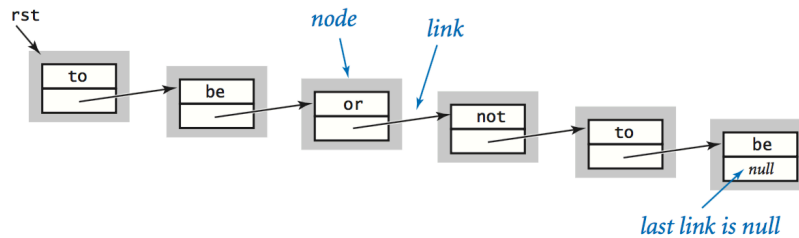


Generics. We have developed stack implementations that allows us to build a stack of one particular type, such as String. A specific mechanism in Java known as *generic types* enables us to build collections of objects of a type to be specified by client code.

- *Implementing a generic collection.* To implement a generic collection, we specify a *type parameter*, such as Item, in angle brackets and use that type parameter in our implementation instead of a specific type. For example, [Stack.java](#) is generic version of [LinkedStackOfStrings.java](#)
- *Using a generic collection.* To use a generic collection, the client must specify the *type argument* when the stack is created:



```
Stack<Integer> stack = new Stack<Integer>();
```

Autoboxing. We have designed our stacks to be *generic*, so that they objects of any type. The Java language features known as *autoboxing* and *unboxing* enable us to reuse *generic* code with primitive types as well. Java supplies built-in object types known as *wrapper types*, one for each of the primitive types: [Boolean](#), [Integer](#), [Double](#), [Character](#), and so forth. Java automatically converts between these reference types and the corresponding primitive types so that we can write code like the following:

```
Stack<Integer> stack = new Stack<Integer>();
stack.push(17);           // autoboxing   (int -> Integer)
int a = stack.pop();      // unboxing     (Integer -> int)
```

Iteration. Sometimes the client needs to access all of the items of a collection, one at a time, without deleting them. To maintain encapsulation, we do not want to reveal the internal representation of the queue (array or linked list) to the client. To accommodate this design pattern, Java provides the *foreach* statement. You should interpret the following for statement in the following code fragment as *for each string s in the collection, print s*.

```
Stack collection = new Stack();
...
for (String s : stack)
    StdOut.println(s);
```

Implementing a collection that supports iteration in this way requires implementing Java's [java.util.Iterator](#) and [java.util.Iterable](#) interfaces. See the textbook for details.

Stack and queue applications. Stacks and queues have numerous useful applications.

- *Arithmetic expression evaluation.* An important application of stacks is in *parsing*. For example, a compiler must parse arithmetic expressions written using *infix notation*. For example the following infix expression evaluates to 212.

```
( 2 + ( ( 3 + 4 ) * ( 5 * 6 ) ) )
```

[Evaluate.java](#) evaluates a fully parenthesized arithmetic expression.

- *Function-call abstraction.* Most programs use stacks implicitly because they support a natural way to implement function calls, as follows: at any point during the execution of a function, define its *state* to be the values of all of its variables *and* a pointer to the next instruction to be executed. The natural way to implement the function-call abstraction is to use a stack. To call a function, push the state on a stack. To return from a function call, pop the state from the stack to restore all variables to their values before the function call and resume execution at the next instruction to be executed.
- *M/M/1 queue.* One of the most important queueing models is known as an *M/M/1* queue, which has been shown to accurately model many real-world situations. It is characterized by three properties:
 - There is one server—a FIFO queue.
 - Interarrival times to the queue obey an exponential distribution with rate λ per minute.
 - Service times from a nonempty queue obey an exponential distribution with rate μ per minute.

[MM1Queue.java](#) simulates an *M/M/1* queue and plots a histogram of waiting times to standard drawing.

- *Load balancing.* [LoadBalance.java](#) simulate the process of assigning n items to a set of m servers. For each item, it chooses a sample of s servers and assigns the item to the server that has the fewest current items.

Exercises

1. Add a method `isFull()` to [ArrayStackOfStrings.java](#).
2. Write a filter [Reverse.java](#) that reads strings one at a time from standard input and prints them to standard output in reverse order.
3. Write a stack client [Parentheses.java](#) that reads a string of parentheses, square brackets, and curly braces from standard input and uses a stack to determine whether they are properly balanced. For example, your program should print true for `[]{}{[]()>()}` and false for `[]()`.
4. What does the following code fragment print when `n` is 50? Give a high-level description of what the code fragment does when presented with a positive integer `n`.

```
Stack stack = new Stack();
while (n > 0) {
    stack.push(n % 2);
    n /= 2;
}
while (!stack.isEmpty())
    StdOut.print(stack.pop());
StdOut.println();
```

Solution: prints the binary representation of `n` (110010 when `n` is 50).

5. What does the following code fragment do to the queue `queue`?

```
Stack stack = new Stack();
while (!queue.isEmpty())
    stack.push(queue.dequeue());
while (!stack.isEmpty())
    queue.enqueue(stack.pop());
```

Solution: reverses the order of the strings in the queue.

6. Add a method `peek()` to [Stack.java](#) that returns the most recently inserted element on the stack (without removing it).
7. Add a method `size()` to both [Queue.java](#) and [Stack.java](#) that returns the number of items in the collection.
8. Write a filter [InfixToPostfix.java](#) that converts an arithmetic expression from infix to postfix.
9. Write a program [EvaluatePostfix.java](#) that takes a postfix expression from standard input, evaluates it, and prints the value. (Piping the output of your program from the previous exercise to this program gives equivalent behavior to [Evaluate.java](#).)
10. Develop a data type [ResizingArrayQueueOfStrings.java](#) that implements a queue with a fixed-length array in such a way that all operations take constant time.
11. Modify [MM1Queue.java](#) to make a program [MD1Queue.java](#) that simulates a queue for which the service times are fixed (deterministic) at rate μ . Verify Little's law for this model.
12. Develop a class [StackOfInts.java](#) that uses a linked-list representation (but no generics) to implement a stack of integers. Write a client that compares the performance of your implementation with `Stack<Integer>` to determine the performance penalty from autoboxing and unboxing on your system.

Linked-List Exercises

23. Suppose *x* is a linked-list node. What is the effect of the following code fragment?

```
x.next = x.next.next;
```

Solution: Deletes from the list the node immediately following *x*.

24. Write a method `delete()` that takes the first node in a linked list and an `int` argument *k* and deletes the *k*th node in the linked list, if it exists.

Solution:

```
// we assume that first is a reference to the first Node in the list
public void delete(int k) {
    if (k <= 0) throw new RuntimeException("Invalid value of k");

    // degenerate case - empty linked list
    if (first == null) return;

    // special case - removing the first node
    if (k == 1) {
        first = first.next;
        return;
    }

    // general case, make temp point to the (k-1)st node
    Node temp = first;
    for (int i = 2; i < k; i++) {
        temp = temp.next;
        if (temp == null) return; // list has < k nodes
    }

    if (temp.next == null) return; // list has < k nodes

    // change temp.next to skip kth node
    temp.next = temp.next.next;
}
```

25. Suppose that *x* is a linked-list node. What is the effect of the following code fragment?

```
t.next = x.next;
x.next = t;
```

Solution: Inserts node *t* immediately after node *x*.

26. Why does the following code fragment not have the same effect as in the previous question?

```
x.next = t;
t.next = x.next;
```

Solution: When it comes time to update *t.next*, *x.next* is no longer the original node following *x*, but is instead *t* itself!

Creative Exercises

1. **Josephus problem.** In the Josephus problem from antiquity, n people are in dire straits and agree to the following strategy to reduce the population. They arrange themselves in a circle (at positions numbered from 0 to $n-1$) and proceed around the circle, eliminating every m th person until only one person is left. Legend has it that Josephus figured out where to sit to avoid being eliminated. Write a Queue client [Josephus.java](#) that takes two integer command-line arguments m and n and prints the order in which people are eliminated (and thus would show Josephus where to sit in the circle).
2. **Topological sort.** You have to sequence the order of n jobs that are numbered 0 to $n-1$ on a server. Some of the jobs must complete before others can begin. Write a program [Topological-Sorter.java](#) that takes a command-line argument n and a sequence on standard input of ordered pairs of jobs (i, j) , and then prints a sequence of integers such that for each pair (i, j) in the input, job i appears before job j . First, from the input, build, for each job (1) a queue of jobs that must follow it and (2) its *indegree* (the number of jobs that must come before it). Then, build a queue of all nodes whose indegree is 0 and repeatedly delete any job with a 0 indegree, maintaining all the data. This process has many applications. For example, you can use it to model course prerequisites for your major so that you can find a sequence of courses to take so that you can graduate.
3. **Copy constructor for a stack.** Create a new constructor for the linked-list implementation of Stack.java so that `Stack<String> t = new Stack<String>(s)` makes t reference a new and independent copy of the stack s . You should be able to push and pop from either s or t without influencing the other. *Recursive solution:* create a copy constructor for a Node and use this to create the new stack.

```
public Node(Node x) {
    item = x.item;
    if (x.next != null)
        next = new Node(x.next);
}
```

```
public Stack(Stack s) {
    first = new Node(s.first);
```

Non-recursive solution (untested):

```
public Node(Node x, Node next) {
    this.x = x;
    this.next = next;
}

public Stack(Stack s) {
    if (s.first != null) {
        first = new Node(s.first.value, s.first.next) {
            for (Node x = first; x.next != null; x = x.next)
                x.next = new Node(x.next.value, x.next.next);
        }
    }
}
```

4. **Quote.** Develop a data type [Quote.java](#) that implements the following API:

```
public class Quote
```

<code>Quote()</code>	<i>create an empty quote</i>
<code>void add(String word)</code>	<i>append word to the end of the quote</i>
<code>void add(int i, String word)</code>	<i>insert word to be at index i</i>
<code>String get(int i)</code>	<i>word at index i</i>
<code>int count()</code>	<i>number of words in the quote</i>
<code>String toString()</code>	<i>the words in the quote</i>

To do so, define a nested class `Card` that holds one word of the quotation and a link to the next word in the quotation:

```
private class Card {
    private String word;
    private Card next;

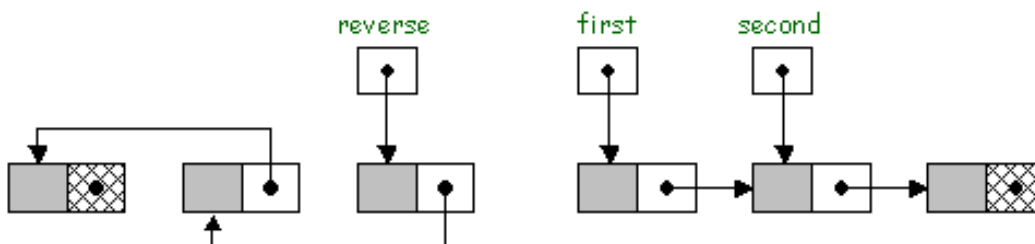
    public Card(String word) {
        this.word = word;
        this.next = null;
    }
}
```

5. **Circular quote.** Repeated the previous exercise, but use a *circular linked list*. In a circular linked list, each node points to its successor, and the last node in the list points to the first node (instead of null, as in a standard null-terminated linked list).

Solution: [CircularQuote.java](#)

6. **Reverse a linked list (iteratively).** Write a nonrecursive function that takes the first Node in a linked list as an argument, and reverses the list, returning the first Node in the result.

Solution: To accomplish this, we maintain references to three consecutive nodes in the linked list, `reverse`, `first`, and `second`. At each iteration we extract the node `first` from the original linked list and insert it at the beginning of the reversed list. We maintain the invariant that `first` is the first node of what's left of the original list, `second` is the second node of what's left of the original list, and `reverse` is the first node of the resulting reversed list.



```
public static Node reverse(Node list) {
    if (first == null || first.next == null) return first;
    Node first    = list;
    Node reverse = null;
```

```

        while (first != null) {
            Node second = first.next;
            first.next = reverse;
            reverse = first;
            first = second;
        }
        return reverse;
    }
}

```

- 7. Reverse a linked list (recursively).** Write a recursive function that takes the first Node in a linked list as an argument and reverses the list, returning the first Node in the result.

Solution: Assuming the linked list has n elements, we recursively reverse the last $n-1$ elements, then append the first element to the end.

```

public Node reverse(Node first) {
    if (first == null || first.next == null) return first;
    Node second = first.next;
    Node rest = reverse(second);
    second.next = first;
    first.next = null;
    return rest;
}

```

- 8. Listing files.** A folder is a list of files and folders. Write a program [Directory.java](#) that takes the name of a folder as a command line argument and prints all of the files contained in that folder, with the contents of each folder recursively listed (indented) under that folder's name.

Web Exercises

1. Write a recursive function that takes as input a queue, and rearranges it so that it is in reverse order. Hint: dequeue() the first element, recursively reverse the queue, and then enqueue the first element.
2. Add a method `Item[] multiPop(int k)` to `Stack` that pops `k` elements from the stack and returns them as an array of objects.
3. Add a method `Item[] toArray()` to `Queue` that returns all `N` elements on the queue as an array of length `N`.
4. What does the following code fragment do?

```
IntQueue q = new IntQueue();
q.enqueue(0);
q.enqueue(1);
for (int i = 0; i < 10; i++) {
    int a = q.dequeue();
    int b = q.dequeue();
    q.enqueue(b);
    q.enqueue(a + b);
    System.out.println(a);
}
```

Fibonacci

5. What data type would you choose to implement an "Undo" feature in a word processor?
6. Suppose you have a single array of size `N` and want to implement two stacks so that you won't get overflow until the total number of elements on both stacks is `N+1`. How would you proceed?
7. Suppose that you implemented `push` in the linked list implementation of `StackList` with the following code. What is the mistake?

```
public void push(Object value) {
    Node second = first;
    Node first = new Node();
    first.value = value;
    first.next = second;
}
```

Solution: By redeclaring `first`, you are creating a new local variable named `first`, which is different from the instance variable named `first`.

8. **Stack with one queue.** Show how to implement a stack using one queue. *Hint:* to delete an item, get all of the elements on the queue one at a time, and put them at the end, except for the last one which you should delete and return.
9. **Listing files with a stack.** Write a program that takes the name of a directory as a command line argument, and prints out all of the files contained in this directory and any subdirectories. Also prints out the file size (in bytes) of each file. Use a stack instead of a queue. Repeat using recursion and name your program `DirectoryR.java`. Modify `DirectoryR.java` so that it prints out each subdirectory and its total size. The size of a directory is equal to the sum of all of the files it contains or that its subdirectories contain.

- 10. Stack + max.** Create a data structure that efficiently supports the stack operations (pop and push) and also return the maximum element. Assume the elements are integers or reals so that you can compare them. *Hint:* use two stacks, one to store all of the elements and a second stack to store the maximums.
- 11. Tag systems.** Write a program that reads in a binary string from the command line and applies the following (00, 1101) tag-system: if the first bit is 0, delete the first three bits and append 00; if the first bit is 1, delete the first three bits and append 1101. Repeat as long as the string has at least 3 bits. Try to determine whether the following inputs will halt or go into an infinite loop: 10010, 100100100100100100. Use a queue.
- 12. Set of integers.** Create a data type that represents a set of integers (no duplicates) between 0 and $n-1$. Support `add(i)`, `exists(i)`, `remove(i)`, `size()`, `intersect`, `difference`, `symmetricDifference`, `union`, `isSubset`, `isSuperSet`, and `isDisjointFrom`.
- 13. Indexing a book.** Write a program that reads in a text file from standard input and compiles an alphabetical index of which words appear on which lines, as in the following input. Ignore case and punctuation. Similar to `FrequencyCount`, but for each word maintain a list of location on which it appears.
- 14. Copy constructor for a resizing array implementation of a stack.** Add a copy constructor to [ArrayStackOfStrings.java](#)
- 15. Reorder linked list.** Given a singly linked list $x_1 \rightarrow x_2 \rightarrow \dots \rightarrow x_{2n}$ containing $2n$ nodes, rearrange the nodes to be $x_1 \rightarrow x_{2n} \rightarrow x_2 \rightarrow x_{2n-1} \rightarrow x_3 \rightarrow \dots$. *Hint:* break the linked list in half; reverse the order of the nodes in the second linked list; merge the two lists together.

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