### Evidencia ecuaciones en LaTex

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July 23, 2020

#### 1 Matrix.

Incidence matrix 1:

$$\begin{bmatrix} 1 & 1 & 0 & 0 & 0 & 0 & -1 \\ -1 & 0 & 1 & -1 & 0 & 0 & 0 \\ 0 & -1 & -1 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & -1 & 1 \end{bmatrix}$$
 (1)

#### 2 Several Models.

$$\min \sum_{s \in N: s \neq t} \sum_{t \in N: t \neq s} \sum_{(ij) \in P} = c_{ij} \ x_{ij}^{st}$$

$$\tag{2}$$

S.t.

$$\sum_{(ij)\in P} x_{ij}^{st} - \sum_{(ij)\in P} x_{ji}^{st} = \begin{cases} 1, & i=s & \forall i\in N; s\in N: s\neq t \\ -1, & i\neq s, t & \forall i\in N; s\in N: s\neq t; t\in N: t\neq s \\ -1, & i=t & \forall i\in N; t\in N: t\neq s \end{cases}$$

$$(3)$$

Domain:

$$x_{ij}^{st} \in \{0,1\} \quad \forall (ij) \in P; i \neq j; (st) \in N; s \neq t$$

$$\tag{4}$$

$$f(tik) = \sum_{t \in \mathbf{T}} \sum_{i \in \mathbf{PL}} \sum_{k \in \mathbf{NP}} (cm_f \ h_{im}^t + cm_r \ h_{im}^{t-1} + cm_n \ h_{im}^{t-2}) \ a_{km}^i \ x_{ki}^t$$
 (5)

$$g(trk) = \sum_{t \in \mathbf{T}} \sum_{r \in \mathbf{CD}} \sum_{k \in \mathbf{NP}} h_{kr}^t y_{kr}^t \tag{6}$$

$$h(tik) = \sum_{t \in \mathbf{T}} \sum_{i \in \mathbf{PL}} \sum_{k \in \mathbf{NP}} pr_{ki}^{i} cc_{il} u_{kil}^{t} + pr_{ki}^{i} cc_{ir} v_{kir}^{t}$$

$$\tag{7}$$

$$p(trk) = \sum_{t \in \mathbf{T}} \sum_{r \in \mathbf{CD}} \sum_{k \in \mathbf{NP}} pr_{kr}^{r} \, cc_{rl} \, w_{krl}^{t}$$

$$\tag{8}$$

The model is given by;

$$min \ f(tik) + g(trk) + h(tik) + p(trk) \tag{9}$$

S.t

$$\sum_{i \in \mathbf{PL}} \sum_{l \in \mathbf{CL}} u_{kil}^t + \sum_{r \in \mathbf{CD}} \sum_{l \in \mathbf{CL}} w_{krl}^t = \sum_{l \in \mathbf{CL}} d_{kl}^t \qquad \forall \ t \in \mathbf{T}; k \in \mathbf{NP}$$
(10)

$$\sum_{r \in \mathbf{CD}} y_{kr}^t \le \sum_{r \in \mathbf{CD}} p_r^t \qquad \forall \ t \in \mathbf{T}; k \in \mathbf{NP}$$
(11)

$$\sum_{i \in \mathbf{PL}} x_{ki}^t \le \sum_{i \in \mathbf{PL}} Q_i^t q_i^k \qquad \forall \ t \in \mathbf{T}; k \in \mathbf{NP}$$
(12)

$$\sum_{i \in \mathbf{PL}} x_{ki}^t - \sum_{i \in \mathbf{PL}} u_{kil}^t - \sum_{i \in \mathbf{PL}} v_{kir}^t = 0 \qquad \forall \ t \in \mathbf{T}; k \in \mathbf{NP}; r \in \mathbf{CD}$$
(13)

Domain:

$$0 \le Q_i^t \le 1 \tag{14}$$

$$a_{km}^{i}, d_{kl}^{t}, q_{i}^{k}, p_{r}^{t}, Q_{i}^{t} \ge 0 \ integer \qquad \forall \ t \in \mathbf{T}; k \in \mathbf{NP}; r \in \mathbf{CD}; i \in \mathbf{PL}$$
 (15)

$$x_{ki}^{t}, y_{kr}^{t}, u_{kil}^{t}, v_{kir}^{t}, w_{krl}^{t} \ge 0 \ integer \qquad \forall \ t \in \mathbf{T}; k \in \mathbf{NP}; r \in \mathbf{CD}; i \in \mathbf{PL}; l \in \mathbf{CL}$$
 (16)

$$h_{kr}^t, pr_{ki}^i, pr_{kr}^r, cc_{il}, cc_{rl}, cc_{ir}h_{im}^t, cm_f, cm_r, cm_n \ge 0 \quad \forall t \in \mathbf{T}; k \in \mathbf{NP}; r \in \mathbf{CD}; i \in \mathbf{PL}; l \in \mathbf{CL}$$
 (17)

## 3 Diff eq.

$$c\frac{\partial C_{mt}}{\partial t} = \frac{\partial \left(\frac{\partial C_{mcr}}{\partial t} + \frac{\partial C_{mpr}}{\partial t} + \frac{\partial C_{mpv}}{\partial t}\right)}{\partial E} + S \tag{18}$$