

Lab Assignment 3

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11/28/2018

```
setwd("~/Desktop/Everything Starts With Data/Lab Assignment 3")
library(quantreg)
```

```
## Loading required package: SparseM
##
## Attaching package: 'SparseM'
## The following object is masked from 'package:base':
##      backsolve
library(e1071)
library(boot)
```

Problem 1

a)

The purpose of MCMC is to sample points from distribution $p(\cdot)$ that is difficult to sample from directly.

b)

Metropolis Algorithm starts with an initial value θ_0 and $q(\cdot|\cdot)$ need to be symmetric.

Metropolis Hastings Algorithm generalizes from the Metropolis Algorithm and $q(\cdot|\cdot)$ does not to have symmetric.

c)

The purpose of Ridge Regression is to minimize SSE subject to $\lambda \sum \beta_j^2 \leq s$

The purpose of Lasso Regression is to minimize SSE subject to $\lambda \sum |\beta_j| \leq s$

d)

IIA is the ratio of the probabilities of choosing two alternatives is independent of the presence or attributes of any other alternative.

Problem 2

```
gas = read.csv("gas_mileage.csv")
```

a)

```
qrfit1 = rq(Mpg ~ ., tau = seq(0.05, 0.95, by=0.05), data = gas)

## Warning in rq.fit.br(x, y, tau = tau, ...): Solution may be nonunique
sumqr = summary(qrfit1)

## Warning in rq.fit.br(x, y, tau = tau, ci = TRUE, ...): Solution may be
## nonunique
## Warning in rq.fit.br(x, y, tau = tau, ci = TRUE, ...): Solution may be
## nonunique
## Warning in rq.fit.br(x, y, tau = tau, ci = TRUE, ...): Solution may be
## nonunique
## Warning in rq.fit.br(x, y, tau = tau, ci = TRUE, ...): Solution may be
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## nonunique
## Warning in rq.fit.br(x, y, tau = tau, ci = TRUE, ...): Solution may be
## nonunique
## Warning in rq.fit.br(x, y, tau = tau, ci = TRUE, ...): Solution may be
## nonunique
## Warning in rq.fit.br(x, y, tau = tau, ci = TRUE, ...): Solution may be
## nonunique
sumqr

##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.05
##
## Coefficients:
##               coefficients   lower bd      upper bd
## (Intercept)    7.505845e+01 -1.797693e+308  1.797693e+308
## Displacement  -3.701000e-02 -1.797693e+308  1.797693e+308
## Hpower        -1.893800e-01 -1.797693e+308  1.797693e+308
## Torque         1.094900e-01 -1.797693e+308  1.797693e+308
## Comp_ratio    -3.509360e+00 -1.797693e+308  1.797693e+308
## Rear_axle_ratio 3.866260e+00 -1.797693e+308  1.797693e+308
## Carb_barrels   2.145330e+00 -1.797693e+308  1.797693e+308
## No._speeds    -2.299040e+00 -1.797693e+308  1.797693e+308
## Length        1.753600e-01 -1.797693e+308  1.797693e+308
## Width         -6.623400e-01 -1.797693e+308  1.797693e+308
## Weight        -3.030000e-03 -1.797693e+308  1.797693e+308
## Trans._type    -9.004500e-01 -1.792682e+01  1.797693e+308
```

```
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.1
##
## Coefficients:
##      coefficients      lower bd      upper bd
## (Intercept)      7.505845e+01 -2.640074e+02  1.965771e+02
## Displacement    -3.701000e-02 -3.574400e-01  6.540000e-02
## Hpower          -1.893800e-01 -7.592400e-01  1.053380e+00
## Torque           1.094900e-01 -3.856000e-01  8.116000e-01
## Comp_ratio      -3.509360e+00 -1.141334e+01  7.802265e+01
## Rear_axle_ratio  3.866260e+00 -1.949856e+01  3.144942e+01
## Carb_barrels     2.145330e+00 -1.083878e+01  1.214711e+01
## No._speeds      -2.299040e+00 -9.998130e+00  1.812914e+01
## Length           1.753600e-01 -2.232600e-01  1.797693e+308
## Width           -6.623400e-01 -1.797693e+308  1.918620e+00
## Weight          -3.030000e-03 -1.060100e-01  1.284000e-02
## Trans._type      -9.004500e-01 -1.561480e+00  1.797693e+308
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.15
##
## Coefficients:
##      coefficients      lower bd      upper bd
## (Intercept)      7.505845e+01 -9.002075e+01  1.453873e+02
## Displacement    -3.701000e-02 -2.327100e-01  2.910000e-02
## Hpower          -1.893800e-01 -6.259600e-01  6.757800e-01
## Torque           1.094900e-01 -2.939300e-01  5.021700e-01
## Comp_ratio      -3.509360e+00 -6.623030e+00  2.989379e+01
## Rear_axle_ratio  3.866260e+00 -1.374687e+01  1.842395e+01
## Carb_barrels     2.145330e+00 -3.081880e+00  6.189830e+00
## No._speeds      -2.299040e+00 -9.698530e+00  1.010556e+01
## Length           1.753600e-01 -8.571000e-02  2.162340e+00
## Width           -6.623400e-01 -3.833210e+00  4.010500e-01
## Weight          -3.030000e-03 -1.328000e-02  1.131000e-02
## Trans._type      -9.004500e-01 -1.446450e+00  1.797693e+308
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.2
##
## Coefficients:
##      coefficients      lower bd      upper bd
## (Intercept)      6.259344e+01 -8.228754e+01  1.409044e+02
## Displacement    -1.956000e-02 -2.040000e-01  3.166000e-02
## Hpower          -1.639200e-01 -6.078400e-01  4.992700e-01
## Torque           8.250000e-02 -3.315400e-01  4.444400e-01
## Comp_ratio      -2.796880e+00 -6.437820e+00  1.030132e+01
## Rear_axle_ratio  2.859870e+00 -4.345210e+00  1.796188e+01
## Carb_barrels     1.786780e+00 -1.398360e+00  3.303940e+00
## No._speeds      -1.428330e+00 -9.994610e+00  1.355025e+01
## Length           1.922900e-01 -1.138700e-01  1.237590e+00
```

```

## Width          -5.698600e-01 -3.078290e+00  5.256000e-02
## Weight         -4.420000e-03 -1.309000e-02  1.036000e-02
## Trans._type    -4.470000e-01 -7.606060e+00  1.797693e+308
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.25
##
## Coefficients:
##              coefficients lower bd      upper bd
## (Intercept)    5.939339e+01 -8.167520e+01  1.244924e+02
## Displacement  -1.917000e-02 -2.322600e-01  2.464000e-02
## Hpower       -1.745200e-01 -5.456900e-01  3.766700e-01
## Torque        8.982000e-02 -3.224100e-01  4.848900e-01
## Comp_ratio   -2.721790e+00 -6.584030e+00  1.024147e+01
## Rear_axle_ratio 2.507430e+00 -6.154160e+00  1.816992e+01
## Carb_barrels   1.825000e+00 -1.590480e+00  3.191410e+00
## No._speeds    -9.305200e-01 -1.021943e+01  1.580215e+01
## Length        1.858100e-01 -1.563300e-01  4.075000e-01
## Width         -5.308900e-01 -2.755050e+00  2.577000e-02
## Weight        -4.380000e-03 -1.345000e-02  9.000000e-03
## Trans._type   -4.767800e-01 -7.956070e+00  1.797693e+308
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.3
##
## Coefficients:
##              coefficients lower bd      upper bd
## (Intercept)    54.06294   -68.83438 103.95882
## Displacement   -0.03751    -0.22369  0.02329
## Hpower        -0.14300    -0.49277  0.31943
## Torque         0.09195    -0.33155  0.43812
## Comp_ratio    -2.15210    -6.28234  9.89148
## Rear_axle_ratio 2.66851    -6.44198 18.14440
## Carb_barrels   1.70373    -3.17755  3.36442
## No._speeds    -1.60050   -10.35158 14.36612
## Length         0.19950    -0.16919  0.42062
## Width         -0.52344    -1.20202  0.04226
## Weight        -0.00444    -0.00998  0.00998
## Trans._type    0.00138    -9.84964 18.44084
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.35
##
## Coefficients:
##              coefficients lower bd      upper bd
## (Intercept)    33.61471   -64.66366 114.81804
## Displacement   -0.03139    -0.21008  0.03422
## Hpower        -0.20400    -0.44658  0.30928
## Torque         0.13156    -0.27674  0.31270
## Comp_ratio    -0.25080    -5.45183  9.81983
## Rear_axle_ratio 3.65908    -7.03406 14.90364

```

```

## Carb_barrels      1.23102      -3.39051      3.63315
## No._speeds        1.41816     -10.18349     11.84650
## Length            0.23047      -0.16893      0.42550
## Width             -0.72708      -1.12616      0.06438
## Weight            -0.00460      -0.00969      0.01709
## Trans._type       1.21189     -13.55527     19.91186
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.4
##
## Coefficients:
##               coefficients lower bd  upper bd
## (Intercept)    39.79782    -38.02844  113.89174
## Displacement   -0.13338     -0.20434   0.03074
## Hpower         -0.18288     -0.42267   0.26439
## Torque          0.24622     -0.04369   0.30530
## Comp_ratio     -0.46214     -5.25613   8.45928
## Rear_axle_ratio 9.72169     -7.02632  13.60216
## Carb_barrels    1.13543     -2.96256   3.81884
## No._speeds     -4.67178    -10.06583  11.59511
## Length          0.22521     -0.17691   0.45815
## Width          -0.71592     -0.96215   0.04934
## Weight         -0.00493     -0.00970   0.01547
## Trans._type     2.03764    -13.21112  13.78413
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.45
##
## Coefficients:
##               coefficients lower bd  upper bd
## (Intercept)    39.79782    -56.56228  106.18042
## Displacement   -0.13338     -0.20343   0.02052
## Hpower         -0.18288     -0.41773   0.25501
## Torque          0.24622     -0.01230   0.30261
## Comp_ratio     -0.46214     -6.14907   8.28425
## Rear_axle_ratio 9.72169     -6.94519  13.35862
## Carb_barrels    1.13543     -2.98675   4.21629
## No._speeds     -4.67178    -10.00668  11.72722
## Length          0.22521     -0.18485   0.43406
## Width          -0.71592     -1.16886   0.17787
## Weight         -0.00493     -0.00847   0.01610
## Trans._type     2.03764    -15.49451   7.66150
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.5
##
## Coefficients:
##               coefficients lower bd  upper bd
## (Intercept)    41.98707    -50.15249  99.41846
## Displacement   -0.13873     -0.19219   0.01530
## Hpower         -0.17596     -0.39591   0.25625

```

```

## Torque          0.24692      -0.02048    0.29231
## Comp_ratio      -1.14223      -6.05074    8.13403
## Rear_axle_ratio  9.03682      -6.58867   12.87569
## Carb_barrels    1.14349      -2.74990    4.52378
## No._speeds      -3.91968      -9.28143    7.94056
## Length          0.17526      -0.17574    0.40710
## Width           -0.54095      -1.21406    0.19273
## Weight          -0.00472      -0.01453    0.01580
## Trans._type     1.99845      -16.08817   12.71580
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.55
##
## Coefficients:
##              coefficients lower bd  upper bd
## (Intercept)   37.45543    -44.82510   83.71515
## Displacement  -0.15632     -0.18890    0.00376
## Hpower        -0.16826     -0.39300    0.25379
## Torque         0.26247     -0.01384    0.30666
## Comp_ratio    -0.66081     -6.06884    6.68266
## Rear_axle_ratio 9.51487     -6.24103   12.86802
## Carb_barrels   1.04178     -3.13414    4.18934
## No._speeds    -4.62124     -9.61926    8.96272
## Length         0.13267     -0.10225    0.52539
## Width         -0.40408     -1.49854    0.22254
## Weight        -0.00460     -0.01807    0.01441
## Trans._type    2.58728     -17.09597   11.63718
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.6
##
## Coefficients:
##              coefficients lower bd  upper bd
## (Intercept)  -12.38280    -43.03643   95.08684
## Displacement  -0.12421     -0.41794   -0.00553
## Hpower        -0.03070     -0.35527    0.24415
## Torque         0.16519     -0.02707    0.42386
## Comp_ratio     2.08188     -5.70257    6.47639
## Rear_axle_ratio 10.01460    -6.14963   12.04353
## Carb_barrels   1.43890     -2.71410    4.09294
## No._speeds    -7.01770     -9.16567    8.71186
## Length         0.37290     -0.10354    0.51369
## Width         -0.29559     -1.54439    0.35325
## Weight        -0.01231     -0.02441    0.00933
## Trans._type    3.20547     -17.37450   10.84163
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.65
##
## Coefficients:
##              coefficients lower bd  upper bd

```

```

## (Intercept)      2.72420    -62.53270   90.21213
## Displacement    -0.12688     -0.45468    0.03413
## Hpower           0.01245     -0.33805    0.20142
## Torque           0.13632     -0.01474    0.71181
## Comp_ratio      -0.30299     -6.43194    7.23641
## Rear_axle_ratio  4.44313     -6.87306   12.41785
## Carb_barrels     0.97970     -3.14994    4.08618
## No._speeds      -1.92379     -9.72640   11.20294
## Length           0.24256     -0.02695    0.54294
## Width            0.07790     -1.54193    0.34287
## Weight          -0.01072     -0.02450    0.00551
## Trans._type      3.86325     -17.61289    6.83024
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.7
##
## Coefficients:
##              coefficients lower bd  upper bd
## (Intercept)    28.85096   -75.12977 102.50991
## Displacement   -0.16541   -0.47664  0.05931
## Hpower          0.07405   -0.33272  0.20573
## Torque          0.18091    0.03334  0.66419
## Comp_ratio     -0.90495   -6.34058  7.71359
## Rear_axle_ratio 5.65233   -7.01015 14.03433
## Carb_barrels   -0.13504   -2.96208  4.04653
## No._speeds     -2.93528  -10.54811 11.40447
## Length          0.16370   -0.07872  0.53613
## Width          -0.19469   -1.21537  0.36292
## Weight         -0.00779   -0.02598  0.00638
## Trans._type     2.07428   -23.65402  5.03042
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.75
##
## Coefficients:
##              coefficients  lower bd      upper bd
## (Intercept)  3.455691e+01 -8.684394e+01  1.032997e+02
## Displacement -1.751100e-01 -4.660100e-01  6.019000e-02
## Hpower        5.674000e-02 -3.025600e-01  8.576000e-02
## Torque        2.073900e-01 -1.951000e-01  5.179700e-01
## Comp_ratio    -9.275300e-01 -7.579510e+00  9.662210e+00
## Rear_axle_ratio 5.785450e+00 -6.660930e+00  1.305027e+01
## Carb_barrels  -7.231000e-02 -3.181530e+00  4.833050e+00
## No._speeds    -3.165050e+00 -1.308105e+01  1.568430e+01
## Length        1.295500e-01 -1.320200e-01  6.347100e-01
## Width         -2.334800e-01 -1.300490e+00  3.444300e-01
## Weight        -6.460000e-03 -2.710000e-02  9.380000e-03
## Trans._type    3.597200e-01 -1.797693e+308  5.314290e+00
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.8

```

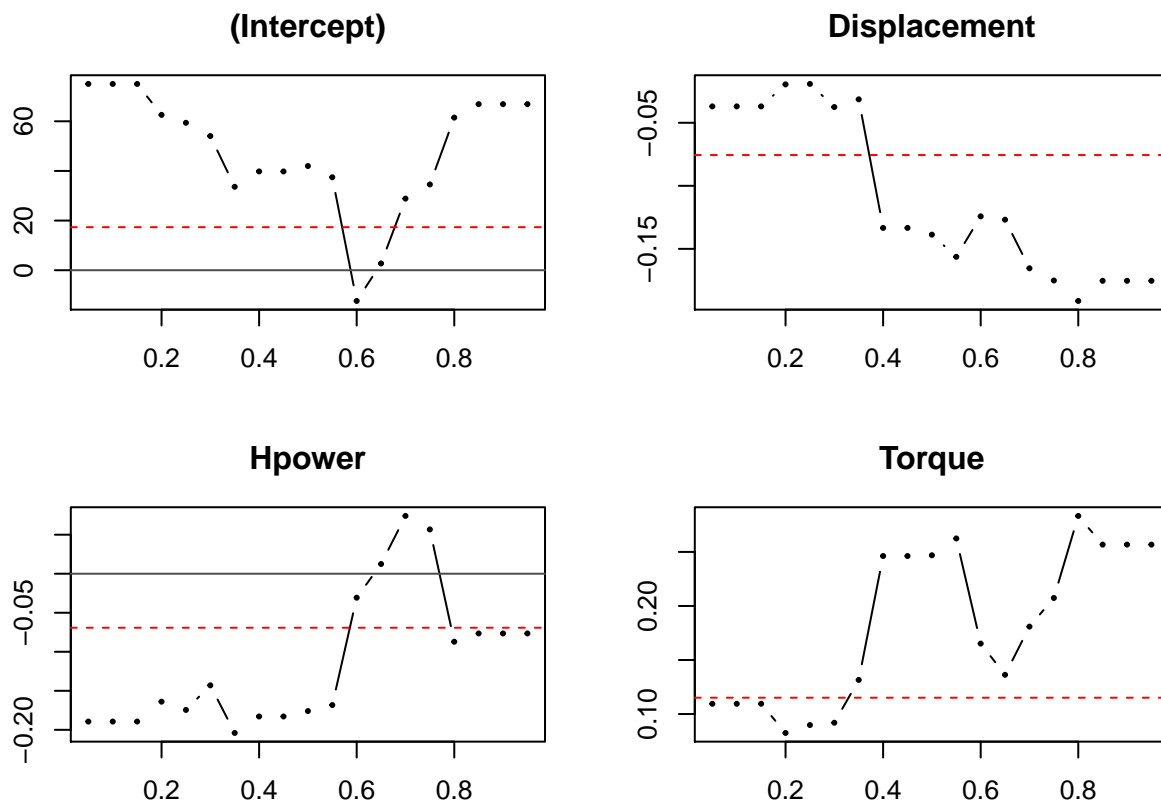
```
##
## Coefficients:
##      coefficients      lower bd      upper bd
## (Intercept)      6.148552e+01 -1.049836e+02  8.566354e+01
## Displacement    -1.913300e-01 -4.137200e-01  6.737000e-02
## Hpower          -8.712000e-02 -2.164400e-01  7.954000e-02
## Torque           2.833300e-01 -2.153400e-01  4.907800e-01
## Comp_ratio       9.368600e-01 -7.735370e+00  9.631920e+00
## Rear_axle_ratio  2.917710e+00 -4.611710e+00  1.369960e+01
## Carb_barrels     1.512300e-01 -4.358200e+00  4.657640e+00
## No._speeds      -4.994060e+00 -1.314589e+01  1.682156e+01
## Length           1.373000e-02 -1.543800e-01  7.594600e-01
## Width            -4.669700e-01 -1.331300e+00  1.108440e+00
## Weight           9.900000e-04 -3.790000e-02  3.420000e-03
## Trans._type      -9.478690e+00 -1.797693e+308  7.201720e+00
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.85
##
## Coefficients:
##      coefficients      lower bd      upper bd
## (Intercept)      6.690518e+01 -1.017219e+02  8.340677e+01
## Displacement    -1.753400e-01 -4.133800e-01  8.903000e-02
## Hpower          -7.653000e-02 -2.252300e-01  2.891000e-02
## Torque           2.567900e-01 -2.193400e-01  5.192900e-01
## Comp_ratio       9.785700e-01 -1.052048e+01  1.013836e+01
## Rear_axle_ratio  1.973560e+00 -4.461560e+00  1.404317e+01
## Carb_barrels     1.741000e-02 -5.369720e+00  4.663750e+00
## No._speeds      -4.769530e+00 -1.477001e+01  1.962953e+01
## Length           1.180000e-03 -2.910870e+00  7.777500e-01
## Width            -4.858100e-01 -1.369200e+00  4.014110e+00
## Weight           1.210000e-03 -4.319000e-02  3.710000e-03
## Trans._type      -1.012671e+01 -1.797693e+308  7.245470e+00
##
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.9
##
## Coefficients:
##      coefficients      lower bd      upper bd
## (Intercept)      6.690518e+01 -9.810508e+01  8.661455e+01
## Displacement    -1.753400e-01 -4.236900e-01  1.289300e-01
## Hpower          -7.653000e-02 -2.656700e-01  4.391000e-02
## Torque           2.567900e-01 -3.484200e-01  5.416000e-01
## Comp_ratio       9.785700e-01 -3.524620e+01  2.352705e+01
## Rear_axle_ratio  1.973560e+00 -6.904900e+00  1.521520e+01
## Carb_barrels     1.741000e-02 -9.354370e+00  4.553580e+00
## No._speeds      -4.769530e+00 -2.477762e+01  2.793282e+01
## Length           1.180000e-03 -1.797693e+308  9.343800e-01
## Width            -4.858100e-01 -5.684390e+00  1.797693e+308
## Weight           1.210000e-03 -4.721000e-02  5.040000e-03
## Trans._type      -1.012671e+01 -1.797693e+308  7.331570e+00
##
```

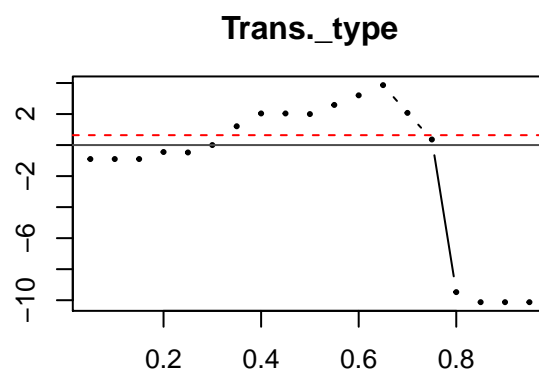
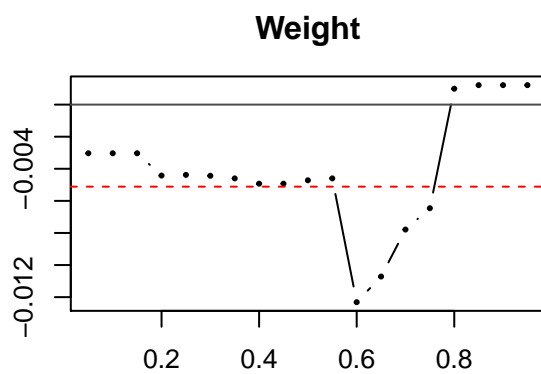
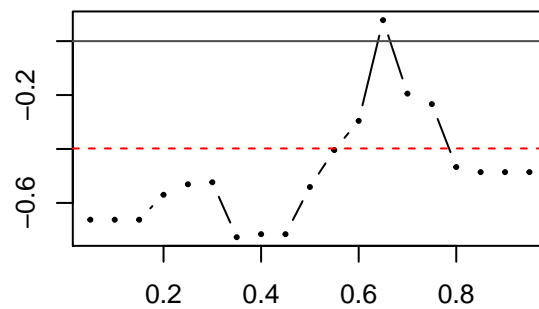
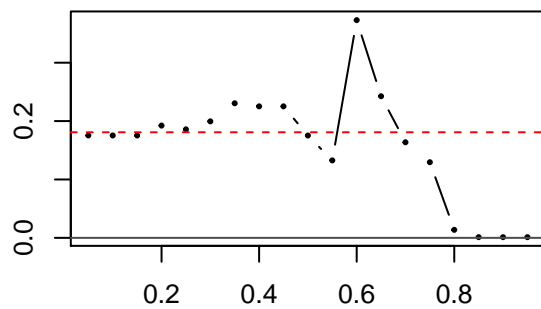
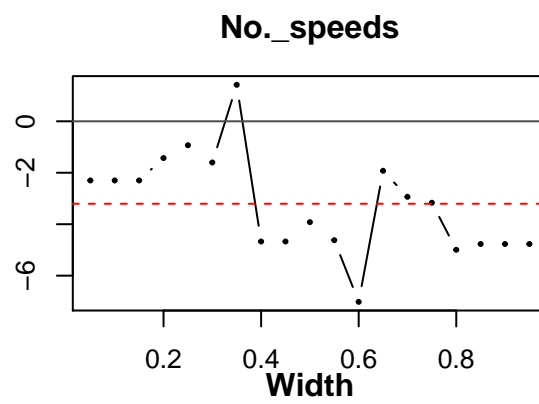
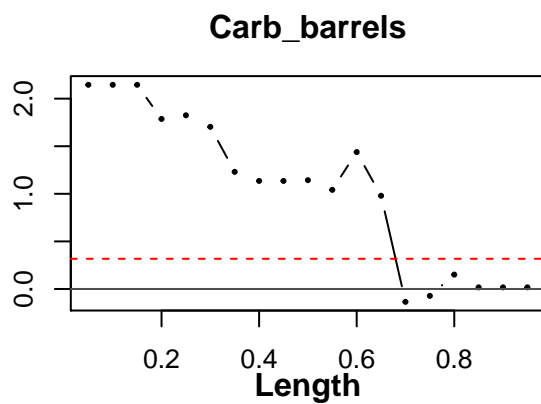
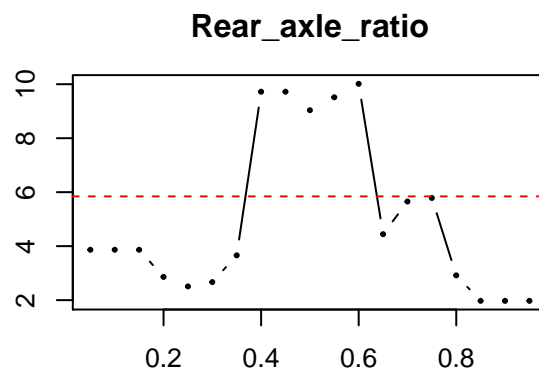
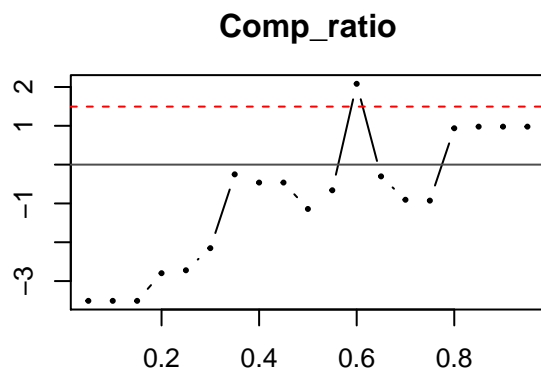


```
## Call: rq(formula = Mpg ~ ., tau = seq(0.05, 0.95, by = 0.05), data = gas)
##
## tau: [1] 0.95
##
## Coefficients:
##              coefficients    lower bd    upper bd
## (Intercept)    6.690518e+01 -1.797693e+308  1.797693e+308
## Displacement   -1.753400e-01 -1.797693e+308  1.797693e+308
## Hpower         -7.653000e-02 -1.797693e+308  1.797693e+308
## Torque          2.567900e-01 -1.797693e+308  1.797693e+308
## Comp_ratio      9.785700e-01 -1.797693e+308  1.797693e+308
## Rear_axle_ratio 1.973560e+00 -1.797693e+308  1.797693e+308
## Carb_barrels    1.741000e-02 -1.797693e+308  1.797693e+308
## No._speeds     -4.769530e+00 -1.797693e+308  1.797693e+308
## Length          1.180000e-03 -1.797693e+308  1.797693e+308
## Width          -4.858100e-01 -1.797693e+308  1.797693e+308
## Weight          1.210000e-03 -1.797693e+308  1.797693e+308
## Trans._type     -1.012671e+01 -1.797693e+308  7.544440e+00
```

b)

```
plot(qrfit1, mfrow = c(2,2))
```





c)

Length: Before 0.55th, with one unit increase th length, there will be on average 0.18 increase in mpg. From about 0.55th to 0.7th, the length has a drastic positive impact on mpg. After that the length has lesser positive impact on mpg. After 0.8th quantile the length has almost no influence on mpg.

Weight: Before 0.6th quantile, onw unit increase in weight will lead to about 0.18 increase in mpg. At 0.6th quantile, 0.1 unit increase in weight will lead to about 0.25 increase in mpg. After 0.8th quantile, weight has no influence on quantile.

comp_ratio: for most part, with the increase in comp_ratio, there will be a lesser negative impact in mpg But for comp_ratio at 0.6th quantile or after 0.8th quantile, it has a positive effect on mpg.

d)

```
median = rq(Mpg ~ ., tau = .5, data = gas)
summary(median, se = "boot")

##
## Call: rq(formula = Mpg ~ ., tau = 0.5, data = gas)
##
## tau: [1] 0.5
##
## Coefficients:
##              Value      Std. Error t value Pr(>|t|)
## (Intercept)  41.98707  52.58797    0.79842  0.43504
## Displacement -0.13873   0.10416   -1.33194  0.19950
## Hpower       -0.17596   0.21068   -0.83516  0.41458
## Torque        0.24692   0.17208    1.43494  0.16845
## Comp_ratio   -1.14223   5.19150   -0.22002  0.82833
## Rear_axle_ratio 9.03682   6.86134    1.31706  0.20434
## Carb_barrels   1.14349   2.53075    0.45184  0.65678
## No._speeds    -3.91968   7.96215   -0.49229  0.62847
## Length        0.17526   0.29047    0.60338  0.55379
## Width        -0.54095   0.62739   -0.86223  0.39990
## Weight       -0.00472   0.01004   -0.46975  0.64418
## Trans._type    1.99845   8.52550    0.23441  0.81731
```

Problem 3

```
car = read.csv("car.csv")
```

a)

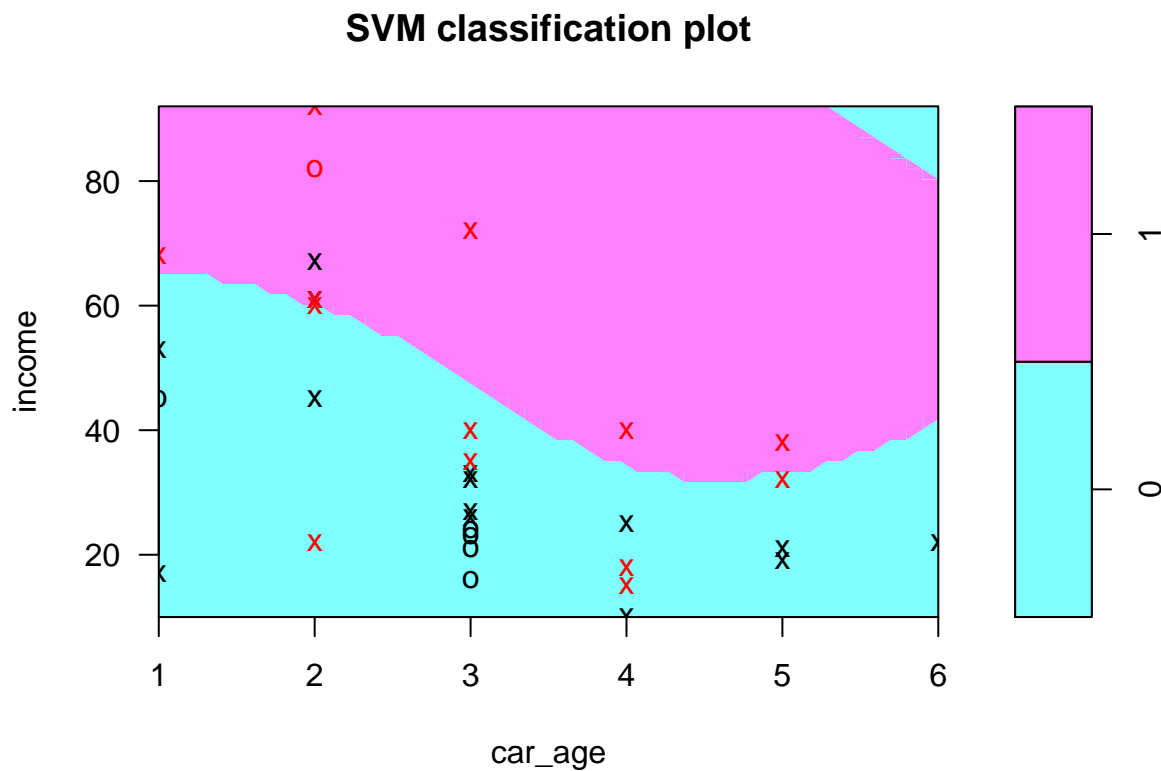
```
carsvm = svm(factor(y) ~ ., data = car)
summary(carsvm)

##
## Call:
## svm(formula = factor(y) ~ ., data = car)
```

```
##
##
## Parameters:
##   SVM-Type:  C-classification
##   SVM-Kernel: radial
##     cost: 1
##     gamma: 0.5
##
## Number of Support Vectors: 27
##
## ( 14 13 )
##
##
## Number of Classes: 2
##
## Levels:
## 0 1
```

b)

```
plot(carsvm, data = car, income ~ car_age)
```



c)

```
predict(carsvm, newdata = data.frame(income = 50, car_age = 5))
```

```
## 1
```

1

Levels: 0 1

This family will purchase a new car.