



Outline

Headings you add to the document will appear here.

CSE331: Automata and Computability

Quiz 3 SET: A Total Marks: 40

Allocated Time: 30 minutes

Name:

ID:

Section and Serial:

Obtained Marks

1 of 2

Part A: Context-Free Grammar [Each question contains 4 points. 5*4 = 20]

a) $L = \{w \in \{(,)\}^*: w \text{ is a valid parenthesis.}\}$

$$S \rightarrow (S) \mid SS \mid \epsilon$$

d) $L = \{w \in \{a, b, 1\}^*: a^n 1^{2n+m+3} b^m, \text{ where } n, m \geq 0\}$

$$\begin{aligned} & a^n 1^{2n+m+3} b^m \\ \Rightarrow & a^n 1^{2n} 1^m 1^3 b^m \quad \text{or} \quad a^n 1^{2n} 1^3 1^m b^m \\ S & \rightarrow PQ \\ P & \rightarrow aP11 \mid \epsilon \\ Q & \rightarrow 1Qb \mid 111 \end{aligned}$$

b) Convert the following Regular Expressions into a CFG: $((aa+bc)^* a)^* + cb$

$$\begin{aligned} & ((aa+bc)^* a)^* + cb \\ S & \rightarrow X \mid Y \\ X & \rightarrow PX \mid \epsilon \\ P & \rightarrow Ma \\ M & \rightarrow FM \mid \epsilon \\ F & \rightarrow aa \mid bc \\ Y & \rightarrow cb \end{aligned}$$

c) $L = \{w \in \{0, 1\}^*: \text{length of } w \text{ is odd and the mid is } 1.\}$

$$S \rightarrow 0S0 \mid 0S1 \mid 1S0 \mid 1S1 \mid 1$$

$$\text{or, } S \rightarrow XSX \mid 1$$

$$X \rightarrow 0 \mid 1$$

Wrong Solve:

$$S \rightarrow A1A$$

$$A \rightarrow 0A \mid 1A \mid \epsilon$$

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d) $L = \{w \in \{0, 1\}^*: w \text{ is an odd-length palindrome.}\}$

$$S \rightarrow 0S0 \mid 1S1 \mid 0 \mid 1$$

d) $L = \{w \in \{0, 1\}^*: w \text{ is an even-length palindrome.}\}$

$$S \rightarrow 0S0 \mid 1S1 \mid \epsilon$$

e) $L = \{w \in \{0, 1\}^*: \text{the length of } w \text{ is three more than the multiple of four.}\}$

$$\begin{aligned} A & \rightarrow MMMMA \mid MMM \\ M & \rightarrow 0 \mid 1 \end{aligned}$$

f) $L = \{w \in \{0, 1\}^*: \text{the length of } w \text{ is two more than the multiple of three.}\}$

$$\begin{aligned} A & \rightarrow MMMA \mid MM \\ M & \rightarrow 0 \mid 1 \end{aligned}$$

meanings you add to the document will appear here.

[Solve the parse tree questions by your own.]