Session 2

In this second session we will apply the Perceptron algorithm to some classification tasks. A simple implementation of the Perceptron algorithm and its application is provided. The main purpose of this session is to extend the example given to other tasks, trying to minimize test error.

Perceptron applied to the Iris dataset

Reading the dataset: we also check that the data matrix and labels have the right number of rows and columns

Dataset partition: We create a split of the Iris dataset with 20% of data for test and the rest for training, previously shuffling the data according to a given seed provided by a random number generator. Here, as in all code that includes randomness (which requires generating random numbers), it is convenient to fix said seed to be able to reproduce experiments with accuracy.

```
In [2]: from sklearn.model_selection import train_test_split
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, shuffle=True, random_state=23)
print(X_train.shape, X_test.shape)

(120, 4) (30, 4)

tany
test

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Perceptron implementation: returns weights in homogeneous notation, $\mathbf{W} \in \mathbb{R}^{(1+D)\times C}$; also the number of errors and \mathcal{O} iterations executed

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)+1
```

Learning a (linear) classifier with Perceptron: Perceptron minimizes the number of training errors (with margin b)

$$\mathbf{W}^* = \underset{\mathbf{W} = (w_1, \dots, w_C)}{\operatorname{argmin}} \sum\limits_{n} \ I(\underset{c \neq y_n}{\max} \ w_c^t x_n + b \ > \ w_{y_n}^t x_n)$$

```
Calculation of test error rate:
In [6]: X testh = np.hstack([np.ones((len(X test), 1)), X_test])
                                                                            ((x1) = organex g(X1) =
        y_test_pred = np.argmax(X_testh @ W) axis=1).reshape(-1, 1)
   err test = np.count nonzero(y test pred != y test) / len(X test)
        print(f"Error rate on test: {err test:.1%}")
        Error rate on test: 16.7%
        Margin adjustment: experiment to learn a value of b
```

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In [7]: for b in (.0, .01, .1, 10, 100):
            W, E, k = perceptron(X train, y train, b=b, K=1000)
            print(b, E, k)
        0.0 3 1000
        0.01 5 1000
        0.1 3 1000
        10 6 1000
```

Interpretation of results: the training data does not appear to be linearly separable; it is not clear that a margin greater than zero can improve results, especially since we only have 30 test samples; with a margin b=0.1 we have already seen that an error (in test) of 16.7% is obtained

100 6 1000

