## Intelligent Systems - Final Exam (Block 2): Test (1.75 points)

ETSINF, Universitat Politècnica de València, January 27th, 2022

## Group, surname(s) and name: 2,

Tick only one choice among the given options. Score:  $\max(0, (\text{correct\_answers-wrong\_answers}/3) \cdot 1.75 / 6)$ .

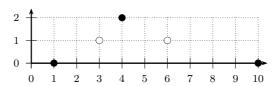
1 Given the following 3 nodes of a classification tree with samples belonging to 3 classes:

c	1	2	3
$n_1$	5/11	4/11	2/11
$n_2$	4/9	3/9	2/9
$n_3$	5/9	1/9	3/9

where each row is the posterior probability of each class in the node. Which of the following inequalities is true?

- A)  $\mathcal{I}(n_1) < \mathcal{I}(n_2) < \mathcal{I}(n_3)$
- B)  $\mathcal{I}(n_2) < \mathcal{I}(n_1) < \mathcal{I}(n_3)$
- C)  $\mathcal{I}(n_3) < \mathcal{I}(n_1) < \mathcal{I}(n_2)$
- D)  $\mathcal{I}(n_3) < \mathcal{I}(n_2) < \mathcal{I}(n_1)$

2 ☐ The figure below shows a partition of 5 two-dimensional points in 2 clusters, • and ○:



If points  $(1,0)^t$  and  $(3,1)^t$  are transferred from one cluster to the other, a variation of the Sum of Square Errors (SSE) is produced,  $\Delta J = J - J'$  (SSE after the transfer minus SSE before the transfer), such that:

- A)  $\Delta J < -7$ .
- B)  $-7 \le \Delta J < 0$ .
- C)  $0 \le \Delta J < 7$ .
- D)  $\Delta J \geq 7$ .

3 Let M be a Markov model with set of states  $Q = \{1, 2, F\}$  and alphabet  $\Sigma = \{a, b\}$ . After the application of an iteration of the Viterbi's reestimation algorithm, the table of state transition probabilities shown on the right has been obtained. From which table of state transition frequencies has been obtained?

A	1	2	F
1	$\frac{3}{6}$	$\frac{1}{6}$	$\frac{2}{6}$
2	$\frac{2}{5}$	$\frac{2}{5}$	$\frac{1}{5}$

- B) A 1 2 F 1 3 1 6 2 2 2 5

Let M be a Markov model with set of states  $Q = \{1, 2, F\}$  and alphabet  $\Sigma = \{a, b\}$ . Given the string x = baa, the Viterbi approximation to  $P_M(x)$ ,  $\tilde{P}_M(x)$ , has been found using the Viterbi algorithm:

$$\begin{split} V_{11} &= \pi_1 B_{1b} = 0.3750 \\ V_{21} &= \pi_2 B_{2b} = 0.3000 \\ V_{12} &= \max(V_{11} A_{11} B_{1a}, V_{21} A_{21} B_{1a}) = \max(0.0312, 0.0375) = 0.0375 \\ V_{22} &= \max(V_{11} A_{12} B_{2a}, V_{21} A_{22} B_{2a}) = \max(0.0750, 0.0300) = 0.0750 \\ V_{13} &= \max(V_{12} A_{11} B_{1a}, V_{22} A_{21} B_{1a}) = \max(0.0031, 0.0094) = 0.0094 \\ V_{23} &= \max(V_{12} A_{12} B_{2a}, V_{22} A_{22} B_{2a}) = \max(0.0075, 0.0075) = 0.0075 \\ \tilde{P}(\text{baa}) &= \max(V_{13} A_{1F}, V_{23} A_{2F}) = \max(0.0016, 0.0019) = 0.0019 \end{split}$$

The most probable path (one of the most probable paths, if there are more than one) through which Mgenerates x is:

- A) 121 F
- B) 221F
- C) 1 1 2 F
- D) 2 1 2 F
- For a three-class classification problem of objects of type  $\mathbf{x} = (x_1, x_2)^t \in \{0, 1\}^2$ , we have the probability distributions shown in the table. Show the interval of the probability of error of the cla

assifier	$c(\mathbf{x})$ provided	in the table, $\varepsilon$ :
Δ)	$\epsilon < 0.25$	

- B)  $0.25 \le \varepsilon < 0.50$ .
- C)  $0.50 \le \varepsilon < 0.75$ .
- D)  $0.75 \le \varepsilon$ .

	2	C.	$P(c \mid \mathbf{x})$				
Γ.	$x_1$	$x_2$	c=1	c=2	c=3	$P(\mathbf{x})$	$c(\mathbf{x})$
	0	0	0.2	0.3	0.5	0	1
	0	1	0.3	0.3	0.4	0.4	1
	1	0	0.2	0.5	0.3	0.5	2
	1	1	0.3	0.6	0.1	0.1	1

Given the following joint frequency distribution for the 3 random variables

A	0	0	0	0	1	1	1	1
В	0	0	1	1	0	0	1	1
С	0	1	U					1
N(A,B,C)	211	140	245	87	39	110	5	163

Which is the value of  $P(A = 1 \mid B = 1, C = 1)$ ?

- A) 0.317
- B) 0.163
- C) 0.652
- D) 0.250

## Intelligent Systems - Final Exam (Block 2): Problem (2 points)

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## Problem: Perceptron algorithm

The table on the left side shows a training set of 3 two-dimension samples that belong to 3 classes, while the table on the right side shows the initial weight vector for each class.

n	$x_{n1}$	$x_{n2}$	$c_n$	
1	1	0	1	
2	0	0	2	
3	-1	0	3	

	$\mathbf{w}_1$	$\mathbf{w}_2$	$\mathbf{w}_3$
$w_{c0}$	-2	-1	-1
$w_{c1}$	2	1	-3
$w_{c2}$	0	0	0

Answer the following questions:

- 1. (1.5 points) Show a trace of the Perceptron algorithm running for one iteration with learning rate  $\alpha = 1$ , margin  $\beta = 0.1$  using the initial weight vectors provided.
- 2. (0.5 points) Plot the decision regions of the resulting classifier, as well as the decision boundaries involved.