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# Best-First Search: Greedy Search

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# Objectives

- ▶ Describe the algorithm of best-first search.
- ▶ Apply greedy search as an instance of best-first search.
- ▶ Analyse the optimality and complexity of greedy search.
- ▶ Show the incompleteness of greedy tree search.

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# 1 Introduction

*Best-first search* consists in enumerating paths until it finds a solution, prioritising those with lowest cost ( $f$ ) and avoiding cycles:

Best-first search generalises  $A^*$  allowing the use of any *evaluation (heuristic) function*  $f$ , not necessarily those in the form of  $f = g + h$ .

## 2 Best-first algorithm (graph search) [1]

```
BF( $G, s', f$ )           //  $G$  weighed graph,  $s'$ ,  $f$  evaluation function  
   $O = \text{InitQueue}(s', f(s'))$            // Open: priority queue  $f$   
   $C = \emptyset$                        // Closed: explored nodes  
  while not  $\text{EmptyQueue}(O)$ :           // best-first:  $s = \arg \min_{n \in O} f_n$   
     $s = \text{Pop}(O)$                        // draws in favour of goal state  
    if  $\text{Goal}(s)$  return  $s$            // solution found!  
     $C = C \cup \{s\}$                        //  $s$  explored  
    for all  $(s, n) \in \text{Adjacents}(G, s)$ : // generation:  $n$  is child of  $s$   
       $x = f(n)$                        // possibly new  $f_n$   
      if  $n \notin C \cup O$ :  $\text{Push}(O, n, f_n \triangleq x)$   
      else if  $n \in O$  and  $x < f_n$ :  $\text{Update}(O, n, f_n \triangleq x)$   
      else if  $n \in C$  and  $x < f_n$ :  $C = C \setminus \{n\}$ ;  $\text{Push}(O, n, f_n \triangleq x)$   
  return NULL                       // solution not found
```

### 3 Greedy search (graph search)

*Greedy search* consists in using **BF** with  $f = h$ :

*Intuition:* to reach solution nodes quickly.

*Optimality:* complete in finite graphs and suboptimal.

*Complexity:*  $O(b^m)$  temporal and spatial ( $m$  maximum depth).

## 4 Best-first algorithm (tree search) [1]

```
BF( $G, s', f$ )           //  $G$  weighed graph,  $s'$ ,  $f$  evaluation function  
   $O = \text{InitQueue}(s', f(s'))$            // Open: priority queue  $f$   
  while not  $\text{EmptyQueue}(O)$ :           // best-first:  $s = \arg \min_{n \in O} f_n$   
     $s = \text{Pop}(O)$                        // draws in favour of goal state  
    if  $\text{Goal}(s)$  return  $s$              // solution found!  
    for all  $(s, n) \in \text{Adjacents}(G, s)$ : // generation:  $n$  is child of  $s$   
       $x = f(n)$                          // possibly new  $f_n$   
      if  $n \notin O$ :  $\text{Push}(O, n, f_n \triangleq x)$   
      else if  $n \in O$  and  $x < f_n$ :  $\text{Update}(O, n, f_n \triangleq x)$   
  return NULL                       // solution not found
```

## 5 Greedy search (tree search)

*Greedy search with tree search* [2] ( $C = \emptyset$ ) is incomplete:



# 6 Conclusions

We have studied:

- ▶ The algorithm of best-first search, both graph and tree search.
- ▶ Greedy search with graph and tree search.
- ▶ Optimality and complexity of greedy search.
- ▶ Incompleteness of greedy tree search.

# References

- [1] J. Pearl. *Heuristics: Intelligent Search Strategies for Computer Problem Solving*. Addison-Wesley, 1984.
- [2] S. Russell and P. Norvig. *Artificial Intelligence: A Modern Approach*. Pearson, third edition, 2010.

```
#!/usr/bin/env python3
import heapq
G={ 'A':[( 'B',1), ( 'C',4)], 'B':[( 'A',1), ( 'D',1)],
→ 'C':[( 'A',4), ( 'E',1)], 'D':[( 'B',1), ( 'E',4)],
→ 'E':[( 'C',1), ( 'D',4)] }
hstar={ 'A':5, 'B':5, 'C':1, 'D':4, 'E':0}
def bf(G,s,t,f):
→fs=f[s]; Od={s:(0,fs)}; Cd={} # Open and Closed g,f dict
→Oh=[]; heapq.heappush(Oh,(fs,s,[s])) # Open heap
→while Od:
→→s=None
→→while s not in Od: fs,s,path=heapq.heappop(Oh) # delete-min
→→gs,fs=Od[s]
→→if s==t: return gs,path
→→del Od[s]; Cd[s]=gs,fs
→→for n,wsn in G[s]:
→→→gn=gs+wsn; fn=f[n]
→→→if n in Cd:
→→→→if fn<Cd[n][1]: del Cd[n] # for variable f (eg with path)
→→→→else: continue
→→→elif n in Od and fn>=Od[n][0]: continue
→→→Od[n]=gn,fn; heapq.heappush(Oh,(fn,n,path+[n]))
print(bf(G,'A','E',hstar))
```

```
(5, ['A', 'C', 'E'])
```