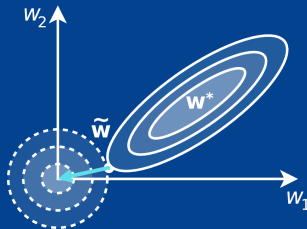




Lesson 09: Regularization, Optimization and Searching

CARSTEN EIE FRIGAARD

AUTUMN 2022



Agenda

- ▶ **Resumé: ML Algorithm and Model Selection:**
k-fold Cross-Validation revisited,
- ▶ **Regularization:**
Regularizers,
Exercise: `L09/regulizers.ipynb`
- ▶ **Optimizers:**
(no exercise).
- ▶ **Searching:**
Gridsearch,
Randomsearch,
Exercise: `09/gridsearch.ipynb`

ML Algorithm Selection and Model Selection

Manually Choosing an Algorithm and Tuning a Model..

- ▶ algorithm selection.

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- ▶ algorithm selection.
- ▶ model selection,
- ▶ model evaluation,

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Model Evaluation, Model Selection, and Algorithm Selection in Machine Learning

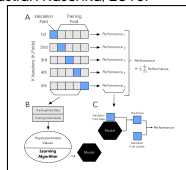
Sebastian Raschka
University of Wisconsin-Madison
Department of Statistics
November 2018
sebastian@stat.wisc.edu

Abstract

The correct use of model evaluation, model selection, and algorithm selection techniques is vital in academic machine learning research as well as in many industrial settings. This article reviews different techniques that can be used for each of these three subtasks and discusses the main advantages and disadvantages of each technique with references to theoretical and empirical studies. Further recommendations are given to encourage best yet feasible practices in research and applications of machine learning. Common methods such as the holdout method for model evaluation and selection are covered, which are not recommended when working with small datasets. Different flavors of the bootstrap technique are introduced for estimating the uncertainty of performance estimates, as an alternative to confidence intervals via normal approximation if bootstrapping is computationally feasible. Common cross-validation techniques such as leave-one-out cross-validation and k-fold cross-validation are reviewed, the bias-variance trade-off for choosing k is discussed, and practical tips for the optimal choice of k are given based on empirical evidence. Different statistical tests for algorithm comparisons are presented, and strategies for dealing with multiple comparisons such as omnibus tests and multiple comparison corrections are discussed. Finally, alternative methods for algorithm selection, such as the combined k -test \times k -fold cross-validation and nested cross-validation, are recommended for comparing machine learning algorithms when datasets are small.

arXiv:1811.12808v2 [cs.LG] 3 Dec 2018

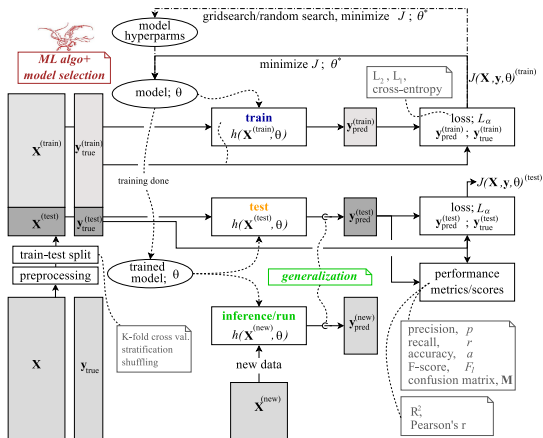
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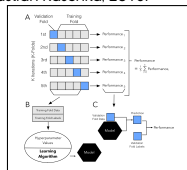
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- ▶ model evaluation:
 - ▶ the performance metric score function,
 - ▶ how do you evaluate **generalization** performance?
 - ▶ holdout method (train-test split) and *k*-fold CV,
 - ▶ three-way split (train-validate-test split)..



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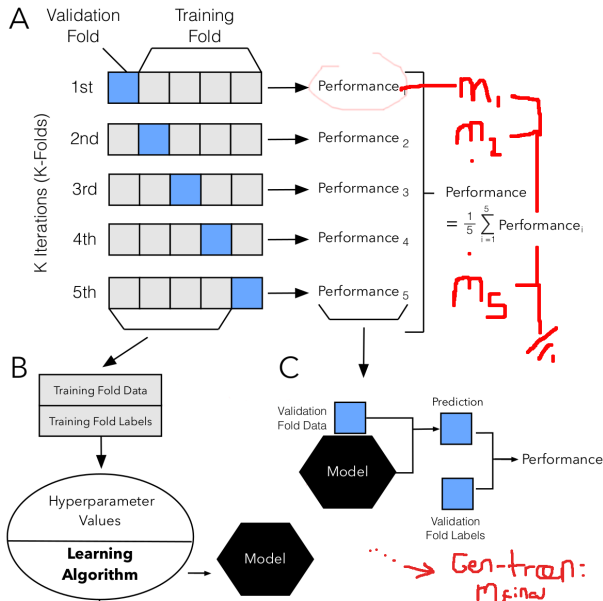
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 - ▶ three-way split (train-validate-test split)..
- ▶ **re-iteration and re-selection!**



NOTE: Model selection: ~ selection the best capacity/hyperparameter for a given model—NOT choosing the ML algo/model itself!

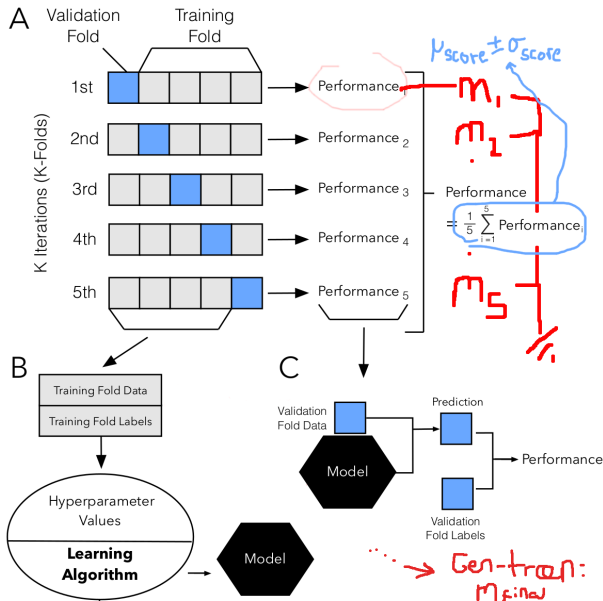
Model Evaluation

k-fold Cross-Validation Procedure, for *k*=5..

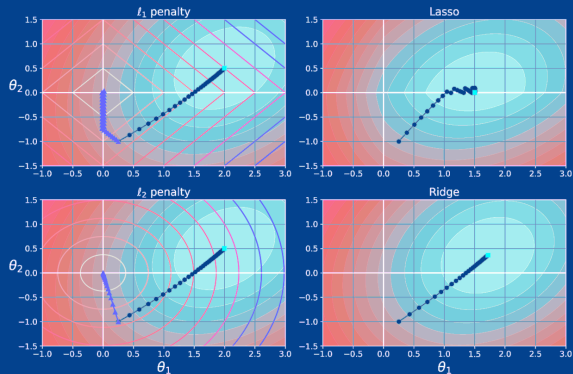


Model Evaluation

k-fold Cross-Validation Procedure, for $k=5$..



REGULARIZATION



Regularization

Adding a Penalty to the Cost Function

For a linear regressor, our cost function was

$$J(\mathbf{X}, \mathbf{y}; \mathbf{w}) = ||\mathbf{X}\mathbf{w} - \mathbf{y}||_2^2 \propto \text{MSE}(\mathbf{X}, \mathbf{y}; \mathbf{w})$$

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But now enters a **penalty factor**, Ω , that scaled with α adds extra cost to J ,

$$\tilde{J}(\mathbf{X}, \mathbf{y}; \mathbf{w}) = \|\mathbf{X}\mathbf{w} - \mathbf{y}\|_2^2 + \alpha\Omega(\mathbf{w})$$

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The effect of the added penalty is to:

- ▶ put a **constraint** on the norm of the weights, \mathbf{w} , disallowing 'em to grow wildly,
- ▶ leading to **reduced overfitting**, disabling the model to learn the background noise in the data.

\mathcal{L}_2 Regularization

Ridge Penalization

Aka Weight Decay, aka Tikhonov regularization

$$\Omega(\mathbf{w}) = \|\mathbf{w}\|_2^2 = \mathbf{w}^\top \mathbf{w}$$

$$\tilde{J}_{\text{ridge}}(\mathbf{X}, \mathbf{y}; \mathbf{w}) = J(\mathbf{X}, \mathbf{y}; \mathbf{w}) + \alpha \mathbf{w}^\top \mathbf{w}$$

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with $\mathbf{w} = [w_1 \ w_2 \ \cdots \ w_n]^\top$ without the bias element w_0 in the regularizer term, Ω , and recalling the Euclidean norm

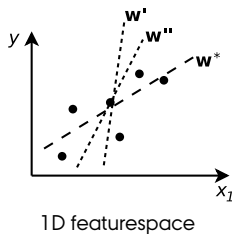
$$\mathcal{L}_2^2 : \|\mathbf{x}\|_2^2 = \mathbf{x}^\top \mathbf{x}$$

NOTE: ..and give-or-take some additional $1/2$ or $1/n$ constant, that we do not care about.

\mathcal{L}_2 Regularization

Ridge Penalization

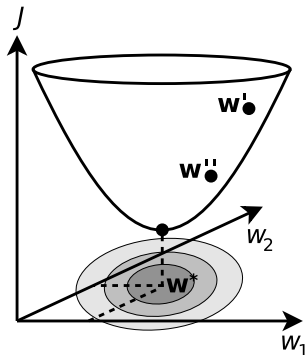
A graphical view for a linear regressor



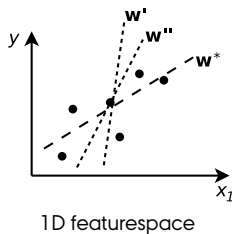
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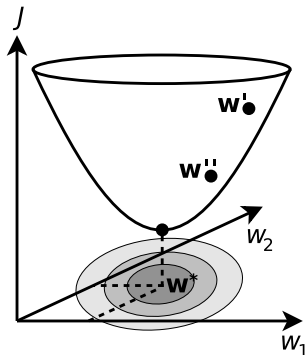
3D: ideal convex loss in $J - \mathbf{w}$ space.



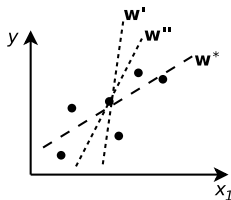
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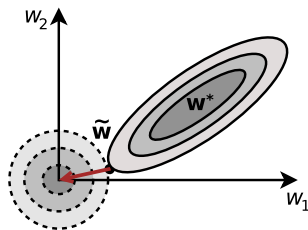
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1D featurespace

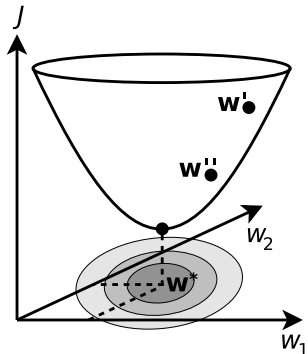


2D: flat $w_2 - w_1$ view with some feature scaling.

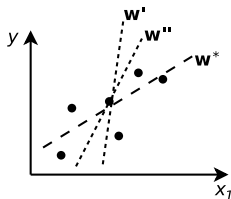
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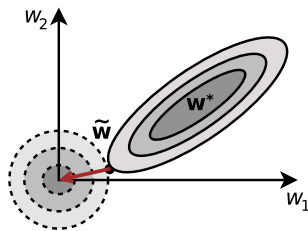
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1D featurespace



2D: flat $w_2 - w_1$ view with some feature scaling.

The tug-of-war: what happens with \tilde{w} ,
if w^* is far from the origin $[w_1, w_2] = (0, 0)$?

\mathcal{L}_1 Regularization

Lasso penalization

Now, just replace the \mathcal{L}_2 with \mathcal{L}_1 and we have the Lasso regularizer

$$\Omega(\mathbf{w}) = \|\mathbf{w}\|_1$$

$$\tilde{J}_{\text{lasso}}(\mathbf{X}, \mathbf{y}; \mathbf{w}) = J(\mathbf{X}, \mathbf{y}; \mathbf{w}) + \alpha \|\mathbf{w}\|_1$$

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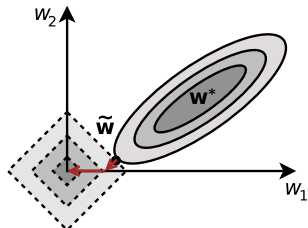
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with the Manhattan norm

$$\mathcal{L}_1 : \|\mathbf{x}\|_1 = \sum_{i=1}^n \text{abs}(x_i)$$

and the \mathcal{L}_1 penalty tends to drive weights to zero:

- ▶ automatic feature selection,
- ▶ outputs a sparse model,
- ▶ i.e few nonzero w 's.



\mathcal{L}_1 and \mathcal{L}_2 Regularization

Elastic-net Penalization

And finally a combination of the two: an Elastic-net regularizer

$$\Omega(\mathbf{w}) = \beta \|\mathbf{w}\|_1 + (1 - \beta) \|\mathbf{w}\|_2^2$$

$$\tilde{J}_{\text{elastic}}(\mathbf{X}, \mathbf{y}; \mathbf{w}) = J(\mathbf{X}, \mathbf{y}; \mathbf{w}) + \alpha (\beta \|\mathbf{w}\|_1 + (1 - \beta) \|\mathbf{w}\|_2^2)$$

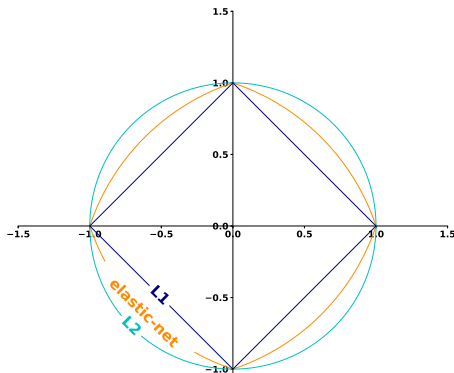
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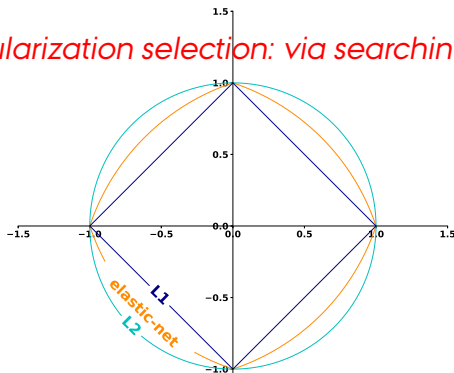
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Regularization selection: via searching..



HOML Fig 4-19 Explained

You can get a sense of why this is the case by looking at Figure 4-19: on the top-left plot, the background contours (ellipses) represent an unregularized MSE cost function ($\alpha = 0$), and the white circles show the Batch Gradient Descent path with that cost function. The foreground contours (diamonds) represent the ℓ_1 penalty, and the triangles show the BGD path for this penalty only ($\alpha \rightarrow \infty$). Notice how the path first reaches $\theta_1 = 0$, then rolls down a gutter until it reaches $\theta_2 = 0$. On the top-right plot, the contours represent the same cost function plus an ℓ_1 penalty with $\alpha = 0.5$. The global minimum is on the $\theta_2 = 0$ axis. BGD first reaches $\theta_2 = 0$, then rolls down the gutter until it reaches the global minimum. The two bottom plots show the same thing but uses an ℓ_2 penalty instead. The regularized minimum is closer to $\theta = \mathbf{0}$ than the unregularized minimum, but the weights do not get fully eliminated.

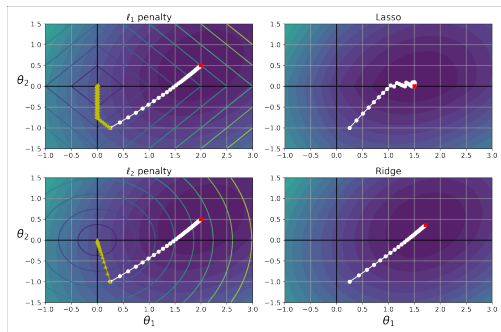


Figure 4-19. Lasso versus Ridge regularization



On the Lasso cost function, the BGD path tends to bounce across the gutter toward the end. This is because the slope changes abruptly at $\theta_2 = 0$. You need to gradually reduce the learning rate in order to actually converge to the global minimum.

HOML fig 4-19 Explained

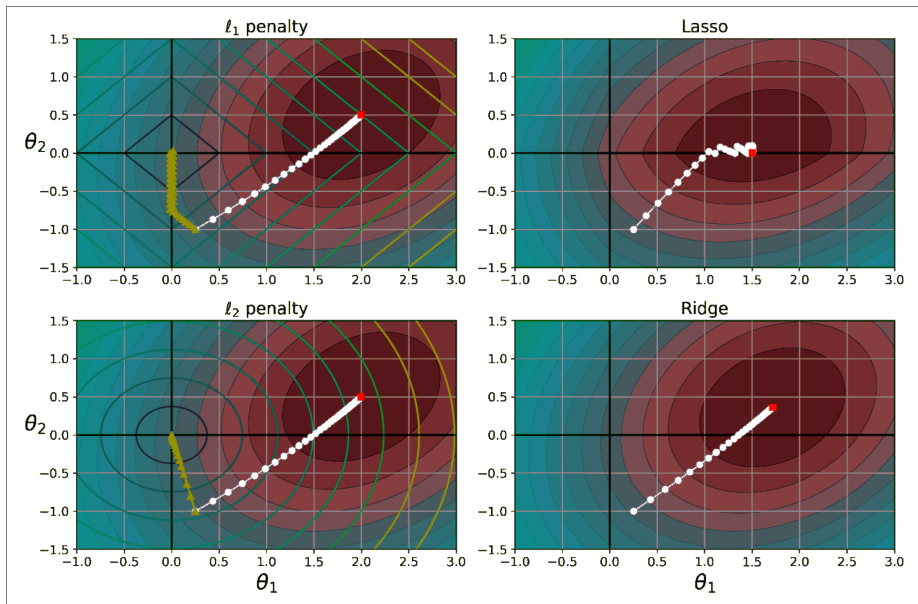
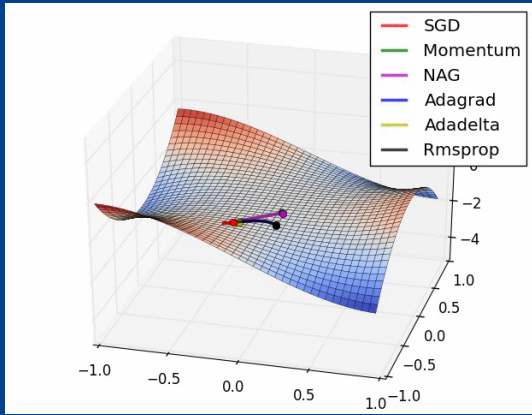
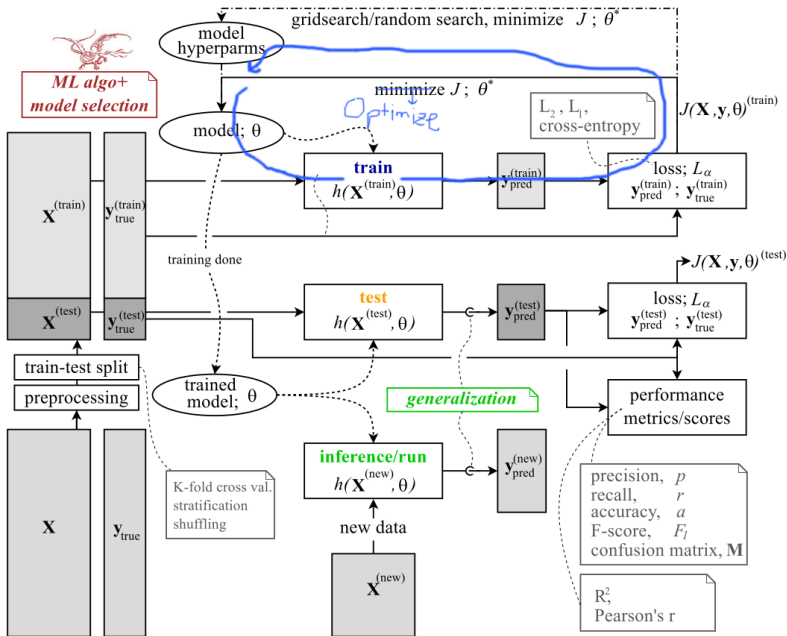


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OPTIMIZERS



Optimizers



Optimizers

Momentum Optimization

Normal GD algo

$$\mathbf{w} \leftarrow \mathbf{w} - \eta \nabla_{\mathbf{w}} J$$

but now with added (physical) momentum

$$\mathbf{m} \leftarrow \beta \mathbf{m} - \eta \nabla_{\mathbf{w}} J$$

$$\mathbf{w} \leftarrow \mathbf{w} + \mathbf{m}$$

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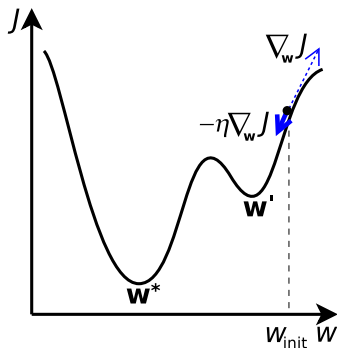
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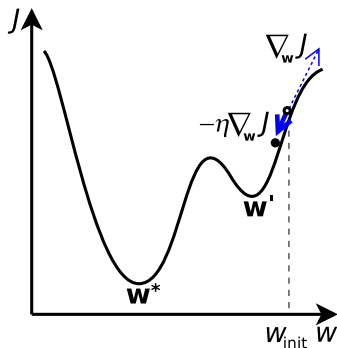
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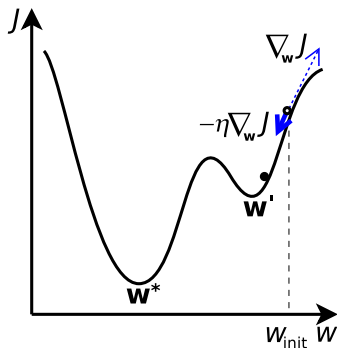
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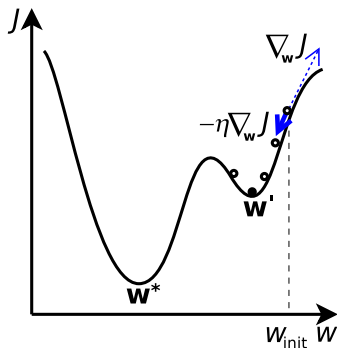
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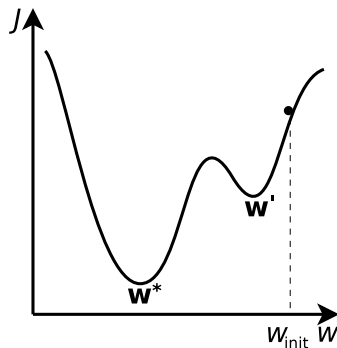
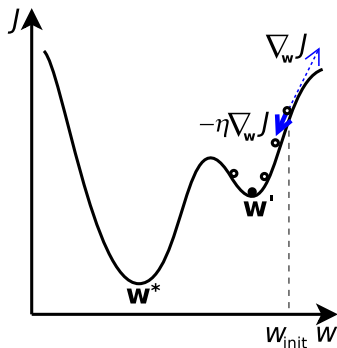
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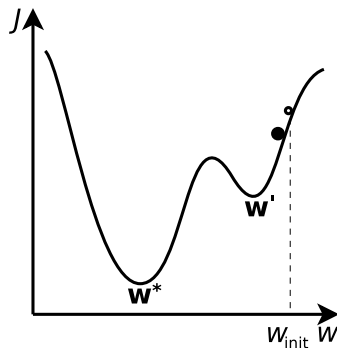
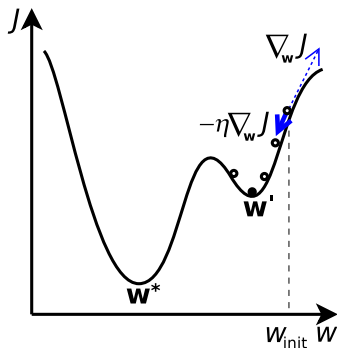
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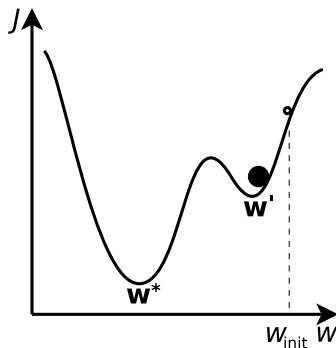
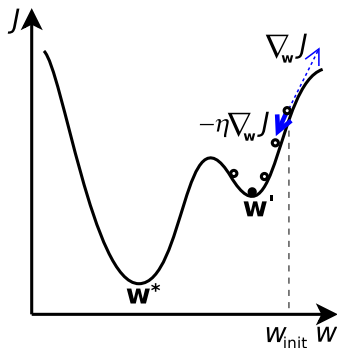
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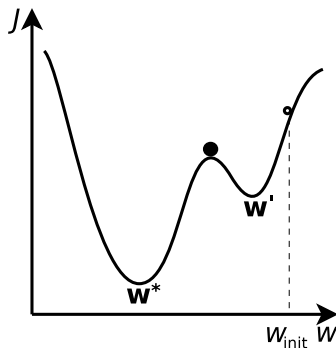
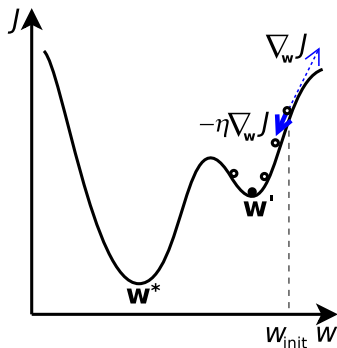
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$$\mathbf{w} \leftarrow \mathbf{w} - \eta \nabla_{\mathbf{w}} J$$

but now with added (physical) momentum

$$\mathbf{m} \leftarrow \beta \mathbf{m} - \eta \nabla_{\mathbf{w}} J$$

$$\mathbf{w} \leftarrow \mathbf{w} + \mathbf{m}$$



Optimizers

Momentum Optimization

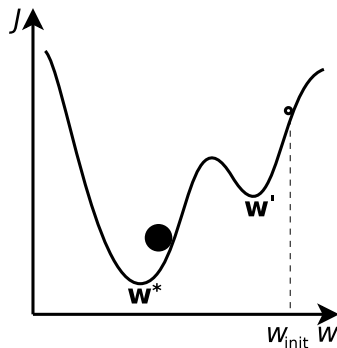
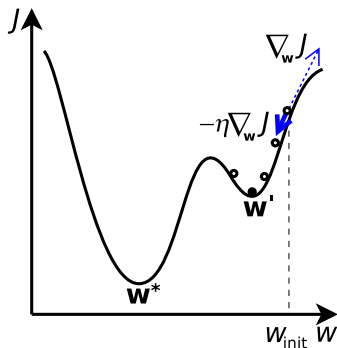
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Optimizers

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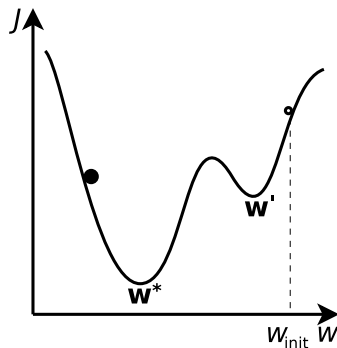
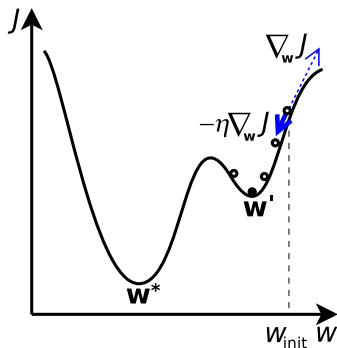
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Optimizers

Momentum Optimization

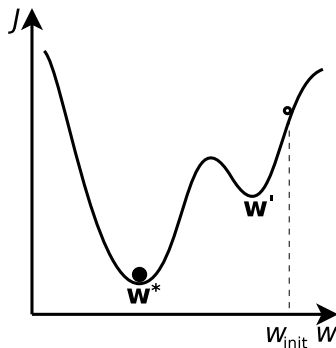
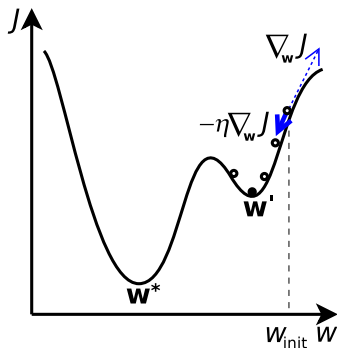
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Optimizers

Momentum Optimization

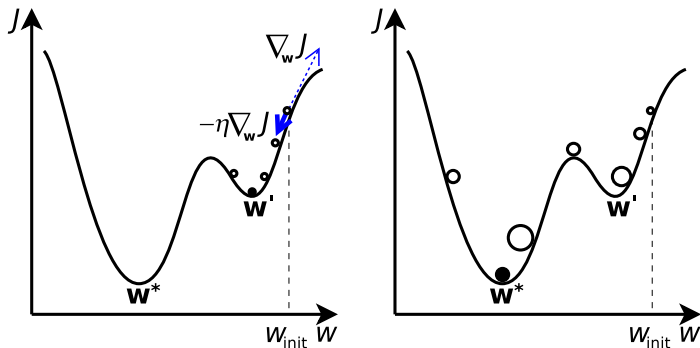
Normal GD algo

$$\mathbf{w} \leftarrow \mathbf{w} - \eta \nabla_{\mathbf{w}} J$$

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$$\mathbf{m} \leftarrow \beta \mathbf{m} - \eta \nabla_{\mathbf{w}} J$$

$$\mathbf{w} \leftarrow \mathbf{w} + \mathbf{m}$$



Optimizer selection: (perhaps) via searching..

`sklearn.neural_network.MLPRegressor`

```
class sklearn.neural_network.MLPRegressor(hidden_layer_sizes=(100, ), activation='relu', *, solver='adam', alpha=0.0001,
batch_size='auto', learning_rate='constant', learning_rate_init=0.001, power_t=0.5, max_iter=200, shuffle=True,
random_state=None, tol=0.0001, verbose=False, warm_start=False, momentum=0.9, nesterovs_momentum=True,
early_stopping=False, validation_fraction=0.1, beta_1=0.9, beta_2=0.999, epsilon=1e-08, n_iter_no_change=10,
max_fun=15000)
```

[\[source\]](#)

Multi-layer Perceptron regressor.

This model optimizes the squared-loss using LBFGS or stochastic gradient descent.

New in version 0.18.

Parameters: `hidden_layer_sizes : tuple, length = n_layers - 2, default=(100,)`

The ith element represents the number of neurons in the ith hidden layer.

`solver : {'lbfgs', 'sgd', 'adam'}, default='adam'`

The solver for weight optimization.

- 'lbfgs' is an optimizer in the family of quasi-Newton methods.
- 'sgd' refers to stochastic gradient descent.
- 'adam' refers to a stochastic gradient-based optimizer proposed by Kingma, Diederik, and Jimmy Ba

Note: The default solver 'adam' works pretty well on relatively large datasets (with thousands of training samples or more) in terms of both training time and validation score. For small datasets, however, 'lbfgs' can converge faster and perform better.

`activation : {'identity', 'logistic', 'tanh', 'relu'}, default='relu'`

Activation function for the hidden layer.

Optimizers

Or optimizers in Keras..



About Keras

Getting started

Developer guides

Keras API reference

Models API

Layers API

Callbacks API

Data preprocessing

Optimizers

Metrics

Losses

Built-in small datasets

Keras Applications

Utilities

Code examples

Why choose Keras?

» [Keras API reference](#) / Optimizers

Optimizers

Usage with `compile()` & `fit()`

An optimizer is one of the two arguments required for compiling a Keras model:

```
from tensorflow import keras
from tensorflow.keras import layers

model = keras.Sequential()
model.add(layers.Dense(64, kernel_initializer='uniform', input_shape=(10,)))
model.add(layers.Activation('softmax'))

opt = keras.optimizers.Adam(learning_rate=0.01)
model.compile(loss='categorical_crossentropy', optimizer=opt)
```

You can either instantiate an optimizer before passing it to `model.compile()`, as in the above example, or you can pass it by its string identifier. In the latter case, the default parameters for the optimizer will be used.

```
# pass optimizer by name: default parameters will be used
model.compile(loss='categorical_crossentropy', optimizer='adam')
```

Available optimizers

- SGD
- RMSprop
- Adam
- Adadelta
- Adagrad
- Adamax
- Nadam
- Ftrl



Optimizers

- ▷ Usage with `compile()` & `fit()`
- ▷ Usage in a custom training loop
- ▷ Learning rate decay scheduling
- ▷ Available optimizers
- ▷ Core Optimizer API
 - apply_gradients method
 - weights property
 - get_weights method
 - set_weights method

Optimizers Demo

L09/Extra/intro_mlp_revisited.ipynb

jupyter intro_mlp_revisited Last Checkpoint: 1 mandags kl. 09:47 (autosaved)



Logout

File Edit View Insert Cell Kernel Widgets Help

Connecting to kernel

Trusted

Python 3

Run Markdown

ITMAL Demo

MLP demo of solvers and a 1-neuron MLP for the OECD data from intro.

In [3]:

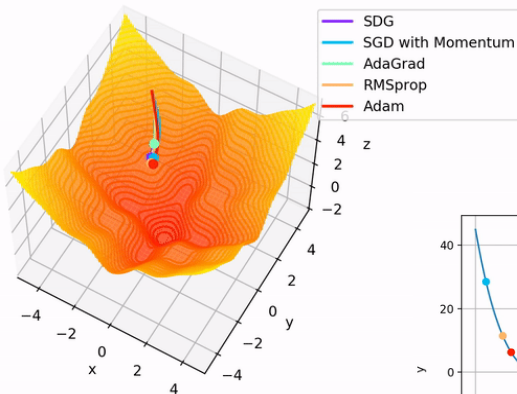
```
1 %matplotlib inline
2
3 import numpy as np
4 import matplotlib
5 import matplotlib.pyplot as plt
6
7 def LoadDataFromL01():
8     import pickle
9     filename = "../L04/Data/itmal_l01_data.pkl"
10    with open(f"{filename}", "rb") as f:
11        (X, y) = pickle.load(f)
12        return X, y
13
14 X, y = LoadDataFromL01()
15
16 print(f"X.shape={X.shape}, y.shape={y.shape}")
17
18 assert X.shape[0] == y.shape[0]
19 assert X.ndim == 2
20 assert y.ndim == 1 # did a y.ravel() before saving to pickle file
21 assert X.shape[0] == 29
22
23 # re-create plot data (not stored in the Pickle file)
24 m = np.linspace(0, 60000, 1000)
25 M = np.empty([m.shape[0], 1])
26 M[:, 0] = m
27
28 print("OK")
```

X.shape=(29, 1), y.shape=(29,)

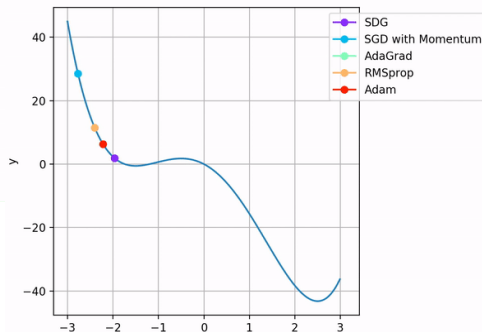
OK

Optimizers

Optimizer Comparison



Optimizer Comparison



Sources: Imgur by Alec Radford and
<https://towardsdatascience.com/complete-guide-to-adam-optimization-1e5f29532c3d>

SEARCHING

ML Algorithm +
Model Selection via Searching

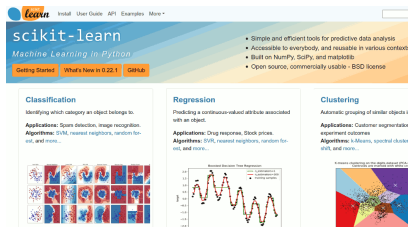


ML Models (or ML algorithms)

Models encountered so far

Some classifiers and regressors..

```
sklearn.neighbors.KNeighborsRegressor  
sklearn.linear_model.LinearRegression  
sklearn.linear_model.SGDClassifier  
sklearn.linear_model.SGDRegressor
```



The screenshot shows the scikit-learn website. At the top, there's a navigation bar with links: Install, User Guide, API, Examples, and More. Below this is the scikit-learn logo and the tagline "Machine Learning in Python". To the right, there are bullet points highlighting features: "Simple and efficient tools for predictive data analysis", "Accessible to everybody and reusable in various contexts", "Built on NumPy, SciPy, and matplotlib", and "Open source, commercially usable - BSD license". Below the header, there are three main sections: "Classification", "Regression", and "Clustering". Each section has a brief description, applications, and algorithms. The Classification section includes a grid of handwritten digits. The Regression section includes a line plot showing a regression model fit. The Clustering section includes a scatter plot showing clusters of data points.

scikit-learn
Machine Learning in Python

Getting Started | What's New in 0.22.1 | GitHub

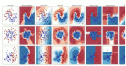
- Simple and efficient tools for predictive data analysis
- Accessible to everybody and reusable in various contexts
- Built on NumPy, SciPy, and matplotlib
- Open source, commercially usable - BSD license

Classification

Identifying which category an object belongs to.

Applications: Spam detection, image recognition.

Algorithms: SVM, nearest neighbors, random forest, and more...

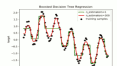


Regression

Predicting a continuous-valued attribute associated with an object.

Applications: Drug responses, stock prices.

Algorithms: OLS, nearest neighbors, random forest, and more...




Clustering

Automatic grouping of similar objects.

Applications: Customer segmentation, experiment outcomes.

Algorithms: k-Means, spectral clustering, and more...



ML Models (or ML algorithms)

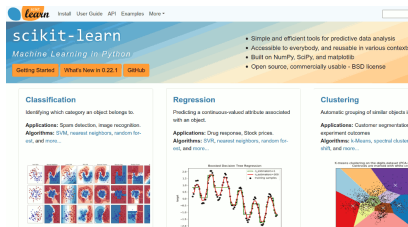
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```

Perhaps..

```
sklearn.naive_bayes.GaussianNB  
sklearn.naive_bayes.MultinomialNB  
sklearn.svm.SVC  
sklearn.svm.SVR
```



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ML Models (or ML algorithms)

Models encountered so far

Some classifiers and regressors..

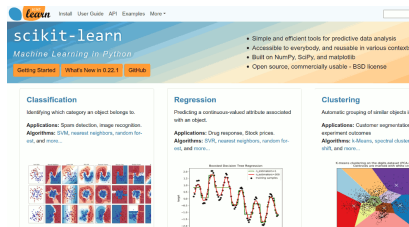
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sklearn.naive_bayes.GaussianNB  
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sklearn.svm.SVC  
sklearn.svm.SVR
```

and to some degree..

```
sklearn.linear_model.LogisticRegression  
sklearn.linear_model.Perceptron  
sklearn.neural_network.MLPClassifier  
sklearn.neural_network.MLPRegressor  
keras.Sequential
```



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scikit-learn
Machine Learning in Python

- Simple and efficient tools for predictive data analysis
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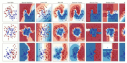
[Getting Started](#) [What's New in 0.22.1](#) [Github](#)

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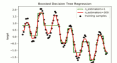


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Perhaps..

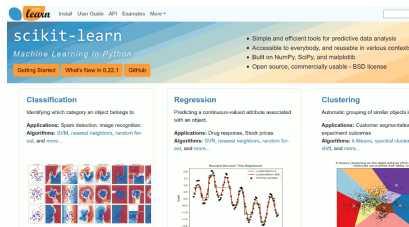
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```

and to some degree..

```
sklearn.linear_model.LogisticRegression  
sklearn.linear_model.Perceptron  
sklearn.neural_network.MLPClassifier  
sklearn.neural_network.MLPRegressor  
keras.Sequential
```

Or even more exotic models like..

- ▶ supervised ensemble: AdaBoost, Bagging, DecisionTree, RandomForest,...
- ▶ semi-supervised: ??
- ▶ unsupervised: K-means, manifolds, restricted Boltzmann machines,...
- ▶ clustering: K-means



ML Algorithm + Model Selection via Searching

What ML algorithm to choose?

- ▶ manual:
 - algorithm characteristics, \mathcal{O} complexity, etc.
 - browsing through Scikit-learn documentation,
 - ...and also based on data assumptions.

ML Algorithm + Model Selection via Searching

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- ▶ semi-automatic:
 - brute-force model search, and fun with python!

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- ▶ semi-automatic:
 - brute-force model search, and fun with python!

```
1  models = {  
2      SVC(gamma="scale"),  
3      SGDClassifier(tol=1e-3, eta0=0.1),  
4      GaussianNB()  
5  }  
6  
7  for i in models:  
8      i.fit(X_train, y_train)  
9      y_pred_test = i.predict(X_test)  
10     p = precision_score(y_test, y_pred_test, average='micro')  
11     print(f'{type(i).__name__:13s}: precision={p:0.2f}')
```

NOTE: Python set = {a, b}
Python dictionary = {a:x, b:y}

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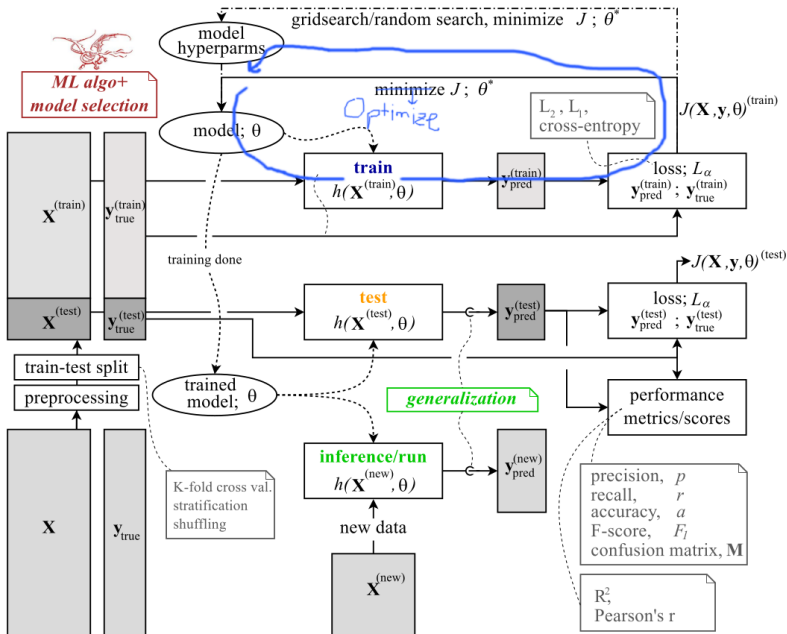
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```

prints..

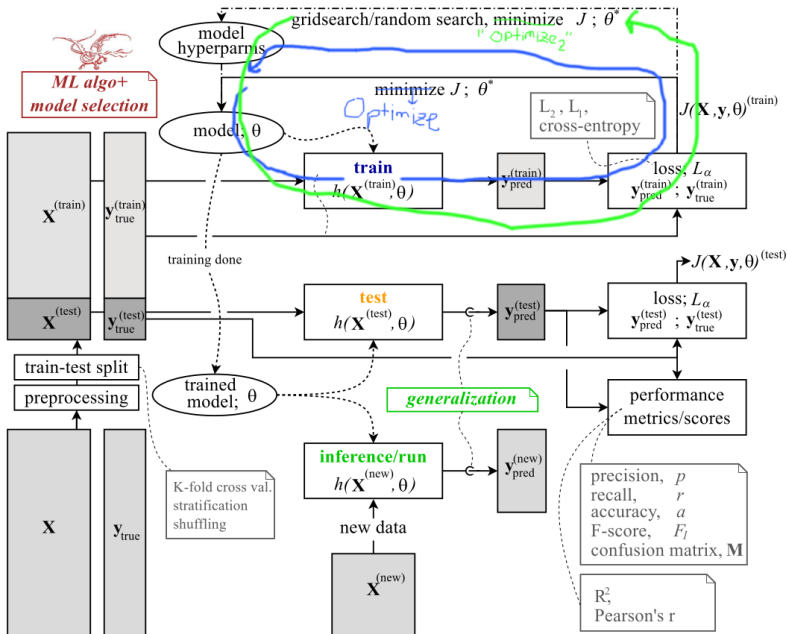
GaussianNB:	p=1.00
SGDClassifier:	p=0.93
SVC:	p=0.98

NOTE: Python set = {a, b}
Python dictionary = {a:x, b:y}

Model Selection via Grid Search



Model Selection via Grid Search



Model Selection via Grid Search

The hyperparameter-set for SGD linear regressor

```
1  class sklearn.linear_model.SGDRegressor(  
2      loss      ='squared_loss', penalty      ='l2',  
3      alpha     =0.0001,      l1_ratio      =0.15,  
4      tol       =None,        shuffle       =True,  
5      verbose   =0,           epsilon      =0.1,  
6      eta0      =0.01,        power_t     =0.25,  
7      n_iter_no_change=5,      warm_start  =False,  
8      fit_intercept =True,    max_iter    =None,  
9      average     =False,    n_iter      =None  
10     random_state  =None,    learning_rate='invscaling',  
11     early_stopping =False,  validation_fraction=0.1  
12 )
```

Model Selection via Grid Search

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1 class sklearn.linear_model.SGDRegressor(  
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Model Selection via Grid Search

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Search best hyperparameters in a (smaller) set, say

Model Selection via Grid Search

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4     tol       = None,                 shuffle     = True,  
5     verbose   = 0,                   epsilon     = 0.1,  
6     eta0      = 0.01,                power_t     = 0.25,  
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8     fit_intercept = True,             max_iter    = None,  
9     average     = False,             n_iter      = None,  
10    random_state  = None,             learning_rate='invscaling',  
11    early_stopping = False,          validation_fraction=0.1  
12 )
```



Search best hyperparameters in a (smaller) set, say

```
1 model = SGDRegressor()  
2 tuning_parameters = {  
3     'alpha': [ 0.001, 0.01, 0.1],  
4     'max_iter': [1, 10, 100, 1000],  
5     'learning_rate': ('constant', 'optimal', 'invscaling', 'adaptive')  
6 }  
7 ..  
8 grid_tuned = GridSearchCV(model, tuning_parameters, ..
```

Model Selection via Grid Search

How to select 'best' set of hyperparameter—using brute force?

Gridsearch seen in 3D for the two hyperspace dimensions:

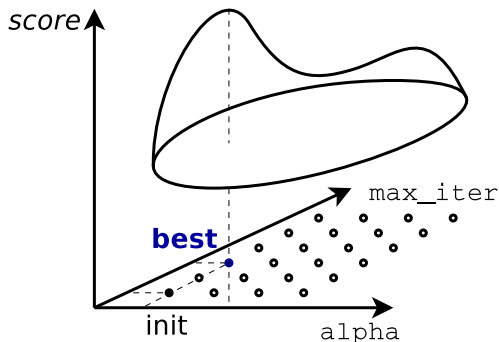
- ▶ `alpha` $\in [1, 2, 3, \dots]$ (NOTE: linear range for this plot only,
- ▶ `max_iter` $\in [1, 2, 3, \dots]$ should be 1, 10, 100 or similar.)

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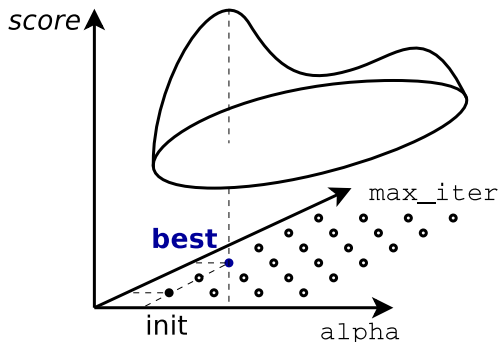


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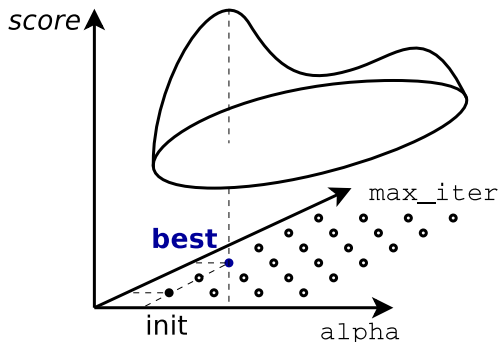
- ▶ why score and not J on z -axis?

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- ▶ $\text{max_iter} \in [1, 2, 3, \dots]$ should be 1, 10, 100 or similar.)



- ▶ why score and not J on z -axis?
- ▶ and what if there are many hyperparameters and many combinations? \rightarrow Zzzzzzz!

Model Selection via Randomized Search

How to select 'best' set of hyperparameters—faster than brute force?

Replace `GridSearchCV()` with

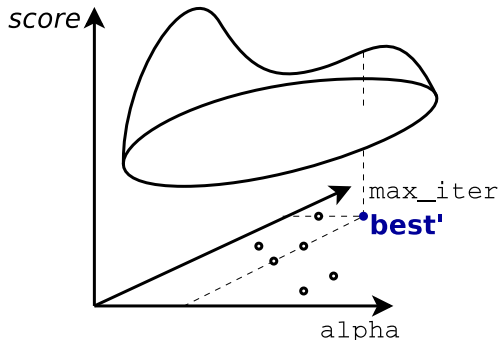
`RandomizedSearchCV(n_iter=100,...)`

Model Selection via Randomized Search

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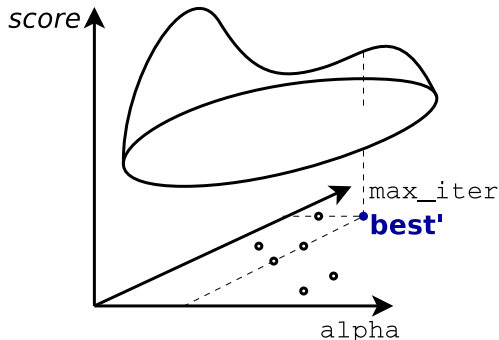


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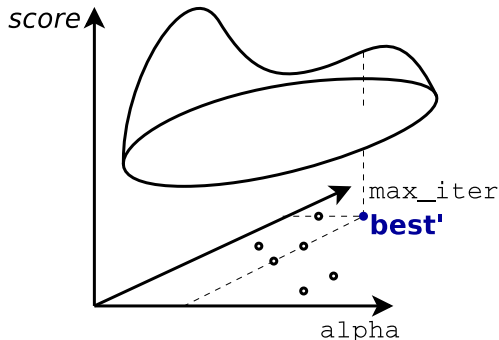
- faster, but will not yield the (sub) optimal score maximum,

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- ▶ faster, but will not yield the (sub) optimal score maximum,
- ▶ ...but does it matter in a huge hyperparameter search-space?

Exercise: L09/gridsearch.ipynb

Qd MNIST Search Quest II: Husk at publicer på Brightspace

**Qd MNIST Search Quest II** ...

Publicer (helt nederst i denne item) løbende dit bedste resultat fra opgaven

gridsearch.ipynb (Qd)

Indtast din model constructor string og score og en kommentar vdr. dit model ala

```
Grp09: best: dat=mnist, score=0.90780, model=SGDClassifier(alpha=1.0,eta0=0.0001,learning_rate='invscaling')
```

```
Grp09: CTOR for best model: SGDClassifier(alpha=1.0, average=False, class_weight=None, early_stopping=False,
epsilon=0.1, eta0=0.0001, fit_intercept=True, l1_ratio=0.15,
learning_rate='invscaling', loss='hinge', max_iter=1000,
n_iter_no_change=5, n_jobs=None, penalty='l2', power_t=0.5,
random_state=None, shuffle=True, tol=0.001,
validation_fraction=0.1, verbose=0, warm_start=False)
```

NB: brug af **neurale netværks** modeller (Perceptrons, MLP's, Keras etc.) samt **KNeighborsClassifier** ikke tilladt i denne quest!

Highscore fra sidste semester = 0.97369

```
model=KNeighborsClassifier(algorithm='ball_tree', n_neighbors=3, p=4,weights='distance')
```

ITMAL Search Quest

Send message...

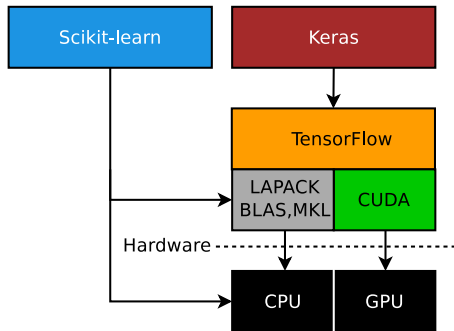
8/31

Extra Slides..

Keras and Tensorflow



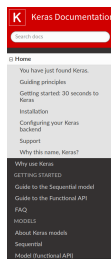
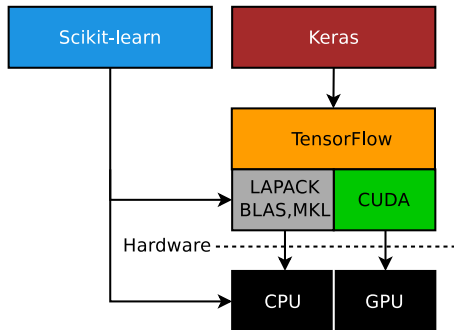
Using the Keras API instead of Scikit-learn or TensorFlow



Keras and Tensorflow



Using the Keras API instead of Scikit-learn or TensorFlow



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Keras: The Python Deep Learning library



You have just found Keras.

Keras is a high-level neural networks API, written in Python and capable of running on top of TensorFlow, CNTK, or Theano. It was developed with a focus on enabling fast experimentation. Being able to go from idea to result with the least possible delay is key to doing good research.

Use Keras if you need a deep learning library that:

- Allows for easy and fast prototyping (through user-friendliness, modularity, and extensibility).
- Supports both convolutional networks and recurrent networks, as well as combinations of the two.
- Runs seamlessly on CPU and GPU.

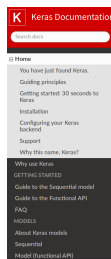
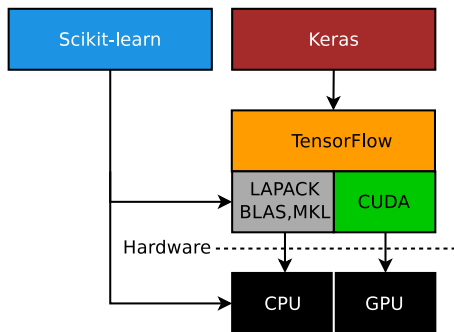
NOTE:

- documentation: <https://keras.io/>

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NOTE:

- ▶ documentation: <https://keras.io/>
- ▶ keras provides a `fit-predict`-interface,
- ▶ many similarities to Scikit-learn,
- ▶ but also many differences!

High-Performance-Computing (HPC)

Running on the ASE GPU cluster:

login=itmal09-e21 (for ITMAL group 9)

password=imal09-e21_123

