property 'boost::edge_bundled_type_t', which is of data type 'my_bundled_edge". Or simply: "edges have a bundled type called my_bundled_edge".

Demo:

```
Algorithm
                189
                                                   the
                                                            'cre-
                          Demonstration
ate\_empty\_directed\_bundled\_edges\_and\_vertices\_graph' function
#include "
   create_empty_directed_bundled_edges_and_vertices_graph
    . h"
void
   create empty directed bundled edges and vertices graph demo
    () noexcept
  const auto g =
     create empty directed bundled edges and vertices graph
  assert(boost::num\_edges(g) == 0);
  assert(boost::num \ vertices(g) == 0);
}
```

10.3 Create an empty undirected graph with bundled edges and vertices

Algorithm 190 Creating an empty undirected graph with bundled edges and vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_edge.h"
#include "my_bundled_vertex.h"

boost::adjacency_list <
   boost::vecS,
   boost::vecS,
   boost::undirectedS,
   my_bundled_vertex,
   my_bundled_edge
>
create_empty_undirected_bundled_edges_and_vertices_graph
        () noexcept
{
   return {};
}
```

This code is very similar to the code described in chapter 10.2, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS). Demo:

```
Algorithm
                 191
                          Demonstration
                                             of
                                                    the
                                                             'cre-
ate\_empty\_undirected\_bundled\_edges\_and\_vertices\_graph' function
#include <cassert>
#include "
   create_empty_undirected_bundled_edges_and_vertices_graph
void
   create\_empty\_undirected\_bundled\_edges\_and\_vertices\_graph\_demo
    () noexcept
  const auto g
        create\_empty\_undirected\_bundled\_edges\_and\_vertices\_graph
  assert(boost::num\_edges(g) == 0);
  assert (boost::num vertices(g) == 0);
```

10.4 Add a bundled edge

Adding a bundled edge is very similar to adding a named edge (chapter 6.3).

Algorithm 192 Add a bundled edge

```
#include <cassert>
#include <boost/graph/adjacency_list.hpp>
#include "my_bundled_edge_h"
template <typename graph>
\mathbf{typename} \hspace{0.2cm} \texttt{boost} :: \mathtt{graph\_traits} \negthinspace < \negthinspace \mathtt{graph} \negthinspace > \negthinspace :: \mathtt{edge\_descriptor}
add bundled edge (
  \textbf{const typename} \hspace{0.2cm} \texttt{boost} :: \texttt{graph\_traits} \negthinspace < \negthinspace \texttt{graph} \negthinspace > \negthinspace ::
        vertex descriptor& vd from,
  const typename boost::graph traits<graph>::
       vertex descriptor& vd to,
  const my_bundled_edge& v,
   graph& g
  noexcept
   static assert (!std::is const<graph>::value, "graph_
       cannot_be_const");
  const auto aer = boost::add_edge(vd_from, vd_to, g);
   assert (aer.second);
  g[aer.first] = v;
  return aer.first;
}
```

When having added a new (abstract) edge to the graph, the edge descriptor is used to set the my edge in the graph.

Here is the demo:

Algorithm 193 Demo of 'add bundled edge'

```
#include <cassert>
\#include "add_bundled_edge.h"
#include "add_bundled_vertex.h"
#include "
   create\_empty\_directed\_bundled\_edges\_and\_vertices\_graph
    . h"
void add_bundled_edge_demo() noexcept
  auto g =
      create_empty_directed_bundled_edges_and_vertices_graph
  const auto vd_from = add_bundled_vertex(
      my bundled vertex("From"), g);
  const auto vd to = add bundled vertex (my bundled vertex
      ("To"), g);
  \verb|add_bundled_edge| (\verb|vd_from|, | \verb|vd_to|, | \verb|my_bundled_edge| ("X")|,
  assert(boost::num\_vertices(g) == 2);
  assert(boost::num\_edges(g) == 1);
```

10.5 Getting the bundled edges my edges

When the edges of a graph are 'my_bundled_edge' objects, one can extract these all as such:

Algorithm 194 Get the edges' my bundled edges

```
#include < vector>
#include <boost/graph/adjacency list.hpp>
#include "my_bundled_edge.h"
template <typename graph>
std::vector<my bundled edge> get my bundled edges(
  const graph& g
) noexcept
{
  using ed = typename boost::graph traits<graph>::
      edge descriptor;
  std::vector<my bundled edge> v(boost::num edges(g));
  const auto eip = edges(g);
  std::transform(eip.first, eip.second, std::begin(v),
    [g](\mathbf{const} \ ed \ e) \ \{ \ \mathbf{return} \ g[e]; \ \}
  );
  return v;
}
```

The 'my_bundled_edge' object associated with the edges are obtained from the graph its property map and then put into a std::vector.

Note: the order of the my_bundled_edge objects may be different after saving and loading.

When trying to get the edges' my_bundled_edge objects from a graph without bundled edges objects associated, you will get the error 'formed reference to void' (see chapter 24.1).

10.6 Creating a Markov-chain with bundled edges and vertices

10.6.1 Graph

Figure 44 shows the graph that will be reproduced:



Figure 44: A two-state Markov chain where the edges and vertices have bundled properies. The edges' and vertices' properties are nonsensical

10.6.2 Function to create such a graph

Here is the code creating a two-state Markov chain with bundled edges and vertices:

Algorithm 195 Creating the two-state Markov chain as depicted in figure 44

```
#include <cassert>
#include "
   create empty directed bundled edges and vertices graph
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS,
  my bundled vertex,
  my bundled edge
create bundled edges and vertices markov chain () noexcept
  auto g
        create empty directed bundled edges and vertices graph
        ();
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  {f const\ auto}\ {f aer\_ba} = {f boost}:: {f add\_edge}({f vd\_b},\ {f vd\_a},\ {f g}) \; ;
  assert (aer ba.second);
  const auto aer bb = boost::add edge(vd b, vd b, g);
  assert (aer bb.second);
  g [vd a]
    = my bundled vertex("Stable", "Right", 1.0, 2.0);
  g[vd b]
    = my bundled vertex("Not_unstable", "Not_left"
        ,3.0,4.0);
  g[aer aa.first]
    = my bundled edge("Red", "Heat", 1.0, 2.0);
  g[aer ab.first]
    = my bundled edge("Orange", "Lose_heat", 3.0,4.0);
  g[aer ba.first]
    = my bundled edge("Yellow_cold", "Heat", 5.0, 6.0);
  g[aer bb.first]
    = my bundled edge("Green_cold", "Stay_cool", 7.0, 8.0);
  return g;
```

10.6.3 Creating such a graph

Here is the demo:

```
Algorithm 196 Demo of the 'create bundled edges and vertices markov chain'
function (algorithm 195)
#include <cassert>
#include "create bundled edges and vertices markov chain.
#include "get my bundled edges.h"
#include "my bundled vertex.h"
void create bundled edges and vertices markov chain demo
   () noexcept
  const auto g =
     create bundled edges and vertices markov chain();
  const std::vector<my bundled edge> edge my edges{
    get my bundled edges (g)
  };
  const std::vector<my bundled edge> expected my edges{
    my_bundled_edge("Red","Heat",1.0,2.0),
    my bundled edge("Orange", "Lose_heat", 3.0, 4.0),
    my bundled edge("Yellow_cold", "Heat", 5.0, 6.0),
    my\_bundled\_edge("Green\_cold", "Stay\_cool", 7.0, 8.0)
  assert (edge my edges == expected my edges);
```

10.6.4 The .dot file produced

```
Algorithm
               197
                       .dot
                                                 from
                                                         the
                                                                 'cre-
ate bundled edges and vertices markov chain'
                                                function
                                                           (algorithm
195), converted from graph to .dot file using algorithm 52
digraph G {
0[label="Stable",comment="Right",width=1,height=2];
1[label="Not$$$SPACE$$$unstable",comment="Not$$$SPACE$$$left",width=3,height=4];
0->0 [label="Red",comment="Heat",width=1,height=2];
0->1 [label="Orange",comment="Lose$$$SPACE$$$heat",width=3,height=4];
1->0 [label="Yellow$$$SPACE$$$cold",comment="Heat",width=5,height=6];
1->1 [label="Green$$$SPACE$$$cold",comment="Stay$$$SPACE$$$cool",width=7,height=8];
```

10.6.5 The .svg file produced

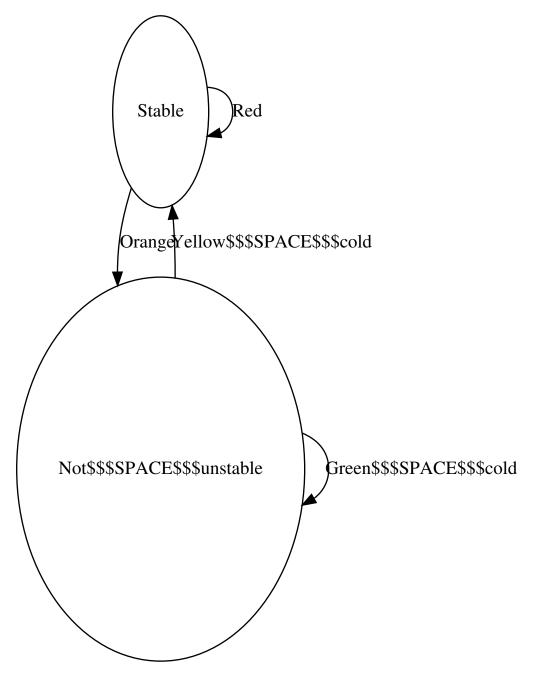


Figure 45: .svg file created from the 'create_bundled_edges_and_vertices_markov_chain' function (algorithm 224) its .dot file, converted from .dot file to .svg using algorithm 361

10.7 Creating K_3 with bundled edges and vertices

Instead of using edges with a name, or other properties, here we use a bundled edge class called 'my_bundled_edge'.

10.7.1 Graph

We reproduce the K_3 with named edges and vertices of chapter 6.8, but with our bundled edges and vertices intead:

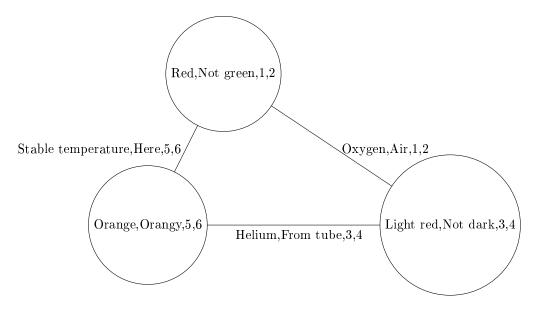


Figure 46: K_3 : a fully connected graph with three named edges and vertices

Algorithm 198 Creating K_3 as depicted in figure 33

```
#include "
   create empty undirected bundled edges and vertices graph
    . h"
#include "add_bundled_edge.h"
#include "add bundled vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  my_bundled_vertex,
  my\_bundled\_edge
create bundled edges and vertices k3 graph() noexcept
  auto g
       create empty undirected bundled edges and vertices graph
  const auto vd a = add bundled vertex (
    my bundled vertex ("Red", "Not_green", 1.0, 2.0),
    g
  );
  const auto vd b = add bundled vertex (
    my bundled vertex("Light_red", "Not_dark", 3.0, 4.0),
    g
  );
  const auto vd c = add bundled vertex (
    my_bundled_vertex("Orange", "Orangy", 5.0,6.0),
    g
  );
  add bundled edge (vd a, vd b,
    my bundled edge("Oxygen", "Air", 1.0, 2.0),
    g
  add bundled edge(vd b, vd c,
    my\_bundled\_edge("Helium", "From\_tube", 3.0, 4.0),
  );
  add bundled edge(vd c, vd a,
    my_bundled_edge("Stable_temperature", "Here", 5.0, 6.0),
    g
  );
  return g;
                             221
}
```

Most of the code is a slight modification of algorithm 132. In the end, the my_edges and my_vertices are obtained as the graph its property_map and set with the 'my_bundled_edge' and 'my_bundled_vertex' objects.

10.7.3 Creating such a graph

Here is the demo:

Algorithm 199 Demo of the 'create_bundled_edges_and_vertices_k3_graph' function (algorithm 198)

10.7.4 The .dot file produced

```
Algorithm
               200
                       .dot
                               file
                                      created
                                                 from
                                                          the
                                                                 'cre-
ate bundled edges and vertices markov chain'
                                                function
                                                            (algorithm
198), converted from graph to .dot file using algorithm 52
O[label="Red",comment="Not$$$SPACE$$$green",width=1,height=2];
1[label="Light$$$PACE$$$red",comment="Not$$$$PACE$$$dark",width=3,height=4];
2[label="Orange",comment="Orangy",width=5,height=6];
0--1 [label="Oxygen",comment="Air",width=1,height=2];
1--2 [label="Helium",comment="From$$$$PACE$$$tube",width=3,height=4];
2--0 [label="Stable$$$SPACE$$$temperature",comment="Here",width=5,height=6];
```

10.7.5 The .svg file produced

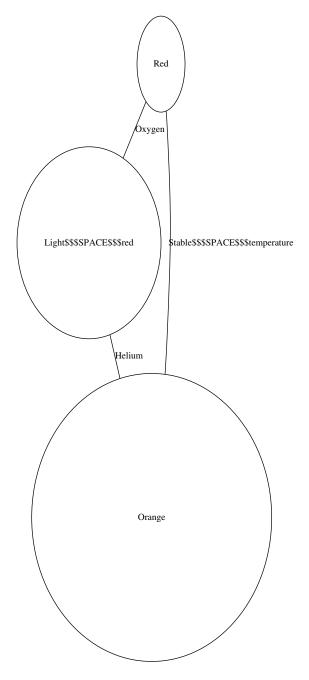


Figure 47: .svg file created from the 'create_bundled_edges_and_vertices_k3_graph' function (algorithm 224) its .dot file, converted from .dot file to .svg using algorithm 361

11 Working on graphs with bundled edges and vertices

$11.1 \quad Has \ a \ my_bundled_edge$

Before modifying our edges, let's first determine if we can find an edge by its bundled type ('my_bundled_edge') in a graph. After obtaing a my_bundled_edge map, we obtain the edge iterators, dereference these to obtain the edge descriptors and then compare each edge its my_bundled_edge with the one desired.

Algorithm 201 Find if there is a bundled edge with a certain my bundled edge

```
#include <boost/graph/properties.hpp>
#include "my_bundled_edge.h"

template <typename graph>
bool has_bundled_edge_with_my_edge(
    const my_bundled_edge& e,
    const graph& g
) noexcept
{
    using ed = typename boost::graph_traits<graph>::
        edge_descriptor;
    const auto eip = edges(g);
    return std::find_if(eip.first, eip.second,
        [e, g](const ed& d)
        {
            return g[d] == e;
        }
        ) != eip.second;
}
```

This function can be demonstrated as in algorithm 202, where a certain 'my_bundled_edge' cannot be found in an empty graph. After adding the desired my_bundled_edge, it is found.

Algorithm 202 Demonstration of the 'has_bundled_edge_with_my_edge' function

Note that this function only finds if there is at least one edge with that my_bundled_edge: it does not tell how many edges with that my_bundled_edge exist in the graph.

11.2 Find a my bundled edge

Where STL functions work with iterators, here we obtain an edge descriptor (see chapter 2.12) to obtain a handle to the desired edge. Algorithm 203 shows how to obtain an edge descriptor to the first edge found with a specific my_bundled_edge value.

Algorithm 203 Find the first bundled edge with a certain my bundled edge

```
#include <cassert>
#include <boost/graph/graph_traits.hpp>
#include "has_bundled_edge_with_my_edge.h"
#include "has edge with my edge.h"
#include "my_bundled edge.h"
template <typename graph>
typename boost::graph\_traits < graph > ::edge\_descriptor
find_first_bundled_edge_with_my_edge(
  const my bundled edge& e,
  const graph& g
) noexcept
  using ed = typename boost::graph traits<graph>::
      edge descriptor;
  const auto eip = edges(g);
  const auto i = std::find if (
    eip.first, eip.second,
    [e,g](\mathbf{const}\ ed\ d) \ \{\ \mathbf{return}\ g[d] == e; \ \}
  );
  assert (i != eip.second);
  return *i;
```

With the edge descriptor obtained, one can read and modify the edge and the vertices surrounding it. Algorithm 204 shows some examples of how to do

Algorithm 204 Demonstration of the 'find_first_bundled_edge_with_my_edge' function

11.3 Get an edge its my_bundled_edge

To obtain the my_bundled_edge from an edge descriptor, one needs to pull out the my_bundled_edges map and then look up the my_edge of interest.

Algorithm 205 Get a vertex its my bundled vertex from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include "my_bundled_edge.h"

template <typename graph>
my_bundled_edge get_my_bundled_edge(
   const typename boost::graph_traits<graph>::
      edge_descriptor& ed,
   const graph& g
) noexcept
{
   return g[ed];
}
```

To use 'get $_{\rm my}$ bundled $_{\rm edge}$ ', one first needs to obtain an edge descriptor. Algorithm 206 shows a simple example.

Algorithm 206 Demonstration if the 'get my bundled edge' function

```
#include <cassert>
#include "add bundled edge.h"
#include "add bundled vertex.h"
#include "
   create_empty_undirected_bundled_edges_and_vertices_graph
   . h"
#include "find_first_bundled_edge_with_my_edge.h"
#include "get my bundled edge.h"
void get my bundled edge demo() noexcept
  auto g
        create empty undirected bundled edges and vertices graph
  const my bundled edge edge{"Dex"};
  const auto vd a = add bundled vertex (
    my_bundled_vertex("A"), g
  const auto vd_b = add_bundled_vertex(
    my bundled vertex ("B"), g
  );
  add bundled_edge(vd_a, vd_b, edge, g);
  \mathbf{const} \ \mathbf{auto} \ \mathrm{ed}
    = find first bundled edge with my edge(edge, g);
  assert (get my bundled edge (ed, g) == edge);
```

11.4 Set an edge its my_bundled_edge

If you know how to get the my_bundled_edge from an edge descriptor, setting it is just as easy, as shown in algorithm 207.

Algorithm 207 Set a bundled edge its my_bundled_edge from its edge descriptor

To use 'set_bundled_edge_my_edge', one first needs to obtain an edge descriptor. Algorithm 208 shows a simple example.

Algorithm 208 Demonstration if the 'set bundled edge my edge' function

```
#include <cassert>
#include "add bundled edge.h"
#include "add bundled vertex.h"
#include "
   create empty undirected bundled edges and vertices graph
   . h"
#include "find first bundled edge with my edge.h"
#include "get my bundled edge.h"
#include "set my bundled edge.h"
void set my bundled edge demo() noexcept
  auto g
       create empty undirected bundled edges and vertices graph
       ();
  const auto vd a = add bundled vertex(my bundled vertex{
     "A" } , g);
  const auto vd b = add bundled vertex(my bundled vertex{
     "B" } , g);
  const my bundled edge old edge {"Dex"};
  add bundled edge(vd a, vd b, old edge, g);
  const auto vd
    = find_first_bundled_edge_with_my_edge(old_edge,g);
  assert (get my bundled edge (vd,g)
    == old edge
  const my bundled edge new edge{"Diggy"};
  set my bundled edge(new edge, vd, g);
  assert (get my bundled edge (vd,g)
    == new edge
  );
}
```

11.5 Storing a graph with bundled edges and vertices as a .dot

If you used the 'create_bundled_edges_and_vertices_k3_graph' function (algorithm 198) to produce a K_3 graph with edges and vertices associated with my_bundled_edge and my_bundled_vertex objects, you can store these my_bundled_edges and my_bundled_vertex-es additionally with algorithm 209:

Algorithm 209 Storing a graph with bundled edges and vertices as a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "make_bundled_vertices_writer.h"
#include "make_bundled_edges_writer.h"

template <typename graph>
void save_bundled_edges_and_vertices_graph_to_dot(
    const graph& g,
    const std::string& filename
)
{
    std::ofstream f(filename);
    boost::write_graphviz(
        f,
        g,
        make_bundled_vertices_writer(g),
        make_bundled_edges_writer(g)
);
}
```

11.6 Load a directed graph with bundled edges and vertices from a .dot file

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with bundled edges and vertices is loaded, as shown in algorithm 210:

 ${f Algorithm~210}$ Loading a directed graph with bundled edges and vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create _ empty _ directed _ bundled _ edges _ and _ vertices _ graph
   . h"
#include "is regular file.h"
#include "graphviz decode.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  my bundled vertex,
  my_bundled_edge
load directed bundled edges and vertices graph from dot (
  const std::string& dot filename
  assert(is_regular_file(dot_filename));
  std::ifstream f(dot_filename.c_str());
     create empty directed bundled edges and vertices graph
  boost::dynamic properties dp(boost::
     ignore_other_properties);
  dp.property("label",get(&my_bundled_vertex::m_name, g))
  dp.property("comment", get(&my bundled vertex::
     m description, g));
  dp.property("width", get(&my_bundled_vertex::m_x, g));
  \tt dp.property("height", get(\&my\_bundled\_vertex::m\_y, g));\\
  dp.property("edge_id",get(&my_bundled_edge::m_name, g))
  dp.property("label",get(&my_bundled_edge::m_name, g));
  dp.property("comment", get(&my_bundled_edge::
     m description, g));
  dp.property("width", get(&my bundled edge::m width, g))
  dp.property("height", get(&my_bundled_edge::m_height, g
  boost::read graphviz(f,g,dp);
  //Decode vertices
                             233
    const auto vip = vertices(g);
    const auto j = vip.second;
    for (auto i = vip.first; i!=j; ++i)
      g[*i].m name = graphviz decode(g[*i].m name);
      g[*i].m\_description = graphviz\_decode(g[*i].
          m description);
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Next to this, a boost::dynamic_properties is created with its default constructor, after which we direct the boost::dynamic_properties to find a 'node_id' and 'label' in the vertex name map, 'edge_id' and 'label' to the edge name map. From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

 $Algorithm\ 211\ shows\ how\ to\ use\ the\ 'load_directed_bundled_edges_and_vertices_graph_from_dot'\ function:$

Algorithm 211 Demonstration of the 'load_directed_bundled_edges_and_vertices_graph_from_dot' function

```
#include "create bundled edges and vertices markov chain.
   h"
#include "get_sorted_bundled_vertex_my vertexes.h"
#include
   load directed bundled edges and vertices graph from dot
   . h"
#include "save bundled edges and vertices graph to dot.h"
void
   load directed bundled edges and vertices graph from dot demo
   () noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create bundled edges and vertices markov chain();
  const std::string filename{
    "create bundled edges and vertices markov chain.dot"
  save bundled edges and vertices graph to dot(g,
     filename);
  const auto h
       load directed bundled edges and vertices graph from dot
      filename
    );
  assert(num edges(g) == num edges(h));
  assert(num \ vertices(g) == num \ vertices(h));
  assert (get sorted bundled vertex my vertexes (g)
    == get sorted bundled vertex my vertexes(h)
  );
}
```

This demonstration shows how the Markov chain is created using the 'create_bundled_edges_and_vertices_markov_chain' function (algorithm 195), saved and then loaded.

11.7 Load an undirected graph with bundled edges and vertices from a .dot file

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with bundled edges and vertices is loaded, as shown in algorithm 212:

 ${\bf Algorithm~212}~{\bf Loading~an~undirected~graph~with~bundled~edges~and~vertices~from~a~.dot~file$

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create_empty_undirected_bundled_edges_and_vertices_graph
   . h"
#include "is regular file.h"
#include "graphviz decode.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  my bundled vertex,
  my\_bundled\_edge
load undirected bundled edges and vertices graph from dot
  const std::string& dot filename
  assert (is_regular_file (dot_filename));
  std::ifstream f(dot filename.c str());
  auto g =
     create empty undirected bundled edges and vertices graph
     ();
  boost::dynamic_properties dp(boost::
     ignore other properties);
  dp.property("label", get(&my bundled vertex::m name, g))
  dp.property("comment", get(&my_bundled_vertex::
     m description, g));
  \tt dp.property("width", get(\&my\_bundled\_vertex::m\_x, g));\\
  \tt dp.property("height", get(\&my\_bundled\_vertex::m\_y, g));\\
  dp.property("edge_id",get(&my_bundled_edge::m_name, g))
  dp.property("label",get(&my_bundled_edge::m_name, g));
  dp.property("comment", get(&my_bundled_edge::
     m description, g));
  dp.property("width", get(&my_bundled_edge::m_width, g))
  dp.property("height", get(&my_bundled_edge::m_height, g
  boost::read_graphviz(f,g,dp);
                             237
  //Decode vertices
    const auto vip = vertices(g);
    const auto j = vip.second;
    for (auto i = vip.first; i!=j; ++i)
      g[*i].m_name = graphviz_decode(g[*i].m_name);
      g[*i].m_description = graphviz_decode(g[*i].
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 11.6 describes the rationale of this function

 $Algorithm\ 213\ shows\ how\ to\ use\ the\ `load_undirected_bundled_vertices_graph_from_dot' function:$

Algorithm 213 Demonstration of the 'load_undirected_bundled_edges_and_vertices_graph_from_dot' function

```
#include "create bundled edges and vertices k3 graph.h"
#include "get sorted bundled vertex my vertexes.h"
#include "
   load undirected bundled edges and vertices graph from dot
   . h"
#include "save bundled edges and vertices graph to dot.h"
void
   load undirected bundled edges and vertices graph from dot demo
   () noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create_bundled_edges_and_vertices_k3_graph();
  const std::string filename{
    "create bundled edges and vertices k3 graph.dot"
  save bundled edges and vertices graph to dot(g,
     filename);
  const auto h
       load undirected bundled edges and vertices graph from dot
      filename
    );
  assert(num\_edges(g) == num\_edges(h));
  assert(num \ vertices(g) == num \ vertices(h));
  assert (get sorted bundled vertex my vertexes (g)
    == get_sorted_bundled_vertex_my_vertexes(h)
  );
}
```

This demonstration shows how K_2 with bundled vertices is created using the 'create_bundled_vertices_k2_graph' function (algorithm 227), saved and

then loaded. The loaded graph is checked to be a graph similar to the original.

12 Building graphs with custom vertices

Instead of using bundled properties, you can also add a new custom property. The difference is that instead of having a class as a vertex, vertices have an additional property where the 'my_custom_vertex' is stored, next to properties like vertex name, edge delay (see chapter 25.1 for all properties). The following graphs will be created:

- An empty directed graph that allows for custom vertices: see chapter 216
- An empty undirected graph that allows for custom vertices: see chapter 12.3
- A two-state Markov chain with custom vertices: see chapter 12.7
- K_2 with custom vertices: see chapter 12.8

In the process, some basic (sometimes bordering trivial) functions are shown:

- Installing a new vertex property, called 'vertex_custom_type': chapter 12.2
- Adding a custom vertex: see chapter 12.5
- Getting the custom vertices my_vertex-es: see chapter 12.6

These functions are mostly there for completion and showing which data types are used.

12.1 Creating the vertex class

Before creating an empty graph with custom vertices, that custom vertex class must be created. In this tutorial, it is called 'my_custom_vertex'. 'my_custom_vertex' is a class that is nonsensical, but it can be replaced by any other class type.

Here I will show the header file of 'my_custom_vertex', as the implementation of it is not important:

Algorithm 214 Declaration of my_custom_vertex

```
#include < string>
#include <iosfwd>
class my custom vertex
public:
  explicit my custom vertex (
    const std::string& name = "",
    const std::string& description = "",
    const double x = 0.0,
    const double y = 0.0
  ) noexcept;
  const std::string& get_description() const noexcept;
  const std::string& get name() const noexcept;
  double get_x() const noexcept;
  \mathbf{double} \ \ \mathtt{get} \_ \mathtt{y} \, (\,) \ \ \mathbf{const} \ \ \mathtt{noexcept} \, ;
private:
  std::string m name;
  std::string m description;
  double m x;
  double m y;
};
bool operator == (const my_custom_vertex& lhs, const
   my_custom_vertex& rhs) noexcept;
bool operator!=(const my custom vertex& lhs, const
   my custom vertex& rhs) noexcept;
bool operator < (const my custom vertex& lhs, const
   my custom vertex& rhs) noexcept;
std::ostream& operator<<(std::ostream& os, const
   my custom vertex& v) noexcept;
std::istream& operator>>(std::istream& os,
   my custom vertex& v) noexcept;
```

'my custom vertex' is a class that has multiple properties:

- It has four private member variables: the double 'm_x' ('m_' stands for member), the double 'm_y', the std::string m_name and the std::string m_description. These variables are private, but there are getters supplied
- It has a default constructor
- It is copyable

- It is comparable for equality (it has operator==), which is needed for searching
- It can be streamed (it has both operator << and operator >>), which is needed for file I/O.

Special characters like comma's, quotes and whitespace cannot be streamed without problems. The function 'graphviz_encode' (algorithm 357) can convert the elements to be streamed to a Graphviz-friendly version, which can be decoded by 'graphviz decode' (algorithm 358).

12.2 Installing the new vertex property

Before creating an empty graph with custom vertices, this type must be installed as a vertex property. Installing a new property would have been easier, if 'more C++ compilers were standards conformant' ([8] chapter 3.6). Boost.Graph uses the BOOST INSTALL PROPERTY macro to allow using a custom property:

Algorithm 215 Installing the vertex custom type property

```
#include <boost/graph/properties.hpp>
namespace boost {
   enum vertex_custom_type_t { vertex_custom_type = 314 };
   BOOST_INSTALL_PROPERTY(vertex, custom_type);
}
```

The enum value 314 must be unique.

12.3 Create the empty directed graph with custom vertices

Algorithm 216 Creating an empty directed graph with custom vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "install_vertex_custom_type.h"
#include "my_custom_vertex.h"

boost::adjacency_list <
   boost::vecS,
   boost::vecS,
   boost::vecs,
   boost::vertex_custom_type_t, my_custom_vertex
   >>
create_empty_directed_custom_vertices_graph() noexcept
{
   return {};
}
```

This graph:

- has its out edges stored in a std::vector (due to the first boost::vecS)
- has its vertices stored in a std::vector (due to the second boost::vecS)
- is directed (due to the boost::directedS)
- The vertices have one property: they have a custom type, that is of data type my vertex (due to the boost::property< boost::vertex custom type t,my vertex>')
- The edges and graph have no properties
- Edges are stored in a std::list

The boost::adjacency_list has a new, fourth template argument 'boost::property
boost::vertex_custom_type_t,my_vertex>'. This can be read as: "vertices
have the property 'boost::vertex_custom_type_t', which is of data type 'my_vertex"'.
Or simply: "vertices have a custom type called my_vertex".
The demo:

Algorithm 217 Demo how to create an empty directed graph with custom vertices

12.4 Create the empty undirected graph with custom vertices

Algorithm 218 Creating an empty undirected graph with custom vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "install_vertex_custom_type.h"
#include "my_custom_vertex.h"

boost::adjacency_list <
   boost::vecS,
   boost::vecS,
   boost::undirectedS,
   boost::property <
      boost::vertex_custom_type_t, my_custom_vertex
>
create_empty_undirected_custom_vertices_graph() noexcept
{
   return {};
}
```

This code is very similar to the code described in chapter 12.3, except that the directedness (the third template argument) is undirected (due to the boost::undirecteds). The demo:

Algorithm 219 Demo how to create an empty undirected graph with custom vertices

12.5 Add a custom vertex

Adding a custom vertex is very similar to adding a named vertex (chapter 4.3).

Algorithm 220 Add a custom vertex

```
#include <type_traits>
#include <boost/graph/adjacency_list.hpp>
#include "install vertex custom type.h"
template <typename graph, typename vertex t>
typename boost::graph traits<graph>::vertex descriptor
add custom vertex (
  const vertex t& v,
  graph& g
 noexcept
  static assert (!std::is const<graph>::value,
    "graph_cannot_be_const"
  const auto vd = boost::add vertex(g);
  const auto my_custom_vertex_map
    = get(boost::vertex_custom_type, g);
  put (my_custom_vertex_map, vd, v);
  return vd;
```

When having added a new (abstract) vertex to the graph, the vertex descriptor is used to set the my vertex in the graph its my vertex map (using

```
'get(boost::vertex_custom_type,g)').
Here is the demo:
```

Algorithm 221 Demo of 'add custom vertex'

```
#include < cassert >
#include "add custom vertex.h"
#include "create_empty_directed_custom_vertices_graph.h"
#include "create empty undirected custom vertices graph.h
void add custom vertex demo() noexcept
  auto g
    = create empty directed custom vertices graph();
  assert(boost::num\_vertices(g) == 0);
  assert(boost::num edges(g) == 0);
  add custom vertex(my custom vertex("X"), g);
  assert(boost::num \ vertices(g) == 1);
  assert(boost::num edges(g) == 0);
  auto h
    = create_empty_undirected_custom_vertices_graph();
  assert(boost::num \ vertices(h) == 0);
  assert(boost::num edges(h) == 0);
  add custom vertex(my custom vertex("X"), h);
  assert(boost::num\_vertices(h) == 1);
  assert(boost::num edges(h) == 0);
}
```

12.6 Getting the vertices' my vertexes¹⁰

When the vertices of a graph have any associated my_vertex, one can extract these as such:

¹⁰the name 'my_vertexes' is chosen to indicate this function returns a container of my_vertex

Algorithm 222 Get the my custom vertex objects

```
#include < vector>
#include <boost/graph/adjacency_list.hpp>
#include "install vertex custom type.h"
#include "my custom vertex.h"
#include "get my custom vertex.h"
template <typename graph>
std::vector<my_custom_vertex> get_my_custom_vertexes(
  const graph& g
 noexcept
  using vd = typename graph::vertex descriptor;
  std::vector<my custom vertex> v(boost::num vertices(g))
  const auto vip = vertices(g);
  std::transform(vip.first, vip.second, std::begin(v),
    [g](const vd& d) {
      return get_my_custom_vertex(d, g);
  );
  return v;
```

The my_vertex object associated with the vertices are obtained from a boost::property map and then put into a std::vector.

The order of the 'my_custom_vertex' objects may be different after saving and loading.

When trying to get the vertices' my_vertex from a graph without my_vertex objects associated, you will get the error 'formed reference to void' (see chapter 24.1).

Demo:

Algorithm 223 Demo how to the vertices' my_custom_vertex objects

```
#include <cassert>
#include "create_custom_vertices_k2_graph.h"
#include "get_my_custom_vertexes.h"

void get_my_custom_vertexes_demo() noexcept
{
   const auto g = create_custom_vertices_k2_graph();
   const std::vector<my_custom_vertex>
        expected_my_custom_vertexes{
        my_custom_vertex("A","source",0.0,0.0),
        my_custom_vertex("B","target",3.14,3.14)
   };
   const std::vector<my_custom_vertex> vertexes{
        get_my_custom_vertexes(g)
   };
   assert(expected_my_custom_vertexes == vertexes);
}
```

12.7 Creating a two-state Markov chain with custom vertices

12.7.1 Graph

Figure 48 shows the graph that will be reproduced:



Figure 48: A two-state Markov chain where the vertices have custom properies and the edges have no properties. The vertices' properties are nonsensical

12.7.2 Function to create such a graph

Here is the code creating a two-state Markov chain with custom vertices:

Algorithm 224 Creating the two-state Markov chain as depicted in figure 48

```
#include <cassert>
#include "create_empty_directed_custom_vertices_graph.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
create custom vertices markov chain() noexcept
{
  auto g
   = create empty directed custom vertices graph();
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer bb = boost::add edge(vd b, vd b, g);
  assert (aer bb.second);
  auto my custom vertex map = get (
    boost::vertex custom type, g
  );
  put (my custom vertex map, vd a,
    my_custom_vertex("Sunny","Yellow_thing",1.0,2.0)
  put (my custom vertex map, vd b,
    my custom vertex ("Rainy", "Grey_things", 3.0, 4.0)
  return g;
}
```

12.7.3 Creating such a graph

Here is the demo:

Algorithm 225 Demo of the 'create_custom_vertices_markov_chain' function (algorithm 224)

```
#include <cassert>
#include "create custom vertices markov chain.h"
#include "get my custom vertexes.h"
void create custom vertices markov chain demo() noexcept
  const auto g
    = create_custom_vertices_markov_chain();
  const std::vector<my custom vertex>
    expected my custom vertexes {
    my custom vertex ("Sunny", "Yellow_thing", 1.0, 2.0),
    my_custom_vertex("Rainy","Grey_things",3.0,4.0)
  };
  const std::vector<my custom vertex>
    vertex my custom vertexes{
    get my custom vertexes(g)
  };
  assert (expected_my_custom_vertexes
    == vertex my custom vertexes
  );
}
```

12.7.4 The .dot file produced

Algorithm 226 .dot file created from the 'create_custom_vertices_markov_chain' function (algorithm 224), converted from graph to .dot file using algorithm 251

```
digraph G {
0[label="Sunny,Yellow$$$SPACE$$$thing,1,1"];
1[label="Rainy,Grey$$$SPACE$$$things,3,3"];
0->0;
1->0;
1->1;
1->1;
}
```

This .dot file may look unexpectedly different: instead of a space, there is this '[[:SPACE:]]' thing. This is because the function 'graphviz_encode' (algorithm 357) made this conversion. In this example, I could have simply surrounded the content by quotes, and this would have worked. I chose to use 'graphviz_encode'

because it works in all contexts.

12.7.5 The .svg file produced

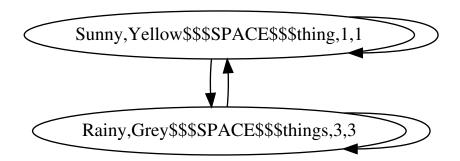


Figure 49: .svg file created from the 'create_custom_vertices_markov_chain' function (algorithm 224) its .dot file, converted from .dot file to .svg using algorithm 361

This .svg file may look unexpectedly different: instead of a space, there is this '[[:SPACE:]]' thing. This is because the function 'graphviz_encode' (algorithm 357) made this conversion.

12.8 Creating K_2 with custom vertices

12.8.1 Graph

We reproduce the K_2 with named vertices of chapter 4.6 , but with our custom vertices intead.

12.8.2 Function to create such a graph

Algorithm 227 Creating K_2 as depicted in figure 20

```
#include "create empty undirected custom vertices graph.h
#include "add custom vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex_custom_type_t, my_custom_vertex
create custom vertices k2 graph() noexcept
  auto g = create_empty_undirected_custom_vertices_graph
     ();
  {\bf const\ auto\ } vd\_a = add\_custom\_vertex(
    my custom vertex ("A", "source", 0.0, 0.0), g
  const auto vd b = add custom vertex(
    my_custom_vertex("B","target",3.14,3.14), g
  const auto aer = boost::add edge(vd a, vd b, g);
  assert (aer.second);
  return g;
}
```

Most of the code is a slight modification of the 'create_named_vertices_k2_graph' function (algorithm 69). In the end, the my_vertices are obtained as a boost::property_map and set with two custom my_vertex objects.

12.8.3 Creating such a graph

Demo:

Algorithm 228 Demo of the 'create_custom_vertices_k2_graph' function (algorithm 227)

```
#include <cassert>
#include "create_custom_vertices_k2_graph.h"
#include "create_custom_vertex_with_my_vertex.h"

void create_custom_vertices_k2_graph_demo() noexcept
{
   const auto g = create_custom_vertices_k2_graph();
   assert(boost::num_edges(g) == 1);
   assert(boost::num_vertices(g) == 2);
   assert(has_custom_vertex_with_my_custom_vertex(
        my_custom_vertex("A", "source", 0.0, 0.0), g)
   );
   assert(has_custom_vertex_with_my_custom_vertex(
        my_custom_vertex("B", "target", 3.14, 3.14), g)
   );
}
```

12.8.4 The .dot file produced

Algorithm 229 .dot file created from the 'create_custom_vertices_k2_graph' function (algorithm 227), converted from graph to .dot file using algorithm 52 graph G {
0[label="A,source,0,0"];
1[label="B,target,3.14,3.14"];
0--1;

12.8.5 The .svg file produced

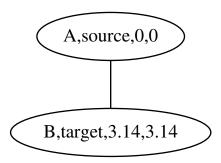


Figure 50: .svg file created from the 'create_custom_vertices_k2_graph' function (algorithm 227) its .dot file, converted from .dot file to .svg using algorithm 361

12.9 Creating a path graph with custom vertices

Here we create a path graph with custom vertices

12.9.1 Graph

Here I show a path graph with four vertices (see figure 51):



Figure 51: A path graph with four vertices

12.9.2 Function to create such a graph

To create a path graph, the following code can be used:

Algorithm 230 Creating a path graph as depicted in figure 51

```
#include < vector >
#include "add_custom_vertex.h"
#include "create empty undirected custom vertices graph.h
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
create_custom_vertices_path_graph(
  const std::vector<my custom vertex>& names
) noexcept
{
  auto g = create empty undirected custom vertices graph
     ();
  if (names.size() == 0) { return g; }
  auto vd_1 = add_custom_vertex(*names.begin(), g);
  if (names. size() == 1) return g;
  const auto j = std :: end (names);
  auto i = std::begin(names);
  for (++i; i!=j; ++i) // Skip first
    auto vd 2 = add custom vertex(*i, g);
    const auto aer = boost::add edge(vd 1, vd 2, g);
    assert (aer.second);
    vd 1 = vd 2;
  }
  return g;
```

12.9.3 Creating such a graph

Algorithm 231 demonstrates how to create a path graph with named vertices and checks if it has the correct amount of edges and vertices:

Algorithm 231 Demonstration of 'create named vertices path graph'

12.9.4 The .dot file produced

This graph can be converted to the .dot file as shown in algorithm 232:

Algorithm 232 .dot file created from the 'create_named_vertices_path_graph' function (algorithm 230), converted from graph to .dot file using algorithm 52

12.9.5 The .svg file produced

The .dot file can be converted to the .svg as shown in figure 52:

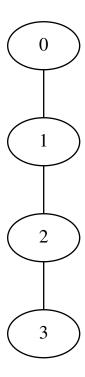


Figure 52: .svg file created from the 'create_named_vertices_path_graph' function (algorithm 230) its .dot file, converted from .dot file to .svg using algorithm 361

Working on graphs with custom vertices (as a custom property)

When using graphs with custom vertices, their state gives a way to find a vertex and working with it. This chapter shows some basic operations on graphs with custom vertices.

- Check if there exists a vertex with a certain 'my vertex': chapter 13.1
- Find a vertex with a certain 'my_vertex': chapter 13.2
- Get a vertex its 'my vertex' from its vertex descriptor: chapter 13.3
- Set a vertex its 'my vertex' using its vertex descriptor: chapter 13.4
- \bullet Setting all vertices their 'my_vertex'es: chapter 13.5
- \bullet Storing an directed/undirected graph with custom vertices as a .dot file: chapter 13.10

- Loading a directed graph with custom vertices from a .dot file: chapter 13.11
- \bullet Loading an undirected directed graph with custom vertices from a .dot file: chapter 13.12

13.1 Has a custom vertex with a my vertex

Before modifying our vertices, let's first determine if we can find a vertex by its custom type ('my_vertex') in a graph. After obtaing a my_vertex map, we obtain the vertex iterators, dereference these to obtain the vertex descriptors and then compare each vertex its my_vertex with the one desired.

Algorithm 233 Find if there is vertex with a certain my_vertex

```
#include < string>
#include <boost/graph/properties.hpp>
#include "install_vertex_custom_type.h"
#include "my custom vertex.h"
template <typename graph>
bool has_custom_vertex_with_my_custom_vertex(
  const my custom vertex& v,
  const graph& g
 noexcept
  using vd = typename graph::vertex descriptor;
  const auto vip = vertices(g);
  return std::find if (vip.first, vip.second,
    [v, g](const vd& d)
      const auto my custom vertexes map
        = get (boost::vertex custom type, g);
      return get (my custom vertexes map, d) == v;
  ) != vip.second;
```

This function can be demonstrated as in algorithm 234, where a certain my_vertex cannot be found in an empty graph. After adding the desired my_vertex, it is found.

Algorithm 234 Demonstration of the 'has_custom_vertex_with_my_vertex' function

```
#include < cassert >
#include <iostream>
#include "add custom vertex.h"
#include "create empty undirected custom vertices graph.h
#include "has custom vertex with my vertex.h"
#include "install vertex custom type.h"
#include "my custom vertex.h"
void has custom vertex with my custom vertex demo()
   noexcept
{
  {f auto}\ {f g}={f create\_empty\_undirected\_custom\_vertices\_graph}
  assert (! has custom vertex with my custom vertex (
     my custom vertex("Felix"),g));
  add_custom_vertex(my_custom_vertex("Felix"),g);
  assert (has custom vertex with my_custom_vertex (
     my custom vertex("Felix"),g));
}
```

Note that this function only finds if there is at least one custom vertex with that my_vertex: it does not tell how many custom vertices with that my_vertex exist in the graph.

13.2 Find a custom vertex with a certain my vertex

Where STL functions work with iterators, here we obtain a vertex descriptor (see chapter 2.6) to obtain a handle to the desired vertex. Algorithm 235 shows how to obtain a vertex descriptor to the first vertex found with a specific my_vertex value.

Algorithm 235 Find the first vertex with a certain my vertex

```
#include <cassert>
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "has custom vertex with my vertex.h"
#include "install vertex custom type.h"
#include "my_custom_vertex.h"
template <typename graph, typename custom_vertex>
typename boost::graph traits<graph>::vertex descriptor
find first custom vertex with my vertex (
  const custom vertex& v,
  const graph& g
  noexcept
{
  using vd = typename graph::vertex descriptor;
  const auto vip = vertices(g);
  const auto i = std::find if (
    vip.first, vip.second,
    [v,g] (const vd d) {
      const auto my_vertex_map = get(boost::
         vertex custom type, g);
      return get (my vertex map, d) == v;
  );
  assert(i != vip.second);
  return *i;
}
```

With the vertex descriptor obtained, one can read and modify the vertex and the edges surrounding it. Algorithm 236 shows some examples of how to do so.

Algorithm 236 Demonstration of the 'find_first_custom_vertex_with_my_vertex' function

13.3 Get a custom vertex its my vertex

To obtain the name from a vertex descriptor, one needs to pull out the $my_vertexes^{11}$ map and then look up the vertex of interest.

 $^{^{11}} Bad \ English \ intended: \ my_vertexes = multiple \ my_vertex \ objects, \ vertices = multiple \ graph \ nodes$

Algorithm 237 Get a my_custom_vertex its my_vertex from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "install vertex custom type.h"
#include "my custom vertex.h"
template <typename graph>
auto get my custom vertex (
  const typename boost::graph traits<graph>::
     vertex descriptor& vd,
  const graph& g
) noexcept -> decltype(get(get(boost::vertex custom type,
   g), vd))
{
  const auto my custom vertexes map
    = get (boost::vertex custom type,
      g
    );
  return get(my_custom_vertexes_map, vd);
}
```

This function creates a property map from the graph, using the 'boost::vertex_custom_type' tag. Then it uses the vertex descriptor to obtain the custom vertex associated with that vertex.

Note how this function deduces the date type of its return value using decltype.

To use 'get_custom_vertex_my_vertex', one first needs to obtain a vertex descriptor. Algorithm 238 shows a simple example.

Algorithm 238 Demonstration if the 'get my custom vertex' function

13.4 Set a custom vertex its my_vertex

If you know how to get the my_vertex from a vertex descriptor, setting it is just as easy, as shown in algorithm 239.

Algorithm 239 Set a custom vertex its my vertex from its vertex descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "install_vertex_custom_type.h"
#include "my custom vertex.h"
\textbf{template} \hspace{0.1cm} < \hspace{-0.1cm} \textbf{typename} \hspace{0.1cm} \operatorname{grap} h >
void set my custom vertex (
  const my_custom_vertex& v,
  const typename boost::graph traits<graph>::
      vertex descriptor& vd,
  graph& g
  noexcept
  static\_assert\;(!\,std::is\_const\!<\!graph\!>::value\;,
     "graph_cannot_be_const"
  );
  const auto my custom vertexes map
     = get(boost::vertex_custom_type, g);
  put(my_custom_vertexes_map, vd, v);
```

To use 'set_my_custom_vertex', one first needs to obtain a vertex descriptor. Algorithm 240 shows a simple example.

Algorithm 240 Demonstration if the 'set my custom vertex' function

```
#include <cassert>
#include "add custom vertex.h"
#include "create empty undirected custom vertices graph.h
#include "find_first_custom_vertex_with_my_vertex.h"
#include "get my custom vertex.h"
#include "set_my_custom_vertex.h"
void set my custom vertex demo() noexcept
  auto g
    = create_empty_undirected_custom_vertices_graph();
  const my custom vertex old vertex{"Dex"};
  add custom vertex (old vertex, g);
  const auto vd
    = find first custom vertex with my vertex(old vertex,
  assert (get_my_custom_vertex (vd,g)
    == old vertex
  );
  const my custom vertex new vertex{"Diggy"};
  set my custom vertex (
    new_vertex, vd, g
  assert (get my custom vertex (vd,g)
    == new vertex
  );
}
```

13.5 Setting all custom vertices' my vertex objects

When the vertices of a graph are associated with my_vertex objects, one can set these my_vertexes as such:

Algorithm 241 Setting the custom vertices' my vertexes

```
#include < string>
#include < vector >
#include <boost/graph/graph traits.hpp>
\# \mathbf{include} < \mathbf{boost} / \mathbf{graph} / \mathbf{properties} . \mathbf{hpp} >
#include "install vertex custom type.h"
#include "my_custom_vertex.h"
template <typename graph>
void set my custom vertexes (
  graph& g,
  const std::vector<my_custom_vertex>& my_custom_vertexes
  noexcept
{
  static assert (!std::is const<graph>::value, "graph_
      cannot_be_const");
  const auto my custom vertex map
    = get (boost::vertex custom type,g);
  auto my_custom_vertexes_begin = std::begin(
      my custom vertexes);
  const auto my_custom_vertexes_end = std::end(
     my_custom_vertexes);
  const auto vip = vertices(g);
  const auto j = vip.second;
    auto i = vip.first;
    i!=j; ++i,
    ++my custom vertexes begin
    assert (my custom vertexes begin !=
        my custom vertexes end);
    put (my_custom_vertex_map, *i,*
        my\_custom\_vertexes\_begin);
}
```

An impressive feature is that getting the property map holding the graph its names is not a copy, but a reference. Otherwise, modifying 'my_vertexes_map' (obtained by non-reference) would only modify a copy.

13.6 Adding an edge between two custom vertices

Instead of looking for an edge descriptor, one can also add an edge from two vertex descriptors. Adding an edge between two selected vertices goes as follows: use the my_custom_vertex of the vertices to get both vertex descriptors, then call 'boost::add_edge' on those two, as shown in algorithm 242.

Algorithm 242 Add an edge between two custom vertices

```
#include <cassert>
#include < string>
#include <boost/graph/adjacency list.hpp>
#include "has vertex with my vertex.h"
#include "find first custom vertex with my vertex.h"
#include "my custom vertex.h"
template <typename graph>
typename boost::graph traits<graph>::edge descriptor
add_edge_between_custom_vertices(
  const my custom vertex& vertex from,
  const my custom vertex& vertex to,
  graph& g
 noexcept
  assert (has vertex with my vertex (vertex from, g));
  assert (has vertex with my vertex (vertex to, g));
  const auto vd 1 =
     find_first_custom_vertex_with_my vertex(vertex from,
      g);
  \mathbf{const} auto \mathrm{vd} 2 =
     find first custom vertex with my vertex (vertex to, g
  const auto aer = boost::add edge(vd 1, vd 2, g);
  assert (aer.second);
  return aer.first;
```

Algorithm 243 shows how the edges can be added:

Algorithm 243 Demonstration of the 'add_edge_between_selected_vertices' function

13.7 Create a direct-neighbour subgraph from a vertex descriptor of a graph with custom vertices

Suppose you have a vertex of interest its vertex descriptor. Let's say you want to get a subgraph of that vertex and its direct neighbours only. This means that all vertices of that subgraph are adjacent vertices and that the edges go either from focal vertex to its neighbours, or from adjacent vertex to adjacent neighbour.

Here is the code that does exactly that:

```
\#include <map>
#include <boost/graph/adjacency list.hpp>
#include "add custom vertex.h"
#include "get_my_custom_vertex.h"
template <typename graph, typename vertex_descriptor>
graph create direct neighbour custom vertices subgraph (
  const vertex descriptor& vd,
  const graph& g
{
  graph h;
  std::map<vertex_descriptor, vertex_descriptor> m;
    const auto vd h = add custom vertex (
      get_my_custom_vertex(vd, g), h
    m. insert (std::make_pair(vd,vd_h));
  //Copy vertices
    const auto vdsi = boost::adjacent vertices (vd, g);
    std::transform(vdsi.first, vdsi.second,
      std::inserter(m, std::begin(m)),
      [g, &h](const vertex_descriptor&d)
        const auto vd h = add custom_vertex(
          get_my_custom_vertex(d,g), h
        return std::make_pair(d,vd_h);
    );
   /\mathit{Copy}\ edges
    const auto eip = edges(g);
    {f const\ auto\ j\ =\ eip.second\ ;}
    for (auto i = eip.first; i!=j; ++i)
      const auto vd_from = source(*i, g);
      const auto vd to = target(*i, g);
      if (m. find (vd_from) = std :: end (m)) continue;
      if (m. find (vd to) == std::end(m)) continue;
      const auto aer = boost::add edge(m[vd from],m[vd to
          ], h);
                             268
      assert (aer.second);
    }
  }
  return h;
```

This demonstration code shows that the direct-neighbour graph of each vertex of a K_2 graphs is ... a K_2 graph!

 ${\bf Algorithm~245~Demo~of~the~`create_direct_custom_vertices_neighbour_subgraph'} function$

```
#include "
   create direct neighbour custom vertices subgraph.h"
#include "create_custom_vertices_k2_graph.h"
#include "get my custom vertexes.h"
void
   create direct neighbour custom vertices subgraph demo
   () noexcept
  const auto g = create_custom_vertices_k2_graph();
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (auto i=vip.first; i!=j; ++i) {
    const auto h =
       create direct neighbour custom vertices subgraph (
      *i,g
    );
    assert(boost::num \ vertices(h) == 2);
    assert (boost::num edges(h) = 1);
    const auto v = get my custom vertexes(h);
    std::set<my custom vertex> vertexes(std::begin(v),std
        :: end(v));
    const my custom vertex a ("A", "source", 0.0, 0.0);
    const my custom vertex b("B", "target", 3.14, 3.14);
    assert (vertexes.count (a) = 1);
    assert (vertexes.count(b) == 1);
  }
}
```

13.8 Creating all direct-neighbour subgraphs from a graph with custom vertices

Using the previous function, it is easy to create all direct-neighbour subgraphs from a graph with custom vertices:

Algorithm 246 Create all direct-neighbour subgraphs from a graph with custom vertices

```
#include < vector >
#include "
   create_direct_neighbour_custom_vertices_subgraph.h"
template <typename graph>
std::vector<graph>
   create all direct neighbour custom vertices subgraphs (
  const graph g
) noexcept
  using vd = typename graph::vertex descriptor;
  std::vector<graph> v;
  v.resize(boost::num_vertices(g));
  const auto vip = vertices(g);
  std::transform(
    vip.first, vip.second,
    std::begin(v),
    [g](const vd& d)
      return
         create direct neighbour custom vertices subgraph
         (
        d, g
      );
    }
  );
  return v;
```

This demonstration code shows how to extract the subgraphs from a path graph:

```
Algorithm 247 Demo of the 'create_all_direct_neighbour_custom_vertices_subgraphs' function
```

The sub-graphs are shown here:

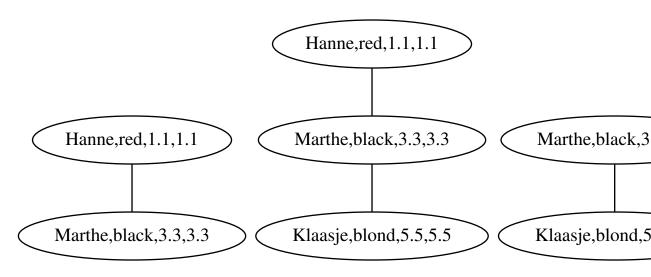


Figure 53: All subgraphs created

13.9 Are two graphs with custom vertices isomorphic?

Algorithm 5.14 checked if two graphs with named vertices are 'label isomorphic'. Here, we do the same for custom vertices.

To do this, there are two steps needed:

- 1. Map all my_custom_vertex objects to an unsigned int.
- 2. Compare the two graphs with that map

Below the class 'my_custom_vertex_invariant' is shown. Its std::map maps the vertex names to an unsigned integer, which is done in the member function 'collect_names'. The purpose of this, is that is is easier to compare integers than custom vertices. Note that operator< must be implemented for the custom class for this to compile.

Algorithm 248 The 'custom_vertex_invariant' functor

```
\#include <map>
#include <boost/graph/adjacency list.hpp>
#include <boost/graph/isomorphism.hpp>
#include "my custom vertex.h"
#include "install vertex custom type.h"
template <class graph>
struct custom_vertex_invariant {
  using custom vertex to int map = std::map<
     my custom vertex, size t >;
  \mathbf{using} \ \mathbf{result\_type} = \mathbf{size\_t} \, ;
  using argument type = typename graph::vertex descriptor
  const graph& m_graph;
  custom vertex to int map& m mappings;
  size t operator()(argument type u) const {
      return m mappings.at(boost::get(boost::
          vertex custom type, m graph, u));
  size t max() const noexcept { return m mappings.size();
  void collect_custom() noexcept {
    for (const auto vd : boost::make iterator range(boost
        :: vertices (m graph))) {
      const size t next id = m mappings.size();
      const auto ins = m mappings.insert (
        { boost::get(boost::vertex custom type, m graph,
            vd), next id}
      );
      if (ins.second) {
        //std::cout << "Mapped ''" << ins.first->first<<
            "', to " << ins. first -> second <math><< "\mid n";
    }
  }
};
```

To check for 'custom vertexness isomorphism', multiple things need to be put in place for 'boost::isomorphism' to work with:

Algorithm 249 Check if two graphs with custom vertices are isomorphic

```
#include "custom vertex invariant.h"
#include <boost/graph/vf2 sub graph iso.hpp>
#include <boost/graph/graph utility.hpp>
template <typename graph>
bool is custom vertices isomorphic (
  const graph &g,
  const graph &h
) noexcept {
  using vd = typename graph::vertex descriptor;
  auto vertex_index_map = get(boost::vertex_index, g);
  std::vector<vd> iso(boost::num vertices(g));
  typename custom vertex invariant < graph > ::
     custom vertex to int map shared custom;
  custom_vertex_invariant<graph> inv1{g, shared_custom};
  custom vertex invariant<graph> inv2 {h, shared custom };
  inv1.collect custom();
  inv2.collect custom();
  return boost::isomorphism(g, h,
    boost::isomorphism map(
      make_iterator_property_map(
        iso.begin(),
        vertex index map
    )
    .vertex_invariant1(inv1)
    .vertex_invariant2(inv2)
  );
```

This demonstration code creates three path graphs, of which two are 'label isomorphic':

Algorithm 250 Demo of the 'is_named_vertices_isomorphic' function

```
#include <cassert>
#include "create_custom_vertices_path_graph.h"
#include "is_custom_vertices_isomorphic.h"
void is custom vertices isomorphic demo() noexcept
  {\bf const\ auto\ g = create\_custom\_vertices\_path\_graph}\,(
    {
      my custom vertex ("Alpha"),
      my custom vertex ("Beta"),
      my custom vertex ("Gamma")
    }
  );
  const auto h = create custom vertices path graph (
      my custom vertex ("Gamma"),
      my\_custom\_vertex("Beta"),
      my custom vertex ("Alpha")
    }
  );
  const auto i = create custom vertices path graph (
      my_custom_vertex("Alpha"),
      my\_custom\_vertex("Gamma"),
      my_custom_vertex("Beta")
    }
  );
  assert( is_custom_vertices_isomorphic(g,h));
  assert (! is custom vertices isomorphic (g, i));
```

13.10 Storing a graph with custom vertices as a .dot

If you used the create_custom_vertices_k2_graph function (algorithm 227) to produce a K_2 graph with vertices associated with my_vertex objects, you can store these my_vertexes additionally with algorithm 251:

Algorithm 251 Storing a graph with custom vertices as a .dot file

```
#include <fstream>
#include < string>
\#include <boost / graph / graphviz . hpp>
#include <boost/graph/properties.hpp>
#include "get my custom vertexes.h"
template <typename graph>
void save_custom_vertices_graph_to_dot(
  const graph& g,
  const std::string& filename
  noexcept
  using vd = typename graph::vertex descriptor;
  std::ofstream f(filename);
  boost::write graphviz(
    f,
    [g](std::ostream& out, const vd& v) {
      const auto my custom vertexes map
        = get (boost::vertex custom type,g)
      const my_custom_vertex m{get(my_custom_vertexes_map
      out << "[label=\"" << m << "\"]";
  );
```

13.11 Loading a directed graph with custom vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with custom vertices is loaded, as shown in algorithm 252:

Algorithm 252 Loading a directed graph with custom vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create empty directed custom vertices graph.h"
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
load_directed_custom_vertices_graph_from_dot(
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g = create empty directed custom vertices graph();
  boost::dynamic properties dp(boost::
     ignore other properties);
  dp.property("label", get(boost::vertex custom type, g))
  boost::read_graphviz(f,g,dp);
  return g;
}
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Next to this, a boost::dynamic_properties is created with its default constructor, after which we direct the boost::dynamic_properties to find a 'node_id' and 'label' in the vertex name map, 'edge_id' and 'label' to the edge name map. From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

Algorithm 253 shows how to use the 'load _directed _custom _vertices _ graph _from _dot' function:

Algorithm 253 Demonstration of the 'load_directed_custom_vertices_graph_from_dot' function

```
#include "create custom vertices markov chain.h"
#include "load directed custom vertices graph from dot.h"
#include "save_custom_vertices_graph_to_dot.h"
#include "get my custom vertexes.h"
{\bf void}\ \ {\bf load\_directed\_custom\_vertices\_graph\_from\_dot\_demo}\,()
   noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create_custom_vertices_markov_chain();
  const std::string filename{
    "create custom vertices markov chain.dot"
  };
  save custom vertices graph to dot(g, filename);
  const auto h
    = load directed custom vertices graph from dot(
       filename);
  assert(num\_edges(g) == num\_edges(h));
  assert (num vertices (g) == num vertices (h));
  assert (get my custom vertexes (g)
    == get my custom vertexes(h)
  );
}
```

This demonstration shows how the Markov chain is created using the 'create_custom_vertices_markov_chain' function (algorithm 224), saved and then loaded. The loaded graph is then checked to be identical to the original.

13.12 Loading an undirected graph with custom vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with custom vertices is loaded, as shown in algorithm 254:

Algorithm 254 Loading an undirected graph with custom vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "create_empty_undirected_custom_vertices_graph.h
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
load undirected custom vertices graph from dot (
  const std::string& dot filename
  assert(is_regular_file(dot_filename));
  std::ifstream f(dot_filename.c_str());
  auto g = create empty undirected custom vertices graph
     ();
  boost::dynamic properties dp(boost::
     ignore_other_properties);
  dp.property("label", get(boost::vertex custom type, g))
  boost::read graphviz(f,g,dp);
  return g;
}
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 13.11 describes the rationale of this function

 $Algorithm\ 255\ shows\ how\ to\ use\ the\ 'load_undirected_custom_vertices_graph_from_dot' function:$

Algorithm 255 Demonstration of the 'load_undirected_custom_vertices_graph_from_dot' function

```
#include <cassert>
#include "create custom vertices k2 graph.h"
#include "load_undirected_custom_vertices_graph_from_dot.
   h "
#include "save custom vertices_graph_to_dot.h"
#include "get my custom vertexes.h"
void load_undirected_custom_vertices_graph_from_dot_demo
   () noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create custom vertices k2 graph();
  const std::string filename{
    "create custom vertices k2 graph.dot"
  save custom vertices graph to dot(g, filename);
  const auto h
    = load undirected custom vertices graph from dot(
       filename);
  assert(num edges(g) == num edges(h));
  assert (num vertices (g) == num vertices (h));
  assert (get_my_custom_vertexes(g) ==
     get my custom vertexes(h));
}
```

This demonstration shows how K_2 with custom vertices is created using the 'create_custom_vertices_k2_graph' function (algorithm 227), saved and then loaded. The loaded graph is then checked to be identical to the original.

14 Building graphs with custom and selectable vertices

We have added one custom vertex property, here we add a second: if the vertex is selected.

- An empty directed graph that allows for custom and selectable vertices: see chapter 14.2
- An empty undirected graph that allows for custom and selectable vertices:

see chapter 14.3

- A two-state Markov chain with custom and selectable vertices: see chapter 14.5
- K_3 with custom and selectable vertices: see chapter 14.6

In the process, some basic (sometimes bordering trivial) functions are shown:

- Installing the new edge property: see chapter 14.1
- Adding a custom and selectable vertex: see chapter 14.4

These functions are mostly there for completion and showing which data types are used.

14.1 Installing the new is selected property

Installing a new property would have been easier, if 'more C++ compilers were standards conformant' ([8], chapter 3.6, footnote at page 52). Boost.Graph uses the BOOST INSTALL PROPERTY macro to allow using a custom property:

Algorithm 256 Installing the vertex is selected property

```
#include <boost/graph/properties.hpp>
namespace boost {
  enum vertex_is_selected_t { vertex_is_selected = 31416
     };
  BOOST_INSTALL_PROPERTY(vertex, is_selected);
}
```

The enum value 31415 must be unique.

14.2 Create an empty directed graph with custom and selectable vertices

Algorithm 257 Creating an empty directed graph with custom and selectable vertices

```
#include <boost/graph/adjacency list.hpp>
#include "install_vertex_custom_type.h"
#include "install vertex is selected.h"
#include "my_custom_vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS,
  boost::property<
    boost::vertex custom type t, my custom vertex,
    boost::property<
      boost::vertex is selected t, bool
create empty directed custom and selectable vertices graph
   () noexcept
  return {};
}
```

This code is very similar to the code described in chapter 12.3, except that there is a new, fourth template argument:

```
boost::property<boost::vertex_custom_type_t, my_custom_vertex,
   boost::property<boost::vertex_is_selected_t, bool,
>
```

This can be read as: "vertices have two properties: an associated custom type (of type my_custom_vertex) and an associated is_selected property (of type bool)".

Demo:

```
Algorithm
                 258
                           Demonstration
                                                     the
                                                               'cre-
ate\_empty\_directed\_custom\_and\_selectable\_vertices\_graph' function
#include "
    create\_empty\_directed\_custom\_and\_selectable\_vertices\_graph
    . h"
void
    create\_empty\_directed\_custom\_and\_selectable\_vertices\_graph\_demo
    () noexcept
  const auto g
        create\_empty\_directed\_custom\_and\_selectable\_vertices\_graph
  assert(boost::num\_edges(g) == 0);
  assert(boost::num \ vertices(g) == 0);
```

14.3 Create an empty undirected graph with custom and selectable vertices

Algorithm 259 Creating an empty undirected graph with custom and selectable vertices

```
#include <boost/graph/adjacency_list.hpp>
#include "install_vertex_custom_type.h"
#include "install_vertex_is_selected.h"
#include "my_custom_vertex.h"

boost:: adjacency_list <
   boost:: vecS,
   boost:: vecS,
   boost:: vecS,
   boost:: property <
      boost:: vertex_custom_type_t, my_custom_vertex,
      boost:: property <
      boost:: vertex_is_selected_t, bool
   >
   >
   create_empty_undirected_custom_and_selectable_vertices_graph
      () noexcept
{
    return {};
}
```

This code is very similar to the code described in chapter 14.2, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS). Demo:

```
Algorithm
                 260
                          Demonstration
                                                    the
                                                              'cre-
ate\_empty\_undirected\_custom\_and\_selectable\_vertices\_graph' function
#include "
   create\_empty\_undirected\_custom\_and\_selectable\_vertices\_graph
    . h"
void
   create_empty_undirected_custom_and_selectable_vertices_graph_demo
    () noexcept
  const auto g
        create\_empty\_undirected\_custom\_and\_selectable\_vertices\_graph
  assert(boost::num\_edges(g) == 0);
  assert(boost::num \ vertices(g) == 0);
```

14.4 Add a custom and selectable vertex

Adding a custom and selectable vertex is very similar to adding a custom vertex (chapter 12.5).

Algorithm 261 Add a custom and selectable vertex

```
#include <type traits>
#include <boost/graph/adjacency_list.hpp>
#include "install vertex custom type.h"
#include "install vertex is selected.h"
template <typename graph, typename vertex t>
typename boost::graph traits<graph>::vertex descriptor
add_custom_and_selectable_vertex(
  const vertex t& v,
  const bool is selected,
  graph& g
) noexcept
  static_assert(!std::is_const<graph>::value,
    "graph_cannot_be_const"
  );
  const auto vd = boost::add vertex(g);
  const auto my custom vertex map
    = get (boost::vertex custom type,
      g
    );
  put (my custom vertex map, vd, v);
  const auto is selected map
    = get(boost::vertex is selected,
    );
  put (is selected map, vd, is selected);
  return vd;
```

When having added a new (abstract) vertex to the graph, the vertex descriptor is used to set the my_custom_vertex and the selectedness in the graph its my_custom_vertex and is_selected_map.

Here is the demo:

Algorithm 262 Demo of 'add custom and selectable vertex'

```
#include <cassert>
#include "add_custom_and_selectable_vertex.h"
#include "
   create empty directed custom and selectable vertices graph
   . h"
#include "
   create_empty_undirected_custom_and_selectable_vertices_graph
   . h"
void add custom and selectable vertex demo() noexcept
  auto g
       create empty directed custom and selectable vertices graph
       ();
  assert(boost::num \ vertices(g) == 0);
  assert(boost::num edges(g) == 0);
  add custom and selectable vertex (
    my_custom_vertex("X"),
    true,
    g
  );
  assert (boost::num vertices(g) == 1);
  assert(boost::num edges(g) == 0);
  auto h
       create empty undirected custom and selectable vertices graph
       ();
  assert(boost::num vertices(h) == 0);
  assert(boost::num edges(h) == 0);
  add custom and selectable vertex (
    my custom vertex ("X"),
    false,
    h
  );
  assert (boost::num vertices(h) == 1);
  assert(boost::num edges(h) == 0);
```

14.5 Creating a Markov-chain with custom and selectable vertices

14.5.1 Graph

Figure 54 shows the graph that will be reproduced:

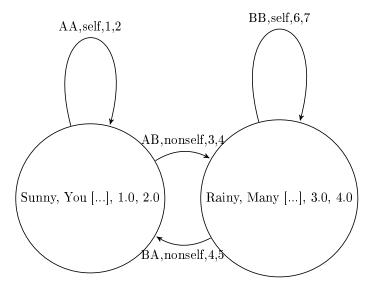


Figure 54: A two-state Markov chain where the edges and vertices have custom properies. The edges' and vertices' properties are nonsensical

14.5.2 Function to create such a graph

Here is the code creating a two-state Markov chain with custom edges and vertices:

Algorithm 263 Creating the two-state Markov chain as depicted in figure 54

```
#include <cassert>
#include "
   create empty directed custom and selectable vertices graph
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex custom type t, my custom vertex,
    boost::property<
      boost::vertex is selected t, bool
 >
create custom and selectable vertices markov chain()
   noexcept
  auto g
       create empty directed custom and selectable vertices graph
        ();
  const auto vd_a = boost :: add_vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer aa.second);
  const auto aer ab = boost :: add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer_bb = boost::add_edge(vd_b, vd_b, g);
  assert (aer bb.second);
  auto my custom vertex map = get (
    boost::vertex_custom_type,g
  put (my custom vertex map, vd a,
    my_custom_vertex("Sunny","Yellow_thing",1.0,2.0)
  );
  put (my custom vertex map, vd b,
    my_custom_vertex("Rainy", "Grey_things", 3.0, 4.0)
  auto is selected map = get (
    boost::vertex is selected, g
  put (is selected map, vd a, 28 Prue);
  put(is_selected_map, vd_b, false);
  return g;
}
```

14.5.3 Creating such a graph

Here is the demo:

Algorithm 264 Demo of the 'create_custom_and_selectable_vertices_markov_chain' function (algorithm 263)

```
#include < cassert >
#include "
    create_custom_and_selectable_vertices_markov_chain.h"
#include "get_vertex_selectednesses.h"
void
    create\_custom\_and\_selectable\_vertices\_markov\_chain\_demo
    () noexcept
  const auto g
    = create_custom_and_selectable_vertices_markov_chain
         ();
  \mathbf{const} \ \mathrm{std} :: \mathrm{vector} \! < \! \mathbf{bool} \! >
    expected selectednesses {
    true, false
  const std::vector<bool>
    vertex selectednesses {
     get_vertex_selectednesses(g)
  assert (expected selectednesses
    == vertex selectednesses
```

14.5.4 The .dot file produced

```
Algorithm
                265
                         .dot
                                 file
                                         created
                                                    from
                                                              the
                                                                      'cre-
ate\_custom\_and\_selectable\_vertices\_markov\_chain' \quad function \quad (algorithm
263), converted from graph to .dot file using algorithm 52
digraph G {
O[label="Sunny, Yellow$$$SPACE$$$thing,1,1", regular="1"];
1[label="Rainy,Grey$$$SPACE$$$things,3,3", regular="0"];
0->0 ;
0->1;
1->0;
1->1;
```

14.5.5 The .svg file produced

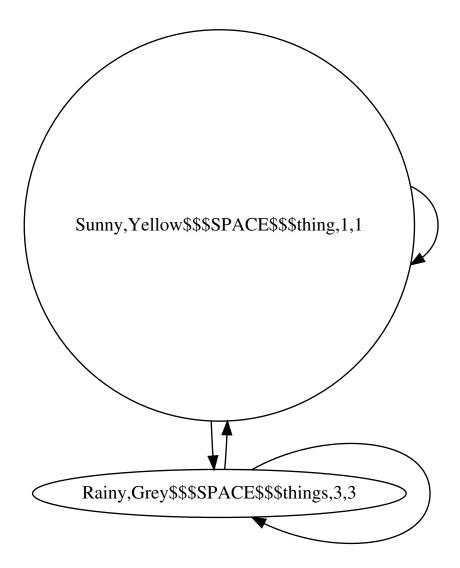


Figure 55: .svg file created from the 'create_custom_and_selectable_vertices_markov_chain' function (algorithm 224) its .dot file, converted from .dot file to .svg using algorithm 361

Note how the .svg changed it appearance due to the Graphviz 'regular' property (see chapter 25.2): the vertex labeled 'Sunny' is drawn according to the Graphviz 'regular' attribute, which makes it a circle. The other vertex, labeled 'Rainy' is not drawn as such and retained its ellipsoid appearance.

14.6 Creating K_2 with custom and selectable vertices

14.6.1 Graph

We reproduce the K_2 with custom vertices of chapter 12.8 , but now are vertices can be selected as well:

[graph here]

14.6.2 Function to create such a graph

Algorithm 266 Creating K_3 as depicted in figure 33

```
#include "
   create empty undirected custom and selectable vertices graph
   . h"
#include "add custom and selectable vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my custom vertex,
    boost::property<
      boost::vertex is selected t, bool
create custom and selectable vertices k2 graph() noexcept
  auto g
       create empty undirected custom and selectable vertices graph
  const my custom vertex a ("A", "source", 0.0, 0.0);
  const my_custom_vertex b("B","target",3.14,3.14);
  const auto vd a = add custom and selectable vertex (a,
     true, g);
  const auto vd_b = add_custom_and_selectable_vertex(b,
     false, g);
  const auto aer = boost::add_edge(vd_a, vd_b, g);
  assert (aer.second);
  return g;
}
```

Most of the code is a slight modification of algorithm 227. In the end, the associated my_custom_vertex and is_selected properties are obtained as boost::property_maps and set with the desired my_custom_vertex objects and selectednesses.

14.6.3 Creating such a graph

Here is the demo:

```
Algorithm 267 Demo of the 'create_custom_and_selectable_vertices_k2_graph' function (algorithm 266)
```

```
#include <cassert>
#include "create custom and selectable vertices k2 graph.
                 h"
#include "has_custom_vertex_with_my_vertex.h"
void create custom and selectable vertices k2 graph demo
                   () noexcept
 {
           const auto g =
                            create custom and selectable vertices k2 graph();
            assert(boost::num edges(g) == 1);
            assert(boost::num \ vertices(g) == 2);
            assert \ (has\_custom\_vertex\_with\_my\_custom\_vertex \ (has\_custom\_vertex) \ (has\_custom\_
                     my_custom_vertex("A", "source",0.0, 0.0), g)
           );
            assert (has custom vertex with my custom vertex (
                     my custom vertex ("B", "target", 3.14, 3.14), g)
           );
 }
```

14.6.4 The .dot file produced

```
Algorithm 268 .dot file created from the 'create_custom_and_selectable_vertices_k2_graph' function (algorithm 266), converted from graph to .dot file using algorithm 52

graph G {
O[label="A,source,0,0", regular="1"];
1[label="B,target,3.14,3.14", regular="0"];
0--1;
}
```

14.6.5 The .svg file produced

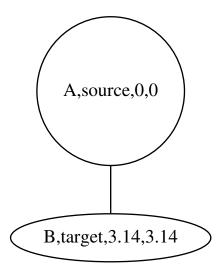


Figure 56: .svg file created from the 'create_custom_and_selectable_vertices_k2_graph' function (algorithm 224) its .dot file, converted from .dot file to .svg using algorithm 361

Note how the .svg changed it appearance due to the Graphviz 'regular' property (see chapter 25.2): the vertex labeled 'A' is drawn according to the Graphviz 'regular' attribute, which makes it a circle. The other vertex, labeled 'B' is not drawn as such and retained its ellipsoid appearance.

15 Working on graphs with custom and selectable vertices

This chapter shows some basic operations to do on graphs with custom and selectable vertices.

- Storing an directed/undirected graph with custom and selectable vertices as a .dot file: chapter 15.6
- \bullet Loading a directed graph with custom and selectable vertices from a .dot file: chapter 15.7
- \bullet Loading an undirected directed graph with custom and selectable vertices from a .dot file: chapter 15.8

15.1 • Getting the vertices with a certain selectedness

15.2 Counting the vertices with a certain selectedness

How often is a vertex with a certain selectedness present? Here we'll find out.

Algorithm 269 Count the vertices with a certain selectedness

```
#include < string>
#include <boost/graph/properties.hpp>
#include "install vertex is selected.h"
template <typename graph>
int count_vertices_with_selectedness(
  const bool selectedness,
  const graph& g
 noexcept
  using vd = typename graph::vertex descriptor;
  const auto vip = vertices(g);
  const auto cnt = std::count if(
    vip.first, vip.second,
    [g, selectedness](const vd& d)
      const auto is_selected_map
        = get(boost::vertex_is_selected, g);
      return selectedness
        == get (is selected map, d);
  );
  return static cast<int>(cnt);
}
```

Here we use the STL std::count_if algorithm to count how many vertices have the desired selectedness.

Algorithm 270 shows some examples of how to do so.

Algorithm 270 Demonstration of the 'count_vertices_with_selectedness' function

```
#include <cassert>
#include "add custom and selectable vertex.h"
#include "
   create_empty_undirected_custom_and_selectable_vertices_graph
   . h"
void count vertices with selectedness demo() noexcept
  auto g =
     create empty undirected custom and selectable vertices graph
  add custom and selectable vertex (
    my custom vertex("A"), true, g
  add custom and selectable vertex (
    my custom vertex("B"), false, g
  add custom and selectable vertex (
    my custom vertex("C"), true, g
  assert (count vertices with selectedness (true, g) == 2)
  assert (count vertices with selectedness (false, g) == 1)
}
```

15.3 Adding an edge between two selected vertices

Instead of looking for an edge descriptor, one can also add an edge from two vertex descriptors. Adding an edge between two selected vertices goes as follows: use the selectedness of the vertices to get both vertex descriptors, then call 'boost::add edge' on those two, as shown in algorithm 271.

Algorithm 271 Add an edge between two selected vertices

```
#include <cassert>
#include < string>
#include <boost/graph/adjacency_list.hpp>
#include "has vertex with name.h"
#include "find_first_vertex_with_name.h"
#include "get_vertices_with_selectedness.h"
#include "count_vertices_with_selectedness.h"
template <typename graph>
typename boost::graph traits<graph>::edge descriptor
add edge between selected vertices (graph& g) noexcept
  assert (count_vertices_with_selectedness (true, g) == 2);
  const auto vds = get_vertices_with_selectedness(true, g
      );
  assert(vds.size() == 2);
  const auto aer = boost::add edge(vds[0], vds[1], g);
  assert (aer.second);
  return aer.first;
}
```

Algorithm 272 shows how the edges can be added:

Algorithm 272 Demonstration of the 'add_edge_between_selected_vertices' function

```
#include <cassert>
#include "add edge between selected vertices.h"
#include "add custom and selectable vertex.h"
#include "
   create empty undirected custom and selectable vertices graph
   . h"
void add edge between selected vertices demo() noexcept
  auto g =
     create empty undirected custom and selectable vertices graph
     ();
  add custom and selectable vertex (my custom vertex ("Bert
     "), true, g);
  add custom and selectable vertex (my custom vertex ("
     Ernie"), true, g);
  add_edge_between selected vertices(g);
  assert(boost::num edges(g) == 1);
}
```

15.4 Create a direct-neighbour subgraph from a vertex descriptor of a graph with custom and selectable vertices

Suppose you have a vertex of interest its vertex descriptor. Let's say you want to get a subgraph of that vertex and its direct neighbours only. This means that all vertices of that subgraph are adjacent vertices and that the edges go either from focal vertex to its neighbours, or from adjacent vertex to adjacent neighbour.

Here is the code that does exactly that:

 ${\bf Algorithm~273~Get~the~direct-neighbour~custom~and~selectable~vertices~subgraph~from~a~vertex~descriptor}$

```
\#include <map>
#include <boost/graph/adjacency list.hpp>
#include "add custom and selectable vertex.h"
#include "get_my_custom_vertex.h"
template <typename graph, typename vertex_descriptor>
graph
   create_direct_neighbour_custom_and_selectable_vertices_subgraph
  const vertex descriptor& vd,
  const graph& g
{
  graph h;
  std::map<vertex descriptor, vertex descriptor> m;
    const auto vd h = add custom and selectable vertex (
      get_my_custom_vertex(vd, g), false, h
    m.insert(std::make pair(vd,vd h));
  //Copy vertices
    const auto vdsi = boost::adjacent vertices(vd, g);
    std::transform(vdsi.first, vdsi.second,
      std::inserter(m, std::begin(m)),
      [g, &h](const vertex_descriptor& d)
        \mathbf{const} auto \mathbf{vd} \mathbf{h} =
            add_custom_and_selectable_vertex(
          get_my_custom_vertex(d,g), false, h
        );
        return std::make pair(d,vd h);
    );
  //\mathit{Copy} e\,dg\,es
    const auto eip = edges(g);
    const auto j = eip.second;
    for (auto i = eip.first; i!=j; ++i)
      const auto vd from = source(*i, g);
      const auto vd to = target(*i, g);
      if (m. find (vd from) = std :: end (m)) continue;
      if (m. find (vd to) = 300 : end (m)) continue;
      const auto aer = boost::add_edge(m[vd_from],m[vd_to
          ], h);
      assert (aer.second);
    }
  return h;
```

Demo:

Algorithm 274 Demo of the 'create_direct_custom_and_selectable_vertices_neighbour_subgraph' function

```
#include "
   create direct neighbour custom and selectable vertices subgraph
#include "create custom and selectable vertices k2 graph.
#include "get my custom vertexes.h"
void
   create direct neighbour custom and selectable vertices subgraph demo
   () noexcept
  const auto g =
     create_custom_and_selectable_vertices_k2_graph();
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (auto i=vip.first; i!=j; ++i) {
    const auto h =
       create direct neighbour custom and selectable vertices subgraph
      *\,\mathrm{i}, g
    );
    assert(boost::num \ vertices(h) == 2);
    assert(boost::num edges(h) == 1);
    const auto v = get_my_custom_vertexes(h);
    std::set<my custom vertex> vertexes(std::begin(v),std
        :: end(v));
    const my custom vertex a("A", "source", 0.0, 0.0);
    const my custom vertex b("B","target",3.14,3.14);
    assert (vertexes.count(a) = 1);
    assert(vertexes.count(b) == 1);
  }
}
```

15.5 Creating all direct-neighbour subgraphs from a graph with custom and selectable vertices

Using the previous function, it is easy to create all direct-neighbour subgraphs from a graph with custom vertices:

Algorithm 275 Create all direct-neighbour subgraphs from a graph with custom vertices

```
#include < vector >
#include "
   create_direct_neighbour_custom_and_selectable_vertices_subgraph
template <typename graph>
std::vector<graph>
   create_all_direct_neighbour_custom_and_selectable_vertices_subgraphs
  const graph g
) noexcept
  using vd = typename graph::vertex descriptor;
  std::vector<graph> v;
  v.resize(boost::num vertices(g));
  const auto vip = vertices(g);
  std::transform(
    vip.first, vip.second,
    std :: begin(v),
    [g](const vd& d)
      return
         create_direct_neighbour_custom_and_selectable_vertices_subgraph
         (
        d, g
      );
    }
  );
  return v;
```

This demonstration code shows how to extract the subgraphs from a path graph:

```
Algorithm 276 Demo of the 'create_all_direct_neighbour_custom_vertices_subgraphs' function
```

```
#include < cassert >
#include "
   create_all_direct_neighbour_custom_and_selectable_vertices_subgraphs
#include "create custom and selectable vertices k2 graph.
   h "
void
   create all direct neighbour custom and selectable vertices subgraphs demo
   () noexcept
{
  const auto v
       create\_all\_direct\_neighbour\_custom\_and\_selectable\_vertices\_subgraphs
        create custom and selectable vertices k2 graph()
  assert(v.size() == 2);
  for (const auto g: v)
    assert(boost::num\_vertices(g) == 2);
    assert(boost::num edges(g) == 1);
}
```

The sub-graphs created from a path graph are shown here:

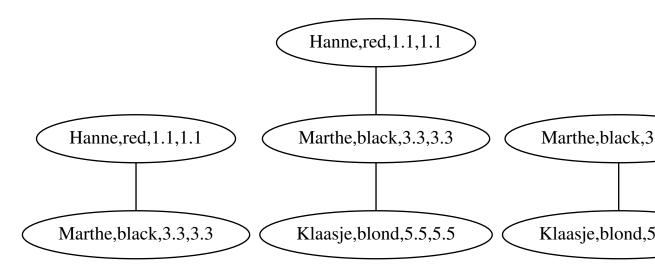


Figure 57: All subgraphs created

15.6 Storing a graph with custom and selectable vertices as a .dot

If you used the 'create_custom_and_selectable_vertices_k2_graph' function (algorithm 266) to produce a K_2 graph with vertices associated with (1) my_custom_vertex objects, and (2) a boolean indicating its selectedness, you can store such graphs with algorithm 277:

Algorithm 277 Storing a graph with custom and selectable vertices as a .dot file

```
#include <fstream>
#include < string>
#include <boost/graph/graphviz.hpp>
#include "install_vertex_custom_type.h"
#include "install vertex is selected.h"
#include "make_custom_and_selectable_vertices_writer.h"
#include "my custom vertex.h"
template <typename graph>
void save custom and selectable vertices graph to dot(
  const graph& g,
  const std::string& filename
  std::ofstream f(filename);
  boost::write graphviz(f, g,
    make custom and selectable vertices writer (
      get(boost::vertex_custom_type,g),
      get (boost::vertex is selected, g)
  );
}
```

This code looks small, because we call the 'make_custom_and_selectable_vertices_writer' function, which is shown in algorithm 278:

Algorithm 278 The 'make_custom_and_selectable_vertices_writer' function

```
template <
  typename my_custom_vertex_map,
  typename is_selected_map
inline custom and selectable vertices writer<
  my_custom_vertex_map,
  is selected map
make_custom_and_selectable_vertices_writer(
  \mathbf{const} \ \mathrm{my\_custom\_vertex\_map} \& \ \mathrm{any\_my\_custom\_vertex\_map} \ ,
  const is selected map& any is selected map
{
  return custom and selectable vertices writer<</pre>
    my\_custom\_vertex\_map,
    is selected map
    any_my_custom_vertex_map,
    any_is_selected_map
  );
}
```

Also this function is forwarding the real work to the 'custom_ and _ selectable _ vertices _ writer', shown in algorithm 279:

Algorithm 279 The 'custom and selectable vertices writer' function

```
#include <ostream>
#include <boost/lexical cast.hpp>
#include "is_graphviz_friendly.h"
template <
  typename my custom vertex map,
  typename is selected map
class custom and selectable vertices writer {
public:
  custom and selectable vertices writer (
    my custom vertex map any my custom vertex map,
    is selected map any is selected map
  ) : m_my_custom_vertex_map{any_my_custom_vertex_map},
      m is selected map { any is selected map }
  template <class vertex descriptor>
  void operator()(
    std::ostream& out,
    const vertex descriptor& vd
  ) const noexcept {
    out << "[label=\""
      << get(m_my_custom_vertex_map, vd) //Can be</pre>
          Graphviz unfriendly
      << " \ " , \ \ \ regular = \ \  " "
      << get(m is selected map, vd)</pre>
      << " \ " ] "
  }
private:
  my custom vertex map m my custom vertex map;
  is selected map m is selected map;
};
```

Here, some interesting things are happening: the writer needs both property maps to work with (that is, the 'my_custom_vertex' and is_selected maps). The 'my_custom_vertex' are written to the Graphviz 'label' attribute, and the is_selected is written to the 'regular' attribute (see chapter 25.2 for most Graphviz attributes).

Special about this, is that even for Graphviz-unfriendly input, it still works.

15.7 Loading a directed graph with custom and selectable vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with custom and selectable vertices is loaded, as shown in algorithm 280:

Algorithm 280 Loading a directed graph with custom vertices from a .dot file

```
#include <fstream>
\# \mathbf{include} < \mathbf{boost} / \operatorname{graph} / \operatorname{graphviz} . hpp>
#include "
   create empty directed custom and selectable vertices graph
    . h"
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex_custom_type_t, my_custom_vertex,
    boost::property<
      boost::vertex is selected t, bool
  >
load_directed_custom_and_selectable_vertices_graph_from_dot
  const std::string& dot filename
  assert(is_regular_file(dot_filename));
  std::ifstream f(dot_filename.c_str());
  auto g =
      create empty directed custom and selectable vertices graph
  boost::dynamic_properties dp(
    boost::ignore other properties
  dp.property("label", get(boost::vertex_custom_type, g))
  dp.property("regular", get(boost::vertex_is_selected, g
  boost::read_graphviz(f,g,dp);
  return g;
}
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Then, a boost::dynamic_properties is created with its default constructor, after which

• The Graphviz attribute 'node id' (see chapter 25.2 for most Graphviz

attributes) is connected to a vertex its 'my custom vertex' property

- The Graphviz attribute 'label' is connected to a vertex its 'my_custom_vertex' property
- The Graphviz attribute 'regular' is connected to a vertex its 'is_selected' vertex property

Algorithm 281 shows how to use the 'load_directed_custom_vertices_graph_from_dot' function:

```
Algorithm 281 Demonstration of the 'load_directed_custom_and_selectable_vertices_graph_from_dot' function
```

```
#include < cassert >
#include "
   create custom and selectable vertices markov chain.h"
#include "is regular_file.h"
#include "
   save custom and selectable vertices graph to dot.h"
void
   load directed custom and selectable vertices graph from dot demo
   () noexcept
  const auto g
    = create custom and selectable vertices markov chain
  const std::string filename{
    "create custom and selectable vertices markov chain.
       dot"
  };
  save_custom_and_selectable_vertices_graph to dot(
    filename
  );
  assert(is_regular_file(filename));
```

This demonstration shows how the Markov chain is created using the 'create_custom_vertices_markov_chain' function (algorithm 224), saved and then checked to exist.

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with custom and selectable vertices is loaded, as shown in algorithm 282:

 ${\bf Algorithm~282~Loading~an~undirected~graph~with~custom~vertices~from~a~.dot~file}$

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create_empty_undirected_custom_and_selectable_vertices_graph
   . h"
#include "install vertex custom type.h"
#include "is regular file.h"
#include "my_custom_vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex_custom_type_t, my_custom_vertex,
    boost::property<
      boost::vertex is selected t, bool
load_undirected_custom_and_selectable_vertices_graph from dot
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot_filename.c_str());
  auto g =
     create empty undirected custom and selectable vertices graph
  boost::dynamic_properties dp(boost::
     ignore_other_properties);
  dp.property("label", get(boost::vertex custom type, g))
  dp.property("regular", get(boost::vertex_is_selected, g
  boost::read_graphviz(f,g,dp);
  return g;
}
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 15.7 describes the rationale of this func-

tion.

 $Algorithm\ 283\ shows\ how\ to\ use\ the\ 'load_undirected_custom_vertices_graph_from_dot' function:$

Algorithm 283 Demonstration of the 'load_undirected_custom_and_selectable_vertices_graph_from_dot function

```
#include <cassert>
#include "create custom and selectable vertices k2 graph.
#include "is regular file.h"
#include "
   save custom and selectable vertices graph to dot.h"
void
   load undirected custom and selectable vertices graph from dot demo
   () noexcept
{
  const auto g
    = create custom and selectable vertices k2 graph();
  const std::string filename{
    "create custom and selectable vertices k2 graph.dot"
  save\_custom\_and\_selectable\_vertices\_graph\_to\_dot(
    filename
  );
  assert (is regular file (filename));
```

This demonstration shows how K_2 with custom vertices is created using the 'create_custom_vertices_k2_graph' function (algorithm 227), saved and then checked to exist.

16 Building graphs with custom edges and vertices

Up until now, the graphs created have had edges and vertices with the built-in name propery. In this chapter, graphs will be created, in which the edges and vertices can have a custom 'my custom edge' and 'my custom edge' type¹².

 An empty directed graph that allows for custom edges and vertices: see chapter 16.3

 $^{^{12}\}mathrm{I}$ do not intend to be original in naming my data types

- ullet An empty undirected graph that allows for custom edges and vertices: see chapter 16.4
- \bullet A two-state Markov chain with custom edges and vertices: see chapter 16.7
- K_3 with custom edges and vertices: see chapter 16.8

In the process, some basic (sometimes bordering trivial) functions are shown:

- Creating the custom edge class: see chapter 16.1
- Installing the new edge property: see chapter 16.2
- Adding a custom edge: see chapter 16.5

These functions are mostly there for completion and showing which data types are used.

16.1 Creating the custom edge class

In this example, I create a custom edge class. Here I will show the header file of it, as the implementation of it is not important yet.

Algorithm 284 Declaration of my_custom_edge

```
#include < string>
#include <iosfwd>
class my custom edge
public:
  explicit my custom edge(
    const std::string& name = "",
    const std::string& description = "",
    {f const\ double\ width\ =\ 1.0},
    const double height = 1.0
  ) noexcept;
  const std::string& get_description() const noexcept;
  const std::string& get name() const noexcept;
  double get_width() const noexcept;
  double get height() const noexcept;
  private:
  std::string m name;
  std::string m description;
  double m width;
  double m height;
};
bool operator == (const my custom edge& lhs, const
   my custom edge& rhs) noexcept;
bool operator!=(const my custom edge& lhs, const
   my custom edge& rhs) noexcept;
bool operator < (const my_custom_edge& lhs, const
   my custom edge& rhs) noexcept;
std::ostream& operator << (std::ostream& os, const
   my custom edge& v) noexcept;
std::istream& operator>>(std::istream& os, my custom edge
   & v) noexcept;
```

my_custom_edge is a class that has multiple properties: two doubles 'm_width' ('m_' stands for member) and 'm_height', and two std::strings m_name and m_description. 'my_custom_edge' is copyable, but cannot trivially be converted to a 'std::string.' 'my_custom_edge' is comparable for equality (that is, operator== is defined).

Special characters like comma's, quotes and whitespace cannot be streamed without problems. The function 'graphviz_encode' (algorithm 357) can convert the elements to be streamed to a Graphviz-friendly version, which can be decoded by 'graphviz_decode' (algorithm 358).

16.2 Installing the new edge property

Installing a new property would have been easier, if 'more C++ compilers were standards conformant' ([8], chapter 3.6, footnote at page 52). Boost.Graph uses the BOOST_INSTALL_PROPERTY macro to allow using a custom property:

Algorithm 285 Installing the edge custom type property

```
#include <boost/graph/properties.hpp>
namespace boost {
  enum edge_custom_type_t { edge_custom_type = 3142 };
  BOOST_INSTALL_PROPERTY(edge, custom_type);
}
```

The enum value 3142 must be unique.

16.3 Create an empty directed graph with custom edges and vertices

Algorithm 286 Creating an empty directed graph with custom edges and vertices

```
#include <boost/graph/adjacency list.hpp>
#include "install_edge_custom_type.h"
#include "install vertex custom type.h"
#include "my_custom_edge.h"
#include "my custom vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS,
  boost::property<
    boost:: vertex\_custom\_type\_t \;, \; my\_custom\_vertex
  boost::property<
    boost::edge_custom_type_t,my_custom_edge
create empty directed custom edges and vertices graph()
   noexcept
  return {};
```

This code is very similar to the code described in chapter 12.3, except that there is a new, fifth template argument:

```
boost::property<br/>boost::edge custom type t, my edge>
```

This can be read as: "edges have the property 'boost::edge_custom_type_t', which is of data type 'my_custom_edge". Or simply: "edges have a custom type called my_custom_edge".

Demo:

```
Algorithm
                 287
                           Demonstration
                                                     the
                                                               'cre-
ate\_empty\_directed\_custom\_edges\_and\_vertices\_graph' function
#include "
    create\_empty\_directed\_custom\_edges\_and\_vertices\_graph\,.
   h"
void
    create\_empty\_directed\_custom\_edges\_and\_vertices\_graph\_demo
    () noexcept
  const auto g =
      create\_empty\_directed\_custom\_edges\_and\_vertices\_graph
  assert(boost::num\_edges(g) == 0);
  assert(boost::num\_vertices(g) == 0);
}
```

16.4 Create an empty undirected graph with custom edges and vertices

Algorithm 288 Creating an empty undirected graph with custom edges and vertices

```
#include <boost/graph/adjacency list.hpp>
#include "install_edge_custom_type.h"
#include "install vertex custom type.h"
#include "my_custom_vertex.h"
#include "my custom edge.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
  boost::property<
    boost::edge_custom_type_t, my_custom_edge
create empty undirected custom edges and vertices graph()
    noexcept
  return {};
```

This code is very similar to the code described in chapter 16.3, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS). Demo:

```
Algorithm
                289
                          Demonstration
                                                    the
                                                             'cre-
ate\_empty\_undirected\_custom\_edges\_and\_vertices\_graph' function
#include <cassert>
#include "
   create_empty_undirected_custom_edges_and_vertices_graph
void
   create\_empty\_undirected\_custom\_edges\_and\_vertices\_graph\_demo
    () noexcept
  const auto g
        create\_empty\_undirected\_custom\_edges\_and\_vertices\_graph
  assert(boost::num edges(g) == 0);
  assert (boost::num vertices(g) == 0);
```

16.5 Add a custom edge

Adding a custom edge is very similar to adding a named edge (chapter 6.3).

Algorithm 290 Add a custom edge

```
#include <cassert>
#include <boost/graph/adjacency_list.hpp>
#include "install edge custom type.h"
#include "my custom edge.h"
template <typename graph>
typename boost::graph traits<graph>::edge descriptor
add custom edge (
  const my custom edge& v,
  graph& g
) noexcept
{
  static_assert(!std::is_const<graph>::value, "graph_
     cannot_be_const");
  const auto vd a = boost::add vertex(g);
  const auto vd_b = boost::add_vertex(g);
  const auto aer
    = boost::add edge(vd a, vd b, g);
  assert (aer.second);
  const auto my edge map
    = get(boost::edge custom type, g);
  put(my_edge_map, aer.first, v);
  return aer.first;
}
```

When having added a new (abstract) edge to the graph, the edge descriptor is used to set the my_edge in the graph its my_custom_edge map (using 'get(boost::edge_custom_type,g)').

Here is the demo:

Algorithm 291 Demo of 'add_custom_edge'

```
#include < cassert >
#include "add custom edge.h"
#include "
   create empty directed custom edges and vertices graph.
   h "
#include "
   create_empty_undirected_custom_edges_and_vertices_graph
   . h"
void add custom edge demo() noexcept
  auto g =
     create\_empty\_directed\_custom\_edges\_and\_vertices\_graph
  add custom edge(my custom edge("X"), g);
  assert(boost::num\_vertices(g) == 2);
  assert(boost::num edges(g) == 1);
  auto h =
     create_empty_undirected_custom_edges_and_vertices_graph
  add custom edge(my custom edge("Y"), h);
  assert (boost::num vertices(h) == 2);
  assert(boost::num edges(h) == 1);
```

16.6 Getting the custom edges my edges

When the edges of a graph have an associated 'my_custom_edge', one can extract these all as such:

Algorithm 292 Get the edges' my custom edges

```
#include < vector>
#include <boost/graph/adjacency_list.hpp>
#include "install edge custom type.h"
#include "my custom edge.h"
#include "get my custom edge.h"
template <typename graph>
std::vector<my_custom_edge> get_my_custom_edges(
  const graph& g
 noexcept
  using ed = typename boost::graph traits<graph>::
      edge descriptor;
  std::vector<my custom edge> v(boost::num edges(g));
  const auto eip = edges(g);
  std::transform(eip.first, eip.second, std::begin(v),
    [g](\mathbf{const} \ \mathrm{ed} \ \mathrm{d}) {
      return get my custom edge(d, g);
  );
  return v;
}
```

The 'my_custom_edge' object associated with the edges are obtained from a boost::property map and then put into a std::vector.

Note: the order of the my_custom_edge objects may be different after saving and loading.

When trying to get the edges' my_custom_edge objects from a graph without custom edges objects associated, you will get the error 'formed reference to void' (see chapter 24.1).

16.7 Creating a Markov-chain with custom edges and vertices

16.7.1 Graph

Figure 58 shows the graph that will be reproduced:

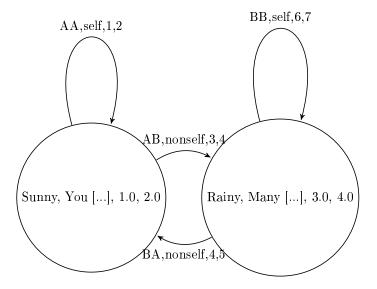


Figure 58: A two-state Markov chain where the edges and vertices have custom properies. The edges' and vertices' properties are nonsensical

16.7.2 Function to create such a graph

Here is the code creating a two-state Markov chain with custom edges and vertices:

```
#include <cassert>
#include "
   create empty directed custom edges and vertices graph.
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex custom type t, my custom vertex
  boost::property<
    boost::edge_custom_type_t, my_custom_edge
create_custom_edges_and_vertices_markov_chain() noexcept
{
  auto g
        create empty directed custom edges and vertices graph
        ();
  const auto vd a = boost :: add vertex(g);
  const \ auto \ vd \ b = boost :: add_vertex(g);
  {f const\ auto}\ {f aer\_aa}\ =\ {f boost}:: {f add\_edge}\left({f vd\_a},\ {f vd\_a},\ {f g}\right);
  assert (aer aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer ba.second);
  const auto aer_bb = boost::add_edge(vd_b, vd_b, g);
  assert (aer bb.second);
  auto my custom vertexes map = get (
    boost::vertex custom type, g
  );
  put (my custom vertexes map, vd a,
    my custom vertex ("Sunny", "Yellow_thing", 1.0, 2.0)
  put (my_custom_vertexes_map, vd_b,
    my_custom_vertex("Rainy","Grey_things",3.0,4.0)
  auto my edges map = get(
    boost::edge custom type,g
  put (my_edges_map, aer_aa. $25st,
    my_custom_edge("Sometimes","20%",1.0,2.0)
  put (my edges map, aer ab. first
    my_custom_edge("Often","80%",3.0,4.0)
  put (my_edges_map, aer_ba.first,
    my\_custom\_edge("Rarely","10\%",5.0,6.0)
```

16.7.3 Creating such a graph

Here is the demo:

```
Algorithm 294 Demo of the 'create_custom_edges_and_vertices_markov_chain' function (algorithm 293)

#include <cassert >
#include "create_custom_edges_and_vertices_markov_chain.h"

#include "get_my_custom_vertexes.h"
```

```
#include "get_my_custom_vertexes.h"
#include "install_vertex_custom_type.h"
#include "my custom vertex.h"
{\bf void} \;\; {\bf create\_custom\_edges\_and\_vertices\_markov\_chain\_demo} \; ()
     noexcept
  const auto g
    = create_custom_edges_and_vertices_markov_chain();
  const std::vector<my_custom_vertex>
    expected my custom vertexes {
    my_custom_vertex("Sunny",
      "Yellow_thing", 1.0, 2.0
    my custom vertex ("Rainy",
      "Grey_things", 3.0, 4.0
  };
  const std::vector<my custom vertex>
    vertex my custom vertexes{
    get_my_custom_vertexes(g)
  };
  assert (expected_my_custom_vertexes
    == vertex_my_custom_vertexes
  );
}
```

16.7.4 The .dot file produced

```
Algorithm
                295
                                file
                        .dot
                                                  from
                                                           the
                                                                   'cre-
                                       created
ate_custom_edges_and_vertices_markov_chain' function (algorithm 293),
converted from graph to .dot file using algorithm 52
digraph G {
O[label="Sunny, Yellow$$$SPACE$$$thing, 1, 1"];
1[label="Rainy,Grey$$$SPACE$$$things,3,3"];
0->0 [label="Sometimes,20%,1,2"];
0->1 [label="Often,80%,3,4"];
1->0 [label="Rarely,10%,5,6"];
1->1 [label="Mostly,90%,7,8"];
```

16.7.5 The .svg file produced

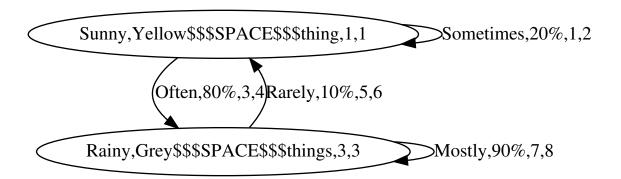


Figure 59: .svg file created from the 'create_custom_edges_and_vertices_markov_chain' function (algorithm 224) its .dot file, converted from .dot file to .svg using algorithm 361

16.8 Creating K_3 with custom edges and vertices

Instead of using edges with a name, or other properties, here we use a custom edge class called 'my_custom_edge'.

16.8.1 Graph

We reproduce the K_3 with named edges and vertices of chapter 6.8, but with our custom edges and vertices intead:

[graph here]

Algorithm 296 Creating K_3 as depicted in figure 33

```
#include "
   create empty undirected custom edges and vertices graph
    . h"
#include "add custom vertex.h"
#include "add custom edge between vertices.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom_type_t, my_custom_vertex
  boost::property<
    boost::edge custom type t, my custom edge
create custom edges and vertices k3 graph() noexcept
{
  auto g
        create empty undirected custom edges and vertices graph
        ();
  {f const} my custom vertex va("top", "source", 0.0, 0.0);
  \mathbf{const} \ \mathrm{my\_custom\_vertex} \ \mathrm{vb} \left( \text{"right","target"}, 3.14, 0 \right);
  const my custom vertex vc("left","target",0,3.14);
  const my custom edge ea("AB", "first", 0.0, 0.0);
  const my custom edge eb("BC", "second", 3.14, 3.14);
  const my custom edge ec ("CA", "third", 3.14, 3.14);
  const auto vd a = add custom vertex(va, g);
  const auto vd b = add custom vertex(vb, g);
  const auto vd c = add custom vertex(vc, g);
  add_custom_edge_between_vertices(ea, vd_a, vd_b, g);
  add custom edge between vertices (eb, vd b, vd c, g);
  add custom edge between vertices (ec, vd c, vd a, g);
  return g;
}
```

Most of the code is a slight modification of algorithm 132. In the end, the my edges and my vertices are obtained as a boost::property map and set

with the 'my custom edge' and 'my custom vertex' objects.

16.8.3 Creating such a graph

Here is the demo:

Algorithm 297 Demo of the 'create_custom_edges_and_vertices_k3_graph' function (algorithm 296)

16.8.4 The .dot file produced

2--0 [label="CA,third,3.14,3.14"];

}

```
Algorithm
                298
                        .dot
                                file
                                                            the
                                        created
                                                   from
                                                                    'cre-
ate custom edges and vertices markov chain' function (algorithm 296),
converted from graph to .dot file using algorithm 52
graph G {
0[label="top,source,0,0"];
1[label="right, target, 3.14, 3.14"];
2[label="left,target,0,0"];
0--1 [label="AB,first,0,0"];
1--2 [label="BC, second, 3.14, 3.14"];
```

16.8.5 The .svg file produced

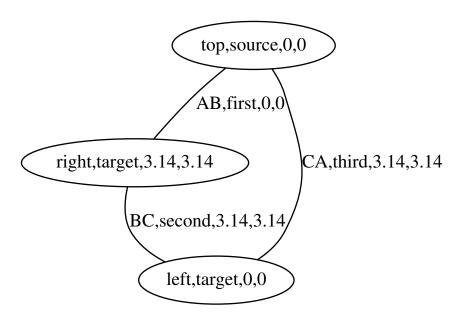


Figure 60: .svg file created from the 'create_custom_edges_and_vertices_k3_graph' function (algorithm 224) its .dot file, converted from .dot file to .svg using algorithm 361

17 Working on graphs with custom edges and vertices

17.1 Has a my_custom_edge

Before modifying our edges, let's first determine if we can find an edge by its custom type ('my_custom_edge') in a graph. After obtaing a my_custom_edge map, we obtain the edge iterators, dereference these to obtain the edge descriptors and then compare each edge its my_custom_edge with the one desired.

Algorithm 299 Find if there is a custom edge with a certain my_custom_edge

```
\# \mathbf{include} < \mathbf{boost} / \mathbf{graph} / \mathbf{properties} . \mathbf{hpp} >
#include "install_edge_custom_type.h"
#include "my custom edge.h"
template <typename graph>
bool has_edge_with_my_edge(
  const my_custom_edge& e,
  const graph& g
) noexcept
{
  using ed = typename boost::graph_traits<graph>::
      edge descriptor;
  const auto eip = edges(g);
  return std::find if (eip.first, eip.second,
     [e, g](\mathbf{const} \ ed\& \ d)
       const auto my edges map
         = get (boost :: edge custom type, g);
       return get(my_edges_map, d) == e;
  ) = eip.second;
}
```

This function can be demonstrated as in algorithm 300, where a certain 'my_custom_edge' cannot be found in an empty graph. After adding the desired my_custom_edge, it is found.

Algorithm 300 Demonstration of the 'has_custom_edge_with_my_edge' function

```
#include <cassert>
#include "add custom edge.h"
#include "
   create_empty_undirected_custom_edges_and_vertices_graph
   . h"
#include "has_edge_with my edge.h"
void has_edge_with_my_edge_demo() noexcept
{
  auto g
       create empty undirected custom edges and vertices graph
  assert (
    !has edge with my edge(
      my custom edge("Edward"),g
  );
  add custom edge(my custom edge("Edward"),g);
  assert (
    has_edge_with_my_edge(
      my custom edge("Edward"),g
  );
}
```

Note that this function only finds if there is at least one edge with that my_custom_edge: it does not tell how many edges with that my_custom_edge exist in the graph.

17.2 Find a my custom edge

Where STL functions work with iterators, here we obtain an edge descriptor (see chapter 2.12) to obtain a handle to the desired edge. Algorithm 301 shows how to obtain an edge descriptor to the first edge found with a specific my custom edge value.

Algorithm 301 Find the first custom edge with a certain my_custom_edge

```
#include <cassert>
#include <boost/graph/graph_traits.hpp>
#include "has edge with my edge.h"
#include "install edge custom type.h"
#include "my custom edge.h"
template <typename graph, typename custom edge>
typename boost::graph\_traits < graph > ::edge\_descriptor
find first custom edge with my edge (
  const custom edge& e,
  const graph& g
 noexcept
  using ed = typename boost::graph traits<graph>::
      edge descriptor;
  const auto eip = edges(g);
  const auto i = std::find if (
    eip.first, eip.second,
    [e,g] (const ed d) {
      const auto my_edges_map = get(boost::
         edge_custom_type, g);
      return get (my edges map, d) == e;
  );
  assert(i != eip.second);
  return *i;
}
```

With the edge descriptor obtained, one can read and modify the edge and the vertices surrounding it. Algorithm 302 shows some examples of how to do so.

Algorithm 302 Demonstration of the 'find_first_custom_edge_with_my_edge' function

17.3 Get an edge its my_custom_edge

To obtain the my_edeg from an edge descriptor, one needs to pull out the my_custom_edges map and then look up the my_edge of interest.

Algorithm 303 Get a vertex its my custom vertex from its vertex descriptor

To use 'get_custom_edge_my_custom_edge', one first needs to obtain an edge descriptor. Algorithm 304 shows a simple example.

Algorithm 304 Demonstration if the 'get custom edge my edge' function

17.4 Set an edge its my_custom_edge

If you know how to get the my_custom_edge from an edge descriptor, setting it is just as easy, as shown in algorithm 305.

Algorithm 305 Set a custom edge its my_custom_edge from its edge descriptor

```
#include <boost/graph/graph_traits.hpp>
#include <boost/graph/properties.hpp>
#include "install_edge_custom_type.h"
#include "my_custom_edge.h"
template <typename graph, typename custom_edge>
void set my custom edge (
  const custom_edge& edge,
  const typename boost::graph traits<graph>::
     edge descriptor& ed,
  graph& g
  noexcept
  static_assert(!std::is_const<graph>::value, "graph_
     cannot_be_const");
  auto my edge map = get(boost::edge custom type, g);
  put (my edge map, ed, edge);
}
```

To use 'set_my_custom_edge', one first needs to obtain an edge descriptor. Algorithm 306 shows a simple example.

Algorithm 306 Demonstration if the 'set my custom edge' function

```
#include <cassert>
#include "add custom edge.h"
#include "
   create empty undirected custom edges and vertices graph
   . h"
#include "find_first custom edge with my edge.h"
#include "get my custom edge.h"
#include "set my custom edge.h"
void set my custom edge demo() noexcept
  auto g
       create empty undirected custom edges and vertices graph
  const my custom edge old edge{"Dex"};
  add custom edge(old edge, g);
  const auto vd
    = find_first_custom_edge_with_my_edge(old_edge,g);
  assert (get my custom edge (vd,g)
   = old edge
  );
  const my custom edge new edge{"Diggy"};
  set_my_custom_edge(new_edge, vd, g);
  assert (get my custom edge (vd, g)
    == new edge
  );
}
```

17.5 Counting the edges with a certain selectedness

How often is an edge with a certain selectedness present? Here we'll find out.

Algorithm 307 Count the edges with a certain selectedness

```
#include < string>
\#include <boost/graph/properties.hpp>
#include "install_edge_is_selected.h"
template <typename graph>
int count_edges_with_selectedness(
  const bool selectedness,
  const graph& g
 noexcept
  using ed = typename graph::edge descriptor;
  const auto eip = edges(g);
  const auto cnt = std::count_if(
    eip.first, eip.second,
    [g, selectedness](const ed& d)
      const auto is selected map
        = get (boost::edge_is_selected, g);
      return selectedness
        == get (is selected map, d);
    }
  );
  return static cast<int>(cnt);
```

Here we use the STL std::count_if algorithm to count how many vertices have the desired selectedness.

Algorithm 308 shows some examples of how to do so.

Algorithm 308 Demonstration of the 'count_edges_with_selectedness' function

```
#include <cassert>
#include "count edges with selectedness.h"
#include "
   create_empty_directed_custom_and_selectable_edges_and_vertices_graph
   . h"
#include "add custom and selectable edge.h"
void count edges with selectedness demo() noexcept
{
  auto g =
     create empty directed custom and selectable edges and vertices graph
  add custom and selectable edge (
    my custom edge("AB"), true, g
  add custom and selectable edge (
    my custom edge("AA"), false, g
  );
  assert (count edges with selectedness (true, g) == 1);
  assert (count_edges_with_selectedness (false, g) == 1);
}
```

17.6 Create a direct-neighbour subgraph from a vertex descriptor of a graph with custom edges and vertices

Suppose you have a vertex of interest its vertex descriptor. Let's say you want to get a subgraph of that vertex and its direct neighbours only. This means that all vertices of that subgraph are adjacent vertices and that the edges go either from focal vertex to its neighbours, or from adjacent vertex to adjacent neighbour.

Here is the code that does exactly that:

Algorithm 309 Get the direct-neighbour custom edges and vertices subgraph from a vertex descriptor

```
\#include <map>
#include <boost/graph/adjacency list.hpp>
#include "add custom vertex.h"
\#include "add_custom_edge_between_vertices.h"
#include "get_my_custom_edge.h"
#include "get my custom vertex.h"
template <typename graph, typename vertex_descriptor>
graph
   create direct neighbour custom edges and vertices subgraph
  const vertex descriptor & vd,
  const graph& g
{
  graph h;
  std::map<vertex descriptor, vertex descriptor> m;
    const auto vd h = add custom vertex (
      get my custom vertex (vd, g), h
    m. insert (std::make pair (vd, vd h));
  //Copy\ vertices
    const auto vdsi = boost::adjacent vertices(vd, g);
    std::transform(vdsi.first, vdsi.second,
      std::inserter(m, std::begin(m)),
      [g, &h](const vertex_descriptor&d)
        const auto vd_h = add_custom_vertex(
          get my custom vertex (d,g), h
        ):
        return std::make pair(d,vd h);
    );
  //\mathit{Copy}\ edges
    const auto eip = edges(g);
    const auto j = eip.second;
    for (auto i = eip.first; i!=j; ++i)
      const auto vd from = source(*i, g);
      const auto vd to = target(*i, g);
      if (m. find (vd_from) = 34\ddleft d :: end (m)) continue;
      if (m. find (vd to) == std :: end (m)) continue;
      add_custom_edge_between_vertices(
        get my custom edge(*i, g),
        m[vd\_from],
        m[vd to],
        h
      );
```

This demonstration code shows that the direct-neighbour graph of each vertex of a K_2 graphs is ... a K_2 graph!

```
Algorithm 310 Demo of the 'create direct custom edges and vertices neighbour subgraph'
function
#include "
   create direct neighbour custom edges and vertices subgraph
#include "create_custom edges and vertices k2 graph.h"
#include "get_my_custom_vertexes.h"
void
   create direct neighbour custom edges and vertices subgraph demo
   () noexcept
  const auto g =
     create custom edges and vertices k2 graph();
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (auto i=vip.first; i!=j; ++i) {
    const auto h =
       create direct neighbour custom edges and vertices subgraph
      *i, g
    );
    assert(boost::num \ vertices(h) == 2);
    assert(boost::num\_edges(h) == 1);
    const auto v = get my custom vertexes(h);
    std::set<my custom vertex> vertexes(std::begin(v),std
        :: end(v));
    const my custom vertex a ("A", "source", 0.0, 0.0);
    const my custom vertex b("B","target",3.14,3.14);
    assert(vertexes.count(a) == 1);
    assert(vertexes.count(b) == 1);
  }
}
```

17.7 Creating all direct-neighbour subgraphs from a graph with custom edges and vertices

Using the previous function, it is easy to create all direct-neighbour subgraphs from a graph with custom vertices:

Algorithm 311 Create all direct-neighbour subgraphs from a graph with custom edges and vertices

```
#include < vector >
#include "
   create direct neighbour custom edges and vertices subgraph
    . h"
template <typename graph>
std::vector < graph >
   create all direct neighbour custom edges and vertices subgraphs
   (
  const graph g
) noexcept
{
  using vd = typename graph::vertex_descriptor;
  std::vector<graph> v;
  v.resize(boost::num_vertices(g));
  const auto vip = vertices(g);
  std::transform(
    vip.first , vip.second ,
    std::begin(v),
    [g](const vd& d)
      return
          create\_direct\_neighbour\_custom\_edges\_and\_vertices\_subgraph
          (
        d, g
      );
    }
  );
  return v;
```

This demonstration code shows how to extract the subgraphs from a path graph:

Algorithm 312 Demo of the 'create_all_direct_neighbour_custom_edges_and_vertices_subgraphs' function

The sub-graphs are shown here:

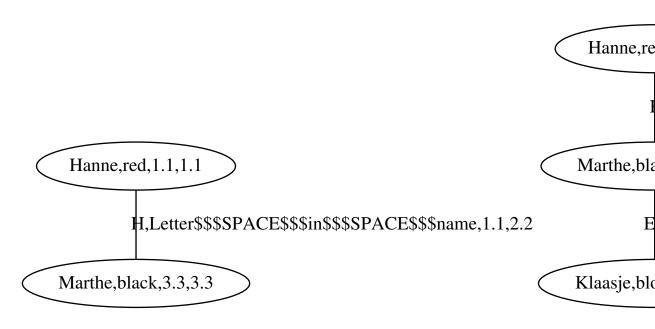


Figure 61: All subgraphs created

17.8 Storing a graph with custom edges and vertices as a .dot

If you used the create_custom_edges_and_vertices_k3_graph function (algorithm 296) to produce a K_3 graph with edges and vertices associated with my_custom_edge and my_custom_vertex objects, you can store these my_custom_edges and my_custom_vertex-es additionally with algorithm 313:

Algorithm 313 Storing a graph with custom edges and vertices as a .dot file

```
#include <fstream>
#include < string>
#include <boost/graph/graphviz.hpp>
#include <boost/graph/properties.hpp>
#include "get my custom edge.h"
#include "get_my_custom_vertex.h"
#include "my custom vertex.h"
template <typename graph>
void save custom edges and vertices graph to dot (
  const graph& g,
  const std::string& filename
{
  using vd = typename graph::vertex descriptor;
  using ed = typename graph::edge descriptor;
  std::ofstream f(filename);
  boost::write_graphviz(
    f,
    g,
    | g | (
      std::ostream& out, const vd& d) {
      const my_custom_vertex m{
        get_my_custom_vertex(d, g)
      };
      [g](std::ostream\& out, const ed\& d) {
      const my custom edge& m{
        get_my_custom_edge(d, g)
      out << "[label=\"" << m << "\"]";
  );
}
```

17.9 Load a directed graph with custom edges and vertices from a .dot file

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with custom edges and vertices is loaded, as shown in algorithm 314:

Algorithm 314 Loading a directed graph with custom edges and vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create empty directed custom edges and vertices graph.
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::property<
    boost::vertex custom_type_t, my_custom_vertex
  >,
  boost::property<
    boost::edge custom type t, my custom edge
load directed custom edges and vertices graph from dot (
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g =
     create empty directed custom edges and vertices graph
     ();
  boost::dynamic properties dp(boost::
     ignore other properties);
  dp.property("label", get(boost::vertex custom type, g))
  dp.property("edge id", get(boost::edge custom type, g))
  dp.property("label", get(boost::edge custom type, g));
  boost::read_graphviz(f,g,dp);
  return g;
}
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Next to this, a boost::dynamic_properties is created with its default constructor, after which we direct the boost::dynamic_properties to find a 'node_id' and 'label' in the vertex name map, 'edge_id' and 'label' to

the edge name map. From this and the empty graph, 'boost::read_graphviz' is called to build up the graph.

Algorithm 315 shows how to use the 'load_directed_custom_edges_and_vertices_graph_from_dot' function:

Algorithm 315 Demonstration of the 'load_directed_custom_edges_and_vertices_graph_from_dot' function

```
#include "create custom edges and vertices markov chain.h
#include "get my custom vertexes.h"
#include "
   load directed custom edges and vertices graph from dot
   . h"
#include "save custom edges and vertices graph to dot.h"
void
   load directed custom edges and vertices graph from dot demo
   () noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create_custom_edges_and_vertices_markov_chain();
  const std::string filename{
    "create custom edges and vertices markov chain.dot"
  save\_custom\_edges\_and\_vertices\_graph\_to\_dot(g,\ filename)
     );
  const auto h
       load directed custom edges and vertices graph from dot
      filename
    );
  assert(num\_edges(g) == num\_edges(h));
  assert(num \ vertices(g) == num \ vertices(h));
  assert (get my custom vertexes (g)
    == get my custom vertexes(h)
  );
}
```

This demonstration shows how the Markov chain is created using the 'create custom edges and vertices markov chain' function (algorithm 293), saved

and then loaded.

17.10 Load an undirected graph with custom edges and vertices from a .dot file

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with custom edges and vertices is loaded, as shown in algorithm 316:

Algorithm 316 Loading an undirected graph with custom edges and vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create empty undirected custom edges and vertices graph
   . h"
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost:: vertex\_custom\_type\_t \;, \; my\_custom\_vertex
  >,
  boost::property<
    boost::edge custom type t, my custom edge
>
load undirected custom edges and vertices graph from dot (
  const std::string& dot filename
{
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g =
     create empty undirected custom edges and vertices graph
     ();
  boost::dynamic properties dp(boost::
     ignore_other_properties);
  dp.property("label", get(boost::vertex custom type, g))
  dp.property("edge id", get(boost::edge custom type, g))
  dp.property("label", get(boost::edge custom type, g));
  boost:: read\_graphviz(f,g,dp);
  return g;
}
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 17.9 describes the rationale of this function.

Algorithm 317 shows how to use the 'load undirected custom vertices graph from dot'

function:

}

```
Algorithm 317 Demonstration of the 'load undirected custom edges and vertices graph from dot'
#include "create custom edges and vertices k3 graph.h"
#include "
   load undirected custom edges and vertices graph from dot
   . h"
#include "save custom edges and vertices graph to dot.h"
#include "get my custom vertexes.h"
void
   load undirected custom edges and vertices graph from dot demo
   () noexcept
  using boost::num edges;
  using boost::num vertices;
  const auto g
    = create_custom_edges_and_vertices_k3_graph();
  const std::string filename{
    "create_custom_edges_and_vertices_k3_graph.dot"
  save_custom_edges_and_vertices_graph_to_dot(g, filename
     );
  const auto h
       load undirected custom edges and vertices graph from dot
       (filename);
  assert(num edges(g) == num edges(h));
```

This demonstration shows how K_2 with custom vertices is created using the 'create_custom_vertices_k2_graph' function (algorithm 227), saved and then loaded. The loaded graph is checked to be a graph similar to the original.

 $assert(num \ vertices(g) == num \ vertices(h));$

assert(get_my_custom_vertexes(g) ==
get my custom vertexes(h));

18 Building graphs with custom and selectable edges and vertices

Now also the edge can be selected

- An empty directed graph that allows for custom and selectable vertices: see chapter 18.2
- An empty undirected graph that allows for custom and selectable vertices: see chapter 18.3
- $\bullet\,$ A two-state Markov chain with custom and selectable vertices: see chapter $18.5\,$
- K_3 with custom and selectable vertices: see chapter 18.6

In the process, some basic (sometimes bordering trivial) functions are shown:

- Installing the new edge property: see chapter 18.1
- Adding a custom and selectable vertex: see chapter 18.4

These functions are mostly there for completion and showing which data types are used.

18.1 Installing the new is selected property

Installing a new property would have been easier, if 'more C++ compilers were standards conformant' ([8], chapter 3.6, footnote at page 52). Boost.Graph uses the BOOST INSTALL PROPERTY macro to allow using a custom property:

Algorithm 318 Installing the edge is selected property

```
#include <boost/graph/properties.hpp>
namespace boost {
  enum edge_is_selected_t { edge_is_selected = 314159 };
  BOOST_INSTALL_PROPERTY(edge, is_selected);
}
```

The enum value 31415 must be unique.

18.2 Create an empty directed graph with custom and selectable edges and vertices

Algorithm 319 Creating an empty directed graph with custom and selectable edges and vertices

```
#include <boost/graph/adjacency list.hpp>
#include "install edge custom type.h"
#include "install_edge_is_selected.h"
#include "install vertex custom type.h"
#include "install vertex is selected.h"
#include "my_custom_edge.h"
#include "my_custom_vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS,
  boost::property<
    boost::vertex custom type t, my_custom_vertex,
    boost::property<
      boost::vertex is selected t, bool
  >,
  boost::property<
    boost::edge custom type t, my custom edge,
    boost::property<
      boost::edge is selected t, bool
create empty directed custom and selectable edges and vertices graph
   () noexcept
  return {};
```

This code is very similar to the code described in chapter 12.3, except that there is a new, fifth template argument:

```
boost::property < boost::edge_custom_type_t, my_custom_edge,
   boost::property < boost::edge_is_selected_t, bool,
>
```

This can be read as: "edges have two properties: an associated custom type (of type my_custom_edge) and an associated is_selected property (of type bool)".

Demo:

```
Algorithm
                 320
                           Demonstration
                                              of
                                                      the
                                                                'cre-
ate_empty_directed_custom_and_selectable_edges_and_vertices_graph'
\underline{\mathrm{function}}
#include "
   create\_empty\_directed\_custom\_and\_selectable\_edges\_and\_vertices\_graph
    . h"
void
   create\_empty\_directed\_custom\_and\_selectable\_edges\_and\_vertices\_graph\_demo
    () noexcept
  const auto g
        create_empty_directed_custom_and_selectable_edges_and_vertices_graph
  assert(boost::num\_edges(g) == 0);
  assert(boost::num\_vertices(g) == 0);
}
```

18.3 Create an empty undirected graph with custom and selectable edges and vertices

Algorithm 321 Creating an empty undirected graph with custom and selectable edges and vertices

```
#include <boost/graph/adjacency list.hpp>
\#include "install\_edge\_custom\_type.h"
#include "install edge is selected.h"
#include "install vertex custom type.h"
#include "install_vertex_is_selected.h"
#include "my_custom_edge.h"
#include "my_custom vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex_custom_type_t, my_custom_vertex,
    boost::property<
      {\tt boost::vertex\_is\_selected\_t}\ ,\ {\tt bool}
  >,
  boost::property<
    boost::edge\_custom\_type\_t\,, \ my\_custom\_edge\,,
    boost::property<
      boost::edge is selected t, bool
create empty undirected custom and selectable edges and vertices graph
   () noexcept
  return {};
```

This code is very similar to the code described in chapter 18.2, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS). Demo:

```
Algorithm
                322
                         Demonstration
                                                  the
                                                           'cre-
ate_empty_undirected_custom_and_selectable_edges_and_vertices_graph'
function
#include "
   create_empty_undirected_custom_and_selectable_edges_and_vertices_graph
void
   create empty undirected custom and selectable edges and vertices graph demo
   () noexcept
  const auto g
        create\_empty\_undirected\_custom\_and\_selectable\_edges\_and\_vertices\_graph
  assert(boost::num\_edges(g) == 0);
  assert(boost::num\_vertices(g) == 0);
}
```

18.4 Add a custom and selectable edge

Adding a custom and selectable edge is very similar to adding a custom and selectable vertex (chapter 14.4).

${\bf Algorithm~323}$ Add a custom and selectable edge

```
#include <type traits>
#include <boost/graph/adjacency_list.hpp>
#include "install_edge_custom_type.h"
#include "install edge is selected.h"
\#include "my_custom_edge.\overline{h}"
#include <cassert>
#include <boost/graph/adjacency list.hpp>
#include "install_edge_custom_type.h"
#include "my custom edge.h"
#include "add custom and selectable edge between vertices
    . h"
\mathbf{template} \ < \! \mathbf{typename} \ \mathrm{grap} \, h \! > \!
typename boost::graph traits<graph>::edge descriptor
add custom and selectable edge (
  const my_custom_edge& edge ,
  const bool is selected,
  graph& g
  noexcept
{
  static assert (!std::is const<graph>::value, "graph_
      cannot_be_const");
  const auto vd_a = boost::add_vertex(g);
  const auto vd b = boost::add vertex(g);
  return add custom and selectable edge between vertices (
    edge\,,\;\;is\_selected\,\,,\;\;vd\_a\,,\;\;vd\_b\,,\;\;g
  );
}
```

When having added a new (abstract) edge to the graph, the edge descriptor is used to set the my_custom_edge and the selectedness in the graph its my_custom_edge and is_selected map.

Here is the demo:

Algorithm 324 Demo of 'add custom and selectable vertex'

```
#include <cassert>
#include "add_custom_and_selectable_edge.h"
#include "
   create empty directed custom and selectable edges and vertices graph
   . h"
#include "
   create_empty_undirected_custom_and_selectable_edges_and_vertices_graph
void add custom and selectable edge demo() noexcept
  auto g =
     create\_empty\_directed\_custom\_and\_selectable\_edges\_and\_vertices\_graph
  assert(boost::num \ vertices(g) == 0);
  assert(boost::num\_edges(g) == 0);
  add custom and selectable edge (
    my\_custom\_edge("X"),
    true,
  );
  assert(boost::num\_edges(g) == 1);
```

18.5 Creating a Markov-chain with custom and selectable vertices

18.5.1 Graph

Figure 62 shows the graph that will be reproduced:

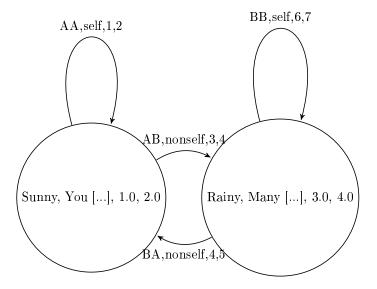


Figure 62: A two-state Markov chain where the edges and vertices have custom properies. The edges' and vertices' properties are nonsensical

18.5.2 Function to create such a graph

Here is the code creating a two-state Markov chain with custom edges and vertices:

Algorithm 325 Creating the two-state Markov chain as depicted in figure 62

```
#include <cassert>
#include "
   create empty directed custom and selectable edges and vertices graph
#include "add custom and selectable edge between vertices
   . h"
#include "add custom and selectable vertex.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost :: directedS,
  boost::property<
    boost::vertex_custom_type_t, my_custom_vertex,
    boost::property<
      boost::vertex is selected t, bool
  >,
  boost::property<
    boost::edge_custom_type_t, my_custom_edge,
    boost::property<
      boost::edge is selected t, bool
 >
create custom and selectable edges and vertices markov chain
   () noexcept
{
  auto g
       create empty directed custom and selectable edges and vertices graph
  const auto vd a = add custom and selectable vertex (
    my_custom_vertex("Sunny","Yellow_thing",1.0,2.0),
    true,
    g
  );
  const auto vd b = add custom and selectable vertex(
    my_custom_vertex("Rainy", "Grey_things", 3.0,4.0),
    false,
    g
  );
  add custom and selectable edge between vertices (
    my custom edge("A_to_A"),
    true,
    vd a, vd a,
                            360
    g
  );
  add custom and selectable edge between vertices (
    my custom edge("A_to_B"),
    false,
    vd_a, vd_b,
    g
```

18.5.3 Creating such a graph

Here is the demo:

```
Algorithm 326 Demo of the 'create custom and selectable edges and vertices markov chain'
function (algorithm 325)
#include < cassert >
#include "
    create\_custom\_and\_selectable\_edges\_and\_vertices\_markov\_chain
#include "get vertex selectednesses.h"
void
    create_custom_and_selectable_edges_and_vertices_markov_chain_demo
    () noexcept
  const auto g
        create_custom_and_selectable_edges_and_vertices_markov_chain
         ();
  \mathbf{const} \ \mathrm{std} :: \mathrm{vector} \! < \! \mathbf{bool} \! >
    expected selectednesses {
    true, false
  };
  const std::vector<bool>
     vertex_selectednesses{
     get_vertex_selectednesses(g)
  };
  assert (expected selectednesses
    == vertex selectednesses
  );
}
```

18.5.4 The .dot file produced

```
Algorithm
               327
                                                         the
                       .dot
                               file
                                      created
                                                 from
                                                                 'cre-
ate_custom_and_selectable_vertices_markov_chain'
                                                  function (algorithm
325), converted from graph to .dot file using algorithm 52
digraph G {
O[label="Sunny, Yellow$$$SPACE$$$thing,1,1", regular="1"];
1[label="Rainy,Grey$$$SPACE$$$things,3,3", regular="0"];
0->0 [label="A$$$$PACE$$$to$$$$PACE$$$A,,1,1", regular="1"];
0->1 [label="A$$$$PACE$$$to$$$$PACE$$$B,,1,1", regular="0"];
1->0 [label="B$$$$PACE$$$to$$$$PACE$$$A,,1,1", regular="0"];
1->1 [label="B$$$$PACE$$$to$$$$PACE$$$B,,1,1", regular="1"];
```

18.5.5 The .svg file produced

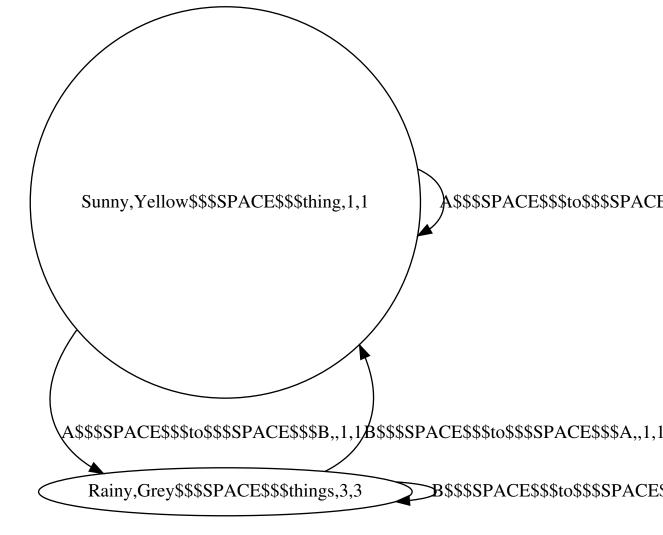


Figure 63: .svg file created from the 'create_custom_and_selectable_vertices_markov_chain' function (algorithm 224) its .dot file, converted from .dot file to .svg using algorithm 361

Note how the .svg changed it appearance due to the Graphviz 'regular' property (see chapter 25.2): the vertex labeled 'Sunny' is drawn according to the Graphviz 'regular' attribute, which makes it a circle. The other vertex, labeled 'Rainy' is not drawn as such and retained its ellipsoid appearance.

Creating K_2 with custom and selectable edges and 18.6 vertices

18.6.1 Graph

We reproduce the K_2 with custom vertices of chapter 12.8 , but now are vertices can be selected as well:
[graph here]

Algorithm 328 Creating K_3 as depicted in figure 33

```
#include "
   create empty undirected custom and selectable edges and vertices graph
   . h"
#include "add custom and selectable vertex.h"
#include "add custom and selectable edge between vertices
   . h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex_custom_type_t, my_custom_vertex,
    boost::property<
      boost::vertex is selected t, bool
   >
  boost::property<
    boost::edge custom type t, my custom edge,
    boost::property<
      boost::edge is selected t, bool
 >
create custom and selectable edges and vertices k2 graph
   () noexcept
  auto g
       create empty undirected custom and selectable edges and vertices graph
  const my custom vertex va("A", "source", 0.0, 0.0);
  const my custom vertex vb("B","target",3.14,3.14);
  const my_custom_edge ea("between");
  const auto vd a = add custom and selectable vertex (va,
     true, g);
  const auto vd b = add custom and selectable vertex (vb,
     false, g);
  add custom and selectable edge between vertices (ea,
     false, vd a, vd b, g);
  return g;
}
```

Most of the code is a slight modification of algorithm 227. In the end, the associated my_custom_vertex and is_selected properties are obtained as boost::property_maps and set with the desired my_custom_vertex objects and selectednesses.

18.6.3 Creating such a graph

Here is the demo:

```
Algorithm 329 Demo of the 'create_custom_and_selectable_edges_and_vertices_k2_graph' function (algorithm 328)
```

```
#include < cassert >
#include "
   create custom and selectable edges and vertices k2 graph
#include "has custom vertex with my vertex.h"
void
   create custom and selectable edges and vertices k2 graph demo
   () noexcept
{
  const auto g =
     create custom and selectable edges and vertices k2 graph
     ();
  assert(boost::num edges(g) == 1);
  assert(boost::num \ vertices(g) == 2);
  assert (has_custom_vertex_with_my_custom_vertex(
    my\_custom\_vertex("A", "source", 0.0, 0.0), g)
  );
  assert (has custom vertex with my custom vertex (
    my_custom_vertex("B", "target", 3.14, 3.14), g)
  );
}
```

18.6.4 The .dot file produced

```
Algorithm 330 .dot file created from the 'create_custom_and_selectable_vertices_k2_graph' function (algorithm 328), converted from graph to .dot file using algorithm 52 graph G {
    O[label="A,source,0,0", regular="1"];
    1[label="B,target,3.14,3.14", regular="0"];
    0--1 [label="between,,1,1", regular="0"];
}
```

18.6.5 The .svg file produced

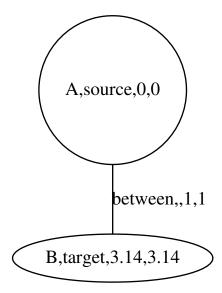


Figure 64: .svg file created from the 'create_custom_and_selectable_vertices_k2_graph' function (algorithm 224) its .dot file, converted from .dot file to .svg using algorithm 361

Note how the .svg changed it appearance due to the Graphviz 'regular' property (see chapter 25.2): the vertex labeled 'A' is drawn according to the Graphviz 'regular' attribute, which makes it a circle. The other vertex, labeled 'B' is not drawn as such and retained its ellipsoid appearance.

19 Working on graphs with custom and selectable edges and vertices

This chapter shows some basic operations to do on graphs with custom and selectable edges and vertices.

- Storing an directed/undirected graph with custom and selectable edges and vertices as a .dot file: chapter 19.3
- \bullet Loading a directed graph with custom and selectable edges and vertices from a .dot file: chapter 19.4
- Loading an undirected directed graph with custom and selectable edges amd vertices from a .dot file: chapter 19.5

19.1 Create a direct-neighbour subgraph from a vertex descriptor of a graph with custom and selectable edges and vertices

Suppose you have a vertex of interest its vertex descriptor. Let's say you want to get a subgraph of that vertex and its direct neighbours only. This means that all vertices of that subgraph are adjacent vertices and that the edges go either from focal vertex to its neighbours, or from adjacent vertex to adjacent neighbour.

Here is the code that does exactly that:

Algorithm 331 Get the direct-neighbour custom edges and vertices subgraph from a vertex descriptor

```
#include <map>
#include <boost/graph/adjacency list.hpp>
#include "add custom and selectable edge between vertices
    . h"
#include "add custom and selectable vertex.h"
#include "get edge selectedness.h"
#include "get_my_custom_edge.h"
#include "get my custom vertex.h"
#include "get vertex selectedness.h"
template <typename graph, typename vertex_descriptor>
graph
   create_direct_neighbour_custom_and_selectable_edges_and_vertices_subgraph
  const vertex descriptor& vd,
  const graph& g
{
  graph h;
  std::map<vertex descriptor, vertex descriptor> m;
    const auto vd_h = add_custom_and_selectable_vertex(
      get_my_custom_vertex(vd, g),
      get_vertex_selectedness(vd, g),
      h
    m. insert (std::make pair (vd, vd h));
  //Copy vertices
    const auto vdsi = boost::adjacent_vertices(vd, g);
    std::transform(vdsi.first, vdsi.second,
      std::inserter(m, std::begin(m)),
      [g, &h](const vertex_descriptor&d)
        \mathbf{const} auto \mathbf{vd} \mathbf{h} =
            add custom and selectable vertex (
          get my custom vertex (d, g),
          get_vertex_selectedness(d, g),
          h
        );
        return std::make pair(d,vd h);
    );
                             370
  //Copy edges
    const auto eip = edges(g);
    const auto j = eip.second;
    for (auto i = eip.first; i!=j; ++i)
      const auto vd from = source(*i, g);
      const auto vd_to = target(*i, g);
```

This demonstration code shows that the direct-neighbour graph of each vertex of a K_2 graphs is ... a K_2 graph!

```
Algorithm 332 Demo of the 'create direct custom and selectable edges and vertices neighbour subgr
function
#include "
   create direct neighbour custom and selectable edges and vertices subgraph
   . h"
#include "
   create_custom_and_selectable_edges_and_vertices_k2_graph
    . h"
#include "get my custom vertexes.h"
void
   create direct neighbour custom and selectable edges and vertices subgraph dem
   () noexcept
  const auto g =
     create custom and selectable edges and vertices k2 graph
     ();
  const auto vip = vertices(g);
  const auto j = vip.second;
  for (auto i=vip.first; i!=j; ++i) {
    const auto h =
       create direct neighbour custom and selectable edges and vertices subgraph
       (
      *\,\mathrm{i}, g
    );
    assert (boost:: num vertices (h) == 2);
    assert(boost::num\_edges(h) == 1);
    const auto v = get my custom vertexes(h);
    std::set<my custom vertex> vertexes(std::begin(v),std
        :: end(v));
    {f const} my_custom_vertex a("A", "source", 0.0,0.0);
    const my_custom_vertex b("B","target",3.14,3.14);
    assert(vertexes.count(a) == 1);
```

assert(vertexes.count(b) == 1);

}

19.2 Creating all direct-neighbour subgraphs from a graph with custom and selectable edges and vertices

Using the previous function, it is easy to create all direct-neighbour subgraphs from a graph with custom vertices:

Algorithm 333 Create all direct-neighbour subgraphs from a graph with custom and selectable edges and vertices

```
#include < vector>
#include "
   create direct neighbour custom and selectable edges and vertices subgraph
   . h"
template <typename graph>
std::vector < graph >
   create all direct neighbour custom and selectable edges and vertices subgraph
  const graph& g
 noexcept
{
  using vd = typename graph::vertex_descriptor;
  std::vector<graph> v;
  v.resize(boost::num vertices(g));
  const auto vip = vertices(g);
  std::transform(
    vip.first, vip.second,
    std::begin(v),
    [g](const vd& d)
    {
      return
          create direct neighbour custom and selectable edges and vertices subgra
        d\,,\ g
      );
    }
  return v;
```

This demonstration code shows how to extract the subgraphs from a path graph:

Algorithm 334 Demo of the 'create_all_direct_neighbour_custom_and_selecteable_edges_and_vertices_function

```
#include <cassert>
#include "
                   create_all_direct_neighbour_custom_and_selectable_edges_and_vertices_subgraph
                    . h"
#include "
                  create\_custom\_and\_selectable\_edges\_and\_vertices\_k2 - graph
                    . h"
void
                  create all direct neighbour custom and selectable edges and vertices subgraphs
                   () noexcept
 {
           const auto v
                                        create\_all\_direct\_neighbour\_custom\_and\_selectable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_subgetable\_edges\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_vertices\_and\_v
                                            create custom and selectable edges and vertices k2 graph
            assert(v.size() == 2);
           for (const auto g: v)
                       assert (boost:: num vertices (g) == 2);
                       assert(boost::num edges(g) == 1);
  }
```

The sub-graphs are shown here:



Figure 65: All subgraphs created

19.3 Storing a graph with custom and selectable edges and vertices as a .dot

If you used the 'create_custom_and_selectable_edges_and_vertices_k2_graph' function (algorithm 328) to produce a K_2 graph with edges and vertices associated with (1) my_custom_edge/my_custom_vertex objects, and (2) a boolean indicating its selectedness, you can store such graphs with algorithm 335:

Algorithm 335 Storing a graph with custom and selectable edges and vertices as a .dot file

```
#include <fstream>
#include < string>
#include <boost/graph/graphviz.hpp>
#include "install edge custom type.h"
#include "install edge is selected.h"
#include "install_vertex_custom_type.h"
#include "install vertex is selected.h"
#include "make_custom_and_selectable_vertices_writer.h"
#include "my custom edge.h"
#include "my custom vertex.h"
template <typename graph>
void
   save\_custom\_and\_selectable\_edges\_and\_vertices\_graph\_to\_dot
  const graph& g,
  const std::string& filename
  std::ofstream f(filename);
  boost::write_graphviz(f, g,
    make custom and selectable vertices writer (
      get (boost::vertex custom type,g),
      get (boost::vertex is selected,g)
    ),
    make custom and selectable vertices writer (
      get (boost::edge custom type,g),
      get(boost::edge is selected,g)
  );
}
```

We re-use the writer.

Special about this, is that even for Graphviz-unfriendly input, it still works.

19.4 Loading a directed graph with custom and selectable edges and vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an directed graph with custom and selectable edges and vertices is loaded, as shown in algorithm 336:

Algorithm 336 Loading a directed graph with custom and selectable edges and vertices from a .dot file

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "
   create_empty_directed_custom_and_selectable_edges_and_vertices_graph
    . h"
#include "install_edge_custom_type.h"
#include "install edge is selected.h"
#include "install vertex custom type.h"
#include "install vertex is selected.h"
#include "is regular file.h"
template < class graph = decltype (
   create empty directed custom and selectable edges and vertices graph
   ())>
graph
   load \quad directed \quad custom \quad and \quad selectable\_edges\_and\_vertices\_graph\_from\_dot
  const std::string& dot filename
  assert(is_regular_file(dot_filename));
  std::ifstream f(dot_filename.c_str());
  graph g;
  boost::dynamic properties dp (
    boost::ignore_other_properties
  dp.property("label", get(boost::vertex custom type, g))
  dp.property("regular", get(boost::vertex is selected, g
     ));
  dp.property("label", get(boost::edge_custom_type, g));
  \tt dp.property("regular", get(boost::edge\_is\_selected, g))
  boost::read graphviz(f,g,dp);
  return g;
```

In this algorithm, first it is checked if the file to load exists. Then an empty directed graph is created. Then, a boost::dynamic_properties is created with its default constructor, after which

• The Graphviz attribute 'node_id' (see chapter 25.2 for most Graphviz attributes) is connected to a vertex its 'my custom vertex' property

- The Graphviz attribute 'label' is connected to a vertex its 'my_custom_vertex' property
- The Graphviz attribute 'regular' is connected to a vertex its 'is_selected' vertex property

 $Algorithm\ 337\ shows\ how\ to\ use\ the\ `load_directed_custom_vertices_graph_from_dot' function:$

```
Algorithm 337 Demonstration of the 'load_directed_custom_and_selectable_edges_and_vertices_graph_function
```

```
#include <cassert>
#include "
   create custom and selectable edges and vertices markov chain
   . h"
#include "is regular file.h"
#include "
   save\_custom\_and\_selectable\_edges\_and\_vertices\_graph\_to\_dot
   . h"
void
   load directed custom and selectable edges and vertices_graph_from_dot_demo
   () noexcept
{
  const auto g
       create custom and selectable edges and vertices markov chain
  const std::string filename{
       create custom and selectable edges and vertices markov chain
       . dot "
  };
  save custom and selectable edges and vertices graph to dot
    filename
  assert(is_regular_file(filename));
}
```

This demonstration shows how the Markov chain is created using the 'create_custom_vertices_markov_chain' function (algorithm 224), saved and then checked to exist.

19.5 Loading an undirected graph with custom and selectable edges and vertices from a .dot

When loading a graph from file, one needs to specify a type of graph. In this example, an undirected graph with custom and selectable vertices is loaded, as shown in algorithm 338:

 $\bf Algorithm~338~{\rm Loading~an~undirected~graph~with~custom~vertices~from~a~.dot~file$

```
#include <fstream>
\# \mathbf{include} < \mathbf{boost} / \operatorname{graph} / \operatorname{graphviz} . hpp>
#include "
   create_empty_undirected_custom_and_selectable_edges_and vertices graph
    . h"
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::property<
    boost::vertex custom type t, my custom vertex,
    boost::property<
      boost::vertex is selected t, bool
    >
  >,
  boost::property<
    boost::edge custom type t, my custom edge,
    boost::property<
      boost::edge is selected t, bool
  >
load_undirected_custom_and_selectable_edges_and_vertices_graph_from_dot
  const std::string& dot filename
  assert (is regular file (dot filename));
  std::ifstream f(dot filename.c str());
  auto g =
     create empty undirected custom and selectable edges and vertices graph
  boost::dynamic_properties dp(
    boost::ignore other properties
  );
  dp.property("label", get(boost::vertex custom type, g))
  dp.property("regular", get(boost::vertex is selected, g
     ));
  dp.property("label", get(boost::edge_custom_type, g));
  dp.property("regular", get(boost::edge is selected, g))
  boost::read graphviz(f,g,dp);
  return g;
```

The only difference with loading a directed graph, is that the initial empty graph is undirected instead. Chapter 19.4 describes the rationale of this function

Algorithm 339 shows how to use the 'load_undirected_custom_vertices_graph_from_dot' function'

 $\overline{\textbf{Algorithm 339}} \ Demonstration \ of the \ `load_undirected_custom_and_selectable_edges_and_vertices_graph function$

```
#include < cassert >
#include "
   create custom and selectable edges and vertices k2 graph
    . h"
#include "is regular file.h"
#include "
   save\_custom\_and\_selectable\_edges\_and\_vertices\_graph\_to\_dot
    . h"
void
   load undirected custom and selectable edges and vertices graph from dot demo
    () noexcept
  const auto g
        create\_custom\_and\_selectable\_edges\_and\_vertices\_k2\_graph
  const std::string filename{
        create\_custom\_and\_selectable\_edges\_and\_vertices\_k2\_graph
  };
  save_custom_and_selectable_edges_and_vertices_graph_to_dot
    g,
    filename
  assert(is_regular_file(filename));
}
```

This demonstration shows how K_2 with custom vertices is created using the 'create_custom_vertices_k2_graph' function (algorithm 227), saved and then checked to exist.

20 Building graphs with a graph name

Up until now, the graphs created have had no properties themselves. Sure, the edges and vertices have had properties, but the graph itself has had none. Until now.

In this chapter, graphs will be created with a graph name of type std::string

- An empty directed graph with a graph name: see chapter
- An empty undirected graph with a graph name: see chapter
- A two-state Markov chain with a graph name: see chapter
- K_3 with a graph name: see chapter

In the process, some basic (sometimes bordering trivial) functions are shown:

- Getting a graph its name: see chapter
- Setting a graph its name: see chapter

20.1 Create an empty directed graph with a graph name property

Algorithm 340 shows the function to create an empty directed graph with a graph name.

Algorithm 340 Creating an empty directed graph with a graph name

```
#include <boost/graph/adjacency_list.hpp>
boost:: adjacency_list <
   boost:: vecS ,
   boost:: vecS ,
   boost:: no_property ,
   boost:: no_property ,
   boost:: property <
      boost:: graph_name_t , std:: string >
   create_empty_directed_graph_with_graph_name() noexcept {
    return {};
}
```

This boost::adjacency list is of the following type:

- the first 'boost::vecS': select (that is what the 'S' means) that out edges are stored in a std::vector. This is the default way.
- the second 'boost::vecS': select that the graph vertices are stored in a std::vector. This is the default way.
- 'boost::directedS': select that the graph is directed. This is the default selectedness
- the first 'boost::no_property': the vertices have no properties. This is the default (non-)property
- the second 'boost::no_property': the vertices have no properties. This is the default (non-)propert
- 'boost::property
boost::graph_name_t, std::string>': the graph itself has a single property: its boost::graph_name has type std::string

 $Algorithm\ 341\ demonstrates\ the\ `create_empty_directed_graph_with_graph_name'\ function.$

```
{\bf Algorithm~341~Demonstration~of~`create\_empty\_directed\_graph\_with\_graph\_name'}
```

20.2 Create an empty undirected graph with a graph name property

Algorithm 342 shows the function to create an empty undirected graph with a graph name.

Algorithm 342 Creating an empty undirected graph with a graph name

```
#include <boost/graph/adjacency_list.hpp>
boost:: adjacency_list <
   boost:: vecS ,
   boost:: vecS ,
   boost:: undirectedS ,
   boost:: no_property ,
   boost:: no_property ,
   boost:: property <
      boost:: graph_name_t , std:: string >
   create_empty_undirected_graph_with_graph_name() noexcept {
    return {};
}
```

This code is very similar to the code described in chapter 340, except that the directedness (the third template argument) is undirected (due to the boost::undirectedS).

 $Algorithm\ 343\ demonstrates\ the\ `create_empty_undirected_graph_with_graph_name'\ function.$

```
Algorithm 343 Demonstration of 'create_empty_undirected_graph_with_graph_name'
```

#include <cassert>

20.3 Get a graph its name property

Algorithm 344 Get a graph its name

```
#include <string>
#include <boost/graph/properties.hpp>

template <typename graph>
std::string get_graph_name(
    const graph& g
) noexcept
{
    return get_property(
        g, boost::graph_name
    );
}
```

Algorithm 345 demonstrates the 'get_graph_name' function.

Algorithm 345 Demonstration of 'get graph name'

```
#include <cassert>
#include "create_empty_directed_graph_with_graph_name.h"
#include "get_graph_name.h"

void get_graph_name_demo() noexcept
{
   auto g = create_empty_directed_graph_with_graph_name();
   const std::string name{"Dex"};
   set_graph_name(name, g);
   assert(get_graph_name(g) == name);
}
```

20.4 Set a graph its name property

Algorithm 346 Set a graph its name

```
#include <cassert>
#include <string>
#include <boost/graph/properties.hpp>

template <typename graph>
void set_graph_name(
    const std::string& name,
    graph& g
) noexcept
{
    static_assert(!std::is_const<graph>::value,
        "graph_cannot_be_const"
);
    get_property(g, boost::graph_name) = name;
}
```

Algorithm 347 demonstrates the 'set graph name' function.

Algorithm 347 Demonstration of 'set graph name'

```
#include <cassert>
#include "create_empty_directed_graph_with_graph_name.h"
#include "get_graph_name.h"
#include "set_graph_name.h"

void set_graph_name_demo() noexcept
{
   auto g = create_empty_directed_graph_with_graph_name();
   const std::string name{"Dex"};
   set_graph_name(name, g);
   assert(get_graph_name(g) == name);
}
```

20.5 Create a directed graph with a graph name property20.5.1 Graph

See figure 6.

20.5.2 Function to create such a graph

Algorithm 348 shows the function to create an empty directed graph with a graph name.

Algorithm 348 Creating a two-state Markov chain with a graph name

```
#include <cassert>
#include "create_empty_directed_graph_with_graph_name.h"
#include "set graph name.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::directedS,
  boost::no property,
  boost::no property,
  boost::property<boost::graph name t, std::string>
create markov chain with graph name() noexcept
  auto g = create_empty_directed_graph_with_graph_name();
  const auto vd a = boost::add vertex(g);
  const auto vd b = boost::add vertex(g);
  const auto aer aa = boost::add edge(vd a, vd a, g);
  assert (aer_aa.second);
  const auto aer ab = boost::add edge(vd a, vd b, g);
  assert (aer ab.second);
  const auto aer ba = boost::add edge(vd b, vd a, g);
  assert (aer_ba.second);
  const auto aer bb = boost::add edge(vd b, vd b, g);
  assert (aer bb.second);
  set graph name("Two-state_Markov_chain", g);
  return g;
}
```

20.5.3 Creating such a graph

Algorithm 349 demonstrates the 'create_markov_chain_with_graph_name' function.

Algorithm 349 Demonstration of 'create markov chain with graph name'

```
#include <cassert>
#include "create_markov_chain_with_graph_name.h"
#include "get_graph_name.h"

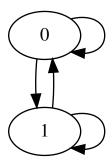
void create_markov_chain_with_graph_name_demo() noexcept
{
   const auto g = create_markov_chain_with_graph_name();
   assert(boost::num_vertices(g) == 2);
   assert(boost::num_edges(g) == 4);
   assert(get_graph_name(g) == "Two-state_Markov_chain");
}
```

20.5.4 The .dot file produced

Algorithm 350 .dot file created from the 'create_markov_chain_with_graph_name' function (algorithm 348), converted from graph to .dot file using algorithm 52

```
digraph G {
name="Two-state Markov chain";
0;
1;
0->0;
0->1;
1->0;
1->1;
```

20.5.5 The .svg file produced



20.6 Create an undirected graph with a graph name property

20.6.1 Graph

See figure 8.

20.6.2 Function to create such a graph

Algorithm 351 shows the function to create K2 graph with a graph name.

Algorithm 351 Creating a K2 graph with a graph name

```
#include "create empty undirected graph with graph name.h
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::no_property ,
  boost::no property,
  boost::property<br/>boost::graph name t, std::string>
create_k2_graph_with_graph_name() noexcept
  auto g = create_empty_undirected_graph_with_graph_name
      ();
  const auto vd a = boost::add vertex(g);
  const auto vd_b = boost::add_vertex(g);
  \mathbf{const} \ \mathbf{auto} \ \mathbf{aer} \ = \ \mathbf{boost} :: \mathbf{add\_edge}(\mathbf{vd\_a}, \ \mathbf{vd\_b}, \ \mathbf{g}) \, ;
  assert (aer.second);
  get property (g, boost::graph name) = "K2";
  return g;
```

20.6.3 Creating such a graph

Algorithm 352 demonstrates the 'create_k2_graph_with_graph_name' function.

Algorithm 352 Demonstration of 'create k2 graph with graph name'

```
#include <cassert>
#include "create_k2_graph_with_graph_name.h"
#include "get_graph_name.h"

void create_k2_graph_with_graph_name_demo() noexcept
{
   const auto g = create_k2_graph_with_graph_name();
   assert(boost::num_vertices(g) == 2);
   assert(boost::num_edges(g) == 1);
   assert(get_graph_name(g) == "K2");
}
```

20.6.4 The .dot file produced

Algorithm 353 .dot file created from the 'create_k2_graph_with_graph_name' function (algorithm 351), converted from graph to .dot file using algorithm 52

```
graph G {
name="K2";
0;
1;
0--1;
}
```

20.6.5 The .svg file produced

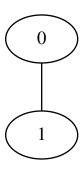


Figure 67: .svg file created from the 'create_k2_graph_with_graph_name' function (algorithm 351) its .dot file, converted from .dot file to .svg using algorithm 361

21 Working on graphs with a graph name

21.1 Storing a graph with a graph name property as a .dot file

This works:

```
Algorithm 354 Storing a graph with a graph name as a .dot file
```

```
#include < string>
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include <boost/graph/properties.hpp>
#include "get_graph_name.h"
template <typename graph>
void save graph with graph name to dot (
  const graph& g,
  const std::string& filename
)
{
  std::ofstream f(filename);
  boost::write graphviz(
    f,
    boost::default_writer(),
    boost::default writer(),
    //Unsure if this results in a graph
    //that can be loaded correctly
    //from\ a\ .dot\ file
    [g](std::ostream \& os) {
      os << "name=\""
        << get_graph_name(g)
        << "\";\n";
  );
```

21.2 Loading a directed graph with a graph name property from a .dot file

This will result in a directed graph with a name:

```
#include <fstream>
#include <boost/graph/graphviz.hpp>
#include "is regular file.h"
boost::adjacency list <
  boost::vecS,
  boost :: vecS,
  boost::directedS,
  boost::no property,
  boost::no property,
  boost::property<
    boost::graph_name_t, std::string
>
load directed graph with graph name from dot (
  const std::string& dot filename
  using graph = boost::adjacency_list<</pre>
    boost :: vecS,
    boost :: vecS,
    boost::directedS,
    boost::no property,
    boost::no property,
    boost::property<
      boost::graph name t, std::string
  assert (is regular file (dot filename));
  graph g;
  boost::ref_property_map<graph*,std::string>
  graph name{
    get_property(g,boost::graph_name)
  boost::dynamic properties dp{
    boost::ignore other properties
  dp.property("name", graph name);
  std::ifstream f(dot filename.c str());
  boost::read graphviz(f,g,dp);
  return g;
                             392
```

21.3 Loading an undirected graph with a graph name property from a .dot file

This will result in an undirected graph with a name:

Algorithm 356 Loading an undirected graph with a graph name from a .dot file

```
#include <fstream>
#include < string>
#include <boost/graph/graphviz.hpp>
#include "create_empty_undirected_graph_with_graph_name.h
#include "is regular file.h"
boost::adjacency list <
  boost :: vecS,
  boost :: vecS,
  boost::undirectedS,
  boost::no property,
  boost::no_property,
  boost::property<
    boost::graph name t, std::string
  >
load _ undirected _ graph _ with _ graph _ name _ from _ dot (
  const std::string& dot filename
{
  using graph = boost::adjacency list <</pre>
    boost :: vecS,
    boost :: vecS,
    boost::undirectedS,
    boost::no property,
    boost::no_property ,
    boost::property<
      boost::graph name t, std::string
    >
  >;
  assert (is regular file (dot filename));
  graph g;
  boost::ref property map<graph*,std::string>
  graph name{
    get_property(g,boost::graph_name)
  boost::dynamic_properties dp{
    boost::ignore other properties
  dp.property("name", graph name);
  std::ifstream f(dot filename.c str());
  boost::read graphviz(f,g,d9);
  return g;
```

22 Other graph functions

Some functions that did not fit in.

22.1 Encode a std::string to a Graphviz-friendly format

You may want to use a label with spaces, comma's and/or quotes. Saving and loading these, will result in problem. This function replaces these special characters by a rare combination of ordinary characters.

Algorithm 357 Encode a std::string to a Graphviz-friendly format

```
#include <boost/algorithm/string/replace.hpp>

std::string graphviz_encode(std::string s) noexcept
{
   boost::algorithm::replace_all(s,",",","$$$COMMA$$$");
   boost::algorithm::replace_all(s,",",","$$$SPACE$$$");
   boost::algorithm::replace_all(s,"\"","$$$QUOTE$$$");
   return s;
}
```

22.2 Decode a std::string from a Graphviz-friendly format

This function undoes the 'graphviz_encode' function (algorithm 357) and thus converts a Graphviz-friendly std::string to the original human-friendly std::string.

Algorithm 358 Decode a std::string from a Graphviz-friendly format to a human-friendly format

```
#include <boost/algorithm/string/replace.hpp>
std::string graphviz_decode(std::string s) noexcept
{
   boost::algorithm::replace_all(s,"$$$COMMA$$$",",");
   boost::algorithm::replace_all(s,"$$$SPACE$$$","\"");
   boost::algorithm::replace_all(s,"$$$QUOTE$$$","\"");
   return s;
}
```

22.3 Check if a std::string is Graphviz-friendly

There are pieces where I check if a std::string is Graphviz-friendly. This is done only where it matters. If it is tested not to matter, 'is_graphviz_friendly' is absent.

Algorithm 359 Check if a std::string is Graphviz-friendly

```
#include "graphviz_encode.h"
bool is_graphviz_friendly(const std::string& s) noexcept
{
   return graphviz_encode(s) == s;
}
```

23 Misc functions

These are some function I needed for creating this tutorial. Although they are not important for working with graphs, I used these heavily. These functions may be compiler-dependent, platform-dependent and/or there may be superior alternatives. I just add them for completeness.

23.1 Getting a data type as a std::string

This function will only work under GCC. I found this code at: http://stackoverflow.com/questions/1055452/c-get-name-of-type-in-template. Thanks to 'mdudley' (Stack Overflow userpage at http://stackoverflow.com/users/111327/m-dudley).

Algorithm 360 Getting a data type its name as a std::string

```
#include < c stdlib >
#include < string>
#include <typeinfo>
#include < cxxabi.h>
template<typename T>
std::string get type name() noexcept
  std::string tname = typeid(T).name();
  int status = -1;
  char * const demangled name{
    abi::__cxa_demangle(
      tname.c_str(), NULL, NULL, &status
  };
  if(status = 0) {
    tname = demangled name;
    std::free(demangled name);
  return tname;
```

23.2 Convert a .dot to .svg

All illustrations in this tutorial are created by converting .dot to a .svg ('Scalable Vector Graphic') file. This function assumes the program 'dot' is installed, which is part of Graphviz.

Algorithm 361 Convert a .dot file to a .svg

```
#include <cassert>
#include < string>
#include <sstream>
#include "has dot.h"
#include "is_regular_file.h"
#include "is_valid_dot_file.h"
void convert_dot_to_svg(
   const std::string& dot filename,
  const std::string& svg filename
   assert (has dot());
   assert(is_valid_dot_file(dot_filename));
   std::stringstream cmd;
  \operatorname{cmd} << \operatorname{"dot}_{\smile} - \operatorname{Tsvg}_{\smile} = << \operatorname{dot} \operatorname{filename} << \operatorname{"}_{\smile} - \operatorname{o}_{\smile} = <<
       svg_filename;
  const int error {
     std::system(cmd.str().c_str())
   };
   assert (!error);
   assert(is_regular_file(svg_filename));
```

'convert_dot_to_svg' makes a system call to the prgram 'dot' to convert the .dot file to an .svg file.

23.3 Check if a file exists

Not the most smart way perhaps, but it does only use the STL.

Algorithm 362 Check if a file exists

24 Errors

Some common errors.

24.1 Formed reference to void

This compile-time error occurs when you create a graph without a certain property, then subsequently reading that property, as in algorithm 363:

Algorithm 363 Creating the error 'formed reference to void'

```
#include "create_k2_graph.h"
#include "get_vertex_names.h"

void formed_reference_to_void() noexcept
{
    get_vertex_names(create_k2_graph());
}
```

In algorithm 363 a graph is created with vertices of no properties. Then the names of these vertices, which do not exists, are tried to be read. If you want to read the names of the vertices, supply a graph that has this property.

24.2 No matching function for call to 'clear out edges'

This compile-time error occurs when you want to clear the outward edges from a vertex in an undirected graph.

Algorithm 364 Creating the error 'no matching function for call to clear out edges'

```
#include "create_k2_graph.h"

void no_matching_function_for_call_to_clear_out_edges()
    noexcept
{
    auto g = create_k2_graph();
    const auto vd = *vertices(g).first;
    boost::clear_in_edges(vd,g);
}
```

In algorithm 364 an undirected graph is created, a vertex descriptor is obtained, then its out edges are tried to be cleared. Either use a directed graph (which has out edges), or use the 'boost::clear vertex' function instead.

24.3 No matching function for call to 'clear_in_edges'

See chapter 24.2.

${\bf 24.4} \quad {\bf Undefined\ reference\ to\ boost:: detail::graph::read_graphviz_new}$

You will have to link against the Boost.Graph and Boost.Regex libraries. In Qt Creator, this is achieved by adding these lines to your Qt Creator project file:

 $LIBS \hspace{0.1cm} +\!\!= -lboost_graph \hspace{0.1cm} -lboost_regex$

24.5 Property not found: node id

When loading a graph from file (as in chapter 3.11) you will be using boost::read_graphviz. boost::read_graphviz needs a third argument, of type boost::dynamic_properties. When a graph does not have properties, do not use a default constructed version, but initializate with 'boost::ignore_other_properties' as a constructor argument instead. Algorithm 365 shows how to trigger this run-time error.

Algorithm 365 Creating the error 'Property not found: node_id'

```
#include <cassert>
#include <fstream>
#include "is_regular_file.h"
#include "create empty undirected graph.h"
#include "create k2 graph.h"
#include "save_graph_to_dot.h"
void property_not_found_node_id() noexcept
  const std::string dot filename{"
     property_not_found_node_id.dot"};
  //Create a file
    const auto g = create k2 graph();
    save graph to dot(g, dot filename);
    assert (is regular file (dot filename));
  //Try to read that file
  std::ifstream f(dot_filename.c_str());
  auto g = create_empty_undirected_graph();
  //Line\ below\ should\ have\ been
  // boost:: dynamic\_properties dp(boost::
     ignore\_other\_properties);
  boost::dynamic properties dp; //Error
  try {
    boost::read graphviz(f,g,dp);
  catch (std::exception&) {
    return; //Should get here
  assert (!"Should_not_get_here");
```

24.6 Stream zeroes

```
When loading a graph from a .dot file, in operator>>, I encountered reading zeroes, where I expected an XML formatted string:

std::istream& ribi::cmap::operator>>(std::istream& is, my_class& any_class) noex
{

std::string s;
```

```
is >> s; //s has an XML format
  assert(s != "0");
  any class = my \ class(s);
  return is;
}
  This was because I misconfigured the reader. I did (heavily simplified code):
graph load from dot(const std::string& dot filename)
  std::ifstream f(dot filename.c str());
  graph g;
  boost::dynamic properties dp;
  dp.property("node_id", get(boost::vertex_custom_type, g));
  dp.property("label", get(boost::vertex custom type, g));
  boost::read_graphviz(f,g,dp);
  return g;
}
  Where it should have been:
graph load from dot(const std::string& dot filename)
  std::ifstream f(dot filename.c str());
  graph g;
  boost::dynamic_properties dp(boost::ignore_other_properties);
  dp.property("label", get(boost::vertex custom type, g));
  boost::read_graphviz(f,g,dp);
  return g;
}
  The explanation is that by setting the boost::dynamic property 'node id'
to 'boost::vertex custom type', operator>> will receive the node indices.
  An alternative, but less clean solution, is to let operator>> ignore the node
indices:
std::istream& ribi::cmap::operator>>(std::istream& is, my_class& any_class) noex
  std::string s;
  is >> s; //s has an XML format
  if (!is xml(s)) { //Ignore node index
    any_class_class = my_class();
    any_class_class = my_class(s);
  return is;
}
```

25 Appendix

25.1 List of all edge, graph and vertex properties

The following list is obtained from the file 'boost/graph/properties.hpp'.

Edge	Graph	Vertex
edge all	graph_all	vertex all
edge_bundle	graph bundle	vertex bundle
edge_capacity	graph_name	vertex centrality
edge_centrality	graph visitor	vertex color
edge color		vertex current degree
edge_discover_time		vertex_degree
$edge_finished$		vertex_discover_time
edge_flow		$vertex_distance$
$edge_global$		$vertex_distance2$
$edge_index$		$vertex_finish_time$
$edge_local$		$vertex_global$
edge_local_index		vertex_in_degree
edge_name		vertex_index
$edge_owner$		$vertex_index1$
edge_residual_capacity		${ m vertex_index2}$
$edge_reverse$		vertex_local
$edge_underlying$		vertex_local_index
edge_update		vertex_lowpoint
$edge_weight$		$vertex_name$
$edge_weight2$		$vertex_out_degree$
		$vertex_owner$
		${ m vertex_potential}$
		$vertex_predecessor$
		vertex_priority
		vertex_rank
		vertex_root
		vertex_underlying
		$vertex_update$

25.2 Graphviz attributes

List created from www.graphviz.org/content/attrs, where only the attributes that are supported by all formats are listed:

Edge	Graph	Vertex
arrowhead	background	color
arrowsize	bgcolor	colorscheme
arrowtail	center	$\operatorname{comment}$
color	$\operatorname{charset}$	distortion
colorscheme	color	fillcolor
comment	colorscheme	fixedsize
decorate	comment	fontcolor
dir	concentrate	fontname
fillcolor	fillcolor	fontsize
fontcolor	fontcolor	gradientangle
fontname	fontname	height
fontsize	fontpath	image
gradientangle	fontsize	imagescale
headclip	forcelabels	label
headlabel	gradientangle	labelloc
headport	imagepath	layer
label	label	margin
labelangle	labeljust	nojustify
labeldistance	labelloc	orientation
labelfloat	landscape	penwidth
labelfontcolor	layerlistsep	peripheries
labelfontname	layers	pos
labelfontsize	layerselect	regular
layer	layersep	sample points
nojustify	layout	$_{ m shape}$
penwidth	margin	shapefile
pos	$\operatorname{nodesep}$	sides
style	nojustify	skew
tailclip	orientation	sortv
taillabel	outputorder	style
tailport	pack	width
weight	packmode	xlabel
xlabel	pad	Z
	page	
	pagedir	
	penwidth	
	quantum	
	ratio	
	rotate	
	size	
	sortv	
	splines	
	style	
	viewport	

References

- [1] Eckel Bruce. Thinking in c++, volume 1. 2002.
- [2] Marshall P Cline, Greg Lomow, and Mike Girou. C++ FAQs. Pearson Education, 1998.
- [3] Jarrod Hollingworth, Bob Swart, and Jamie Allsop. C++ Builder 5 Developer's Guide with Cdrom. Sams, 2000.
- [4] John Lakos. Large-scale C++ software design, volume 10. Addison-Wesley Reading, 1996.
- [5] Jesse Liberty. Sams teach yourself C++ in 24 hours. Sams Publishing, 2001.
- [6] Steve McConnell. Code complete. Pearson Education, 2004.
- [7] Scott Meyers. Effective C++: 55 specific ways to improve your programs and designs. Pearson Education, 2005.
- [8] Jeremy G Siek, Lie-Quan Lee, and Andrew Lumsdaine. Boost Graph Library: User Guide and Reference Manual, The. Pearson Education, 2001.
- [9] Bjarne Stroustrup. The C++ Programming Language (3rd edition). 1997.
- [10] Bjarne Stroustrup. The C++ Programming Language (4th edition). 2013.
- [11] Herb Sutter and Andrei Alexandrescu. C++ coding standards: 101 rules, guidelines, and best practices. Pearson Education, 2004.

Index

$\# { m include},\ 19$ $K_2 { m with\ named\ edges\ and\ vertices,\ create,\ 138}$	boost::adjacency_matrix, 20 boost::clear_in_edges, 103 boost::clear_out_edges, 102
K_2 with named vertices, create, 78	boost::clear_vertex, 102
K_2 , create, 36	boost::degree does not exist, 50
K_3 with named edges and vertices, create, 142	boost::directedS, 21, 70, 128, 177, 242, 382
K_3 , create, 39	boost::dynamic_properties, 65, 123, 171,
K_3 with named vertices, create, 81	$202,\ 234,\ 277,\ 309,\ 347,\ 376,$
'demo' function, 12	400
'do' function, 12	boost::edge does not exist, 52
[[:SPACE:]], 249, 250	boost::edge_bundled_type_t, 208
Add a grant are 24	boost::edge_custom_type, 321
Add an edge 28	boost::edge_custom_type_t, 317
Add hundled edge 211	boost::edge_name_t, 128, 129
Add bundled edge, 211 Add bundled vertex, 178	boost::edges does not exist, 30–32
Add custom and selectable edge, 357	boost::get does not exist, 13, 72, 102
Add custom and selectable edge, 337 Add custom and selectable vertex, 286	boost::graph_name, 382
Add custom edge, 321	boost::graph_name_t, 382
Add custom vertex, 244	boost::ignore_other_properties, 65, 400
Add edge between custom vertices, 266	boost::in_degree does not exist, 50
Add edge between named vertices, 106	boost::isomorphism, 117, 273 boost::make label writer, 120
Add edge between selected vertices, 298	boost::no property, 382
Add named edge, 130, 131	boost::num_edges, 23
Add named edge between vertices, 132	boost::num_eages, 25 boost::num_vertices, 22
Add named vertex, 71, 72	boost::out_degree does not exist, 50
Add vertex, 24	boost::property, 70, 128, 129, 208, 242,
add edge, 29	317, 382
aer, 30	boost::put does not exist, 72, 102
All edge properties, 403	boost::read graphviz, 65, 123, 171, 202,
All graph properties, 403	234, 277, 348, 400
All vertex properties, 403	boost::remove_edge, 107, 161
Alternative syntax for put, 73	boost::remove_vertex, 104
assert, 22, 29	boost::undirectedS, 21, 71, 129, 178,
auto, 20	209, 243, 284, 319, 355, 383
1	boost::vecS, 21, 69, 127, 129, 177, 242,
boost::add_edge, 28, 29, 34, 37, 105,	382
131, 266, 297	boost::vertex_custom_type, 245
boost::add_edge result, 30	boost::vertex_custom_type_t, 242
boost::add_vertex, 24, 34, 37	boost::vertex_name, 72
boost::adjacency_list, 20, 70, 128, 129,	$boost::vertex_name_t,\ 70,\ 128,\ 129$
242	

57 boost::write graphviz, 64, 120 Create an empty directed graph, 19 BOOST INSTALL PROPERTY, 241, Create an empty directed graph with 281, 316, 352 named edges and vertices, 127 bundled vertices writer, 199 Create an empty directed graph with named vertices, 69 Clear first vertex with name, 103 Create an empty graph, 20 const, 20 Create an empty graph with named edges const-correctness, 20 and vertices, 129 Convert dot to svg, 398 Create an empty undirected graph with Count connected components, 60, 62 named vertices, 70 Count edges with selectedness, 339 Create bundled edges and vertices K3 Count vertices with selectedness, 296 graph, 221 Counting the number of edges, 23 Create bundled edges and vertices Markov Counting the number of vertices, 22 chain, 215 Create K_2 , 36 Create bundled vertices K2 graph, 186 Create K_2 graph, 37 Create bundled vertices Markov chain, Create K_2 with named edges and ver-181 tices, 138 Create custom and selectable edges and Create K_2 with named vertices, 78 vertices K2 graph, 366 Create K_3 , 39 Create custom and selectable edges and Create K_3 graph, 40 vertices Markov chain, 360 Create K_3 with named edges and ver-Create custom and selectable vertices tices, 142 K2 graph, 293 Create K_3 with named vertices, 81 Create custom and selectable vertices Create .dot from graph, 63 Markov chain, 289 Create .dot from graph with bundled Create custom edges and vertices K3 edges and vertices, 231 graph, 328 Create .dot from graph with custom Create custom edges and vertices Markov edges and vertices, 345 chain, 325 Create .dot from graph with named edges Create custom vertices K2 graph, 251 and vertices, 168 Create custom vertices Markov chain, Create .dot from graph with named ver-248 tices, 119 Create custom vertices path graph, 254 Create all direct-neighbour custom and Create direct-neighbour custom and seselectable edges and vertices lectable edges and vertices subsubgraphs, 372 graph, 370 Create all direct-neighbour custom edges Create direct-neighbour custom and seand vertices subgraphs, 343 lectable vertices subgraph, 300 Create all direct-neighbour custom ver-Create direct-neighbour custom edges tices subgraphs, 270, 302 and vertices subgraph, 341 Create all direct-neighbour named edges Create direct-neighbour custom vertices and vertices subgraphs, 166 subgraph, 268

boost::vertices does not exist, 26, 28,

Create all direct-neighbour subgraphs,

Create direct-neighbour named edges

and vertices subgraph, 164

Create all direct-neighbour named ver-

tices subgraphs, 114

subgraph, 112 Create direct-neighbour subgraph, 55 Create directed graph, 33 Create directed graph from .dot, 64 Create directed graph with named edges and vertices from .dot, 170 Create directed graph with named vertices from .dot, 122 Create empty directed bundled edges and vertices graph, 208 Create empty directed bundled vertices graph, 177 Create empty directed custom and selectable edges and vertices graph, Create empty directed custom and selectable vertices graph, 282 Create empty directed custom edges and vertices graph, 317 Create empty directed custom vertices graph, 242 Create empty directed graph, 19 Create empty directed graph with graph Create named vertices K2 graph, 79 name, 381 Create empty directed named edges and vertices graph, 127 Create empty directed named vertices graph, 69 Create empty undirected bundled edges and vertices graph, 209 Create empty undirected bundled vertices graph, 178 Create empty undirected custom and selectable edges and vertices graph, 355 Create empty undirected custom and selectable vertices graph, 284 Create empty undirected custom edges and vertices graph, 319 Create empty undirected custom vertices graph, 243 Create empty undirected graph, 21

Create empty undirected graph with

graph name, 383

Create direct-neighbour named vertices

Create empty undirected named edges and vertices graph, 129 Create empty undirected named vertices graph, 71 Create K2 graph with graph name, 389 Create K3 vertices path graph, 82 Create Markov chain, 34 Create Markov chain with graph name, Create Markov chain with named edges and vertices, 135 Create Markov chain with named vertices, 75 Create named edges and vertices K_2 graph, 140 Create named edges and vertices K3 graph, 143 Create named edges and vertices Markov chain, 136 Create named edges and vertices path graph, 147 Create named edges and vertices Petersen graph, 151 Create named vertices Markov chain, Create named vertices path graph, 85 Create named vertices Petersen graph, 89 Create path graph, 41, 42 Create path graph with custom vertices, 253 Create path graph with named edges and vertices, 145 Create path graph with named vertices, 84 Create Petersen graph, 44, 46 Create Petersen graph with named vertices, 87, 149 Create undirected graph from .dot, 66 Create undirected graph with bundled edges and vertices from .dot, 236 Create undirected graph with custom

edges and vertices from .dot,

349

```
Create undirected graph with named
                                                                              Find first edge by name, 157
                  vertices from .dot, 124
                                                                               Find first vertex with name, 95, 110
custom and selectable vertices writerFormed reference to void, 399
                  307
                                                                               get, 13, 72, 102, 245, 321
custom vertex invariant, 273
                                                                               Get bundled vertex my bundled vertex,
Declaration, my bundled edge, 207
                                                                                                 194
Declaration, my bundled vertex, 176
                                                                               Get bundled vertex my vertexes, 179
Declaration, my custom edge, 315
                                                                               Get custom edge my custom edge, 335
Declaration, my custom vertex, 240
                                                                               Get custom vertex my custom vertex
decltype, 261
                                                                                                 objects, 247
decltype(auto), 13
                                                                               Get edge between vertices, 53
directed graph, 15
                                                                               Get edge descriptors, 32
Directed graph, create, 33
                                                                               Get edge iterators, 31
                                                                               Get edge my_bundled_edges, 213
ed , 32
                                                                               Get edge my custom edges, 323
edge, 52
                                                                               Get edge name, 158
Edge descriptor, 31
                                                                               Get first vertex with name out degree,
Edge descriptors, get, 32
                                                                                                 97
Edge iterator, 30
                                                                               Get graph name, 384
Edge iterator pair, 30
                                                                               Get my bundled edge, 228
Edge properties, 403
                                                                               Get my custom vertex, 261
Edge, add, 28
                                                                               Get my custom vertexes, 246
edge is selected, 352
                                                                               Get n edges, 23
edge is selected t, 352
                                                                               Get n vertices, 22
edges, 30, 32
                                                                               Get type name, 397
Edges, counting, 23
                                                                               Get vertex descriptors, 27
eip , 30
                                                                               Get vertex iterators, 26
Empty directed graph with named edges
                                                                               Get vertex name, 99
                  and vertices, create, 127
                                                                               Get vertex names, 74
Empty directed graph with named ver-
                                                                               Get vertex out degrees, 50
                  tices, create, 69
                                                                               Get vertices, 26
Empty directed graph, create, 19
                                                                               get edge names, 134
Empty graph with named edges and
                                                                               Graph properties, 403
                  vertices, create, 129
                                                                               Graphviz, 63
Empty graph, create, 20
                                                                               graphviz decode, 395
Empty undirected graph with named
                                                                               graphviz encode, 395
                  vertices, create, 70
Find first \ bundled \ edge \ with \ my\_bundled \ edge, \\ bundled \ edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge \ with \ my\_bundled\_edge, \\ as bundled \ edge, \\ as bundled \ edge \ with \ edge \ edge, \\ as bundled \ edge \
\label{lem:condition} Find first \ bundled \ vertex \ with \ my\_vertex, \\ \\ Has \ bundled \ vertex \ with \ my\_vertex, \\ \\
Find first custom edge with my_custom_edge, ustom vertex with my_vertex, 257 \,
                                                                               Has edge between vertices, 52
Find first custom vertex with my_vertex, Has edge with my_custom_edge, 331
                                                                               Has edge with name, 155
                  259
```

Has vertex with name, 94 Load undirected graph with bundled header file, 19 edges and vertices from .dot, 236 idegree, 50 Load undirected graph with custom edges in degree, 50 and vertices from .dot, 349 Install edge custom type, 316 Load undirected graph with named ver-Install edge is selected, 352 tices from .dot, 124 Install vertex custom type, 241 Load undirected named edges and ver-Install vertex is selected, 281 tices graph from dot, 173 Is isomorphic, 58, 118, 274 Load undirected named vertices graph Is regular file, 398 from dot, 125 is graphviz friendly, 396 m , 176, 207, 240, 315 link, 400 macro, 241, 281, 316, 352 Load directed bundled edges and vermake bundled vertices writer, 198 tices graph from dot, 233 make custom and selectable vertices writer, Load directed bundled vertices graph from dot, 201 Markov chain with named edges and Load directed custom and selectable vertices, create, 135 edges and vertices graph from Markov chain with named vertices, credot, 376 ate, 75 Load directed custom edges and vermember, 176, 207, 240, 315 tices graph from dot, 347, 392 my bundled edge, 207 Load directed custom vertices graph my bundled edge declaration, 207 from dot, 277, 309 my bundled edge.h, 207 Load directed graph from .dot, 64 my_bundled_vertex, 176, 177 Load directed graph from dot, 65 my bundled vertex.h, 176 Load directed graph with named edges my custom edge, 315 and vertices from .dot, 170 my custom edge declaration, 315 Load directed graph with named ver $my_custom_edge.h,\,315$ tices from .dot, 122 my custom vertex, 240 Load directed named edges and vermy custom vertex declaration, 240 tices graph from dot, 170 my custom vertex.h, 240 Load directed named vertices graph from my edge, 208, 317 dot, 123 my vertex, 242 Load undirected bundled edges and vermy vertex declaration, 176 tices graph from dot, 237 Load undirected bundled vertices graph Named edge, add, 130 from dot, 204 Named edge, add between vertices, 132 Load undirected custom edges and ver-Named edges and vertices, create empty directed graph, 127 tices graph from dot, 350, 394 Load undirected custom vertices graph Named edges and vertices, create empty from dot, 279, 312, 379 graph, 129 Load undirected graph from .dot, 66 Named vertex, add, 71 Load undirected graph from dot, 67 Named vertices, create empty directed

graph, 69

Named vertices, create empty undirected	1 Save graph as dot 63
graph, 70	Save graph as .dot, 63
named vertex invariant, 117	Save graph with bundled edges and ver-
No matching function for call to clear o	
399	Save graph with custom edges and ver-
node id, 400	tices as .dot, 345
noexcept, 19	Save graph with graph name to dot, 391
noexcept specification, 19	Save graph with name edges and ver-
Number of edges, get, 23	
Number of vertices, get, 22	tices as .dot, 168 Save graph with named vertices as .dot,
operator <, 272	119
out degree, 50	
	Save named edges and vertices graph
Path graph with custom vertices, cre-	to dot, 169
${ m ate,\ 253}$	Save named vertices graph to dot, 120
Path graph with named edges and ver-	Save named vertices graph to dot using
tices, create, 145	lambda function, 121
Path graph with named vertices, cre-	Set bundled edge my_bundled_edge,
ate, 84	230
Path graph, create, 41	Set bundled vertex my_bundled_vertexes, 197
Petersen graph with named vertices,	 -
create, 87, 149	Set edge name, 160
Petersen graph, create, 44	Set graph name, 385
Property not found: node_id, 400, 401	Set my_custom_edge, 337
Property not found, 400	Set my_custom_vertex, 263
put, 72, 102	Set my_custom_vertexes, 265
put, alternative syntax, 73	Set vertex name 100
	Set vertex name, 100
read_graphviz_new, 400	Set vertex names, 101
read_graphviz_new, undefined refer-	Set vertices names, 101
ence, 400	static_assert, 24, 72
Remove edge between vertices with names static cast, 22	
108	std::copy, 28
Remove first edge with name, 162	std::count_if, 110, 296, 339
Remove first vertex with name, 104	std::cout, 64
C 91 999	std::ifstream, 65
S, 21, 382	std::list, 20
Save bundled edges and vertices graph	std::ofstream, 64
to dot, 232	std::pair, 29
Save bundled vertices graph to dot, 198	std::vector, 20
Save custom and selectable edges and	STL, 20
vertices graph to dot, 375	Undefined reference to read graphviz new,
Save custom edges and vertices graph	400
to dot, 346	undirected graph, 15
Save custom vertices graph to dot, 276,	unsigned long, 22
305	unoi 81100 10118, 22

vd, 29vd , 25 Vertex descriptor, 25, 28Vertex descriptors, get, 27 Vertex iterator, 26Vertex iterator pair, 26 $Vertex\ iterators,\ get,\ 26$ Vertex properties, 403 Vertex, add, 24 Vertex, add named, 71 $vertex_custom_type,\ 239$ $vertex_is_selected,\,281$ $vertex_is_selected_t, 281$ vertices, 26, 28 Vertices, counting, 22 Vertices, set names, 101 $\mathrm{vip}_-,\,26$