$$\frac{\alpha Q}{\alpha \beta} = \sum_{i=1}^{n} 2wi(yi - \beta xi)(-xi) = 0$$

$$\sum_{i=1}^{n} wixi(\beta xi - yi) = 0$$

$$\sum_{i=1}^{n} wi\beta xi^{2} = \sum_{i=1}^{n} wixiyi$$

$$\beta = \sum_{i=1}^{n} \frac{\sum_{i=1}^{n} wixiyi}{\sum_{i=1}^{n} wixi^{2}}$$

2.8  
If 
$$r = 0.25$$
  
 $y1 - 69 = 0.25(x1 - 68)$   $y1 = 70$   
 $y2 - 69 = 0.25(x2 - 68)$   $y2 = 68$   
if  $r = 0.75$   
 $y1 - 69 = 0.75(x1 - 68)$   $y1 = 72$   
 $y2 - 69 = 0.75(x2 - 68)$   $y2 = 66$ 

r	0.25	0.5	0.75
y1	70	71	72
y2	68	67	66

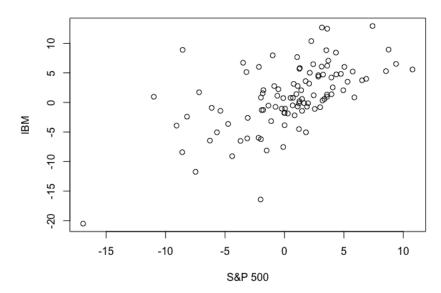
Conclusion: With r increasing, the degree of regression to mean decreases.

## 2.9

```
a)

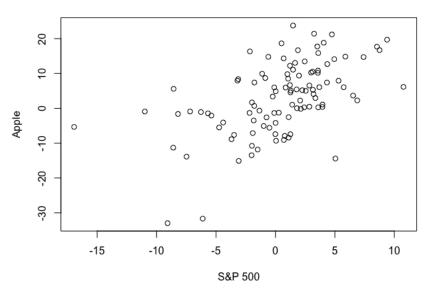
1  #2.9
2  #a)
3  #read file from csv
4  return = read.csv("Desktop/Predictive Analytics/Assignment/1/IBM-Apple-SP500 RR Data.csv",skip = 1)
5  #turn the type of "date" from factor to numeric
7  sp = as.numeric(str_replace(return$S.P.500,"%",""))
8  ibm = as.numeric(str_replace(return$IBM,"%",""))
9  apple = as.numeric(str_replace(return$Apple,"%",""))
10
11  #plot
12  plot(sp,ibm,xlab = 'S&P 500',ylab = 'IBM',main = 'IBM vs S&P 500')
13  plot(sp,apple,xlab = 'S&P 500',ylab = 'Apple',main = 'Apple vs S&P 500')
14
```

#### IBM vs S&P 500



Comment: The return rate between IBM and S&P 500 are positively linear correlated. Return rates mostly concentrate between 0 and 5%.





Comment: The return rate between Apple and S&P 500 are positively linear correlated. Return Rates mostly concentrate between 0 and 10%

```
b)
16 #b)
17 #regression for ibm
18 fit1=lm(ibm~sp)
19 summary(fit1)
20
```

```
Call:
lm(formula = ibm \sim sp)
Residuals:
     Min
              1Q Median
                               3Q
                                       Max
-15.5646 -2.4261 -0.6636 2.2188 14.6414
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 0.64164
                       0.44136 1.454 0.149
                       0.09898 7.525 2.15e-11 ***
            0.74481
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 4.478 on 102 degrees of freedom
Multiple R-squared: 0.357, Adjusted R-squared: 0.3507
F-statistic: 56.63 on 1 and 102 DF, p-value: 2.15e-11
β for IBM and S&P 500 is 0.74481
 21 #regression for apple
 22 fit2=lm(apple~sp)
 23 summary(fit2)
 24
Call:
lm(formula = apple \sim sp)
Residuals:
              1Q Median
     Min
                               30
-26.5378 -5.9191 0.4677 5.5363 19.4413
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
                     0.8606 2.889 0.00472 **
(Intercept) 2.4863
             1.2449
                        0.1930 6.450 3.8e-09 ***
sp
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 8.732 on 102 degrees of freedom
Multiple R-squared: 0.2897, Adjusted R-squared: 0.2827
F-statistic: 41.6 on 1 and 102 DF, p-value: 3.799e-09
```

#### β for Apple and S&P 500 is 1.2449

Apple had a higher expected return relative to S&P 500 because the  $\beta$  Apple is larger than the  $\beta$  of IBM.

```
C)
25 #c)
26 #need to be divided by 100 since they are percentages
27 sd(sp) |
28 sd(ibm)
29 sd(apple)
```

```
> sd(sp)
[1] 4.457853
> sd(ibm)
[1] 5.557105
> sd(apple)
[1] 10.3104
 31 #calculate the correlation matrix
  32 install.packages("corrplot")
  33 source("http://www.sthda.com/upload/rquery_cormat.r")
  35 corre <- data.frame("sp" = sp,"ibm" = ibm,"apple" = apple)
 36 rquery.cormat(corre)
corrplot 0.84 loaded
      apple sp ibm
apple
       1
       0.54 1
ibm
       0.41 0.6 1
$p
        apple
                  sp ibm
apple
           0
      3.8e-09
sp
ibm 1.2e-05 2.2e-11 0
$sym
      apple sp ibm
apple 1
sp
ibm .
attr(,"legend")
[1] 0 ' ' 0.3 '.' 0.6 ',' 0.8 '+' 0.9 '*' 0.95 'B' 1
 38 #calculate b
 39 cor(ibm,sp)*sd(ibm)/sd(sp)
 40 cor(apple,sp)*sd(apple)/sd(sp)
> cor(ibm,sp)*sd(ibm)/sd(sp)
[1] 0.7448088
> cor(apple,sp)*sd(apple)/sd(sp)
[1] 1.244856
d)
\beta = r *Sy/Sx
```

With same Sx and similar r, If Sy is larger, then  $\beta$  is larger, which means high return. Sy represents the volatility of dependent variable. Therefore, the higher the volatility, the higher the return.

### 2.10

<u>a)</u>

```
42 #2.10
 43 #a)
 44
     price = read.csv("Desktop/Predictive Analytics/Assignment/1/Steak+Prices.csv")
 45
 46
 47
     chuck = as.numeric(str_replace(price$Chuck.Price,"\\$",""))
     porthse = as.numeric(str_replace(price$PortHse.Price,"\\$",""))
 48
 49
     ribeye = as.numeric(str_replace(price$RibEye.Price,"\\$",""))
 51
     fit1=lm(log(price$Chuck.Qty)~log(chuck))
 52
     summary(fit1)
 53
 54
     fit2=lm(log(price$PortHse.Qty)~log(porthse))
 55
     summary(fit2)
 56
 57
     fit3=lm(log(price$RibEye.Qty)~log(ribeye))
 58 summary(fit3)
> fit1=lm(log(price$Chuck.Qty)~log(chuck))
> summary(fit1)
lm(formula = log(price$Chuck.Qty) ~ log(chuck))
Residuals:
    Min
              1Q Median
                               30
                                       Max
-0.32463 -0.12036 -0.01714 0.09430 0.49725
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 5.8899
                        0.2871 20.513 < 2e-16 ***
                        0.3199 -4.278 9.44e-05 ***
log(chuck) -1.3687
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.1812 on 46 degrees of freedom
Multiple R-squared: 0.2846, Adjusted R-squared: 0.2691
F-statistic: 18.3 on 1 and 46 DF, p-value: 9.441e-05
> fit2=lm(log(price$PortHse.Qty)~log(porthse))
> summary(fit2)
lm(formula = log(price$PortHse.Qty) ~ log(porthse))
Residuals:
                                3Q
    Min
              1Q Median
-0.57655 -0.23544 0.00317 0.23511 0.49991
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
                      0.5136 17.742 < 2e-16 ***
            9.1123
(Intercept)
                         0.2752 -9.654 1.23e-12 ***
log(porthse) -2.6565
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.283 on 46 degrees of freedom
Multiple R-squared: 0.6695,
                            Adjusted R-squared: 0.6624
F-statistic: 93.2 on 1 and 46 DF, p-value: 1.233e-12
```

```
> fit3=lm(log(price$RibEye.Qty)~log(ribeye))
> summary(fit3)
lm(formula = log(price$RibEye.Qty) ~ log(ribeye))
Residuals:
    Min
              1Q Median
                               30
-0.54075 -0.21801 0.03995 0.20328 0.70950
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) 7.6627 0.7537 10.167 2.39e-13 ***
                       0.3731 -3.876 0.000335 ***
log(ribeye) -1.4460
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.2943 on 46 degrees of freedom
Multiple R-squared: 0.2462,
                             Adjusted R-squared: 0.2298
F-statistic: 15.02 on 1 and 46 DF, p-value: 0.0003352
```

The absolute values of correlation coefficients are in following orders:

Chuck < ribeye < porthse

If chuck is the cheapest beef, then its price elasticity should be the most volatile one. But it is not. So, the price elasticities are not in the expected order.

<u>b)</u>

$$\ln y1 = \alpha + \beta \ln x1$$

$$\ln y2 = \alpha + \beta \ln x2$$

$$\ln \frac{y2}{y1} = \beta \ln \frac{x2}{x1}$$

$$\frac{y2}{y1} = \left(\frac{x2}{x1}\right)^{\beta}$$

$$y2 = 1.1^{\beta}$$

$$\frac{y2 - y1}{y1} = 1.1^{\beta} - 1$$

```
60 #b)
61 (1.1)^-1.3687 - 1 #demand change of chuck
62 (1.1)^-2.6565 - 1 #demand change of porthse
63 (1.1)^-1.4460 - 1 #demand change of ribeye

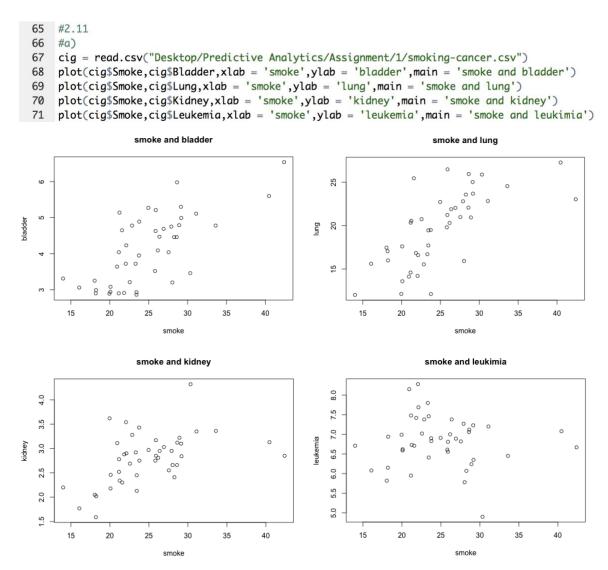
> (1.1)^-1.3687 - 1
[1] -0.1223005

> (1.1)^-2.6565 - 1
[1] -0.2236808

> (1.1)^-1.4460 - 1
[1] -0.1287432

>
```

### 2.11



Smoking and deaths of bladder, lung have apparent linear relationships. Smoking and deaths of kidney have a tiny linear relationship. Smoking and leukemia have no linear relationships. Outliers exists in all of the charts.

```
b)
74 #b)
75 cor.test(cig$Bladder,cig$Smoke)
76 cor.test(cig$Lung,cig$Smoke)
77 cor.test(cig$Kidney,cig$Smoke)
78 cor.test(cig$Leukemia,cig$Smoke)
```

# > cor.test(cig\$Bladder,cig\$Smoke) Pearson's product-moment correlation data: cig\$Bladder and cig\$Smoke t = 6.4173, df = 42, p-value = 9.964e-08alternative hypothesis: true correlation is not equal to 095 percent confidence interval: 0.5141412 0.8276195 sample estimates: cor 0.7036219 > cor.test(cig\$Lung,cig\$Smoke) Pearson's product-moment correlation data: cig\$Lung and cig\$Smoke t = 6.3064, df = 42, p-value = 1.439e-07 alternative hypothesis: true correlation is not equal to 095 percent confidence interval: 0.5051008 0.8237330 sample estimates: cor 0.6974025 > cor.test(cig\$Kidney,cig\$Smoke) Pearson's product-moment correlation data: cig\$Kidney and cig\$Smoke t = 3.6174, df = 42, p-value = 0.0007922 alternative hypothesis: true correlation is not equal to 0 95 percent confidence interval: 0.2227387 0.6851336 sample estimates: cor 0.4873896 > cor.test(cig\$Leukemia,cig\$Smoke) Pearson's product-moment correlation data: cig\$Leukemia and cig\$Smoke t = -0.44485, df = 42, p-value = 0.6587 alternative hypothesis: true correlation is not equal to ${\bf 0}$ 95 percent confidence interval: -0.3580815 0.2331390 sample estimates: cor -0.06848123

From the results of correlation test, it can be seen that the p-value of the leukemia is larger than 0.5, which means there is not enough evidence to prove that smoke has relationships with leukemia. For the rest of the three, test of bladder has the largest correlation coefficient. So, deaths of bladder is mostly significant to smoking.