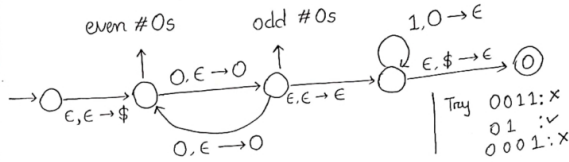


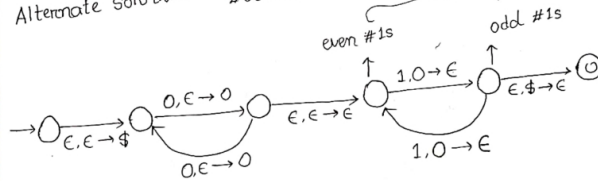
Pushdown Automata (PDA)

we will have same amount of 0s & 1s and n is odd

$$L = \{w \in \{0,1\}^* : w = 0^n 1^n, \text{ where } n \text{ is odd}, n \geq 0\}$$

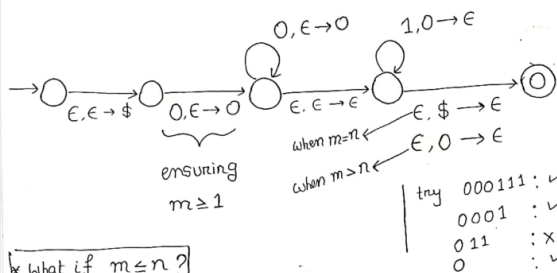


Previously, we simply counted the # 1s, which was enough. Because, if #0s = #1s, then their parity will be same. However, you can do this as well.



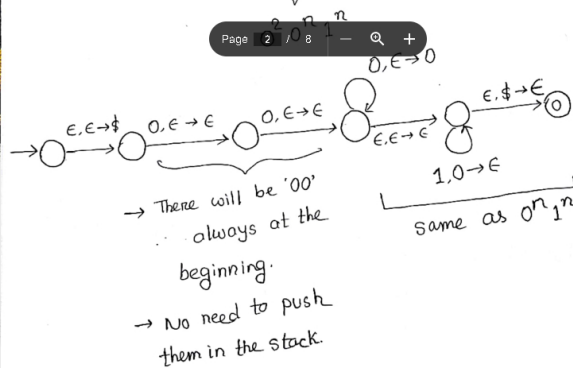
* what if $L = \{w \in \{0,1\}^* : w = 0^m 1^n, \text{ where } m \text{ and } n \text{ are odd}\}$

$$L = \{w \in \{0,1\}^* : w = 0^m 1^n, \text{ where } m \geq 1, n \geq 0, \text{ and } m \geq n\}$$

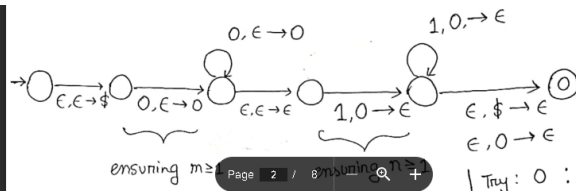


What if $m \leq n$?

$$L = \{w \in \{0,1\}^* : w = 0^{2+n} 1^n, \text{ where } n \geq 0\}$$



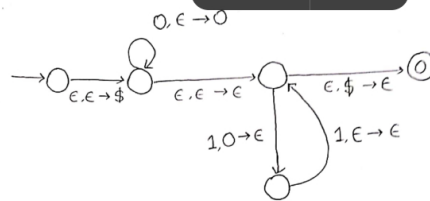
$$L = \{w \in \{0,1\}^* : w = 0^m 1^n, \text{ where } m, n \geq 1, \text{ and } m \geq n\}$$



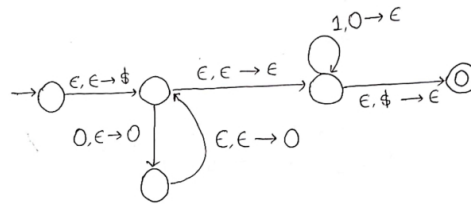
compare the problem with

$$L = \{w = 0^m 1^n, \text{ where } m \geq 1, n \geq 0, \text{ and } m \geq n\}$$

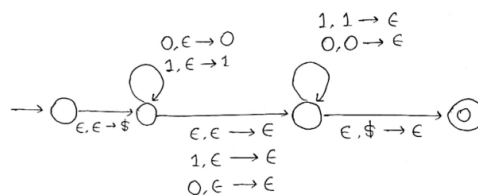
$$L = \{w \in \{0,1\}^* : w = 0^n 1^{2n}, \text{ where } n \geq 0\}$$



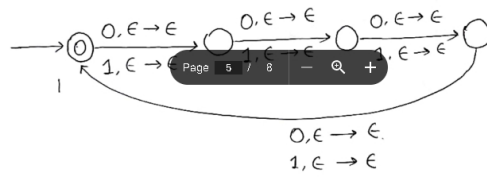
Alternate solution:



$$L = \{w \in \{0,1\}^* : w \text{ is a palindrome}\}$$



$L = \{ \omega \in \{0,1\}^* : \omega \mid \text{the length of } \omega \text{ is multiple of four} \}$



Since the language is regular, we don't have to use the stack. If you use stack, it is also fine. 'use the stack' means, pushing and popping element from the stack.

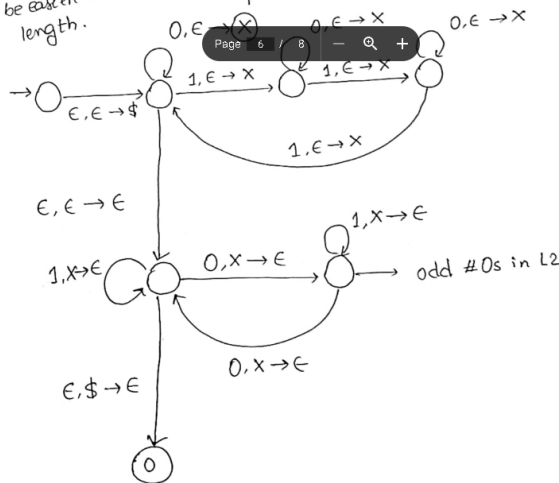
$L_1 = \#1s \text{ in } \omega \text{ is multiple of 3}$

$L_2 = \omega \text{ contains even \#0s}$

$L = L_1 \cap L_2 = \{ \omega : \omega = uv, \text{ where } u \in L_1, v \in L_2 \rightarrow \text{regular} \}$
 $|u| = |v| \rightarrow \text{non regular}$

Inserting a common element for both 0 and 1, it will be easier to count the length.

we will use stack to count the lengths one equal

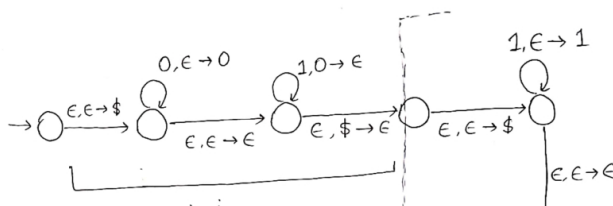


$L = \{ \omega \in \{0,1\}^* : \omega = 0^i 1^j 0^k \mid j = i+k \text{ and } i, k \geq 0 \}$

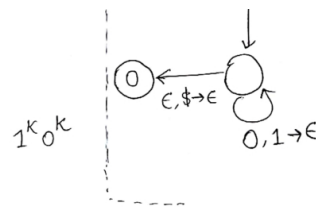
$$= 0^i 1^j 0^k$$

$$= 0^i 1^{i+k} 0^k$$

$$= \underline{0^i 1^i} 1^k 0^k$$



$0^L 1^L$



$$L = \{ \omega \bar{\omega}^R : \omega \in \{0,1\}^* \}$$

for example, $\omega = 0100$

complement of $\omega = \bar{\omega} = 1011$

reverse of $\bar{\omega} = \bar{\omega}^R = 1101$

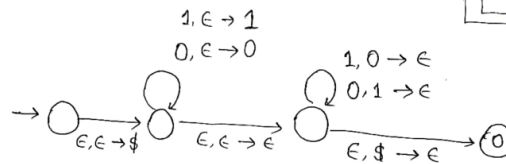
Doing $\omega \rightarrow \bar{\omega}^R$
will be same thing

$$\omega \bar{\omega}^R = 01001101$$

this is even length
↑
palindrome

first think how to solve: $\omega \bar{\omega}^R = 01001101$
so if we complement the part

$$\omega \bar{\omega}^R = 01001101$$



Alternate solution:

