

# DFNA9 genotype ~ phenotype analysis

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## Introduction

This R Markdown notebook is used to document the various aspects of the genotype-phenotype analysis in many subjects with hereditary hearing loss based on mutation in the DFNA9 gene. We have data collected [...].

## Load R-packages

```
library(ggplot2)
library(drc)
```

```
## Loading required package: MASS
##
## 'drc' has been loaded.
## Please cite R and 'drc' if used for a publication,
## for references type 'citation()' and 'citation('drc')'.
##
## Attaching package: 'drc'
## The following objects are masked from 'package:stats':
##
##     gaussian, getInitial
```

```
library(sjPlot)
```

```
## Registered S3 methods overwritten by 'lme4':
##   method                      from
##   cooks.distance.influence.merMod car
##   influence.merMod              car
##   dfbeta.influence.merMod       car
##   dfbetas.influence.merMod      car
## Learn more about sjPlot with 'browseVignettes("sjPlot")'.
```

```
library("readxl")
library("nlme")
library(lme4)
```

```
## Loading required package: Matrix
##
## Attaching package: 'lme4'
```

```
## The following object is masked from 'package:nlme':
##
##      lmList
library(knitr)
library(forcats)
library(tidyr)

##
## Attaching package: 'tidyr'

## The following objects are masked from 'package:Matrix':
##
##      expand, pack, unpack
library(dplyr)

##
## Attaching package: 'dplyr'

## The following object is masked from 'package:nlme':
##
##      collapse
## The following object is masked from 'package:MASS':
##
##      select
## The following objects are masked from 'package:stats':
##
##      filter, lag
## The following objects are masked from 'package:base':
##
##      intersect, setdiff, setequal, union
```

## Load data and clean data-frames

Load data from Excel file and select only relevant columns/rows. The first analyses will be based on pure-tone average (PTA). The selected subset dataframe consists of the columns patient id (pid), group, age (Leeftijd), and the PTA (PTA54ADS).

```
data_raw <- read_excel("../data/raw_data/database_20-04-2020.xlsx")
data_raw$group = factor(data_raw$Domain)
#leave out data with only n=1 dataset per domain/certain unpublished data.
data_subset <- subset(data_raw, Smits=='no' & Domainrec!=1 & group!="Ivd1")
data <- subset(data_subset, select=c('pid', 'group', 'Leeftijd', 'PTA54ADS'))
data <- droplevels(data)
#data_raw %>% group_by(group) %>% summarize(count=n())
#head(data)
#check for NaNs in PTA and Leeftijd, should be 0.
nrow(data[is.na(data$PTA54ADS) | is.na(data$Leeftijd), ])

## [1] 0

#number (n) of counts (i.e. audiograms) per subject (pid)
summarytable <- data %>% count(group, pid)
```

## Group description

In the group of DFNA9 patients we have some for which there is longitudinal data, i.e. multiple audiograms over time/age (Leeftijd). First, create a table and histogram of number of measurements for each subject id (pid) across the groups

```
num_meas_per_id <- aggregate(PTA54ADS ~ pid , data, function(x) length(unique(x)))
t1 <- table(num_meas_per_id$PTA54ADS)
```

In total there are 283 subjects with 716 measurements; 159 patients with only 1 measurement and 123 patients with 2 or more measurements, see e.g. table 1 or the histogram.

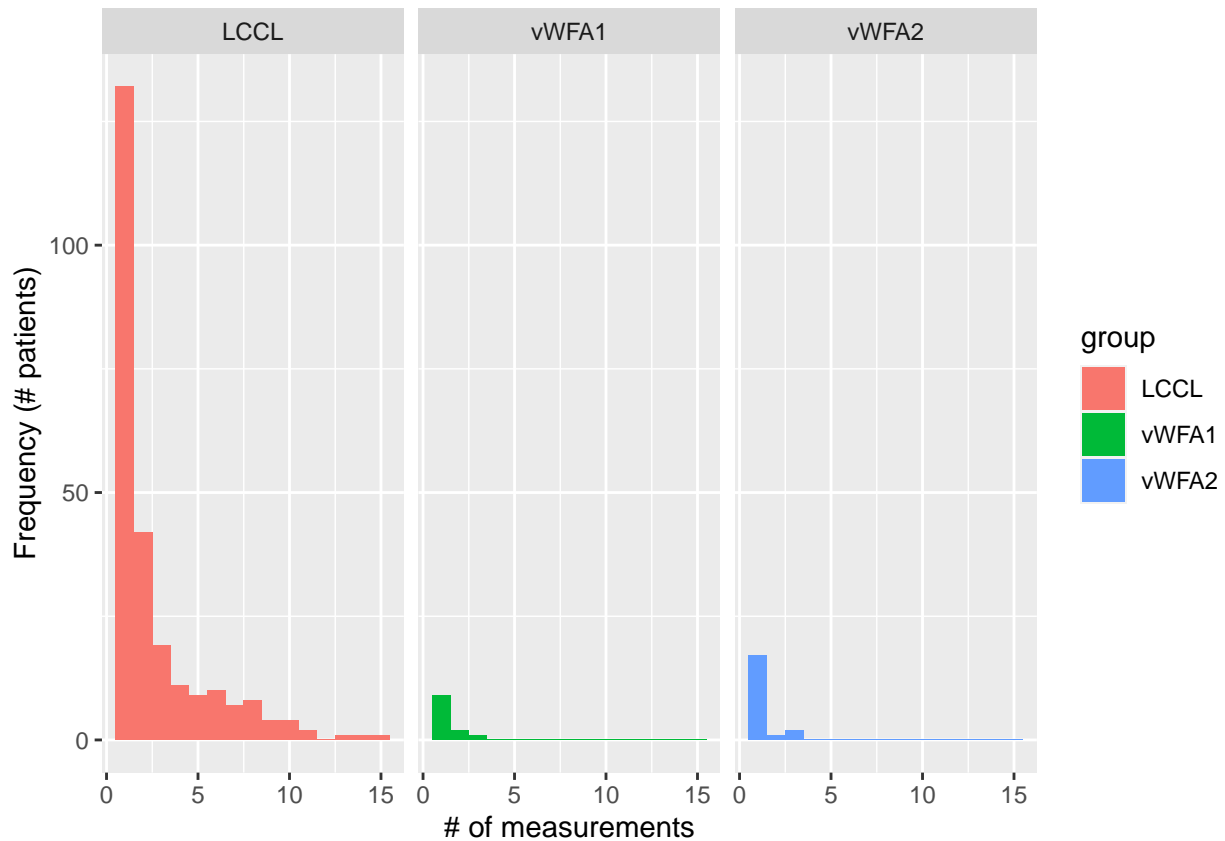
```
kable(t1, caption = "Table 1. The number of subjects that each have n audiograms", col.names = c("# aud
```

Table 1: Table 1. The number of subjects that each have n audiograms

| # audiograms | # subjects |
|--------------|------------|
| 1            | 159        |
| 2            | 47         |
| 3            | 21         |
| 4            | 10         |
| 5            | 13         |
| 6            | 11         |
| 7            | 4          |
| 8            | 7          |
| 9            | 3          |
| 10           | 3          |
| 11           | 3          |
| 12           | 1          |
| 15           | 1          |

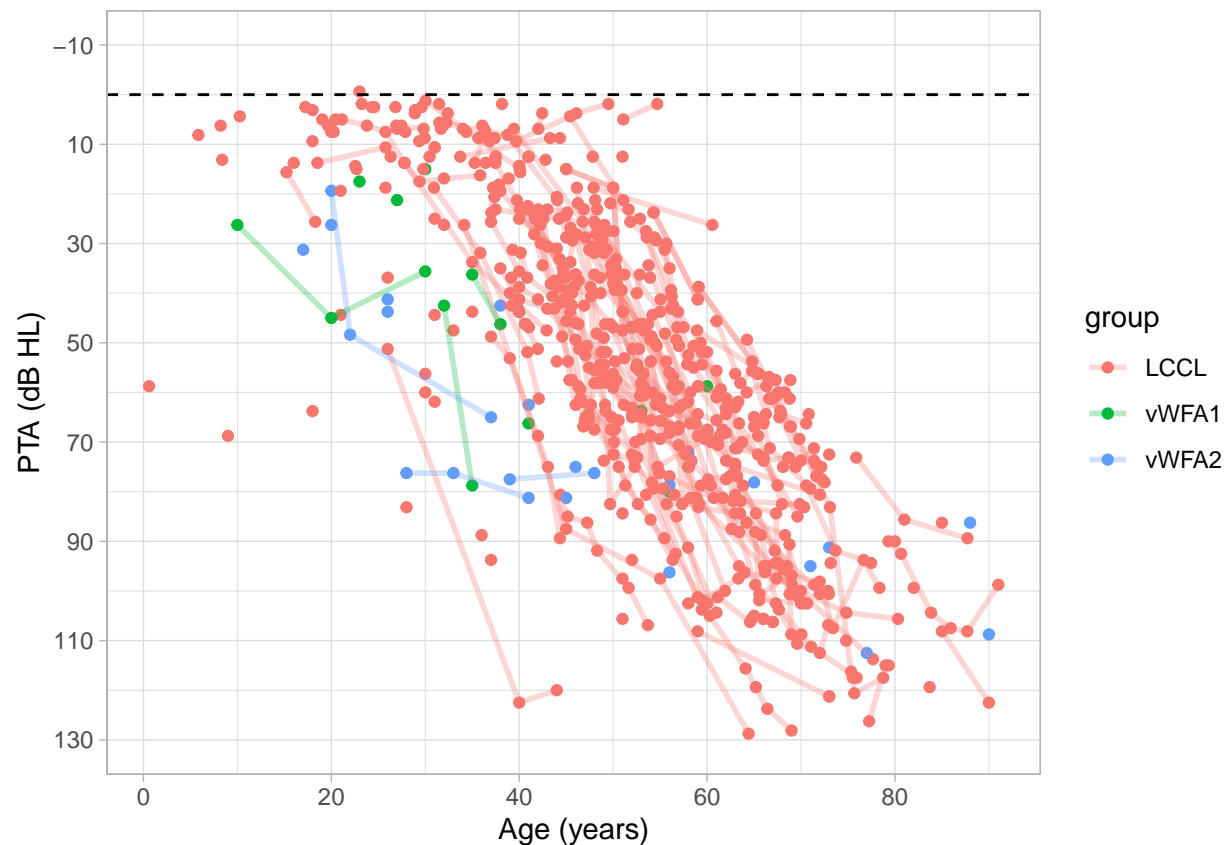
Now make a histogram of the number of audiograms across patients in each of the groups

```
ggplot(data=summarytable, aes(x=n,fill=group)) +
  geom_histogram(binwidth=1) +
  facet_wrap(~group) +
  xlab("# of measurements") +
  ylab("Frequency (# patients)")
```



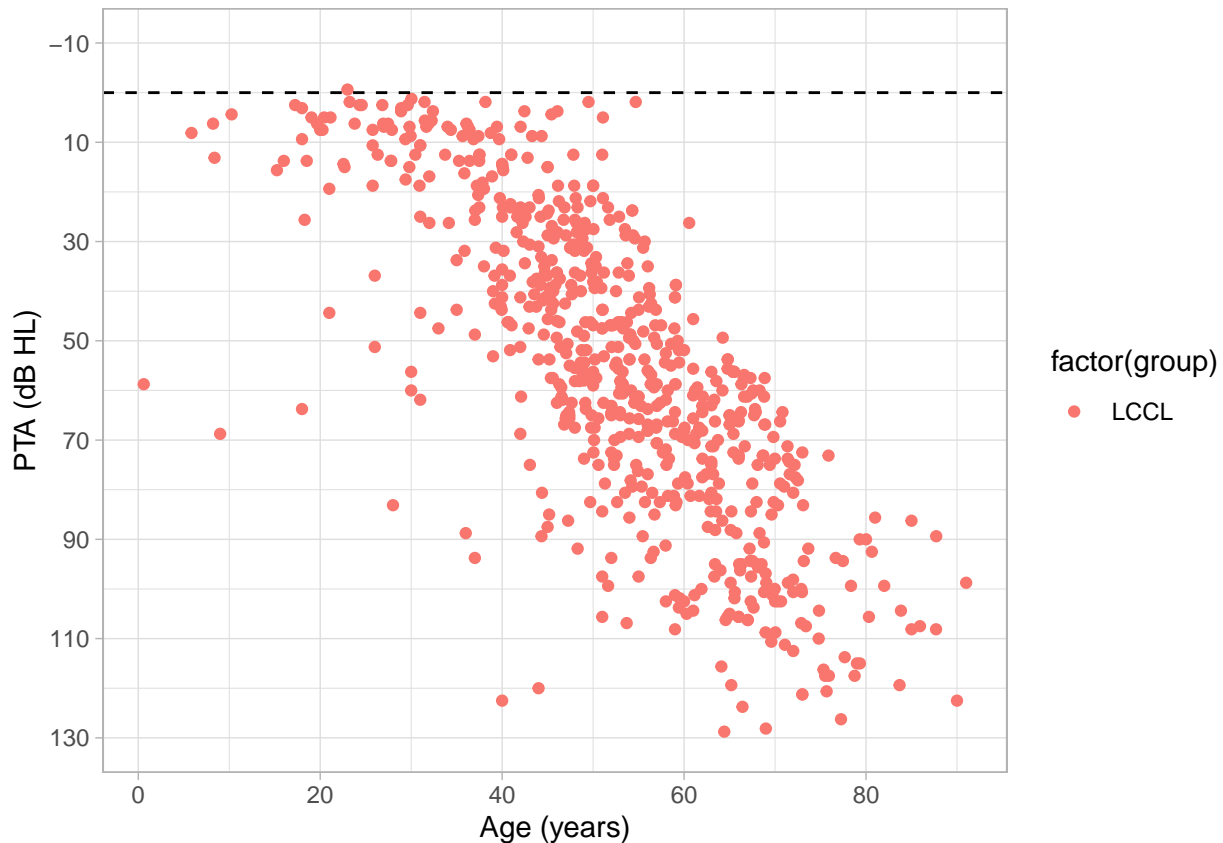
Relation of PTA with age for the different groups; connecting lines show longitudinal data of patients' PTA over time

```
ggplot(data, aes(x = Leeftijd, y = PTA54ADS, group = pid, color = group)) +
  #xlab("Age (years)") +
  #ylab("PTA (dB HL)") +
  geom_point(aes(colour = factor(group))) +
  geom_line(data=data, size=1, alpha = .3) +
  geom_hline(yintercept=0, linetype="dashed") +
  scale_x_continuous(breaks=seq(0,100,20)) +
  scale_y_reverse(breaks=seq(-10,130,20), limits=c(130,-10)) +
  #scale_y_reverse(limits=c(130,-10)) +
  xlab("Age (years)") +
  ylab("PTA (dB HL)") +
  theme_light()
```



## Logistic fit of PTA with age Perform non-linear fit; first focus on LCCL domain.

```
lccl = subset(data, group=="LCCL")
ggplot(lccl, aes(x=Leeftijd, y=PTA54ADS), group=pid, color=group) +
  xlab("Age (years)") +
  ylab("PTA (dB HL)") +
  geom_point(aes(colour = factor(group))) +
  geom_hline(yintercept=0, linetype="dashed") +
  scale_x_continuous(breaks=seq(0,100,20)) +
  scale_y_reverse(breaks=seq(-10,130,20), limits=c(130,-10)) +
  #scale_y_reverse(limits=c(130,-10)) +
  theme_light()
```



```
lin_fit <- nls(PTA54ADS ~ a*Leeftijd + b, lccl)
```

```
## Warning in nls(PTA54ADS ~ a * Leeftijd + b, lccl): No starting values specified for some parameters.
## Initializing 'a', 'b' to '1.'.
## Consider specifying 'start' or using a selfStart model
```

```
summary(lin_fit)
```

```
##
## Formula: PTA54ADS ~ a * Leeftijd + b
##
## Parameters:
##      Estimate Std. Error t value Pr(>|t|)
## a    1.60851    0.05331  30.170  <2e-16 ***
## b   -28.43929    2.89132  -9.836  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 20.01 on 673 degrees of freedom
##
## Number of iterations to convergence: 1
## Achieved convergence tolerance: 9.99e-10
```

```
nls_fit <- nls(PTA54ADS ~ a*Leeftijd^b, lccl, start = list(a = 0.05, b = 1.5))
summary(nls_fit)
```

```
##
## Formula: PTA54ADS ~ a * Leeftijd^b
##
```

```
## Parameters:
##   Estimate Std. Error t value Pr(>|t|)
## a  0.07298    0.01859   3.926 9.51e-05 ***
## b  1.66646    0.06175  26.988 < 2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 19.54 on 673 degrees of freedom
##
## Number of iterations to convergence: 5
## Achieved convergence tolerance: 2.93e-06

startvec <- c(Asym = 120, xmid = 50, scal = 15)
nls_logis<- nls(PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid, scal),
               data=lccl,
               start = startvec)
summary(nls_logis)
```

```
##
## Formula: PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid, scal)
##
## Parameters:
##   Estimate Std. Error t value Pr(>|t|)
## Asym  126.351    9.477   13.33 <2e-16 ***
## xmid   56.974    2.619   21.76 <2e-16 ***
## scal   15.410    1.371   11.24 <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 19.29 on 672 degrees of freedom
##
## Number of iterations to convergence: 4
## Achieved convergence tolerance: 3.603e-06
```

Compare power-law fit and the logistic function and display the results

```
anova(nls_fit,nls_logis)
```

```
## Analysis of Variance Table
##
## Model 1: PTA54ADS ~ a * Leeftijd^b
## Model 2: PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid, scal)
##   Res.Df Res.Sum Sq Df Sum Sq F value    Pr(>F)
## 1      673      257033
## 2      672      250020  1 7013.2   18.85 1.632e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

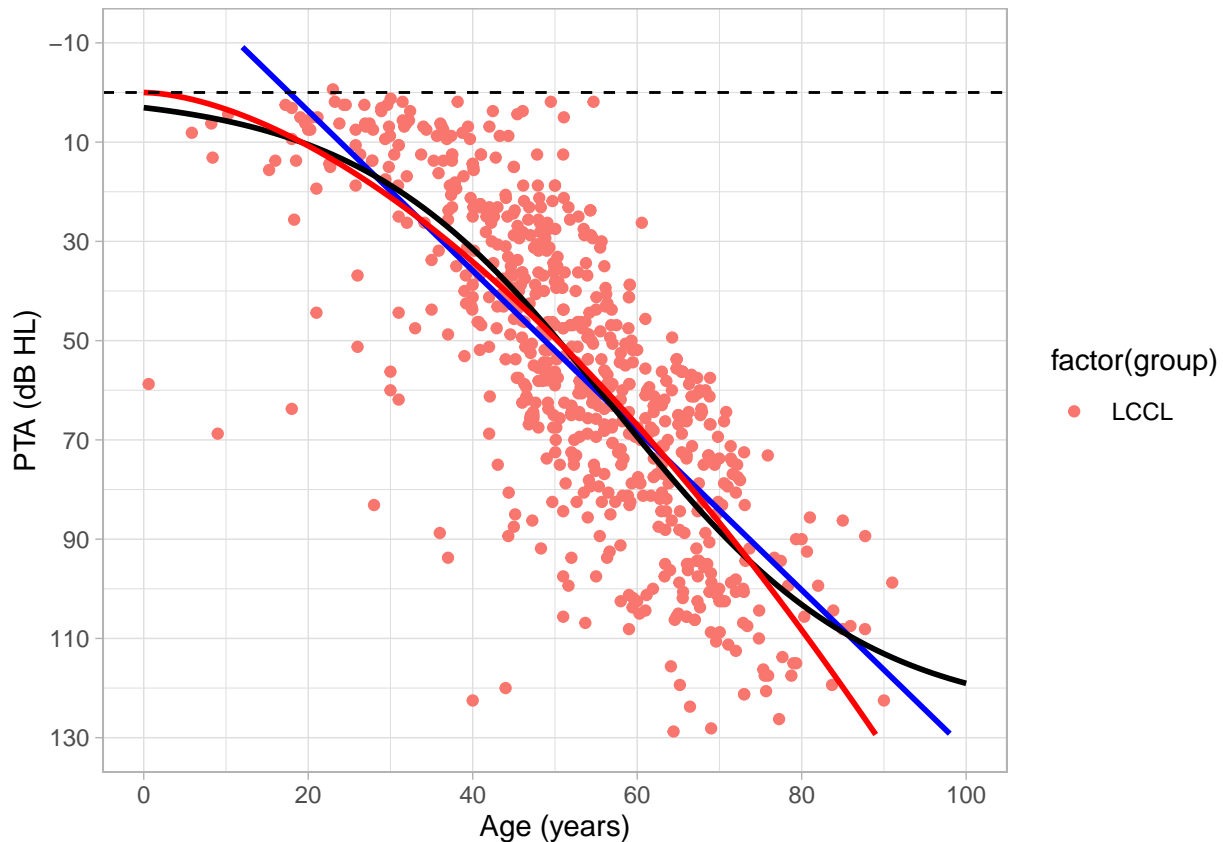
newdat = expand.grid(Leeftijd = seq(0, 100, by = 1))
newdat$lin <-predict(lin_fit, newdata = newdat)
newdat$pta_logistic <- predict(nls_logis,newdata = newdat)
newdat$pta_power <- predict(nls_fit,newdata = newdat)
#newdat
ggplot(lccl, aes(x=Leeftijd, y=PTA54ADS)) +
  geom_point(aes(colour = factor(group))) +
  geom_line(data = newdat, aes(y = lin), size = 1, col='blue') +
```

```
geom_line(data = newdat, aes(y = pta_logistic), size = 1) +
geom_line(data = newdat, aes(y = pta_power), size = 1, col='red') +

geom_hline(yintercept=0, linetype="dashed") +
scale_x_continuous(breaks=seq(0,100,20)) +
scale_y_reverse(breaks=seq(-10,130,20), limits=c(130,-10)) +
#scale_y_reverse(limits=c(130,-10)) +
xlab("Age (years)") +
ylab("PTA (dB HL)") +
theme_light()
```

```
## Warning: Removed 14 row(s) containing missing values (geom_path).
```

```
## Warning: Removed 11 row(s) containing missing values (geom_path).
```



As we can see, the logistic function (SSlogis) describes the data better than the power-law function ( $F = 18.9$ ;  $p = 1.6 \times 10^{-5}$ ). This function has also been used in describing the (frequency-specific) thresholds in Pauw et al., 2011 and will be used in the subsequent sections.

## Group comparison

The main question is whether the function that describes the PTA (dB HL) as a function of age (years) differs between the groups @ref(fig:plot\_pta\_age\_groups).

Start with a group-fit; discarding grouping information

```
fit0 <- nls(PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid, scal), data=data)
summary(fit0)
```



```
##
## Formula: PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid, scal)
##
## Parameters:
##      Estimate Std. Error t value Pr(>|t|)
## Asym   135.557    12.188   11.12  <2e-16 ***
## xmid    59.258     3.517   16.85  <2e-16 ***
## scal    17.807     1.639   10.86  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 19.78 on 713 degrees of freedom
##
## Number of iterations to convergence: 4
## Achieved convergence tolerance: 2.948e-06
```

```
coef(fit0)
```

```
##      Asym      xmid      scal
## 135.55740  59.25776  17.80669
```

Now, add a grouping-variable with the mid-point (xmid)

```
# https://stats.stackexchange.com/questions/27273/how-do-i-fit-a-nonlinear-mixed-effects-model-for-repe
# https://stats.stackexchange.com/questions/316801/how-to-compare-logistic-regression-curves
fit1 <- nls(PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid[group], scal),
           data=data,
           start=list(Asym=rep(120,1), xmid=rep(50,3), scal=rep(15,1)))
summary(fit1)
```

```
##
## Formula: PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid[group], scal)
##
## Parameters:
##      Estimate Std. Error t value Pr(>|t|)
## Asym   116.114     6.242   18.60  <2e-16 ***
## xmid1   54.188     1.813   29.89  <2e-16 ***
## xmid2   43.644     3.462   12.61  <2e-16 ***
## xmid3   34.631     3.185   10.87  <2e-16 ***
## scal    14.394     1.127   12.77  <2e-16 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 19.13 on 711 degrees of freedom
##
## Number of iterations to convergence: 7
## Achieved convergence tolerance: 4.654e-06
```

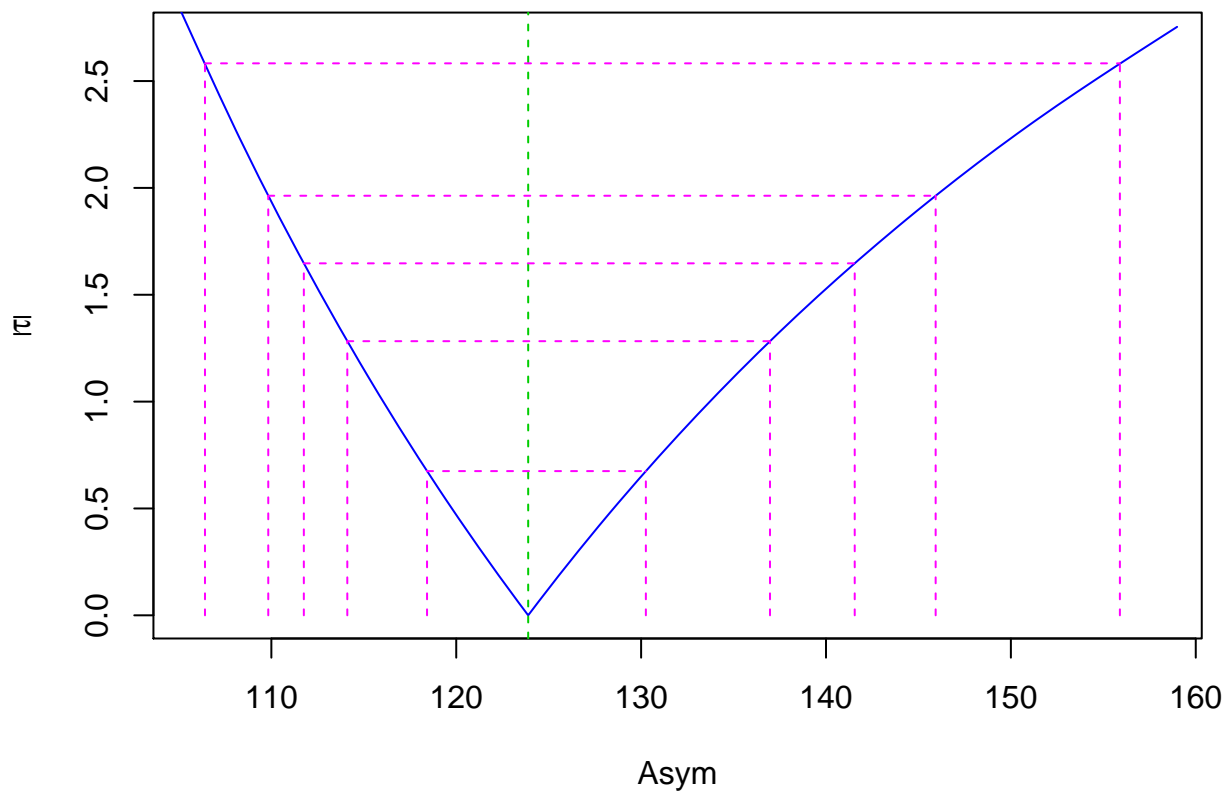
And add the scaling [scal] as a grouping variable; does it further explain differences between groups?

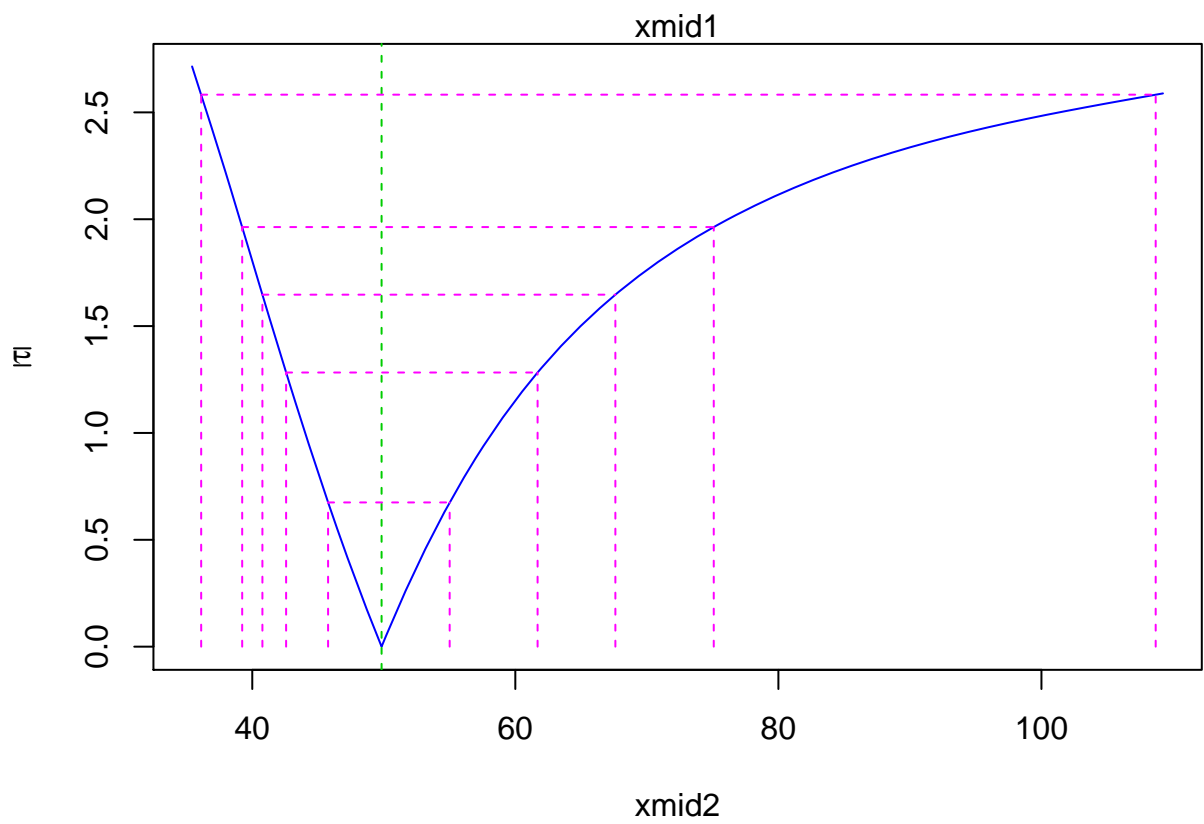
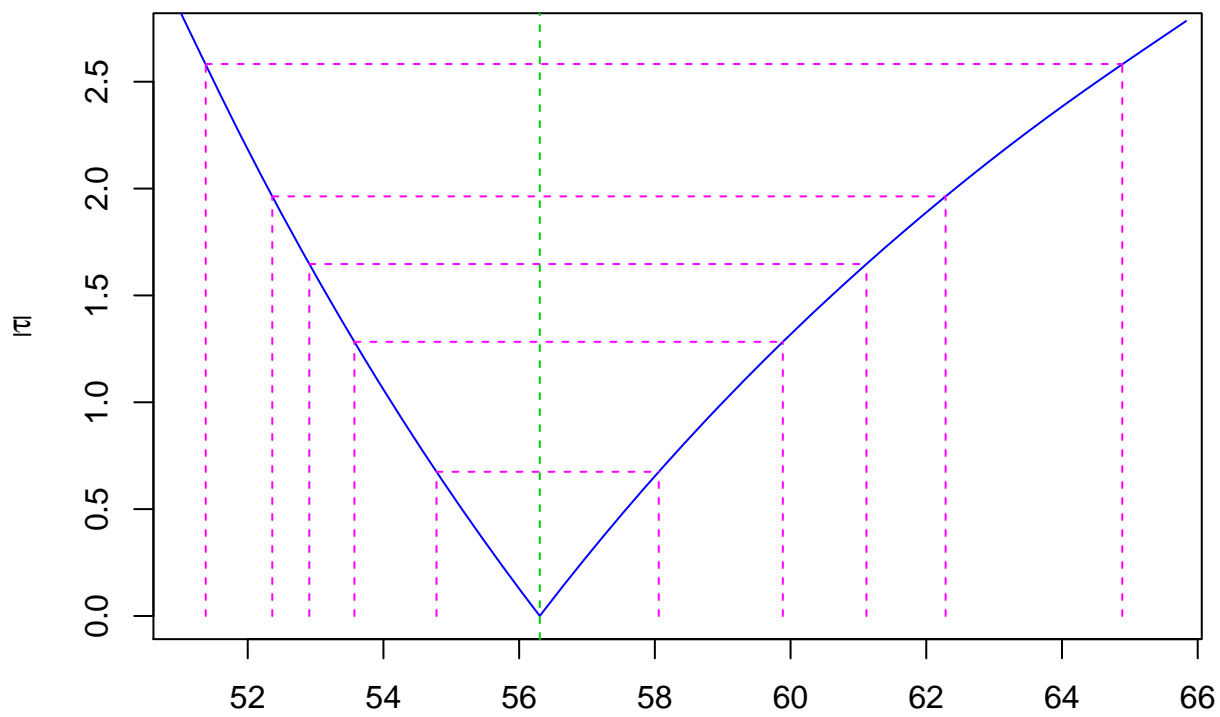
```
fit2 <- nls(PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid[group], scal[group]),
           data=data,
           start=list(Asym=rep(120,1), xmid=rep(50,3), scal=rep(15,3)))
summary(fit2)
```

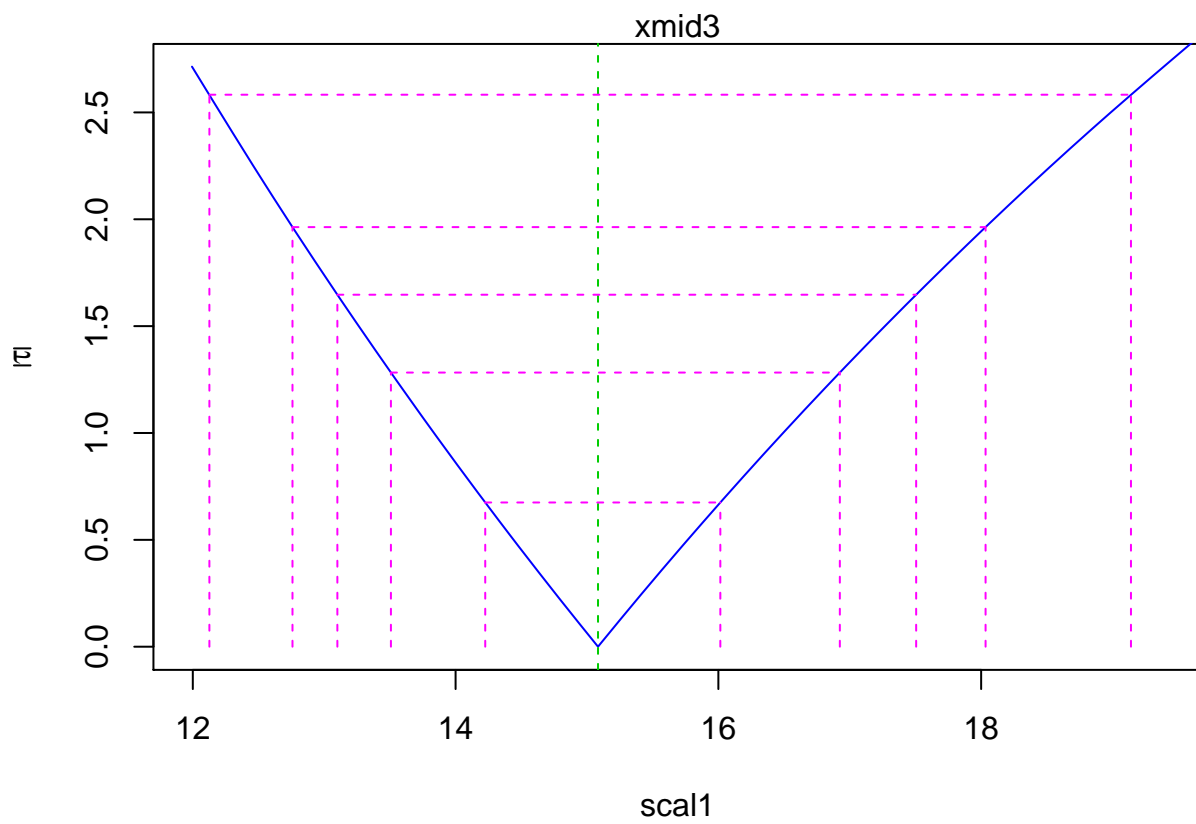
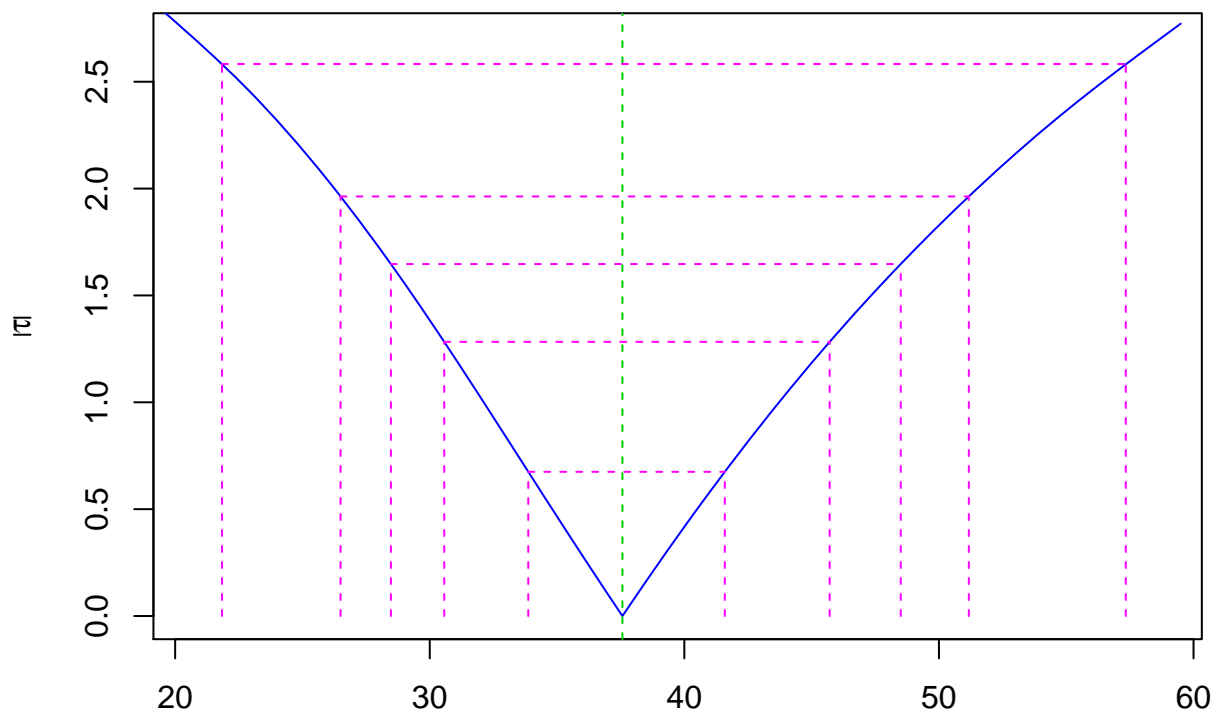
```
##
## Formula: PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid[group], scal[group])
```

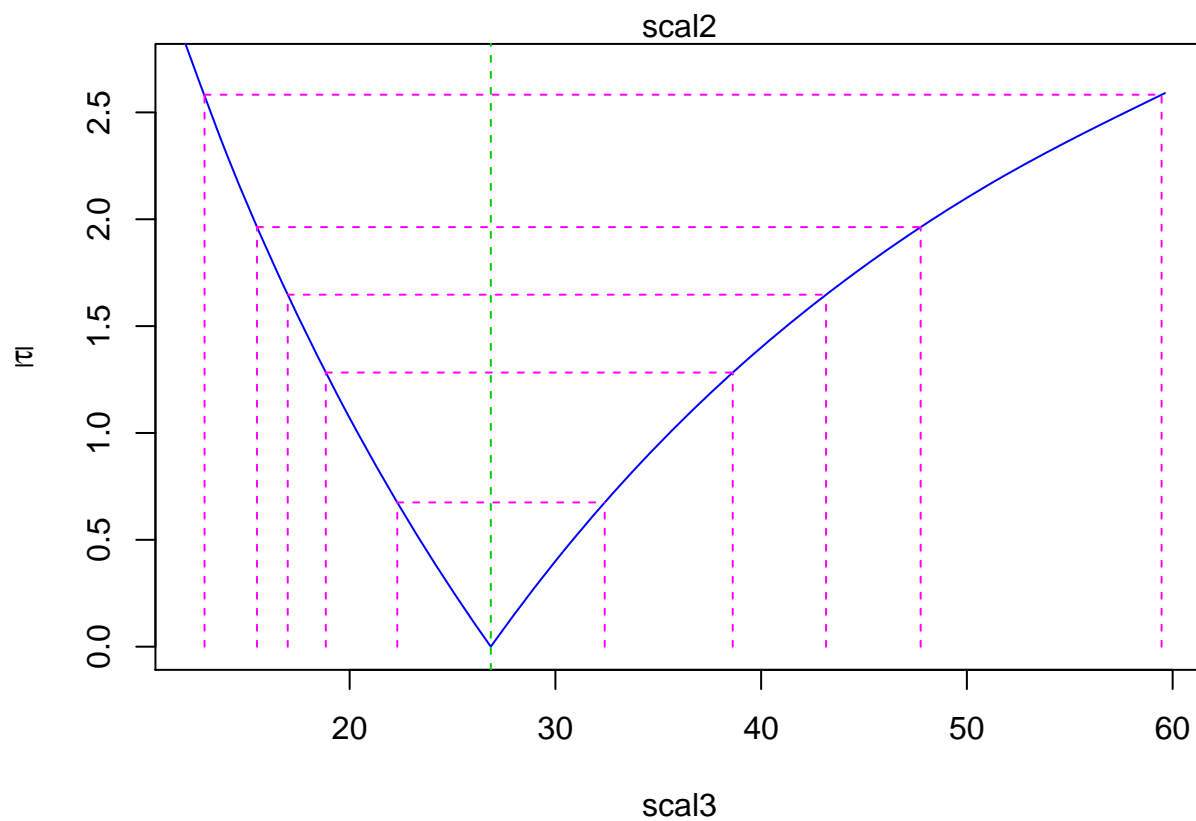
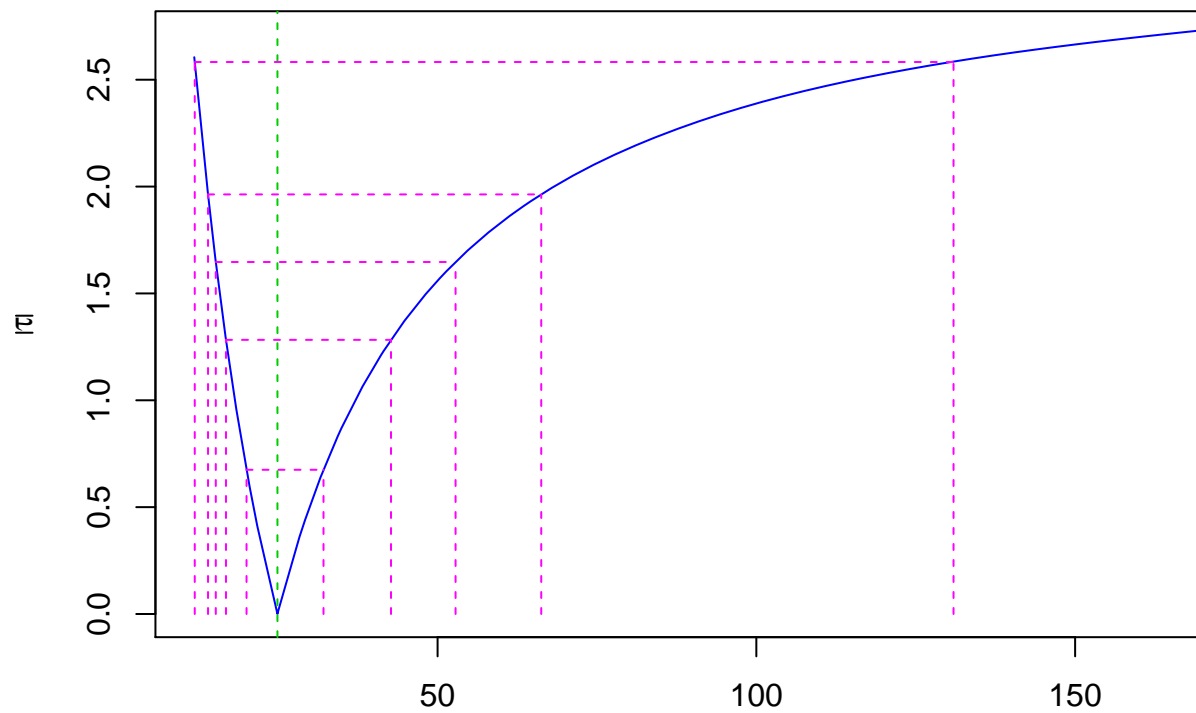
```
##
## Parameters:
##      Estimate Std. Error t value Pr(>|t|)
## Asym    123.891      8.563  14.468 < 2e-16 ***
## xmid1    56.304      2.381  23.652 < 2e-16 ***
## xmid2    49.833      6.541   7.618 8.24e-14 ***
## xmid3    37.568      5.595   6.715 3.86e-11 ***
## scal1    15.084      1.291  11.682 < 2e-16 ***
## scal2    24.884      8.419   2.956 0.00322 **
## scal3    26.860      6.824   3.936 9.09e-05 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 19.05 on 709 degrees of freedom
##
## Number of iterations to convergence: 6
## Achieved convergence tolerance: 2.195e-06
```

```
plot(profile(fit2))
```









And now add the asymptotic value of the fit (Leeftijd -> infinity) (Asym):

```
fit3 <- nls(PTA54ADS ~ SSlogis(Leeftijd, Asym[group], xmid[group], scal[group]),
  data=data,
  start=list(Asym=rep(120,3), xmid=rep(50,3), scal=rep(15,3)))
```

```
summary(fit3)
```

```
##
## Formula: PTA54ADS ~ SSlogis(Leeftijd, Asym[group], xmid[group], scal[group])
##
## Parameters:
##      Estimate Std. Error t value Pr(>|t|)
## Asym1  126.350      9.361  13.497 < 2e-16 ***
## Asym2   89.933     60.449   1.488  0.1373
## Asym3   97.280     10.751   9.049 < 2e-16 ***
## xmid1   56.974      2.587  22.025 < 2e-16 ***
## xmid2   34.989     26.673   1.312  0.1900
## xmid3   27.148      4.666   5.819 8.99e-09 ***
## scal1   15.410      1.354  11.383 < 2e-16 ***
## scal2   17.424     17.929   0.972  0.3315
## scal3   13.988      5.807   2.409  0.0163 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 19.05 on 707 degrees of freedom
##
## Number of iterations to convergence: 8
## Achieved convergence tolerance: 3.258e-06
```

Now test the various models. Which of the parameters explain the data best?

```
anova(fit0,fit1,fit2,fit3)
```

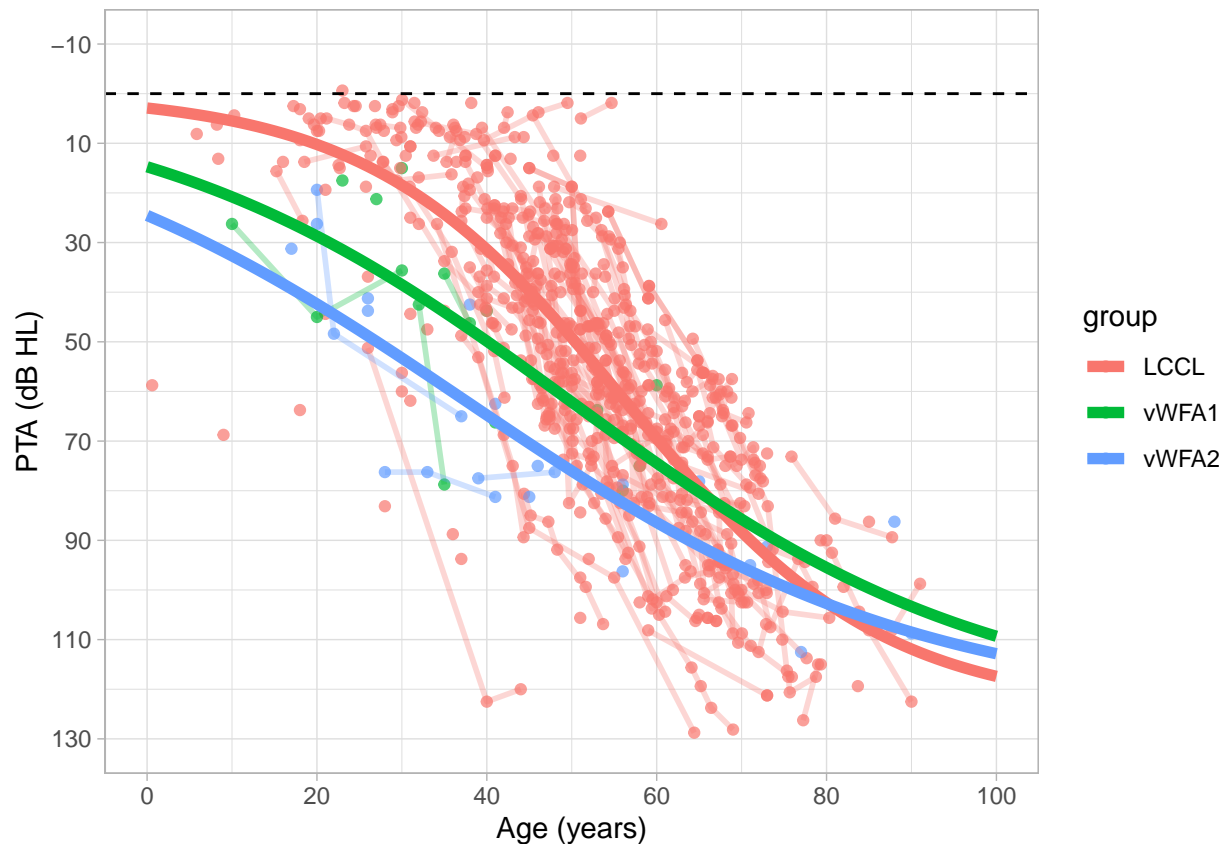
```
## Analysis of Variance Table
##
## Model 1: PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid, scal)
## Model 2: PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid[group], scal)
## Model 3: PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid[group], scal[group])
## Model 4: PTA54ADS ~ SSlogis(Leeftijd, Asym[group], xmid[group], scal[group])
##   Res.Df Res.Sum Sq Df Sum Sq F value    Pr(>F)
## 1     713    279067
## 2     711    260324  2 18743.2 25.5958 1.844e-11 ***
## 3     709    257309  2  3014.8  4.1535  0.01609 *
## 4     707    256670  2    639.6  0.8809  0.41487
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

It turns out the both the variables [xmid] and [scale], i.e. the midpoint and slope at the midpoint significantly differ between the three groups, but that adding the asymptotic value does not describe the data significantly better.

```
newdat = expand.grid(Leeftijd = seq(0, 100, by = 1), group = c("LCCL","vWFA1","vWFA2"))
newdat$fit <- predict(fit2, newdata = newdat)
```

```
ggplot(data, aes(x=Leeftijd, y=PTA54ADS, group = pid, color = group)) +
  geom_point(aes(colour = factor(group)), alpha = .7) +
  geom_line(data=data, size=1, alpha = .3) +
  geom_line(data = newdat, aes(y = fit, group = group, colour = factor(group)), size = 2) +
  geom_hline(yintercept=0, linetype="dashed") +
  scale_x_continuous(breaks=seq(0,100,20)) +
  scale_y_reverse(breaks=seq(-10,130,20), limits=c(130,-10)) +
```

```
#scale_y_reverse(limits=c(130,-10)) +
xlab("Age (years)") +
ylab("PTA (dB HL)") +
theme_light()
```



Now perform fit on individual data by subsetting the data to keep individuals with more than 4 longitudinal datapoints. Is it the case that using a non-linear mixed-model approach may help us?

```
#https://stackoverflow.com/questions/14439770/filter-rows-in-dataframe-by-number-of-rows-per-level-of-a
pidlengths <- ave(as.numeric(data$pid),
                  data$pid, FUN = length)
#df2 <- lccl[pidlengths > 5, ]
df2 <- data[pidlengths > 2, ]
with(df2, table(group))
```

```
## group
## LCCL vWFA1 vWFA2
## 459 3 6
```

```
models <- nlsList(PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid, scal) | pid, data = df2)
```

```
## Warning: 37 errors caught in (attr(object, "initial"))(mCall = mCall, data = data, LHS = LHS). The
##
## singular matrix 'a' in solve
## 1
## singular gradient
## 2
## step factor 0.000488281 reduced below 'minFactor' of 0.000976562
```

```
## 12
## too few distinct input values to fit a logistic model
## 22
```

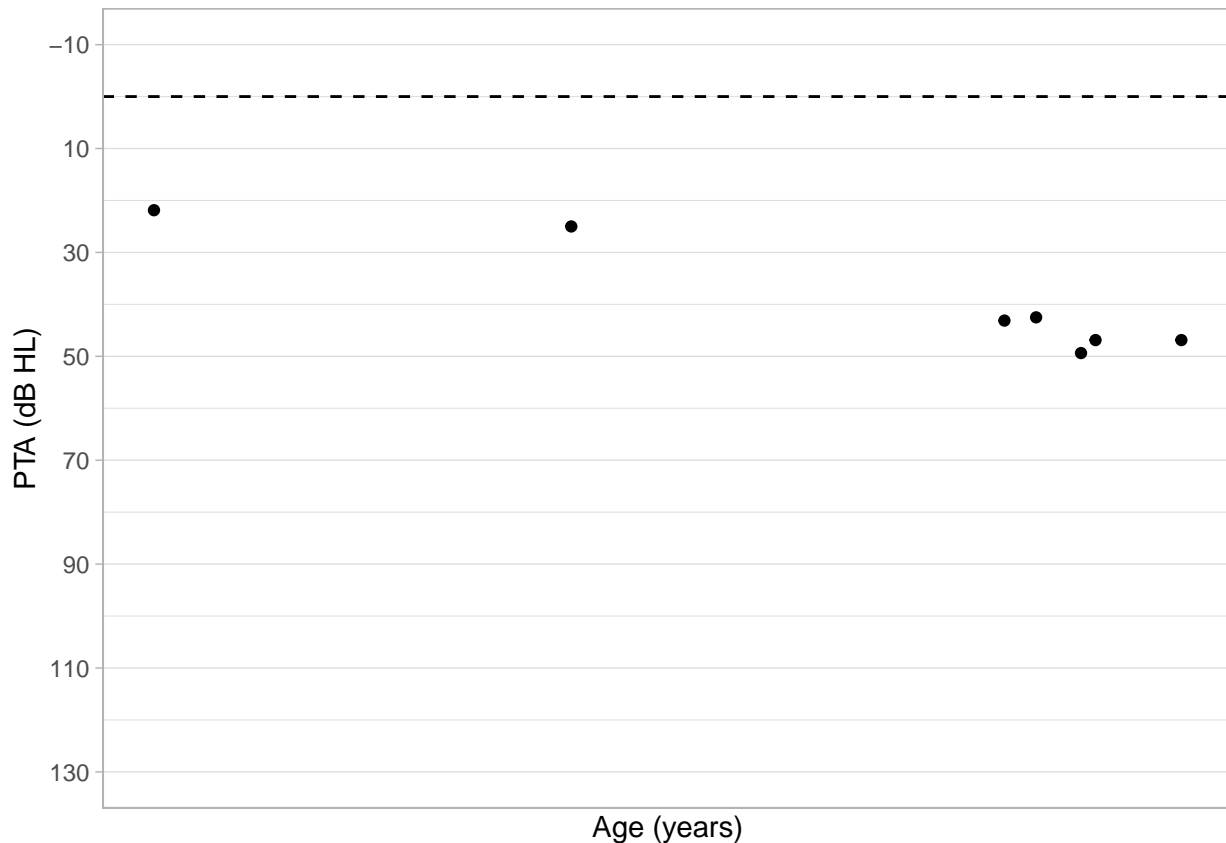
As we can see, some model-predictions failed; they end up with NaNs in the model fit list (nlslist); see e.g. pid 147

```
data_id <- subset(df2, pid=="147")
data_id
```

```
## # A tibble: 7 x 4
##   pid group Leeftijd PTA54ADS
##   <dbl> <fct>   <dbl>   <dbl>
## 1   147 LCCL    49.7    21.9
## 2   147 LCCL    52.9    25
## 3   147 LCCL    56.4    42.5
## 4   147 LCCL    56.1    43.1
## 5   147 LCCL    56.8    46.9
## 6   147 LCCL    57.5    46.9
## 7   147 LCCL    56.7    49.4
```

```
ggplot(data=data_id, aes(x=Leeftijd, y=PTA54ADS)) +
  geom_point() +
  geom_hline(yintercept=0, linetype="dashed") +
  scale_x_continuous(breaks=seq(0,100,20)) +
  scale_y_reverse(breaks=seq(-10,130,20), limits=c(130,-10)) +
  #scale_y_reverse(limits=c(130,-10)) +
  xlab("Age (years)") +
  ylab("PTA (dB HL)") +
  theme_light()
```





Predict for all pid's the fit to the model and remove the pid's that give NaNs. Check how many subjects per group we end up with.

```
df2$Pred <- predict(models)
df2_na <- na.omit(df2)
with(df2_na, table(group, pid))
```

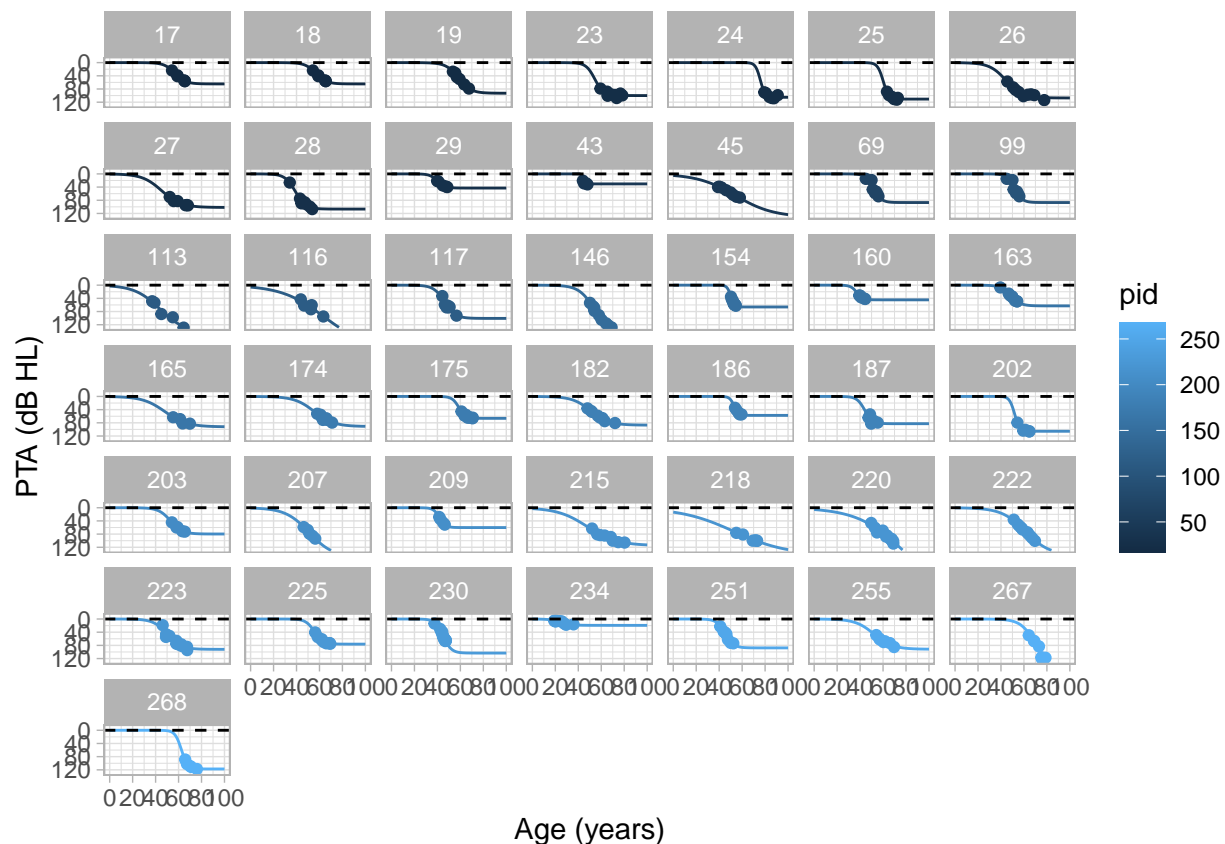
```
##      pid
## group 17 18 19 23 24 25 26 27 28 29 43 45 69 99 113 116 117 146 154 160 163
## LCCL   6  6  6  8  6  6  9  6  9  5  4  8  7  7  5  5  7  10  10  5  8
## vWFA1  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0
## vWFA2  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0
##      pid
## group 165 174 175 182 186 187 202 203 207 209 215 218 220 222 223 225 230 234
## LCCL   4  7  8  8  5  6  5  5  5  4  8  6  11  10  11  9  14  10
## vWFA1  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0
## vWFA2  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0  0
##      pid
## group 251 255 267 268
## LCCL   8  7  8  5
## vWFA1  0  0  0  0
## vWFA2  0  0  0  0
```

We only keep the pid's from the LCCL group. The pid's in the other groups are not properly fitted.

```
le <- unique(df2_na$pid)
#le
newdat = expand.grid(Leeftijd = seq(0, 100, by = 1), pid=le)
newdat$prednlm <- predict(models, newdata=newdat)
```

<https://stackoverflow.com/questions/37122994/plotting-a-list-of-non-linear-regressions-with-ggplot>  
<https://aosmith.rbind.io/2018/11/16/plot-fitted-lines/>

```
ip <- ggplot(data=df2_na, aes(x=Leeftijd, y=PTA54ADS, colour = pid)) +
  geom_point() +
  geom_line(data=newdat, aes(y=prednlm)) +
  facet_wrap(~pid) +
  geom_hline(yintercept=0, linetype="dashed") +
  scale_x_continuous(breaks=seq(0,100,20)) +
  scale_y_reverse(breaks=seq(0,120,40), limits=c(130,-10)) +
  #scale_y_reverse(limits=c(130,-10)) +
  xlab("Age (years)") +
  ylab("PTA (dB HL)") +
  theme_light()
ip
```

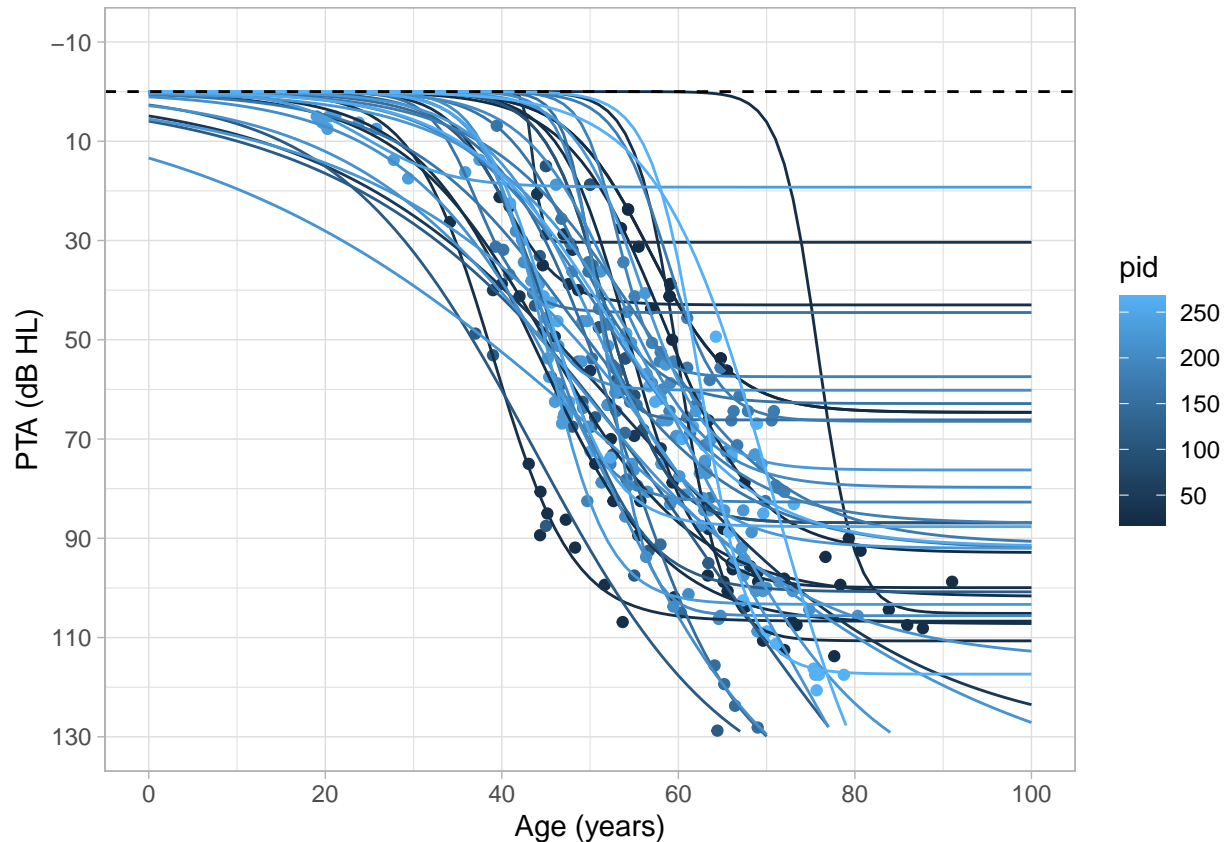


So, it seems we can fit the data for individual subjects by some extent. It often ‘fails’ by over- or underestimating the tail (coef.lm1st Asym column). We can also plot it all in one figure.

```
ggplot(data=df2_na, aes(x=Leeftijd, y=PTA54ADS, colour = pid)) +
  geom_point() +
  geom_line(data=newdat, aes(y=prednlm, group = pid)) +
  geom_hline(yintercept=0, linetype="dashed") +
  scale_x_continuous(breaks=seq(0,100,20)) +
  scale_y_reverse(breaks=seq(-10,130,20), limits=c(130,-10)) +
  #scale_y_reverse(limits=c(130,-10)) +
  xlab("Age (years)") +
```

```
ylab("PTA (dB HL)" +  
theme_light())
```

```
## Warning: Removed 176 row(s) containing missing values (geom_path).
```



Feed the remaining data into the non-linear mixed-models with the parameters Asym, xmid, and scal as random factors.

```
nm1 <- nlmer(PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid, scal) ~ Asym + xmid + scal | pid, df2_na, start =  
summary(nm1)
```

```
## Warning in vcov.merMod(object, use.hessian = use.hessian): variance-covariance matrix computed from  
## not positive definite or contains NA values: falling back to var-cov estimated from RX
```

```
## Warning in vcov.merMod(object, correlation = correlation, sigma = sig): variance-covariance matrix co  
## not positive definite or contains NA values: falling back to var-cov estimated from RX
```

```
## Nonlinear mixed model fit by maximum likelihood ['nlmerMod']
```

```
## Formula: PTA54ADS ~ SSlogis(Leeftijd, Asym, xmid, scal) ~ Asym + xmid +
```

```
## scal | pid
```

```
## Data: df2_na
```

```
##
```

```
## AIC BIC logLik deviance df.resid
```

```
## 2152.6 2189.9 -1066.3 2132.6 297
```

```
##
```

```
## Scaled residuals:
```

```
## Min 1Q Median 3Q Max
```

```
## -3.14923 -0.50051 -0.03471 0.44682 2.94717
```

```
##
```

```
## Random effects:
##   Groups   Name Variance Std.Dev.  Corr
##   pid      Asym 166.742  12.913
##           xmid 44.562   6.675   0.23
##           scal 4.541   2.131  -0.53  0.11
## Residual      24.231   4.922
## Number of obs: 307, groups:  pid, 43
##
## Fixed effects:
##       Estimate Std. Error t value
## Asym 113.0219     3.6536   30.93
## xmid  52.5762     1.1214   46.88
## scal   8.4703     0.5342   15.86
##
## Correlation of Fixed Effects:
##       Asym  xmid
## xmid 0.409
## scal 0.343 0.265
```

```
coef(nm1)
```

```
## $pid
##       Asym      xmid      scal
## 17 111.91187 65.06896 9.290262
## 18 111.91187 65.06896 9.290262
## 19 118.54557 61.92052 7.638449
## 23 105.58459 49.24825 8.413491
## 24 108.87821 59.45191 9.966515
## 25 120.90609 54.73558 7.417888
## 26 109.08970 44.38473 7.839455
## 27 104.65608 46.09939 8.880052
## 28 113.29662 39.58856 5.379525
## 29 110.04858 52.98010 9.196106
## 43 113.90947 55.69913 8.459887
## 45  97.34802 45.33117 11.001626
## 69 126.47538 55.14536 5.067873
## 99 126.47538 55.14536 5.067873
## 113 123.85066 40.51042 7.292063
## 116 108.56522 47.02774 9.350318
## 117 118.05750 48.05015 6.749991
## 146 134.07677 52.99453 5.877904
## 154 124.71754 54.34416 5.675409
## 160 109.08630 48.12987 9.147920
## 163 117.51108 56.10667 7.451837
## 165  99.26396 50.66147 10.224177
## 174 102.01522 57.42787 10.467515
## 175  97.48613 60.86962 11.260595
## 182  98.61739 53.12833 10.230050
## 186 116.11258 59.74771 8.184632
## 187 108.57918 45.24103 8.603256
## 202 118.30537 48.75103 6.916644
## 203 106.80804 56.87895 9.709881
## 207 117.38917 46.67863 7.318511
## 209 117.73015 48.63513 6.977685
## 215 107.53529 48.52569 9.239854
```

```
## 218 107.19360 48.27288 9.002671
## 220 115.49471 52.50751 8.928806
## 222 118.37714 57.36307 8.206486
## 223 106.36951 52.52182 8.571337
## 225 102.56742 57.96347 10.083785
## 230 126.08938 46.73509 4.317173
## 234 106.64376 50.20636 10.065763
## 251 120.23932 48.56520 5.913720
## 255 102.15156 53.94762 10.178729
## 267 141.71632 68.79567 5.386864
## 268 126.58949 58.22265 6.962851
```

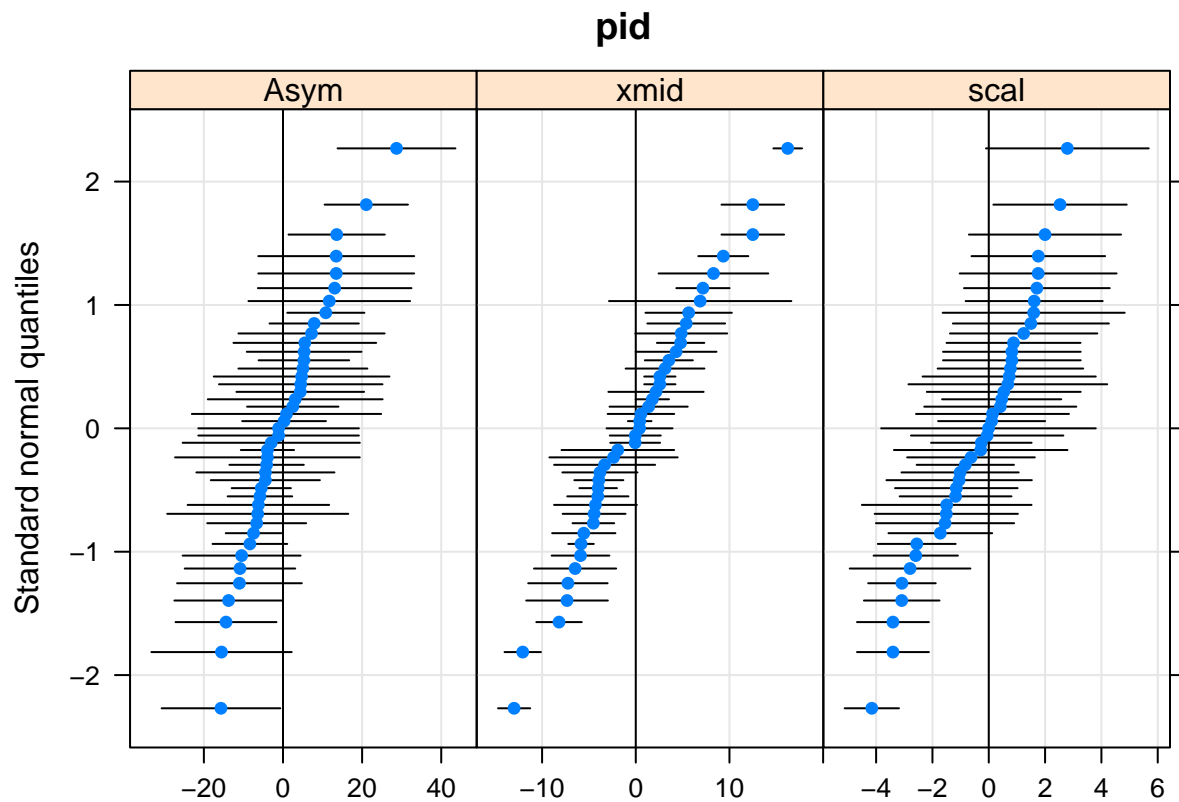
```
##
## attr("class")
## [1] "coef.mer"
```

```
require(lattice)
```

```
## Loading required package: lattice
```

```
qqmath(ranef(nm1, condVar=TRUE))
```

```
## $pid
```



Now subset the data to contain individual frequencies

```
data_all <- subset(data_subset, select=c('pid', 'group', 'Leeftijd', '250.AD', '500.AD', '1000.AD', '2000',
head(data_all)
```

```
## # A tibble: 6 x 15
##   pid group Leeftijd `250.AD` `500.AD` `1000.AD` `2000.AD` `4000.AD` `8000.AD`
##   <dbl> <fct>   <dbl>   <dbl>   <dbl>   <dbl>   <dbl>   <dbl>   <dbl>
```

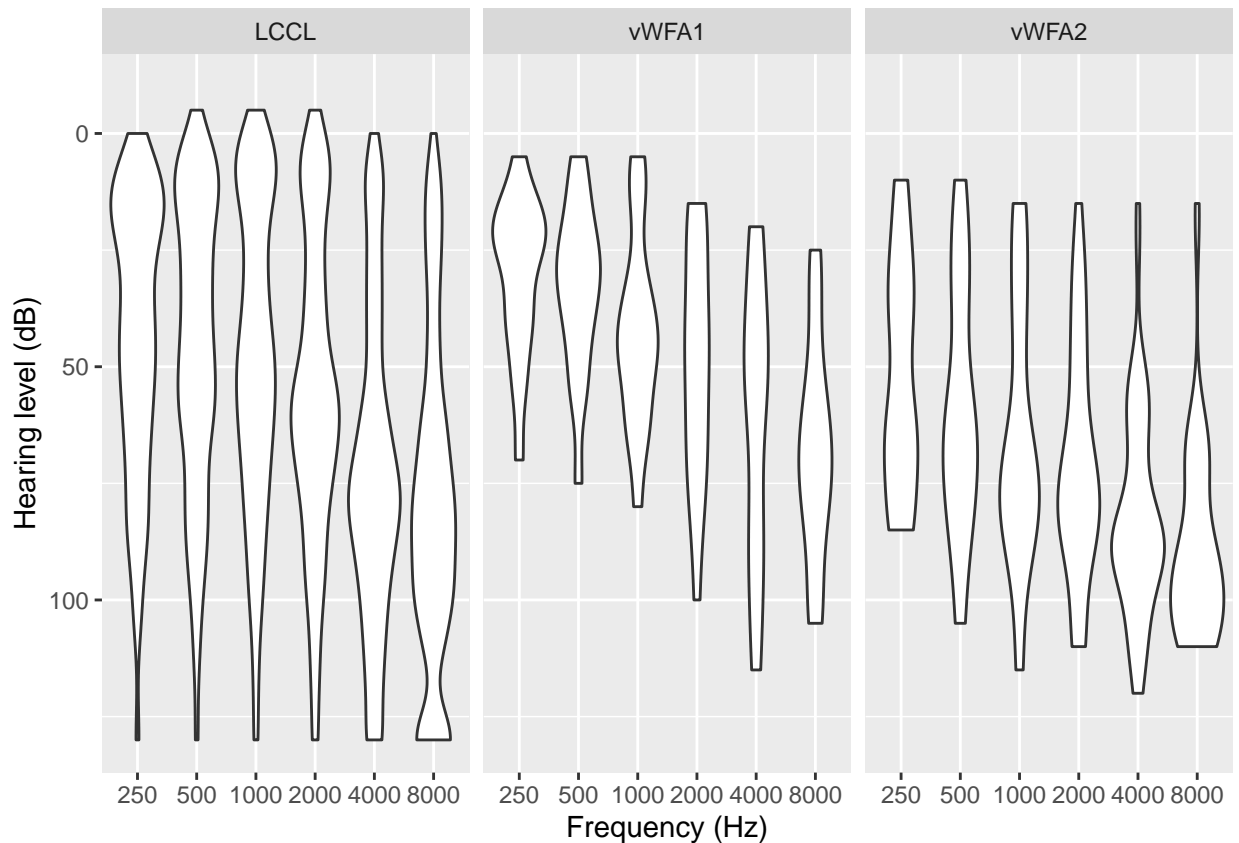
```
## 1      1 LCCL      60      NA      45      50      60      80      85
## 2      2 LCCL      82      70      75     100     130     130      NA
## 3      3 LCCL      68      80      80      80      90     130     130
## 4      4 LCCL      48      10       5      10      15      65      60
## 5      4 LCCL      55      20      20      15      40      80      85
## 6      5 LCCL      48       5       5       0       0      45      60
## # ... with 6 more variables: `250.AS` <dbl>, `500.AS` <dbl>, `1000.AS` <dbl>,
## #   `2000.AS` <dbl>, `4000.AS` <dbl>, `8000.AS` <dbl>
```

Convert 'wide' dataset into 'long' format using tidyr and remove NaNs

```
tidier <- data_all %>%
  gather(f, dB, -pid, -group, -Leeftijd)
data_all_l <- tidier %>%
  separate(f, into = c("frequency", "ear"), sep = "\\.")
#head(data_all_l)
data_all_l$frequency = factor(data_all_l$frequency)
data_all_l$ear = factor(data_all_l$ear)
data_all_l <- na.omit(data_all_l)
#head(data_all_l)

p <- data_all_l %>%
  mutate(frequency = fct_relevel(frequency, "250", "500", "1000", "2000", "4000", "8000")) %>%
  ggplot(aes(x = frequency, y = dB)) +
    #geom_bar(stat="identity") +
    #geom_histogram() +
    geom_violin() +
    facet_wrap(~ group, ncol = 3) +
    #geom_point()
    xlab("Frequency (Hz)") +
    ylab("Hearing level (dB)") +
    scale_y_reverse(limits=c(130,-10))
    #theme_classic()

p
```



simple linear model: PTA is a function of the affected domain; here are two levels in this mixed model; 1: timepoints for each patient; 2: genetic domain, with domain the fixed effect and patient the random effect allowing the intercept to vary across patient ( $\sim 1|pid$ ).

```
random_intercept <-lme(dB ~ frequency ,
  random = ~1|pid,      #p. 896
  method = "ML",
  na.action = na.exclude,
  control = list(opt="optim"),
  correlation = corAR1(), #see p.897; timepoints are not equally spaced;use corCAR1
  data = data_all_1)
summary(random_intercept)
```

```
## Linear mixed-effects model fit by maximum likelihood
## Data: data_all_1
##      AIC      BIC logLik
##  70816 70879.26 -35399
##
## Random effects:
## Formula: ~1 | pid
##      (Intercept) Residual
## StdDev:    30.66465 17.63885
##
## Correlation Structure: AR(1)
## Formula: ~1 | pid
## Parameter estimate(s):
##      Phi
## 0.4384654
```

```
## Fixed effects: dB ~ frequency
##           Value Std.Error   DF  t-value p-value
## (Intercept)  43.50693 1.9538723 8068 22.26703  0.0000
## frequency2000  6.76735 0.6766851 8068 10.00074  0.0000
## frequency250  -2.45973 0.7709764 8068 -3.19041  0.0014
## frequency4000 22.58725 0.7647918 8068 29.53386  0.0000
## frequency500  -1.96178 0.6766216 8068 -2.89937  0.0037
## frequency8000 30.51271 0.7951280 8068 38.37459  0.0000
## Correlation:
##           (Intr) fr2000 frq250 fr4000 frq500
## frequency2000 -0.173
## frequency250  -0.197  0.410
## frequency4000 -0.196  0.565  0.479
## frequency500  -0.174  0.362  0.561  0.414
## frequency8000 -0.201  0.454  0.540  0.612  0.436
##
## Standardized Within-Group Residuals:
##           Min           Q1           Med           Q3           Max
## -4.2543260 -0.5913403  0.0373855  0.6194437  3.9226279
##
## Number of Observations: 8347
## Number of Groups: 274
```

```
anova(random_intercept)
```

```
##           numDF denDF  F-value p-value
## (Intercept)     1  8068 783.1713 <.0001
## frequency       5  8068 538.4169 <.0001
```

now add Leeftijd as fixed effect; PTA ~ Domain + Leeftijd<sup>4</sup> (see. e.g. p.897)

```
timeRI <- update(random_intercept, .~. + Leeftijd)
summary(timeRI)
```

```
## Linear mixed-effects model fit by maximum likelihood
## Data: data_all_1
##           AIC           BIC       logLik
## 67842.65 67912.94 -33911.32
##
## Random effects:
## Formula: ~1 | pid
##           (Intercept) Residual
## StdDev:  0.1104064 24.88384
##
## Correlation Structure: AR(1)
## Formula: ~1 | pid
## Parameter estimate(s):
##           Phi
## 0.8322339
## Fixed effects: dB ~ frequency + Leeftijd
##           Value Std.Error   DF  t-value p-value
## (Intercept) -50.31584 1.6018876 8067 -31.41034  0.0000
## frequency2000  5.13859 0.5814116 8067  8.83812  0.0000
## frequency250  -1.30225 0.7394264 8067 -1.76116  0.0782
## frequency4000 20.24899 0.7377572 8067 27.44668  0.0000
## frequency500  -0.94485 0.5808559 8067 -1.62665  0.1038
```



```
## frequency8000 29.31740 0.8033935 8067 36.49196 0.0000
## Leeftijd      1.93967 0.0258142 8067 75.13958 0.0000
## Correlation:
##              (Intr) fr2000 frq250 fr4000 frq500 fr8000
## frequency2000 -0.196
## frequency250  -0.228 0.283
## frequency4000 -0.262 0.635 0.419
## frequency500  -0.176 0.195 0.631 0.284
## frequency8000 -0.304 0.464 0.551 0.713 0.369
## Leeftijd      -0.819 0.018 -0.023 0.032 -0.015 0.049
##
## Standardized Within-Group Residuals:
##           Min           Q1           Med           Q3           Max
## -3.07541243 -0.70824164 -0.07201688 0.58548467 5.01653320
##
## Number of Observations: 8347
## Number of Groups: 274
```

#### sessionInfo()

```
## R version 3.6.0 (2019-04-26)
## Platform: x86_64-apple-darwin15.6.0 (64-bit)
## Running under: macOS 10.15.4
##
## Matrix products: default
## BLAS: /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRblas.0.dylib
## LAPACK: /Library/Frameworks/R.framework/Versions/3.6/Resources/lib/libRlapack.dylib
##
## locale:
## [1] en_US.UTF-8/en_US.UTF-8/en_US.UTF-8/C/en_US.UTF-8/en_US.UTF-8
##
## attached base packages:
## [1] stats graphics grDevices utils datasets methods base
##
## other attached packages:
## [1] lattice_0.20-40 dplyr_0.8.4 tidyr_1.0.2 forcats_0.5.0
## [5] knitr_1.28 lme4_1.1-21 Matrix_1.2-18 nlme_3.1-145
## [9] readxl_1.3.1 sjPlot_2.8.2 drc_3.0-1 MASS_7.3-51.5
## [13] ggplot2_3.3.0
##
## loaded via a namespace (and not attached):
## [1] splines_3.6.0 carData_3.0-3 modelr_0.1.6 gtools_3.8.1
## [5] assertthat_0.2.1 highr_0.8 cellranger_1.1.0 yaml_2.2.1
## [9] bayestestR_0.5.2 pillar_1.4.3 backports_1.1.5 glue_1.4.0
## [13] digest_0.6.25 minqa_1.2.4 colorspace_1.4-1 sandwich_2.5-1
## [17] htmltools_0.4.0 pkgconfig_2.0.3 broom_0.5.5 haven_2.2.0
## [21] purrr_0.3.3 xtable_1.8-4 mvtnorm_1.1-0 scales_1.1.0
## [25] openxlsx_4.1.4 rio_0.5.16 emmeans_1.4.5 tibble_2.1.3
## [29] generics_0.0.2 farver_2.0.3 car_3.0-6 ellipsis_0.3.0
## [33] sjlabelled_1.1.3 TH.data_1.0-10 withr_2.1.2 cli_2.0.2
## [37] survival_3.1-8 magrittr_1.5 crayon_1.3.4 effectsize_0.2.0
## [41] estimability_1.3 evaluate_0.14 fansi_0.4.1 foreign_0.8-76
## [45] tools_3.6.0 data.table_1.12.8 hms_0.5.3 lifecycle_0.2.0
## [49] multcomp_1.4-12 stringr_1.4.0 munsell_0.5.0 plotrix_3.7-7
## [53] zip_2.0.4 ggeffects_0.14.1 compiler_3.6.0 rlang_0.4.5
```

|         |                  |                |                   |                  |
|---------|------------------|----------------|-------------------|------------------|
| ## [57] | grid_3.6.0       | nloptr_1.2.1   | parameters_0.5.0  | labeling_0.3     |
| ## [61] | rmarkdown_2.1    | boot_1.3-24    | gtable_0.3.0      | codetools_0.2-16 |
| ## [65] | abind_1.4-5      | sjstats_0.17.9 | curl_4.3          | sjmisc_2.8.3     |
| ## [69] | R6_2.4.1         | zoo_1.8-7      | performance_0.4.4 | utf8_1.1.4       |
| ## [73] | insight_0.8.1    | stringi_1.4.6  | Rcpp_1.0.4.6      | vctrs_0.2.4      |
| ## [77] | tidyselect_1.0.0 | xfun_0.12      |                   |                  |