



Outline

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CSE331: Automata and Computability

Quiz 4 SET: A Total Marks: 36

Allocated Time: 30 minutes

Name:

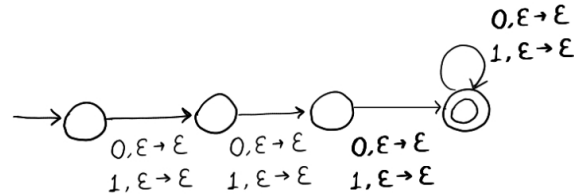
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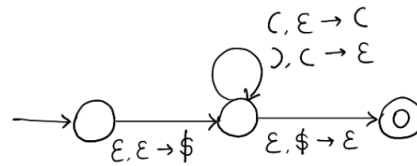
Obtained Marks

Construct Pushdown Automata for the following languages. Each question carries 6 marks.

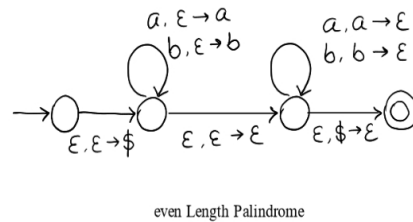
a)  $L = \{w \in \{0,1\}^* : \text{length of } w \text{ is at least three.}\}$  [Hint: Recall what kind of language  $L$  is.]



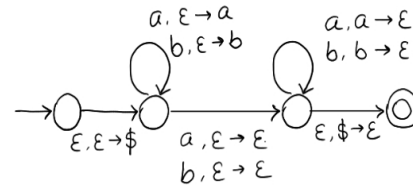
b)  $L = \{w \in \{ (, ) \}^* : w \text{ is a valid parenthesis}\}$



c)  $L = \{w \in \{a, b\}^* : w \text{ is a even length palindrome}\} / L = \{w \in \{a, b\}^* : w \text{ is a odd length palindrome}\}$



even Length Palindrome



odd Length Palindrome

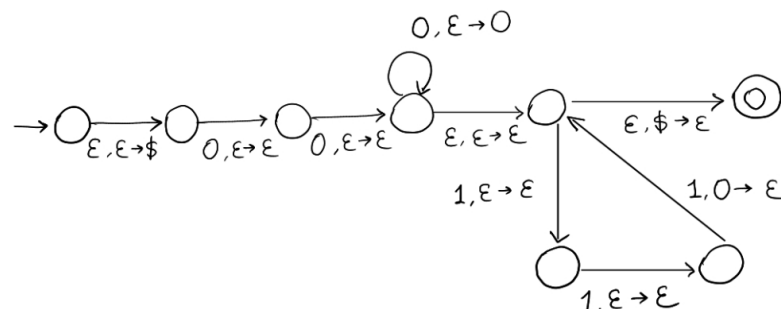
1

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d)  $L = \{w \in \{0,1\}^* : 0^{n+2}1^{3n}, \text{ where } n \geq 0\}$

$$0^{n+2}1^{3n} \Rightarrow 0^2 0^n 1^{3n}$$

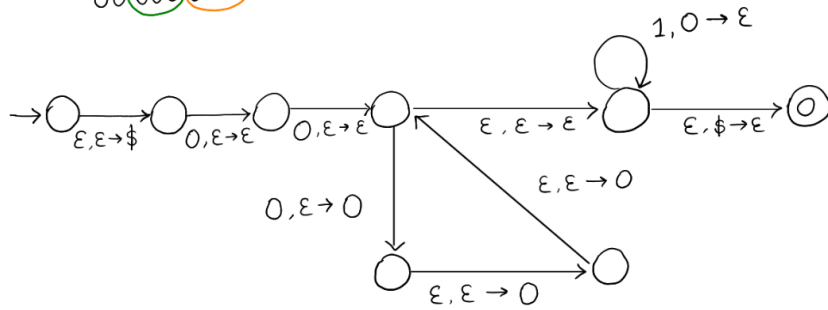
$n=0 : 00$   
 $n=1 : 000111$   
 $n=2 : 000111111$



e)  $L = \{w \in \{0,1\}^* : 0^{n+2}1^{3n}, \text{ where } n \geq 0\}$  [Alternate Solution Idea of Qc(c)]

2) Let  $\Sigma = \{0, 1\}$ ,  $n \in \mathbb{N}$ , where  $n \leq 3$ . Give finite automaton for  $L_n = \{w \in \Sigma^* : |w| = n\}$

$n=2$ , 0000 1111 11  
00(000)000 111111

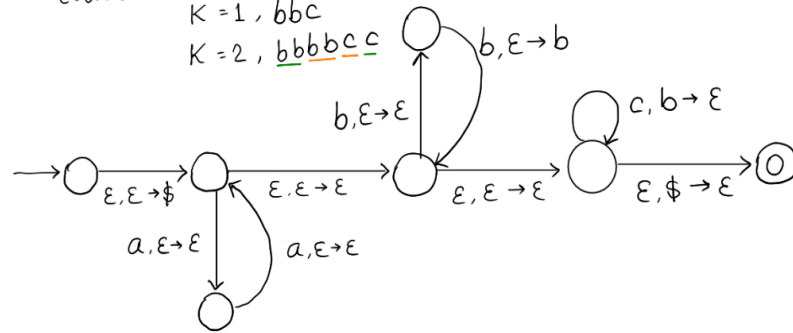


2

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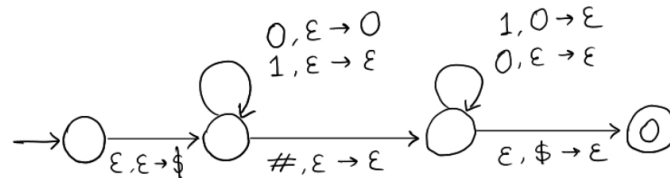
f)  $L = \{w \in \{a, b, c\}^* : a^i b^j c^k, \text{ where } i \text{ is even, } j = 2k \text{ and } i, j, k \geq 0\}$

$a^i b^j c^k, j=2k$   
 $\Rightarrow a^i b^{2k} c^k$   
even  $a$   $\downarrow$   $\downarrow$   
 $K=0, \epsilon$   
 $K=1, b b c$   
 $K=2, b b b b c c$



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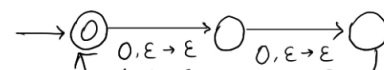
g) Let  $\Sigma = \{0, 1, \#\}$ .  $L = \{w_1 \# w_2 \mid \text{number of 0s in } w_1 \text{ is equal to number of 1s in } w_2\}$



3

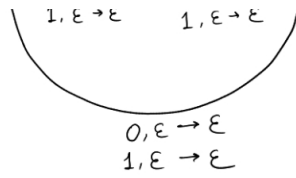
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h)  $L = \{w \in \{0,1\}^* : \text{length of } w \text{ is multiple of three}\}$  [Hint: Recall what kind of language L is.]

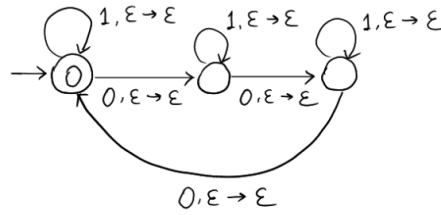


הערה: תוכן זה יופיע כאן.

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i)  $L = \{w \in \{0,1\}^*: \text{number of 0s in } w \text{ is multiple of three}\}$  [Hint: Recall what kind of language  $L$  is.]



j)  $L = \{w \in \{0,1\}^*: \text{length of } w \text{ is at most two}\}$  [Hint: Recall what kind of language  $L$  is.]

