CS150A Database

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Today:

- Query Optimization II:
 - Costing and Searching

Readings:

 Database Management Systems (DBMS), Chapter 15

What is needed for query optimization?

- Given: A closed set of operators
 - Relational ops (table in, table out)
 - Physical implementations (of those ops and a few more)
- 1. Plan space all possible solutions
 - Based on relational equivalences, different implementations
- Cost estimation based on
 - · Cost formulas size of doita go into operators.
 - Size estimation, in turn based on
 - Catalog information on base tables
 - Selectivity (Reduction Factor) estimation

 Size of ctoved tables
- 3. A search algorithm
 - To sift through the plan space and find lowest cost option!

Reminder

- We're focusing on "System R" ("Selinger") optimizers
 - Remarkably comprehensive framework
 - Many of the details have been refined over time
 - We'll see some refinements today
 - This remains an area of ongoing research!

Big Picture of System R Optimizer

- Works well for up to 10-15 joins.
- Plan Space: Too large, must be pruned.
 - Algorithmic insight:
 - Many plans could have the same "overpriced" subtree
 - Ignore all those plans
 - Common heuristic: consider only left-deep plans
 - Common heuristic: avoid Cartesian products
- Cost estimation
 - Very inexact, but works ok in practice.
 - Stats in system catalogs used to estimate sizes & costs
 - Considers combination of CPU and I/O costs.
 - System R's scheme has been improved since that time.
- Search Algorithm: Dynamic Programming

Not covered: flatten into single blocks

Query Blocks: Units of Optimization

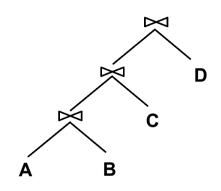
- Break query into query blocks
- Optimize one block at a time
- Uncorrelated nested blocks computed once
- Correlated nested blocks are like function calls
 - But sometimes can be "decorrelated"
 - Beyond the scope of CS150A!

```
SELECT S.sname
FROM Sailors S
WHERE S.age IN
```

Outer block

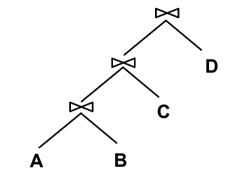
(SELECT MAX (S2.age)
FROM Sailors S2
GROUP BY S2.rating)

Nested block



Query Blocks: Units of Optimization Pt 2

- For each block, the plans considered are:
 - All relevant access methods, for each relation in FROM clause.
 - All left-deep join trees
 - right branch always a base table
 - consider all join orders and join methods



```
SELECT S.sname
FROM Sailors S
WHERE S.age IN
```

Outer block

(SELECT MAX (S2.age)
FROM Sailors S2
GROUP BY S2.rating)

Nested block

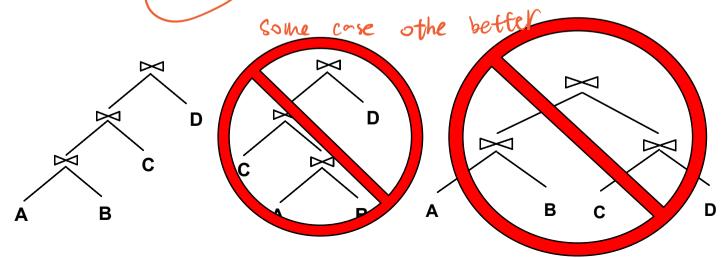
"Physical" Properties

- Two common "physical" properties of an output:
 - Sort order
 - Hash Grouping
- E.g. Index scan (result is sorted) Sorted by index legs (if B+ tree)
 - E.g. Sort (result is sorted)
 - E.g. Hash (result is grouped)
- Certain operators require these properties at input
 - E.g. MergeJoin requires sorted input
- Certain operators preserve these properties from inputs
 - E.g. MergeJoin preserves sort order of inputs
 - E.g. INLJ preserves sort order of outer (left) input



Queries Over Multiple Relations

- A System R heuristic: only left-deep join trees considered.
 - Restricts the search space
 - Left-deep trees allow us to generate all fully pipelined plans.
 - Intermediate results not written to temporary files.
 - Not all left-deep trees are fully pipelined (e.g., SM join).



Plan Space Review

- For a SQL query, full plan space:
 - All equivalent relational algebra expressions
 - Based on the equivalence rules we learned
 - All mixes of physical implementations of those algebra expressions
- We might prune this space:
 - Selection/Projection pushdown
 - Left-deep trees only
 - Avoid cartesian products

- Along the way we may care about physical properties like sorting
 - Because downstream ops may depend on them
 - And enforcing them later may be expensive

Query Optimization: Cost Estimation

- 1. Plan Space
- 2. Cost Estimation
- 3. Search Algorithm

Cost Estimation

- For each plan considered, must estimate total cost:
 - Must estimate cost of each operation in plan tree.
 - Depends on input cardinalities.
 - We've already discussed this for various operators
 - sequential scan, index scan, joins, etc.
 - Must estimate size of result for each operation in tree!
 - Because it determines downstream input cardinalities!
 - Use information about the input relations.
 - For selections and joins, assume independence of predicates.
- In System R, cost is boiled down to a single number consisting of #I/O + CPU-factor * #tuples

focus only

Statistics and Catalogs

- Need info on relations and indexes involved.
- Catalogs typically contain at least:

Statistic	Meaning					
NTuples	# of tuples in a table (cardinality)					
NPages	# of disk pages in a table					
Low/High	min/max value in a column					
Nkeys	# of distinct values in a column					
IHeight	the height of an index					
INPages	# of disk pages in an index					

- Catalogs updated periodically.
 - Too expensive to do continuously
 - Lots of approximation anyway, so a little slop here is ok.
- Modern systems do more
 - Esp. keep more detailed statistical information on data values
 - e.g., histograms

Size Estimation and Selectivity

 (C_{M})

- Max output cardinality = product of input cardinalities
- Selectivity (sel) associated with each term (in Inc.)
 - reflects the impact of the term in reducing result size.
 - selectivity = |output| / |input| (ar o
 - Book calls selectivity "Reduction Factor" (RF)
- Avoid confusion:
 - "highly selective" in common English is opposite of a high selectivity value (|output|/|input| high!)

```
SELECT attribute list
FROM relation list
WHERE term1 AND ... AND termk
```

Result Size Estimation

- Result cardinality = Max # tuples * product of all selectivities.
- Term col=value (given Nkeys(I) on col)
 - sel = 1/NKeys(I)
- Term col1=col2 (handy for joins too...) Li, li : table
 - sel = 1/MAX(NKeys(I1), NKeys(I2))
 - Why MAX? See bunnies in 2 slides...
- Term col>value
 - sel = (High(I)-value)/(High(I)-Low(I) + 1)

12345

Note, if missing the needed stats, assume 1/10!!!

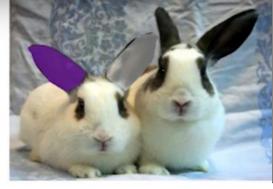
Let's dig into selectivity estimation more deeply

- Clarify how some of these estimates came to be
 - Refine our stored statistics
 - Expose our statistical assumptions

phrity

P(leftEar = rightEar)

- 100 bunnies
- 2 distinct LeftEar colors
 - {C1, C2}
- 10 distinct RightEar colors
 - {C1..C10}
- Independent ears
- What's the probability of matching ears?



$$\begin{split} P(L=R) &= \sum_{i} P(C_{i},C_{i}) \\ &= P(C_{1},C_{1}) + P(C_{2},C_{2}) + P(C_{3},C_{3}) + \dots \\ &= (\frac{1}{2} \cdot \frac{1}{10}) + (\frac{1}{2} \cdot \frac{1}{10}) + (0 \cdot \frac{1}{10}) + \dots \\ &= 1/10 \\ &= 1/\text{MAX}(2,10) \end{split}$$

Postgres 10.0: src/include/utils/selfuncs.h

```
/* default selectivity estimate for equalities such as "A = b" */
    #define DEFAULT EQ SEL 0.005
    /* default selectivity estimate for inequalities such as "A < b" */
    /* default selectivity estimate for range inequalities "A > b AND A < c" */
    #define DEFAULT RANGE INEQ SEL 0.005
/* default selectivity estimate for pattern-match operators such as LIKE */
    #define DEFAULT MATCH SEL 0.005
    /* default number of distinct values in a table */
    #define DEFAULT NUM DISTINCT 200
    /* default selectivity estimate for boolean and null test nodes */
    #define DEFAULT UNK SEL 0.005
    #define DEFAULT NOT UNK SEL (1.0 - DEFAULT UNK SEL)
```

distribution

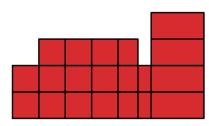
Reduction Factors & Histograms

For better estimation, use a histogram

equiwidth	of	Vo	Ire	V			
No. of Values	2	3	3	1	8	2	1
Value	099	1-1.99	2-2.99	3-3.99	4-4.99	5-5.99	6-6.99



No. of Values	2	3	3	3	3	2	4
Value	099	1-1.99	2-2.99	3-4.05	4.06-4.67	4.68-4.99	5-6.99



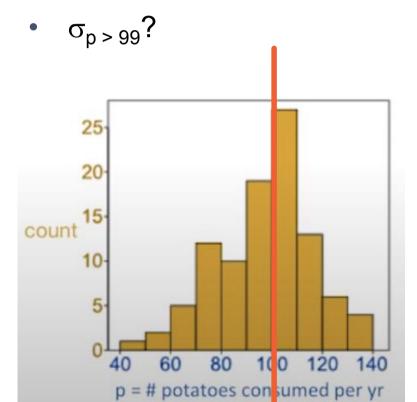
Note: 10-bucket equidepth histogram divides the data into deciles

- akin to quantiles, median, etc.

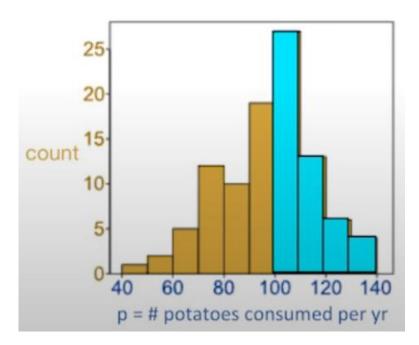
Common trick: "end-biased" histogram

very frequent values in their own buckets
 See also V-Optimal histograms on Wikipedia

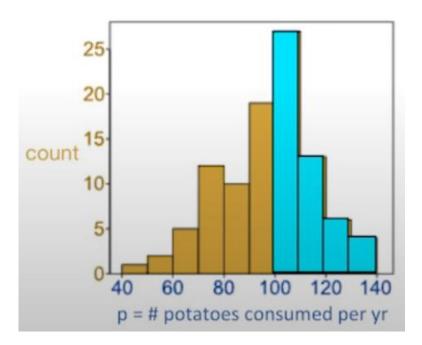
100 rows



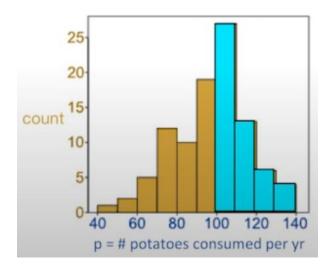
- 100 rows
- $\sigma_{p > 99}$?

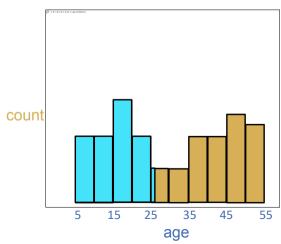


- 100 rows
- $\sigma_{p > 99}$? 50/100 = 50%.

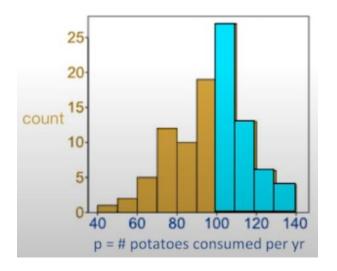


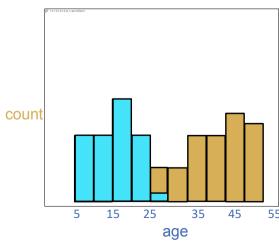
- 100 rows
- $\sigma_{\text{age} < 26}$?





- 100 rows
- $\sigma_{\text{age} < 26}$?





- 100 rows
- $\sigma_{\text{age} < 26}$?

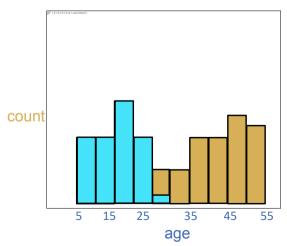
25-20-15-10-40 60 80 100 120 140 p = # potatoes consumed per yr



Uniformity assumption:

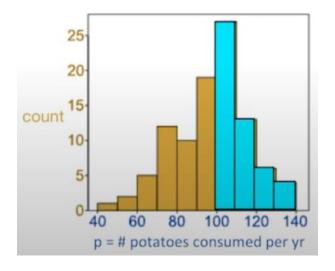
Uniform distribution within each bin
Each vertical slice the same
Hence ⅓ of the population of bin [25,30)
has age < 26.

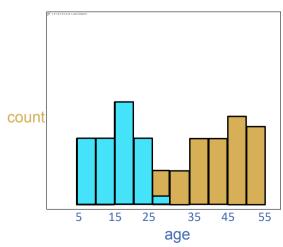
$$10 + 10 + 15 + 10 + (\frac{1}{5} * 5) = 46/100 = 46\%$$



Selectivity of Conjunction

- 100 rows
- $\sigma_{p > 99 \land age < 26}$?





Selectivity of Conjunction, cont

- 100 rows
- $\sigma_{p > 99 \land age < 26}$?

25-20count 15-10-5-10-40-60-80-100-120-140 p = # potatoes consumed per yr

Independence assumption:

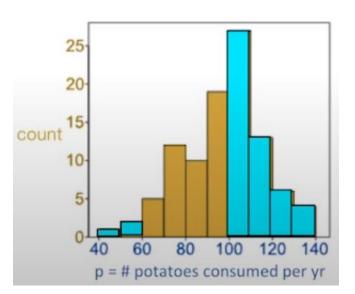
- Age and potato consumption are independent
- Hence p bins all shrink by 46%.
- Hence age bins all shrink by 50%.

Selectivity: 50% × 46% = **23%**

Selectivity of Disjunction

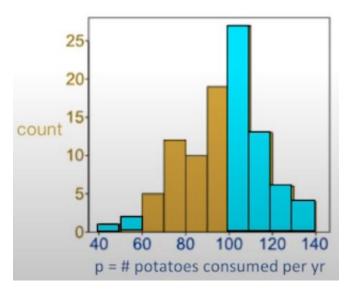
- 100 rows
- $\sigma_{p > 99 \ v \ p < 60}$?

 50% 3%



Selectivity of Disjunction, Part 2

- 100 rows
- $\sigma_{p > 99 \ v \ p < 60}$?
 50% 3%
- Selectivity: 50% + 3% = **53%**



Selectivity of Disjunction, Part 3

100 rows

20

10

5

count

• $\sigma_{p > 99 \text{ v age } < 26}$?

100 120 140

80

p = # potatoes consumed per yr

60

25-20count 15-5 15 25 35 45 55 age

- Answer tuples satisfy one or both predicates
- By independence assumption:
 - Satisfy the first predicate: 50%
 - Satisfy the second predicate: 46%
 - Satisfy both: 50% × 46%
 - Don't double-count!

Selectivity:

$$50\% + 46\% - (50\% \times 46\%) = 73\%$$

Selectivity for more complicated queries?

- $R\bowtie_p \sigma_q(S)$
 - Selectivity of join predicate p is s_p
 - Selectivity of selection predicate q is s_q
 - How to think about overall selectivity?

Join Selectivity

- Recall from algebraic equivalences: $R \bowtie_p S \equiv \sigma_p(R \times S)$
- Hence join selectivity is "just" selectivity s_p
 - Over a big input: |R| × |S|!
- Total rows: $s_p \times |R| \times |S|$

Selectivity for our earlier query?

Recall from algebraic equivalences

$$\mathsf{R}\bowtie_{\mathsf{p}}\sigma_{\mathsf{q}}(\mathsf{S})\equiv\sigma_{\mathsf{p}}(\mathsf{R}\times\sigma_{\mathsf{q}}(\mathsf{S}))\equiv\sigma_{\mathsf{p}\wedge\mathsf{q}}(\mathsf{R}\times\mathsf{S})$$

- Hence selectivity just s_ps_q
 - Applied to |R| × |S|!
- Total rows: s_ps_q|R||S|

potatoes consumed per yr

Intuition: similar to bunny ears, but weighted by the histogram bins.

```
> bin untaining U
                                                            uniform as unption
For each value v covered in either histogram:
    // uniformity assumption within bins:
    // P(T.p = v) = \frac{\text{height}(\text{binp}(v))}{n} * 1/\text{width}(\text{binp}(v))
    // P(T.age = v) = height(binage(v))/n * 1/width(binage(v))
                              count
          80
             100 120
                                           25
                                             35
```

age

Column Equality?

T.p = T.age ??

```
Intuition: similar to bunny ears, but weighted by the histogram bins.
s = 0
For each value v covered in either histogram:
    // uniformity assumption within bins:
    // P(T.p = v) = height(binp(v))/n * 1/width(binp(v))
    // P(T.age = v) = height(binage(v))/n * 1/width(binage(v))
    // independence assumption across columns:
    // P(T.p = v \wedge T_age = v)
    // = P(T.p = v) P(T.age = v)
    s += height(binp(v))/(n*width(binp(v)))
               * height(binage(v))/(n*width(binage(v)))
```

Upshot

- Know how to compute selectivities for basic predicates
 - The original Selinger version
 - The histogram version
- Assumption 1: uniform distribution within histogram bins
 - Within a bin, fraction of range = fraction of count

- Assumption 2: independent predicates
 - Selectivity of AND = product of selectivities of predicates
 - Selectivity of OR = sum of selectivities of predicates product of selectivities of predicates
 - Selectivity of NOT = 1 selectivity of predicates
- Joins are not a special case
 - Simply compute the selectivity of all predicates
 - And multiply by the product of the table sizes



Query Optimization

- 1. Plan Space
- 2. Cost Estimation
- 3. Search Algorithm

Enumeration of Alternative Plans

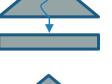
- There are two main cases:
 - Single-table plans (base case)
 - Multiple-table plans (induction)
- Single-table queries include selects, projects, and groupBy/agg:
 - Consider each available access path (file scan / index)
 - Choose the one with the least estimated cost
 - Selection/Projection done on the fly
 - Result pipelined into grouping/aggregation

Cost Estimates for Single-Relation Plans

- > fetch tuple from Index I on primary key matches selection:
 - Cost is (Height(I) + 1) + 1 for a B+ tree.
- Clustered index I matching selection:
 - (NPages(I)+NPages(R)) * selectivity.
- # of page in index in Table
 Non-clustered index I matching selection:
 - - (NPages(I)+NTuples(R)) * selectivity.
 - Sequential scan of file:
 - NPages(R).

Recall: Must also charge for duplicate elimination if required

R: rend I: index







Schema for Examples

Reserves:

- Each tuple is 40 bytes long, 100 tuples per page, 1000 pages.
- 100 distinct bids.

Sailors:

- Each tuple is 50 bytes long,
- 80 tuples per page, 500 pages.
- 10 ratings, 40,000 sids.

Example

```
SELECT S.sid
FROM Sailors S
WHERE S.rating=8
```

- If we have an index on rating:
 - Cardinality = (1/NKeys(I)) * NTuples(R) = (1/10) * 40000 tuples
 - Clustered index: (1/NKeys(I)) * (NPages(I)+NPages(R)) = (1/10) * (50+500) = **55 pages are retrieved**. (This is the cost.)
 - Unclustered index: (1/NKeys(I)) * (NPages(I)+NTuples(R))= (1/10) * (50+40000) = 4005 pages are retrieved.
- If we have an index on sid:
 - Would have to retrieve all tuples/pages. With a clustered index, the cost is 50+500, with unclustered index, 50+40000.
- Doing a file scan:
 - We retrieve all file pages (500).

Enumeration of Left-Deep Plans

- Left-deep plans differ in
 - · the order of relations index scan/ her scan
 - the access method for each leaf operator
 - the join method for each join operator



- Enumerated using N passes (if N relations joined):
 - Pass 1: Find best 1-relation plan for each relation
 - Pass i: Find best way to join result of an (i -1)-relation plan (as outer) to the i' th relation. (i between 2 and N.)



- For each subset of relations, retain only:
 - Cheapest plan overall, plus

possible makes

Cheapest plan for each interesting order of the tuples.



The Principle of Optimality

- Richard Bellman (slightly adapted to our setting)
- The best overall plan is composed of best decisions on the subplans
 - Optimal result has optimal substructure
- For example, the best left-deep plan to join tables A, B, C is either:
 - (The best plan for joining A, B) ⋈ C
 - (The best plan for joining A, C) ⋈ B
 - (The best plan for joining B, C) ⋈ A
- This is great!
 - When optimizing a subplan (e.g. A ⋈ B), we don't have to think about how it will be used later (e.g. when dealing with C)!

{A, B}

• When optimizing a higher-level plan (e.g. $A \bowtie B \bowtie C$) we can reuse the best results of subroutines (e.g. $A \bowtie B$)!



Dynamic Programming Algorithm for System R

- Principle of optimality allows us to build best subplans "bottom up"
 - Pass 1: Find best plans of height 1 (base table accesses), and record them in a table
 - Pass 2: Find best plans of height 2 (joins of base tables) by combining plans of height 1, record them in a table
 - ...
 - Pass i: Find best plans of height i by combining plans of height i 1 with plans of height 1, record them in a table
 - ...
 - Pass n: Find best plan overall by combining plans of height n-1 with plans of height 1.





The Basic Dynamic Programming Table

Table keyed on 1st column

Subset of tables in FROM clause	Best plan	Cost
{R, S}	hashjoin(R,S)	1000
{R, T}	mergejoin(R,T)	700

A Wrinkle: Interesting Orders

- Physical properties can break the principle of optimality
 - For example, consider a suboptimal plan p for A ⋈ B that is ordered on column x
 - Suppose we need to join with table C on column x
 - Sort-merge of p with C might be the best overall plan
 - The best plan for A ⋈ B requires us to sort for Sort-Merge join
 - But the suboptimal plan p doesn't require us to sort A ⋈ B
- Solution: expand our definition of "optimal substructure"
 - The structure will include both the set of tables and the physical properties (order)
 - But not all orders are "interesting"! We can prune further

A Note on "Interesting Orders"

- Physical property: Order.
 When should we care? When is it "interesting"?
- An intermediate result has an "interesting order" if it is sorted by anything we can use later in the query ("downstream" the arrows):
 - ORDER BY attributes
 - GROUP BY attributes
 - Join attributes of yet-to-be-added joins
 - subsequent merge join might be good

The Dynamic Programming Table

Subset of tables in FROM clause	Interesting- order columns	Best plan	Cost
{R, S}	<none></none>	hashjoin(R,S)	1000
{R, S}	<r.a, s.a=""></r.a,>	sortmerge(R,S)	1500

Table keyed on concatenation of 1st two columns

Enumeration of Plans (Contd.)

- First figure out the scans and joins (select-project-join) using D.P.
 - **Avoid Cartesian Products** in dynamic programming as follows: When matching an i -1 way subplan with another table, only consider it if
 - There is a join condition between them, **or**
 - All predicates in WHERE have been "used up" in the i -1 way subplan.



- Then handle ORDER BY, GROUP BY, aggregates etc. as a post-processing step
 - Via "interestingly ordered" plan if chosen (free!)

Or via an additional sort/hash operator

Despite pruning, this System R D.P. algorithm is exponential in #tables.



Example

```
SELECT S.sid, COUNT(*) AS number
FROM Sailors S, Reserves R, Boats B
WHERE S.sid = R.sid Scan
AND R.bid = B.bid
AND B.color = "red" Selection
GROUP BY S.sid
```

Sailors:

Hash, B+ tree indexes on sid

Reserves:

Clustered B+ tree on bid

B+ on *sid*

Boats

B+ on *color*

I preserve bid

can be for Join

Pass 1: Best plan(s) for each relation

Sailors, Reserves: File Scan

Also B+ tree on Reserves.bid as interesting order

Also B+ tree on Sailors.sid as interesting order

Boats: B+ tree on color for Selection

	Subset of tables in FROM clause	Interesting- order columns	Best plan	Cost
	{Sailors}		filescan	
	{Reserves}		Filescan	
	{Boats}	-	B-tree on color	
)	{Reserves}	(bid)	B-tree on bid	
-	{Sailors}	(sid)	B-tree on sid	

Pass 2

```
// for each left-deep logical plan
for each plan P in pass 1
 for each FROM table T not in P (others)
    // for each physical plan
   for each access method M on T
     for each join method generate P \bowtie M(T) \rightarrow cheap \circ R
          File Scan Reserves (outer) with Boats (inner)
                                                         (Riserves, bothin pass, but not other table)
          File Scan Reserves (outer) with Sailors (inner)
      Reserves Btree on bid (outer) with Boats (inner)
      Reserves Btree on bid (outer) with Sailors (inner)
          File Scan Sailors (outer) with Boats (inner)
          File Scan Sailors (outer) with Reserves (inner)
          Boats Btree on color with Sailors (inner)
          Boats Btree on color with Reserves (inner)
    Retain cheapest plan for each (pair of relations, order)
```

Subset of tables in FROM clause	Interesting- order columns	Best plan	Cost
{Sailors}		filescan	
{Reserves}		Filescan	
{Boats}		B-tree on color	
{Reserves}	(bid)	B-tree on bid	
{Sailors}	(sid)	B-tree on sid	
{Boats, Reserves}	(B.bid) (R.bid)	SortMerge(B-tree on Boats.color, filescan Reserves)	New
Etc			

Pass 3 and beyond

- Using Pass 2 plans as outer relations, generate plans for the next join in the same way as Pass 2
 - E.g. {SortMerge(B-tree on Boats.color, filescan Reserves)} (outer) |
 with Sailors (B-tree sid) (inner)
- Then, add cost for groupby/aggregate:
 - This is the cost to sort the result by sid, unless it has already been sorted by a previous operator.
- Then, choose the cheapest plan

```
SELECT S.sid, COUNT(*) AS number
FROM Sailors S, Reserves R, Boats B
WHERE S.sid = R.sid
AND R.bid = B.bid
AND B.color = "red"
GROUP BY S.sid
```

Now you understand the optimizer!

- Benefit #1: You could build one.
 - And you will!
- Benefit #2: You can influence one
 - People who write non-trivial SQL often get frustrated with the optimizer
 - It picked a crummy plan!
 - It didn't use the index I built!
 - · Etc.
 - Understanding the optimizer can lead you to:
 - Design your DB & Indexes better
 - Avoid "weak spots" in your optimizer's implementation
 - Coax your optimizer to do what you want