# CS150A Homework2 -- Coding

## **Instructions / Notes:**

## Read these carefully

- Please read all the points of the "Notes" sections- they're important for this homework!!!
- You are not required to do any plotting in this homework only in certain problems to provide the tuples that would generate a plot. You can then optionally plot (in the notebook with matplotlib, in Excel, wherever works)
- You may create new IPython notebook cells to use for e.g. testing, debugging, exploring, etc.- this is
  encouraged in fact!- just make sure that your final answer for each question is in its own cell and
  clearly indicated
- Have fun!

## **Problem 1: Double Trouble**

## [25 points total]

In this problem we'll explore an optimization often referred to as **double buffering**, which we'll use to speed up the **external merge sort algorithm**.

Although we haven't explicitly modeled it in many of our calculations so far, recall that *sequential IO* (i.e. involving reading from / writing to consecutive pages) is generally much faster that *random access IO* (any reading / writing that is not sequential). Additionally, on newer memory technologies like SSD reading data can be faster than writing data (if you want to read more about SSD access patterns look <a href="here">here</a> (<a href="http://codecapsule.com/2014/02/12/coding-for-ssds-part-5-access-patterns-and-system-optimizations/).

In other words, for example, if we read 8 consecutive pages from file A, this should be much faster than reading 1 page from A, then 1 page from file B, then the next page from A.

In this problem, we will begin to model this, by assuming that 8 sequential *READS* are "free", i.e. the total cost of 8 sequential reads is 1 IO. We will also assume that the writes are always twice as expensive as a read. Sequential writes are never free, therefore the cost of N writes is always 2N.

## Other important notes:

- NO REPACKING: Consider the external merge sort algorithm using the basic optimizations, but do not use the repacking optimization.
- ONE BUFFER PAGE RESERVED FOR OUTPUT: Assume we use one page for output in a merge, e.g. a
   B-way merge would require B + 1 buffer pages
- **REMEMBER TO ROUND:** Take ceilings (i.e. rounding up to nearest integer values) into account in this problem for full credit! Note that we have sometimes omitted these (for simplicity).
- Consider worst case cost: In other words, if 2 reads *could happen* to be sequential, but in general might not be, consider these random IO

## Part (a)

#### [15 points]

Consider a modification of the external merge sort algorithm where **reads are always read in 8-page chunks** (i.e. 8 pages sequentially at a time) so as to take advantage of sequential reads. Calculate the cost of performing the external merge sort for a setup having B+1=40 buffer pages and an unsorted input file with 320 pages.

Show the steps of your work and make sure to explain your reasoning by writing them as python comments above the final answers.

## Part (a.i)

What is the **exact** IO cost of spliting and sorting the files? As is standard we want runs of size B + 1.

## In [100]:

```
io_split_sort = 680
# split 320/8 = 40; sort 320*2 = 640; 640+40 = 680
```

## Part (a.ii)

After the file is split and sorted, we can merge n runs into 1 using the merge process. What is largest n we could have, given reads are always read in 8-page chunks? Note: this is known as the arity of the merge.

## In [101]:

```
merge_arity = 4
# floor(B/8) = 4
```

#### Part (a.iii)

How many passes of merging are required?

#### In [102]:

```
merge_passes = 3
# chunk number = 320/40 = 8; ceiling(log4(8)) + 1 = 3
```

#### Part (a.iv)

What is the IO cost of the first pass of merging? Note: the highest arity merge should always be used.

pass0: use B buffer pages, produce N/B sorted runs of B pages each

#### In [103]:

```
merge_pass_1 = 680
# pass 0: conquer (split)
# split 320/8 = 40; write/read 320*2 = 640; 640+40 = 680
```

## Part (a.v)

What is the total IO cost of running this external merge sort algorithm? **Do not forget to add in the remaining passes (if any) of merging.** 

## In [104]:

```
total_io = 2040

# pass 0: 680

# pass 1: 680

# pass 2: 680

# number of sort run differs of diff passes, but I/O not changed
```

## Part (b)

## [5 points]

Now, we'll generalize the reasoning above by writing a python function that computes the *approximate*\* cost of performing this version of external merge sort for a setup having B+1 buffer pages, a file with N pages, and where we now read in P-page chunks (replacing our fixed 8 page chunks in Part (a)).

\*Note: our approximation will be a small one- for simplicity, we'll assume that each pass of the merge phase has the same IO cost, when actually it can vary slightly... Everything else will be exact given our model!

We'll call this function  $external\_merge\_sort\_cost(B, N, P)$ , and we'll compute it as the product of the cost of reading in and writing out all the data (which we do each pass), and the number of passes we'll have to do.

Even though this is an approximation, make sure to take care of floor / ceiling operations- i.e. rounding down / up to integer values properly!

Importantly, to simplify your calculations: Your function will only be evaluated on cases where the following hold:

- (B + 1) % P == 0 (i.e. the buffer size is divisible by the chunk size)
- N % (B + 1) == 0 (i.e. the file size is divisible by the buffer size)

## Part (b.i)

First, let's write a python function that computes the **exact** total IO cost to create the initial runs:

## In [105]:

```
def cost_initial_runs(B, N, P):
    # YOUR CODE HERE
    # initial: split and read/wirte of all pages of the file
    # return (N/P + 2*N) or only split?
    return N/P + 2*N
```

## Part (b.ii)

Next, let's write a python function that computes the *approximate\** total IO cost to read in and then write out all the data during one pass of the merge:

#### In [106]:

```
def cost_per_pass(B, N, P):
    # YOUR CODE HERE
    # in every pass
    return 2*N + N/P
```

\*Note that this is an approximation: when we read in chunks during the merge phase, the cost per pass actually varies slightly due to 'rounding issues' when the file is split up into runs... but this is a small difference

#### Part (b.iii)

Next, let's write a python function that computes the exact total number of passes we'll need to do

## In [107]:

```
import math
def num_passes(B, N, P):
    # YOUR CODE HERE
    merge_arity = math.floor(B/P)
    # B+1 buffer pages
    return math.ceil(math.log(N/(B+1), merge_arity)) + 1
    # math.log(x[, base])
    # normal merge-sort: 1 + log(B-1, N/B)
```

Finally, our total cost function is:

```
In [108]:
```

```
def external_merge_sort_cost(B, N, P):
    return cost_initial_runs(B, N, P) + cost_per_pass(B, N, P)*num_passes(B, N, P)
```

## Part (c)

#### [10 points]

For B+1=100 and N=900, find the optimal P according to your IO cost equation above. Return both the optimal P value (  $P_{opt}$  ) and the list of tuples **for feasible values of** P that would generate a plot of P vs. IO cost, at resolution =1 (every value of P), stored as  $P_{oints}$ :

```
In [109]:
```

```
print(external_merge_sort_cost(99, 900, 12))
print(external_merge_sort_cost(99, 900, 11))
print(external_merge_sort_cost(99, 900, 10))
```

```
7500. 0
5645. 454545454545
5670. 0
```

## In [110]:

```
# Save the optimal value here
P = 11
# Save a list of tuples of (P, io_cost) here, for all feasible P's
# B+1 = 100
points = [(x, external_merge_sort_cost(99, 900, x)) for x in range(1,50)]
```

\*Below we provide starter code for using <code>matplotlib</code> in the notebook, if you want to generate the graph of P vs. IO cost; however any other software that allows you to visualize the plot (Excel, Google spreadsheets, MATLAB, etc) is fine!

## In [111]:

```
# Shell code for plotting in matplotlib
%matplotlib inline
import matplotlib.pyplot as plt

# Plot
plt.plot(*zip(*points))
plt.show()
```

## **Problem 2: IO Cost Models**

## [15 points total]

In this problem we consider different join algorithms when joining relations R(A, B), S(B, C), and T(C, D). We want to investigate the cost of various pairwise join plans and try to determine the best join strategy given some conditions.

Specifically, for each part of this question, we are intereseted determining some (or all) of the following variables:

- PR: Number of pages of R
- PS: Number of pages of S
- P\_RS : Number of pages of output (and input) RS
- P\_T : Number of pages of T
- P\_RST: Number of pages of output (and input) RST
- B: Number of pages in buffer
- I0 cost join1: Total IO cost of first join
- I0\_cost\_join2 : Total IO cost of second join

## Note:

- \*\* The output of join1 is always feed as one of the inputs to join 2 \*\*
- Use the "vanilla" versions of the algorithms as presented in lecture, i.e. without any of the optimizations we mentioned
- · Again assume we use one page for output, as in lecture!
- \*\* The abbreviates for the joins used are Sort-Merge Join (SMJ), Hash Join (HJ), and Block Nested Loop Join (BNLJ). \*\*

## Part (a)

## [8 points]

#### Given:

- P\_R: 20
- PS:200
- P\_T: 2000
- P RS: 100
- P\_ST: 1000
- P\_RST: 500
- B: 32

## Compute the IO cost for the following query plans:

- IO\_Cost\_HJ\_1 where only hash join is used, join1 = R(a, b), S(b, c) and join2 = join1(a, b, c), T(c, d)
- IO\_Cost\_HJ\_2 where only hash join is used, join1 = T(c, d), S(b, c) and join2 = join1(b, c, d), R(a, b)
- IO\_Cost\_SMJ\_1 where only sort merge join is used, join1 = R(a, b), S(b, c) and join2 = join1(a, b, c), T(c, d)
- IO\_Cost\_SMJ\_2 where only sort merge join is used, join1 = T(c, d), S(b, c) and join2 = join1(b, c, d), R(a, b)
- IO\_Cost\_BNLJ\_1 where only block nested loop join is used, join1 = R(a, b), S(b, c) and join2 = join1(a, b, c), T(c, d)
- IO\_Cost\_BNLJ\_2 where only block nested loop merge join is used, join1 = T(c, d), S(b, c) and join2 = join1(b, c, d), R(a, b)

#### Note: again, be careful of rounding for this problem. Use ceiling/floors whenever it is necessary.

Include 1-2 sentences (as a python comment) above each answer explaining the performance for each algorithm/query plan.

In [112]:

```
# cost of 2-pass hash join: 3([R]+[S])
# Need to count the save cost (write in size of output)
IO Cost HJ 1 = 7560
# 3*(P R+P S) + P RS + 3*(P RS+P T) + P RST = 3*(20+200) + 100 + 3*(100+2000) + 500 = 7560
# 3*(P R+P S) + P RS + 3*(P RS+P T) + P RST = 3*(20+200) + 100 + 3*(100+2000) = 7060 (not consider t
IO Cost HJ 2 = 11160
# 3*(P T+P S) + P ST + 3*(P ST+P R) + P RST = 3*(2000+20) + 1000 + 3*(1000+20) + 500 = 11160
#3*(PT+PS) + PST + 3*(PST+PR) + PRST = 3*(2000+20) + 1000 + 3*(1000+20) = 10660 (not consider
\# cost of sort-merge: 2*N*ceil(1+log(B-1, N/B))
\# cost of sort-merge join: sort(R) + sort(S) + ([R]+[S])
IO Cost SMJ 1 = 16160
\# sort(P_R) = 2*20*(1+ceil(log(31, 20/32))) = 40
\# \text{ sort}(P S) = 2*200*(1+\text{ceil}(\log(31,200/32))) = 800
# RS is sorted
\# \text{ sort}(P T) = 2*2000*(1+\text{ceil}(\log(31,2000/32))) = 12000
# save cost included
# consider save RS cost and save RST cost and sort RS cost and read RS cost:
\# sort (P RS) = 2*100*2=400
# sort(P_R) + sort(P_S) + P_R + P_S + P_RS + sort(P_T) + sort(P_RS)+ P_RS + P_T + P_RST
# = 40 + 800 + 20 + 200 + 100 + 400 + 100 + 12000 + 2000 + 500 = 16160
# for RS, no need to read or sort again? (dismiss this)
# sort(P_R) + sort(P_S) + P_R + P_S + P_RS + sort(P_T) + P_T + P_RST
# consider save RS cost and save RST cost
\# = 40 + 800 + 20 + 200 + 100 + 12000 + 2000 + 500 = 15660
IO Cost SMJ 2 = 23560
\# \text{ sort}(P T) = 2*2000*(1+\text{ceil}(\log(31,20/32))) = 12000
\# \text{ sort}(P S) = 2*200*(1+\text{ceil}(\log(31,200/32))) = 800
\# \text{ sort}(P R) = 2*20*(1+\text{ceil}(\log(31,2000/32))) = 40
\# \text{ sort}(P \text{ ST}) = 2*1000*(1+\text{ceil}(\log(31,1000/32))) = 6000
# save cost included
# sort(P T) + sort(P S) + P T + P S + P TS + sort(P ST) + sort(P R) + P ST + P R + P RST
\# = 12000 + 800 + 2000 + 200 + 1000 + 6000 + 40 + 1000 + 20 + 500 = 23560
# for TS, no need to read or sort again? (dismiss this)
# sort(P_T) + sort(P_S) + P_T + P_S + P_TS + sort(P_R) + P_R + P_RST
# consider save RS cost and save RST cost
\# = 12000 + 800 + 2000 + 200 + 1000 + 40 + 20 + 500 = 16560
# cost of block nested loop join:
IO Cost BNLJ 1 = 8920
\# \cos t = [R] + ceil([R]/(B-2))*[S]
# P R + cei1(P R/(B-2))*P S + P RS + P RS + cei1(P RS/(B-2))*P T + P RST
\# = 20 + ceil(20/30)*200 + 100 + 100 + ceil(100/30)*2000 + 500 = 8920
# cost of nested loop merge join:
IO Cost BNLJ 2 = 16720
# P S + cei1(P S/(B-2))*P T + P ST + P R + cei1(P R/(B-2))*P ST + P RST
# = 200 + \text{ceil}(200/30)*2000 + 1000 + 20 + \text{ceil}(20/30)*1000 + 500 = 16720
```

## Part (b)

For the query plan where join1 = R(a, b), S(b, c) and join2 = join1(a, b, c), T(c, d) find a configuration where using HJ for join1 and SMJ for join2 is cheaper than SMJ for join1 and HJ for join2. The output sizes you choose for P\_RS and P\_RS must be non-zero and feasible (e.g. the maximum output size of join1 is P\_R\*P\_S).

## [8 points]

```
In [113]:
```

```
P R = 200
P S = 200
P T = 100
P RS = 100
P RST = 100
B = 10
# cost of 2-pass hash join: 3([R]+[S])
# cost of sort-merge: 2*N*ceil(1+log(B-1, N/B))
\# sort(R) = 2*200*ceil(1+log(10-1,200/10)) = 1200
\# \text{ sort}(S) = 2*200*ceil(1+log(10-1,200/10)) = 1200
\# \text{ sort}(T) = 2*100*\text{ceil}(1+\log(10-1,100/10)) = 600
\# \text{ sort}(RS) = 2*100*ceil(1+log(10-1,100/10)) = 600
\# cost of sort-merge join: sort(R) + sort(S) + ([R]+[S])
HJ IO Cost join1 = 1000
# 3*(P R+P S) + P RS
SMJ IO Cost join2 = 1500
# sort(RS) + sort(T) + P_RS + P_T + P_RST
SMJ IO Cost join1 = 2900
\# sort(R) + sort(S) + P_R + P S + P RS
HJ IO Cost join2 = 1000
# 3*(P RS+P T) + P RST
```

# **Problem 3: Sequential Flooding**

## [10 points total]

Note: Before doing this question, it is highly recommended that you go through <u>Activity 15 (./Activity-15.ipynb)</u>, which covers eviction policies for buffer managers such as LRU, and why sequential flooding can sometimes occurs with LRU.

In the activity accompanying Lecture, we saw something called *sequential flooding* that can occur when a default eviction policy (for example LRU) is used by the buffer manager. We saw that we can achieve much lower IO cost by using a different eviction policy, MRU ("most recently used").

Note that "Most recently used" means most recently accessed, either from buffer or disk, consistent with what we showed in Activity-15.

For this problem, we will take a closer look at the IO cost of different eviction policies when reading the pages of a file sequentially multiple times.

## Part (a)

## Part (a.i)

## [1 point]

Write a python function  $1 \text{ru\_cost}(N, M, B)$  that computes the IO cost of the LRU eviction policy when reading in all the papers of an N-page file sequentially, M times, using a bugger with B+1 pages. Assume that after reading the files, you don't need to write them out (you can just release them, so there is no write IO cost).

## In [114]:

```
def lru_cost(N, M, B):
    if N > B+1: return M*N
    else: return N

# Discards the least recently used items first
# if N page can not fit into the B+1, no hits, M*N in worse case for LRU
# example: after read 1-N for M1, reading 1 in M2, 1 from M1 is discarded for that it is the least r
# if N page can fit into B+1, hits everytime, N
```

## Part (a.ii)

## [2 points]

Write a python function  $mru\_cost(N, M, B)$  that computes the IO cost of the MRU eviction policy when reading in all the papers of an N-page file sequentially, M times, using a buffer with B+1 pages. Assume that after reading the files, you don't need to write them out (you can just release them, so there is no write IO cost).

#### In [115]:

```
def mru_cost(N, M, B):
    cost = 0
    if N>B+1:
       buffer ids = []
       mr_pos = 0
        for time in range (0, M):
            for pid in range (0, N):
                # if in the buffer, not cost
                if pid not in buffer ids:
                    # when buffer not full, just append
                    if len(buffer ids) < B+1: buffer ids.append(pid)
                    # when full, MRU
                    else: buffer ids[mr pos] = pid
                    # write cost for this new page
                    cost = 1
                # upadate most recent position
                mr pos = buffer ids.index(pid)
    else: cost = N
    return cost
# MRU discards the most recently used items first
# if N page can not fit into the B+1, MRU
# if N page can fit into B+1, hits everytime, N
```

## Part (a.iii)

#### [2 points]

Now that you have written these functions, provide the tuples which generate the plot of **M vs. the absolute** value of the difference between LRU and MRU in terms of IO cost for B=4, N=7, and M between 1 and 20 inclusive (saved as the variable  $p3\ 1ru\ points$ )

```
In [116]:
```

```
B = 4
N = 7
M = 20

# Provide a list of tuple (m, difference between LRU and MRU in terms of IO cost) here:
p3_lru_points = [(m, abs(lru_cost(7, m, 4) - mru_cost(7, m, 4))) for m in range(1, 21)]
```

Again, you can optionally plot your answer to check that it seems reasonable- starter code for doing this in the notebook below:

## In [117]:

```
# Shell code for plotting in matplotlib
%matplotlib inline
import matplotlib.pyplot as plt

# Plot
plt.plot(*zip(*p3_lru_points))
plt.show()
```

## Part (b)

Recall that the LRU eviction policy removes the least recently used page when the buffer is full and a new page is referenced which is not there in buffer. The basic idea behind LRU is that you timestamp your buffer elements, and use the timestamps to decide when to evict elements. Doing so efficiently, requires some serious book-keeping, this is why in practice many buffer managers try to approximate LRU with other eviction policies that are easier to implement.

Here we will focus on the *CLOCK* or *Second Chance* policy. In the CLOCK eviction policy, the candidate pages for removal are considered left-to-right in a circular manner(with wraparound), and a page that has been accessed between consecutive considerations will not be replaced. The page replaced is the one that - considered in a circular manner - has not been accessed since its last consideration.

In more details the CLOCK policy proceeds maintains a circular list of pages in the buffer and uses an additional *clock* (or second chance) bit for each page to track how often a page is accessed. The bit is set to 1 whenever a page is referenced. When clock needs to read in a new page in the buffer, it sweeps over existing pages in the buffer looking for one with second chance bit set to 0. It basically replaces pages that have not been referenced for one complete revolution of the clock.

A high-level implementation of clock:

- 1. Associate a "second chance" bit with each page in the buffer. Initialize all bits to ZERO (0).
- 2. Each time a page is referenced in the buffer, set the "second chance" bit to ONE (1). this will give the page a second chance...
- 3. A new page read into a buffer page has the second chance bit set to ZERO (0).

- 4. When you need to find a page for removal, look in left-to-right in a circular manner(with wraparound) in the buffer pages:
  - If the second chance bit is ONE, reset its second chance bit (to ZERO) and continue.
  - If the second chance bit is ZERO, replace the page in the buffer.

You can find more details on CLOCK <a href="http://cseweb.ucsd.edu/classes/wi08/cse221-a/papers/carr81.pdf">here (http://cseweb.ucsd.edu/classes/wi08/cse221-a/papers/carr81.pdf)</a>.

## Part (b.i)

## [4 points]

Write a python function  $clock\_cost(N, M, B)$  that computes the IO cost of the CLOCK eviction policy when reading in all the papers of an N-page file sequentially, M times, using a bugger with B+1 pages. Assume that after reading the files, you don't need to write them out (you can just release them, so there is no write IO cost).

## In [118]:

```
def clock_cost(N, M, B):
    if N > B+1: return M*N
    else: return N
# if N page can not fit into the B+1, no hits, M*N in worse case for CLOCK
# if N page can fit into B+1, hits everytime, N
```

## Part (b.ii)

## [1 point]

Now that you have written the CLOCK cost function, provide the tuples which generate the plot of **M vs. the** absolute value of the difference between LRU and CLOCK in terms of IO cost for B=4, N=7, and M between 1 and 20 inclusive (saved as the variable  $p3\_clock\_points$ ).

```
In [119]:
```

```
B = 4

N = 7

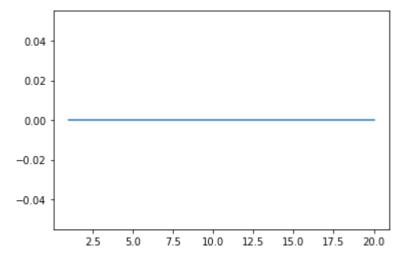
M = 20

p3_clock_points = [(m, abs(lru_cost(7, m, 4)-clock_cost(7, m, 4))) for m in range(1, 21)]
```

#### In [120]:

```
# Shell code for plotting in matplotlib
%matplotlib inline
import matplotlib.pyplot as plt

# Plot
plt.plot(*zip(*p3_clock_points))
plt.show()
```



Does the CLOCK eviction policy prevent sequential flooding? How does it perform against LRU? Write a short explanation in the field below.

```
In [121]:
```

```
# EXPLANATION GOES HERE

# It does not prevent sequential flooding

# It performs samilarly with LRU

# CLOCK's pin depending style just like LRU (least recent = least pinned)
```

## **Problem 4: Hash Join Madden**

## [10 points total]

The NFL season has started strong and Jack Del Rio (The Oakland Raider's (https://www.youtube.com/watch? v=YXj7I1RzLSE) coach) wants to find out if Joe Flacco is an elite quarterback. He wants to do this by being more of a sabermetrics guy than a numbers guy. As a first step in doing this he wants to find out which are the colleges each NFL teams prefers drafting players from. We have access to two tables: (i) a table named "teams" which contains (team, player) pairs, and (ii) a table named "colleges" which contains (player, college) pairs. Being all excited about databases you decide that there is no other way but to join the two tables and get the desired results. However, you have no access to a database. Not even a challenge for you who decide to implement your favorite join algorithm on your own. And of course HASH JOIN is the way to go!!!

# Load and explore the data

The two tables are stored in files which can be loaded into memory as two lists of **named tuples** using the code below:

```
In [122]:
```

```
# Load data
import nfl
from nfl import *
teams, colleges = loadData()
```

Named tuples are basically lightweight object types and instances of named tuple instances can be referenced using object like variable deferencing or the standard tuple syntax. The following code prints the first 10 tuples from teams and colleges. *Notice how fields of named tuples are accessed inside the loops.* 

## In [123]:

```
# Print List Entries
print ('Table teams contains %d entries in total' % len(teams))
print ('Table colleges contains %d entries in total' % len(colleges))
print ()
print ('First 10 entries in teams table')
for i in range(10):
    team = teams[i]
    print ('Entry %d' %(i+1),':', team. teamname, '|', team. playername)
print ()
print ('First 10 entries in college table')
for i in range(10):
    college = colleges[i]
    print ('Entry %d' %(i+1),':', college. collegename, '|', college. playername)
```

## Down to business

During the lectures we saw that hash joins consist of two phases: The **Partition Phase** where using a hash function h we split the two tables we want to join into B buckets, and the **Matching Phase** where we iterate over each bucket and join the tuples from the two tables that match. Here you will need to implement a hash join in memory.

You are determined to implement the most efficient hash join possible! This is why you decide to implement your own hash function that will uniformly partition the entries of a table across B buckets so that all buckets have roughly the same number of entries. You decide to use the following hash function:

```
In [124]:
```

```
# Define hash function
def h(x, buckets):
   rawKey = ord(x[1])
   return rawKey % buckets
```

You use this hash function to partition the tables. To do so you can use the helper method partitionTable (table, hashfunction, buckets) for convenience as shown next:

```
In [125]:
```

```
# Fix the number of buckets to 500
buckets = 500
# Partition the teams table using hash function h
teamsPartition = partitionTable(teams, h, buckets)
```

The output of partitionTable() is a dictionary with its keys corresponding to bucket numbers in [0, B-1] and its entries to lists of named tuples.

## Part (a)

## Part (a.i)

## [4 points]

It's now time to implement your own hash join! You only need to implement the merge phase of the hash join. The output of the method should correspond to the result of a join between teams and colleges over the *playername* attribute. The partition phase is implemented. You need to fill in the merge phase.

Note: You should only use the two dictionaries t1Partition and t1Partition provide. No other data structures are allowed.

## In [126]:

```
def hashJoin(table1, table2, hashfunction, buckets):
    # Parition phase
    t1Partition = partitionTable(table1, hashfunction, buckets)
    t2Partition = partitionTable(table2, hashfunction, buckets)
    # Merge phase
    result = []
    for i in range(0, buckets):
        for t1e in t1Partition[i]:
            for t2e in t2Partition[i]:
                if t1e.playername == t2e.playername:
                      result.append((t1e.teamname, t1e.playername, t2e.collegename))
# ANSWER GOES HERE
# To populate your output you should use the following code(t1Entry and t2Entry are possible var
# result.append((t1Entry.teamname, t1Entry.playername, t2Entry.collegename))
    return result
```

## Part (a.ii)

## [1 point]

It time to evaluate your algorithm! The code provided below executes the join between teams and colleges and measures the total execution time. What is the total number of entries output by your algorithm?

Does the runtime of your algorithm seem reasonable? Provide a brief explanation.

## In [127]:

```
import time
start_time = time.time()
res1 = hashJoin(teams, colleges, h, buckets)
end_time = time.time()
duration = (end_time - start_time)*1000 #in ms
print ('The join took %0.2f ms and returned %d tuples in total' % (duration, len(res1)))
# EXPLANATION GOES HERE
# The join took 1295.57 ms and returned 12740 tuples in total
# the runtime of it seems not reasonable. It is bit slow
# The hash function does not make output uniform in distribution across buckets
```

# Part (b)

You decide to investigate the performance of hashJoin() further. Since you implemented the merge phase of hashJoin() yourself you focus on the partitioning obtained by using the provided hash function h(). In the lectures we saw that a good hash function should partition entries uniformly across buckets. We will now check if h() is indeed a good function.

The following code generates a histogram of the bucket sizes for table teams (using the above hash function h and 500 buckets) to help figure out what is going wrong.

#### In [128]:

```
# Examine if this is a good partition function
def histogramPoints(partition):
    ids = range(buckets)
    items = []
    for i in range (buckets):
        if i in partition:
            items.append(len(partition[i]))
        else:
            items. append (0)
    return ids, items
%matplotlib inline
import matplotlib.pyplot as plt
# Plot bucket histogram
buckets = 500
teamsPartition = partitionTable(teams, h, buckets)
ids, counts = histogramPoints(teamsPartition)
plt.plot(ids, counts)
plt.plot()
```

## Part (b.i)

## [3 points]

Now find the skew associated with the above histogram. Skew is defined as the standard deviation of the number of entries in the buckets. A uniform hash function produces buckets of equal size, leading to 0 skew, but our candidate hash function h is imperfect so you should observe a positive skew.

#### In [129]:

```
# ANSWER
# partition- a table partition as returned by method partitionTable
# return value - a float representing the skew of hash function (i.e. stdev of chefs assigned to eac
def calculateSkew(partition):
    # ANSWER STARTS HERE
    sum_all = sum([len(partition[i]) for i in range(0, len(partition))])
    mean = sum_all / len(partition)
    skew = math.sqrt(sum([(len(partition[i])-mean)**2 for i in range(0, len(partition))])/len(partition) # ANSWER ENDS HERE
    return skew

print (calculateSkew(teamsPartition))
    ...
```

## Part (b.ii)

## [1 point]

Use python's hash function to see if you can produce a better (aka smaller) runtime for hash join. As at the beginning of part b, make a histogram of the bucket sizes (this time using the new hash function and 500 buckets). You can plot your histogram using the same code provided above.

#### In [130]:

```
# Design a better hash function and print the skew difference for
def hBetter(x, buckets):
    rawKey = hash(x)  #ANSWER GOES HERE
    return rawKey % buckets

# Plot bucket histogram
buckets = 500
teamsPartition = partitionTable(teams, hBetter, buckets)
ids, counts = histogramPoints(teamsPartition)
plt.plot(ids, counts)
plt.plot()
```

## Part (b.iii)

## [1 point]

Rerun your hash join algorithm with the new hash function you designed and 500 buckets. Does the algorithm run faster? If so what is the speed-up you are observing?

## In [131]:

```
start_time = time.time()
res1 = hashJoin(teams, colleges, hBetter, buckets) # ENTER CODE HERE
end_time = time.time()
duration = (end_time - start_time)*1000 #in ms
print ('The join took %0.2f ms and returned %d tuples in total' % (duration, len(res1)))
# WRITE DOWN THE SPEED UP
```

# Part (c)

## [0 points]

For our internal sabermetrics purposes. Is Joe Flacco an elite quarterback? (True for elite, False for not elite)

```
In [132]:
```

```
flacco_elite = '誰か'
```