



**Prolog Project: Sudoku Solver** 

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## 1. INTRODUCION

### 1.1. Scryer Prolog

To do this project I used Scryer Prolog that is an open source industrial strength production environment that is also a testbed for bleeding edge research in logic and constraint programming, which is itself written in a high-level language.

#### 1.2. What is a Sudoku

Sudoku is a puzzle game designed for a single player, much like a crossword puzzle. The puzzle itself is nothing more than a grid of little boxes called "cells". They are stacked nine high and nine wide, making 81 cells total. The puzzle comes with some of the cells (usually less than half of them) already filled in, like this:

		6		5	4	9		
1				6			4	2
7				8	9			
	7				5		8	1
	5		3	4		6		
4		2						
	3	4				1		
9			8				5	
			4			3		7

Sudoku cells has to be filled with numbers (1-2-3-4-5-6-7-8-9)

#### **1.3.** Rules

The rules of the game are simple: each of the nine blocks must contain all the numbers from 1 to 9 within its squares. Each number can only appear once in a row, column or box(the subsquares 3x3).

#### 2. SUDOKU SOLVER'S CODE

## 2.1. How to represent a generic sudoku puzzle

A generic sudoku puzzle may be represented like a list of rows (list of lists) as in the example below:

$$\begin{bmatrix} [X_{1}, X_{2}, X_{3}, X_{4}, X_{5}, X_{6}, X_{7}, X_{8}, X_{9}], \\ [X_{10}, X_{11}, X_{12}, X_{13}, X_{14}, X_{15}, X_{16}, X_{17}, X_{18}], \\ [X_{19}, X_{20}, X_{21}, X_{22}, X_{23}, X_{24}, X_{25}, X_{26}, X_{27}], \\ [X_{28}, X_{29}, X_{30}, X_{31}, X_{32}, X_{33}, X_{34}, X_{35}, X_{36}], \\ [X_{37}, X_{38}, X_{39}, X_{40}, X_{41}, X_{42}, X_{43}, X_{44}, X_{45}], \\ [X_{46}, X_{47}, X_{48}, X_{49}, X_{50}, X_{51}, X_{52}, X_{53}, X_{54}], \\ [X_{55}, X_{56}, X_{57}, X_{58}, X_{59}, X_{60}, X_{61}, X_{62}, X_{63}], \\ [X_{64}, X_{65}, X_{66}, X_{67}, X_{68}, X_{69}, X_{70}, X_{71}, X_{72}], \\ [X_{73}, X_{74}, X_{75}, X_{76}, X_{77}, X_{78}, X_{79}, X_{80}, X_{81}] \end{bmatrix}$$

#### 2.2. Sudoku's structure Code:

1 Rows is a list of 9 elements.

Maplist is a predicate using to compact the code.

Append is a predicate to concatenate all elements to the list VS (between 1 and 9).

- 2 I used the predicate <u>transpose</u> to do the same for the column
- To define the sub-squares, I named each of the rows and I considered three elements of the rows at the time

The first Block is the base case

The second one, if each list starts with 3 elements, so 1 of the sub-squares is complete and all the numbers are distinct.

#### 3. HOW TO SOLVE A SUDOKU PUZZLE

Normally to define a unique sudoku puzzle, I need at least 16 clues, as in the example:

But I can complete the sudoku without searching anything:

I can do that using the constraint propagation.

I use the predicates ins and all\_distinct:

```
-ins, states the domains of variables-all_distinct, describe a list of different integers
```

#### 3.1. Example constraint propagation:

## 3.2. Consistency Propagation

all\_distinct uses a powerful method from **graph theory** to prune the search space. Prolog automatically detects where will be the solution and also detects which of this sudoku's number will not be the solution, so prolog removes automatically that value from the domain of that cell. In this way prolog obtains the data consistency.

## 3.2.1. Graph theory

It is the study of graphs, which are mathematical structures used to model pairwise relations between objects.

I can divide each cell in 9 regions (Domain). the inconsistent value is indicated with a small dot.

1 2 3	123	123	4 5 6 4 5 6 4 5 6 4 5 6 4 5	23 123
4 5 6	456	456		56 456
7 8 9	789	789		89 789
1 2 3 4 5 6 7 8 9	$\begin{array}{c} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{array}$	1 2 3 4 5 6 7 8 9		23 123 56 456 89 789
123	123	1 2 3	1 2 3 1 2 3 1 2 3 1 2 3 1 2 3 1 2 4 5 6 4 5 6 4 5 6 4 5 6 4 5 6 4 5 6 7 8 9 7	23 123
456	456	4 5 6		56 456
789	789	7 8 9		89 789
123	123	123		23 123
456	456	456		56 456
789	789	789		89 789
1 2 3	123	1 2 3	1 2 3 1 2 3 1 2 3 1 2 3 1 2 3 1 4 5 6 4 5 6 4 5 6 4 5 6 4 5 6 4 5 6 7 8 9 7 8	23 123
4 5 6	456	4 5 6		56 456
7 8 9	789	7 8 9		89 789
1 2 3	123	123	1 2 3 1 2 3 1 2 3 1 2 3 1 2 3 1 4 5 6 4 5 6 4 5 6 4 5 6 4 5 6 4 5 6 7 8 9 7 8	23 123
4 5 6	456	456		56 456
7 8 9	789	789		89 789
1 2 3	123	1 2 3	1 2 3 1 2 3 1 2 3 1 2 3 1 2 3 1 4 5 6 4 5 6 4 5 6 4 5 6 4 5 6 4 5 6 7 8 9 7 8	23 123
4 5 6	456	4 5 6		56 456
7 8 9	789	7 8 9		89 789
1 2 3	123	1 2 3		23 123
4 5 6	456	4 5 6		56 456
7 8 9	789	7 8 9		89 789
1 2 3 4 5 6 7 8 9	$\begin{smallmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{smallmatrix}$	$\begin{array}{c} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{array}$	1 2 3 1 2 3 1 2 3 1 2 3 1 2 3 1 4 5 6 4 5 6 4 5 6 4 5 6 4 5 6 4 5 6 7 8 9 7 8 9 7 8 9 7 8 9 7 8	23 123 56 456 89 789

When I started the sudoku, this code rules out immediately all the integers signed by the dot.

Advantages about this technique:

1)I can start with all cells empty, initially each of the integers from 1 to 9 can be place in any cell.

2)you can complete the puzzle without having removed anything that you have already drawn

# 3.3. Example

I considered the past puzzle:

If you focus on the first sub-square you can see that the integer 4 misses only in 1 sub-cell, so 4 can be placed only here, when I complete 1 cell the prolog system, through the consistency

propagation, detects that

1	<b>:::</b>	4	•	•	<b>:</b> ∙.	: .	:	:
::	<b>::</b> :	2	7	4	∷.	:•	:	:
::	:::	::	5	:•	:•.	• • •	••	4
· ·	3	·:.	$\cdot$ :	• :		:	:	. :
7	5	·:·	٠.	··.	٠٠.	•••	•••	:
:::	:::	.::	. ::	٠:	9	6	:	٠:
:	4	••	:-	•	٠.	•	•	•
:		••		•		•		•
:	•••	••	•	•		•		•

If I do the same for each cell, I can obtain this result:

1	8	-	9	6	3	7 • •	2 .	. 5
5	6	2	7	4	. 8	• • 3	1	• • • •
• • 3	• • • 9	7	5	1	• 2 •	8 .	. 6	4
2 .	3	• • 9	• • 6	- 5	7 • •	1	4	. 8
7	5	. 6	1	. 8 .	4 • •	• 2 •	9	• • 3
4	1 • •		• 2 •	• • 3	9	6	• 5 •	7
9	4	1	• • 3	7	6	5	8	. 2
6	2 .	• • 3	• • • • • • • • • • • • • • • • • • •	• • • 9	5 .	4	7	1
8	7	. 5	4	• 2 •	1	9	3	• • 6

this concrete puzzle was solved by constraint propagation alone, I don't use the research, but in general research is needed to obtain concrete solutions.

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